The CYGNUS Galactic Directional Recoil Observatory



*Natural radioactivity recorded by the LIME detector at LNGS

or else, how to surf the neutrino fog with directionality



Elisabetta Baracchini



on behalf of the CYGNUS proto-collaboration





Outline



- The need (now more than ever) for a directional DM detector at the ton scale
- The CYGNUS project for a Galactic Directional Recoil Observatory
 - Feasibility studies for WIMP searches through nuclear recoils (arXiv:2008.12587)
 - Solar neutrinos through electron recoils physics case
- TPCs projects in the world and R&Ds towards CYGNUS

From neutrino floor to neutrino fog



D. S. Akerib et al., 2022 Snowmass Summer Study, arXiv:2203.08084

Discovery limit as function of the observed N neutrino background events and uncertainty δΦ on neutrino fluxes

Background free

$$N < 1, \sigma \propto 1/N$$

Poissonian background subtraction

$$N\delta\Phi^2\ll 1,\sigma\propto 1/\sqrt{N}$$

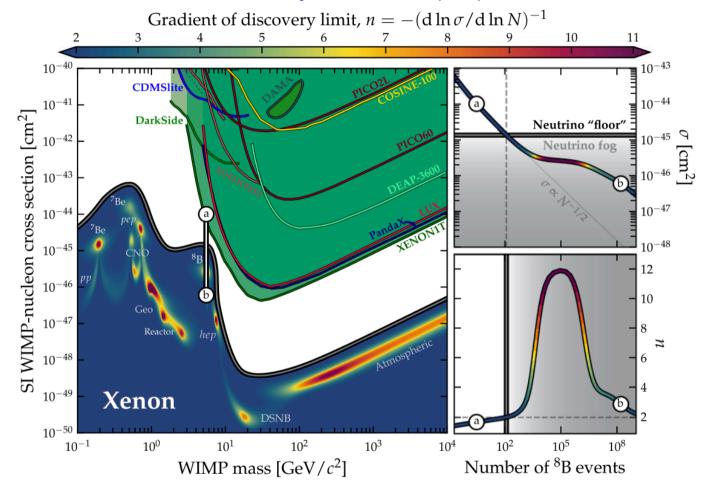
Purely dominated by systematics

$$N\delta\Phi^2\gg 1, \sigma\propto \sqrt{(1+N\delta\Phi^2)/N}$$

- $\Im n$ is defined so that n = 2 under normal Poissonian subtraction, and n > 2 when there is saturation
 - From The value of the cross section σ at which n crosses 2 is defined as the neutrino floor.

$$n = - \Big(\frac{d\log\sigma}{d\log MT}\Big)^{-1}$$

C. A. J. O'Hare, Phys. Rev. Lett. 127 (2021) 25, 251802



Reducing the sensivity of an experiment by a factor x requires an increas in the exposure by $at least x^n$

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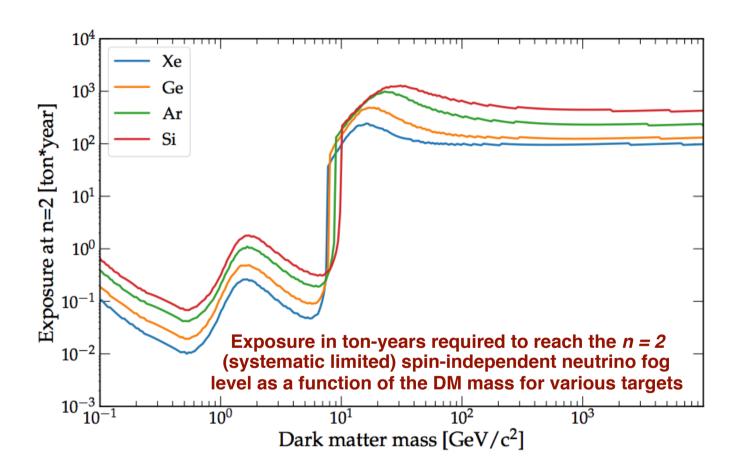
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 - Fig. The value of the cross section σ at which n crosses 2 is defined as the neutrino floor.

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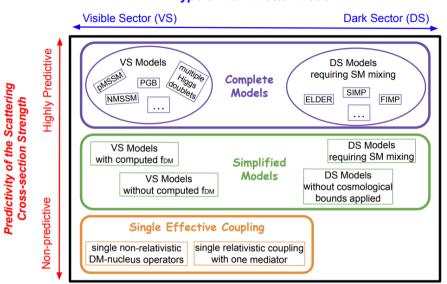
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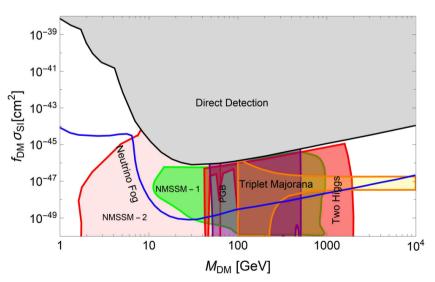


The need to penetrate the fog

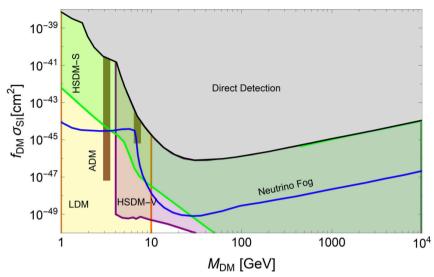




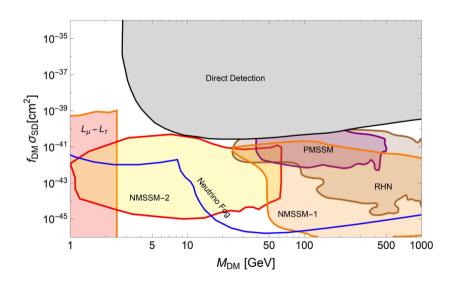




Visible sector models SI



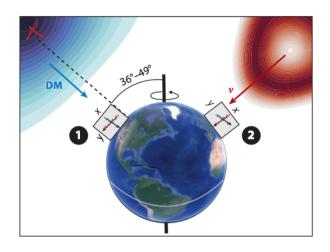
Dark sector models SI

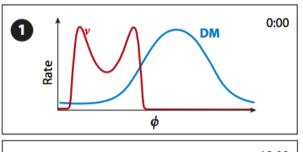


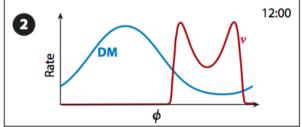
Visible sector models SD

How to see through the neutrino fog?

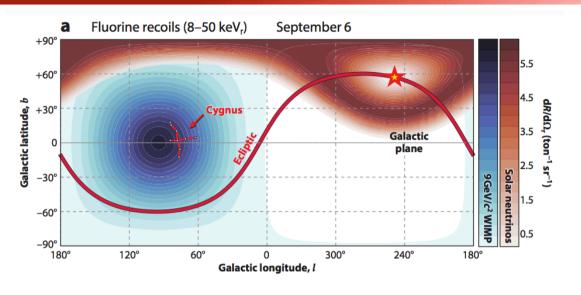




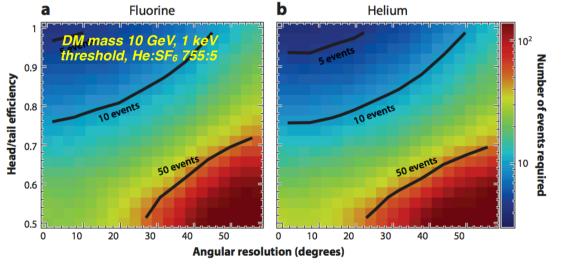




DM and solar neutrinos event rate as a function of some angle φ on a twodimensional readout plane at 12 h time distance or 180° of longitude



Required number of detected He and F recoils to exclude solar neutrinos at 90% C.L. vs angular resolution and head-tail efficiency

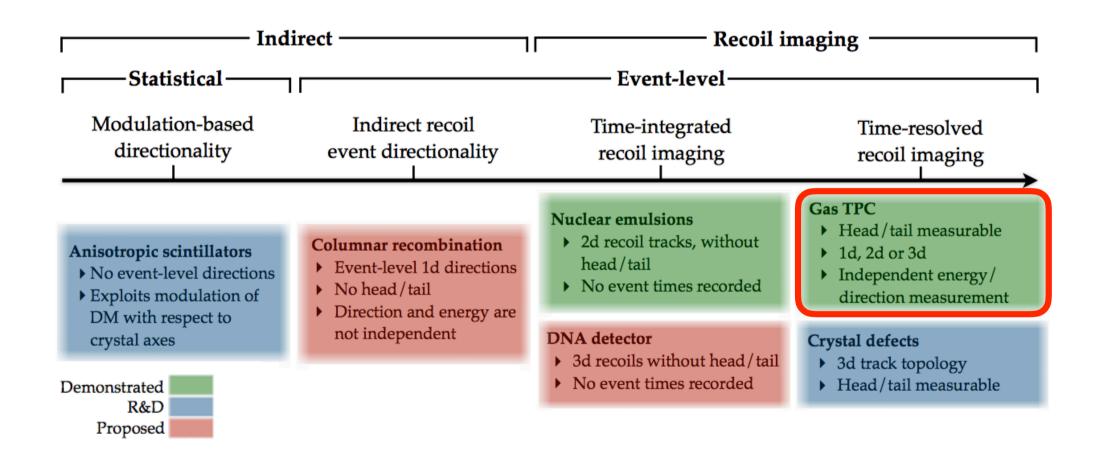


Take away message: head-tail is more important than angular resolution



Detector classes by directional information





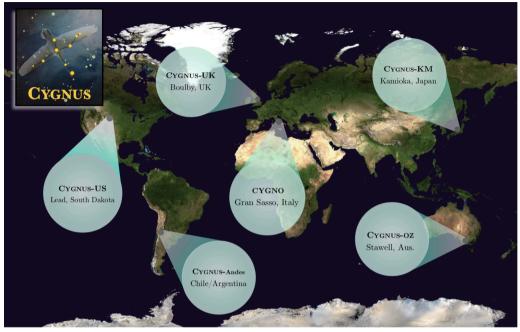
We believe gaseous TPC to be the best experimental approach because it can provide the best observables not only for DM searches but for multiple physics cases



The CYGNUS project

CYGNUS proto-collaboration





- About 70 members
- Steering group:
 - Elisabetta Baracchini (GSSI/INFN, Italy)
 - Greg Lane (Canberra, Australia)
 - Kentaro Miuchi (Kobe, Japan)
 - ♥Neil Spooner (Sheffield, UK)
 - Sven Vahsen (Hawaii, USA)









A multi-site, multi-target Galactic Nuclear and Electron Recoil Observatory at the ton-scale to probe Dark Matter below the Neutrino Floor and measure solar Neutrinos with directionality

Helium/Fluorine gas mixtures at 1 bar

- Sensitivity to O(GeV) WIMP for both SI & SD couplings
- Possibility of switching between higher (search mode) and lower gas densities (improved directionality) for signal confirmation

Reduced diffusion

- Through negative ion drift or "cold" gases (CF₄)
- 3D fiducialization
 - Through minority carriers or fit to diffusion
- Directional threshold at O(keV)
- Full background rejection at O(keV)
- Both electronic and optical charge readout investigated

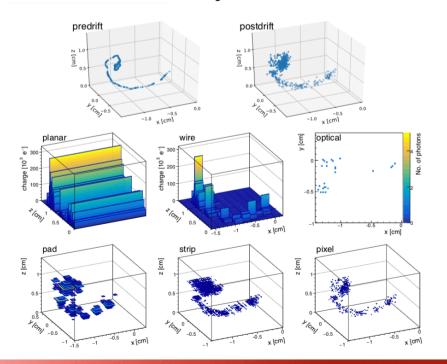
arXiv: 2008.12587 Cygnus: Feasibility of a nuclear recoil observatory with directional sensitivity to dark matter and neutrinos

S. E. Vahsen, ¹ C. A. J. O'Hare, ² W. A. Lynch, ³ N. J. C. Spooner, ³ E. Baracchini, ^{4,5,6} P. Barbeau, ⁷ J. B. R. Battat, ⁸ B. Crow, ¹ C. Deaconu, ⁹ C. Eldridge, ³ A. C. Ezeribe, ³ M. Ghrear, ¹ D. Loomba, ¹⁰ K. J. Mack, ¹¹ K. Miuchi, ¹² F. M. Mouton, ³ N. S. Phan, ¹³ K. Scholberg, ⁷ and T. N. Thorpe^{1,6}

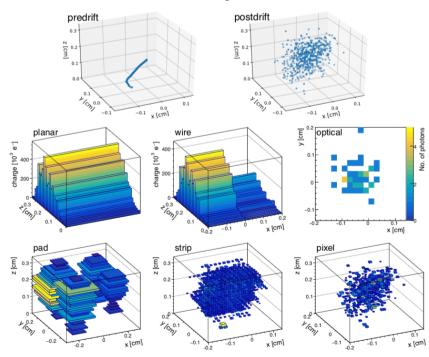


- Extensive concept paper on 1000 m³ gaseous NITPC detector focused on technical feasibility and WIMP searches through nuclear recoils
- Detailed simulation of seven readout options with negative ion drift in He:SF₆ at 1 atm
 with a cost/benefit FOM
- Background discrimination studies
- Detailed simulation and study of all internal and external backgrounds
- Engineering studies for a 1000 m³ detector

20 keV_{ee} electron recoil in He:SF₆ 740:20 Torr



20 keV_{nr} Helium nuclear recoil in He:SF₆ 740:20 Torr





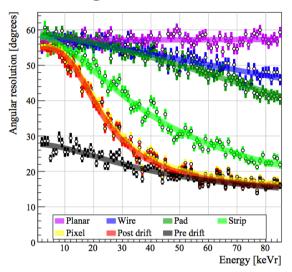
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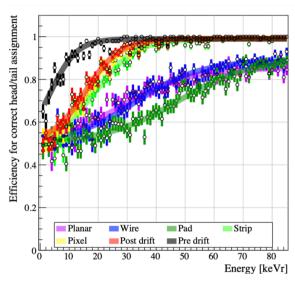
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Angular resolution



Sense recognition



Negative ion drift in He:SF₆ 755:5 Torr

Pixels extract the entire directional information left after diffusion

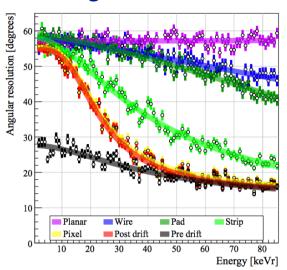
Strips readout perform almost as pixels, but at much lower costs

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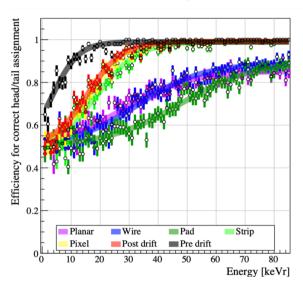
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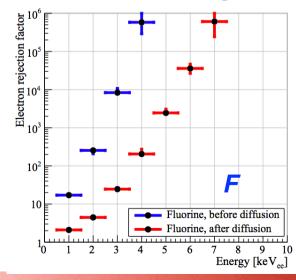


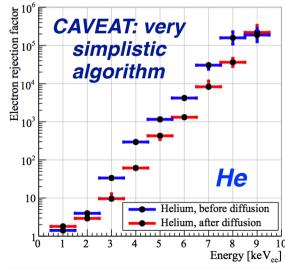
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Background rejection





Rejection at O (keV_{nr}) possible, > 10⁶ @ 10 keV_{nr}

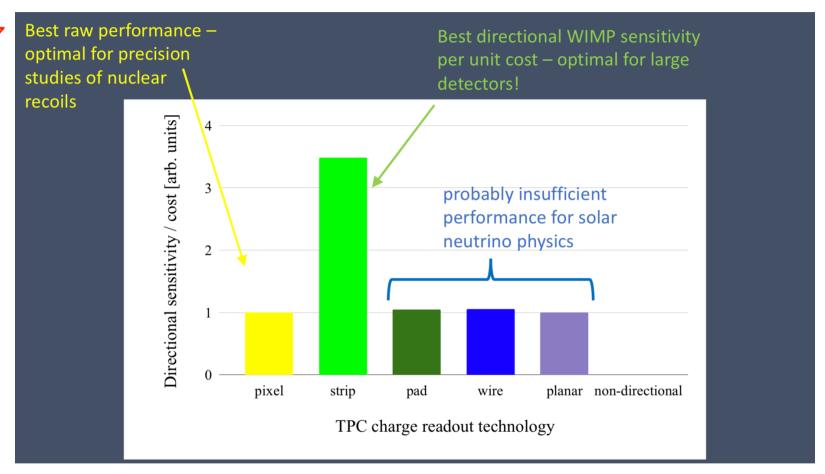
Can be sigificantly improved by combination of more variables (x 100 with HD readout arXiv: 2012.13649) or machine learning approach (under development)



Cost vs benefit study result



arXiv: 2008.12587



For He:SF₆ 755:5 with negative ion drift, strips results the best choice in terms of costs versus performances, radiation budget and engineering cosiderations

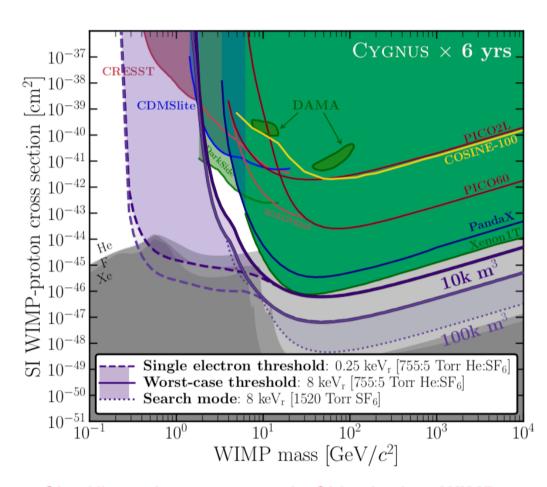
Cost benefit study and gas optimisation for electron drift with both charge and optical readout under development



S CYGNUS 1 ton WIMP searches expected sensitivity



He:SF₆ 755:5



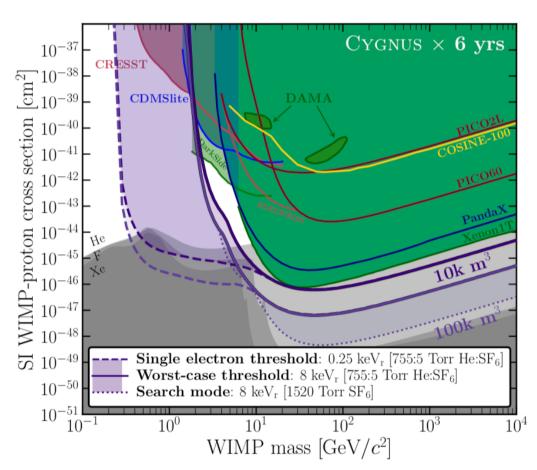
Significant improvement in SI in the low WIMP mass region, expect 10-50 IDENTIFIED neutrino nuclear recoil events



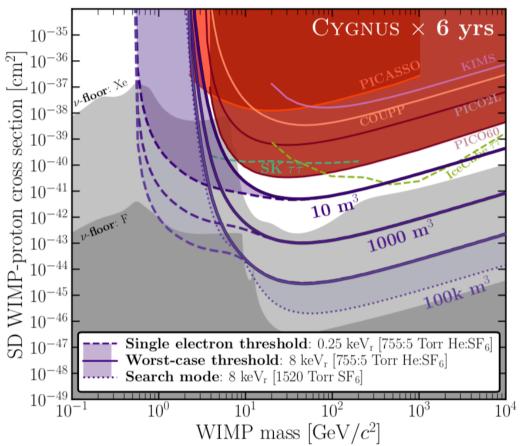
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He:SF₆ 755:5



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Significant improvement in SD reach over existing experiments for all WIMP masses, a 10 m³ detector can already breach the Xe neutrino floor

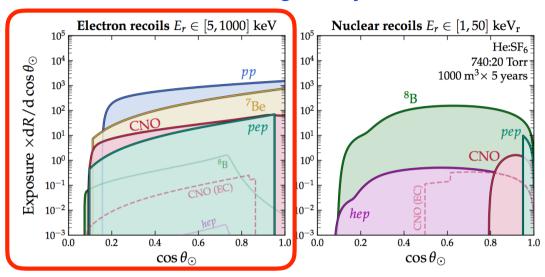
Neutrinos in CYGNUS:

C. A. J. O'Hare et al., 2022 Snowmass Summer Study, arXiv:2203.05914

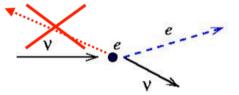


promoting background to signal

Expected number of ER and NR events as a function of the cosine of the angle away from the Sun



Given the Sun position, e recoils in opposite direction are kinematically forbidden



Differently from WIMPs, background can be measured on sidebands data

- Electron recoils directionality in CYGNUS enables solar neutrino spectroscopy through neutrino-electron elastic scattering on an event-by-event basis
 - An O(10) m³ ER directional detector could extend Borexino pp measurement to lower energy
 - CYGNUS 1 ton could measure the CNO cycle by breaking the degeneracy with pep + ⁷Be fluxes through directionality

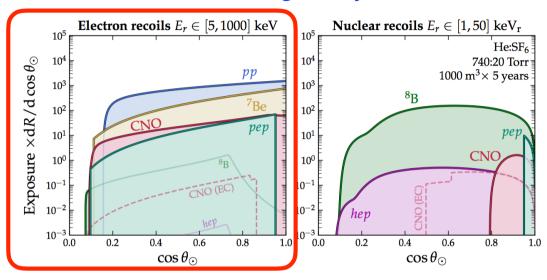
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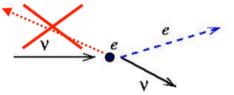


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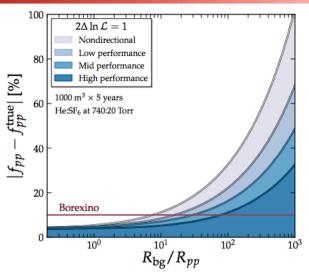


Given the Sun position, 6 recoils in opposite direction are kinematically forbidden

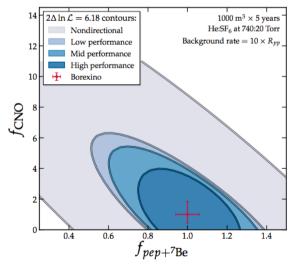


Differently from WIMPs. background can be measured on sidebands data

- Electron recoils directionality in CYGNUS enables solar neutrino spectroscopy through neutrino-electron elastic scattering on an event-by-event basis
 - An O(10) m³ ER directional detector could extend Borexino pp measurement to lower energy
 - Second Cycle by breaking the degeneracy with pep + 7Be fluxes through directionality



1 σ sensitivity to pp flux as a function of the total non-neutrino ER background

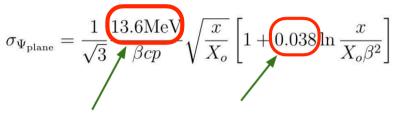


2 σ sensitivity to combined measurement of the CNO and pep + 7Be pp fluxes, fixing the background rate to 10 times the pp electron recoil rate

ER multiple scattering revisited



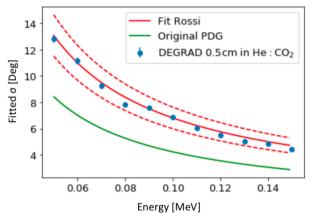
Found to be inadequate to describe MS for ER: we fit these two parameters to DEGRAD simulation of gas mixtures

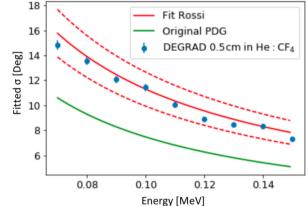


Lynch and Dahl obtain these parameters by fitting to RMS values for nuclear recoils distributions with Geant. They fit to different values of x and $Z(X_o)$, for singly charged (z=1) heavy particles with beta = 1.

Gas Mixture	Pressure	Rad. Length		
60% He 40% CF ₄	760 torr	220 m		
70% He 30% CO ₂	760 torr	606 m		

M. Ghrear & S, Vahsen, paper in preparation





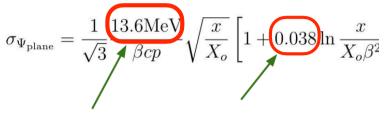
ER multiple scattering revisited & optimal track length for directionality



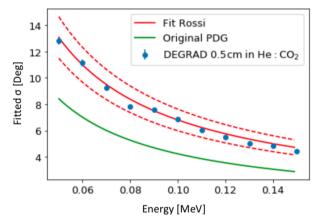
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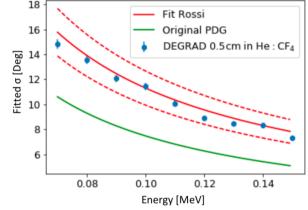
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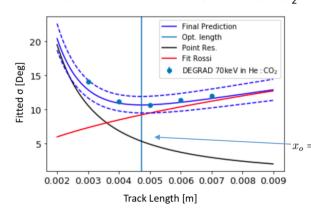


By combining the fitted multiple scattering with the point resolution as from S. E. Vahsen et al. NIM A 788 (2015) 95-105:

$$\sigma_{\Psi}^{\text{plane}}(x) = \sqrt{a^2x + b^2x^{-3}}$$

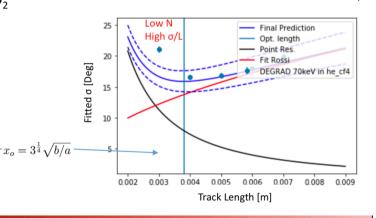
$$a \equiv \frac{1}{\sqrt{3}} \frac{13.1 \text{MeV}}{\beta c p \sqrt{X_o}} \quad b \equiv \sigma_{x/y/z} \sqrt{\frac{12W}{dE/dx}}$$

we can estimate the expected ER angular resolution from gas mixture properties and predict the optimal track length for angle evaluation (with simple SVD algorithm)



 $\sigma_{\phi}^{\mathrm{plane}} = \frac{\sqrt{120 \, x/y/z}}{L\sqrt{N}}$

70 keV electron recoils in 60% He 40% CF₄





ER angular resolution from full simulation of 2D optical readout within the CYGNO project



Simulations:

S. Torelli PhD Thesis within CYGNO Collaboration, paper in prepration

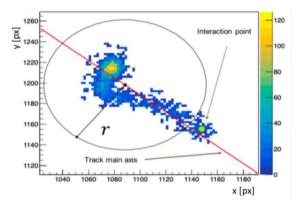
- Electron recoils simulated in GEANT4
- Angular resolution evaluated on MC simulated sCMOS images that take into account GEM gain fluctuations, photon production, sensor calibration and diffusion during drift as evaluated on LIME. PMT waveforms information can further improve this scenario (on going work)
- First part of the algorithm: search for the beginning of the track with:
 - Skewness
 - Distance of pixels from barycenter (farthest pixels)
- Second part of the algorithm aims to find the direction:
 - Track point intensity rescalad with the distance from the interaction point: $W(d_{ip}) = exp(-d_{ip}/w)$
 - Direction taken as the the main axis of the rescaled track passing from the interaction Point
 - Orientation given following the light in the Pixels
- Algorithm adapted from X-ray polarimetry:

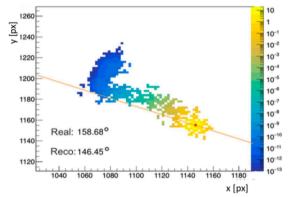
"Measurement of the position resolution of the Gas Pixel Detector" Nuclear Instruments and Methods in Physics Research Section A, Volume 700, 1 February 2013, Pages 99-105

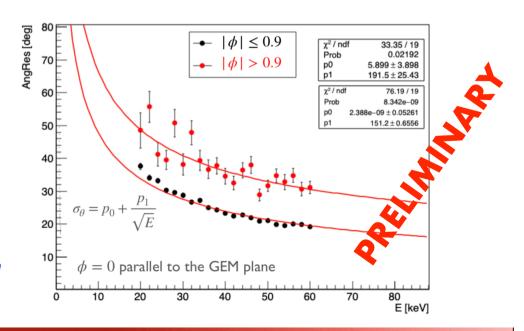
Fit expectation for 70 keV ER compatible with prediction from previous slide and in the "Mid-perfornance" range

LIME detector (now underground @ LNGS): 50 L volume (33 x 33 cm² for 50 cm drift)

He:CF₄ 60:40 1 bar









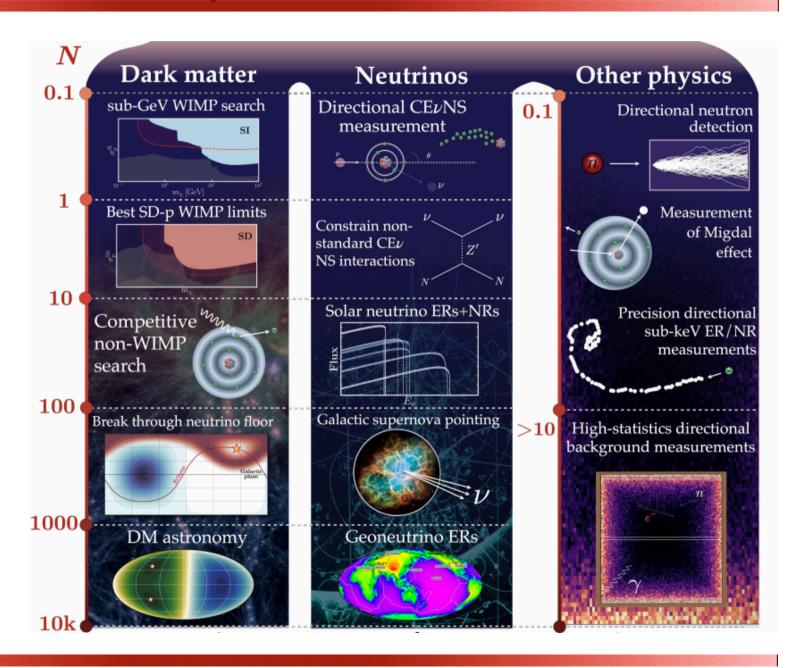
Physics cases for directional TPCs as a function of exposure



N = volume in m³ assuming 1 atm operation

Many interesting physics opportunities already at relatively small scale

See also I. Katsisoulas talk on MIGDAL measurement today at 18.00 in the Dark Matter session

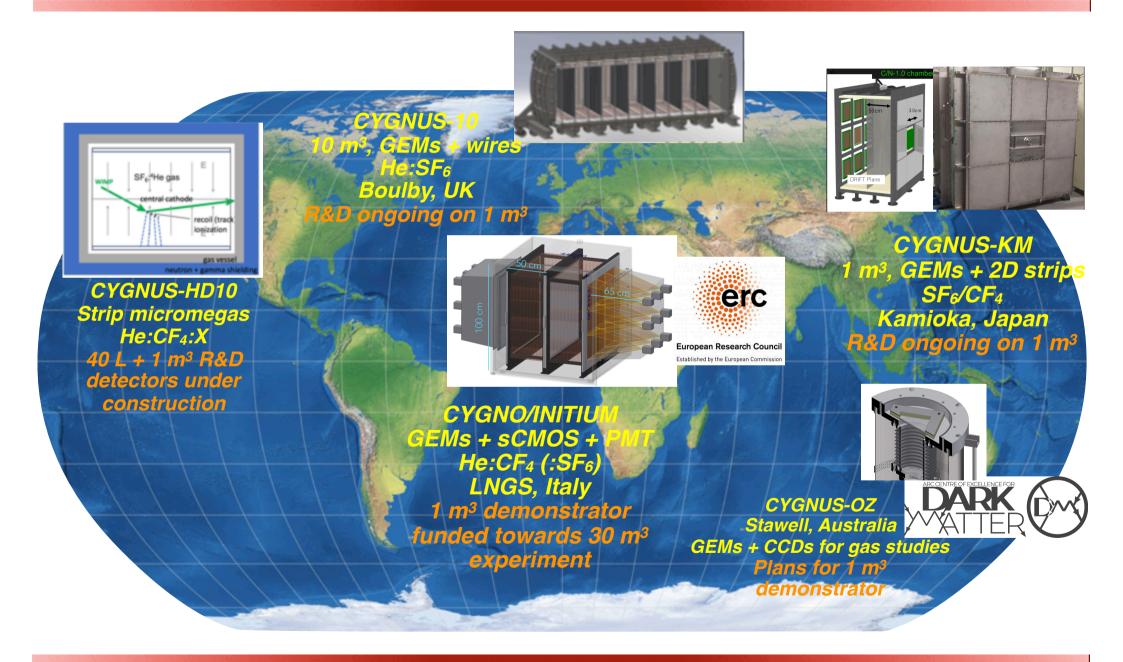




TPCs projects within CYGNUS



G S CYGNUS projects in the world





Gaseous TPC experimental scenery within CYGNUS



	Established readout & directionality	Established gas	R&D readout	R&D gas	Largest detector realised	Detector under development	
DRIFT	MWPC 1.5 D	CS ₂ :CF ₄ :O ₂ @ 0.05 bar	THGEM + wire/ micromegas	SF6:(CF4) @ 0.05 bar	1 m³ (underground)	10 m³ (under study)	
NEWAGE	GEM + muPIC 3D	CF ₄ @ 0.1 bar	GEM + muPIC	SF ₆ @ 0.03 bar	0.04 m³ (underground)	1 m ³ (vessel funded)	
D ³ /CYGNUS- HD	2 GEMs + pixels 3D	Ar/He:CO ₂ @ 1 bar	Strip micromegas	He:CF₄:X @ 1 bar	0.0003 m ³	40 L + 1 m ³ (under construction)	
New Mexico	THGEM + CCD 2D	CF ₄ @ 0.13 bar	THGEM + CMOS	CF ₄ :CS ₂ /SF ₆ @ 0.13 bar	0.000003 m ³		
CYGNO	3 GEMs + CMOS + PMT 2D + 1 D	He:CF₄ @ 1 bar	3 GEMs + CMOS + PMT	He:CF ₄ :SF ₆ @ 0.8-1 bar	0.05 m ³ (underground)	0.4 m³ (funded)	
CYGNUS-OZ			3 GEMs + PMT + charge	He:CF ₄ :(SF ₆) @ 0.05-0.1 bar		100 mL (funded)	
CYGNUS			All of the above	Helium-Fluorine @ 1 bar		1000 m ³	

Electron drift Negative ion drift

Charge readout Optical readout

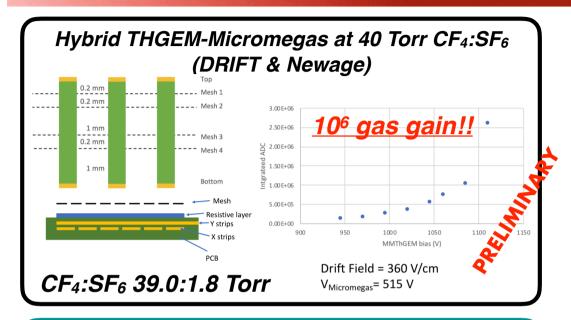


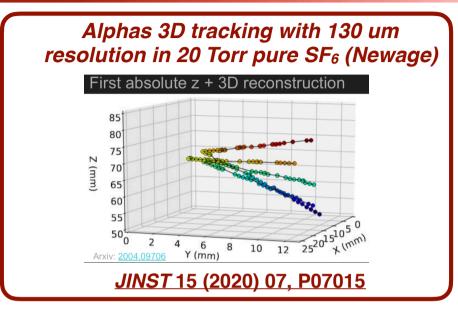
Some highlights from R&D towards CYGNUS

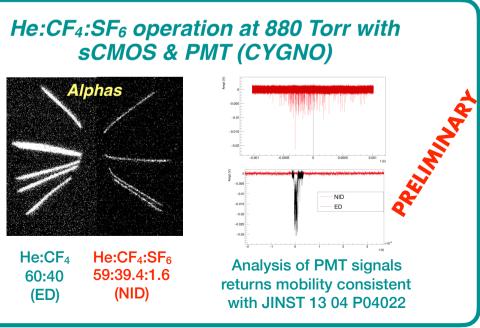
- Operation with SF₆
- Large vessels realisations & projects
- Simulation & analysis

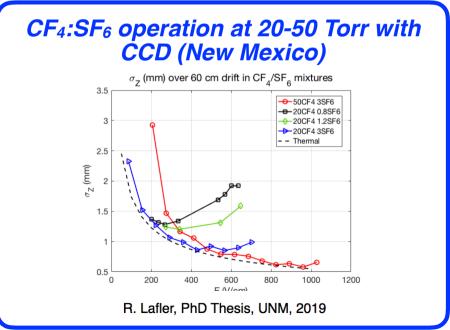
Operation with SF₆











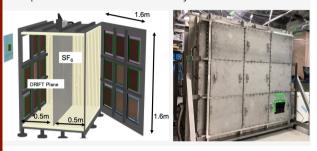
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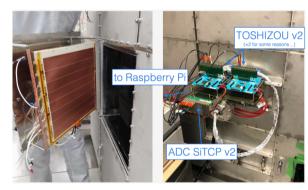
Large detectors realisation & projects



CYGNUS-KM/ NEWAGE (C/N-1.0)

- 18 modules capable 1 m³ chamber
- → placed in Kobe University

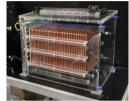


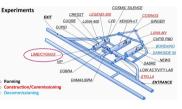


- A single 30 x 30 cm² module for 50 cm drift length commissioning the chamber at Kobe University
 - **§** Goal: detect SF₆ and SF₅ peaks
- After commissioning, to be moved to underground Kamioka Mine

LIME - CYGNO PHASE 0 1 sCMOS + 4 PMT + 3 GEMs 33 x 33 cm² readout area 50 cm drift length

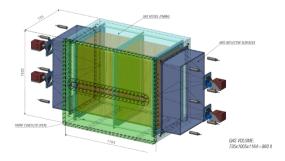








Base module design for PHASE 1
@ underground LNGS taking data



CYGNO PHASE 1 0.4 m³ detector & shielding TDR submitted to INFN

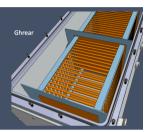
CYGNUS HD "Keiki"

CERN strip Micromegas + SRS

20 x 20 cm² readout area

50 cm drift length x 2 (double sided)





Under construction

Goal: evaluation of components
for follow-on 1 m³ detector



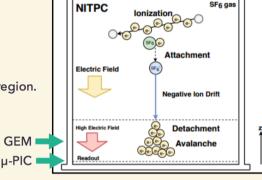
1 m³ vessel design completed

Simulation & analysis



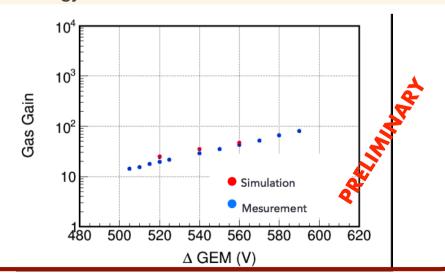
Garfield++ simulation of negative ion drift TPC (Newage)

- 1. lonized electrons are produced.
- 2. Attachment.
- 3. Negative ion are produced.
- 4. Negative ion are drifted.
- 5. Detachment in high electric field region.
- 6. Avalanche amplification.



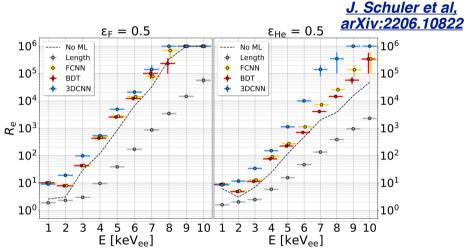
Cross section model

Detach with probability by calculating the mean free path from energy vs cross section.

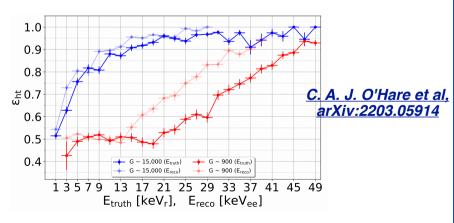


Machine Learning in simulated high definition TPCs (CYGNUS-HD)

Diffusion & quantization included



O(105) ER rejection below 10 keV achievable



Head-tail at 1 keV achievable

Conclusions & Outlook



- **CYGNUS** goal is to establish a Galactic Recoil Observatory to test the DM hypothesis inside the neutrino fog with directionality and perform solar neutrino measurements through both ER and NR recoils signals
 - Extensive concept paper on 1000 m³ gaseous NITPC detector focused on technical feasibility and WIMP searches through nuclear recoils arXiv:2008:12587
 - Alternative physics cases, also involving electron recoils, under development
- CYGNUS will have installations in multiple underground sites, and will proceed through a staged expansion approach
 - Interesting physics opportunities at each stage of development
- **○CYGNUS** groups are working on a coordinated R&D to experimentally establish at the O(1) m³ scale the performances of different readout and gas options
 - Several significant advancements in recent years for SF6 operation, large detectors realisation, simulation and analysis

CYGNUS has recently received interest as part of the Snowmass Decal Planning Exercise

in the US arXiv:2203.05914







Stay tuned for (a flock of) CYGNUS birth!



Backup slides



Comparison of "neutrino floors"



C. A. J. O'Hare, Phys. Rev. Lett. 127 (2021) 25, 251802

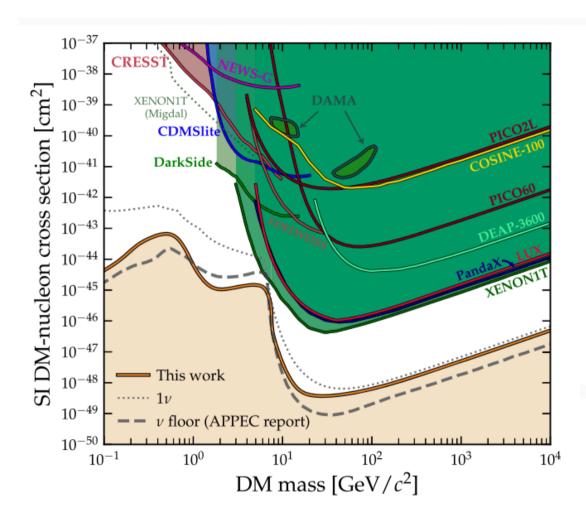


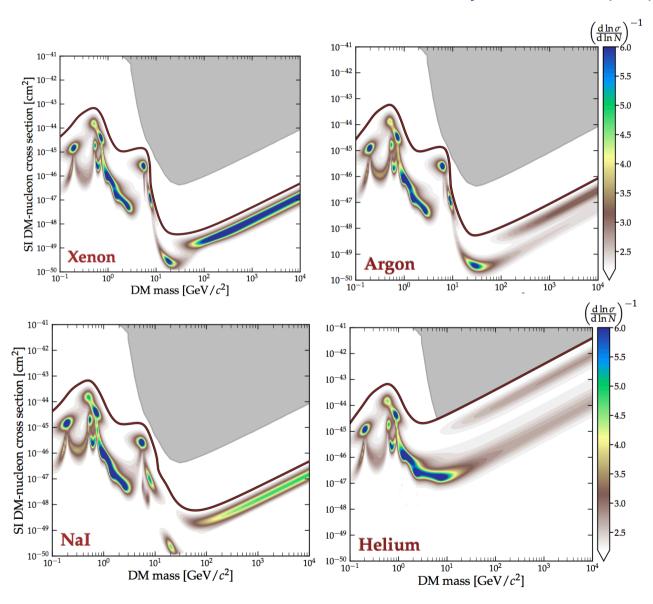
FIG. 1. Present exclusion limits on the spin-independent DM-nucleon cross section (assuming equal proton or neutron couplings) [7,58–71]. Beneath these limits we show three definitions of the neutrino floor for a xenon target. The previous discovery-limit-based neutrino floor calculation shown by the dashed line is taken from the recent APPEC report [72] (based on the technique of Ref. [32]). The envelope of 90% C.L. exclusion limits seeing one expected neutrino event is shown as a dotted line. The result of our work is the solid orange line. We define this notion of the neutrino floor to be the boundary of the neutrino fog, i.e., the cross section at which any experiment sensitive to a given value of m_{χ} leaves the standard Poissonian regime and begins to be saturated by the background.

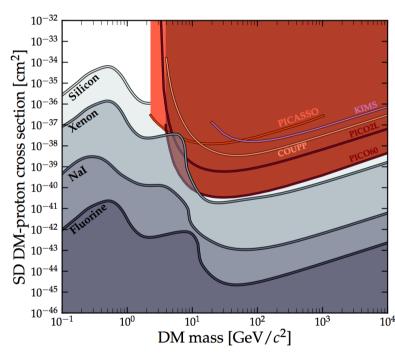


Nuetrino fog for various targets



C. A. J. O'Hare, Phys. Rev. Lett. 127 (2021) 25, 251802

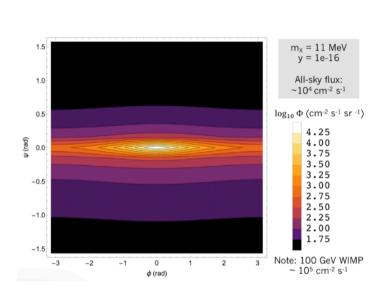


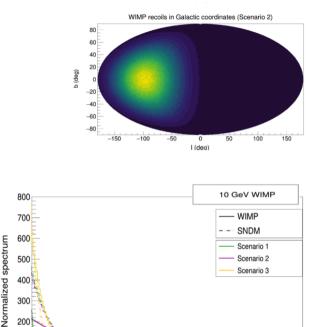


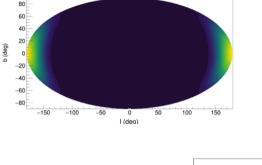


Not only WIMP Dark Matter: potentialities for discovery of MeV DM from SN with directionality

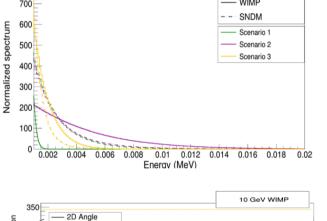


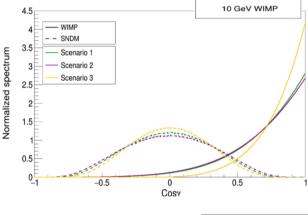


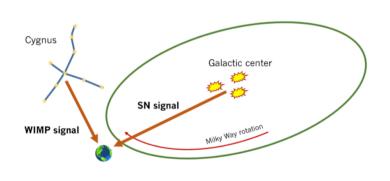


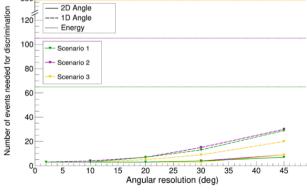


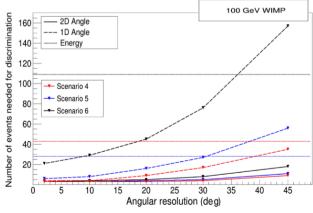
SNDM recoils in Galactic coordinates (Scenario 2)













1992

Solar neutrino spectroscopy with gaseous TPCs





J. Séguinot, T. Ypsilantis Collège de France, IN2P3 - CNRS

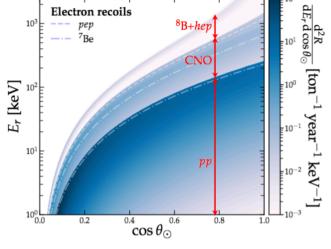
CERN, Genève, Suisse et INFN-Laboratoire national du Gran Sasso, Italie

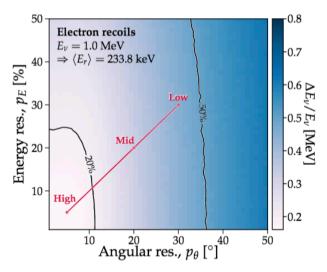
A possible gas for solar neutrino spectroscopy

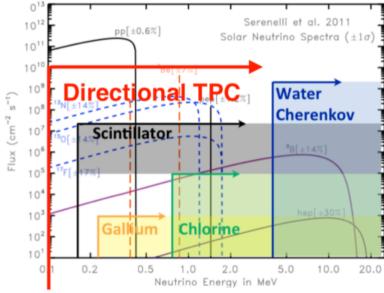
C. Arpesella a, C. Broggini b, C. Cattadori * LN.F.N. Laboratori Nazionali del Gran Sasso. 1-67010 Assergi (AQ), Italy
* LN.F.N. Sezione di Pudova, via Marzolo 8, 1-35131 Pudova, Italy
* LN.F.N. Sezione di Milano, via Celoria 16, 1-20133 Milano, Italy Received 25 July 1995; revised 24 October 1995

A. Zichichi

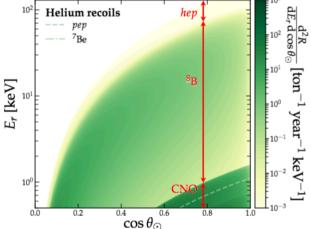
et CERN, Genève, Suisse











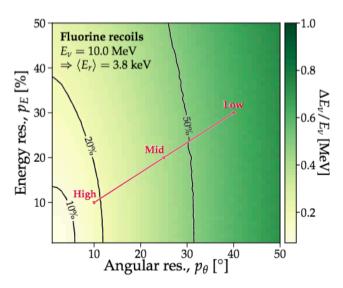


Table 1 Approximate expected numbers of neutrino-induced nuclear and electron recoils

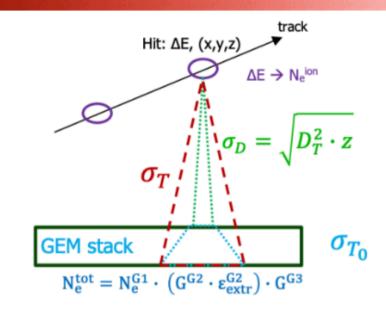
** *									
Nuclear recoils	SF ₆		CF ₄			He			
Threshold (keV _r)	1	5	10	1	5	10	1	5	10
Solar (mainly ⁸ B)	73	15	2	54	16	3	3	2	1
3-kpc supernova	25	18	12	18	13	10	0.6	0.5	0.5
Electron recoils	SF ₆		CF ₄			He			
Threshold (keV)	5	500	1,000	5	500	1,000	1	500	1,000
Solar (total)	537	42	4	438	34	3	102	8	0.8
Solar (CNO)	15	5	0.6	12	4	0.5	3	0.9	0.1
Geoneutrinos	0.2	<0.1	< 0.1	0.2	<0.1	<0.1	<0.1	<0.1	<0.1

^aAssuming a target volume of 1,000 m³, 1 atmosphere pressure, and an exposure time of 1 year.

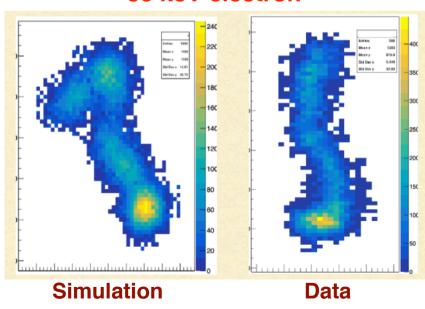


- Electron tracks generated with GEANT4
- # of primary ionisation electrons extracted from a Poisson distribution with mean $N_e = \Delta E/W_i$ with $W_i = 46.2 eV/pair$
- Primary ionisation electron diffused longitudinally and transversally along drift following Gaussian distribution with $\sigma_T = \operatorname{sqrt}(\sigma^2_0 + D^2_T z)$ with $\sigma_0 \& D_T$ from measurements
- Electron avalanche fluctuation taken into account for the first GEM foil
 - For each ionisation electron k, NG1,ke multiplication electron at first foil extracted from exponential distribution with mean = GGEM
 - **©** Total # of multiplication electron from first foil $N^{G1}_e = \sum_k$ NG1,k
 - **G**GEM = 123 from IEEE, Vol. 65, No.1, Jan 2018
- Total electron gain $N^{tot}_e = N^{G1}_e \cdot (G_{GEM})^2$
- Mean total number of photon Ntoty from Poisson distribution with mean $N^{\text{mean}}_{\gamma} = 0.07 \text{ g/e}$
- $\stackrel{\checkmark}{=}$ Number of photon hitting the sensor $N_γ = N^{tot}_γ \cdot Ω$
- SCMOS sensor noise from real data

$$\Omega = \frac{1}{(4(1/\delta + 1) \times a)^2} \qquad \delta = \frac{f}{d - f}$$

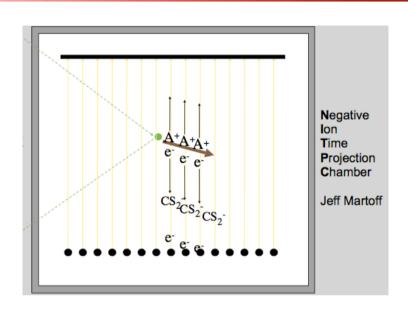


30 keV electron

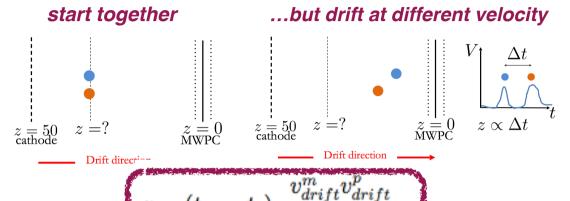


Negative ion drift (NID): improved tracking & full fiducialization

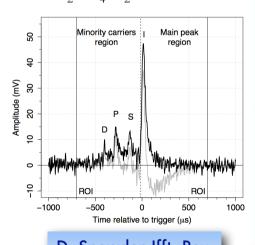




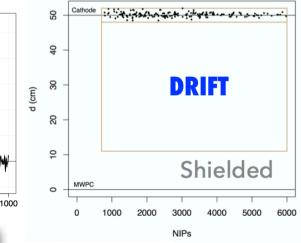
Multiple charge carriers



• CS₂:CF₄:O₂ 30:10:1 Torr



D. Snowden-Ifft, Rev. Sci. Instrum. 85 (2014) 013303



Astroparticle Physics

91 (2017) 65-74

- Electronegative dopant in the gas mixture (CS₂, SF₆, CH₃NO₂, ...)
- Primary ionization electrons captured by electronegative gas molecules at O(100) um
- Anions drift to the anode acting as the effective image carrier instead of the electrons and reducing both longitudinal and transverse diffusion to thermal limit

$$\sigma = \sqrt{\frac{2kTL}{eE}} = 0.7 \, \text{mm} \left(\frac{T}{300 \, \text{K}}\right)^{1/2} \left(\frac{580 \, \text{V/cm}}{E}\right)^{1/2} \left(\frac{L}{50 \, \text{cm}}\right)^{1/2}$$
 low diffusion increases active volume per readout area

T. Ohnuki et al., NIM A 463 J. Martoff et al., NIM A 440 355