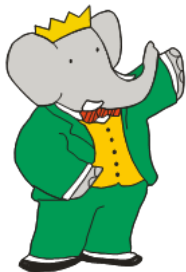


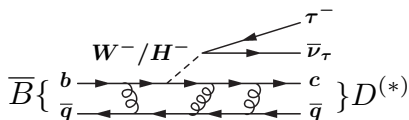
# Status of $R(D^{(*)})$ measurement with semileptonic tagging at *BABAR*

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Bologna, Italy



# Motivation for $R(D^{(*)})$ measurements



$$R(D^{(*)}) = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \nu_\tau)}{\mathcal{B}(B \rightarrow D^{(*)} l \nu_l)}$$

Signal mode

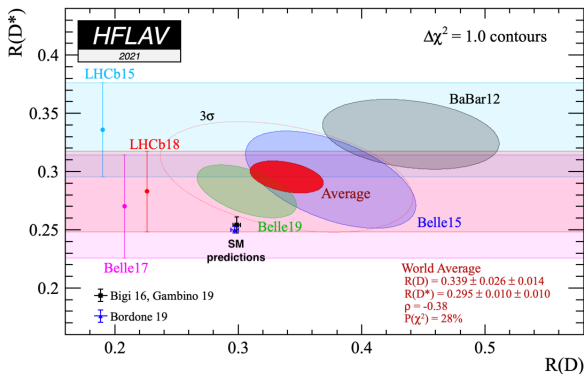


Normalization mode

- Semileptonic decays of  $B$  mesons mediated by  $W$  bosons.
- Decays involving electrons or muons are less sensitive to beyond standard model (BSM) contribution, while decays involving higher-mass  $\tau$  lepton are sensitive to additional amplitudes.
- Development of heavy quark effective theory (HQET) and precise measurements of  $B \rightarrow D^{(*)} l \nu$  (HFLAV2021):

$$R(D)_{\text{SM}} = 0.299 \pm 0.003, R(D^*)_{\text{SM}} = 0.254 \pm 0.005$$

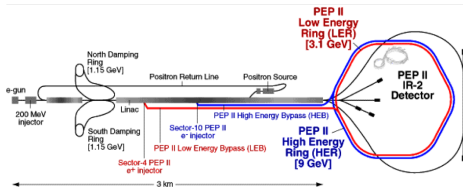
# Previous measurements



Experiment	$R(D)$	$R(D^*)$	Method
BaBar 2012	$0.440 \pm 0.058 \pm 0.042$	$0.322 \pm 0.024 \pm 0.018$	hadronic tag, $\tau \rightarrow l\nu\nu$
Belle 2015	$0.375 \pm 0.064 \pm 0.026$	$0.293 \pm 0.038 \pm 0.015$	hadronic tag, $\tau \rightarrow l\nu\nu$
LHCb 2015	-	$0.336 \pm 0.027 \pm 0.030$	$\tau \rightarrow \mu\nu\nu$
Belle 2017	-	$0.270 \pm 0.035 \pm 0.027$	hadronic tag
LHCb 2018	-	$0.283 \pm 0.019 \pm 0.029$	$\tau \rightarrow 3\pi\nu$
Belle 2019	$0.307 \pm 0.037 \pm 0.016$	$0.283 \pm 0.018 \pm 0.014$	semileptonic tag

The discrepancy between measurements and the SM predictions is about  $3.3\sigma$ .

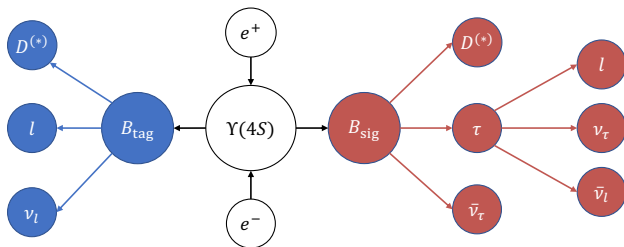
# BABAR experiment



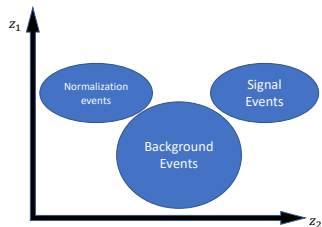
- Asymmetric  $e^+e^-$  collider operating at center-of-mass energy of 10.58 GeV.
- Total integrated luminosity of  $514 \text{ fb}^{-1}$  was collected (1999-2008), mostly at the  $\Upsilon(4S)$  resonance, but also at the  $\Upsilon(3S)$  and  $\Upsilon(2S)$  peaks, as well as off-resonance.

**Collaboration is still active more than 10 years after data taking ended!**

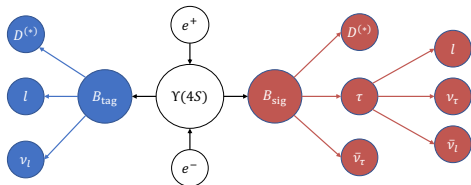
# Analysis strategy



- Measure  $R(D^{(*)})$  using semileptonic tagging and leptonic  $\tau$  decays.
- Combined measurements of  $R(D^0)$  and  $R(D^+)$  with isospin average.
- 2-dimensional maximum likelihood fit on data for signal extraction.
- The yields of signal and normalization modes are extracted simultaneously, aiming to eliminate some sources of systematic uncertainties.



# Reconstruction

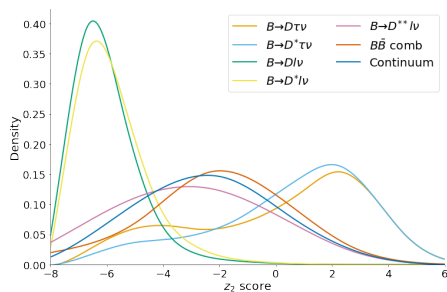
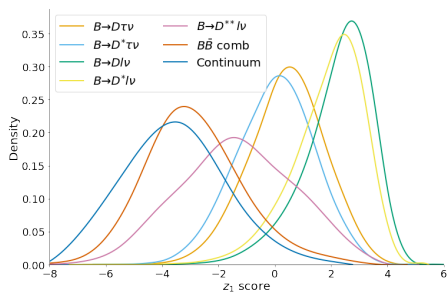


- Charged tracks are identified using loose PID. Photons are only considered with energy larger than 30 MeV.
- Criteria on reconstructed  $m(D)$  and  $\Delta M = m(D^*) - m(D)$  based on resolution for each  $D^{(*)}$  mode.
- To identify  $B_{\text{tag}}$ , we require  $\cos \theta_{B-D^{(*)}l}^{\text{tag}} \in [-2, 1]$ .

$$\cos \theta_{B-D^{(*)}l}^{\text{tag}} = \frac{2E_{\text{beam}}E_{D^{(*)}l} - m_B^2 - m_{D^{(*)}l}^2}{2|\mathbf{p}_B| \cdot |\mathbf{p}_{D^{(*)}l}|}$$

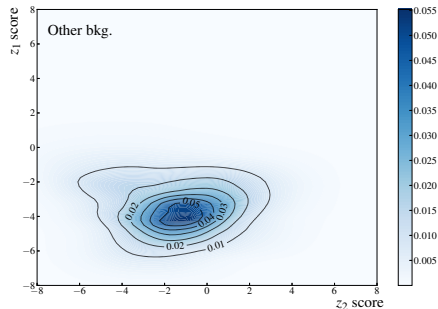
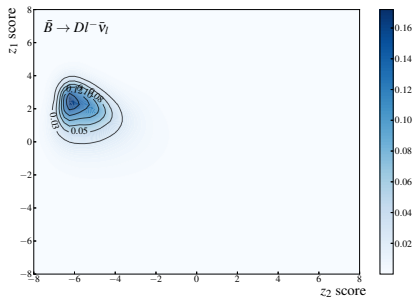
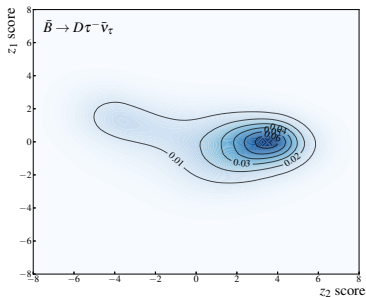
- Search for  $D^{(*)}l$  from the remaining tracks and neutral clusters:  $D^+l, D^0l, D^{*+}l, D^{*0}l$ .
- No extra charged tracks,  $K_S^0$  or  $\pi^0$  particles.

# Multivariate analysis for signal separation



- $z_1$  aims to distinguish signal and normalization events from all types of backgrounds.
- $z_2$  aims to distinguish between signal and normalization events.
- Both classifiers are boosted decision tree (BDT) models.

# Signal modeling



- Adaptive kernel density estimation is applied to learn the PDFs for each event type densities.
- Introduce local bandwidth factors to control the local smoothing.
- Cross validation technique to find optimal bandwidths.



# Computation time speed-up

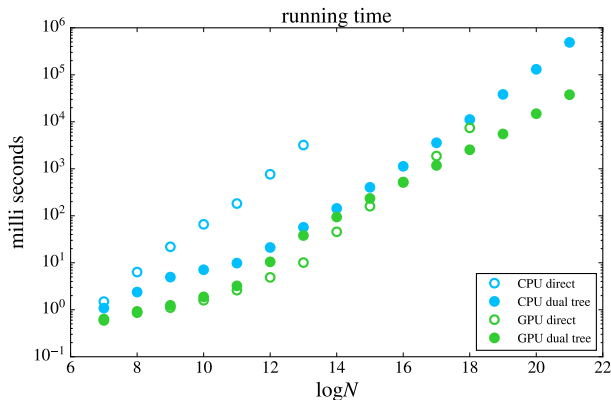


Figure: Benchmark performance for various implementations, as a function of sample size ( $N$ ) ( $\log = \log_2$ ).

Dual-tree algorithm with GPU acceleration for speed-up [A. Gray and A. Moore, 2003].

# 2D fit

- Extract signals from each of four subsets  $D^{+l}, D^{0l}, D^{*+l}, D^{0*l}$  **independently**.
- For each subset, the distribution is combination of signal, normalization, feed-up (feed-down),  $B \rightarrow D^{**}l\nu, B\bar{B}$  combinatorial and continuum events.
- Maximum likelihood fit is applied on each subset. **All the yields are free parameters** ( $Y_j$ ) during the 2D fit.

$$\max_{\mathbf{Y}} \mathcal{L} = \prod_{i=1}^n (\sum_{j=1}^C Y_j \cdot f(z_{1j}, z_{2j}))$$
$$s.t. \sum_{j=1}^C Y_j = N$$

(1)

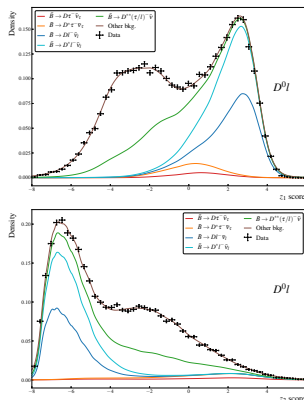


Figure: Example of 2D fit on  $D^{0l}$  subset.

# Systematic uncertainties (preliminary)

Source	$\Delta R(D)$ (%)	$\Delta R(D^*)$ (%)
$B \rightarrow D l \nu$ form factor	0.48	0.30
$B \rightarrow D^* l \nu$ form factor	0.96	0.58
$B \rightarrow D^{**} l \nu$ form factor	0.35	0.20
$\mathcal{B}(B \rightarrow D^{(*)} l \nu)$	0.47	0.32
$\mathcal{B}(b \rightarrow c \bar{c})$	0.49	0.25
$\mathcal{B}(B \rightarrow D^{**} l \nu)$	2.94	2.53
$\mathcal{B}(D)$	0.87	0.91
PDF shapes MC statistics	4.12	4.37
$B\bar{B}$ Background calibration	2.60	0.94
$\mathcal{B}(Y(4S))$	0.29	0.33
PID efficiency	0.29	0.40
Soft $\pi^0$ efficiency	0.84	1.24
$\mathcal{B}(\tau \rightarrow l^- \bar{\nu}_l \nu_\tau)$	0.16	0.16
Systematic Total	5.98	5.31
Statistical Uncertainty	19.6	9.9
Total	20.68	11.23

Table: Summary of uncertainties evaluated on MC.

- The overall uncertainties are still dominated by statistics.

# Systematic uncertainty due to $\mathcal{B}(B \rightarrow D^{**}(l/\tau)\nu)$

- Generally,  $D^{**}$  is defined as any excited charmed meson states that is not in the 1S ground state. The following possibilities are considered in this analysis:
  - Resonant  $D^{**}(1P)$  state: four lightest orbitally excited states  $D_0^*(2400)$ ,  $D_1'(2430)$ ,  $D_1(2420)$ ,  $D_2^*(2460)$ .
  - Resonant  $D^{**}(2S)$  state: radially-excited modes.
  - Non-resonant  $B \rightarrow D^{**}(l/\tau)\nu$  where  $D^{**} \rightarrow D^{(*)}\pi$
- Some uncertainties from  $\mathcal{B}(B \rightarrow D^{**}\tau\nu)$  are estimated using phase space model:

$$\mathcal{R}(D^{**}) = \frac{\mathcal{B}(\bar{B} \rightarrow D^{**}\tau^-\bar{\nu}_\tau)}{\mathcal{B}(\bar{B} \rightarrow D^{**}l^-\bar{\nu}_l)} \approx \frac{\Phi(\bar{B} \rightarrow D^{**}\tau^-\bar{\nu}_\tau)}{\Phi(\bar{B} \rightarrow D^{**}l^-\bar{\nu}_l)}$$

# Conclusion

- A measurement of  $R(D^{(*)})$  from *BABAR* after a decade.
- *BABAR*'s first  $R(D^{(*)})$  measurement using semileptonic  $B$ -tagging method and leptonic  $\tau$  decays.
- Developed a new measurement method, more data-driven during signal extraction.
- The analysis is currently under internal review.

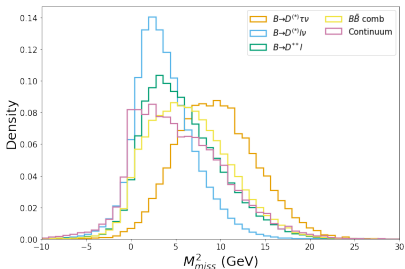
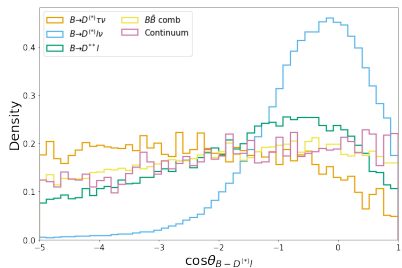
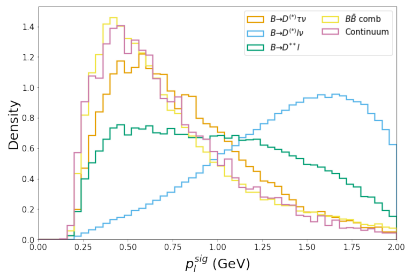
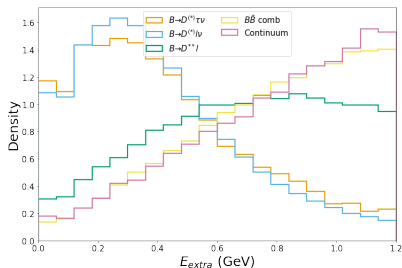
**Thanks for your attention!**

# Event types definition for the measurement

Event type		Description
Signal event	signal $D$	One $B$ decays to $D^{(*)}l\nu$ , the other $B$ decays to $D\tau\nu$ , $\tau \rightarrow$ leptons
	signal $D^*$	One $B$ decays to $D^{(*)}l\nu$ , the other $B$ decays to $D^*\tau\nu$ , $\tau \rightarrow$ leptons
Normalization event	norm $D$	One $B$ decays to $D^{(*)}l\nu$ , the other $B$ decays to $Dl\nu$
	norm $D^*$	Both $B$ decay to $D^*l\nu$
$D^{**}$ event		At least one $B$ decays to $D^{**}(l/\tau)\nu$ , where $D^{**}$ includes $1P$ states $D_0^*, D_1, D_1', D_2^*$ , $2S$ states, and non-resonant states.
combinatorial $BB$ event		Any $BB$ events that are not signal and not normalization and not $D^{**}$ .
Continuum event		non- $BB$ events produced in the detector

Table: Definition of event types in the  $B$ -factory system.

# Distribution of selected variables



# Maximum likelihood estimation details

For the  $D^+l$  subset, the distribution is combination of signal, signal feed-down, normalization, normalization feed-down,  $B \rightarrow D^{**}l\nu$ ,  $B\bar{B}$  combinatorial and continuum events:

$$\begin{aligned} f(z_1, z_2) = & N_{B \rightarrow D\tau\nu} f_{B \rightarrow D\tau\nu}(z_1, z_2) + N_{B \rightarrow D^*\tau\nu} f_{B \rightarrow D^*\tau\nu}(z_1, z_2) \\ & + N_{B \rightarrow Dl\nu} f_{B \rightarrow Dl\nu}(z_1, z_2) + N_{B \rightarrow D^*l\nu} f_{B \rightarrow D^*l\nu}(z_1, z_2) \\ & + N_{B \rightarrow D^{**}l\nu} f_{B \rightarrow D^{**}l\nu}(z_1, z_2) + N_{\text{Other Bkgs}} f_{\text{Other Bkgs}}(z_1, z_2) \end{aligned} \quad (2)$$