



Exploring SMEFT operators through single top-quark production associated with the Higgs boson at the LHC

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Introduction

- The **SM has been successful**, compatible with all experimental measurements, and no evidence of light states are present till now
- This indicates **BSM physics** may reside at somewhat higher scale
- This motivates to interpret deviations from the dim=4 SM Lagrangian predictions in terms of an EFT:

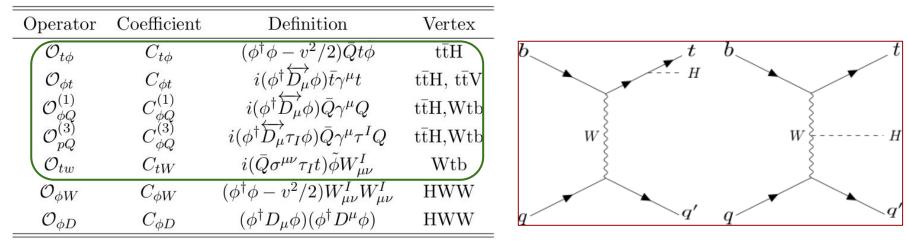
$$\mathcal{L}_{SMEFT} = \mathcal{L}_{SM} + rac{1}{\Lambda^2}\sum_{i=1}^{N_{d6}}C_i^{(6)}\mathcal{O}_i^{(6)}$$

- There can be **59 independent set of operators** in dim=6 EFT expansion
- In this work, we focus on operators related to the tHq process and mainly affecting top-quark interactions which can be a sensitive probe for new physics having close relation to EWSB

• **<u>Symmetry assumption</u>**, to focus on top quark related operators

 $U(3)_l imes U(3)_e imes U(2)_Q imes U(2)_u imes U(3)_d\equiv U(2)^2 imes U(3)^3$

<u>Relevant operators (Warsaw basis)</u>

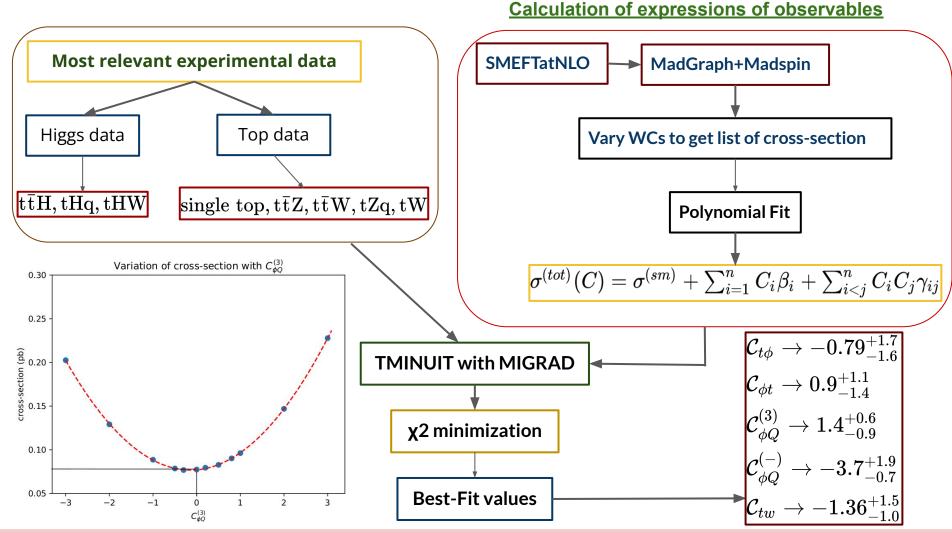


- The operators affecting HWW vertex are found not to be much sensitive and are constrained mainly by EW precision data
- 5 operators are relevant

$$\mathcal{O}_{t\phi}, \mathcal{O}_{\phi t}, \mathcal{O}_{pQ}^{(3)}, \mathcal{O}_{tw}, \mathcal{O}_{\phi Q}^{(-)} \equiv \mathcal{O}_{\phi Q}^{(1)} - \mathcal{O}_{\phi Q}^{(3)}$$

Constraints on Wilson Coefficients

- There exists constraints from global fits of operators (JHEP 04 (2021) 279, JHEP 11 (2021) 089)
- Some recent measurements sensitive to the chosen operators are not included
- We try to find a complementary approach of constraining with a subset of data which are most relevant and recent



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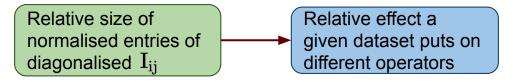
- Fits are carried out for both linear and quadratic order in WCs
- Both for individual operator at a time or combined fit of all operators
- Quadratic fits was seen to put much stronger constraints

Information Matrix (I_{ij}) (Phys.Rev.D 95)

(Phys.Rev.D 95 (2017) 7, 073002)

$$I_{ij} = E\left[\sum_{m=1}^{N_{exp}} \frac{1}{\delta_{exp,m}^2} \left(\gamma_{m,ij} \left(\sigma_m^{(sm)} - \sigma_m^{(exp)}\right) + \left(\beta_{m,i}^{(eft)} + \sum_{l=1}^{N_{wc}} C_l \gamma_{m,il}^{(eft)}\right) \left(\beta_{m,j}^{(eft)} + \sum_{l'=1}^{N_{wc}} C_{l'} \gamma_{m,il'}^{(eft)}\right)\right)\right]$$

 Provides a quantitative measurement of the information about the parameters that one can derive from a set of observations



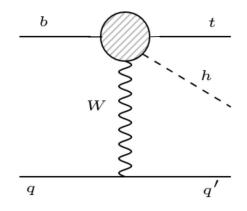
Diagonal entries for each dataset Normalized to 100

	$C_{pQ}^{(3)}$	$C_{pQ}^{(-)}$	$C_{\phi t}$	$C_{t\phi}$	C_{tw}
tH	15.7	15.6	16.4	33.4	18.5
$\mathrm{tt}\mathrm{H}$	2.4	0.4	3.7	92.1	1.2
${ m tj}$	79.6	0.4	0.4	0.8	18.4
ttV	2.3	55.3	41.6	0.6	0.4
tZ	50.1	37.2	0.2	0.003	12.4
tW	64.0	0.7	0.1	0.002	35.1

Implications at the LHC

What effects can we see in the distributions at the LHC?

- → Unlike other processes like ttH, ggH etc., tHq poses the
 bw→ tH scattering sub amplitude (JHEP 10 (2019) 004)
- → This results in an **energy growth** for specific operators
- → We use H→bb decay mode
- → We consider both leptonic and hadronic decay mode of Top-quark

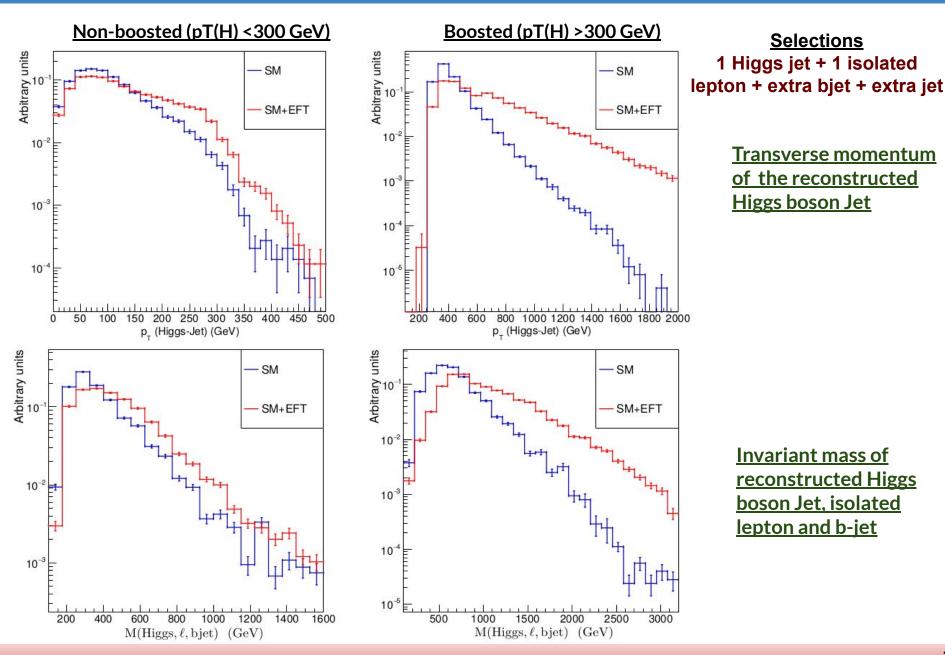


Simulation



Event selection

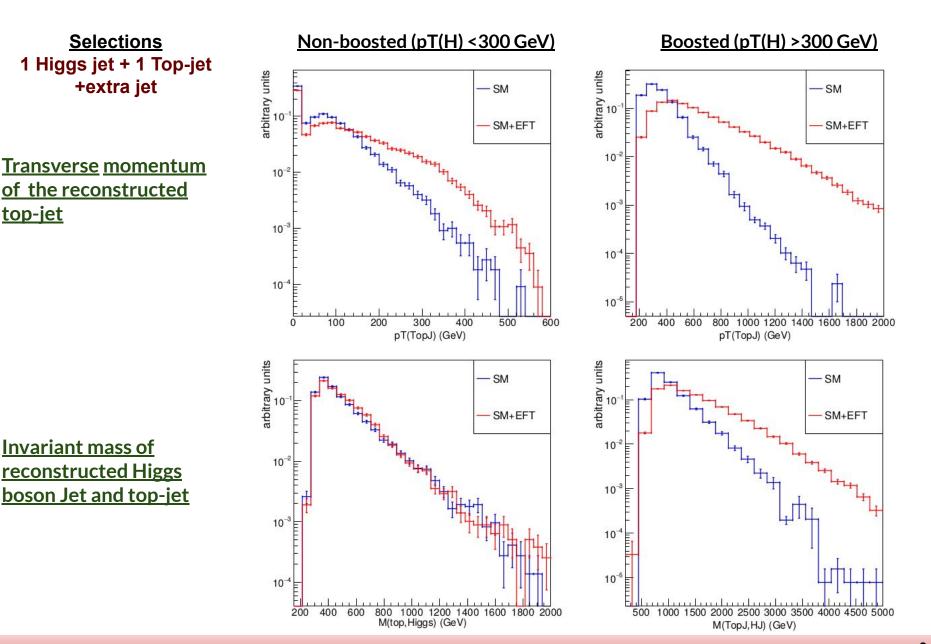
- → One reconstructed Higgs Jet
 - For boosted region, tagging **CA8 fat-jets with two b-like subjects** and **[100,150]** mass window
 - For non-boosted region, using **combination of AK4 b-jets**
- → One isolated lepton (for leptonic final state)
- → One reconstructed Top Jet (for hadronic final state)
 - Using HEPTopTagger, in boosted region
- → At least one extra AK4 jet with pT>30 GeV



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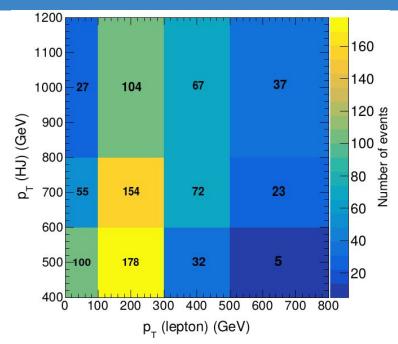
Distributions at reconstructed level (Hadronic final state)



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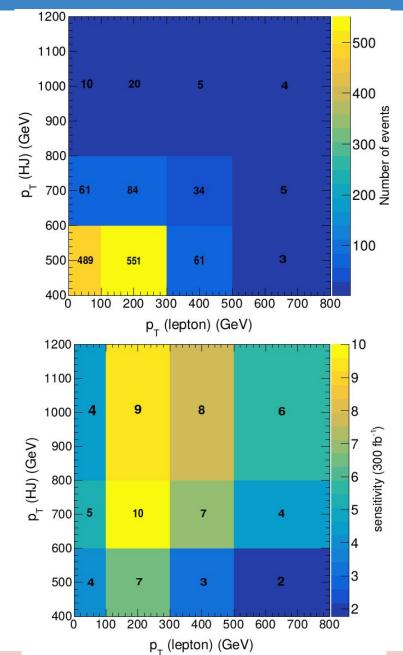
Estimation of backgrounds (Leptonic final state)



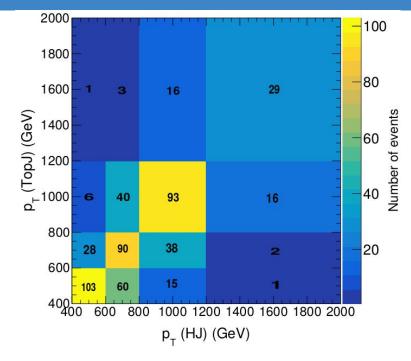
 We have considered the following backgrounds:

 ${
m tar t},~{
m tar t}{
m H},~{
m tar t}{
m Z},~{
m tar t}{
m bar b},~{
m tar t}{
m W},{
m WH}$

- ✤ Following selections were imposed $1 \text{ HJ} + 1 \text{ lepton} + \ge b \text{jet} + \ge 1 \text{ Other jets}$
- Significant excess of events can be observed at 300 fb⁻¹ luminosity



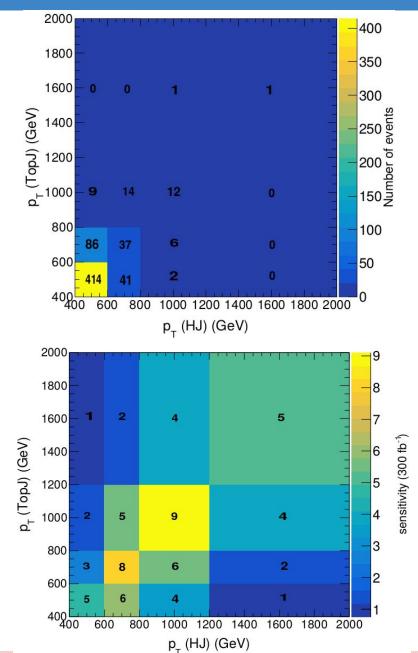
Estimation of backgrounds (Hadronic final state)



 We have considered the following backgrounds:

 ${
m tar{t}H,tar{t},tar{t}bar{b},tar{t}Z,tar{t}W}$

- Following selections were imposed $1 \text{ HJ} + 1 \text{ Top} - \text{J} + \ge 1 \text{ Other jets}$
- Significant excess of events can be observed at 300 fb⁻¹ luminosity



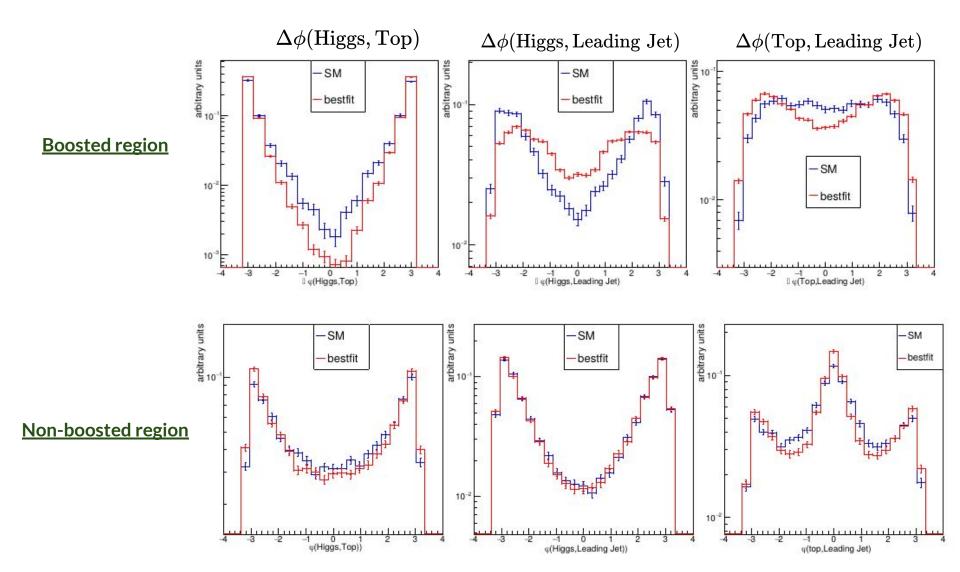


- Top quark interactions have important footprints of EWSB
- Within SMEFT framework, these interaction can be probed through tHq process
- Using various relevant and recent measurements, the set of operators are constrained
- The implications at the collider are studied using the best-fit values
- Distinguishable deviations from SM can be visible
- A signal background simulation shows promising signal significance in pT-binned analysis 300 fb⁻¹

Back Up



Angular distributions (hadronic final state)



	Process	observable	$\mathcal{L} (\mathrm{fb}^{-1})$	Value	Ref.
ATLAS	$t\bar{t}H,H\rightarrow b\bar{b}$	μ	79.8	$0.79\substack{+0.61\\-0.60}$	Phys. Lett. B 784 (2018) 173
	$t\bar{t}H,H\to ZZ(4\ell)$	μ	79.8	< 1.77 at $68\%~{\rm CL}$	Phys. Lett. B 784 (2018) 173
	$t\bar{t}H,H\rightarrow Multilepton$	μ	79.8	$1.56\substack{+0.42\\-0.40}$	Phys. Lett. B 784 (2018) 173
CMS	$t\bar{t}H,H\rightarrow b\bar{b}$	μ	35.9	$0.72_{-0.45}^{+0.45}$	JHEP 03 (2019) 026
	$t\bar{t}H,H\to ZZ(4\ell)$	μ	137	$0.16\substack{+0.98\\-0.16}$	Eur. Phys. J. C 81 (2021) 488
	$\rm t\bar{t}H, \rm H \rightarrow Multilepton$	μ	35.9	$1.23\substack{+0.45\\-0.43}$	JHEP 08 (2018) 066
	tHq + thW, combined	σ	35.9	$0.9~{ m pb}$	Phys. Rev. D 99, 092005 (2019)

- Dedicated ttH, tHq measurements are not generally used in previous fits
- Important for operators related to top-Higgs coupling

Singletop measurements used in fit

8					
51	Process	observable	$\mathcal{L} ~(\mathrm{fb}^{-1})$	Value	-
	tj (t-channel)	tj (t-channel) $\sigma_{tot}(t)$		$130{\pm}19~{\rm pb}$	Phys. Lett. B 800 (2019)
tj (t-channel)		$\sigma_{ m tot}({ m ar t})$	35.9	$77{\pm}12$ pb	135042
\mathbf{CMS}	tj (t-channel)	$(1/\sigma)d\sigma/d y^{t+\bar{t}} $	2.3	$0.64 \pm 0.14(\text{bin 1})$	CMS-PAS-TOP-1
				$0.55 \pm 0.12 ({ m bin}\ 2)$	6-004
				$0.50 \pm 0.12 (bin 3)$	
				0.18 ± 0.08 (bin 4)	
		$(1/\sigma)d\sigma/d y^t $	35.9	$0.58 \pm 0.15 (bin 5)$	Eur. Phys. J. C
				0.53 ± 0.08 (bin 6)	80 (2020) 370
				$0.5\pm0.09(\mathrm{bin}~7)$	
				$0.47 \pm 0.09 ({ m bin}\ 8)$	
9				$0.26 \pm 0.02 (bin 9)$	_
ATLAS	tj (t-channel)	$\sigma_{ m tot}(t)$	3.2	$156{\pm}28 \text{ pb}$	JHEP 04 (2017) 086
	tj (t-channel)	$\sigma_{ m tot}({ m ar t})$	3.2	$91{\pm}19~{\rm pb}$	_

ttV measurements used in fit

-	Process	observable	\mathcal{L} (fb ⁻¹)	Value	
	$t\bar{t}Z$	$\sigma_{\rm tot}$	36.1	0.95±0.13 pb Phys. R	ev. D 99,
ATLAS	${ m t\bar{t}W} { m t\bar{t}Z}$	$\sigma_{ m tot} \ (1/\sigma) d\sigma/dp_T^Z$	$36.1 \\ 139$	$0.87 \pm 0.19 \text{ pb}$ 072009 $0.0018 \pm 0.0013 (\text{bin 1})$ Eur.	(2019) Phys. J. C 81
		(1/0)40/497	100	$0.0010 \pm 0.0010(0001)$	1) 737
				$0.0053 \pm 0.002(\text{bin } 3)$	
				$0.0057 \pm 0.0015(\text{bin } 4)$	
				$0.0022 \pm 0.00085(\text{bin } 5)$	
				0.0006 ± 0.0004 (bin 6)	
				$0.0006 \pm 0.00025(\text{bin 7}))$	
\mathbf{CMS}	$t\bar{t}Z$	$\sigma_{ m tot}$	35.9	$0.99{\pm}0.14~{ m pb}$ jher o	8 (2018) 011
	$t\bar{t}W$	$\sigma_{ m tot}$	35.9	$0.77{\pm}0.17~\mathrm{pb}$ JHEP 0	8 (2018) 011
	$t\bar{t}Z$	$\sigma_{ m tot}$	77.5	$0.95{\pm}0.08~{ m pb}$ jher o	3 (2020) 056
	$t\bar{t}Z$	$(1/\sigma)d\sigma/dp_T^Z$	77.5	$0.004 \pm 0.001 ({ m bin}\ 1)$ JHEP (03 (2020) 056
				$0.005 \pm 0.0009(\text{bin } 2)$	
				$0.0022 \pm 0.0005(\text{bin } 3)$	
				$0.0003 \pm 0.0001(\text{bin } 4)$	

	Process	observable	\mathcal{L} (fb ⁻¹)	Value	
	$tZq(l^+, 2\ell)$	$\sigma_{ m tot}$	138	$62.2^{+7.4}_{-6.8}$ fb	JHEP 02 (2022) 107
CMS	$tZq(l^-,2\ell)$	$\sigma_{ m tot}$	138	$26.1^{+5.6}_{-5.4}$ fb	JHEP 02 (2022) 107
	tW	$\sigma_{ m tot}$	36	$89{\pm}13~{ m pb}$	JHEP 11 (2021) 111
	tW	$\sigma_{ m tot}$	35.9	$63{\pm}7~{ m pb}$	JHEP 10 (2018) 117
	tZ	$1/\sigma d\sigma/dp_T^Z$	138	$0.1\pm0.035({ m bin}$)	1) JHEP 02 (2022) 107
				$0.1\pm0.03({\rm bin}~2$)
				$0.035\pm0.015(\mathrm{bin}$	3)
				$0.01\pm0.0075(\mathrm{bin}$	4)
ATLAS	tZ	$\sigma_{ m tot}$	139	$97{\pm}15~{\rm pb}$	JHEP 07 (2020) 124
	tW	$\sigma_{ m tot}$	3.2	94^{+30}_{-24} pb	JHEP 01 (2018) 63

Fisher Information Matrix

$$\begin{split} I_{ij}(\vec{C}) = -E\left[\frac{\partial^2 f(X|\vec{C})}{\partial c_i \partial c_j}\right] & \longrightarrow f(X|\vec{C}) \text{ is the distribution of the experimental} \\ & \text{measurements X given the true values of WCs C} \end{split}$$

→ The smallest achievable uncertainty can be obtained by the Cramer-Rao bound

$$\mathrm{C_{ij}} \geq \mathrm{I_{ij}^{-1}}$$

→ Considering $f(X|\vec{C})$ a Gaussian distribution, the FIM can be expressed as.

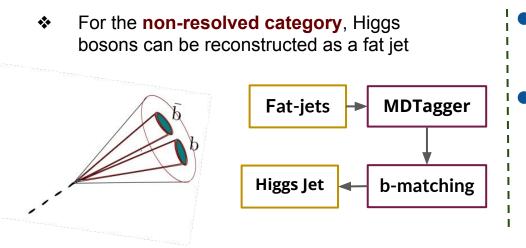
$$\begin{split} I_{ij} &= E \left[\sum_{m=1}^{N_{exp}} \frac{1}{\delta_{exp,m}^2} \left(\gamma_{m,ij} \left(\sigma_m^{(sm)} - \sigma_m^{(exp)} \right) + \left(\beta_{m,i}^{(eff)} + \sum_{l=1}^{N_{wc}} C_l \gamma_{m,il}^{(eff)} \right) \left(\beta_{m,j}^{(eff)} + \sum_{l'=1}^{N_{wc}} C_{l'} \gamma_{m,il'}^{(eff)} \right) \right) \right] \\ \vec{C} &= \begin{bmatrix} C_{\phi Q}^{(3)} \\ C_{\phi Q} \\ C_{f \psi} \end{bmatrix} \qquad \begin{bmatrix} 212.4 & -1.9 & -1.8 & 1.0 & 55.5 \\ -1.9 & 0.02 & -1.5 & -1.6 & -0.9 \\ -1.8 & -1.5 & -0.03 & 1.1 & -0.8 \\ -1.0 & -1.6 & 1.1 & 0.12 & -0.8 \\ 55.5 & -0.9 & -0.8 & -0.8 & -40.1 \end{bmatrix} \qquad \begin{bmatrix} 223.5 \\ -1.1 \\ -1.2 \\ 2.3 \\ -51.5 \end{bmatrix} \qquad \underbrace{\text{Example:}}_{single-top \ data} \\ \text{Eigen-values} \end{split}$$

→ Single-top data mostly affects $C_{\phi Q}^{(3)}$ and C_{tW}

Fat jet reconstruction

- Used Fastjet3.3.4 and Delphes e-flow objects
- CA algorithm, R=0.8
- pT (jet) > 300 GeV, |η| <4.0

Higgs jet reconstruction



In **resolved category**, pair of b-jets giving invariant mass closest to 125 GeV are identified

Ordinary jet reconstruction

pT (jet) > 30 GeV, |n| <4.0

Anti-KT algorithm, R=0.4

If **100 GeV < m(bb) <150 GeV**, assign the resultant 4-momentum to Higgs-Jet

- **For b-matching.** sub-jets are matched with b-quarks of the event
 - **Used** ΔR <0.3, |η|<2.5
 - Also cross-checked the procedure by confirming presence of b-hadrons inside the tagged b-jets

JHEP 10 (2010) 085

X ³		φ^6 and $\varphi^4 D^2$		$\psi^2 arphi^3$	
Q_G	$f^{ABC}G^{A\nu}_{\mu}G^{B\rho}_{\nu}G^{C\mu}_{\rho}$	Q_{arphi}	$(arphi^\dagger arphi)^3$	Qeq	$(arphi^{\dagger}arphi)(ar{l}_{p}e_{r}arphi)$
$Q_{\widetilde{G}}$	$f^{ABC} \widetilde{G}^{A\nu}_{\mu} G^{B\rho}_{\nu} G^{C\mu}_{\rho}$	$Q_{\varphi \Box}$	$(\varphi^{\dagger}\varphi)\Box(\varphi^{\dagger}\varphi)$	$Q_{u\varphi}$	$(arphi^{\dagger}arphi)(ar{q}_{p}u_{r}\widetilde{arphi})$
Q_W	$\varepsilon^{IJK}W^{I\nu}_{\mu}W^{J\rho}_{\nu}W^{K\mu}_{\rho}$	$Q_{\varphi D}$	$\left(arphi^{\dagger} D^{\mu} arphi ight)^{\star} \left(arphi^{\dagger} D_{\mu} arphi ight)$	$Q_{d\varphi}$	$(arphi^\dagger arphi) (ar q_p d_r arphi)$
$Q_{\widetilde{W}}$	$\varepsilon^{IJK}\widetilde{W}^{I\nu}_{\mu}W^{J\rho}_{\nu}W^{K\mu}_{\rho}$				
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^{\dagger}\varphiG^{A}_{\mu u}G^{A\mu u}$	Q_{eW}	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W^I_{\mu\nu}$	$Q^{(1)}_{arphi l}$	$(\varphi^{\dagger}i\overleftrightarrow{D}_{\mu}\varphi)(\bar{l}_{p}\gamma^{\mu}l_{r})$
$Q_{arphi \widetilde{G}}$	$arphi^\dagger arphi \widetilde{G}^A_{\mu u} G^{A\mu u}$	Q_{eB}	$(\bar{l}_p \sigma^{\mu u} e_r) \varphi B_{\mu u}$	$Q^{(3)}_{arphi l}$	$(\varphi^{\dagger}i\overleftrightarrow{D}^{I}_{\mu}\varphi)(\overline{l}_{p}\tau^{I}\gamma^{\mu}l_{r})$
$Q_{\varphi W}$	$\varphi^{\dagger}\varphi W^{I}_{\mu u}W^{I\mu u}$	Q_{uG}	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \widetilde{\varphi} G^A_{\mu\nu}$	$Q_{arphi e}$	$(\varphi^{\dagger}i\overleftrightarrow{D}_{\mu}\varphi)(\bar{e}_{p}\gamma^{\mu}e_{r})$
$Q_{arphi \widetilde{W}}$	$arphi^{\dagger}arphi \widetilde{W}^{I}_{\mu u}W^{I\mu u}$	Q_{uW}	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \widetilde{\varphi} W^I_{\mu\nu}$	$Q^{(1)}_{arphi q}$	$(\varphi^{\dagger}i\overleftrightarrow{D}_{\mu}\varphi)(\bar{q}_{p}\gamma^{\mu}q_{r})$
$Q_{\varphi B}$	$arphi^\dagger arphi B_{\mu u} B^{\mu u}$	Q_{uB}	$(\bar{q}_p \sigma^{\mu u} u_r) \widetilde{\varphi} B_{\mu u}$	$Q^{(3)}_{arphi q}$	$(\varphi^{\dagger}i\overleftrightarrow{D}^{I}_{\mu}\varphi)(\overline{q}_{p}\tau^{I}\gamma^{\mu}q_{r})$
$Q_{arphi \widetilde{B}}$	$arphi^\dagger arphi \widetilde{B}_{\mu u} B^{\mu u}$	Q_{dG}	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G^A_{\mu\nu}$	$Q_{\varphi u}$	$(\varphi^{\dagger}i\overleftrightarrow{D}_{\mu}\varphi)(\bar{u}_{p}\gamma^{\mu}u_{r})$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W^I_{\mu u} B^{\mu u}$	Q_{dW}	$(\bar{q}_p \sigma^{\mu u} d_r) \tau^I \varphi W^I_{\mu u}$	$Q_{arphi d}$	$(\varphi^{\dagger}i\overleftrightarrow{D}_{\mu}\varphi)(\bar{d}_{p}\gamma^{\mu}d_{r})$
$Q_{\varphi \widetilde{W}B}$	$arphi^\dagger au^I arphi \widetilde{W}^I_{\mu u} B^{\mu u}$	Q_{dB}	$(\bar{q}_p \sigma^{\mu u} d_r) \varphi B_{\mu u}$	$Q_{arphi u d}$	$i(\widetilde{\varphi}^{\dagger}D_{\mu}\varphi)(\bar{u}_{p}\gamma^{\mu}d_{r})$

Warsaw Basis - II

JHEP 10 (2010)	085
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	$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$			
Q_{ll}	$(ar{l}_p \gamma_\mu l_r) (ar{l}_s \gamma^\mu l_t)$	Q_{ee}	$(ar{e}_p \gamma_\mu e_r) (ar{e}_s \gamma^\mu e_t)$	Q_{le}	$(ar{l}_p \gamma_\mu l_r) (ar{e}_s \gamma^\mu e_t)$			
$Q_{qq}^{(1)}$	$(ar q_p \gamma_\mu q_r) (ar q_s \gamma^\mu q_t)$	Q_{uu}	$(ar{u}_p \gamma_\mu u_r)(ar{u}_s \gamma^\mu u_t)$	Q_{lu}	$(ar{l}_p \gamma_\mu l_r) (ar{u}_s \gamma^\mu u_t)$			
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r) (\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{dd}	$(ar{d}_p\gamma_\mu d_r)(ar{d}_s\gamma^\mu d_t)$	Qid	$(\bar{l}_p \gamma_\mu l_r) (\bar{d}_s \gamma^\mu d_t)$			
$Q_{lq}^{(1)}$	$(ar{l}_p \gamma_\mu l_r) (ar{q}_s \gamma^\mu q_t)$	Qeu	$(ar{e}_p \gamma_\mu e_r) (ar{u}_s \gamma^\mu u_t)$	Q_{qe}	$(ar{q}_p \gamma_\mu q_r) (ar{e}_s \gamma^\mu e_t)$			
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r) (\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{ed}	$(ar{e}_p \gamma_\mu e_r) (ar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(ar{q}_p \gamma_\mu q_r) (ar{u}_s \gamma^\mu u_t)$			
		$Q_{ud}^{(1)}$	$(ar{u}_p \gamma_\mu u_r) (ar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r) (\bar{u}_s \gamma^\mu T^A u_t)$			
		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r) (\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(ar{q}_p\gamma_\mu q_r)(ar{d}_s\gamma^\mu d_t)$			
				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r) (\bar{d}_s \gamma^\mu T^A d_t)$			
$(\bar{L}R)$	$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		<i>B</i> -violating					
Q_{ledq}	$(ar{l}_p^j e_r)(ar{d}_s q_t^j)$	Q_{duq}	$\varepsilon^{\alpha\beta\gamma}\varepsilon_{jk}\left[(d_p^{\alpha})^T C u_r^{\beta}\right]\left[(q_s^{\gamma j})^T C l_t^k\right]$					
$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	Q_{qqu}	$Q_{qqu} \qquad \varepsilon^{\alpha\beta\gamma}\varepsilon_{jk} \left[(q_p^{\alpha j} $		$)^{T}Cq_{r}^{eta k}] \left[(u_{s}^{\gamma})^{T}Ce_{t} ight]$			
$Q_{quqd}^{(8)}$			$\varepsilon^{\alpha\beta\gamma}\varepsilon_{jk}\varepsilon_{mn}\left[(q_p^{\alpha j})^T C q_r^{\beta k}\right]\left[(q_s^{\gamma m})^T C l_t^n\right]$					
$Q_{lequ}^{(1)}$	$Q_{lequ}^{(1)} \qquad (\bar{l}_p^j e_r) \varepsilon_{jk}(\bar{q}_s^k u_t) \qquad Q_{duu}$		$arepsilon^{lphaeta\gamma}\left[(d_p^lpha)^TCu_r^eta ight]\left[(u_s^\gamma)^TCe_t ight]$		$\left[(u_s^\gamma)^T C e_t ight]$			
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$							