



Search for Heavy Neutral Leptons in τ decays with *BABAR*

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BABAR
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on behalf of the *BABAR* Collaboration

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Heavy Neutral Leptons

- ▶ Heavy Neutral Leptons (HNLs) are additional neutrino states. Have mass so interact via gravity, but no weak hyper-charge, electric charge, weak isospin and color charge. Could be produced in experiments only via mixing with active neutrinos.
- ▶ Considered singlets - no associated charged lepton - they are “sterile.”
- ▶ HNLs are proposed by several beyond Standard Model (BSM) theories to explain three major observational phenomena:
 - Neutrino oscillations and origins of their mass via See-saw models etc. ([Phys. Rev. D 23,165](#));
 - Baryonic asymmetry of Universe ([Phys. Rev. Lett. 81, 1359](#));
 - Dark matter candidate ([Phys. Lett.B 631, 151–156](#)).
- ▶ Lighter sterile (eV-scale) neutrinos can also help explain various experimental observations:
 - “Reactor Anti-neutrino anomaly:” ([Phys. Rev. D 83, 07300](#)).
 - “Gallium anomaly:” ([Phys. Rev. C 80 015807](#)).
 - “Accelerator anomaly:” LSND ([Phys. Rev. D 64, 112007](#)) MiniBooNE ([Phys. Rev. Lett. 110, 161801](#))

This is why its important to explore HNLs.

Possible Mass-scale of HNLs

Depending on the model, wide range of models proposing HNLs across mass ranges :

1. $m_4 \sim O(\text{eV}/c^2)$: solve so-called “oscillation anomalies”.
2. $m_4 \sim O(\text{keV}/c^2)$: warm dark matter candidate.
3. $m_4 \sim O(\text{MeV}/c^2 - \text{GeV}/c^2)$: deviations in SM decays.
4. $m_4 \sim O(\text{GeV}/c^2 - \text{TeV}/c^2)$: can explain Baryonic Asymmetry via low-scale scenarios of leptogenesis without conflict with other cosmological observations.

e.g. ν -MSM model introduces three right-handed singlet HNLs:

- ▷ Two GeV/c^2 scale particles solve origin and smallness of SM neutrino mass with see saw mech.
- ▷ Third HNL is dark matter candidate with mass $\sim \text{keV}/c^2$. Also provides lepto-genesis due to Majorana mass term
(Phys. Rev. Lett. 81, 1359)
- ▷ ν -MSM fits with all current experimental constraints.
- ▷ keV-GeV scale can be searched for at existing experiments.

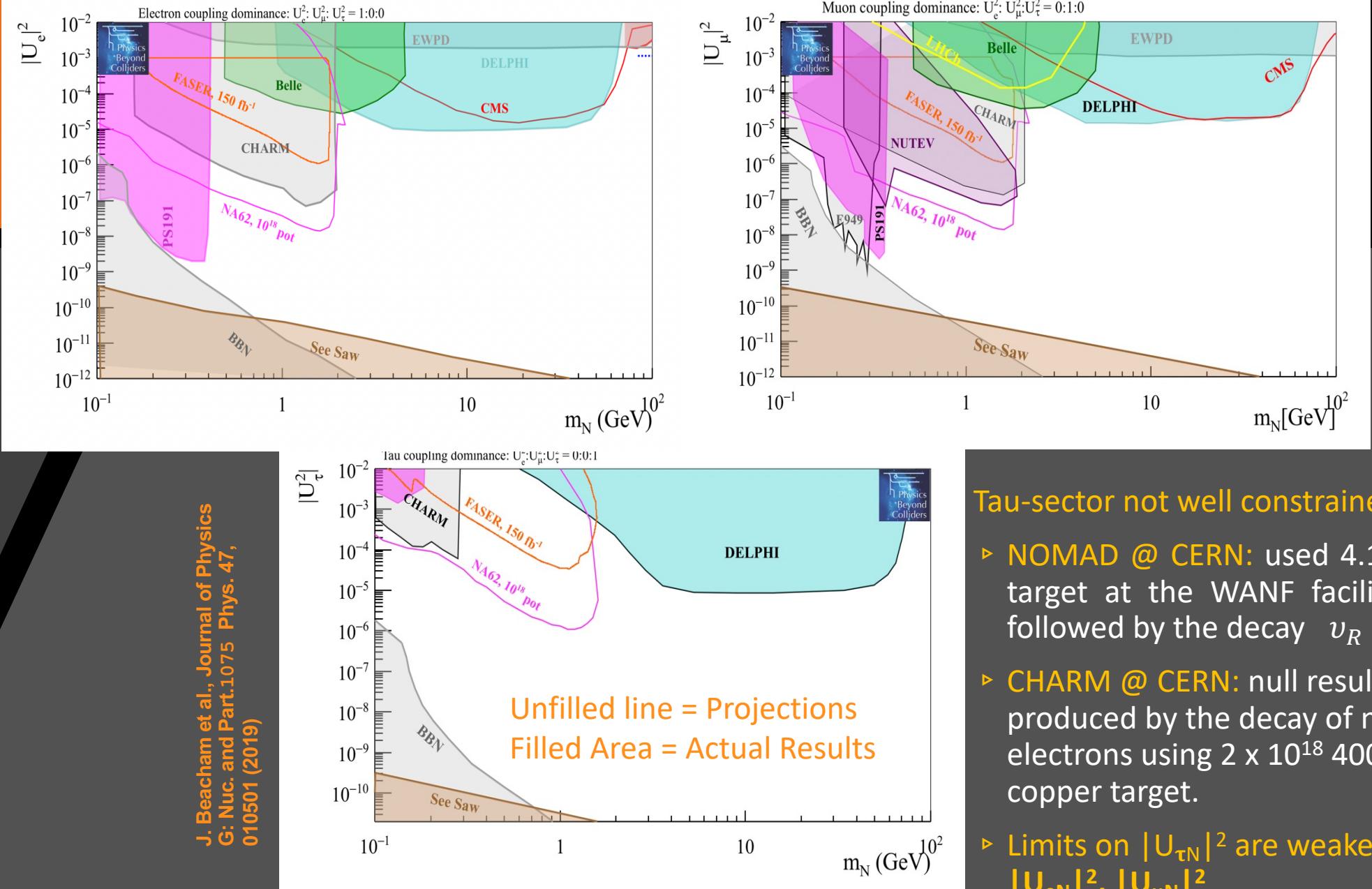
γ	0	0
photon	0	0
g	0	0
gluon	91.2 GeV	0
Z^0	weak force	0
W^\pm	80.4 GeV	± 1
Higgs boson	126 GeV	0
N_1	$\sim 10 \text{ keV}$	0
N_2	$\sim \text{GeV}$	0
N_3	$\sim \text{GeV}$	0
e	0.511 MeV	-1
electron	Left Right	
μ	105.7 MeV	-1
muon	Left Right	
τ	1.777 GeV	-1
tau	Left Right	
V_e	Left Right	
V_μ	Left Right	
V_τ	Left Right	
d	4.8 MeV	-1/3
down	Left Right	
s	104 MeV	-1/3
strange	Left Right	
u	2.4 MeV	2/3
up	Left Right	
c	1.27 GeV	2/3
charm	Left Right	
t	173.2 GeV	2/3
top	Left Right	

Extended PMNS Matrix

- Extend the PMNS for additional neutrino states:

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \\ \nu_s \\ \vdots \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} & U_{e4} & \dots \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} & U_{\mu 4} & \dots \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} & U_{\tau 4} & \dots \\ U_{s1} & U_{s2} & U_{s3} & U_{s4} & \dots \\ \vdots & \vdots & \vdots & \ddots & \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \\ \nu_4 \\ \vdots \end{pmatrix}.$$

- Experiments try to measure the matrix elements $|U_{ln}|^2$ where $l = e, \mu, \tau$ and $n = 4, 5, 6 \dots$
- Introduce new mass states $m_4, m_5 \dots$ etc. and sterile flavor state.
- Experiments generally quote results in parameter space of elements $|U_{ln}|^2$.v. HNL mass hypothesis.



Bounded from below by the BBN constraint (JCAP 1210 (2012) 014, [1202.2841]) and the see-saw limit (JCAP1009 (2010) 001, [1006.0133])

Tau-sector not well constrained:

- ▶ **NOMAD @ CERN:** used 4.1×10^{19} 450 GeV protons on target at the WANF facility. Searched for $D_s \rightarrow \tau v_R$ followed by the decay $v_R \rightarrow \nu_\tau e^+ e^-$.
- ▶ **CHARM @ CERN:** null result of a search for events produced by the decay of neutral particles into two electrons using 2×10^{18} 400 GeV protons on a solid copper target.
- ▶ Limits on $|U_{\tau N}|^2$ are weaker, motivating $|U_{\tau N}|^2 \gg |U_{e N}|^2, |U_{\mu N}|^2$

J. Beacham et al., Journal of Physics G: Nuc. and Part.1075 Phys. 47, 010501 (2019)

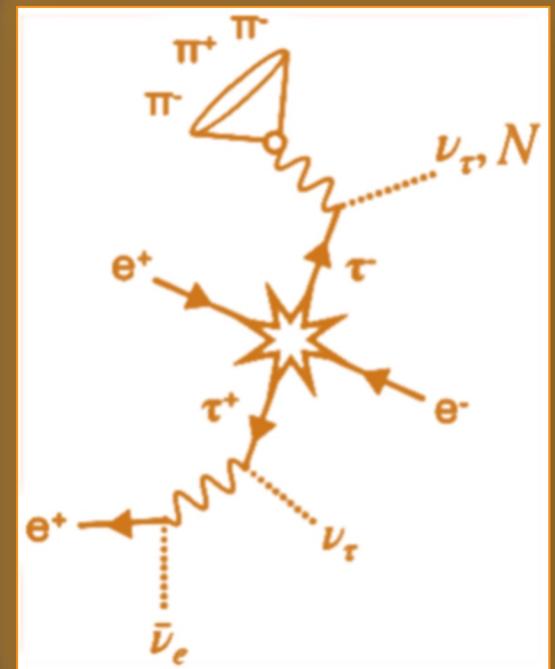
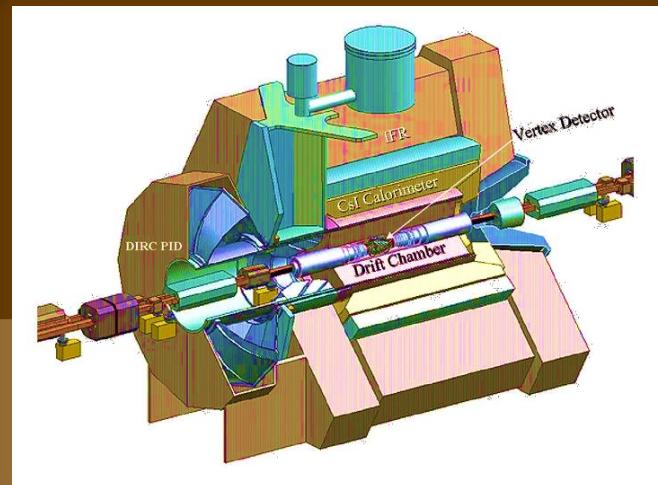
CHARM: Phys. Lett. B550 (2002) 8–15, [hep-ph/0208075].

NOMAD: Phys. Lett. B506 (2001) 27–38, [hep-ex/0101041].

DELPHI: Z. Phys. C74 (1997) 57–71.

Searching for HNLs at *BABAR*

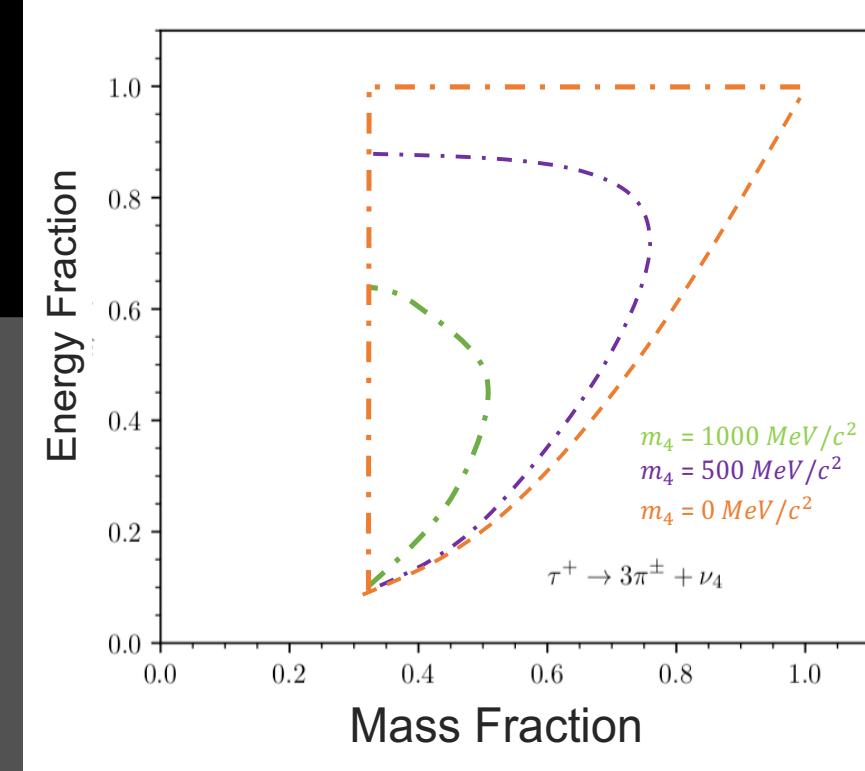
- ▶ For overview of experiment: Nucl. Instrum. Meth. A 729, 615 (2013).
- ▶ New analysis from *BABAR* – using the kinematics of hadronic tau decays:
 - ▶ $\sigma(e^+e^- \rightarrow \tau^+\tau^-) = 0.919 \pm 0.003 \text{ nb}$
 - ▶ Integrated luminosity in runs used = 424 fb^{-1}
=> $N_{\tau\tau} = 4.6 \times 10^8 \text{ events}$
- ▶ Strategy follows from proposal in Phys. Rev. D 91, 0530061135 based on ALEPH technique (Eur. Phys. J. 1137C 2, 395).
- ▶ Looks only at kinematics, no assumptions on underlying model, except that there must be some small mixing with tau sector.:
 1. “signal side” : three pronged pionic tau decay ($\tau^- \rightarrow \pi^-\pi^-\pi^+\nu_\tau$) as it allows access to region $100 < m_4 < 1360 \text{ MeV}/c^2$ where current limits are loose.
 2. “tag side” : Second tau decay must be leptonic, due to cleaner environment.



Method

Templates for each mass in the form of 2D plots of E_h .v. m_h . Boundary of curved region in this plot due to massive neutrino if present.

- ▶ Model 3-pronged decay as if it were 2-body with HNL and hadronic system as outgoing particles.
- ▶ Define E_h as energy and m_h as the invariant mass of the hadronic products.
- ▶ $E_\tau = \frac{E_{cms}}{2}$ in the limit of no ISR. The value of m_h can exist, in principle, in the range: $3m_{\pi^\pm} < m_h < m_\tau - m_{HNL}$. The range of E_h is



$$E_\tau - \sqrt{m_4^2 + q_+^2} < E_h < E_\tau - \sqrt{m_4^2 + q_-^2},$$

$$q_\pm = \frac{m_\tau}{2} \left(\frac{m_h^2 - m_\tau^2 - m_4^2}{m_\tau^2} \right) \sqrt{\frac{E_\tau^2}{m_\tau^2} - 1} \pm \frac{E_\tau}{2} \sqrt{\left(1 - \frac{(m_h + m_4)^2}{m_\tau^2}\right) \left(1 - \frac{(m_h - m_4)^2}{m_\tau^2}\right)};$$

SM Tau Decay

$$\frac{d\Gamma_{tot}(\tau^- \rightarrow \nu h^-)}{dm_h dE_h} = [(1 - |U_{\tau 4}|^2) \frac{d\Gamma(\tau^- \rightarrow \nu h^-)}{dm_h dE_h}]_{m_\nu=0} + |U_{\tau 4}|^2 \frac{d\Gamma(\tau^- \rightarrow \nu h^-)}{dm_h dE_h}]_{m_\nu=m_4}.$$

BSM Tau Decay

Backgrounds and Signal Simulations

- ▶ All SM neutrinos are assumed to have no mass, upper limit on heaviest mass neutrino is currently $< 18.2 \text{ MeV}/c^2$.i.e. \ll our search HNL masses.
- ▶ All backgrounds are subtracted using reconstructed Monte Carlo (MC).
- ▶ MCs passed through GEANT4 simulation of *BABAR* plus digitization and reconstruction modelling. Beam background and data filters are included.
- ▶ Four potential sources of events in data:
 - 1. SM 3 pronged decay to 3 charged pions ($\tau^- \rightarrow \pi^-\pi^-\pi^+\nu_\tau$) - (TAUOLA, KK2F)
 - 2. Other SM tau decays accidentally tagged as (1) - (TAUOLA, KK2F)
 - 3. SM non-tau backgrounds:
 - $e^+e^- \rightarrow \gamma(4S) \rightarrow B^+B^-$ and $e^+e^- \rightarrow \gamma(4S) \rightarrow B^0\bar{B}^0$ - (EvtGen)
 - $e^+e^- \rightarrow \bar{u}u, \bar{d}d, \bar{s}s$ and $e^+e^- \rightarrow \bar{c}c$ - (JETSET)
 - $e^+e^- \rightarrow \mu^+\mu^-(\gamma)$ - (KK2F)
 - 4. HNL : characterized by large missing mass (TAUOLA+KK2F – custom function, mass modified)

Backgrounds

{

Signal

{

TAUOLA: Comp. Phys. Co. 130, 260–325 (2000)

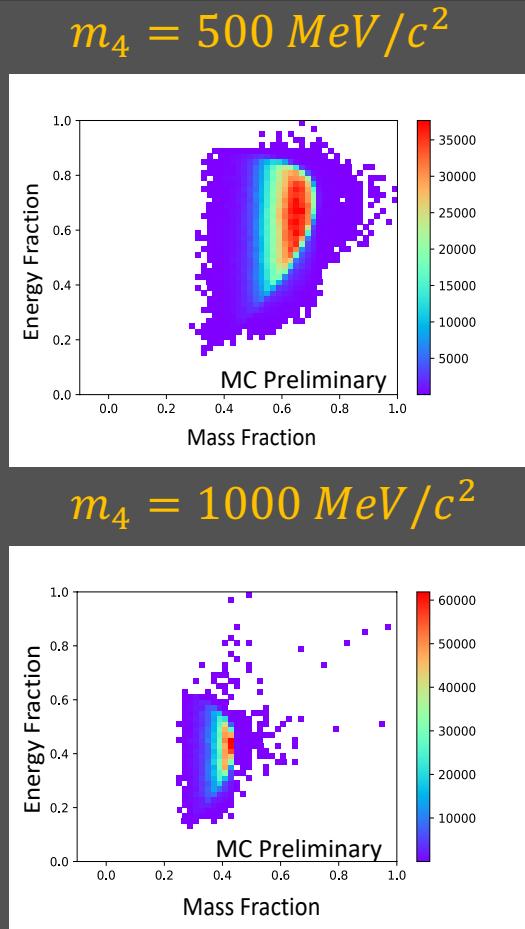
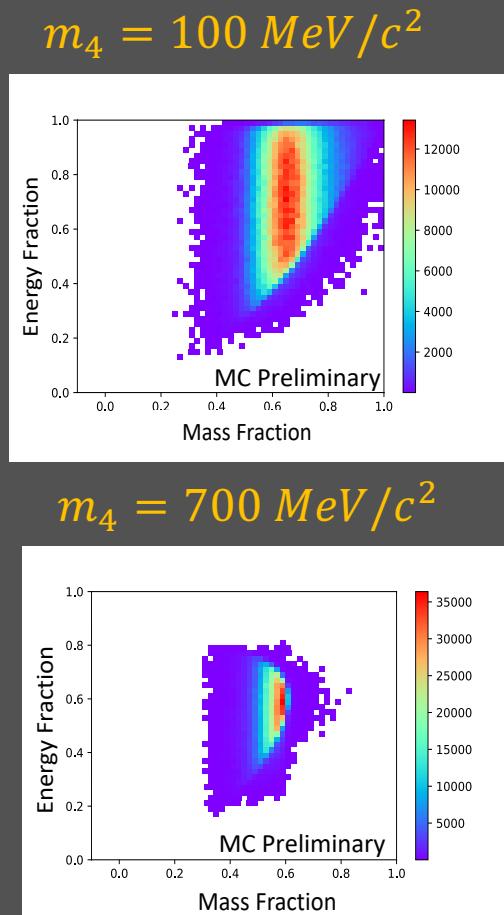
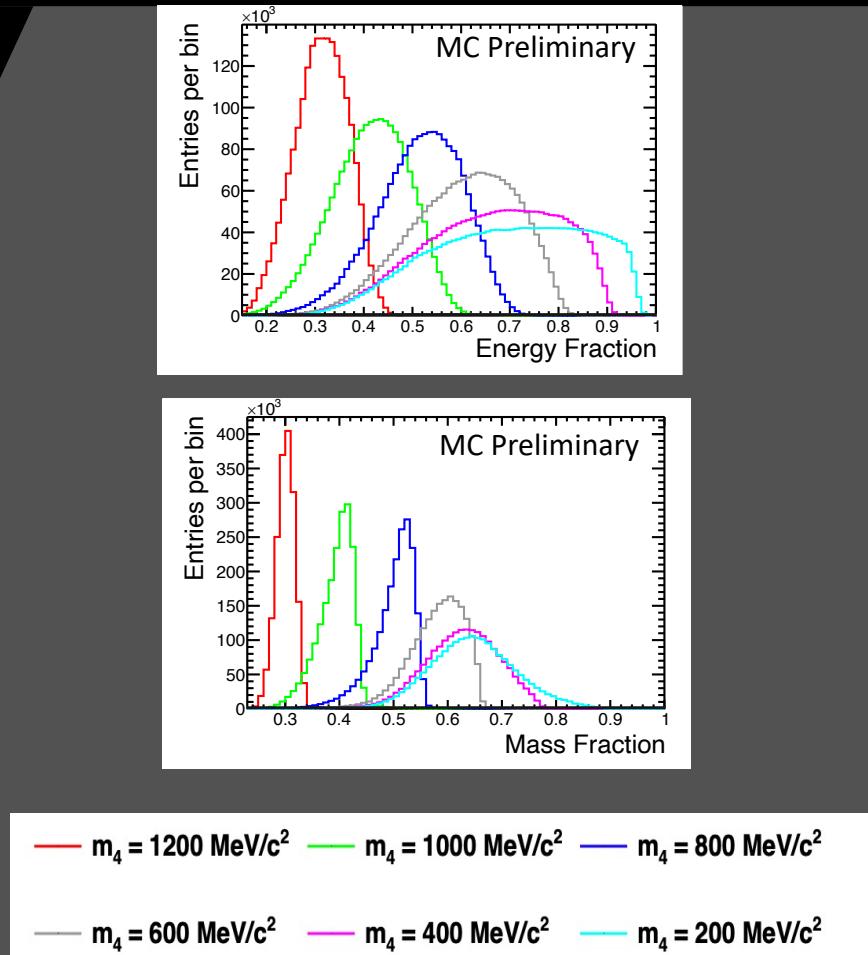
KK2F: Comp. Phys. Co. 64, 275 (1991)

EvetGen: Nucl. Instrum. Meth. A 462, 152 (2001)

JetSet: Comp. Phys. Co. 39, 347 (1986)

Signal Samples

- ▶ Plots illustrate in 1D projections and final 2D templates
- ▶ Show phase space changes with HNL mass
- ▶ Plots for leptonic (electron 1 prong + BSM 3-prong process).



Assume each bin (i, j) in 2D plots can be represented by a Poisson sampling function:

$$\mathcal{L} = \prod_{\text{charge}} \left(\prod_{\text{channel}} \left(\prod_{\text{bin}} \left(\prod_{\text{bin}} \left(\frac{1}{n_{\text{obs},ij}!} \left[N_{\tau,\text{gen}} \cdot |U_{\tau 4}|^2 \cdot p_{\text{HNL},ij} + N_{\tau,\text{gen}} \cdot (1 - |U_{\tau 4}|^2) \cdot p_{\tau-\text{SM},ij} + n_{BKG,ij}^{\text{reco}} \right]^{(n_{\text{obs}})_{ij}} \times \exp \left[- (N_{\tau,\text{gen}} \cdot |U_{\tau 4}|^2 \cdot p_{\text{HNL},ij} + N_{\tau,\text{gen}} \cdot (1 - |U_{\tau 4}|^2) \cdot p_{\tau-\text{SM},ij} + n_{BKG,ij}^{\text{reco}}) \right] \right)_{\text{bin}} \times \prod_k f(\theta_k, \hat{\theta}_k) \right)_{\text{channel}} \right)_{\text{charge}}$$

Number of generated taus:

$$N_{\tau,\text{gen}} = \mathcal{L} * \sigma * BR(3\pi) * BR(\text{lepton})$$

Find parameter of interest through minimizing ratio:

$$q = -2\ln \left(\frac{\mathcal{L}_{H_0}(|U_{\tau 4}|_0^2; \hat{\theta}_0, \text{data})}{\mathcal{L}_{H_1}(|\hat{U}_{\tau 4}|^2; \hat{\theta}, \text{data})} \right) = -2\ln(\Delta \mathcal{L}).$$

Where n_{ij} is content of a given bin in 2D template, N and M are number of bins on each direction (=50)

Selection Criteria

Signature:

$$e^+e^- \rightarrow \tau^+\tau^- \text{ followed by } \tau^\pm \rightarrow l^\pm\nu_l \text{ & } \tau^\mp \rightarrow \pi^\mp\pi^\mp\pi^\pm\nu_{HNL}?$$

- ▶ Set of criteria enforced to improve signal selection and remove problematic backgrounds:

Cut	Purpose
Number of tracks	Ensure 1+3 prong topology
Total charge on all 4 charged tracks is 0	Charge conservation
$p_{CM}^{miss} > 0.9\% \sqrt{s}$	Suppresses non-tau backgrounds
All tracks: $p_{trans} > 250\text{MeV}/c$	To reach DIRC ¹
All tracks: $-0.76 < \cos(\theta) < 0.9$	Acceptance of DIRC ¹
1 prong: $\frac{2p}{E} < 0.9\%$	Consistent with tau decay
PID Requirements	Uses Electron and Muon ID algorithms

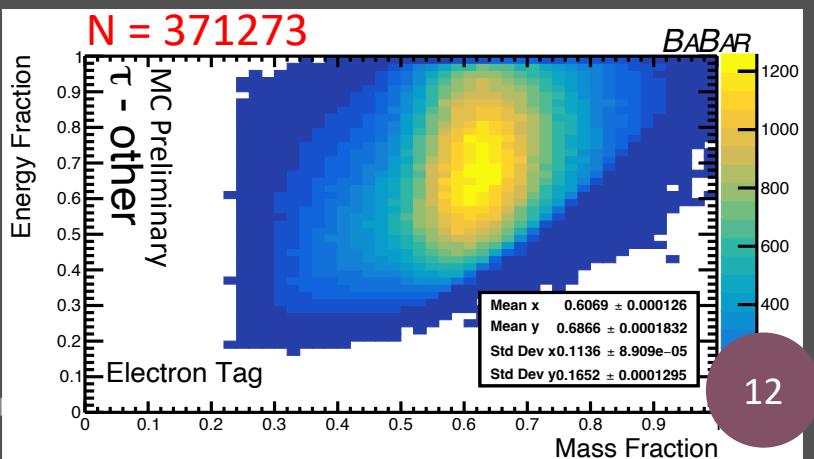
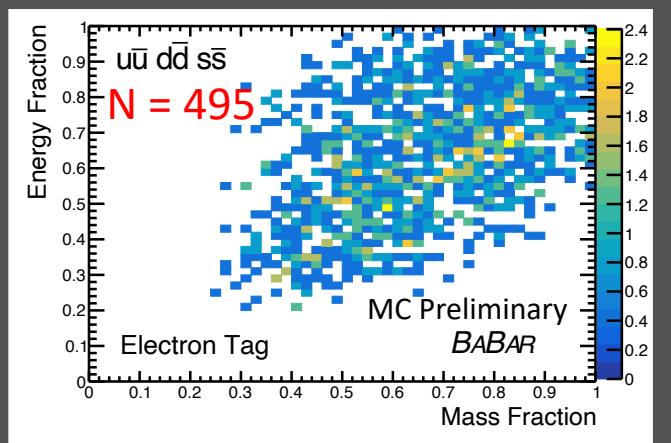
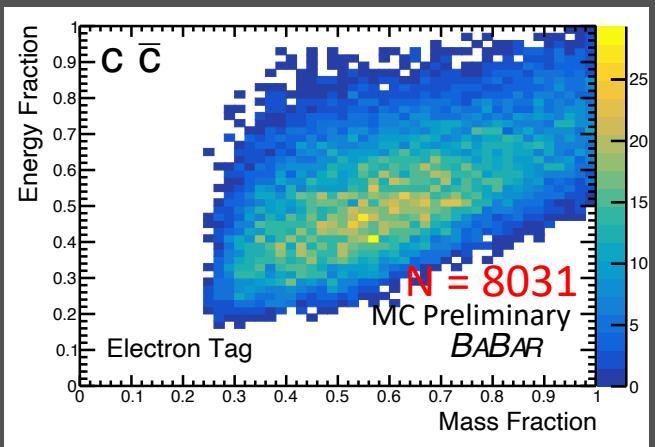
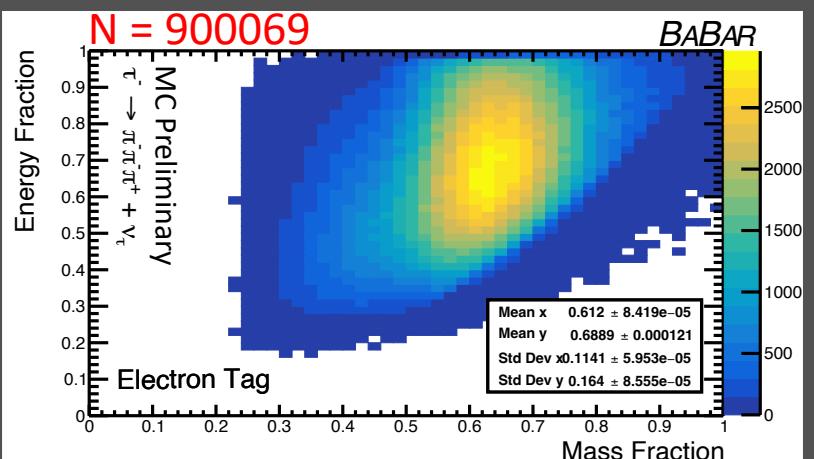
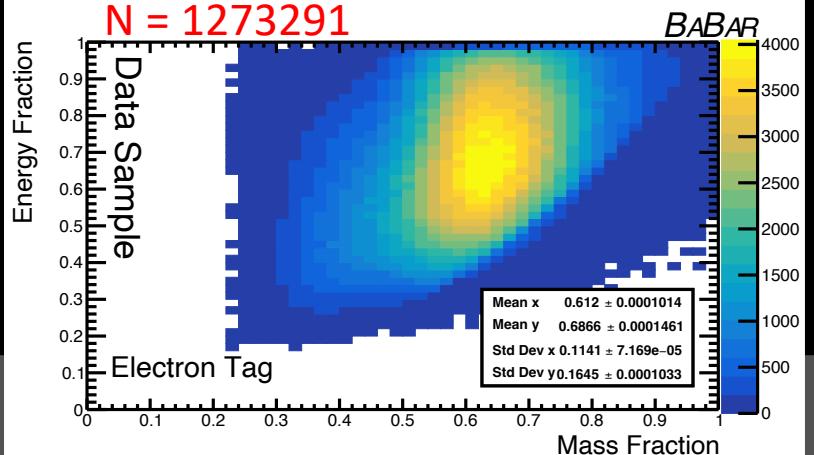
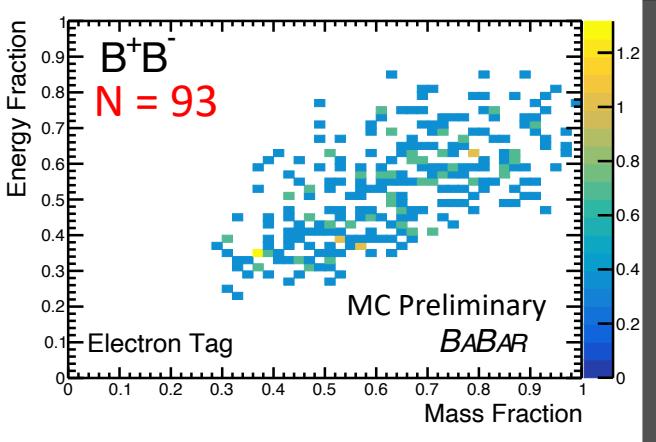
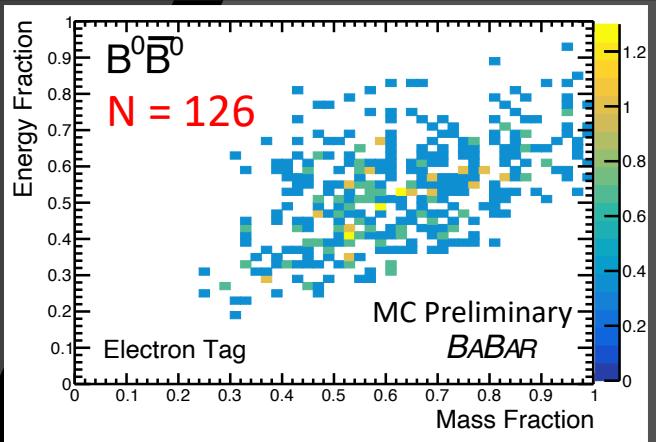
¹ Detection of Internally Reflected Cherenkov light = **BABAR** PID Detector System

Example 2D Plots

Data Total = 1273291, MC Total = 1283654

Plots for
Sig = Neg. 3 prong
Tag = Pos. electron

Discrepancy in TAUOLA
modelling discussed later

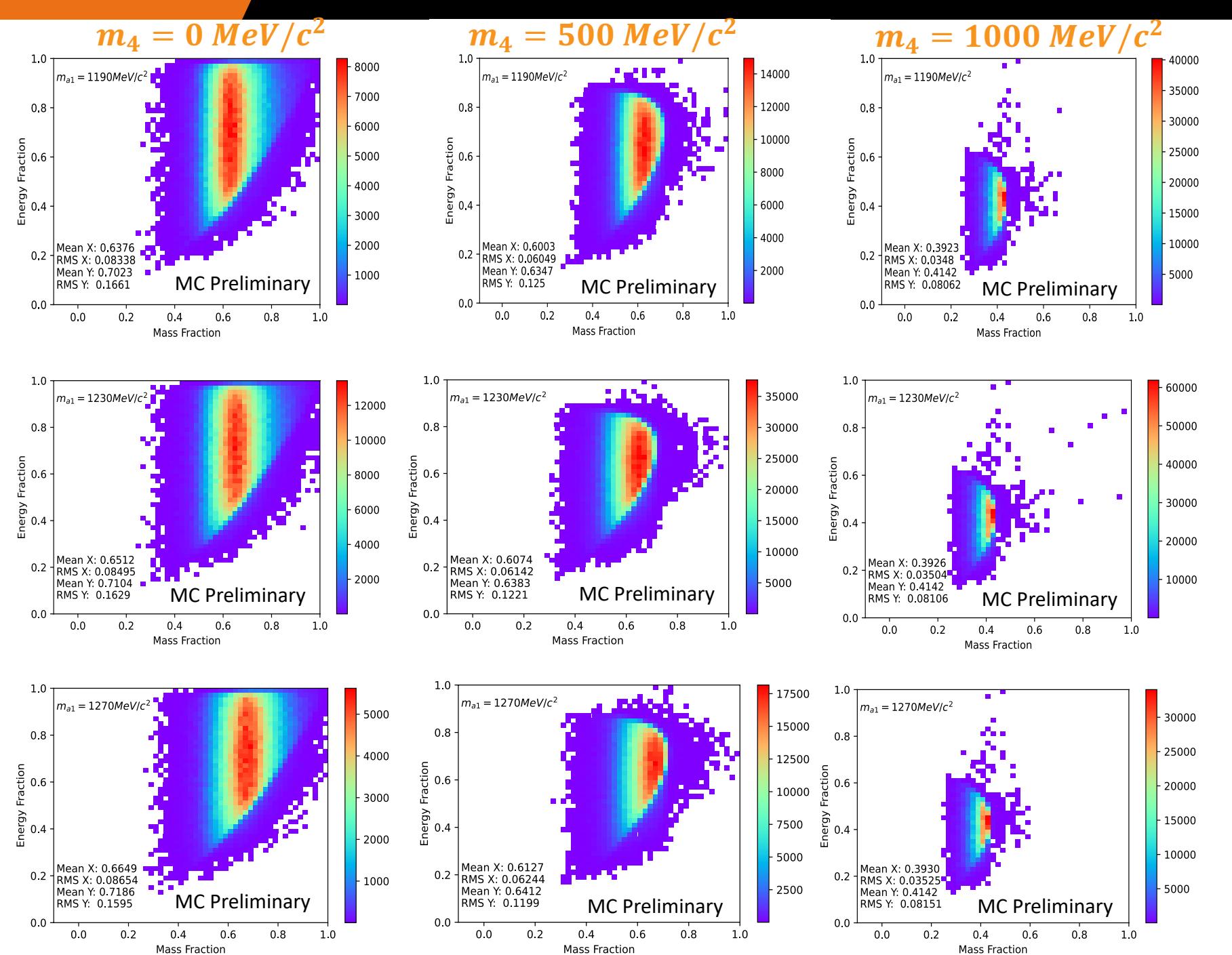


Normalization Uncertainties

- ▶ Normalization uncertainties effect all bins uniformly.
- ▶ Have small effect on overall yield.
- ▶ They will be characterized as Gaussian nuisance parameters in the likelihood.

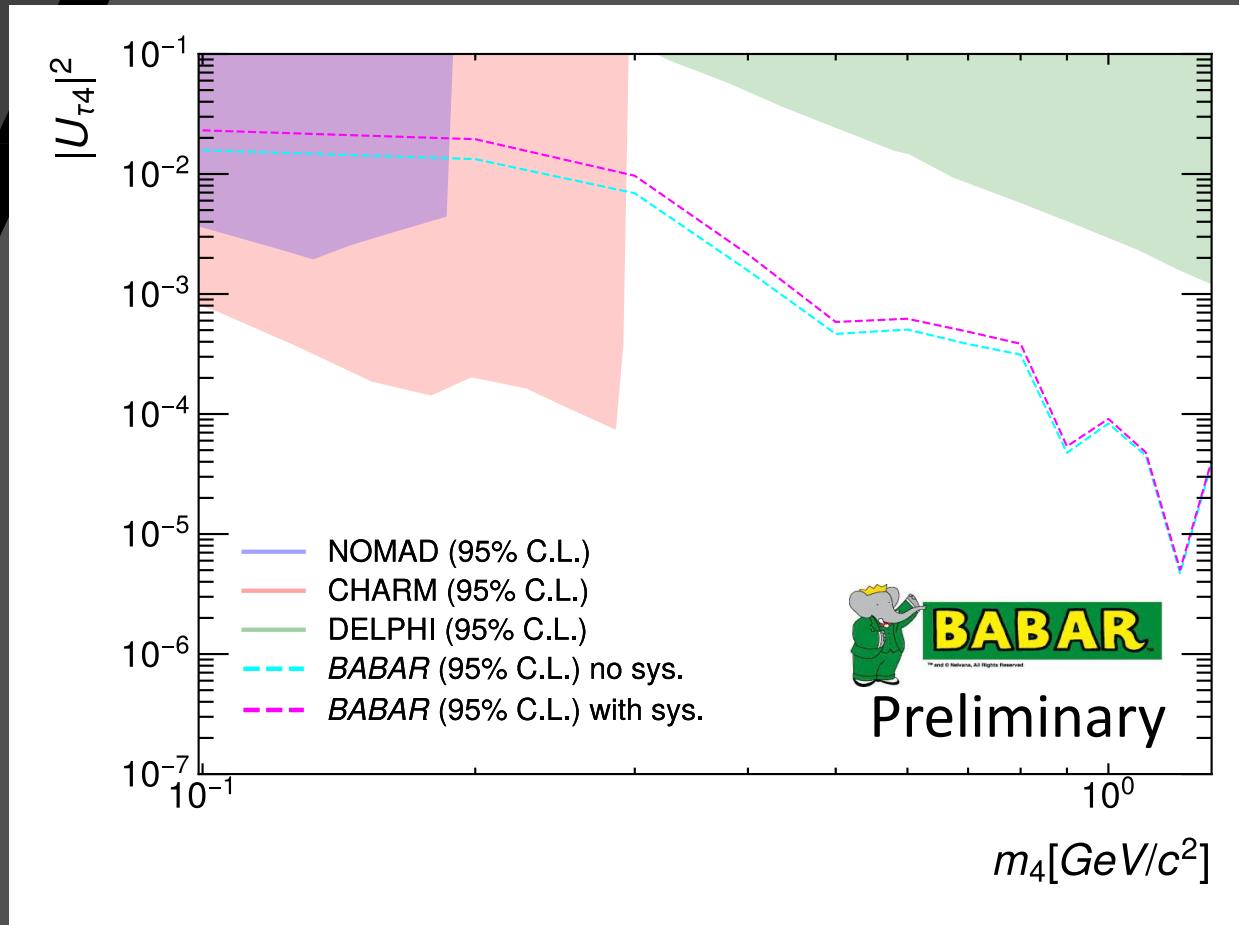
Uncertainty	Contribution
Luminosity	0.44 % [BaBar]
Cross-section	0.31% [Data]
Branching fraction of 1-prong tau decays	Electron : 0.23 % [PDG] Muon: 0.23% [PDG]
Branching fraction of 3-prong tau decays	3 pions : 0.57 % [PDG]
PID Efficiency	Electron : 2 % [BaBar] Muons : 1 % Pions : 3 %
$q\bar{q}$ and Bhabha Contamination	0.3 % [Control region analysis]
Bin Size	< 1% [Alter bins, check results]
Tracking Efficiency	N/A
Detector Modelling	N/A
Tau Mass uncertainty	N/A
Tau Energy	N/A

Systematic Shape Uncertainties



- ▶ Dominant shape systematic from modelling of the hadronic tau decays in TAUOLA
- ▶ $\tau^- \rightarrow \pi^- \pi^- \pi^+ \nu_\tau$ is mediated by the a_1 resonance 97% of the time.
- ▶ $m_{a_1} = 1230 \pm 40 \text{ MeV}/c^2$ and $\Gamma_{a_1} = 420 \pm 35 \text{ MeV}/c^2$ (PDG estimates 250 – 600 MeV/c²)

Searching for HNLs at *BABAR*



- Binned profile likelihood approach used to find 95% C.L. on $|U_{\tau 4}|^2$.
- Considers both lepton tags and + and - signal tau channels.
- Provides new upper limits for HNLs mixing with taus in range $400 < |U_{\tau 4}|^2 < 1300 \text{ MeV}/c^2$

Summary & Outlook

- ▶ HNLs offer ways of explaining several observational phenomena.
- ▶ The possible masses of the HNLs is model dependent and can range from eV/c^2 up to very heavy masses.
- ▶ In the last few years several new results have been published including results from collider-based experiments and neutrino experiments.
- ▶ This talk has given details on the newest analysis from **BABAR** which presents new upper limits on $|U_{\tau 4}|^2$ at 95 % C.L. between $100 \text{ MeV}/c^2 - 1300 \text{ MeV}/c^2$:
 - ▶ Competitive with projections for experiment results expected in coming decade.
 - ▶ New technique can be applied to data from other experiments e.g. Belle-II.
 - ▶ Expect publication in next few weeks.

Useful Resources for Additional Reading

- ▶ J. Beacham et al., Journal of Physics G: Nuc. and Part. Phys. 47, 010501 (2019).
- ▶ A. M. Abdullahi et al., in 2022 Snowmass Summer Study (2022) arXiv:2203.08039 [hep-ph].
- ▶ R. N. Mohapatra and G. Senjanovic, Phys. Rev. D 23, 165 (1981)
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- ▶ A. Palazzo, Mod. Phys. Lett. A 28, 1330004 (2013).
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- ▶ A. V. Artamonov et al. (E949 Collaboration), Phys. Rev. D 91, 052001 (2015).
- ▶ M. Aoki et al. (PIENU Collaboration), Phys. Rev. D 84 052002 (2011).

Back up Slides

Neutrino Oscillations

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

- ▶ Neutrino oscillations are only experimentally verified physics beyond the SM. Imply at least two of the neutrino states must have non-zero mass.
- ▶ Mixing parameterized using the PMNS matrix.
- ▶ Measurements of neutrino compositions at accelerators, reactors and underground facilities have provided measurements of the three Euler angles parametrizing the PMNS matrix and Δm_{21}^{-2} and Δm_{32}^{-2}

But many unanswered questions in neutrino physics, including:

- ▶ Why is neutrino mixing so different from quark mixing?
- ▶ Why is neutrino mass so small? What are the origins of this mass?
- ▶ **See-saw models:** if neutrinos get their mass from the Higgs, Yukawa couplings are small, why? Can add dim-5 operator and additional neutrinos (Majorana) within see saw models to also account for neutrino mass.
[PhysRevD.23.165, https://doi.org/10.3389/fphy.2018.00040.](https://doi.org/10.3389/fphy.2018.00040)

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta_{CP}} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta_{CP}} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} P$$

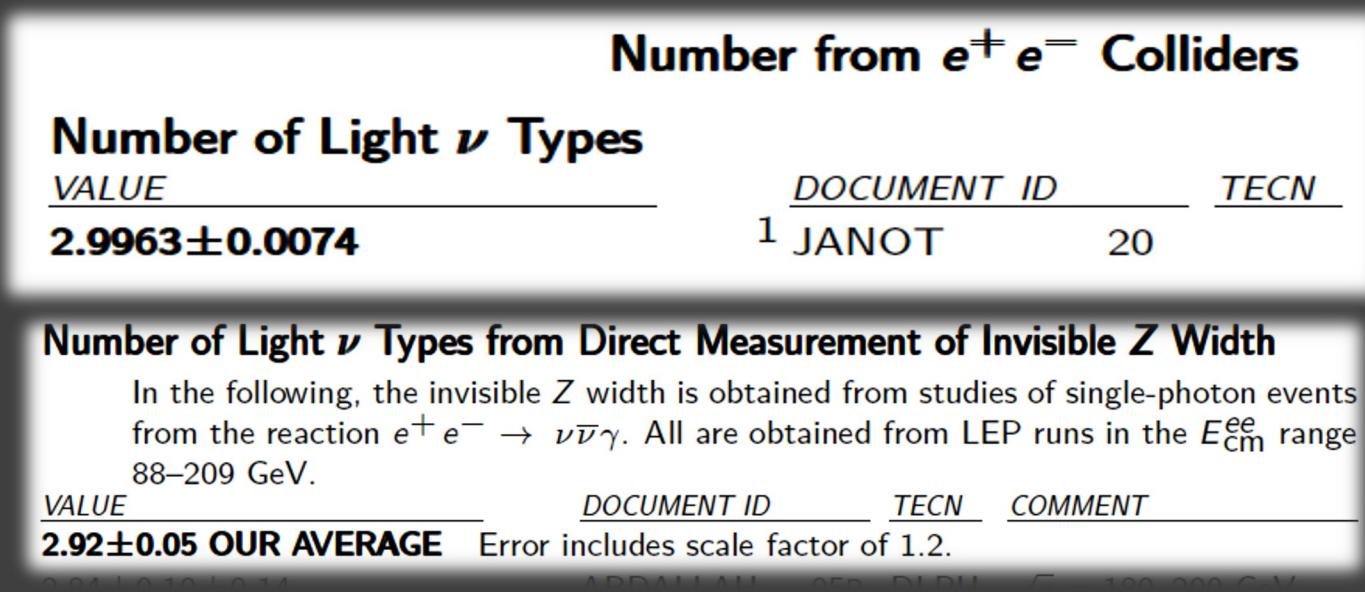
Event Yields

Bkg. Type	Electron Tag MC Yield	[%]	Muon Tag MC Yield	[%]
$\tau^+ \rightarrow \pi^+ \pi^+ \pi^- \bar{\nu}_\tau$	894864	70	810586	71
$\tau^+ \rightarrow \pi^+ \pi^+ \pi^- \pi^0 \bar{\nu}_\tau$	332008	26	278830	24
$\tau^+ \rightarrow \pi^+ \pi^+ \pi^- 2\pi^0 \bar{\nu}_\tau$	34050	2.7	28841	2.5
$\tau^+ \rightarrow 2\pi^\pm K^\pm \bar{\nu}_\tau$	3391	0.27	3101	0.27
$\tau^+ \rightarrow \pi^+ \pi^+ \pi^- 3\pi^0 \bar{\nu}_\tau$	1541	0.12	821	0.07
$\tau^+ \rightarrow \pi^\pm \pi^0 \bar{\nu}_\tau$	498	0.039	207	0.017
$\tau^+ \rightarrow \pi^\pm 2\pi^0 \bar{\nu}_\tau$	252	0.02	92	0.27
$\tau^+ \rightarrow 2K^\pm \pi^\pm \bar{\nu}_\tau$	207	0.016	146	0.013
$e^+ e^- \rightarrow Y(4S) \rightarrow c\bar{c}$	8031	0.63	6512	0.55
$e^+ e^- \rightarrow Y(4S) \rightarrow u\bar{u}, s\bar{s}, d\bar{d}$	542	0.043	13898	1.19
$e^+ e^- \rightarrow Y(4S) \rightarrow B^0 \bar{B}^0$	108	0.009	99	0.0084
$e^+ e^- \rightarrow Y(4S) \rightarrow B^+ B^-$	100	0.008	89	0.0076
$e^+ e^- \rightarrow \mu^+ \mu^-$	0	0	15	0.0013
Total MC	1278339	-	1143237	-
Data	1265698	-	1137521	-

Bkg. Type	Electron Tag MC Yield	[%]	Muon Tag MC Yield	[%]
$\tau^- \rightarrow \pi^- \pi^- \pi^+ \nu_\tau$	900069	70	817342	70
$\tau^- \rightarrow \pi^- \pi^- \pi^+ \pi^0 \nu_\tau$	334565	26	281613	25
$\tau^- \rightarrow \pi^- \pi^- \pi^+ 2\pi^0 \nu_\tau$	34255	2.7	29287	2.5
$\tau^- \rightarrow 2\pi^\pm K^\pm \nu_\tau$	3567	0.27	3228	0.27
$\tau^- \rightarrow \pi^- \pi^- \pi^+ 3\pi^0 \nu_\tau$	1535	0.12	795	0.07
$\tau^- \rightarrow \pi^\pm \pi^0 \nu_\tau$	476	0.039	217	0.019
$\tau^- \rightarrow \pi^\pm 2\pi^0 \nu_\tau$	240	0.02	92	0.08
$\tau^- \rightarrow 2K^\pm \pi^\pm \nu_\tau$	202	0.016	152	0.013
$e^+ e^- \rightarrow Y(4S) \rightarrow c\bar{c}$	8031	0.63	6837	0.58
$e^+ e^- \rightarrow Y(4S) \rightarrow u\bar{u}, s\bar{s}, d\bar{d}$	495	0.043	16602	1.42
$e^+ e^- \rightarrow Y(4S) \rightarrow B^0 \bar{B}^0$	126	0.009	98	0.0083
$e^+ e^- \rightarrow Y(4S) \rightarrow B^+ B^-$	93	0.008	103	0.0088
$e^+ e^- \rightarrow \mu^+ \mu^-$	0	0	10	0.0009
Total MC	1283654	-	1155920	-
Data	1273291	-	1150350	-

Possible Flavor of Additional Neutrinos

- ▶ Experimental data from Z decays and cosmology favors “3 lepton flavors.”
- ▶ Additional neutrinos in the mass range explored must be “sterile”



Zyla et al. (Particle Data Group), Prog. Theor. Exp. Phys. 2020, 083C01 (2020)

