

MInternational UON Collider Collaboration



# Muon Collider

D. Schulte for the International Muon Collider Collaboration

ICHEP July 2022

# Introduction

Muon Collider, ICHEP, July 2022

Previous studies in US (now very strong interest again), experimental programme in UK and alternatives studies by INFN

New strong interest:

- Focus on high energy
  - 10+ TeV
  - potential initial energy stage

D. Schulte

• Technology and design advanced

New collaboration started

Initial integrated luminosity targets

- could be reached in 5 years
- to be refined with physics studies



#### **Discovery reach**

14 TeV lepton collisions are comparable to 100-200 TeV proton collisions for production of heavy particle pairs





# **Collider Overview**

MInternational UON Collider Collaboration

Would be easy if the muons did not decay Lifetime is  $\tau = \gamma \times 2.2 \ \mu s$ 



Short, intense proton bunch Protons produce decay into muor muons are captu			Ionisatic muon in	on cooling of matter	Acceleration to o energy	collision	Collision
		produce pion ito muons are captured	s which				
		D. Schulte	Μ	luon Collider, ICHEP, July	/ 2022		

## **Sustainability**



CLIC is highest energy proposal with CDR

- No obvious way to further improve linear colliders (decades of R&D)
- Cost 18 GCHF, power 590 MW

Rough rule of thumb:

- cost proportional to energy
- power proportional to luminosity .

Muon Collider challenging but reasonable goals (10 TeV):

- Much more luminosity (L=20x10<sup>34</sup>, CLIC: L=2x10<sup>34</sup>/6x10<sup>34</sup>)
- Lower power consumption than CLIC at 3 TeV (P<sub>beam.MC</sub>=0.5P<sub>beam.CLIC</sub>)
- Lower cost

Staging is possible

Synergies exist (neutrino/higgs)

Unique opportunity for a **high-energy**, **high-luminosity lepton collider** 



D. Schulte

# **Initial Target Parameters**



ranget integrated furnitosities						
$\sqrt{s}$	$\int \mathcal{L} dt$					
3 TeV	$1 {\rm ~ab^{-1}}$					
$10 { m TeV}$	$10 {\rm ~ab^{-1}}$					
$14 { m TeV}$	$20 {\rm ~ab^{-1}}$					

Target integrated luminosities

Note: currently focus on 10 TeV, also explore 3 TeV

- Tentative parameters based on MAP study, might add margins
- Achieve goal in 5 years
- FCC-hh to operate for 25 years

D. Schulte

• Aim to have two detectors

Parameter	Unit	3 TeV	10 TeV	14 TeV	CLIC at 3 TeV
L	10 <sup>34</sup> cm <sup>-2</sup> s <sup>-1</sup>	1.8	20	40	2 (6)
N	<b>10</b> <sup>12</sup>	2.2	1.8	1.8	
f <sub>r</sub>	Hz	5	5	5	
P <sub>beam</sub>	MW	5.3	14.4	20	28 MW
С	km	4.5	10	14	
<b></b>	т	7	10.5	10.5	
ε <sub>L</sub>	MeV m	7.5	7.5	7.5	
σ <sub>E</sub> / Ε	%	0.1	0.1	0.1	
σ <sub>z</sub>	mm	5	1.5	1.07	
β	mm	5	1.5	1.07	
3	μm	25	25	25	
$\sigma_{x,y}$	μm	3.0	0.9	0.63	
Muc	on Collider, ICHEP	, July 2022		a contraction of the	

## Accelerator R&D Roadmap

Label



Aspirational

On request by Council LDG develop R&D Roadmap

- global community participated
- a global roadmap
- with estimates of required resources

No obstacle found for the muon collider

but important need for R&D

#### Council asked for implementation plan

We are trying to secure resources

Scenario	FTEy	M MCHF
Full scenario	445.9	11.9
Reduced scenario	193	2.45

D. Schulte

#### http://arxiv.org/abs/2201.07895

				[FTEy] [kCHF] [F]		[FTEy]	[kCHF]
MC.SITE	2021	2025	Site and layout	15.5	300	13.5	300
MC.NF	2022	2026	Neutrino flux miti-	22.5	250	0	0
			gation system				
MC.MDI	2021	2025	Machine-detector	15	0	15	0
			interface				
MC.ACC.CR	2022	2025	Collider ring	10	0	10	0
MC.ACC.HE	2022	2025	High-energy com-	11	0	7.5	0
			plex				
MC.ACC.MC	2021	2025	Muon cooling sys-	47	0	22	0
			tems				
MC.ACC.P	2022	2026	Proton complex	26	0	3.5	0
MC.ACC.COLL	2022	2025	Collective effects	18.2	0	18.2	0
			across complex				
MC.ACC.ALT	2022	2025	High-energy alter-	11.7	0	0	0
			natives				
MC.HFM.HE	2022	2025	High-field magnets	6.5	0	6.5	0
MC.HFM.SOL	2022	2026	High-field	76	2700	29	0
			solenoids				
MC.FR	2021	2026	Fast-ramping mag-	27.5	1020	22.5	520
			net system				
MC.RF.HE	2021	2026	High Energy com-	10.6	0	7.6	0
			plex RF				
MC.RF.MC	2022	2026	Muon cooling RF	13.6	0	7	0
MC.RF.TS	2024	2026	RF test stand + test	10	3300	0	0
			cavities				
MC.MOD	2022	2026	Muon cooling test	17.7	400	4.9	100
			module				
MC.DEM	2022	2026	Cooling demon- 34.1		1250	3.8	250
			strator design	60	1.10.5	0	
MCTAR	2022	2026	Target system	60	1405	9	25
MC.INT	2022	2026	Coordination and	13	1250	13	1250
			integration				
	1		Sum	445.9	11875	193	2445

Begin End Description

Table 5.5: The resource requirements for the two scenarios. The personnel estimate is given in full-time equivalent years and the material in kCHF. It should be noted that the personnel contains a significant number of PhD students. Material budgets do not include budget for travel, personal IT equipment and similar costs. Colours are included for comparison with the resource profile Fig. 5.7.

# Timeline

Goals for next strategy

- Assessment report
- R&D plan ready for implementation

Prudently explore if MuC can be option as next project (i.e. operation mid 2040s)

- e.g. in Europe if higgs factory built elsewhere
- very strong ramp-up required after 2026
- some compromises on initial performance



D. Schulte Muon Collider, ICHEP, July 2022





# Target





# **Muon Cooling**



# **Cooling Cell Technology**

C. Marchand, Alexej Grudiev et al. (CEA, Milano, CERN, Tartu)

#### MAP demonstrated 30 T solenoid

- now magnets aim for 40+ T
- even more can be possible
- synergy with high-field research



L. Bottura et al. INFN (Task Leader), CEA, CERN, LNCMI, PSI, SOTON, UNIGE and TWENTE, in collaboration with KEK and **US-MDP** 

D. Schulte

#### **RF** cavities

Will develop **cooling cell** 

tight constraints

instrumentation,...)

early preparation of

J. Ferreira Somoza et al.

demonstrator facility

(absorbers,

additional technologies

integration

MAP demonstrated higher than goal gradient Improve design based on theoretical understanding

Preparation of new experiments

- Test stand at CEA (700 MHz, need funding)
- Test at other frequencies in the UK considered
- Use of CLIC breakdown experiment considered



🛕 International JON Collider ollaboration



# **Acceleration Complex**

Muon Collider, ICHEP, July 2022



D. Schulte



L. Bottura et al. (LNCMI, Darmstadt,

#### **Alternative FFA**



# **Collider Ring**



MAP developed 4.5 km ring for 3 TeV with Nb<sub>3</sub>Sn

- magnet specifications in the HL-LHC range
- 5 mm beta-function at IP

Work on 10 km ring for 10 TeV collider ring

- around 16 T Nb<sub>3</sub>Sn or HTS dipole field around 15 cm
- final focus based on HTS

designs

1.5 mm beta-function at IP •

15 cm aperture for Shielding Energy density per bunch crossing (mJ/cm<sup>3</sup>)  $10^{0}$ shielding to ensure  $10^{-1}$ A. Lechner 20 10<sup>-2</sup> magnet lifetime D. Calzolari 10<sup>-3</sup> 10  $10^{-4}$ (CERN) 10<sup>-5</sup> Need stress 10<sup>-6</sup> Coil -10 managed magnet 10<sup>-7</sup> 10<sup>-8</sup> WEPOST001 10<sup>-9</sup> INFN, Milano, Kyoto, -30 -20 -10 0 10 20 30 CERN, profit from US x (cm) D. Schulte



## Field choice will be reviewed for cost Example alternatives:

- a 6 km 3 TeV ring with **NbTi** at 8 T in arcs
- a 15 km 10 TeV ring with HL-LHC • performances
- slight reduction in luminosity

# **Other Key Studies**



### Review proton complex

- average power of 2 MW is no problem
- but merging into 5 pulses of 400 kJ per second needs to be verified

Collective effects across the whole complex to identify bottlenecks

- review apertures, feedback and other specifications
  - first results for aperture requirements
- potential instability of interaction of muon beam with matter

### Power and cost optimisation

Vacuum and absorber, instrumentation, cryogenics, ...

Reuse of existing infrastructure, e.g. LHC tunnel to house accelerator

N. Milas et al. (ESS, Uppsala)

E. Metral et al. (CERN, EPFL/ CHART)

J. Ferreira Somoza, M. Wendt, et al.

D. Schulte



## **Demonstrator Facility Consideration**

Planning **demonstrator** facility with muon production target and cooling stations

Suitable site exists on CERN land and can use PS proton beam

could combine with NuStorm or other option

Other sites should be explored (FNAL?)





D. Schulte

# Key Next Steps

Muon Collider, ICHEP, July 2022



Turn the Roadmap into an evolving workplan

- adjusting to priorities and resources
- Securing resources
- In different institutes
- Request to national funding
- EU Design Study proposal submitted
- EU technology study planned for next call

D. Schulte

• US Snowmass/P5 process

1 Collider **CERN** Council poration Other regional body LDG \_\_\_\_\_ **ICB** SB IAC Cordination Committee Proton **Physics** Magnets Demonstr. US acc. Complex Detector Muon RF Ц Cool. cell US det. prod./cool and MDI **Beam-matter** Asia acc. Accelerat. target techn. Collider. Ц Coll. eff. Asia det. site/NF

But are already working

...

# MoC and Design Study Partners



al ۶r

IEIO CERN	UK	STFC-RAL	PT	LIP
FR CEA		UK Research and Innovation	NL	University of Twente
CNRS-LNCMI		University of Lancaster	FI	Tampere University
DE DESY		University of Southampton	US	Iowa State University
Technical University of		University of Strathclyde		BNL
		University of Sussex	China	Sun Yat-sen University
		Imperial College		IHEP
		Royal Holloway		Peking University
		University of Huddersfield	EST	Tartu University
University of Milano		University of Oxford	LAT	Riga Technical Univers.
University of Padova			AU	НЕРНҮ
University of Pavia		University of warwick	FS	13W
University of Bologna	SE	ESS	LU	IJW
ENEA		University of Uppsala	CHART is	s contributing (and EPFL)
CH PSI			mornar	
University of Geneva			Note: sor	me MoC still being prcessed
D. Schulte		Muon Collider. ICHEP. July 2022		

# Conclusion

- MInternational UON Collider Collaboration
- Muon collider is unique opportunity for high-energy, high-luminosity lepton collider
- Currently two different options considered
  - goal of 10+ TeV
  - potential 3 TeV intermediate stage explored
  - will consider other options later
- Need to turn Roadmap into a workplan to change this
- Important activities have started
- First important results are already obtained

http://muoncollider.web.cern.ch

Many thanks to the Muon Beam Panel, the collaboration, the MAP study, the MICE collaboration, and many others



## Reserve



D. Schulte

# Alternatives: The LEMMA Scheme







$$e^+e^- \to \mu^+\mu^-$$

### Excellent idea, but nature is cruel

Detailed estimates of fundamental limits show that we require a very large positron bunch charge to reach the same luminosity as the proton-based scheme

 $\Rightarrow$  Need same game changing invention

D. Schulte

Muon Collider, ICHEP, July 2022

Note: New proposal by C. Curatolo and L. Serafini needs to be looked at

Uses Bethe-Heitler production with electrons



# **MICE:** Cooling Demonstration

7th February 2015



D. Schulte



More particles at smaller amplitude after absorber is put in place

Principle of ionisation cooling has been demonstrated Use of data for benchmarking is still ongoing

WEPOPT053

Muon Collider, ICHEP, July 2022



🖌 International

UON Collider

Nature vol. 578, p. 53-59 (2020)

More complete experiment with higher statistics, more than one stage required

Integration of magnets, RF, absorbers, vacuum is engineering challenge

## Neutrino Flux



Dense neutrino flux cone can impact environment Challenge scales with **E x L** 

Goal is to reduce to negligible level, similar to LHC

• 3 TeV, 200 m deep tunnel is about OK

Expand idea of Mokhov, Ginneken to move beam in aperture: move collider ring components, e.g. vertical bending with 1% of main field

- 14 TeV, in 200 m deep tunnel comparable to LHC case with +/- 1 mradian
- scales with luminosity toward higher E

Need to study mover system, magnet, connections and impact on beam

Working on different approaches for experimental insertion

D. Schulte





Other optimisations are possible (magnetic field, emittance etc.)

# **Machine-Detector Interface**



#### Main background sources

- Muon decay products (40,000 muons/m/crossing at 14 TeV)
- Beam-beam background
- Note: background reduces while beam burns off



#### Mitigation methods

- masks
- detector granularity
- detector timing (background out of time)
- track direction (background from wrong vertices)
- event reconstruction strategies
- ...

### Active study of background is ongoing

- Encouraging results at 1.5 and 3 TeV
- 10 TeV studies started, lower rate of loss
- Beam-beam started
- started to study impact of lattice design

**ICHEP** 

D. Lucchesi, A. Lechner, C Carli et al.

D. Schulte Muon Collid

# Muon Decay



About 1/3 of energy in electrons and positrons: **Experiments** needs to be protected from **background** by masks

- simulations of 1.5, 3 and 10 TeV
- optimisation of masks and lattice design
- first results look encouraging
- will be discussed at ICHEP

**Collider ring magnets** need to be shielded from losses Losses elsewhere will also need to be considered but are less severe



ICHEP

D. Lucchesi, A. Lechner, C Carli et al.

Neutrino flux to have negligible impact on environment

- want to be **negligible**
- opening cone decreases with energy
- cross section and shower energy increase with energy
- need to do something above around 3 TeV



D. Schulte



Mover system and impact on beam will be addressed in the coming years before end if 2025

D. Schulte

# **Collider Ring**



**MOPOTK031** 

Three considerations:

- luminosity is proportional to average magnetic field
- muon beam decay requires larger apertures (O(15cm)
- very small beta-function at IP required

MAP developed 3 TeV with Nb<sub>3</sub>Sn magnets and 4.5 km circumference

magnet specifications in the HL-LHC range

Work on 10 TeV collider ring with 10 km circumference and either Nb<sub>3</sub>Sn or HTS magnets

D. Schulte

- around 16 T dipole field aperture around 15 cm
- final focus based on HTS

### **Option**:

at 3 TeV, **NbTi** with 8 T in arcs could fit in 6 km ring, slight decrease of L =  $1.35 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$ , could be at 10 TeV, use of HL-LHC performances would lead to 15 km ring and L= $13 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$ 

Muon Collider, ICHEP, July 2022



C. Carli et al.

# **Collider Ring**

Muon beam decay produces high-energy electrons and positrons (1/3 of beam power, 500 W/m)

- need to shield magnets  $\Rightarrow$
- Mokhov et al. showed shielding to 1% at 3 TeV with 30-50mm ⇒ shielding
- new study at 10 TeV shows that radiation dose is OK with 30 mm shielding, similar to 3 TeV

Cooling power required at 10 TeV for 2 K 700 x 0.01 x 1/3 x 14 MW = 33 MW 70 x 0.01 x 1/3 x 14 MW = 3.3 MW for 20 K

Magnets require stress management

L. Bottura et al.



D. Schulte

# **Cooling Principle**



# **Cooling Principle**



## Cooling Principle and Demonstration





WEPOPT053





D. Schulte

# Thanks



**Muon Beam Panel:** Daniel Schulte (CERN, chair), Mark Palmer (BNL, co-chair), Tabea Arndt (KIT), Antoine Chance (CEA/ IRFU) Jean-Pierre Delahaye (retired), Angeles Faus-Golfe (IN2P3/IJClab), Simone Gilardoni (CERN), Philippe Lebrun (European Scientific Institute), Ken Long (Imperial College London), Elias Metral (CERN), Nadia Pastrone (INFN-Torino), Lionel Quettier (CEA/IRFU), Magnet Panel link, Tor Raubenheimer (SLAC), Chris Rogers (STFC-RAL), Mike Seidel (EPFL and PSI), Diktys Stratakis (FNAL), Akira Yamamoto (KEK and CERN) **Contributors:** Alexej Grudiev (CERN), Roberto Losito (CERN), Donatella Lucchesi (INFN)

**Community conveners:** *Radio-Frequency (RF)*: Alexej Grudiev (CERN), Jean-Pierre Delahaye (CERN retiree), Derun Li (LBNL), Akira Yamamoto (KEK). *Magnets:* Lionel Quettier (CEA), Toru Ogitsu (KEK); Soren Prestemon (LBNL), Sasha Zlobin (FNAL), Emanuela Barzi (FNAL). *High-Energy Complex (HEC)*: Antoine Chance (CEA), J. Scott Berg (BNL), Alex Bogacz (JLAB), Christian Carli (CERN), Angeles Faus-Golfe (IJCLab), Eliana Gianfelice-Wendt (FNAL), Shinji Machida (RAL). *Muon Production and Cooling (MPC)*: Chris Rogers (RAL), Marco Calviani (CERN), Chris Densham (RAL), Diktys Stratakis (FNAL), Akira Sato (Osaka University), Katsuya Yonehara (FNAL). *Proton Complex (PC)*: Simone Gilardoni (CERN), Hannes Bartosik (CERN), Frank Gerigk (CERN), Natalia Milas (ESS). *Beam Dynamics (BD)*: Elias Metral (CERN), Tor Raubenheimer (SLAC and Stanford University), Rob Ryne (LBNL). *Radiation Protection (RP)*: Claudia Ahdida (CERN). *Parameters, Power and Cost (PPC)*: Daniel Schulte (CERN), Mark Palmer (BNL), Jean-Pierre Delahaye (CERN retiree), Philippe Lebrun (CERN retiree and ESI), Mike Seidel (PSI), Vladimir Shiltsev (FNAL), Jingyu Tang (IHEP), Akira Yamamoto (KEK). *Machine Detector Interface (MDI)*: Donatella Lucchesi (University of Padova), Christian Carli (CERN), Anton Lechner (CERN), Nicolai Mokhov (FNAL), Nadia Pastrone (INFN), Sergo R Jindariani (FNAL). *Synergy*: Kenneth Long (Imperial College), Roger Ruber (Uppsala University), Koichiro Shimomura (KEK). *Test Facility (TF)*: Roberto Losito (CERN), Alan Bross (FNAL), Tord Ekelof (ESS,Uppsala University).

### And the participants to the community meetings and the study

# Muon Decay



About 1/3 of energy in electrons and positrons: **Experiments** needs to be protected from **background** by masks

- simulations of 1.5, 3 and 10 TeV
- optimisation of masks and lattice design started
- first results look encouraging
- will be discussed at ICHEP

**Collider ring magnets** need to be shielded from losses Losses elsewhere will also need to be considered but are less severe



Donatella, ICHEP

D. Lucchesi, A. Lechner, C Carli et al.

Neutrino flux to have negligible impact on environment

- want to be **negligible** (same level as LHC)
- opening cone decreases, cross section and shower energy increase with energy
- Above about 3 TeV need to make beam point in different vertical directions
- Mechanical system with 15cm stroke, 1% vertical bending
- Length of pattern to be optimised for minimal impact on beam

D. Schulte



# Neutrino Flux



E\_10

8000

9000



D. Schulte

# **Acceleration Complex**





Recirculating linacs Sequence of rings

- baseline: pulsed synchrotron (RCS)
- alternative: FFA

#### Alternative FFA

- Fixed (high-field) magnets but large energy acceptance
- Challenging lattice design for large bandwidth and limited cost
- Complex high-field magnets
- Challenging beam dynamics



**Hybrid RCS** combines static superconducting magnets and fast-ramping normal-conducting magnets



D. Schulte

MAP study S. Berg et al.



Test of fast-ramping normal-conducting magnet design

MAP study

# **RCS Challenge**



RCS is probably the main cost driver and could be substantial power user

Numbers for illustration, are subject to optimisation

Studies started on the key challenges:

- Longitudinal dynamics along whole complex and RF system
  - distribution around ring, frequency choice
- Lattice design
  - energy swing, path length control, distribution of RF,
- Fast-ramping magnets and power converter system
  - cost of stored energy seems OK, cost of ramp shaping to be developed with RF experts

Need to match ramping speed of magnets with accelerating RF

D. Schulte

- Integrated design optimisation is needed
- Energy recovery from pulse to pulse is critical

Param.	unit	RCS 1	RCS 2	RCS 3
E	GeV	60-300	300-1500	1500-5000
С	km	2.8	13.8	35
<g></g>	MV/m	2	2	1
turns		44	44	95
T <sub>ramp</sub>	ms	0.4	2	11.67
dB/dt	kT/s	10	2	0.34
E <sub>ramp</sub>	MJ	6.4	32	93.3

Lattice and integration: A. Chance et al. (CEA) Long. dynamics and RF systems: H. Damerell, F. Batsch, U. van Rienen, A. Grudiev et al. (Rostock, Milano, CERN) Power converter: F. Boattini et al. Magnets: L. Bottura et al. (LNCMI, Darmstadt, Bologna, Twente)

Muon Collider, IC

## **Sustainability**



**CLIC** 

D. Schulte

CLIC is highest energy proposal with CDR

- at the limit of what one can do (decades of R&D)
- No obvious way to further improve linear . colldiers
- Cost 18 GCHF, power 590 MW .

MC 3 TeV

LHC

#### **Muon Collider:**

Acceleration and collision in multiple turns in rings promises

- **Power efficiency** •
- Compact tunnels, 10 TeV similar to 3 TeV CLIC
- **Cost effectiveness** •
- Natural staging is natural Synergies exist (neutrino/higgs) Unique opportunity for a high-energy, high-luminosity lepton collider

![](_page_36_Picture_13.jpeg)

![](_page_36_Picture_14.jpeg)

# **Cooling Principle**

![](_page_37_Figure_1.jpeg)

![](_page_37_Figure_2.jpeg)

![](_page_37_Figure_3.jpeg)

Nature vol. 578, p. 53-59 (2020)

**MuCool**: demonstrated cavity with >50 MV/m in 5 T solenoid

- H2-filled copper cavities
- Cavities with Be end caps

![](_page_37_Picture_8.jpeg)

Principle of ionisation cooling with no RF has been demonstrated in **MICE at RAL** Use of data for benchmarking is still ongoing

Need to develop full cooling demonstrator

Time-of-flight

hodoscope 1

(ToF 0)

Cherenkov counters (CKOV)

Muor

Bean

MICF

D. Schulte

wuon comuer, ICHEP, July 2022

# **Emittance Development**

![](_page_38_Picture_1.jpeg)

MAP designs almost achieve 10 TeV goal

• miss factor two for final cooling

Work on improvement of **final cooling** by design and improved solenoid

- lower beam energy helps
- higher solenoid field helps

![](_page_38_Picture_7.jpeg)

MAP design with demonstrated 30 T solenoid

- now magnets aim for 40+ T
- even more can be possible
- synergy with high-field research

#### L. Bottura et al.

INFN (Task Leader), CEA, CERN, LNCMI, PSI, SOTON, UNIGE and TWENTE, in collaboration with KEK and US-MDP

WEPOMS046

WEPOMS047

![](_page_38_Figure_14.jpeg)

## **Integration/optimisation** of overall cooling design, also considering integrating improved technology

HTS has synergies with power applications

C. Rogers et al.

# **Cooling Cell Technology**

![](_page_39_Picture_1.jpeg)

### **RF** cavities

Improve design based on theoretical understanding

### Preparation of new experiments

- Test stand at CEA (700 MHz, need funding)
- Test at other frequencies in the UK considered
- Use of CLIC breakdown experiment considered

C. Marchand, Alexej Grudiev et al. (CEA, Milano, CERN, Tartu)

### Will develop cooling cell integration

- tight constraints
- additional technologies (absorbers, instrumentation,...)

D. Schulle

- early preparation of demonstrator facility
  - L. Rossi et al. (INFN, Milano, STFC, CERN)
  - J. Ferreira Somoza et al.

### Consider HTS solenoids for 6D cooling

![](_page_39_Figure_17.jpeg)