Triple-leptoquark interactions for tree- and loop-level proton decays



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Effective lagrangian describing baryon number violation

Lattice QCD for the hadronic part

Scalar Leptoquarks

Triple leptoquark interactions

Proton decay at tree-level

Proton decay at loop-level

Motivation

• Wigner suggested proton decay in1949 and 1952

Theoretical side



Wigner "It is conceivable, for instance, that a conservation law for the number of heavy particles (protons and neutrons) is responsible for the stability of the protons in the same way as the conservation law for charges is responsible for the stability of the electron. Without the conservation law in question, the proton could disintegrate, under emission of a light quantum, into a positron, just as the electron could disintegrate, were it not for the conservation law for the electric charge, into a light quantum and a neutrino."

• 1965 Sakharov



After 1965 Sakharov returned to fundamental science and began working on particle physics and particle cosmology. He tried to explain the <u>baryon asymmetry</u> of the universe; in that regard, he was the first to give a theoretical motivation for proton decay.

• 1974: Grand unified theories, Georgi & Glashow SU(5)





Future experiments



Proton decays in effective Lagrangian approach

dimension 6

$$\mathcal{L}_{d=6} = y_{abcd}^{1} \epsilon^{\alpha\beta\gamma} (\overline{d}_{a,\alpha}^{C} u_{b,\beta}) (\overline{Q}_{i,c,\gamma}^{C} \epsilon_{ij} L_{j,d}) + y_{abcd}^{2} \epsilon^{\alpha\beta\gamma} (\overline{Q}_{i,a,\alpha}^{C} \epsilon_{ij} Q_{j,b,\beta}) (\overline{u}_{c,\gamma}^{C} \ell_{d}) + y_{abcd}^{3} \epsilon^{\alpha\beta\gamma} \epsilon_{il} \epsilon_{jk} (\overline{Q}_{i,a,\alpha}^{C} Q_{j,b,\beta}) (\overline{Q}_{k,c,\gamma}^{C} L_{l,d}) + y_{abcd}^{4} \epsilon^{\alpha\beta\gamma} (\overline{d}_{a,\alpha}^{C} u_{b,\beta}) (\overline{u}_{c,\gamma}^{C} \ell_{d}) + \text{h.c.},$$

Q, L \rightarrow SU(2)_L quark, lepton doublets u ,d, l \rightarrow SU(2)_L u, d, charged lepton singlets C \rightarrow charge conjugation





$$\Gamma(p \to e^+ \pi^0) \simeq \frac{1}{2 \times 10^{34} \,\mathrm{yr}} \left| \frac{y_{1111}^j}{(3 \times 10^{15} \,\mathrm{GeV})^{-2}} \right|^2.$$

$$\Gamma(n \to \bar{\nu}_{\tau} \pi^0) \simeq \frac{1}{10^{33} \,\mathrm{yr}} \left| \frac{y_{3333}^4}{(5 \times 10^8 \,\mathrm{GeV})^{-2}} \right|^2.$$



Instead of X,Y scalar leptoquarks can mediate this process



e.g. Doršner, SF & Košnik, 1204.0674

Important: scalar LQ should have di-quark couplings that proton decays at the tree level (dim-6, dim-9,...)

(SU(3), SU(2), U(1))	Spin	Symbol	Type	F
$(\overline{3}, 3, 1/3)$	0	S_3	$LL\left(S_{1}^{L} ight)$	-2
(3, 2, 7/6)	0	R_2	$RL(S^L_{1/2}),LR(S^R_{1/2})$	0
(3, 2, 1/6)	0	$ ilde{R}_2$	$RL(ilde{S}^{L}_{1/2}),\overline{LR}(ilde{S}^{\overline{L}}_{1/2})$	0
$(\overline{3},1,4/3)$	0	$ ilde{S}_1$	$RR\left(ilde{S}_{0}^{R} ight)$	-2
$(\overline{3},1,1/3)$	0	S_1	$LL\left(S_{0}^{L} ight),RR\left(S_{0}^{R} ight),\overline{RR}\left(S_{0}^{\overline{R}} ight)$	-2
$(\overline{\bf 3}, {\bf 1}, -2/3)$	0	$ar{S}_1$	$\overline{RR}(ar{S}_0^{\overline{R}})$	-2
$({\bf 3},{\bf 3},2/3)$	1	U_3	$LL\left(V_{1}^{L} ight)$	0
$(\overline{\bf 3},{f 2},5/6)$	1	V_2	$RL(V_{1/2}^L), LR(V_{1/2}^R)$	-2
$(\overline{3}, 2, -1/6)$	1	$ ilde{V}_2$	$RL(ilde{V}^L_{1/2}),\overline{LR}(ilde{V}^{\overline{R}}_{1/2})$	-2
$({f 3},{f 1},5/3)$	1	$ ilde{U}_1$	$RR(ilde{V}^R_0)$	0
$({f 3},{f 1},2/3)$	1	U_1	$LL\left(V_{0}^{L} ight),RR\left(V_{0}^{R} ight),\overline{RR}\left(V_{0}^{\overline{R}} ight)$	0
$({f 3},{f 1},-1/3)$	1	$ar{U}_1$	$\overline{RR}(ar{V}_0^{\overline{R}})$	0

I. Dorsner, SF, A. Greljo, J.F. Kamenik and Košnik, 1603.04993

F- fermion number F = 3B + LF=0 proton stable

Tree-level renormalizable interactions are not the only possible source of baryon number violation. It might also occur through higher-dimensional operators.

Proton decay to charged leptons

channel	$(\Delta L_e, \Delta L_\mu)$	limit/years
$p \rightarrow e^+ e^+ e^-$	(1,0)	793×10^{30}
$p \to e^+ \mu^+ \mu^-$	(1,0)	359×10^{30}
$p \rightarrow \mu^+ e^+ e^-$	(0,1)	529×10^{30}
$p \to \mu^+ \mu^+ \mu^-$	(0,1)	675×10^{30}
$p \to \mu^+ \mu^+ e^-$	(-1, 2)	359×10^{30}
$p \rightarrow e^+ e^+ \mu^-$	(2, -1)	529×10^{30}

Hambye & Heeck 1712.04871 16 dimension-nine operators



F - new fermion



Arnold et al., 1212.455, Murgui & Wise, 2105.14029 found if three LQ X_1 are in the same representation that this amplitude vanishes.

Triple-leptoquark interactions for tree- and loop-level proton decays





Triple-LQs - scalars only!

Two different proton decay topologies

- with or without a Higgs vacuum expectation value

- Δ_Q , Δ_Q , and $\Delta_{Q'}$ are scalar leptoquark mass eigenstates with electric charges Q, Q', and Q'', respectively.

Classification

Leptoquark multiplets	Yukawa interactions
$R_2 = (3, 2, 7/6)$	$-(y_{R_2}^L)_{ij} \bar{u}_{Ri} R_2 i \tau_2 L_j + (y_{R_2}^R)_{ij} \bar{Q}_i R_2 e_{Rj} + \text{h.c.}$
$ ilde{R}_2 = ({f 3}, {f 2}, 1/6)$	$-(y_{\tilde{R}_2}^L)_{ij}\bar{d}_{Ri}\tilde{R}_2i\tau_2L_j+\text{h.c.}$
$S_1 = (\bar{3}, 1, 1/3)$	$(y_{S_1}^L)_{ij} \bar{Q}_i^C i \tau_2 S_1 L_j + (y_{S_1}^R)_{ij} \bar{u}_{Ri}^C S_1 e_{Rj} + \text{h.c.}$
$S_3 = (\bar{3}, 3, 1/3)$	$(y_{S_3}^L)_{ij} \bar{Q}_i^C i \tau_2 (\vec{\tau} \cdot \vec{S}_3) L_j + \text{h.c.}$
$\tilde{S}_1 = (\bar{3}, 1, 4/3)$	$(y_{\tilde{S}_1}^R)_{ij}\bar{d}_{Ri}^C\tilde{S}_1e_{Rj}+\text{h.c.}$

scalars

Scalar leptoquark multiplets and their interactions with the SM quark-lepton pairs.

The SM extended with up to three different scalar leptoquark multiplets, denoted with Δ , Δ' , and Δ'' and study all possible cubic and quartic contractions Δ - Δ' - Δ'' and Δ - Δ' - Δ'' -H, yield to 3-LQ interactions and 3-LQ (H).



 $S_3^{1/3} = S_3^3, \ S_3^{4/3} = (S_3^1 - iS_3^2)/\sqrt{2}, \ S_3^{-2/3} = (S_3^1 + iS_3^2)/\sqrt{2}$

Cubic and quartic leptoquark multiplet contractions at the $SU(3) \times SU(2) \times U(1)$ level and the associated triple-leptoquark interactions at the $SU(3) \times U(1)_{em}$ level

$$\begin{split} \tilde{R}_2 &- \tilde{R}_2 - \tilde{R}_2 - H^*, \ S_1 - S_1 - R_2^* - H, \\ \tilde{R}_2 &- \tilde{R}_2 - S_3^*, \ S_1 - S_1 - \tilde{R}_2^* - H^* \\ & \text{vanish} \end{split}$$

symmetric under the exchange of two identical electric charge eigenstates in direct conflict with the antisymmetric nature in the colour SU(3) space.

Way out: to accommodate them in different representations.

Phenomenological analysis



$$\Gamma(p \to e^+ e^+ e^-) \simeq \frac{m_p}{(16\pi)^3} \left(\frac{m_p^5 v}{\Lambda^6}\right)^2 |\lambda y_{ue}^2 y_{de}|^2$$

$$\Gamma(p \to \pi^0 e^+) \simeq \frac{m_p}{16\pi} \left(\frac{m_p^2}{\Lambda^2}\right)^2 |y_{ud} y_{ue}|^2$$

Comparison tree and loop level proton decay width

an example



$$\frac{\Gamma(p \to e^+ e^+ e^-)}{\Gamma(p \to \pi^0 e^+)} \simeq \frac{1}{\pi^2} \left(\frac{m_p^3}{m_f \Lambda^2}\right)^2 \simeq 10^{-7} \left(\frac{m_e}{m_f}\right)^2 \left(\frac{1 \,\mathrm{TeV}}{\Lambda}\right)^4,$$

The loop-induced processes are more sensitive probes of the triple-leptoquark interactions than the tree-level ones

comparison of the existing data
$$p \rightarrow e^- e^+ e^+$$
 $p \rightarrow \pi^0 e^+$

$$\Gamma(p \to \pi^0 \ell^+) \sim \frac{1}{10} \Gamma(p \to \ell^+ \ell^- \ell^+)$$

	Contractions	Operators	Proton decay (tree)	Proton decay (one-loop)
$(a) \tilde{D} \tilde{D} C^*$	$ddd\bar{e}\nu\bar{\nu}$	$p \to \pi^+ \pi^+ e^- \nu \bar{\nu}$	_	
(a)	(a) $R_2 - R_2 - S_1$	$ddu e \bar{e} \bar{\nu}$	$p \to \pi^+ e^+ e^- \nu$	$p \to \pi^+ \nu$
(1) D \tilde{D} \tilde{C}^*	$ddde \bar{e} \bar{e}$	$p \to \pi^+ \pi^+ e^- e^+ e^-$	_	
	$(0) \qquad n_2 \cdot n_2 \cdot s_1$	$ddu e \bar{e} \bar{\nu}$	$p \to \pi^+ e^+ e^- \nu$	$p \to \pi^+ \nu$
	$ddu e \bar{e} \nu$	$p \to \pi^+ e^+ e^- \bar{\nu}$	$p \to \pi^+ \bar{\nu}$	
(c)	$S_{1}-S_{2}-B_{2}^{*}-H$	$duue \nu \bar{\nu}$	$p \to e^+ \nu \bar{\nu}$	$p \to \pi^0 e^+$
	$(c) S_1 - S_3 - R_2 - R_1$	$duuee\bar{e}$	$p \rightarrow e^+ e^+ e^-$	$p \to \pi^0 e^+$
		$uuuee\bar{\nu}$	$p \to \pi^- e^+ e^+ \nu$	-
		$ddu e \bar{e} \nu$	$p \to \pi^+ e^+ e^- \bar{\nu}$	$p \to \pi^+ \bar{\nu}$
(d) $S_3-S_3-R_2^*-H$	$duue \nu \bar{\nu}$	$p \to e^+ \nu \bar{\nu}$	-	
	$duuee\bar{e}$	$p \rightarrow e^+ e^+ e^-$	$p \rightarrow \pi^0 e^+$	
(e) S. \tilde{S} R* H*	$ddu e \bar{e} \nu$	$p \to \pi^+ e^+ e^- \bar{\nu}$	$p \to \pi^+ \bar{\nu}$	
	51 51 102 11	$duuee\bar{e}$	$p \rightarrow e^+ e^+ e^-$	$p \to \pi^0 e^+$
		$ddu e \bar{e} \nu$	$p \to \pi^+ e^+ e^- \bar{\nu}$	$p \to \pi^+ \bar{\nu}$
(f)	$S_3 - \tilde{S}_1 - R_2^* - H^*$	$duue \nu \bar{\nu}$	$p \to e^+ \nu \bar{\nu}$	$p \to \pi^0 e^+$
		$duuee\bar{e}$	$p \rightarrow e^+ e^+ e^-$	$p \rightarrow \pi^0 e^+$
		$ddu \nu \bar{\nu} \nu$	$p \to \pi^+ \nu \bar{\nu} \bar{\nu}$	$p \to \pi^+ \bar{\nu}$
$(g) S_1 - S_3 - \tilde{R}_2^* - H$	S S Ã* H*	$ddu e \bar{e} \nu$	$p \to \pi^+ e^+ e^- \bar{\nu}$	$p \to \pi^+ \bar{\nu}$
	51-53-112-11	$duue \nu \bar{\nu}$	$p \to e^+ \nu \bar{\nu}$	$p \to \pi^0 e^+$
		$duuee\bar{e}$	$p \rightarrow e^+ e^+ e^-$	$p \to \pi^0 e^+$
(h)	$S_3 - S_3 - \tilde{R}_2^* - H^*$	$ddu\nu\bar{\nu}\nu$	$p \to \pi^+ \nu \bar{\nu} \bar{\nu}$	$p \rightarrow \pi^+ \bar{\nu}$
		$ddu e \bar{e} \nu$	$p \to \pi^+ e^+ e^- \bar{\nu}$	-
		$duue \nu \bar{\nu}$	$p \to e^+ \nu \bar{\nu}$	$p \to \pi^0 e^+$

non-trivial Δ - Δ ' - Δ " and Δ - Δ ' - Δ " -H contractions,

d = 9 effective operators, and corresponding proton decay

The effective operators in scenarios (a) and (b) conserve B + L, while the ones appearing in the remaining scenarios conserve B - L, where B and L are baryon and lepton numbers, respectively.

Tree-level leptoquark mediation of $p \rightarrow e^- e^+ e^+$

$$\begin{aligned} \mathcal{L}_{\text{eff}}^{(d=9)} \supset \sum_{X=L,R} \epsilon_{abc} C_X \left(\bar{u}_a^C P_L e \right) (\bar{d}_b^C P_L e) (\bar{e} P_X u_c) + \text{h.c.}, \\ C_L &= \frac{2\sqrt{2}\lambda v}{m_{3_3}^4 m_{R_2}^2} (V^* y_{3_3}^L) y_{3_3}^L (Vy_{R_2}^R)^*, \\ C_R &= -\frac{2\sqrt{2}\lambda v}{m_{3_3}^4 m_{R_2}^2} (V^* y_{3_3}^L) y_{3_3}^L (y_{3_3}^L)^*. \\ C_{abc} \langle 0 | (\bar{u}_a^C P_R d_b) P_L u_c | p \rangle = \alpha_p P_R u_p \\ \epsilon_{abc} \langle 0 | (\bar{u}_a^C P_L d_b) P_L u_c | p \rangle = \beta_p P_L u_p \\ \theta_p &= +0.0144(3)(21) \text{ GeV}^3 \\ \theta_p &= +0.0144(3)(21) \text{ GeV}^3 \\ \text{Lattice QCD} \quad \text{Aoki et al. 1705.01338} \\ \text{Decay width} \quad \Gamma(p \rightarrow e^+ e^+ e^-) = \frac{m_p^5}{6(16\pi)^3} \left(\beta_p^2 |C_L|^2 + \alpha_p^2 |C_R|^2 \right) \\ \tau(p \rightarrow e^+ e^+ e^-) > 3.4 \times 10^{34} \text{ years} \quad \begin{array}{c} \text{experiment SuperKamiokande} \\ \text{Takenaka et al., 2010.16098} \\ \text{Takenaka et al., 2010.16098} \\ m_{S_3} &= m_{R_2} = \Lambda \\ m_{S_3} &= m_{R_2} = \Lambda \\ \end{array} \right) \xrightarrow{p \rightarrow e^+ e^+ e^- : \Lambda \ge 1.6 \times 10^2 \text{ TeV}} \end{aligned}$$

Loop-level leptoquark mediation of $p \to \pi^0 e^+$

$$\mathcal{L}_{\text{eff}}^{(d=6)} \supset C_{LL}^{udeu} \left(\overline{u}^{C} P_{L} d \right) \left(\overline{e}^{C} P_{L} u \right) + C_{LR}^{udeu} \left(\overline{u}^{C} P_{L} d \right) \left(\overline{e}^{C} P_{R} u \right) + \text{h.c.},$$

Explicit loop computation

General scenario

$$\mathcal{L}_{\text{scalar}} \supset \lambda \, v \, \varepsilon_{abc} \, \Delta_a^Q \, \Delta_b^{Q'} \, \Delta_c^{Q''} + \text{h.c.}$$

LQ interactions with quarks and leptons

$$\mathcal{L}_{\text{yuk.}} \supset \overline{q} \left(y_R P_R + y_L P_L \right) \ell \, \Delta^Q + \overline{q'^C} \left(y'_R P_R + y'_L P_L \right) \ell \, \Delta^{Q'*} + \text{h.c.}$$

The loop diagram corresponds to a loop-induced diquark coupling of the $\Delta_{Q'}$ leptoquark

$$\mathcal{L}_{qq'} = \varepsilon_{abc} \,\overline{q_a^C} \left(y_{qq'}^L P_L + y_{qq'}^L P_R \right) q_b' \,\Delta_c^{Q''} + \text{h.c.}$$
$$y_{qq'}^L = \frac{\lambda v}{16\pi^2 m_\Delta^2} \left(m_\ell \, y_L' y_R^* - \frac{m_q}{4} y_R' y_R^* - \frac{m_{q'}}{4} y_L' y_L^* \right)$$
$$y_{qq'}^R = \frac{\lambda v}{16\pi^2 m_\Delta^2} \left(m_\ell \, y_R' y_L^* - \frac{m_q}{4} y_L' y_L^* - \frac{m_{q'}}{4} y_R' y_R^* \right)$$

Chirality flip in the internal lepton and external quark lines



Ingredients

$$C_{LL}^{udeu} = \frac{\sqrt{2\lambda}}{8\pi^2} \frac{vm_e}{\Lambda^4} (V^* y_{S_3}^L) \left[y_{S_3}^L (Vy_{R_2}^R)^* + \frac{m_d}{4m_e} y_{S_3}^L (y_{R_2}^L)^* \right],$$

$$C_{LR}^{udeu} = \frac{\lambda}{32\pi^2} \frac{vm_u}{\Lambda^4} (V^* y_{S_3}^L)^2 (y_{R_2}^L)^*.$$

$$\left\langle \pi^0 \left| \mathcal{O}^{\Gamma\Gamma'} \right| p \right\rangle = \left[W_0^{\Gamma\Gamma'} (q^2) - \frac{iq}{m_p} W_1^{\Gamma\Gamma'} (q^2) \right] P_{\Gamma'} u_p$$

$$\mathcal{O}^{\Gamma\Gamma'} = (\overline{u}^C P_{\Gamma} d) P_{\Gamma'} u \qquad \text{Form factors}$$

$$\Gamma, \Gamma' = R, L. \quad \langle \pi^+ | (\overline{u}^C P_{\Gamma} d) P_{\Gamma'} d | p \rangle = \sqrt{2} \langle \pi^0 | (\overline{u}^C P_{\Gamma} d) P_{\Gamma'} u | p \rangle$$

$$\Gamma(p \to \pi^0 e^+) = \frac{m_p}{32\pi} \left(1 - \frac{m_\pi^2}{m_p^2} \right)^2 \left[(W_0^{LL})^2 |C_{LL}^{udeu}|^2 + (W_0^{RL})^2 |C_{LR}^{udeu}|^2 \right]$$

$$W_0^{LL} = 0.134(5) \text{ GeV}^2 \quad W_0^{LR} = -0.131(4) \text{ GeV}^2 \quad \text{Lattice QCD, Aoki et al., 1705.01338}$$

assuming
$$y_{S_3}^L = y_{R_2}^L = y_{R_2}^R = \lambda = 1$$
 and $m_{S_3} = m_{R_2} = \Lambda$
 $p \to \pi^0 e^+ : \quad \Lambda \ge 1.8 \times 10^4 \,\mathrm{TeV}$

 $p \to \pi^+ \bar{\nu}$



$$\Gamma(p \to \pi^+ \nu) = \frac{m_p}{16\pi} \left(1 - \frac{m_\pi^2}{m_p^2} \right)^2 \left[(W_0^{LL})^2 |C_{LL}^{ud\nu d}|^2 + (W_0^{RL})^2 |C_{RL}^{ud\nu d}|^2 \right]$$

assuming
$$y_{S_3}^L = y_{R_2}^L = y_{R_2}^R = \lambda = 1$$
 and $m_{S_3} = m_{R_2} = \Lambda$
 $p \to \pi^+ \bar{\nu} : \qquad \Lambda \ge 1.2 \times 10^4 \,\mathrm{TeV}$

Conclusions

- we study a phenomenological impact of triple-leptoquark interactions on proton stability;
- there are two different decay topologies under the assumption that scalar leptoquarks of interest couple solely to the quark-lepton pairs;
- the tree level topology has been analysed in the literature before in the context of baryon number violation while the one-loop level one has not been featured in any scientific study to date;
- we demonstrate that it is the one-loop level topology that is producing more stringent bounds on the scalar leptoquark masses of the two, if and when they coexist;

$$p \to e^+ e^+ e^- : \quad \Lambda \ge 1.6 \times 10^2 \,\mathrm{TeV}$$

 $p \to \pi^0 e^+ : \quad \Lambda \ge 1.8 \times 10^4 \,\mathrm{TeV}$

 we also specify the most prominent proton decay signatures due to the presence of all non-trivial cubic and quartic contractions involving three scalar leptoquark multiplets, where in the latter case one of the scalar multiplets is the SM Higgs doublet

Thanks



Grazie

dimension-nine operators

$\mathcal{O}_1^9 = (QQ)_1(\bar{L}\bar{L})_1(\ell d) ,$	$\mathcal{O}_2^9 = (QQ)_1(\bar{L}\ell)(\bar{L}d),$
$\mathcal{O}_3^9 = (QL)_1(\bar{L}d)(\bar{L}d) ,$	$\mathcal{O}_4^9 = (\bar{\ell}Q)(\bar{L}d)(\ell d) ,$
$\mathcal{O}_5^9 = (ar{L}ar{L})(ud)(\ell d),$	$\mathcal{O}_6^9 = (\bar{L}u)(\bar{L}d)(\ell d) ,$
$\mathcal{O}_7^9 = (ar{L}d)(ar{L}\ell)(ud),$	$\mathcal{O}_8^9 = (\bar{L}d)(\bar{L}d)(\ell u) ,$
$\mathcal{O}_9^9 = (QL)_3((\bar{L}d)(\bar{L}d))_3,$	$\mathcal{O}_{10}^9 = (QL)_1(\bar{L}\bar{L})_1(dd),$
$\mathcal{O}_{11}^9 = (QL)_3(\bar{L}\bar{L})_3(dd) ,$	${\cal O}^9_{12} \; = (ar \ell Q) (ar L \ell) (dd) ,$
$\mathcal{O}^{9}_{13} = (\bar{L}\bar{L})(u\ell)(dd) ,$	$\mathcal{O}_{14}^9 = (\bar{L}u)(\bar{L}\ell)(dd) ,$
$\mathcal{O}^9_{15} = (\bar{\ell}L)(\bar{L}d)(dd) ,$	$\mathcal{O}^9_{16} = (ar{\ell}ar{\ell})(\ell d)(dd) .$

$$\Gamma(p \to \ell_{\alpha}^{+} \ell_{\beta}^{+} \ell_{\gamma}^{-}) \sim \frac{\langle H \rangle^{2} \beta_{\mathrm{h}}^{2} m_{p}^{5}}{6144 \pi^{3} \Lambda^{12}} \simeq \frac{\left(100 \,\mathrm{TeV}/\Lambda\right)^{12}}{10^{33} \,\mathrm{yrs}}$$

d = 9 effective operators

$$\begin{split} \mathcal{L}_{(a)} &\supset \frac{2\kappa\epsilon_{abc}}{m_{R_2}^4} (y_{R_2}^L)_{1j}^* (\bar{\nu}_L^j d_{Ra}) (y_{R_2}^L)_{1k}^* (\bar{e}_L^k d_{Rb}) \\ &\times \left[(V^* y_{S_1}^L)_{1i} (\bar{u}_L^C e_L^i) - (y_{S_1}^L)_{1i} (\bar{d}_L^C \nu_L^i) + (y_{S_1}^R)_{1i} (\bar{u}_R^C e_R^i) \right] + \text{h.c.} \,, \\ \mathcal{L}_{(b)} &\supset \frac{\kappa\epsilon_{abc}}{m_{S_1}^2 m_{R_2}^2} \left\{ \left[(Vy_{R_2}^R)_{1j}^* (\bar{e}_R^j u_{La}) - (y_{R_2}^L)_{1j}^* (\bar{e}_L^j u_{Ra}) \right] (y_{R_2}^L)_{1k}^* (\bar{\nu}_L^k d_{Rb}) \\ &+ \left[(y_{R_2}^L)_{1i}^* (\bar{\nu}_L^j u_{Ra}) + (y_{R_2}^R)_{1j}^* (\bar{e}_R^j d_{La}) \right] (y_{R_2}^L)_{1k}^* (\bar{e}_L^k d_{Rb}) \right\} (y_{S_1}^R)_{1i} (\bar{d}_L^C e_R^i) + \text{h.c.} \,, \\ \mathcal{L}_{(c)} &\supset \frac{\lambda\epsilon_{abc}v}{\sqrt{2}m_{S_3}^2 m_{R_2}^2 m_{S_1}^2} \left[(V^* y_{S_1}^L)_{1i} (\bar{u}_L^C e_L^i) - (y_{S_1}^L)_{1i} (\bar{d}_L^C \nu_L^i) + (y_{S_1}^R)_{1i} (\bar{u}_R^C e_R^i) \right] \\ &\quad \times \left\{ \left[(V^* y_{S_3}^L)_{1j} (\bar{u}_L^C e_L^j) + (y_{S_3}^L)_{1j} (\bar{d}_L^C u_L^j) \right] \left[(y_{R_2}^L)_{1k}^* (\bar{\nu}_L^k u_{Rb}) + (y_{R_2}^R)_{1k}^* (\bar{e}_R^k d_{Lb}) \right] \\ &- \sqrt{2} (y_{S_3}^L)_{1j} (\bar{d}_L^C e_L^j) \left[(Vy_{R_2}^R)_{1k}^* (\bar{e}_R^k u_{Lb}) - (y_{R_2}^L)_{1k}^* (\bar{e}_L^k u_{Rb}) \right] \right\} + \text{h.c.} \,, \\ \mathcal{L}_{(d)} &\supset \frac{2\sqrt{2}\lambda\epsilon_{abc}v}{m_{A_3}^4 m_{R_2}^2} (y_{S_3}^L)_{1j} (\bar{d}_L^C e_L^j) \\ &\quad \times \left\{ (V^* y_{S_3}^L)_{1k} (\bar{u}_L^C \nu \nu_L^k) \left[(y_{R_2}^L)_{1i}^* (\bar{\nu}_L^i u_{Rc}) + (y_{R_2}^R)_{1i}^* (\bar{e}_R^i d_{Lc}) \right] \\ &\quad + \left[(y_{S_3}^L)_{1k} (\bar{d}_L^C \nu \nu_L^k) + (V^* y_{S_3}^L)_{1k} (\bar{u}_L^C e_L^k) \right] \left[(y_{R_2}^L)_{1i}^* (\bar{e}_L^i u_{Rc}) - (Vy_{R_2}^R)_{1i}^* (\bar{e}_R^i u_{Lc}) \right] \right\} \\ &\quad + \text{h.c.} \end{split}$$

$$\begin{split} \mathcal{L}_{(e)} &\supset \frac{-\lambda \epsilon_{abc} v}{\sqrt{2} m_{\tilde{S}_{1}}^{2} m_{R_{2}}^{2} m_{S_{1}}^{2}} (y_{\tilde{S}_{1}}^{R})_{1i} (\bar{d}_{Rc}^{C} e_{R}^{i}) \Big[(y_{R_{2}}^{L})_{1j}^{*} (\bar{e}_{L}^{j} u_{Ra}) - (Vy_{R_{2}}^{R})_{1j}^{*} (\bar{e}_{R}^{j} u_{La}) \Big] \\ &\times \Big[(V^{*} y_{S_{1}}^{L})_{1k} (\bar{u}_{Lb}^{C} e_{L}^{k}) + (y_{S_{1}}^{R})_{1k} (\bar{u}_{Rb}^{C} e_{R}^{k}) - (y_{S_{1}}^{L})_{1k} (\bar{d}_{Lb}^{C} \nu_{L}^{k}) \Big] + \text{h.c.} \,, \\ \mathcal{L}_{(f)} &\supset \frac{\lambda \epsilon_{abc} v}{\sqrt{2} m_{R_{2}}^{2} m_{S_{3}}^{2} m_{\tilde{S}_{1}}^{2}} (y_{\tilde{S}_{1}}^{R})_{1i} (\bar{d}_{c}^{C} P_{R} e^{i}) \\ &\times \Big\{ 2 (V^{*} y_{S_{3}}^{L})_{1j} (\bar{u}_{La}^{C} \nu_{L}^{j}) \Big[(y_{R_{2}}^{L})_{1k}^{*} (\bar{\nu}_{L}^{k} u_{Rb}) + (y_{R_{2}}^{R})_{1k}^{*} (\bar{e}_{R}^{k} d_{Lb}) \Big] \\ &+ \Big[(y_{S_{3}}^{L})_{1j} (\bar{d}_{La}^{C} \nu_{L}^{j}) + (V^{*} y_{S_{3}}^{L})_{1j} (\bar{u}_{La}^{C} e_{L}^{j}) \Big] \Big[(y_{R_{2}}^{L})_{1k}^{*} (\bar{e}_{L}^{k} u_{Rb}) - (Vy_{R_{2}}^{R})_{1k}^{*} (\bar{e}_{R}^{k} u_{Lb}) \Big] \Big\} \\ \mathcal{L}_{(g)} &\supset \frac{\lambda \epsilon_{abc} v}{\sqrt{2} m_{S_{3}}^{2} m_{\tilde{R}_{2}}^{2} m_{S_{1}}^{2}} \Big[(V^{*} y_{S_{1}}^{L})_{1i} (\bar{u}_{Lc}^{C} e_{L}^{j}) - (y_{S_{1}}^{L})_{1i} (\bar{d}_{Lc}^{C} \nu_{L}^{j}) + (V_{S_{1}}^{R})_{1i} (\bar{u}_{Rc}^{C} e_{R}^{i}) \Big] \\ &\times \Big\{ \Big[(y_{S_{3}}^{L})_{1j} (\bar{d}_{La}^{C} \nu_{L}^{j}) + (V^{*} y_{S_{3}}^{L})_{1j} (\bar{u}_{La}^{C} e_{L}^{j}) \Big] (y_{\tilde{R}_{2}}^{L})_{1k}^{*} (\bar{e}_{L}^{k} d_{Rb}) \\ &+ 2 (V^{*} y_{S_{3}}^{L})_{1j} (\bar{u}_{La}^{C} \nu_{L}^{j}) (y_{\tilde{R}_{2}}^{L})_{1k}^{*} (\bar{\nu}_{L}^{k} d_{Rb}) \Big\} + \text{h.c.} \,, \\ \mathcal{L}_{(h)} &\supset \frac{2 \sqrt{2} \lambda \epsilon_{abc} v}{m_{S_{3}}^{K} m_{\tilde{R}_{2}}^{2}} \Big\{ (y_{S_{3}}^{L})_{1j} (\bar{d}_{La}^{C} e_{L}^{j}) (V^{*} y_{\tilde{S}_{3}}^{L})_{1k} (\bar{d}_{Lb}^{C} \nu_{L}^{k}) (y_{\tilde{R}_{2}}^{L})_{1k}^{*} (\bar{d}_{Lb}^{c} e_{L}^{k}) \\ &- (y_{\tilde{R}_{2}}^{L})_{1i}^{*} (\bar{\nu}_{L}^{k} d_{Rc}) (V^{*} y_{S_{3}}^{L})_{1j} (\bar{u}_{La}^{C} e_{L}^{j}) \Big[(y_{S_{3}})_{1k}^{L} (\bar{d}_{Lb}^{C} \nu_{L}^{k}) + (V^{*} y_{S_{3}}^{L})_{1k} (\bar{u}_{Lb}^{C} e_{L}^{k}) \Big] \Big\} + \text{h.c.} \,. \end{aligned}$$

Channel	$ \Delta(B-L) $	$\frac{\Gamma^{-1}}{10^{30}\mathrm{yr}}$
$p \to e^+ + \gamma$	0	41000 [72]
$p \to e^+ + \pi^0$	0	16000 [24]
$p \to e^+ + \eta$	0	10000 [73]
$p \to e^+ + \rho^0$	0	720 [73]
$p \to e^+ + \omega$	0	$1600 \ [73]$
$p \to e^+ + K^0$	0	$1000 \ [74]$
$p \to e^+ + K^{*,0}$	0	84 [65]
$p \to \mu^+ + \gamma$	0	21000 [72]
$p \to \mu^+ + \pi^0$	0	$7700 \ [24]$
$p \to \mu^+ + \eta$	0	4700 [73]
$p \to \mu^+ + \rho^0$	0	570 [73]
$p \to \mu^+ + \omega$	0	2800 [73]
$p \to \mu^+ + K^0$	0	$1600 \ [75]$
$p \to \nu + \pi^+$	0,2	390 [76]
$p \to \nu + \rho^+$	0,2	$162 \ [65]$
$p \to \nu + K^+$	0,2	5900 [77]
$p \rightarrow \nu + K^{*,+}$	$0,\!2$	130 [78]

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