

# A last chance for kinetic mixing: explaining $(g-2)_\mu$ with semi-visible dark photons

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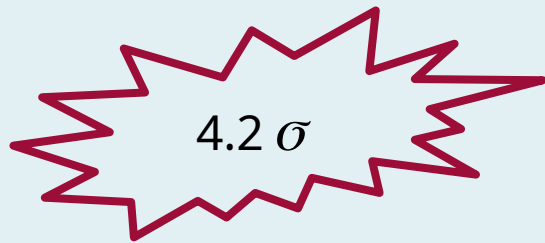
ALMA MATER STUDIORUM  
UNIVERSITÀ DI BOLOGNA



# FNAL measurement

FNAL confirmed  $(g-2)_\mu$  discrepancy with SM

$$\Delta a_\mu = a_\mu^{\text{EXP}} - a_\mu^{\text{SM}} = (251 \pm 59) \times 10^{-11}$$

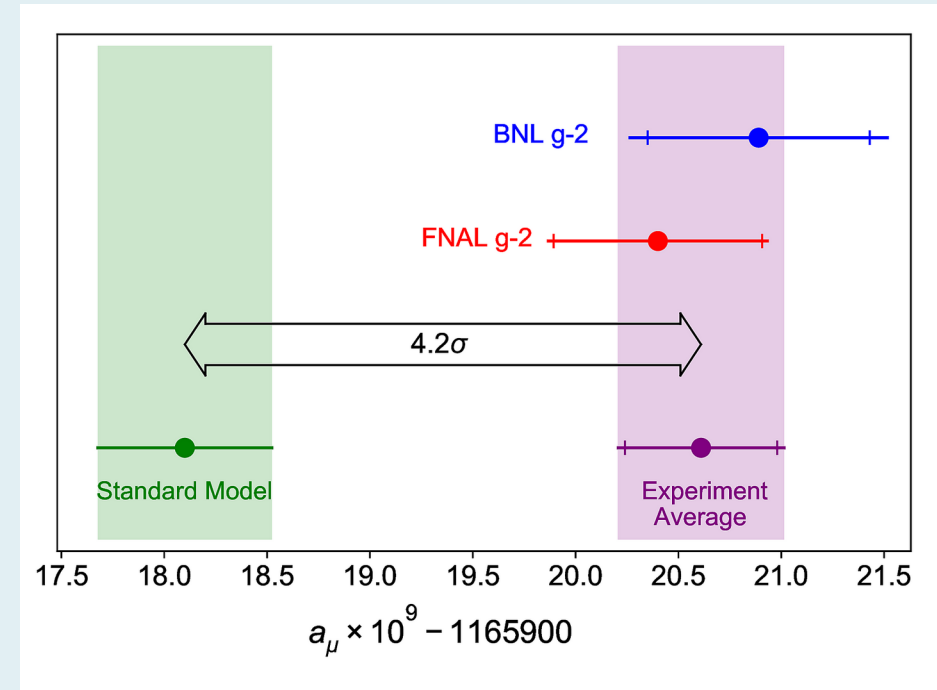


**Hints for new physics?**

Not too far out of reach

$$\Delta a_\mu \propto \frac{g^2}{16\pi^2} \frac{m_\mu^2}{\Lambda^2} \Rightarrow \frac{\Lambda}{g} \approx \mathcal{O}(10^2) \text{ GeV}$$

\*Recent comparison of Lattice Results for Leading Order Hadron Vacuum Polarization would reduce the significance to 2.9  $\sigma$ . [Cè et al. (2022), arXiv:2206.06582]



[B. Abi et al. Phys. Rev. Lett. 126.14 (2021), p. 141801]

# Dark photon as a solution

$$\mathcal{L} \supset \frac{\varepsilon}{2} B^{\mu\nu} X_{\mu\nu}$$

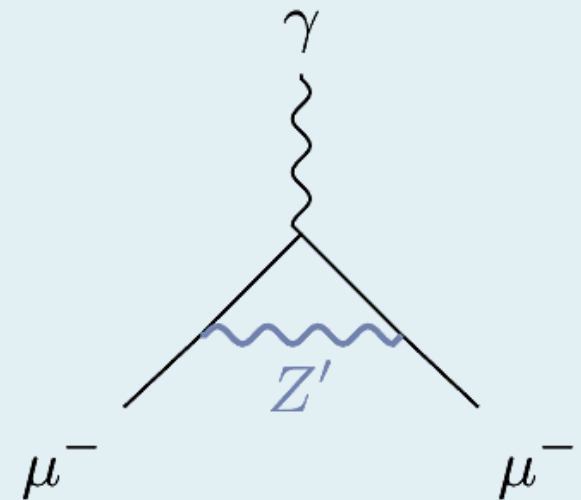
New  $U(1)'$  gauge group with vector boson  $Z'$ , kinetically mixed to  $U(1)_Y$  gauge boson

**Positive contribution to  $a_\mu$**

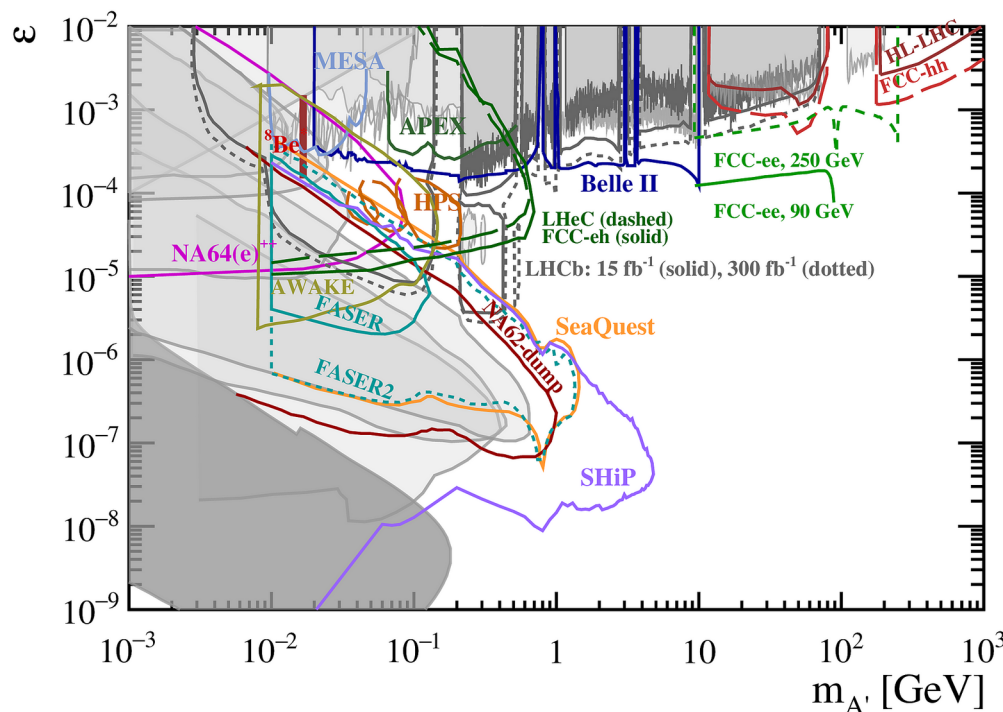
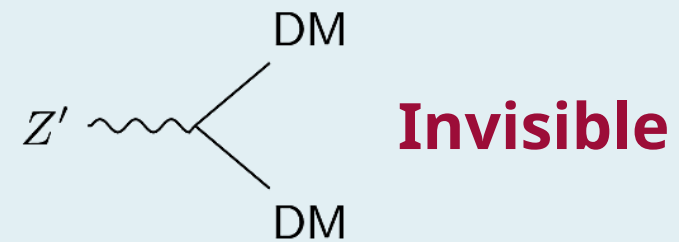
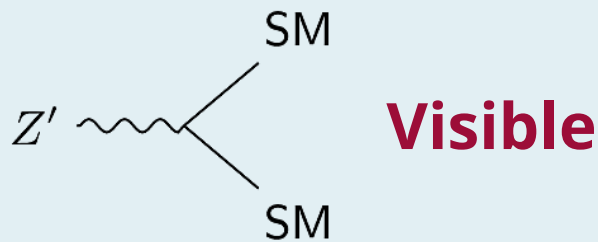
$$\Delta a_\mu = \frac{\alpha}{2\pi} \varepsilon^2 \int_0^1 dz \frac{2m_\mu^2 z(1-z)^2}{m_\mu^2(1-z)^2 + m_{Z'}^2 z}$$

[M. Pospelov. Phys. Rev. D 80 (2009), p. 095002]

Detection: decay modes in minimal models

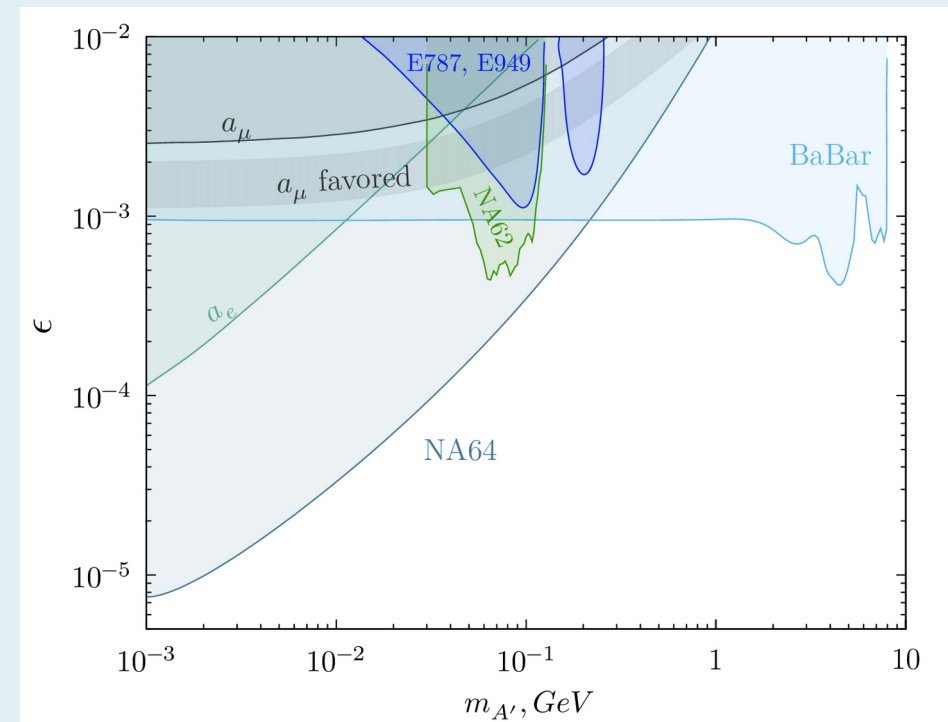


# Dark photon decay modes



[M. Fabbrichesi et al. (2020). arXiv: 2005.01515]

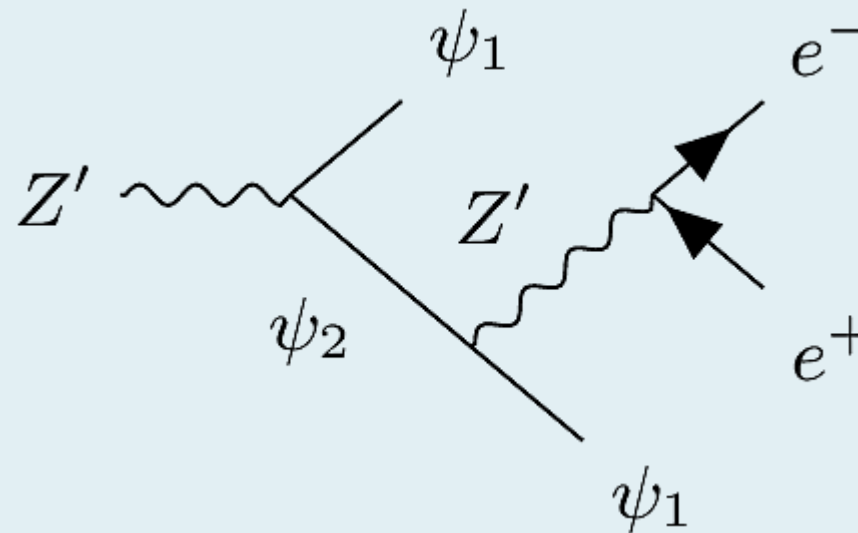
Visible decays in SM final states are **excluded** by colliders in resonance searches



[D. Banerjee et al. Phys. Rev. Lett. 123.12 (2019), p. 121801]

Invisible decays **fully excluded** by BaBar and NA64

# Semi-visible to the rescue



[E. Izaguirre et al. Phys. Rev. D 96.5 (2017), p. 055007]

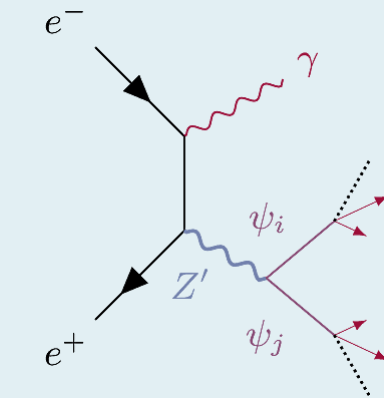
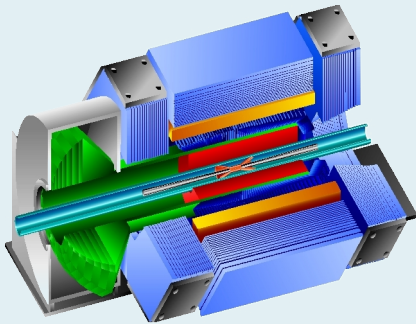
[G. Mohlabeng. Phys. Rev. D 99.11 (2019), p. 115001]

## Potential solution

- Evade visible constraints with **missing energy**
- Evade invisible constraints with **visible final states**

# Main constraints

## BaBar monophoton



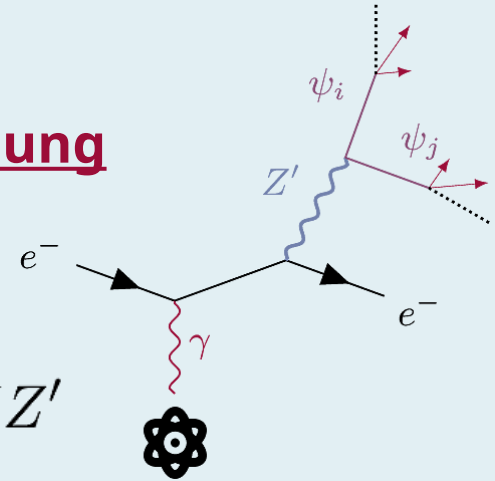
$$e^+e^- \rightarrow \gamma Z'$$

Monophoton + missing energy

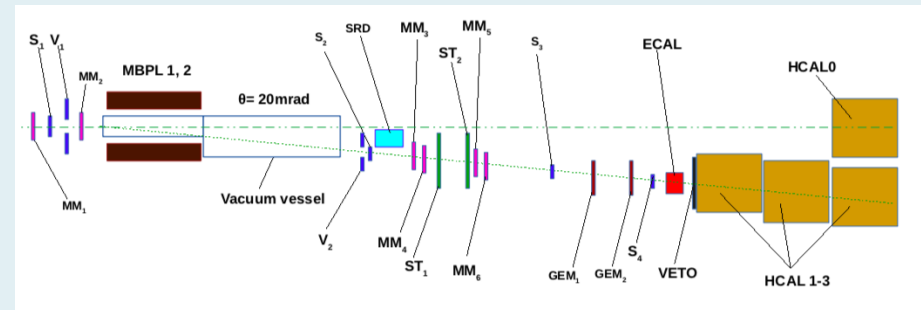
### Are semi-visible $Z'$ viable?

- ☑ Simulate production of semi-visible  $Z'$  in BaBar and NA64 detector
- ☑ Apply selection criteria
- ☑ Recast the bound

## NA64 $Z'$ bremsstrahlung



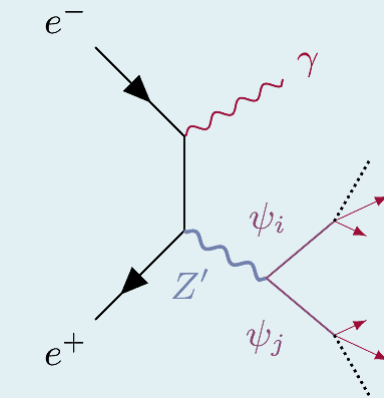
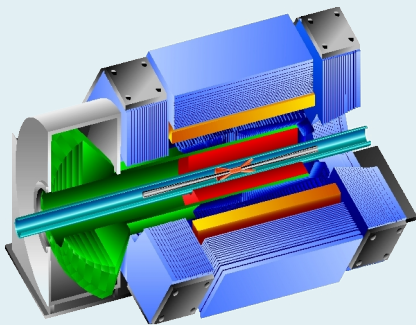
$$e^- N \rightarrow e^- N Z'$$



Missing energy events with dark photon produced in electron bremsstrahlung

# Main constraints

## BaBar monophoton



$$e^+e^- \rightarrow \gamma Z'$$

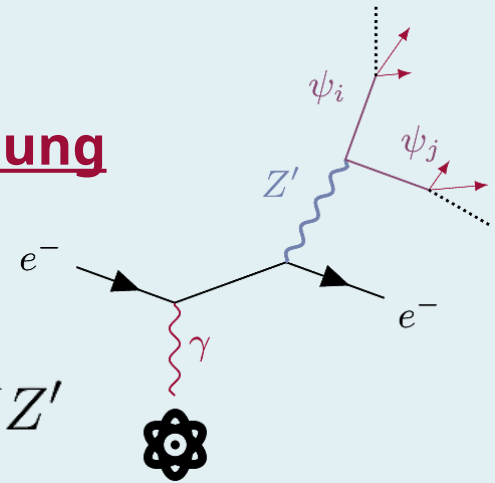
Monophoton + missing energy

### Are semi-visible $Z'$ viable?

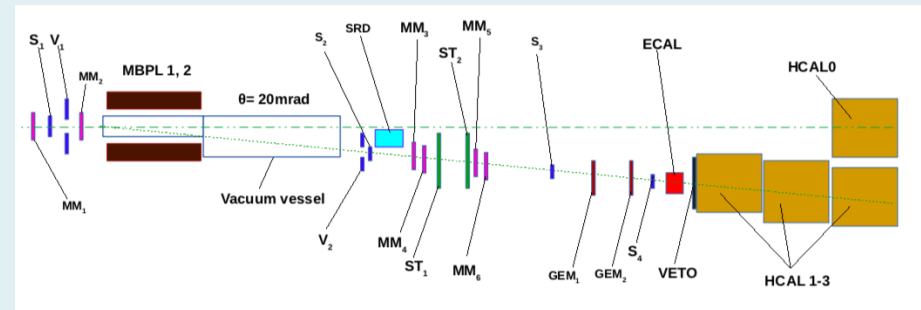
- ☑ Simulate production of semi-visible  $Z'$  in BaBar and NA64 detector
- ☑ Apply selection criteria
- ☑ Recast the bound

$$\varepsilon_{\text{bound}} = \varepsilon_{\text{new}} \sqrt{P^{\text{inv}}(\varepsilon_{\text{new}}, m_{Z'})}$$

## NA64 $Z'$ bremsstrahlung



$$e^- N \rightarrow e^- N Z'$$



Missing energy events with dark photon produced in electron bremsstrahlung

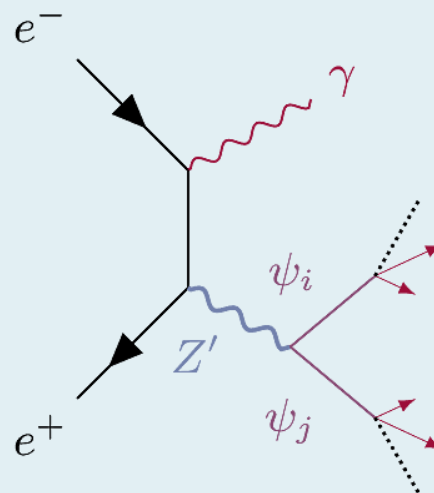
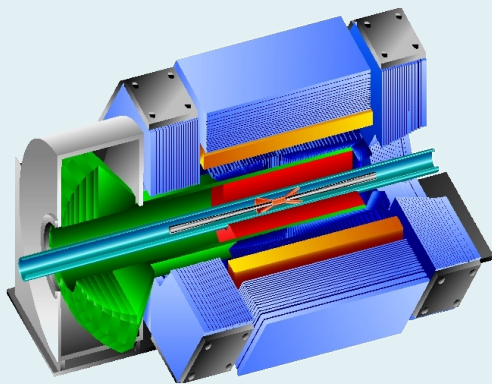
# The BaBar simulation: generation

**Process:**  $e^+e^- \rightarrow \gamma Z'$

- ✓ Generate  $O(10^6)$  events for given  $m_{Z'}$  and  $\varepsilon$
- ✓ Apply primary selection cut on monophoton CM angle
- ✓ Apply veto criteria and compute new  $P^{\text{inv}}$

$Z'$  decays instantly to HNL, producing pairs of leptons final states:

$$Z' \rightarrow (\psi_i \rightarrow (\psi_k \rightarrow \dots) e^+ e^-) (\psi_j \rightarrow (\psi_l \rightarrow \dots) e^+ e^-)$$



Events containing visible final states are vetoed



# The NA64 simulation: generation

**Process:**  $e^- N \rightarrow e^- N Z'$

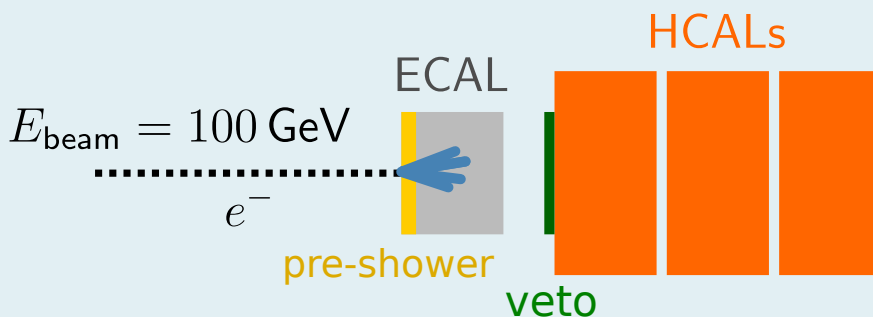
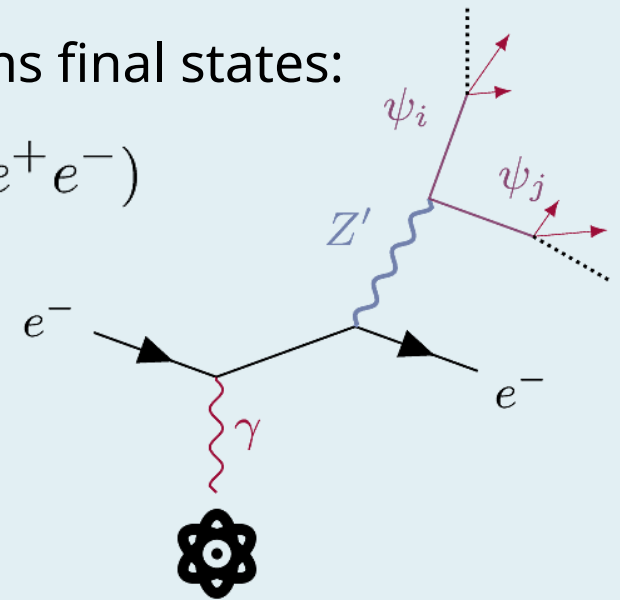
- ☑ Generate  $O(10^5)$  events for given  $m_{Z'}$  and  $\varepsilon$
- ☑ Apply veto criteria and compute new  $P^{\text{inv}}$

$Z'$  decays instantly to HNL, producing pairs of leptons final states:

$$Z' \rightarrow (\psi_i \rightarrow \psi_k e^+ e^-) (\psi_j \rightarrow \psi_l e^+ e^-)$$

**Recast:** solve  $\varepsilon_{\text{NA64}} = \varepsilon \sqrt{P^{\text{inv}}(\varepsilon, m_{Z'})}$

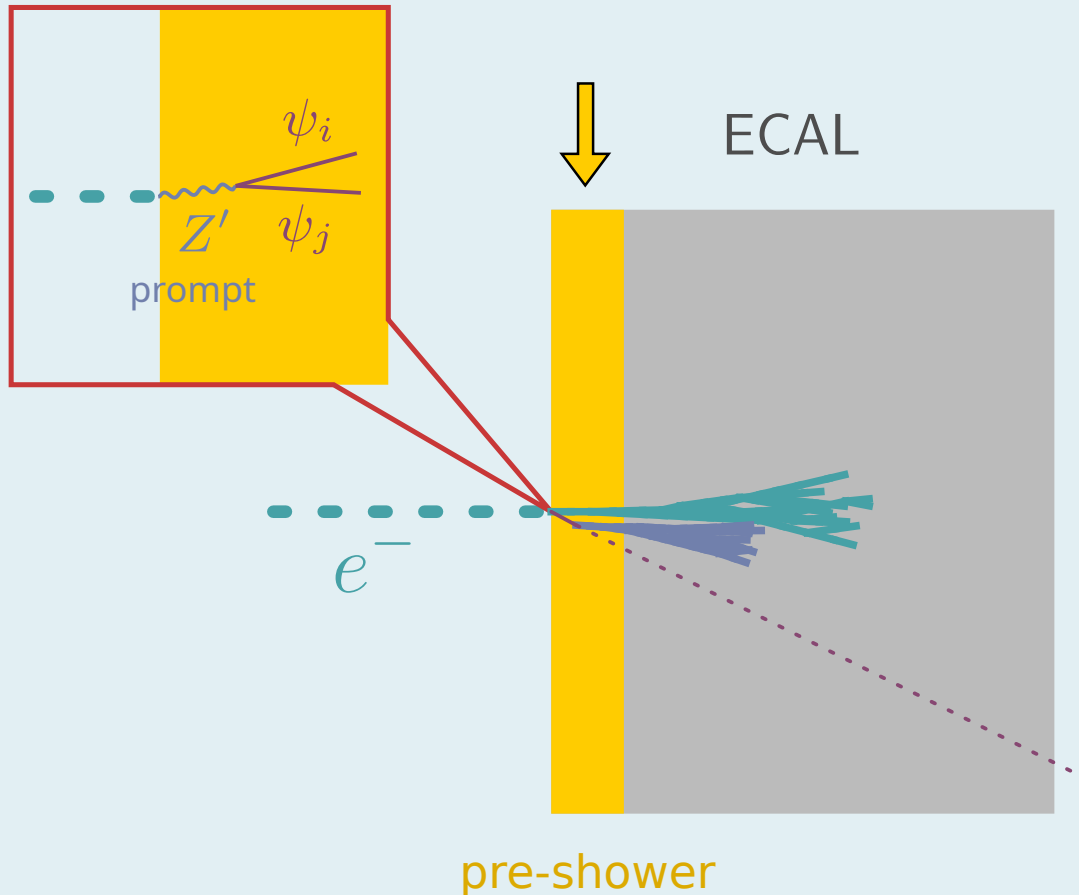
$$\text{where } P^{\text{inv}}(\varepsilon, m_{Z'}) = 1 - \frac{N_{\text{veto}}(\varepsilon, m_{Z'})}{N(\varepsilon, m_{Z'})}$$



$e^+ e^-$  pairs deposit energy in the calorimeters or in the veto, so new events are vetoed according cut conditions.

# Recast of the “invisible” bound

[Phys. Rev. Lett. 123.12 (2019), p. 121801]



✓ Pre-shower ECAL

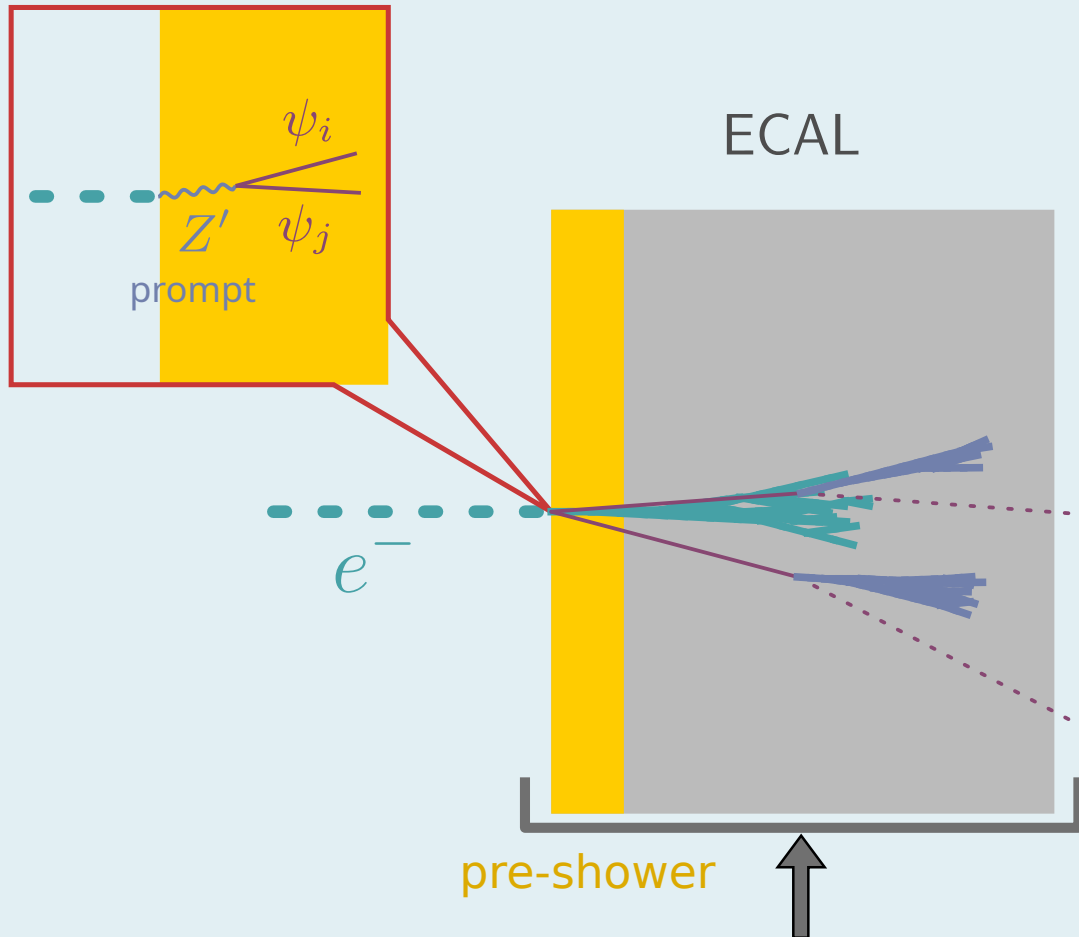
$$E_{\text{tot}} \notin [0.5, 10] \text{ GeV}$$

## Assumptions:

- $e^+e^-$  sufficiently overlapped: sum energies;
- Everything is forward: neglect *leakage* of particles from detector.

# Recast of the “invisible” bound

[Phys. Rev. Lett. 123.12 (2019), p. 121801]



✓ Pre-shower ECAL

$$E_{\text{tot}} \notin [0.5, 10] \text{ GeV}$$

✓ ECAL

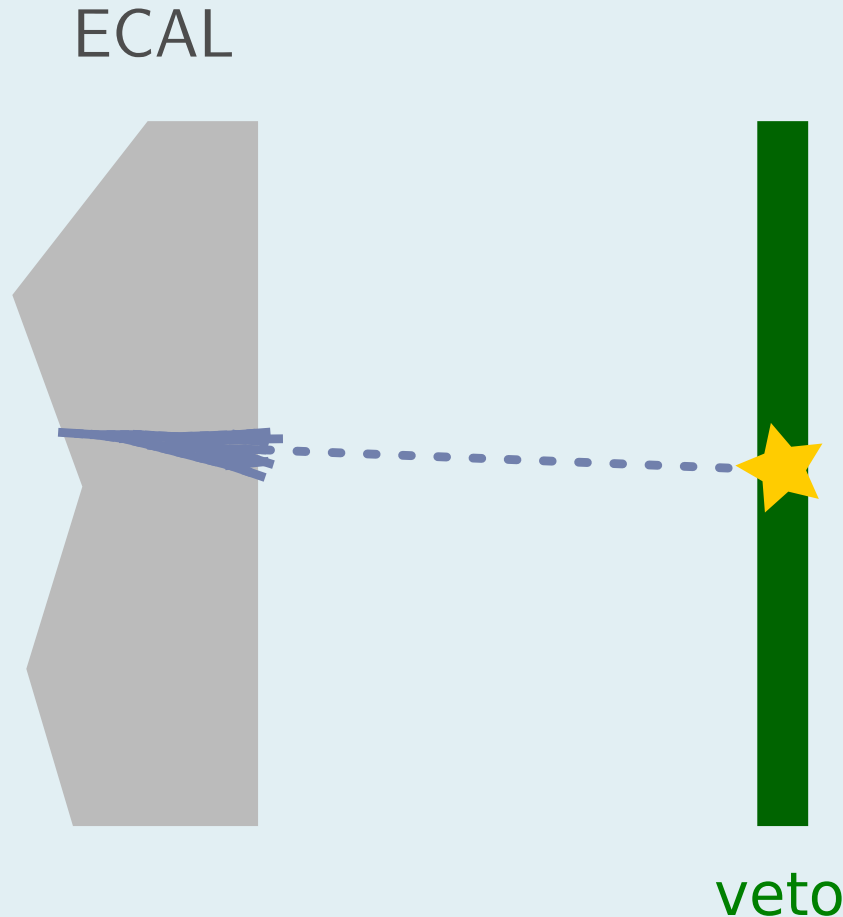
$$E_{\text{tot}} > 50 \text{ GeV}$$

## Assumptions:

- $e^+e^-$  sufficiently overlapped: sum energies;
- Everything is forward: neglect *leakage* of particles from detector.

# Recast of the “invisible” bound

[Phys. Rev. Lett. 123.12 (2019), p. 121801]



✓ Pre-shower ECAL

$$E_{\text{tot}} \notin [0.5, 10] \text{ GeV}$$

✓ ECAL

$$E_{\text{tot}} > 50 \text{ GeV}$$

✓ Veto

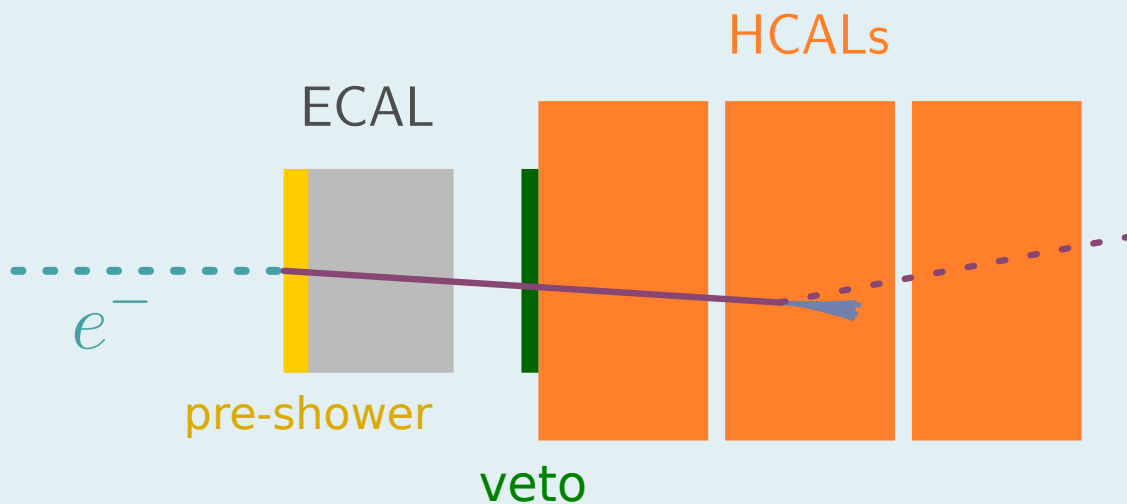
$$E_{\pm}(x_{\text{veto}}) > 10 \text{ MeV}$$

## Assumptions:

- $e^+e^-$  sufficiently overlapped: sum energies;
- Everything is forward: neglect *leakage* of particles from detector.

# Recast of the “invisible” bound

[Phys. Rev. Lett. 123.12 (2019), p. 121801]



✓ Pre-shower ECAL

$$E_{\text{tot}} \notin [0.5, 10] \text{ GeV}$$

✓ ECAL

$$E_{\text{tot}} > 50 \text{ GeV}$$

✓ Veto

$$E_{\pm}(x_{\text{veto}}) > 10 \text{ MeV}$$

✓ HCAL

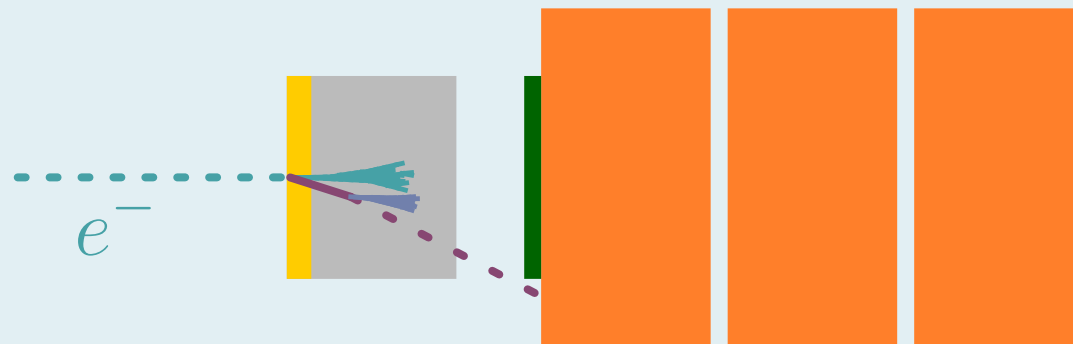
$$E_{\pm} > 1 \text{ GeV}$$

## Assumptions:

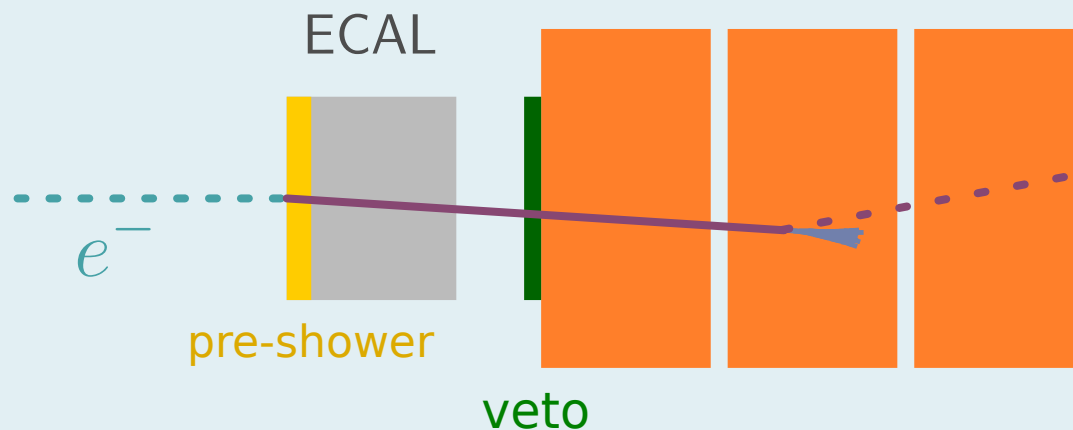
- $e^+e^-$  sufficiently overlapped: sum energies;
- Everything is forward: neglect *leakage* of particles from detector.

# Semi-visible optimized cuts

[Eur. Phys. J. C 81.10 (2021), p. 959]



✓ Any  $e^+e^-$  pair triggering an activity before HCAL 2



✓ Max 1  $e^+e^-$  pair in HCAL

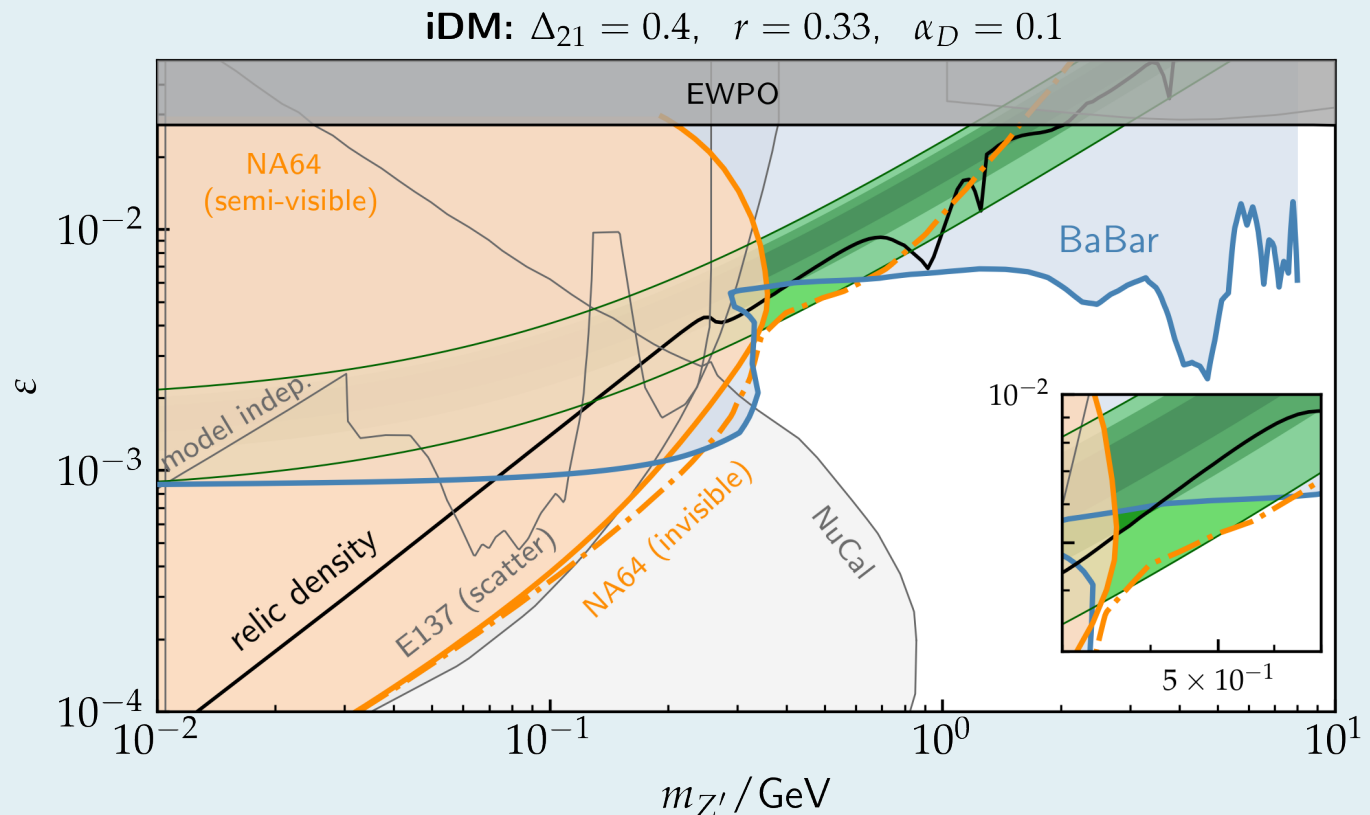
**Model dependent:** inelastic dark matter model: 1 dark photon and 2 HNFs  
Analysis with optimized cuts.

# Model 1: inelastic dark matter (iDM) with one pseudo-Dirac pair

$$\mathcal{L} \supset g_D \bar{\psi}_1 \not{Z}' \psi_2$$

- After diagonalisation, lightest state  $\psi_1$  is DM, with  $\psi_2$  decaying semi-visibly
- DM relic abundance from co-annihilations

**Minimal iDM is  
almost excluded**



# Model 2: iDM with several pseudo-Dirac pair

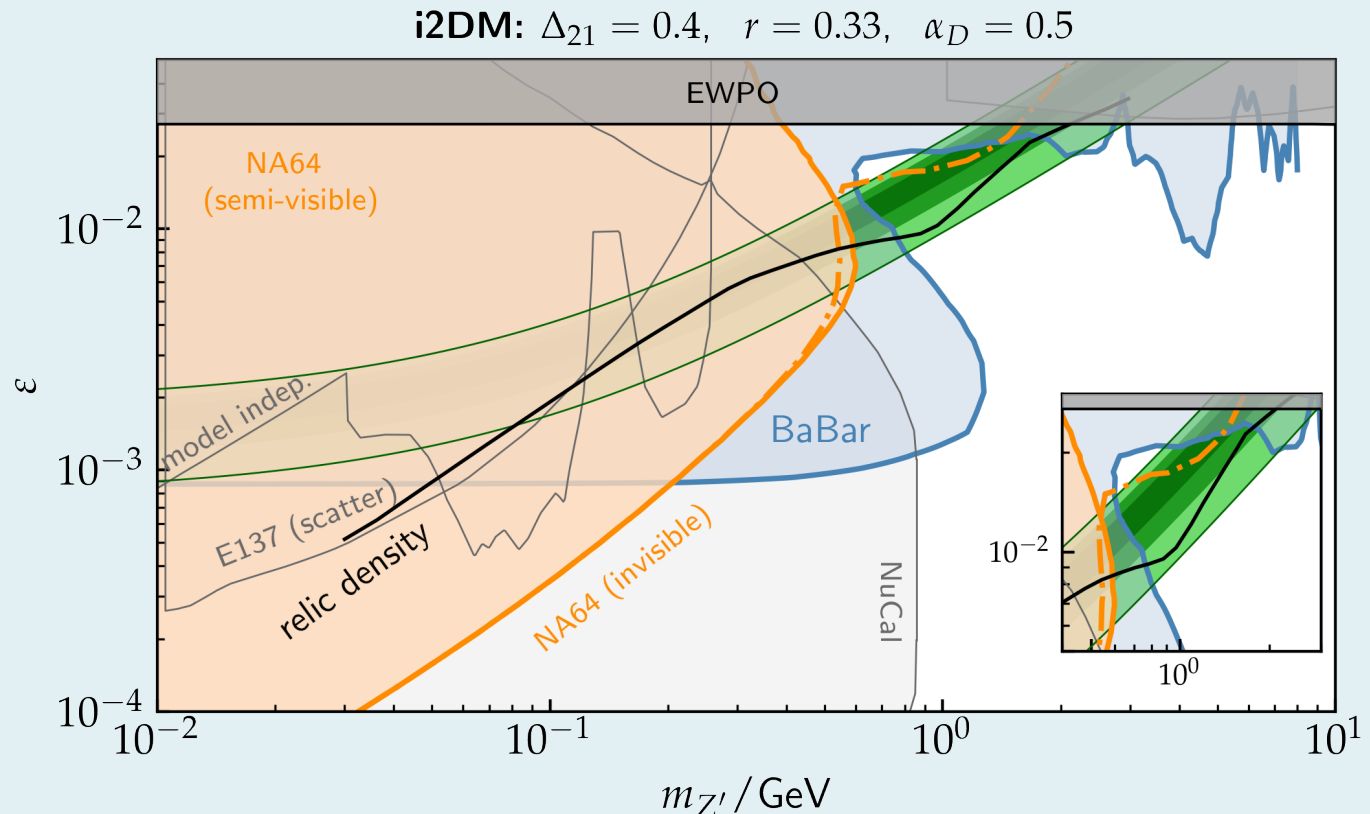
$$\mathcal{L} \supset g_D \theta^2 \bar{\psi}_1 \not{Z}' \psi_1 + g_D \theta \bar{\psi}_2 \not{Z}' \psi_1 + g_D \bar{\psi}_2 \not{Z}' \psi_2$$

- After diagonalisation: light neutral state  $\psi_1$  and heavier state  $\psi_2$  more strongly coupled to dark force with small mixing  $\vartheta$

**Tip:** inject more visible final states

- $Z' \rightarrow \psi_1 \psi_1$
- $Z' \rightarrow \psi_1 \psi_2$
- $Z' \rightarrow \psi_2 \psi_2$

**Modified iDM allowed**

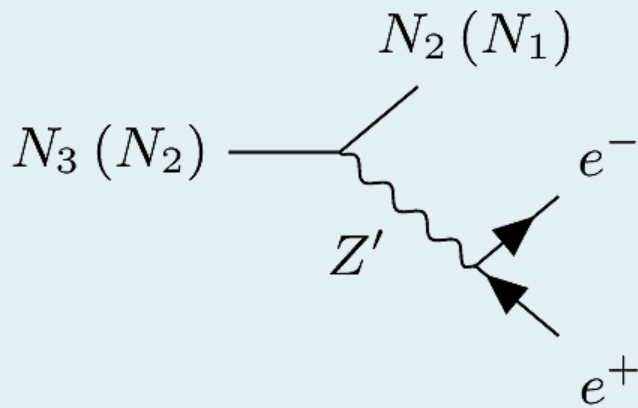




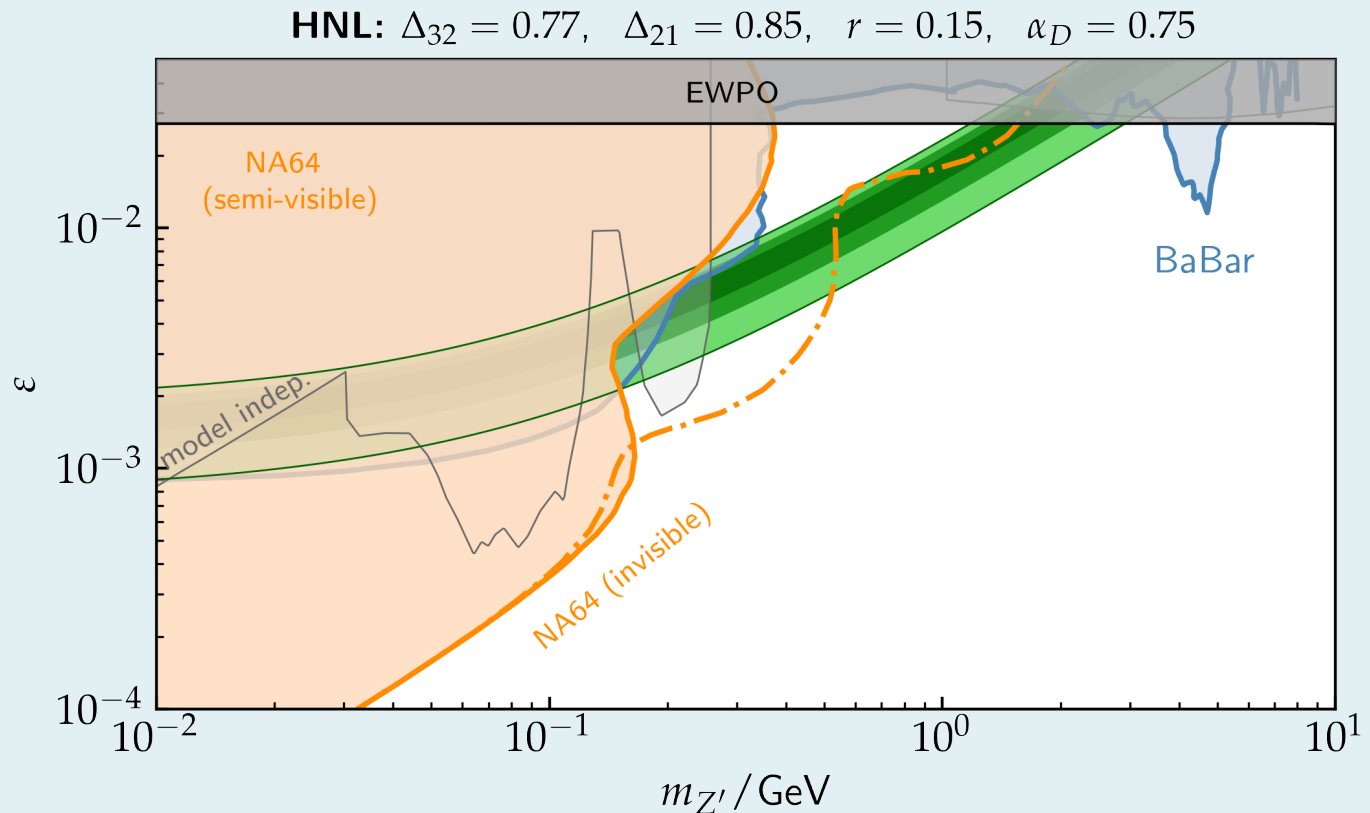
# Model 3: HNLs

$$\mathcal{L} \supset g_D V_{ij} \bar{N}_i \not{Z}' N_j + \text{h.c.}$$

- After diagonalisation: we obtain 3 HNLs, interacting by  $V_{ij}$
- BPs and model: [A. Abdullahi et al. Phys. Lett. B 820 (2021), p. 136531]



**HNLs model allowed**



# Backup slides

# The BaBar simulation: veto criteria

**Veto criteria:** if decays happen in instrumented region of detector then veto event if both

(1) Energy of lepton tracks exceeds BaBar detection threshold

(1)  $\theta_{\text{sep}} > 10^\circ : E_{\pm} > 100 \text{ MeV}$  well separated pairs

(2)  $\theta_{\text{sep}} < 10^\circ : E_+ + E_- > 100 \text{ MeV}$  overlapping pairs

(2) Wide polar angle to avoid electrons escaping along the beam pipeline

$$17^\circ < \theta_{\text{pol}} < 142^\circ$$

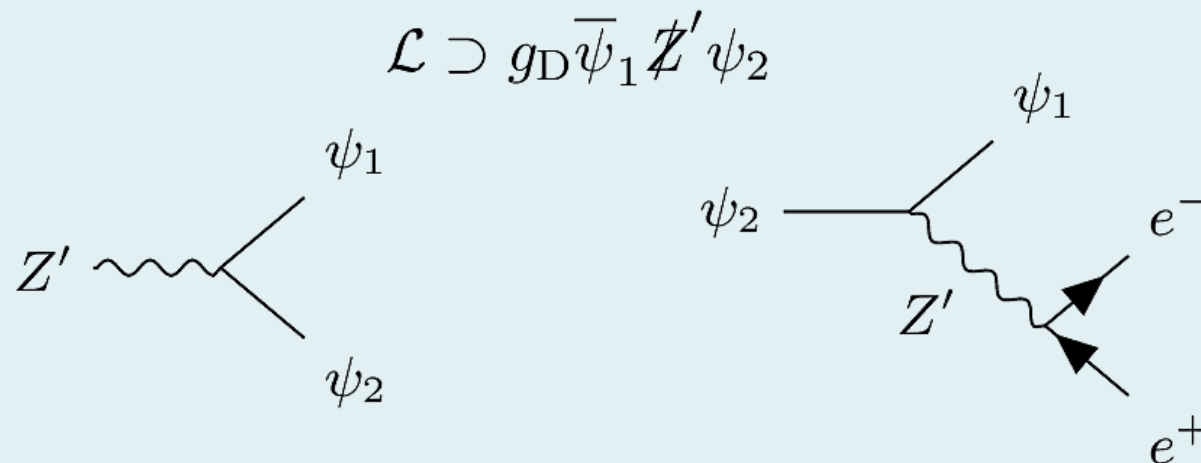
**Recast:** solve  $\varepsilon_{\text{BaBar}} = \varepsilon \sqrt{P^{\text{inv}}(\varepsilon, m_{Z'})}$

$$\text{where } P^{\text{inv}}(\varepsilon, m_{Z'}) = 1 - \frac{N_{\text{veto}}(\varepsilon, m_{Z'})}{N(\varepsilon, m_{Z'})}$$

# Model 1: inelastic dark matter (iDM) with one pseudo-Dirac pair

$$\mathcal{L} \supset \frac{1}{2} \begin{pmatrix} \overline{\psi_L} & \overline{\psi_R^c} \end{pmatrix} \begin{pmatrix} \mu_L & m_D \\ m_D & \mu_R \end{pmatrix} \begin{pmatrix} \psi_L^c \\ \psi_R \end{pmatrix} + \text{h.c.}$$

- $\mu_L \approx \mu_R \ll m_D$ : on-diagonal couplings suppressed
- After diagonalisation, lightest state  $\psi_1$  is DM, with  $\psi_2$  decaying visibly
- DM relic abundance from co-annihilations



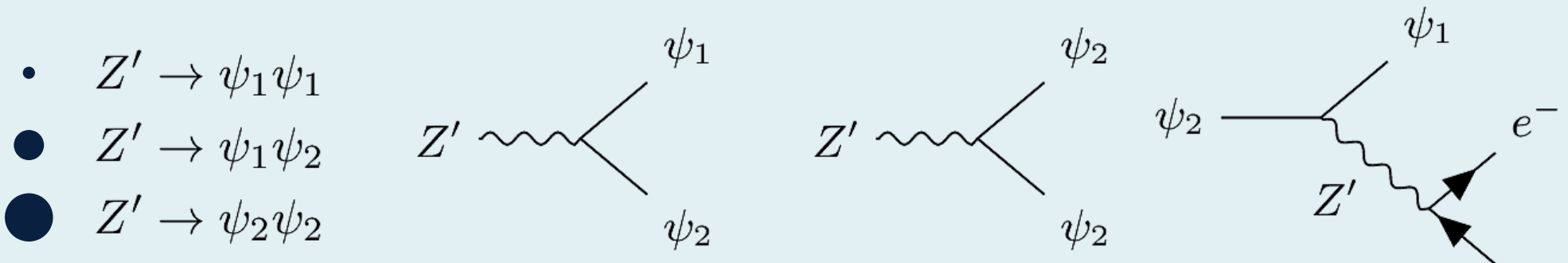
- Proposed in [G. Mohlabeng. Phys. Rev. D 99.11 (2019), p. 115001], where the study assumed BaBar energy threshold of 60 MeV (optimistic, we used 100 MeV, which is the same used in BaBar selection criteria)

# Model 2: iDM with several pseudo-Dirac pair

$$\mathcal{L} \supset (\eta_L \quad \chi_L) \begin{pmatrix} M_1 & M_L \\ M_R & M_2 \end{pmatrix} \begin{pmatrix} \eta_R \\ \chi_R \end{pmatrix} + \text{h.c.}$$

- neutral ( $\eta$ ) and  $U(1)'$  charged ( $\chi$ ) pseudo-Dirac pairs
- After diagonalisation: light neutral state  $\psi_1$  and heavier state  $\psi_2$  more strongly coupled to dark force with small mixing  $\vartheta$

$$\mathcal{L} \supset g_D \theta^2 \bar{\psi}_1 \not{Z}' \psi_1 + g_D \theta \bar{\psi}_2 \not{Z}' \psi_1 + g_D \bar{\psi}_2 \not{Z}' \psi_2$$



- $\psi_1$  can not be dark matter, unless secluded annihilations
- If not DM, then must decay (e.g. mixing w/ SM  $\nu$ ).

# Model 3: HNLs

[A. Abdullahi et al. Phys. Lett. B 820 (2021), p. 136531]

$$\mathcal{L} \supset (\overline{N} \quad \overline{\psi}_L \quad \overline{\psi}_R^c) \begin{pmatrix} M_N & \Lambda_L & \Lambda_R \\ \Lambda_L^T & 0 & M_X \\ \Lambda_R^T & M_X^T & 0 \end{pmatrix} \begin{pmatrix} N^c \\ \psi_L^c \\ \psi_R \end{pmatrix} + \text{h.c.}$$

- With neutral state  $N$  and  $U(1)'$ -charged fermions
- After diagonalisation we obtain 3 HNLs, interacting by  $V_{ij}$  (in principle they can mix also with SM  $\nu$ ).

$$\mathcal{L} \supset g_D V_{ij} \overline{N}_i \not{Z}' N_j + \text{h.c.}$$

