





Flavor phenomenology with scalar leptoquarks

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Flavor in the SM: Organized but not understood



• Many **free parameters** (*fixed by data*!), which exhibit a **striking hierarchy** (*does not look accidental...*):

$$V_{\rm CKM} = \begin{pmatrix} \bullet & \bullet \\ \bullet & \bullet \\ \bullet & \bullet \end{pmatrix} \qquad \qquad M_{u,d,e} = \begin{pmatrix} \bullet & \bullet \\ \bullet & \bullet \\ \bullet & \bullet \end{pmatrix}$$

Is there a **flavor theory** that could **predict** the observed **pattern of Yukawas**?

⇒ Difficult problem to solve (at which NP scale?) — Exp. guidance needed!



Olcyr Sumensari (IJCLab, Orsay)

LFU in $b \rightarrow c \tau \bar{\nu}$

Experiment



• R_D^{exp} and $R_{D^*}^{exp}$: dominated by BaBar!

• LHCb confirmed tendency $R_{J/\psi}^{exp} > R_{J/\psi}^{SM}$, i.e. $B_c \to J/\psi \ell \bar{\nu}$ — with large uncertainties.

Needs clarification from **Belle-II** and **LHCb (run-2)** data!

Why leptoquarks?

• EFT interpretations:

[Di Luzio et al. '17]

- Leptoquarks induce large semileptonic contributions (at tree-level), while remaining consistent with purely leptonic and quark-level observables (loop-level):



- Well-motivated theoretically:
 - GUTs;
 - <u>Neutrino masses;</u>



see e.g. [Dorsner et al. '17]

. . .

Which leptoquark?

[Angelescu, Becirevic, Faroughy, Jaffredo, **OS**. '21]

[Buchmuller, Wyler. '88]





	Model	$R_{K^{(*)}}$	$R_{D^{(*)}}$	$R_{K^{(*)}} \& R_{D^{(*)}}$
0	$S_3 \ ({f \bar 3},{f 3},1/3)$	\checkmark	×	×
Spin 1 Spin	$S_1 \ ({f \bar 3},{f 1},1/3)$	×	✓	×
	R_2 (3, 2, 7/6)	× *	\checkmark	×
	U_1 (3 , 1 , 2/3)	\checkmark	✓	✓
	U_3 (3 , 3 , 2/3)	\checkmark	×	×

Which leptoquark?

[Angelescu, Becirevic, Faroughy, Jaffredo, OS. '21]

[Buchmuller, Wyler. '88]



• The U_1 LQ can do the job alone, but <u>UV completion needed</u>.

See talk by D. Faroughy!

- $\mathscr{G}_{PS} = SU(4) \times SU(2)_L \times SU(2)_R$ contains $U_1 \sim (3, 1, 2/3)$
- Viable TeV models proposed: $U_1 + Z' + g'$

[Di Luzio et al. '17, Bordone et al. '18, Blanke et al. '18...]

<u>This talk</u>: Two scalar LQs are also viable!

[Crivellin et al. '17, Marzocca '18] [Becirevic et al. '18]

Scalar LQs for $b \rightarrow s \mu \mu$



$$\mathcal{L}_{\text{eff}} = \frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{\alpha_{\text{em}}}{4\pi} \left[\bar{s}_L \gamma^\mu b_L \right] \left[\bar{\ell} (C_9 + C_{10} \gamma_5) \ell \right] + \dots$$

 $S_3 = (\bar{3}, 3, 1/3)$

Purely left-handed operator preferred [4.6σ]:

$$\delta C_9^{\mu\mu} = -\delta C_{10}^{\mu\mu} = -0.41 \pm 0.09$$

Scalar LQs for $b \rightarrow s \mu \mu$



$$b_{L} \xrightarrow{b_{L}} h_{L}$$

$$\int S_{3}^{(-4/3)} S_{3}^{(-4/3)}$$

$$S_{L} \xrightarrow{b_{L}} h_{L}$$

$$\int S_{4} \xrightarrow{b_{L}} h_{L}$$

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• Tree-level prediction:

$$\mathcal{L}_{S_3} = \boldsymbol{y}_L^{ij} \ \overline{Q^C} i\tau_2 (\vec{\tau} \cdot \vec{S}_3) L_j + \text{h.c.}$$

$$\delta C_9 = -\delta C_{10} \propto \frac{v^2}{m_{S_3}^2} y_L^{s\mu} y_L^{b\mu *}$$

NB. Consistent with other constraints: Δm_{B_s} , $B \to K \nu \bar{\nu}$, ...

LFU in charged currents

$$\mathcal{L}_{\text{eff}} = -2\sqrt{2}G_F V_{cb} \Big[(1+g_{V_L}) \big(\bar{c}_L \gamma_\mu b_L \big) \big(\bar{\ell}_L \gamma_\mu \nu_L \big) + g_{V_R} \big(\bar{c}_R \gamma_\mu b_R \big) \big(\bar{\ell}_L \gamma_\mu \nu_L \big) \\ + g_{S_R} \big(\bar{c}_L b_R \big) \big(\bar{\ell}_R \nu_L \big) + g_{S_L} \big(\bar{c}_R b_L \big) \big(\bar{\ell}_R \nu_L \big) + g_T \big(\bar{c}_R \sigma_{\mu\nu} b_L \big) \big(\bar{\ell}_R \sigma_{\mu\nu} \nu_L \big) \Big] + \text{h.c.}$$



Viable solutions:

$$\begin{array}{l} -g_{V_L} > 0 \\ -g_{S_L} = -4g_T > 0 \end{array} \end{array} \Rightarrow \begin{array}{l} S_1 = (\overline{\mathbf{3}}, \mathbf{1}, 1/3) \\ -g_{S_L} = +4g_T \in i \mathbb{R} \quad \Rightarrow \end{array}$$

NB. More information is needed to distinguish among the viable solutions.

$$\Rightarrow$$
 e.g., $B \rightarrow D^{(*)} \tau \nu$ angular observables.

See talk by Damir Becirevic

Combined explanation: $R_2 \& S_3$



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$$\mathcal{L} \supset y_R^{ij} \ ar{Q}_i \ell_{Rj} R_2 + y_L^{ij} \ ar{u}_{Ri} L_j \widetilde{R}_2^{\dagger} + y^{ij} \ ar{Q}_i^C i au_2(au_k S_3^k) L_j + ext{h.c.}$$

 $R_2 = (3, 2, 7/6), \ S_3 = (ar{3}, 3, 1/3)$

Flavor ansatz motivated by a SU(5) GUT scenario: $y_R = y_R^T \quad \& \quad y = -y_L$

$$y_R E_R^{\dagger} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & y_R^{b\tau} \end{pmatrix}, \ U_R y_L = \begin{pmatrix} 0 & 0 & 0 \\ 0 & y_L^{c\mu} & y_L^{c\tau} \\ 0 & 0 & 0 \end{pmatrix}, \ U_R = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos\theta & -\sin\theta \\ 0 & \sin\theta & \cos\theta \end{pmatrix}$$

Parameters: m_{R_2} , m_{S_3} , $y_R^{b au}$, $y_L^{c\mu}$, $y_L^{c au}$ and heta



Results and predictions

NB. $g_{S_L}(\Lambda) = 4g_T(\Lambda)$



low-energy observables!

See back-up!

[Becirevic et al. '22]

Suitable couplings:

 $y_L^{c\mu} = 0.2, \quad y_L^{c\tau} = 1.0, \quad y_R^{b\tau} = -0.2 - 1.2i, \quad \theta = -1.5$

LHC constraints



See talks by Lukas Allwicher and Florentin Jaffredo this afternoon!

Lepton Flavor Violation

• $\mathsf{LFUV} \leftrightarrow \mathsf{LFV}$:



LFV B- and τ -decays are bounded from above and below!

NB. Similar conclusions for other minimalistic solutions of *B*-anomalies:

See e.g. [Cornella et al. '21]

[Angelescu, Becirevic, Faroughy, Jaffredo, **OS**. '21]

Predictions for $B_s \rightarrow \mu \tau \quad B \rightarrow K^{(*)} \mu \tau$ New searches (95% CL): [LHCb]

$$\mathcal{B}(B_s \to \mu \tau)^{\exp} < 4.2 \times 10^{-5}$$
$$\mathcal{B}(B \to K^{(*)} \mu \tau)^{\exp} < 4.5 \times 10^{-5}$$



B-decays with missing energy

• Relatively **clean observable** in the SM:

$$\mathcal{B}(B^+ \to K^+ \nu \bar{\nu})^{\rm SM} = 4.6(5) \times 10^{-6}$$

[Buras et al. '14, Blake et al. '16]

Models for the *B*-anomalies predict sizable deviations from SM predictions.





Promising results from early Belle-II data!

e.g. [Becirevic et al. '22]

What about loop-level solutions?

Model	$R_{K^{(*)}}$	$R_{D^{(*)}}$	$ R_{K^{(*)}} \& R_{D^{(*)}} $
S_3 ($\bar{3}, 3, 1/3$)	✓	×	×
S_1 ($\bar{3}, 1, 1/3$)	×	✓	×
R_2 (3 , 2 , 7/6)	× *	\checkmark	×
U_1 (3 , 1 , 2/3)	\checkmark	✓	\checkmark
U_3 (3 , 3 , 2/3)	\checkmark	×	×

$R_2 = (3, 2, 7/6)$

• LFU violation can also be generated via loops! First attempt in [Bauer, Neubert, '15]. A compelling scenario can be obtained with R_2 :

$$\mathcal{L}_{R_2} = -y_L^{ij} \,\bar{u}_{Ri} R_2 i\tau_2 L_j + y_R^{ij} \,\bar{Q}_i R_2 \ell_{Rj} + \text{h.c.}$$

• **Tree-level** prediction **strongly disfavored** by current data:



$$\delta C_9^{\mu\mu} = \delta C_{10}^{\mu\mu} \stackrel{\text{tree}}{=} -\frac{\pi v^2}{2\lambda_t \alpha_{\text{em}}} \frac{y_R^{s\mu} (y_R^{b\mu})^*}{m_{R_2}^2}$$

$R_2 = (3, 2, 7/6)$

• LFU violation can also be generated via loops! First attempt in [Bauer, Neubert, '15]. A compelling scenario can be obtained with R_2 :

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• **Tree-level** prediction **strongly disfavored** by current data:



• For $y_R = 0$, leading contributions are **loop-induced** (with the **correct pattern**!):

$$\delta C_{9}^{\mu\mu} = -\delta C_{10}^{\mu\mu} \stackrel{\text{loop}}{=} \sum_{i \in \{u,c,t\}} \frac{V_{ib} V_{is}^{*}}{V_{tb} V_{ts}^{*}} \frac{y_{L}^{i\mu} (y_{L}^{j\mu})^{*}}{m_{R_{2}}^{2}} \mathcal{G}(x_{u_{i}}, x_{u_{j}})$$

$$= \frac{|y_{L}^{t\mu}|^{2}}{16\pi\alpha_{\text{em}}} \frac{m_{t}^{2}}{m_{R_{2}}^{2}} \log\left(\frac{m_{t}}{m_{R_{2}}}\right) + \dots$$
As we want



- Current deviations ($\approx 15\%$) are too large to be explained by R₂.
- If the *deviations* turn out to be *smaller*, this scenario would be <u>interesting again</u>!

Perspectives / Beyond LFU anomalies

Perspectives / Beyond LFU anomalies

- Experimental situation remains unclear!
 - Wait for Belle-II for an independent cross-check!
- We identified the mediators that can explain $R_{K^{(*)}}$ and/or $R_{D^{(*)}}$.
 - The vector U_1 is viable. Two scalar LQs can do the job too.
 - Interesting phenomenology of R_2 (at one-loop!).
- Upcoming low- and high-energy measurements will be fundamental to refute or confirm the remaining viable models.

 $pp \to \ell \ell' \qquad \qquad R_{D^{(*)}, D^{(*)}_s, \Lambda^{(*)}_c, \dots} \qquad \qquad R_{K^{(*)}, \phi, \dots} \qquad \qquad B \to K^{(*)} \mu \tau \qquad \qquad B \to K^{(*)} \nu \bar{\nu}$

- Even if the LFU anomalies disappear, we definitely have learned a lot:
 - We need theoretically clean observables!
 - Flavor physics at high-pr.
 - New attempts to address the flavor problem at the TeV scale!

. . .

Thank you!

Back-up

[Intermezzo] - Lesson from LFU anomalies!

Global $b \to s\ell\ell$ fit

 $\mathsf{LFU} + \mathscr{B}(B_s \to \mu\mu)$



See talk by B. Capdevilla, M. Fedele, S. Neshatpour, P. Stangl at LHCb Implications '21

We need observables that are mildly sensitive to hadronic uncertainties!

EFT for
$$b \rightarrow s\ell\ell$$

$$\mathcal{L}_{\text{eff}} = \frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \left[\sum_{i=1}^6 C_i(\mu) \mathcal{O}_i + \sum_{7,8,9,10,P,S} \left(C_i(\mu) \mathcal{O}_i + \mathcal{C}'_i(\mu) \mathcal{O}'_i \right) \right] + \text{h.c.}$$

• Semileptonic operators:

$$\mathcal{O}_{9}^{(\prime)} = (\bar{s}\gamma_{\mu}P_{L(R)}b)(\bar{\ell}\gamma^{\mu}\ell)$$
$$\mathcal{O}_{10}^{(\prime)} = (\bar{s}\gamma_{\mu}P_{L(R)}b)(\bar{\ell}\gamma^{\mu}\gamma_{5}\ell)$$

$$\mathcal{O}_{S}^{(\prime)} = (\bar{s}P_{R(L)}b)(\bar{\ell}\ell)$$
$$\mathcal{O}_{P}^{(\prime)} = (\bar{s}P_{R(L)}b)(\bar{\ell}\gamma_{5}\ell)$$

• Dimension-6 tensor operator is not allowed by $SU(2)_L \times U(1)_Y$

[Buchmuller, Wyler. '85]

• (Pseudo)scalar operators are tightly constrained by

$$\overline{\mathcal{B}}(B_s \to \mu\mu)^{\text{exp}} = (2.85 \pm 0.22) \times 10^{-9}$$
$$\overline{\mathcal{B}}(B_s \to \mu\mu)^{\text{SM}} = (3.66 \pm 0.14) \times 10^{-9}$$

[Our exp. average: CMS, ATLAS, LHCb]

[Beneke et al. '19]

[Intermezzo] $B_s \rightarrow \mu \mu$

[Angelescu, Becirevic, Faroughy, Jaffredo, **OS**. '21]

[Our exp. average: CMS, ATLAS, LHCb]



[LHCb '21]

- Good agreement between LHCb results and the SM predictions;
- Small deficit in the exp. average *due to ATLAS measurement*.

Warning!

 $\frac{\mathrm{d}\mathcal{B}}{\mathrm{d}q^2}(B \to D^* \ell \nu) \propto |V_{cb}|^2 \, |\mathcal{F}(w)|^2$

$$\left[w = \frac{m_B^2 + m_{D^*}^2 - q^2}{2m_B m_{D^*}}\right]$$



SM predictions

Form-factors: *R*_D

Lattice QCD at q² ≠ q²_{max} (w ≠ 1) available for both leading (vector) and subleading (scalar) form-factors:

$$\langle D(k)|\bar{c}\gamma^{\mu}b|B(p)\rangle = \left[(p+k)^{\mu} - \frac{m_B^2 - m_D^2}{q^2}q^2\right]f_+(q^2) + q^{\mu}\frac{m_B^2 - m_D^2}{q^2}f_0(q^2)$$

with $f_+(0) = f_0(0)$

[MILC/Fermilab '15, HPQCD '15]



[Intermezzo] How to improve the SM prediction for R_{D^*} ?

• Theory uncertainties are related to m_{τ} , i.e the only source of LFU breaking in the SM:

• A simple redefinition can reduce these uncertainties:



NB. Re-weighting of the muon rate by $\omega_{\tau}(q^2)/\omega_{\mu}(q^2)$ can further reduce the theory uncertainties.

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From EFTs to concrete models

Many papers in the literature...



Challenging task because of the numerous exp. constraints: flavor, LHC, EWPT...

LHC constraints

i. LQ pair-production

Production dominated by QCD:

$$\sigma(pp \to \mathrm{LQ} \,\mathrm{LQ}^{\dagger}) \times \underbrace{\mathcal{B}(\mathrm{LQ} \to \ell q)^2}_{\equiv \beta^2}$$



see [Dorsner et al. '18] for a recent review

See talk by K. Yong Sheng!

ATLAS and CMS results for
$$\beta = 1 \text{ (or } 0.5)$$

Decays	Scalar LQ limits	Vector LQ limits	$\mathcal{L}_{\mathrm{int}}$ / Ref.
$jj auar{ au}$	_	_	_
$b\bar{b} auar{ au}$	$1.0 (0.8) { m TeV}$	1.5 (1.3) TeV	36 fb^{-1} [39]
$t\bar{t} auar{ au}$	$1.4 (1.2) { m TeV}$	2.0 (1.8) TeV	$140 \ {\rm fb}^{-1}$ [40]
$jj\muar\mu$	$1.7 (1.4) { m TeV}$	2.3 (2.1) TeV	$140 \ {\rm fb}^{-1}$ [41]
$bar{b}\muar{\mu}$	$1.7 (1.5) { m TeV}$	2.3 (2.1) TeV	$140 \ {\rm fb}^{-1}$ [41]
$tar{t}\muar{\mu}$	$1.5 (1.3) { m TeV}$	2.0 (1.8) TeV	$140 \ {\rm fb}^{-1}$ [42]
jj uar u	$1.0 (0.6) { m TeV}$	1.8 (1.5) TeV	36 fb^{-1} [43]
$b\bar{b}\nu\bar{ u}$	$1.1 \ (0.8) \ {\rm TeV}$	1.8 (1.5) TeV	36 fb^{-1} [43]
$t\bar{t} u\bar{ u}$	$1.2 (0.9) { m TeV}$	$1.8 (1.6) { m TeV}$	$140 \text{ fb}^{-1} [44]$

[Angelescu, Becirevic, Faroughy, Jaffredo, **OS**. '21]

LHC constraints

ii. Di-lepton production at high- p_T

See talks by Lukas Allwicher and Florentin Jaffredo this afternoon!



Useful upper limits on LQ couplings:



Example: $S_3 \sim (\bar{3}, 3, 1/3)$

$$\mathcal{L}_{S_3} = y_L^{ij} \ \overline{Q^C} i\tau_2 (\vec{\tau} \cdot \vec{S}_3) L_j + \text{h.c.}$$

First considered by [Eboli, '88]

[Angelescu, Becirevic, Faroughy, Jaffredo, OS. '21]

High- p_T **package**

[Allwicher, Faroughy, Jaffredo, OS, Wilsch. 2204.XXXX]



HighPT : High-p_T Tails

<<HighPT`

- Authors : Lukas Allwicher, Darius A. Faroughy, Florentin Jaffredo, Olcyr Sumensari, and Felix Wilsch
- Reference : arXiv:22xx.xxxxx
- Website : https://github.com/HighPT/HighPT

HighPT is free software under the terms of the MIT License.

Please submit bugs and feature requests using GitHub's issue system at:

https://github.com/HighPT/HighPT/issues

Recast of LHC searches for the SMEFT and simplified scenarios



 $pp \to \tau\tau$ $pp \to ee, \ \mu\mu$ $pp \to \tau\nu$ $pp \to e\nu, \ \mu\nu$ $pp \to e\mu, \ e\tau, \ \mu\tau$

[arXiv:2002.12223] CMS-PAS-EXO-19-019 ATLAS-CONF-2021-025 [arXiv:1906.05609] CMS-PAS-EXO-19-014

Effective Lagrangian at $\mu \approx m_{LQ}$:

•
$$b \to c\tau\bar{\nu}$$
:
 $\propto \frac{y_L^{c\tau}y_R^{b\tau*}}{m_{R_2}^2} \left[(\bar{c}_R b_L)(\bar{\tau}_R \nu_L) + \frac{1}{4} (\bar{c}_R \sigma_{\mu\nu} b_L)(\bar{\tau}_R \sigma^{\mu\nu} \nu_L) \right] + \dots$

NB. $\Lambda_{\rm NP}/g_{\rm NP} \approx 30 {
m TeV}$

$$\propto \sin 2 heta \, rac{|y_L^{c\mu}|^2}{m_{S_3}^2} \, (ar{s}_L \gamma^\mu b_L) (ar{\mu}_L \gamma_\mu \mu_L)$$

•
$$\Delta m_{B_s}$$
:

• $b \rightarrow s \mu \mu$:

$$\propto \sin^2 2 heta \; rac{\left[\left(y_L^{\,c\mu}
ight)^2 + \left(y_L^{\,c au}
ight)^2
ight]^2 }{m_{S_3}^2} (ar{s}_L \gamma^\mu b_L)^2$$

 \Rightarrow Suppression mechanism of $b \rightarrow s\mu\mu$ wrt $b \rightarrow c\tau\bar{\nu}$ for small $\sin 2\theta$.

 \Rightarrow Phenomenology suggests $\theta \approx \pi/2$ and $y_R^{b\tau}$ complex

Other notable constraints...

• $R_{e/\mu}^{K \text{ exp}} = 2.488(10) \times 10^{-5}$ [PDG], $R_{e/\mu}^{K \text{ SM}} = 2.477(1) \times 10^{-5}$ [Cirigliano 2007]

$$R_{e/\mu}^{K} = \frac{\Gamma(K^{-} \to e^{-}\bar{\nu})}{\Gamma(K^{-} \to \mu^{-}\bar{\nu})}$$

• $R_{\mu/e}^{D \exp} = 0.995(45)$ [Belle 2017], $R_{\mu/e}^{D^* \exp} = 1.04(5)$ [Belle 2016]

$$R^{D^{(*)}}_{\mu/e} = \frac{\Gamma(B \to D^{(*)} \mu \bar{\nu})}{\Gamma(B \to D^{(*)} e \bar{\nu})}$$

- $\mathcal{B}(\tau \to \mu \phi) < 8.4 \times 10^{-8}$ [PDG]
- Loops: $\Delta m_{B_s}^{\text{exp}} = 17.7(2) \text{ ps}^{-1}$ [PDG], $\Delta m_{B_s}^{\text{SM}} = (19.0 \pm 2.4) \text{ ps}^{-1}$ [FLAG 2016]
- Loops: $Z \to \mu\mu$, $Z \to \tau\tau$, $Z \to \nu\nu$ [PDG]

$$\frac{g_V^{\tau}}{g_V^e} = 0.959(29) , \quad \frac{g_A^{\tau}}{g_A^e} = 1.0019(15) \qquad \frac{g_V^{\mu}}{g_V^e} = 0.961(61) , \quad \frac{g_A^{\mu}}{g_A^e} = 1.0001(13)$$
$$N_{\nu}^{\exp} = 2.9840(82)$$



CPV ASPECTS OF R₂

Nejc Kosnik slides at Invisibles'22

- + How to test large CPV phase $y_R^{b au} = -0.2 1.2i$?
 - Charm electric dipole moment induces neutron EDM

W. Dekens, J. de Vries, M. Jung, K. K. Vos, 1809.09114

 Neutron on the lattice:
 $g_T^c = -(2.4 \pm 1.6) \times 10^{-4}$ C. Alexandrou, et al, 1909.00485

 Neutron EDM:
 $d_n < 1.8 \times 10^{-26} e \, \mathrm{cm}$ PSI, 2001.11966

 $\implies |\Im(g_{S_L})| < 0.76$

Improving precision of the lattice result could well probe relevant range $|\Im(g_{S_L})| \approx 0.5$

* Angular spectra of $\Lambda_b \to \Lambda_c (\to \Lambda \pi) \tau \nu$

P. Böer, A. Kokulu, J. N. Toelstede, D. van Dyk, 1907.12554

$$\begin{aligned} \frac{d^{4}\mathcal{B}}{dq^{2}d\cos\theta_{\tau}d\cos\theta d\phi} &= 8\pi \left[\mathcal{A}_{1} + \mathcal{A}_{2}\cos\theta \right. \\ &+ \left(\mathcal{B}_{1} + \mathcal{B}_{2}\cos\theta \right)\cos\theta_{\tau} + \left(\mathcal{C}_{1} + \mathcal{C}_{2}\cos\theta \right)\cos^{2}\theta_{\tau} \\ &+ \left(\mathcal{D}_{3}\sin\theta\cos\phi + \mathcal{D}_{4}\sin\theta\sin\phi \right)\sin\theta_{\tau} \\ &+ \left(\mathcal{E}_{3}\sin\theta\cos\phi + \mathcal{E}_{4}\sin\theta\sin\phi \right)\sin\theta_{\tau}\cos\theta_{\tau} \right], \end{aligned}$$