



SCUOLA
NORMALE
SUPERIORE

Closing the window on WIMP Dark Matter

Salvatore Bottaro

Based on: 2107.09688 and 2205.04486

with D.Buttazzo, M.Costa, R.Franceschini, P.Panci, D.Redigolo, L.Vittorio

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- Not fully nor systematically explored

Real WIMPs - Odd n , $Y = 0$

2107.09688

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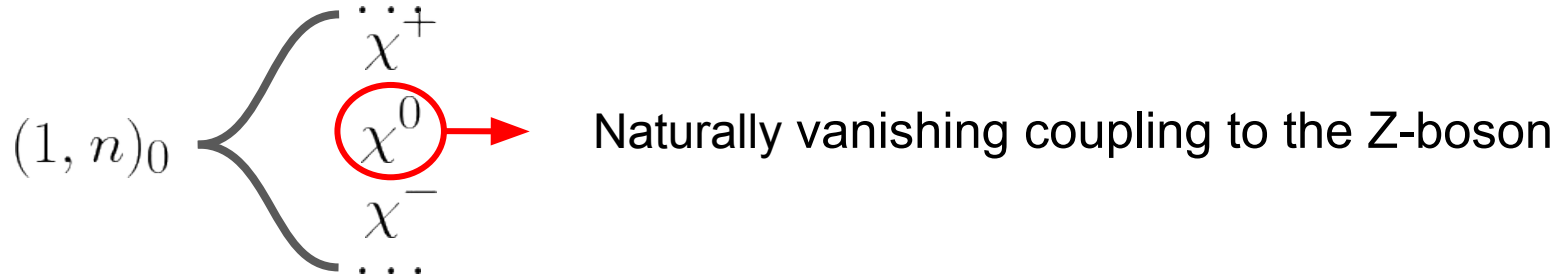
$$\begin{aligned}\mathcal{L}_s &= \frac{1}{2} (D_\mu \chi)^2 - \frac{1}{2} M_\chi^2 \chi^2 - \frac{\lambda_H}{2} \chi^2 |H|^2 - \frac{\lambda_\chi}{4} \chi^4, \\ \mathcal{L}_f &= \frac{1}{2} \chi (i \bar{\sigma}^\mu D_\mu - M_\chi) \chi,\end{aligned}$$

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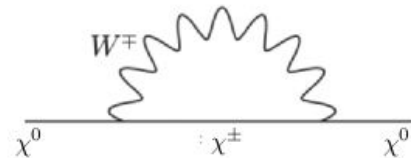
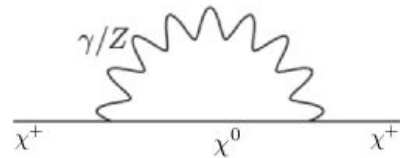
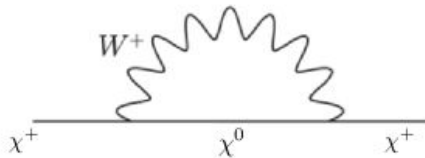
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$$(1, n)_0 \left\{ \begin{array}{l} \ddot{\chi}^+ \\ \chi^0 \\ \chi^- \\ \dots \end{array} \right\} \quad \Delta M = (167 \pm 4) \text{ MeV}$$



Cheng '98
Feng '99
Gherghetta '99
Ibe '12
McKay '18

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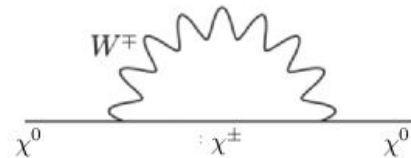
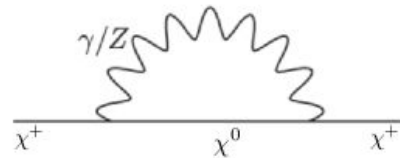
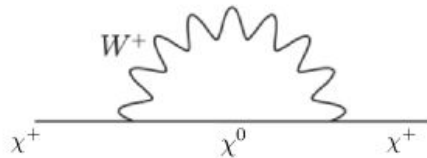
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$$(\chi^T T^a \chi)(H^\dagger T^a H) \rightarrow 0$$



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Computing the DM Relic Abundance

Boltzmann equation:

$$\frac{dY}{dx} = -\frac{s(x)}{xH(x)} \langle \sigma v \rangle \left(1 - \frac{x}{3g_*(x)} \frac{dg_*}{dx} \right) (Y^2(x) - Y_{eq}^2(x))$$

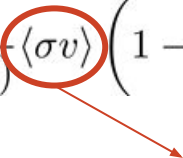
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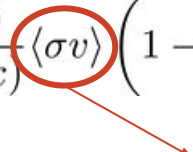


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Std. tree-level cross-section: $\langle \sigma v \rangle_0 = \frac{\pi \alpha_2^2 (2n^4 + 17n^2 - 19)}{16g_\chi M_\chi^2}$ Correct...

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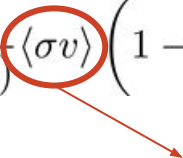
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- Sommerfeld enhancement
- Bound states formation

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} Large *non-perturbative, non-relativistic* effects!

Sommerfeld Effect (SE) & Bound States (BS)

SE: Potentials deform the wave function of incoming particles

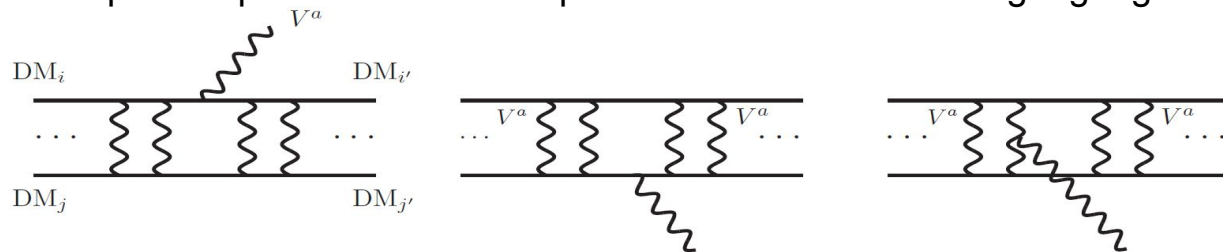
$$-\frac{\nabla^2\psi}{M_\chi} + V\psi = E\psi \qquad \langle\sigma v\rangle_0 \rightarrow \begin{cases} \langle\sigma v\rangle = S_{Som}(x)\langle\sigma v\rangle_0 \\ S_{Som}(x) \propto |\psi(0)|^2 \end{cases}$$

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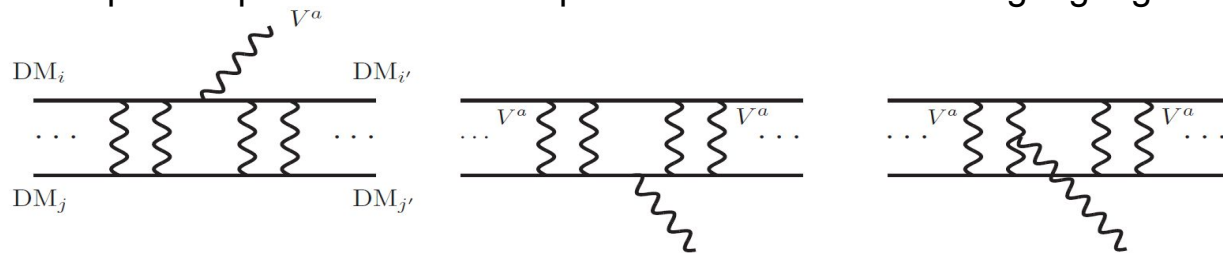


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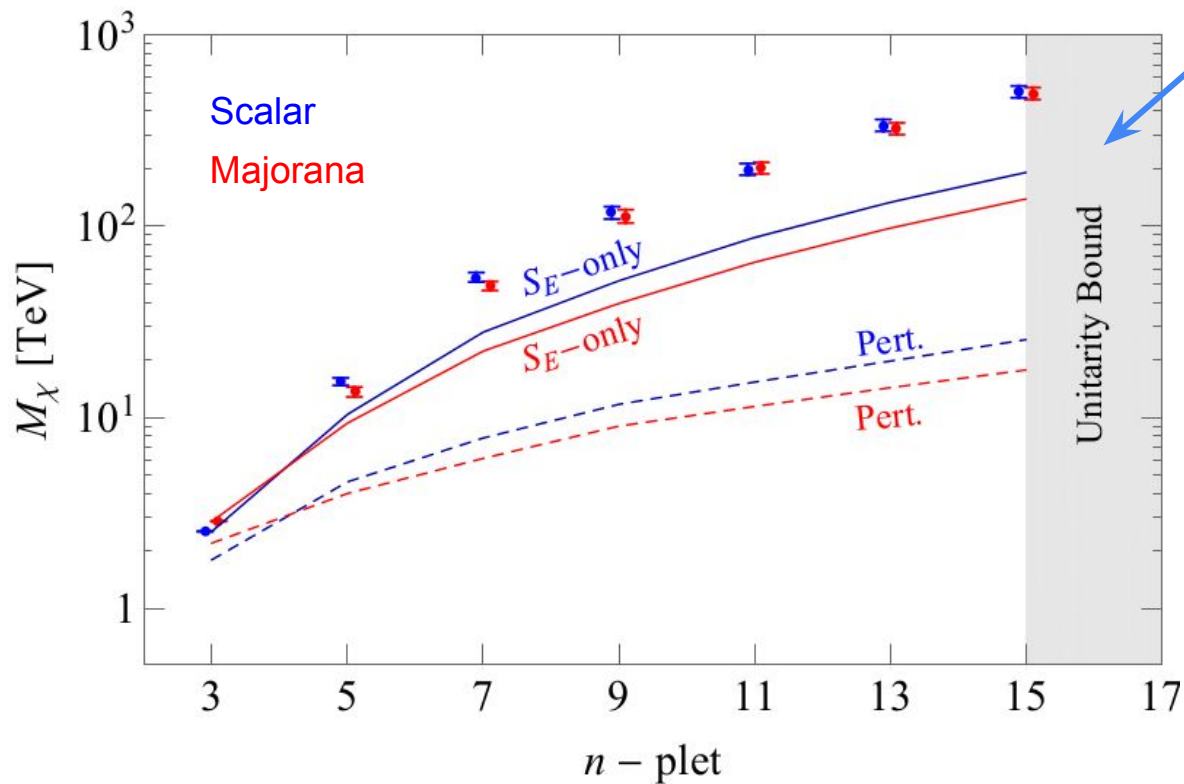
The pair in the bound state later annihilates into SM (annihilation enhancement)

Mitridate '17

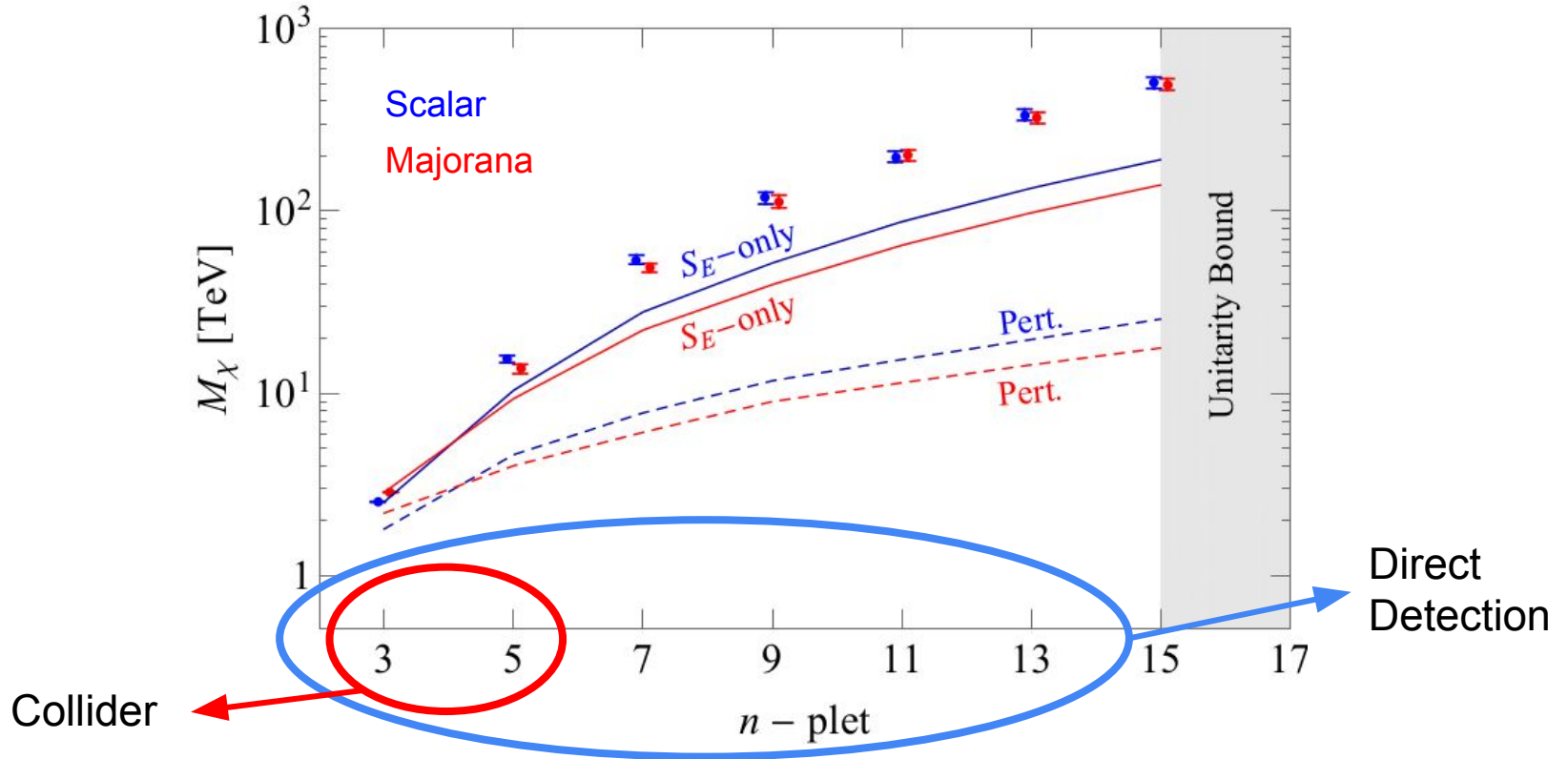
$$S(x) = S_{Som}(x) + \left[\frac{\langle\sigma v\rangle_0}{\langle\sigma_I v\rangle} + \frac{g_\chi^2 \langle\sigma v\rangle_0 M_\chi^3}{2g_I \Gamma_{ann}} \left(\frac{1}{4\pi x} \right)^{\frac{3}{2}} e^{-x E_{B_I}/M_\chi} \right]^{-1}$$

Real WIMPs - Odd n , $Y = 0$

$$(\sigma v_{\text{rel}})^J \leq \frac{4\pi(2J+1)}{M_{\text{DM}}^2 v_{\text{rel}}}$$

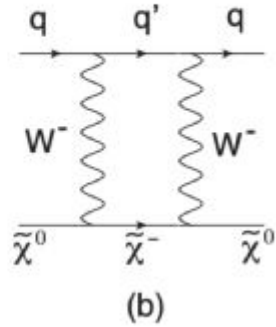
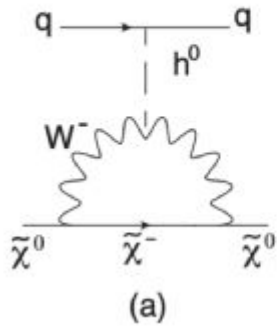


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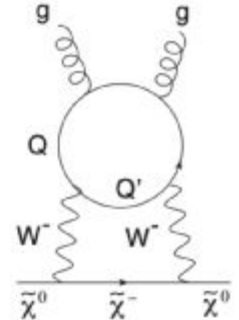
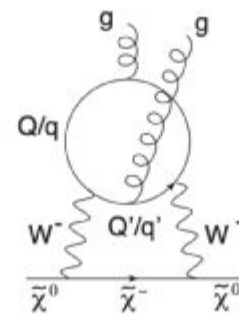
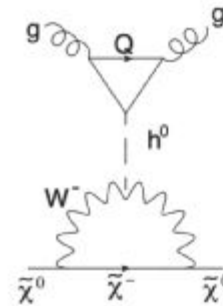


Direct Detection

1-loop

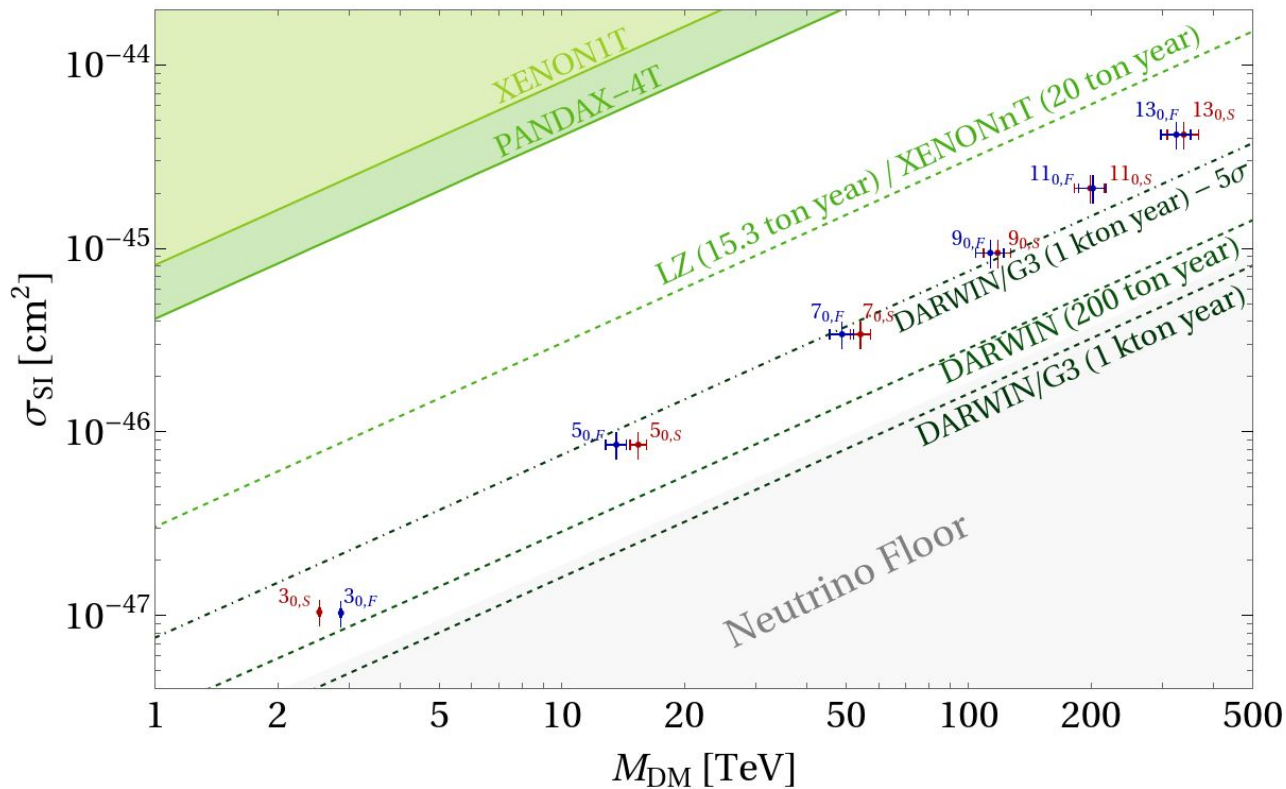


2-loop



Hisano '05, Hisano '10

Direct Detection

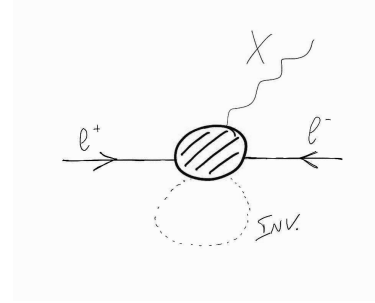


Muon collider

Muon collider

- Mono-X and Di-X searches ($X = \gamma, W, Z$)

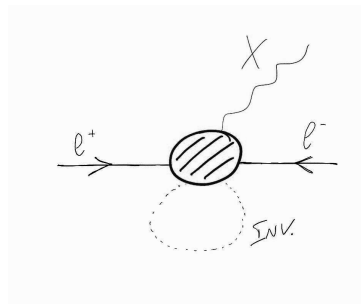
See also Han et al. 2009.11287



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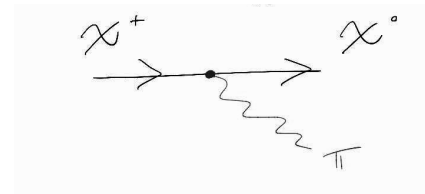
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- Disappearing tracks (1DT, 2DT)

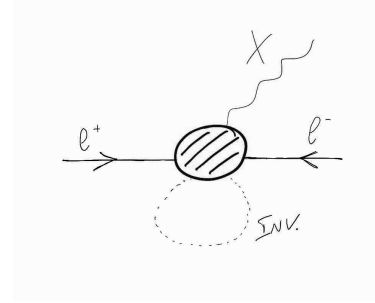
Recast of Capdevila et al.
2102.11292



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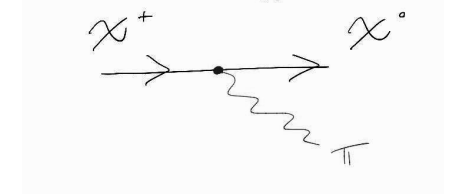
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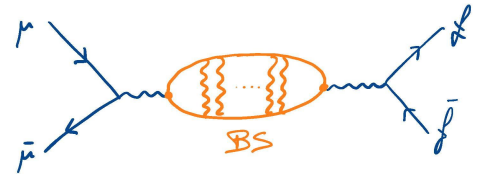
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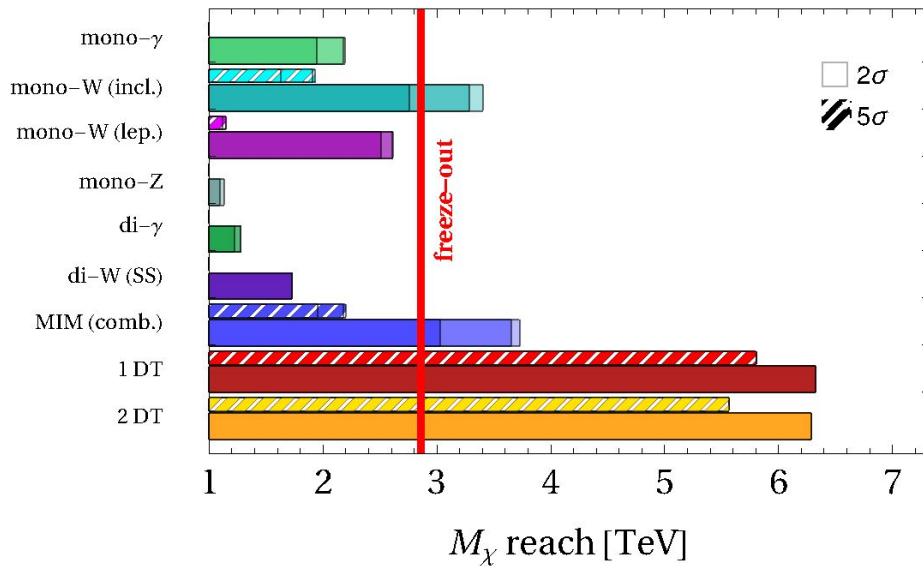
- Resonant production of bound states

Bottaro et al. 2103.12766

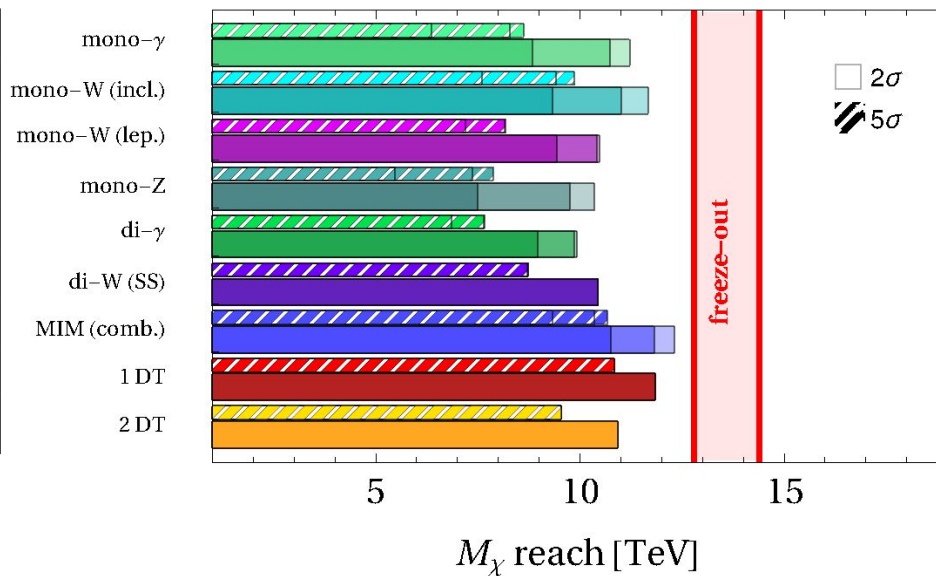


Reach

$\sqrt{s} = 14 \text{ TeV}$, $\mathcal{L} = 20 \text{ ab}^{-1}$, Majorana 3-plet



$\sqrt{s} = 30 \text{ TeV}$, $\mathcal{L} = 90 \text{ ab}^{-1}$, Majorana 5-plet



Complex WIMPs - $Y \neq 0$

2205.04486

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2205.04486

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$$\Gamma(\chi_0 \rightarrow \chi_{DM} SM) > \tau_{\text{BBN}}^{-1}$$

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$$\Delta M_{\text{gauge}} = 167 \text{ MeV} \left(Q^2 + \frac{2QY}{\cos \theta_W} \right) \longrightarrow$$

\mathcal{O}_+ necessary to make DM the lightest component of the multiplet unless

$$Y = 0, \quad |Y| = \frac{n-1}{2}$$

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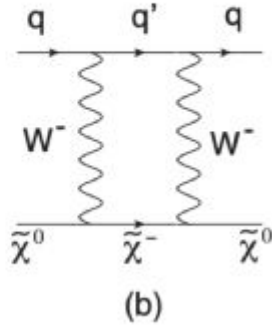
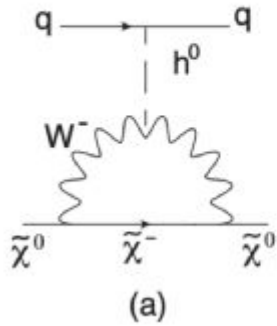
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Surviving candidates:

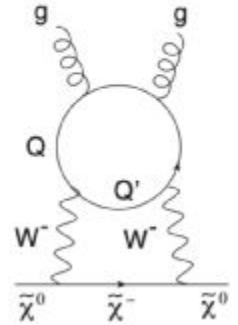
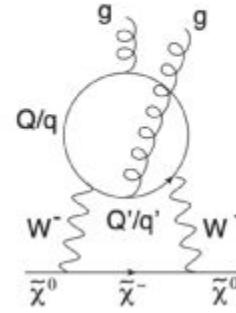
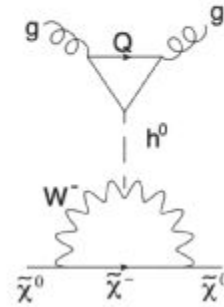
- $Y=1/2$, $n < 13$ (perturbative unitarity bound)
- $Y=1$, $n=3, 5$ (perturbativity of mass splitting)
- $Y > 1$ are non-perturbative!

Direct Detection

1-loop

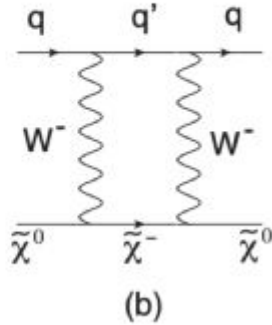
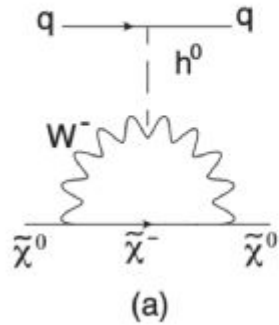


2-loop

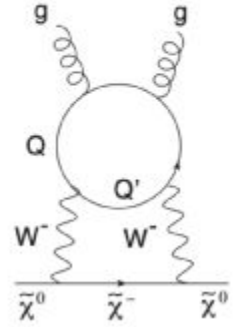
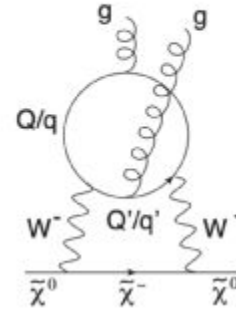
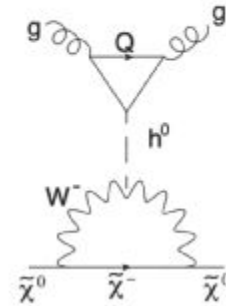


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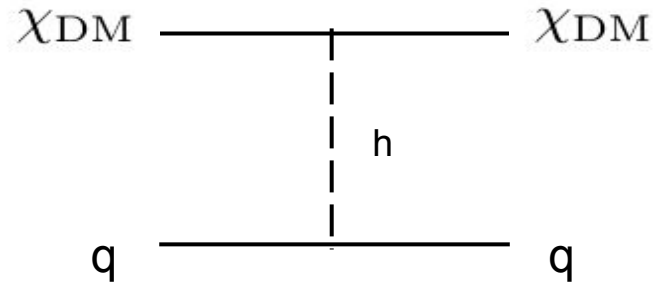
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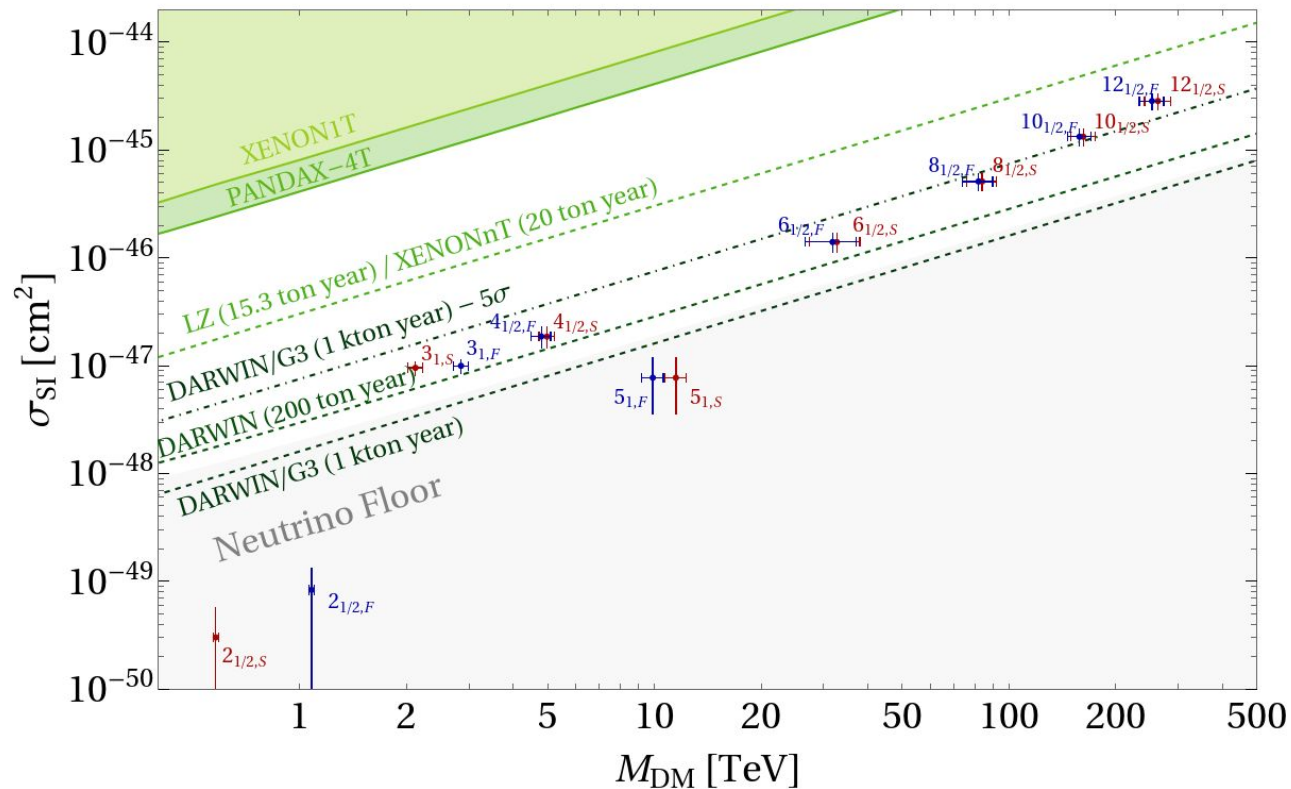
2-loop



$\mathcal{O}_0, \mathcal{O}_+$ $\xrightarrow{\text{generate tree-level coupling to the Higgs}}$

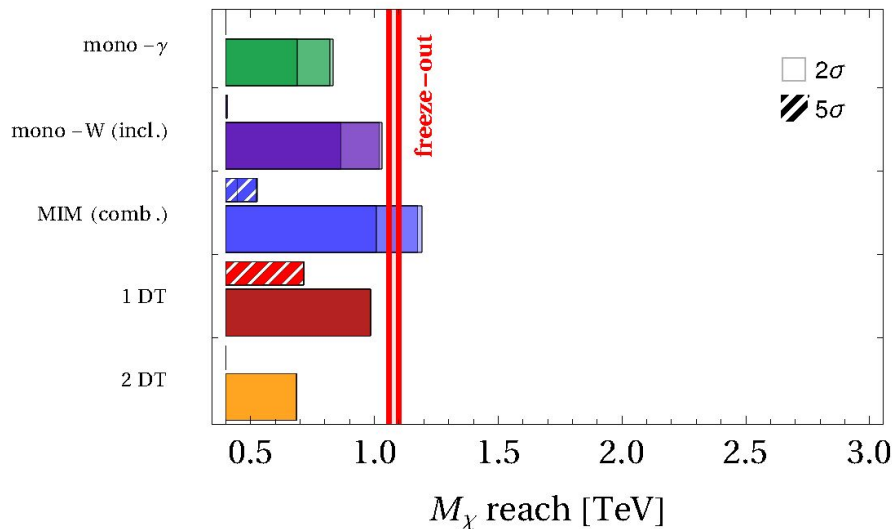


Direct Detection - Minimal Splitting

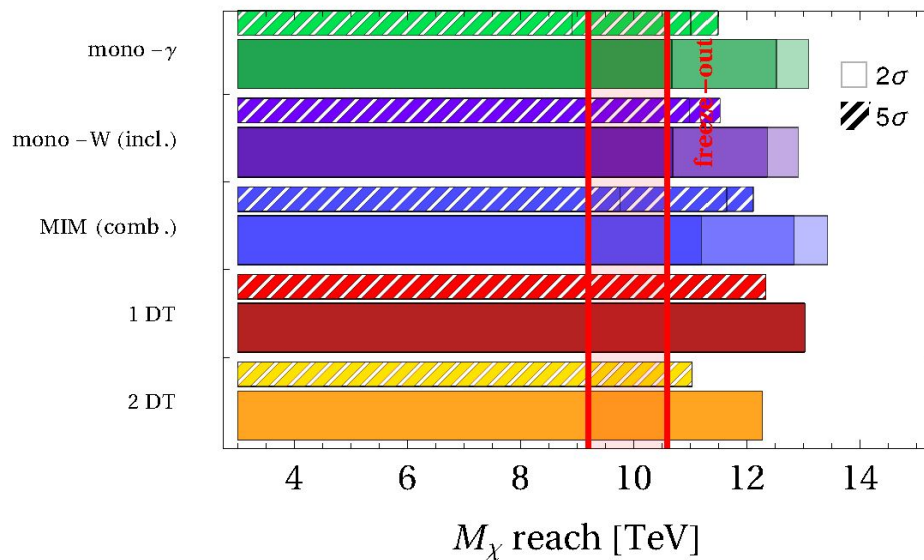


Muon Collider - Minimal Splitting

$\sqrt{s} = 6 \text{ TeV}, \mathcal{L} = 4 \text{ ab}^{-1}, \text{Dirac } 2_{1/2}$

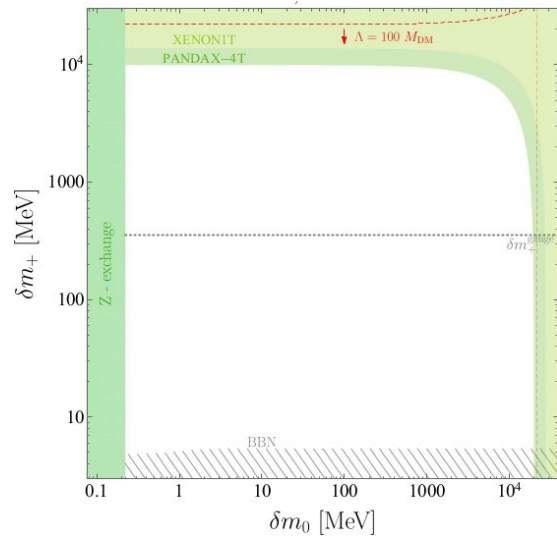


$\sqrt{s} = 30 \text{ TeV}, \mathcal{L} = 90 \text{ ab}^{-1}, \text{Dirac } 5_1$

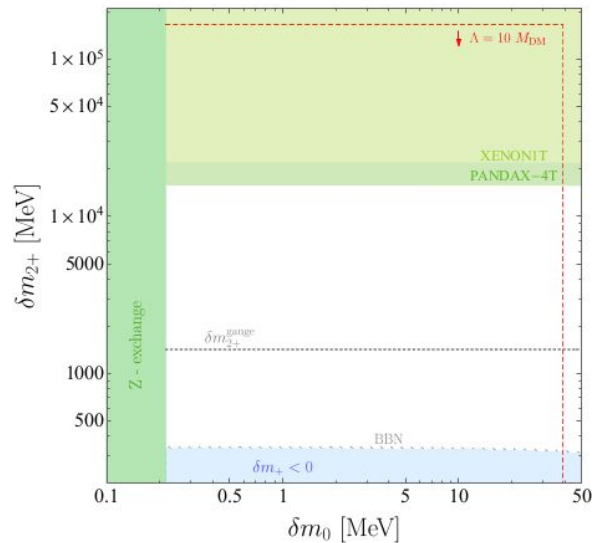


Non minimal splitting

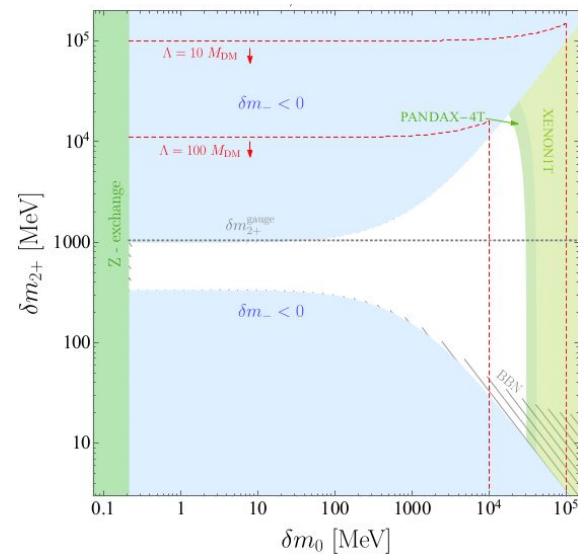
$n = 2$



$n = 3$

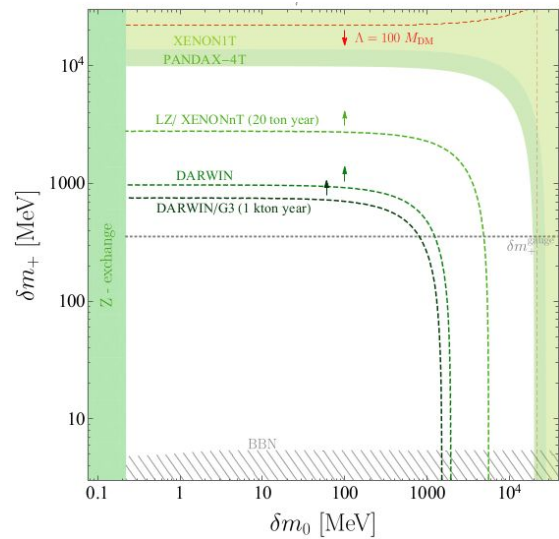


$n = 4$

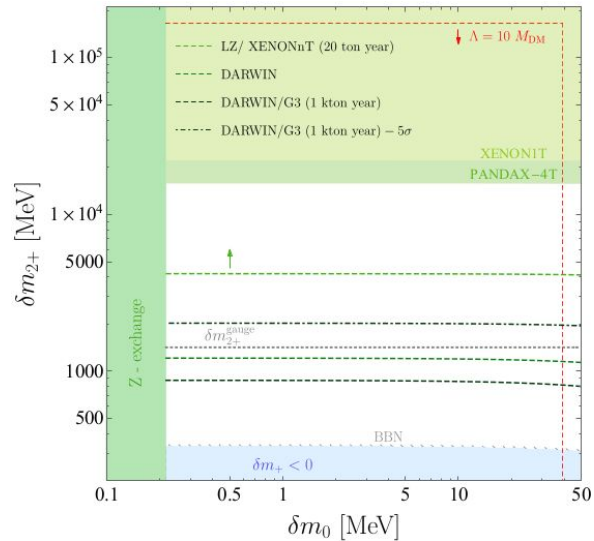


Non minimal splitting

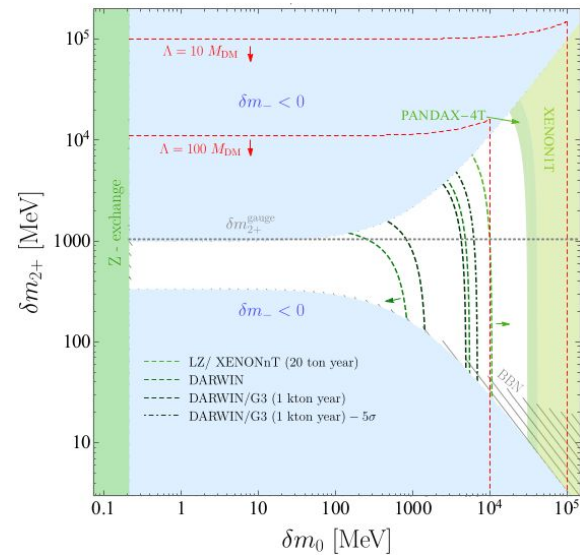
$n = 2$



$n = 3$

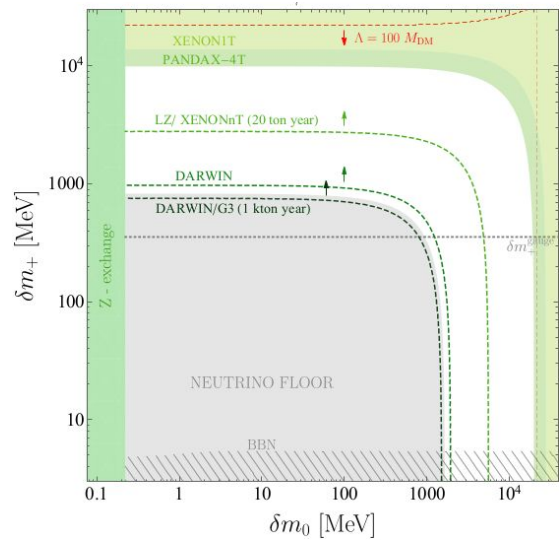


$n = 4$

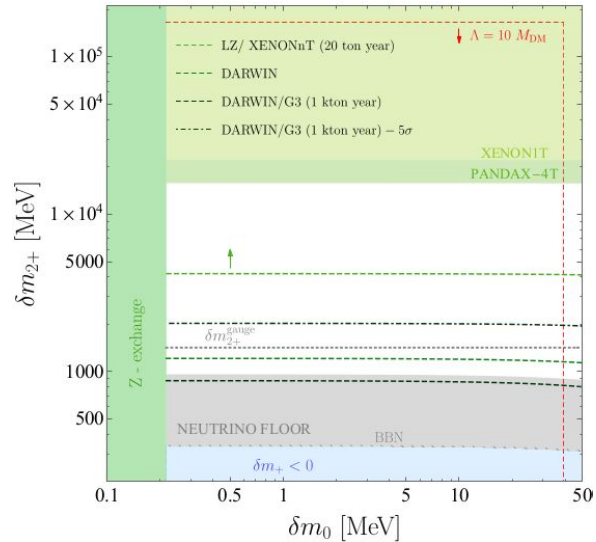


Non minimal splitting

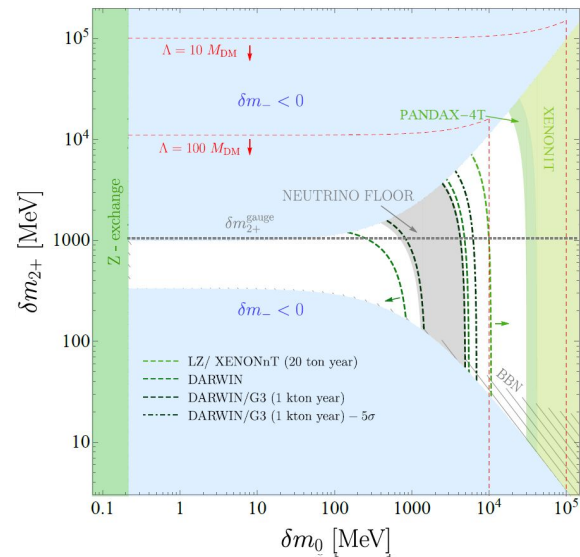
$n = 2$



$n = 3$

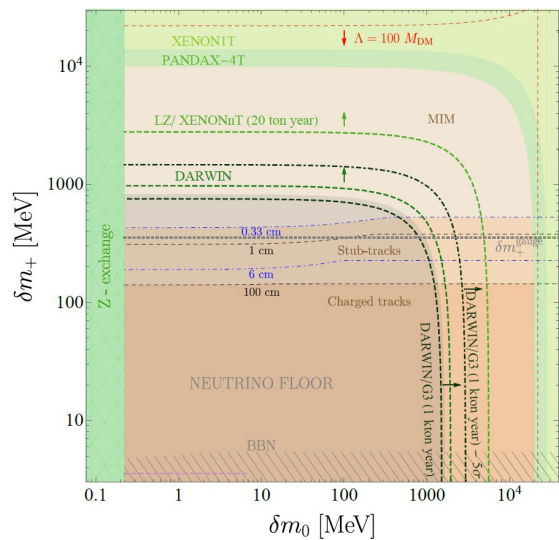


$n = 4$

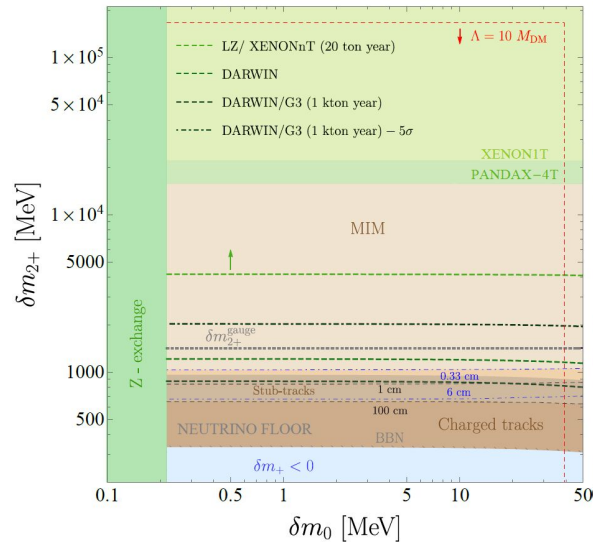


Non minimal splitting

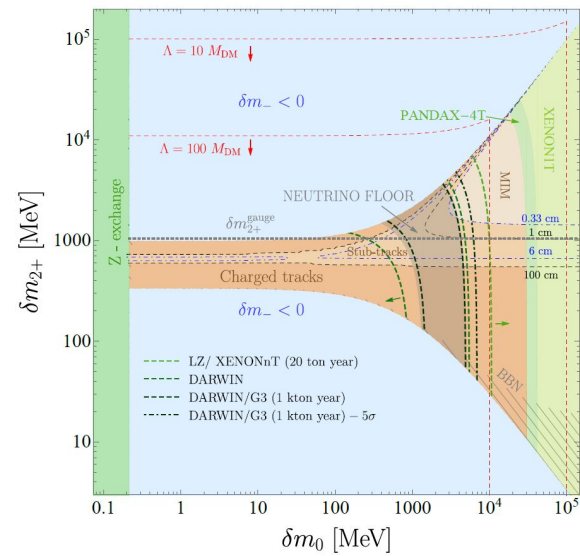
$n = 2$



$n = 3$



$n = 4$



Conclusions

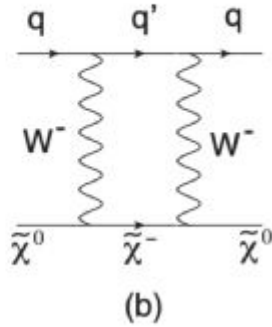
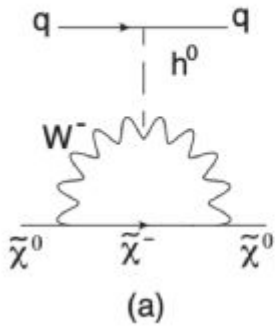
- We computed the thermal mass of all perturbative WIMP candidates
- Real candidates can all be excluded by high exposure ($> 200 \text{ ton} \times \text{year}$)
Xenon experiments like DARWIN
- Complex candidates with $Y \neq 0$ and minimal splitting can also be excluded by DARWIN, with the exception of $n=2$ and 5
- Future DD experiments can close most of the parameter space spanned by mass splittings
- Collider can close the parameter space for light multiplets, while ID for the heavier ones (future work)

Thanks for the attention

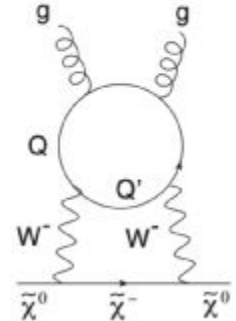
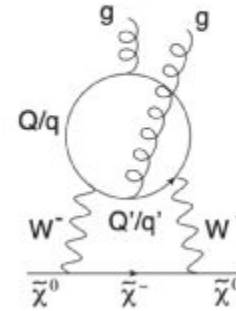
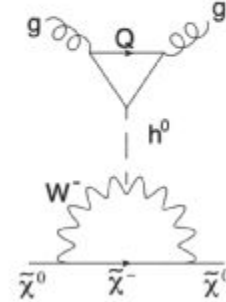
Back-up

Direct Detection

1-loop



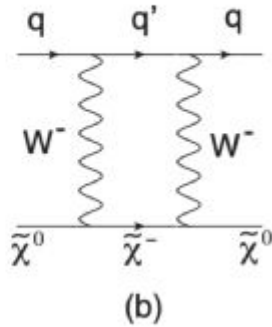
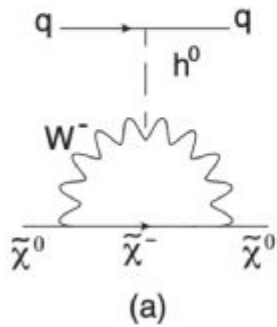
2-loop



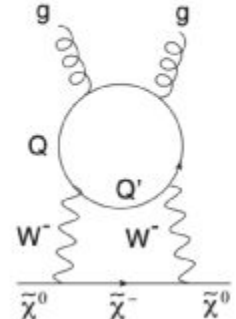
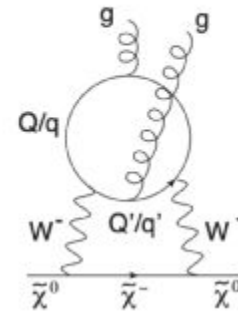
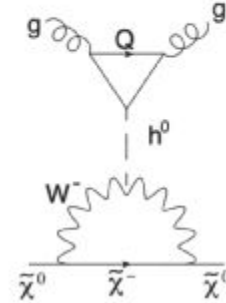
$$\mathcal{L}_{\text{eff}}^{\text{SI}} = \bar{\chi}\chi (f_q m_q \bar{q}q + f_G G_{\mu\nu} G^{\mu\nu}) + \frac{g_q}{M_\chi} \bar{\chi} i \partial^\mu \gamma^\nu \chi \mathcal{O}_{\mu\nu}^q$$

Direct Detection

1-loop



2-loop



$$\mathcal{L}_{\text{eff}}^{\text{SI}} = \bar{\chi}\chi (f_q m_q \bar{q}q + f_G G_{\mu\nu} G^{\mu\nu}) + \frac{g_q}{M_\chi} \bar{\chi} i \partial^\mu \gamma^\nu \chi \mathcal{O}_{\mu\nu}^q$$

Real WIMPs

DM spin	EW n-plet	M_χ (TeV)	$(\sigma v)_{\text{tot}}^{J=0}/(\sigma v)_{\text{max}}^{J=0}$	$\Lambda_{\text{Landau}}/M_{\text{DM}}$	$\Lambda_{\text{UV}}/M_{\text{DM}}$
Real scalar	3	2.53 ± 0.01	—	2.4×10^{37}	$4 \times 10^{24*}$
	5	15.4 ± 0.7	0.002	7×10^{36}	3×10^{24}
	7	54.2 ± 3.1	0.022	7.8×10^{16}	2×10^{24}
	9	117.8 ± 15.4	0.088	3×10^4	2×10^{24}
	11	199 ± 42	0.25	62	1×10^{24}
	13	338 ± 102	0.6	7.2	2×10^{24}
Majorana fermion	3	2.86 ± 0.01	—	2.4×10^{37}	$2 \times 10^{12*}$
	5	13.6 ± 0.8	0.003	5.5×10^{17}	3×10^{12}
	7	48.8 ± 3.3	0.019	1.2×10^4	1×10^8
	9	113 ± 15	0.07	41	1×10^8
	11	202 ± 43	0.2	6	1×10^8
	13	324.6 ± 94	0.5	2.6	1×10^8

Complex WIMPs $Y=0$

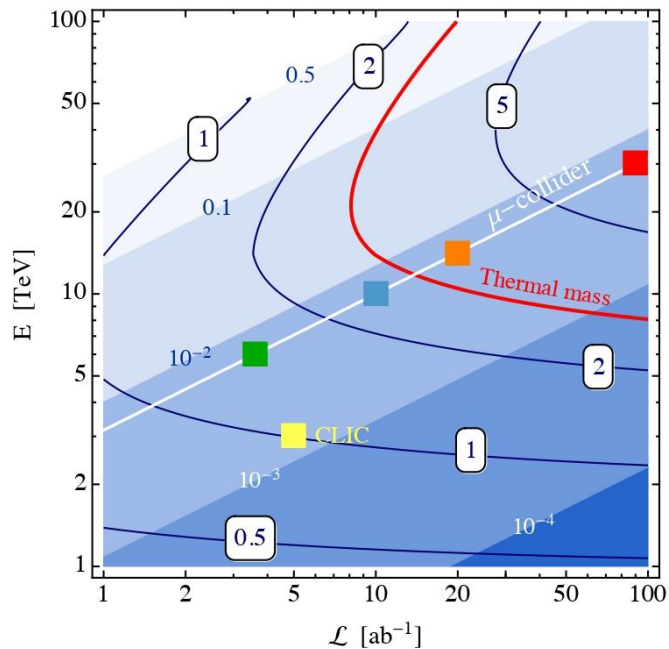
DM spin	n_ϵ	M_{DM} (TeV)	$\Lambda_{\text{Landau}}/M_{\text{DM}}$	$(\sigma v)_{\text{tot}}^{J=0}/(\sigma v)_{\text{max}}^{J=0}$
Complex scalar	3	$1.60 \pm 0.01 - 2.4^*$	$> M_{\text{Pl}}$	-
	5	11.3 ± 0.6	$> M_{\text{Pl}}$	0.003
	7	47 ± 3	2×10^6	0.02
	9	118 ± 9	110	0.09
	11	217 ± 17	7	0.25
	13	352 ± 30	3	0.6
Dirac fermion	3	$2.0 \pm 0.1 - 2.4^*$	$> M_{\text{Pl}}$	-
	5	9.1 ± 0.5	4×10^6	0.002
	7	45 ± 3	80	0.02
	9	115 ± 9	6	0.09
	11	211 ± 16	2.4	0.3
	13	340 ± 27	1.6	0.7

Complex WIMPs $Y \neq 0$

DM spin	n_Y	M_{DM} (TeV)	$\Lambda_{\text{Landau}}/M_{\text{DM}}$	$(\sigma v)_{\text{tot}}^{J=0}/(\sigma v)_{\text{max}}^{J=0}$	δm_0 [MeV]	$\Lambda_{\text{UV}}^{\text{max}}/M_{\text{DM}}$	δm_{Q_M} [MeV]
Dirac fermion	$2_{1/2}$	1.08 ± 0.02	$> M_{\text{Pl}}$	-	$0.22 - 2 \times 10^4$	10^7	$4.8 - 10^4$
	3_1	2.85 ± 0.14	$> M_{\text{Pl}}$	-	$0.22 - 40$	60	$312 - 1.6 \times 10^4$
	$4_{1/2}$	4.8 ± 0.3	$\simeq M_{\text{Pl}}$	0.001	$0.21 - 3 \times 10^4$	5×10^6	$20 - 1.9 \times 10^4$
	5_1	9.9 ± 0.7	3×10^6	0.003	$0.21 - 3$	25	$10^3 - 2 \times 10^3$
	$6_{1/2}$	31.8 ± 5.2	2×10^4	0.01	$0.5 - 2 \times 10^4$	4×10^5	$100 - 2 \times 10^4$
	$8_{1/2}$	82 ± 8	15	0.05	$0.84 - 10^4$	10^5	$440 - 10^4$
	$10_{1/2}$	158 ± 12	3	0.16	$1.2 - 8 \times 10^3$	6×10^4	$1.1 \times 10^3 - 9 \times 10^3$
	$12_{1/2}$	253 ± 20	2	0.45	$1.6 - 6 \times 10^3$	4×10^4	$2.3 \times 10^3 - 7 \times 10^3$
Complex scalar	$2_{1/2}$	0.58 ± 0.01	$> M_{\text{Pl}}$	-	$4.9 - 1.4 \times 10^4$	-	$4.2 - 7 \times 10^3$
	3_1	2.1 ± 0.1	$> M_{\text{Pl}}$	-	$3.7 - 500$	120	$75 - 1.3 \times 10^4$
	$4_{1/2}$	4.98 ± 0.25	$> M_{\text{Pl}}$	0.001	$4.9 - 3 \times 10^4$	-	$17 - 2 \times 10^4$
	5_1	11.5 ± 0.8	$> M_{\text{Pl}}$	0.004	$3.7 - 10$	20	$650 - 3 \times 10^3$
	$6_{1/2}$	32.7 ± 5.3	$\simeq 6 \times 10^{13}$	0.01	$4.9 - 8 \times 10^4$	-	$50 - 5 \times 10^4$
	$8_{1/2}$	84 ± 8	2×10^4	0.05	$4.9 - 6 \times 10^4$	-	$150 - 6 \times 10^4$
	$10_{1/2}$	162 ± 13	20	0.16	$4.9 - 4 \times 10^4$	-	$430 - 4 \times 10^4$
	$12_{1/2}$	263 ± 22	4	0.4	$4.9 - 3 \times 10^4$	-	$10^3 - 3 \times 10^4$

Lumi vs Energy (Mono-W)

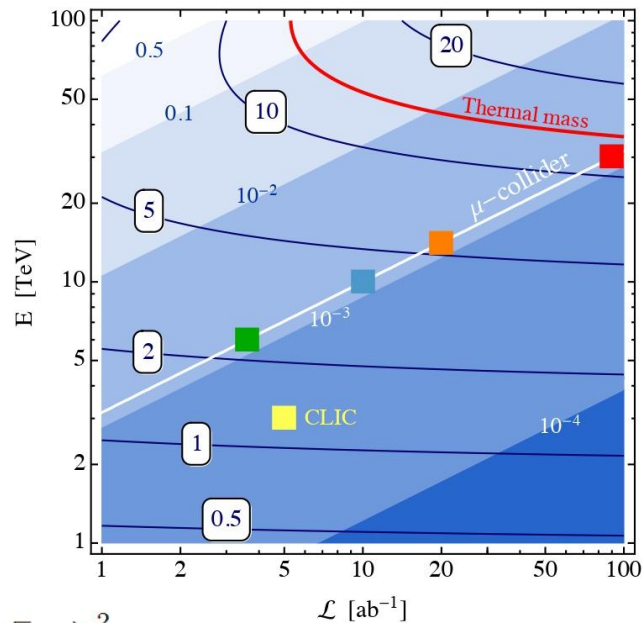
Majorana 3-plet



2σ : 12 TeV

$\epsilon=0\%$

Majorana 5-plet

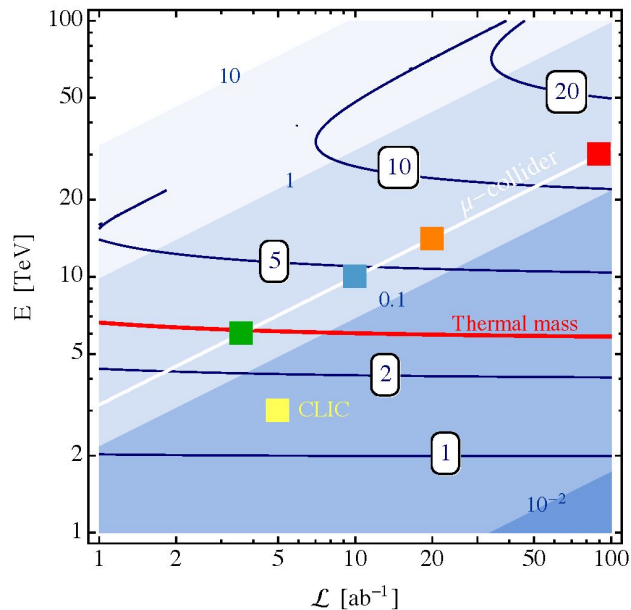


2σ : 35 TeV

$$\mathcal{L} \simeq 10 \text{ ab}^{-1} \cdot \left(\frac{\sqrt{s}}{10 \text{ TeV}} \right)^2$$

Lumi vs Energy (Disappearing tracks)

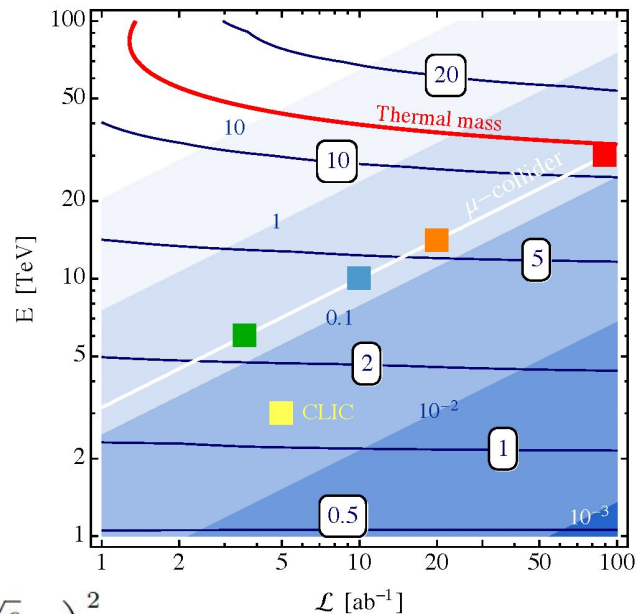
Majorana 3-plet



2σ : 6 TeV

$\epsilon=0\%$

Majorana 5-plet

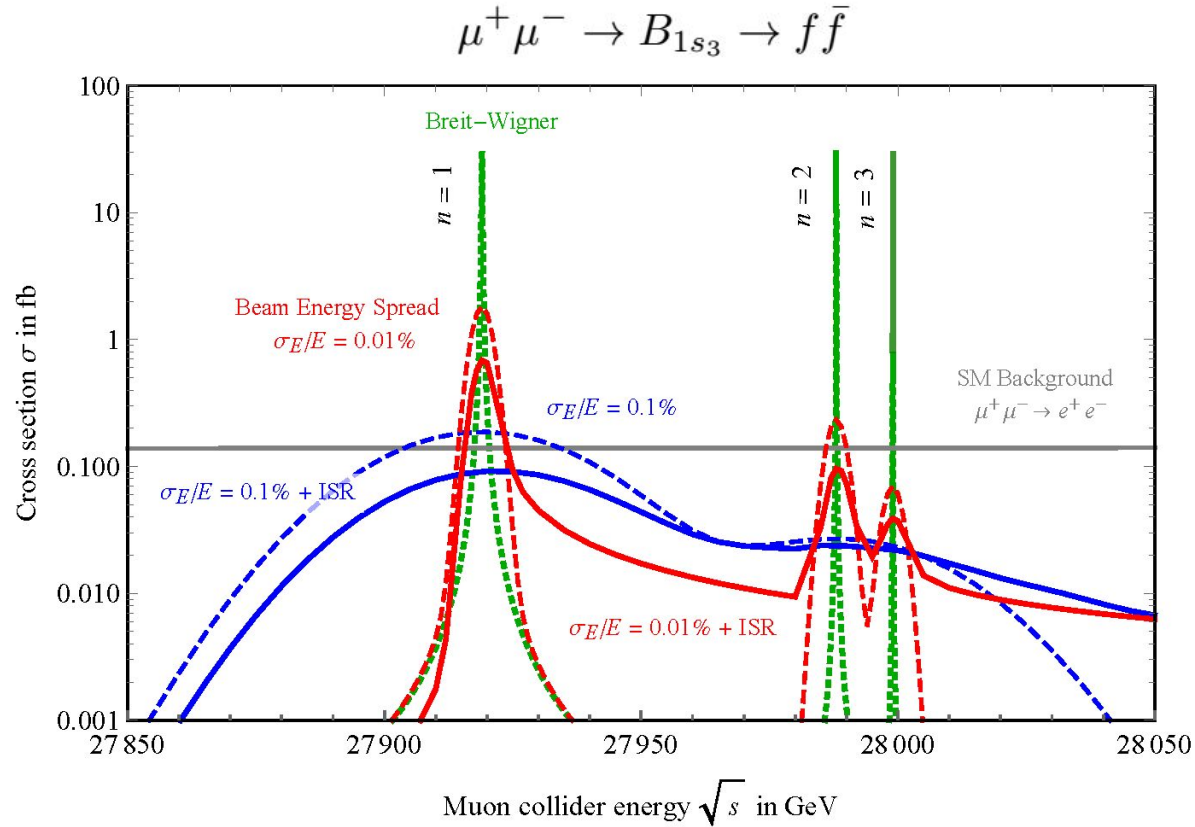


2σ : 35 TeV

$$\mathcal{L} \simeq 10 \text{ ab}^{-1} \cdot \left(\frac{\sqrt{s}}{10 \text{ TeV}} \right)^2$$

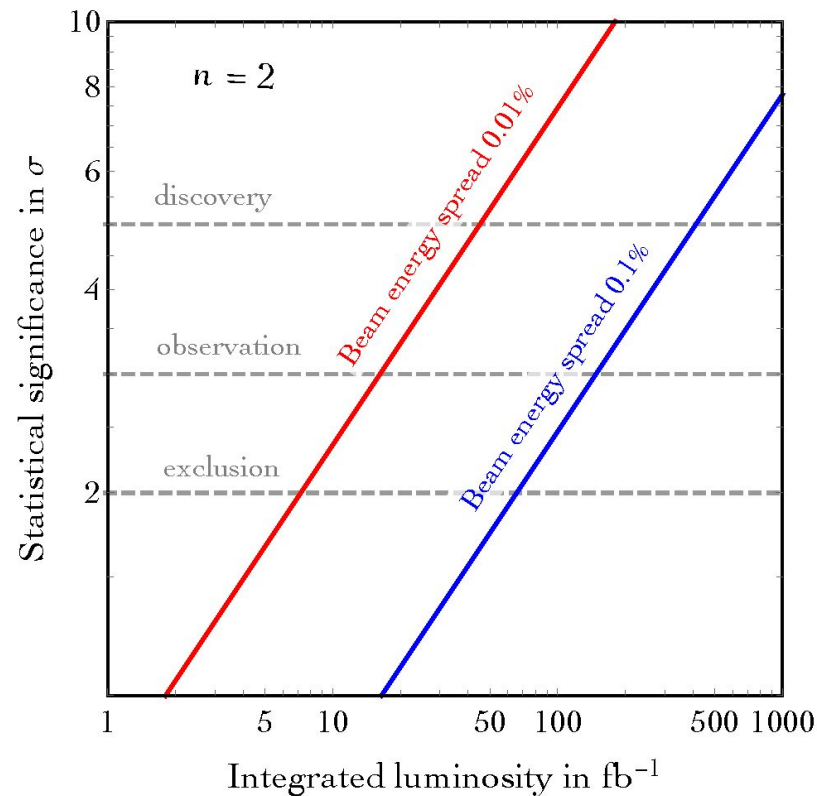
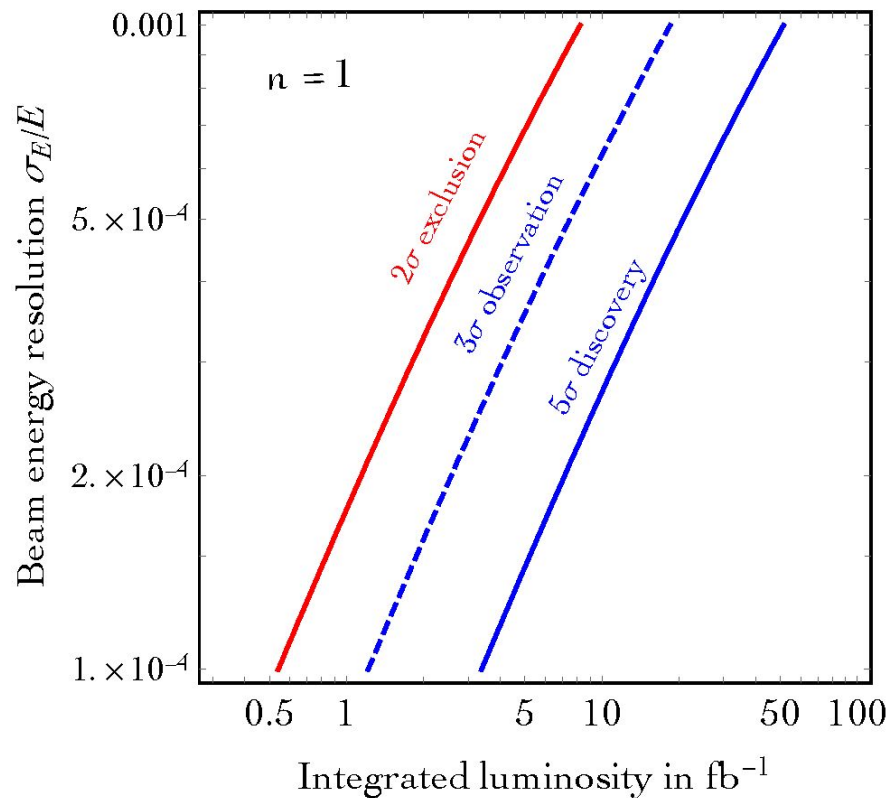
Bound states at muon colliders

2103.12766

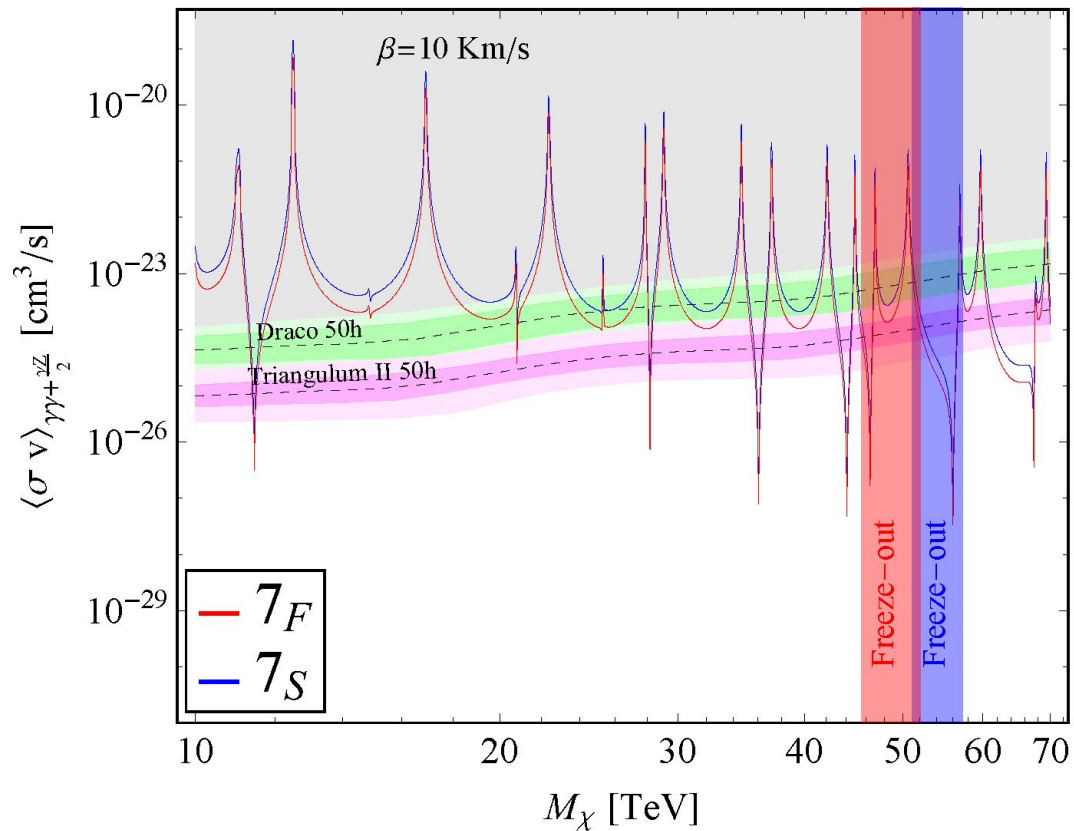


Bound states at muon colliders

2103.12766

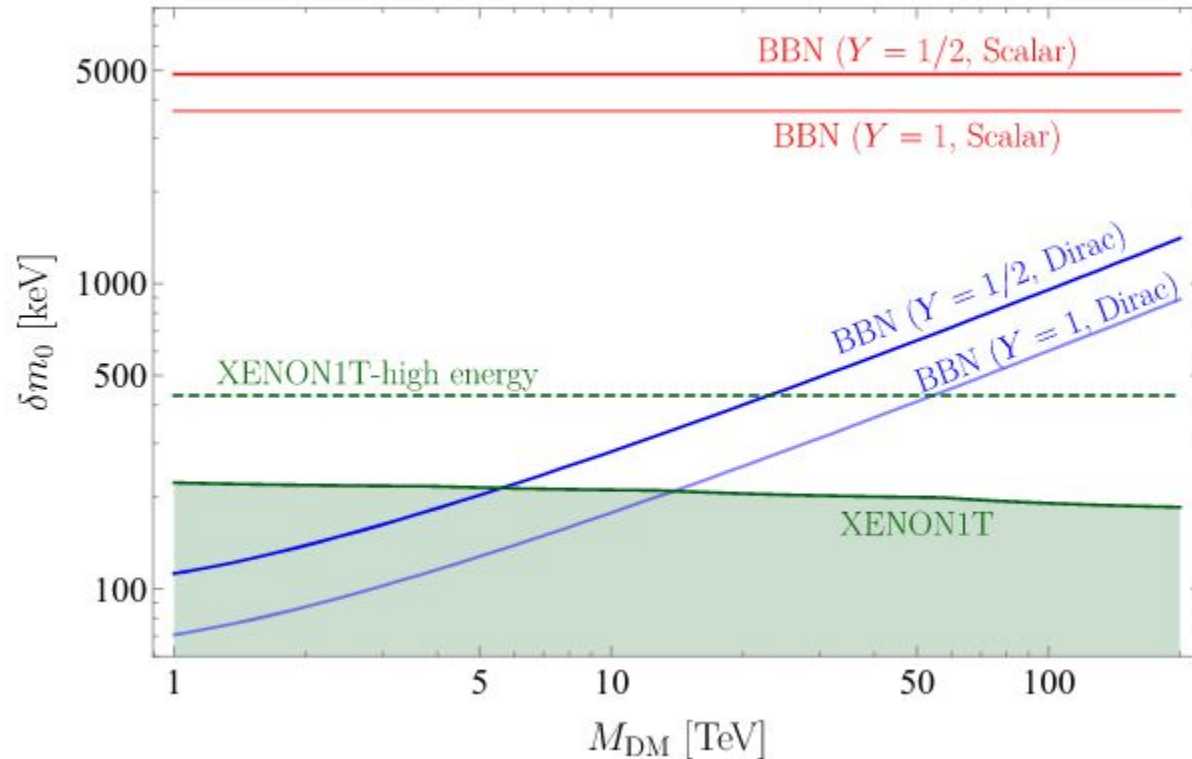


Indirect Detection

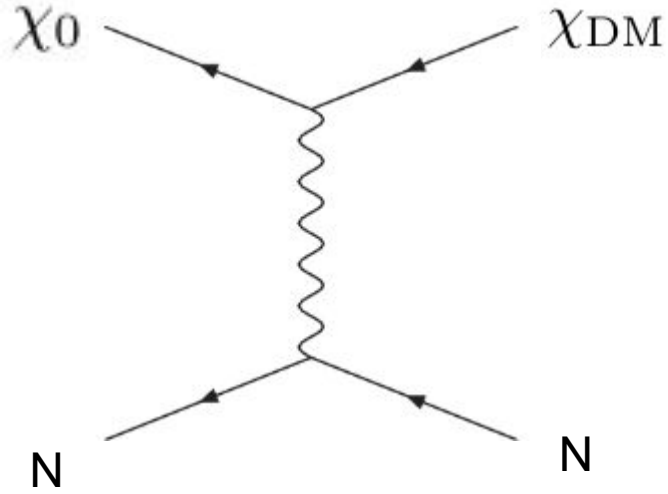


Complex WIMPs - $Y \neq 0$

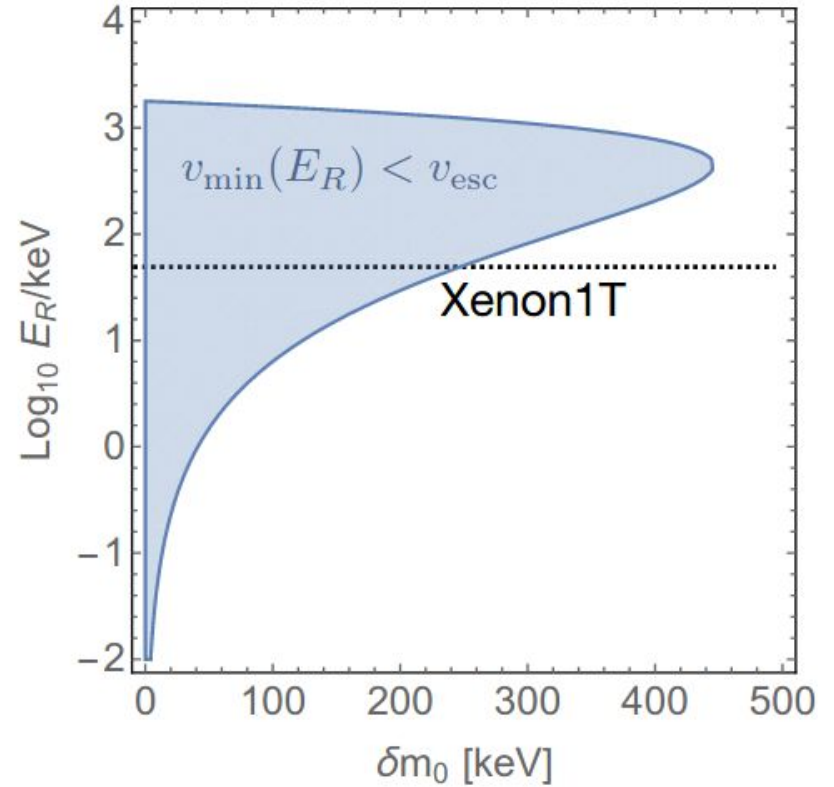
2205.04486



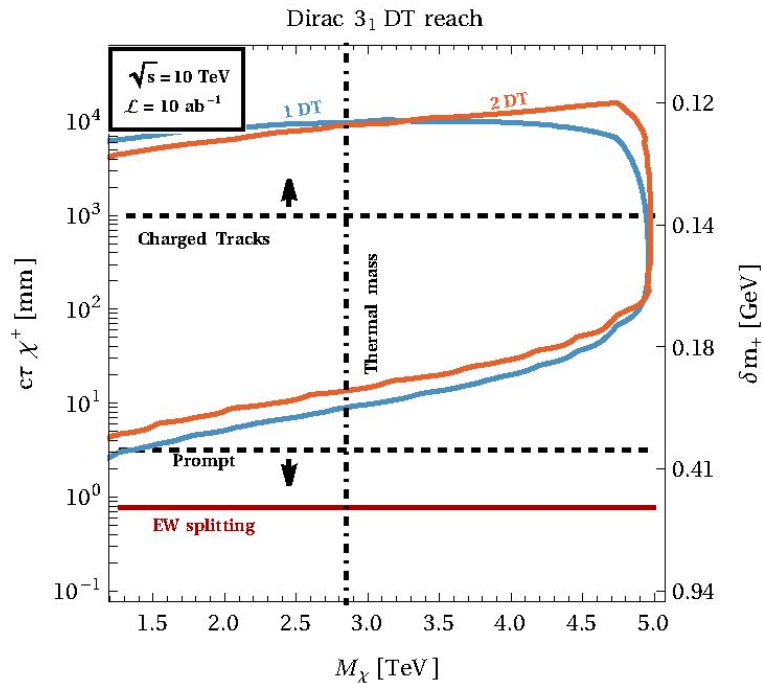
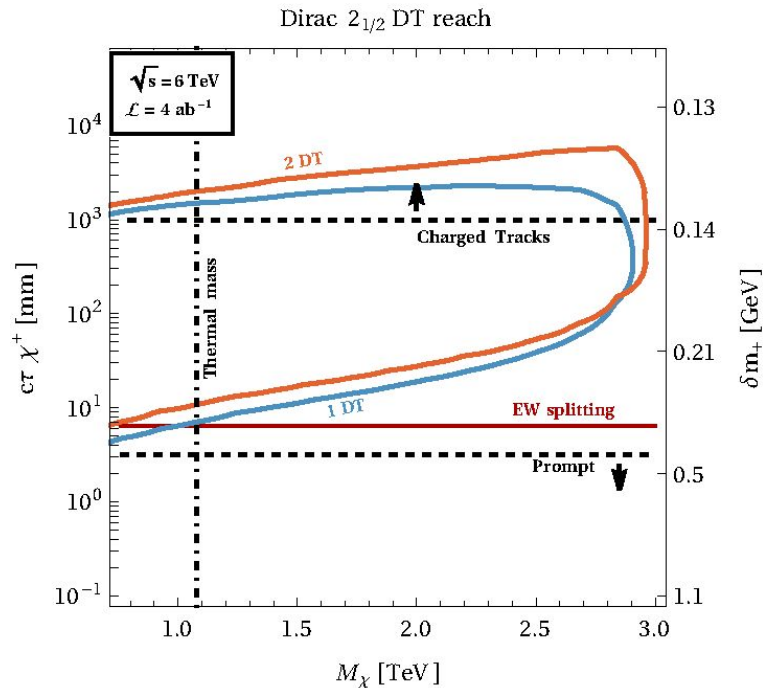
Inelastic DM



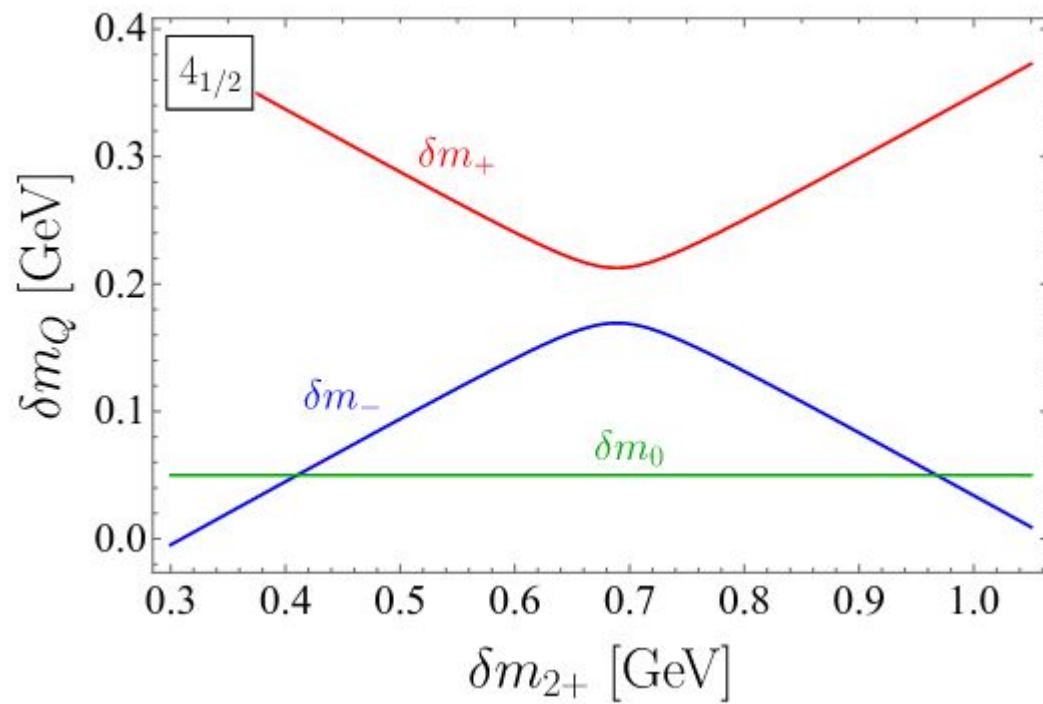
$$v_{\min}(E_R) = \frac{E_R + \delta m_0}{\sqrt{2m_N E_R}}$$



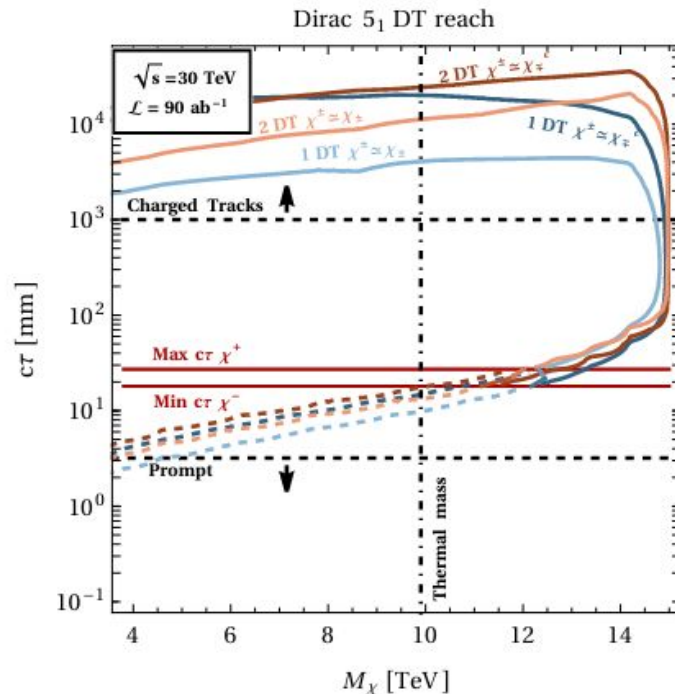
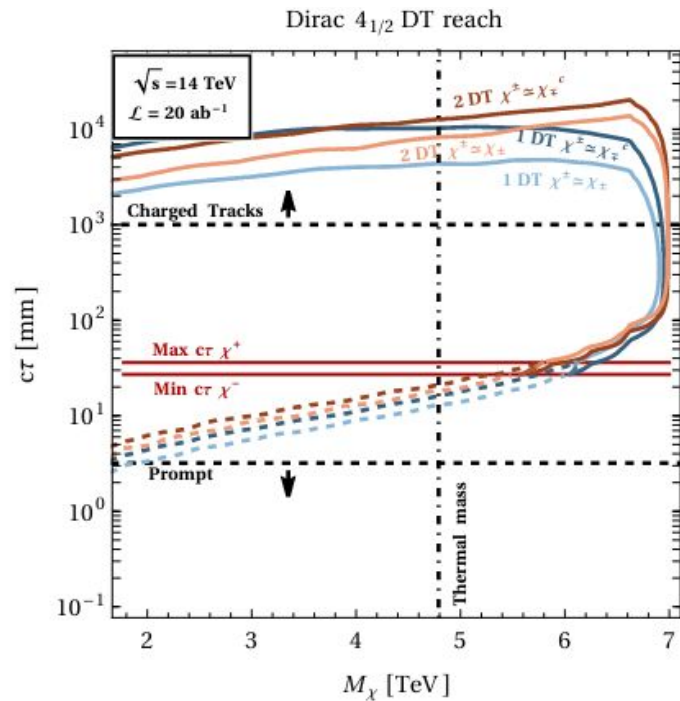
Reach Disappearing Tracks



Spectrum $4_{1/2}$

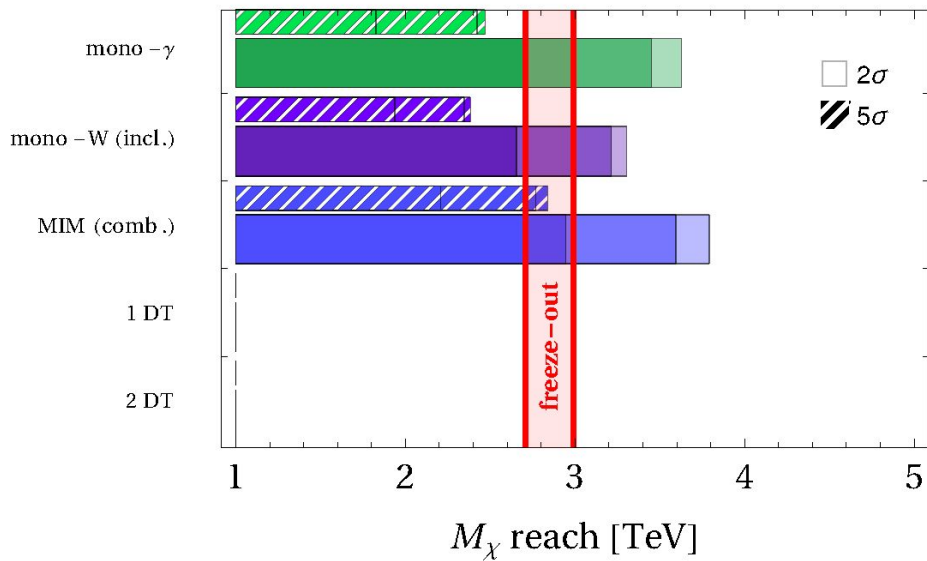


Reach Disappearing Tracks

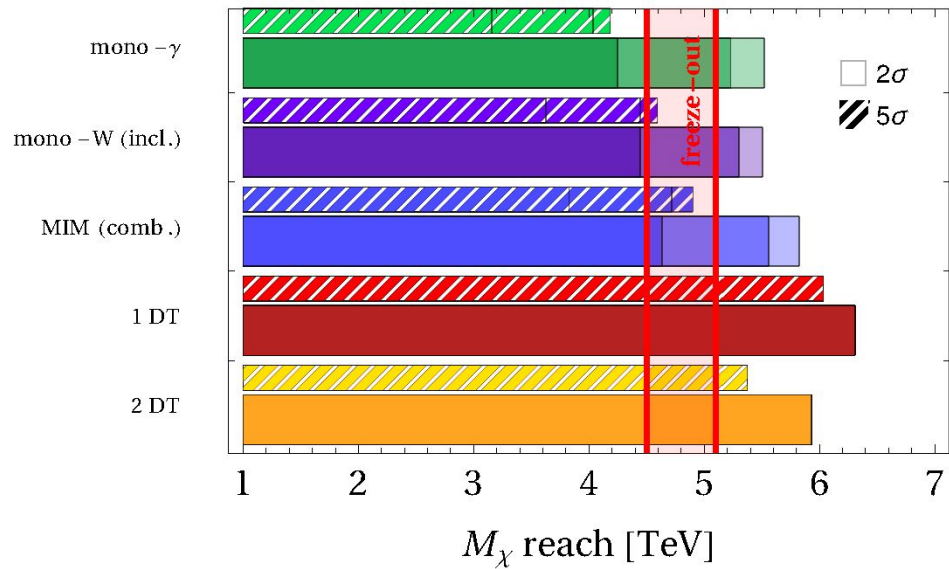


Reach

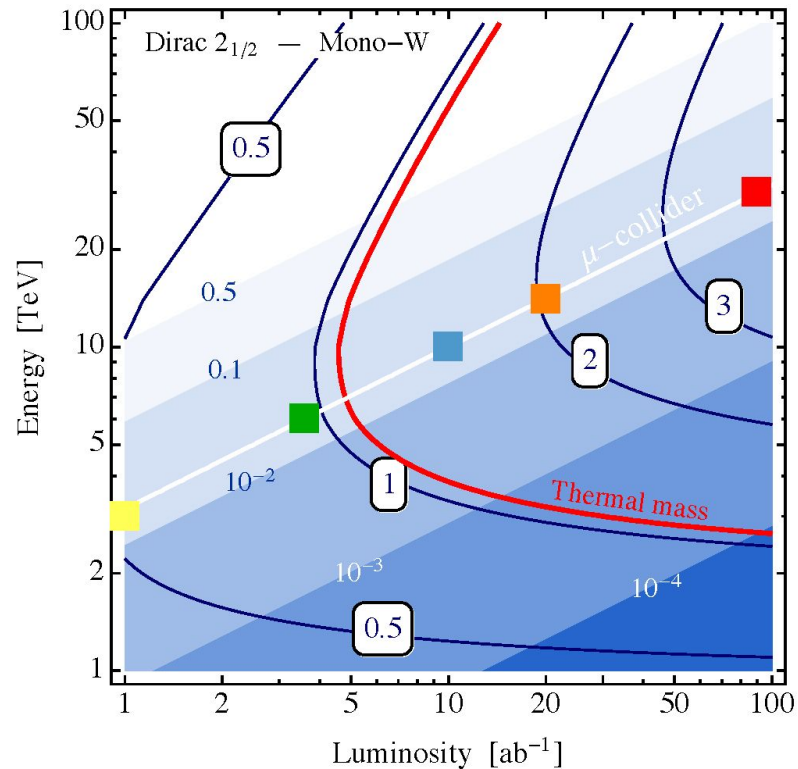
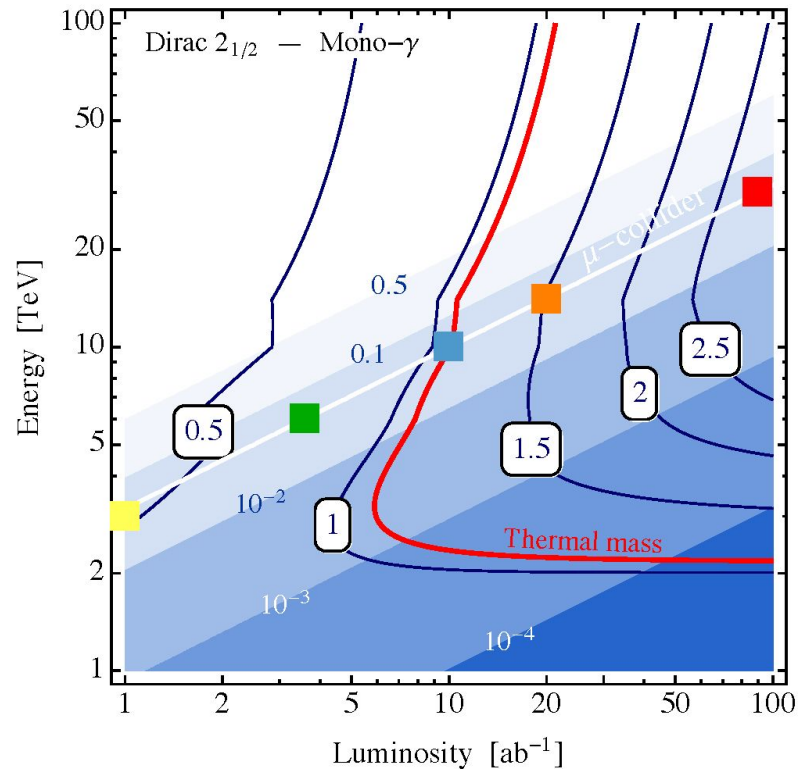
$\sqrt{s} = 10 \text{ TeV}, \mathcal{L} = 10 \text{ ab}^{-1}, \text{Dirac } 3_1$



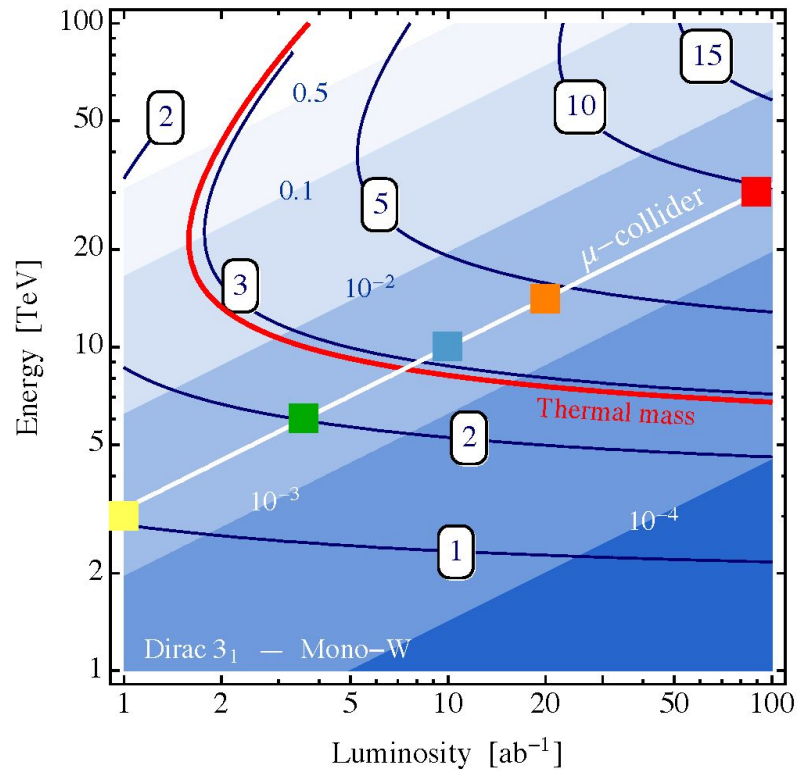
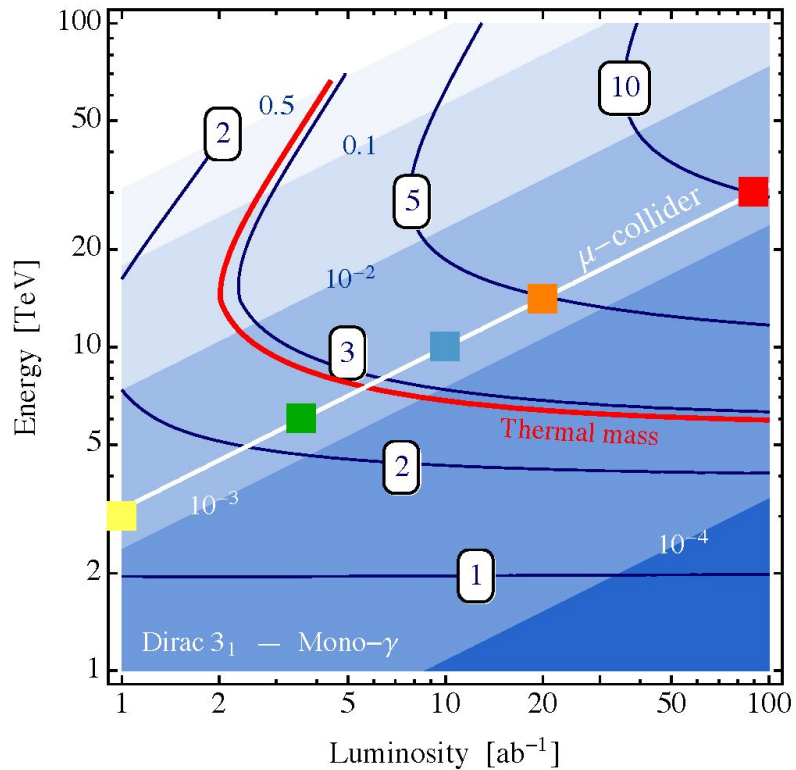
$\sqrt{s} = 14 \text{ TeV}, \mathcal{L} = 20 \text{ ab}^{-1}, \text{Dirac } 4_{1/2}$



Lumi vs Energy Dirac $2_{1/2}$



Lumi vs Energy Dirac 3_1



Lumi vs Energy Dirac $4_{1/2}$

