

# Extending the ALICE strong-interaction studies to nuclei: measurement of proton-deuteron correlations in pp collisions at $\sqrt{s} = 13$ TeV

**Bhawani Singh**

Technische Universität München

on behalf of the **ALICE Collaboration**



**ICHEP 2022  
BOLOGNA**



**ALICE**

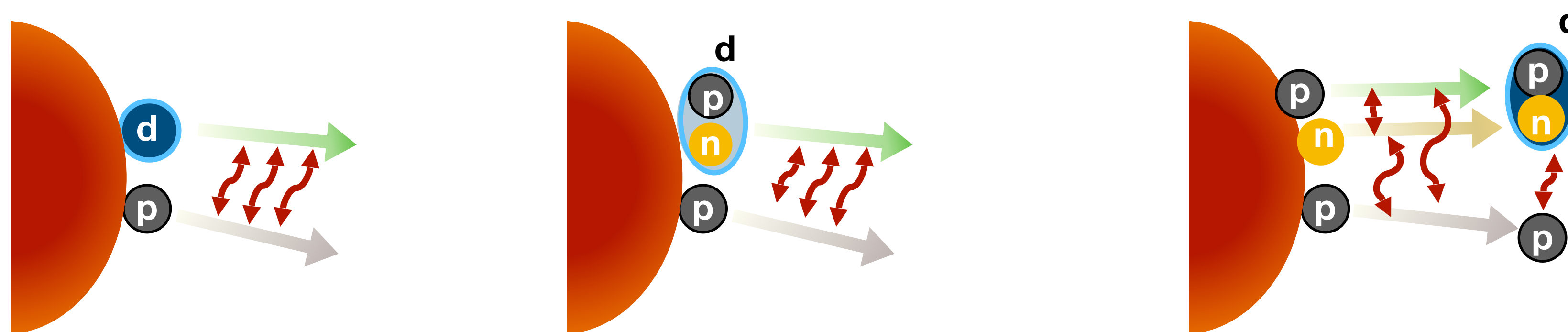


- **Proton-deuteron (p–d) interaction**

- Three-nucleon force: doorway to probe short distances
- p–d interaction can be constrained from the scattering experiments

- **Production mechanism of light nuclei not understood:**

- Models: information on single particle, **Statistical Hadronisation Model<sup>1, 2</sup>** or **Coalescence Model<sup>3</sup>**
- Final-state interactions: probe the formation time of deuterons (antideuterons)

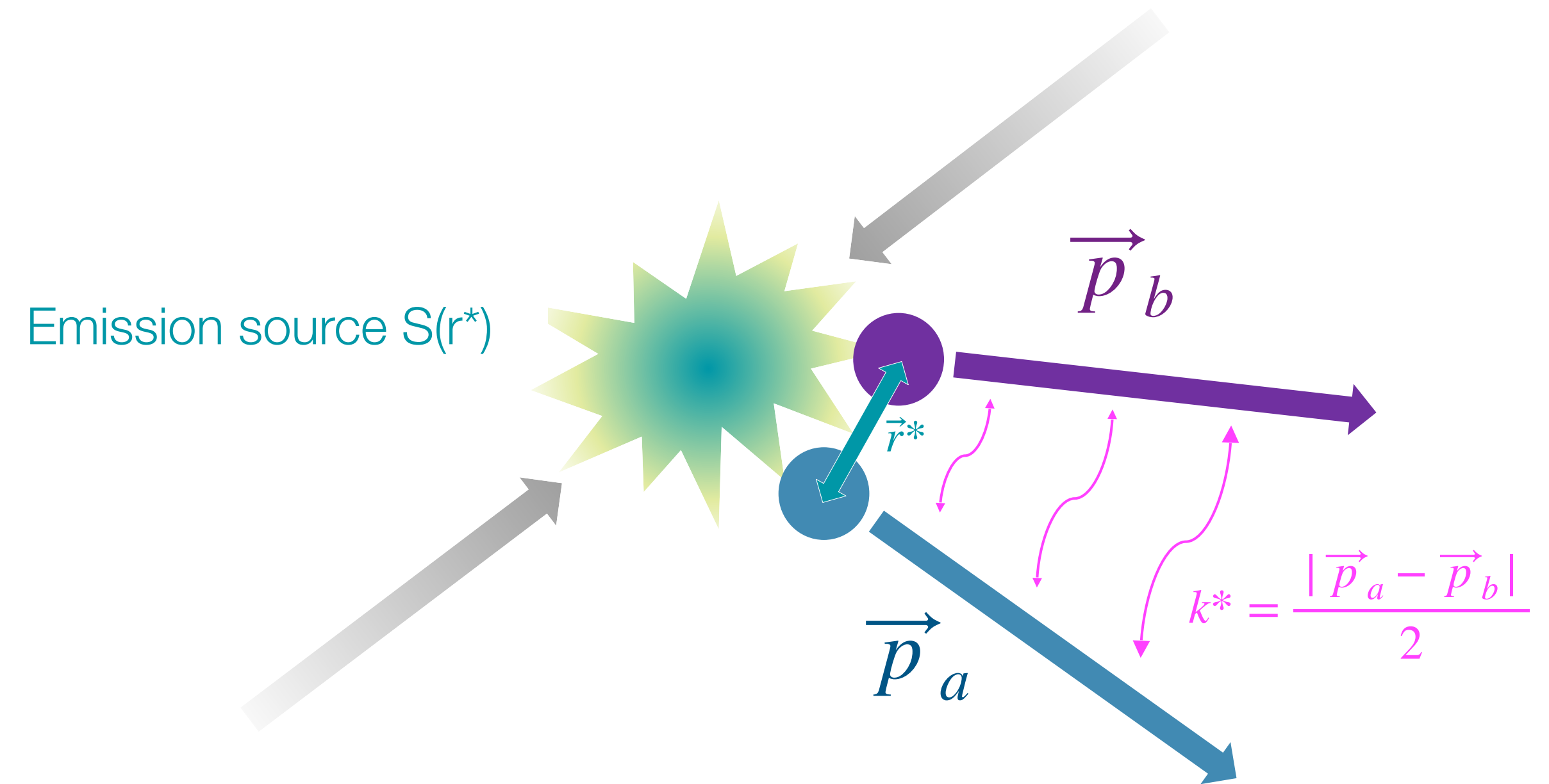


<sup>1</sup>J. Cleymans et al, Phys. Rev. C 74, 034903 (2006)

<sup>2</sup>J. Cleymans et al, Z. Phys. C 57, 135–147 (1993)

<sup>3</sup>K. Blum et al, Phys. Rev. C 99, 04491(2019)

- **Main observable:** correlation in the relative momentum  $k^*$  distribution of a particle pair
  - **Emitting source:** hypersurface of kinematic freeze-out for final-state particles, in pp collision the source size  $\sim 1$  fm (Gaussian profile)
  - **Two-particle relative wave function:** expresses the interaction between particles
- Study the emission source if the interaction among the particle pair is known
- Or study the interaction among the particles if emission source is known



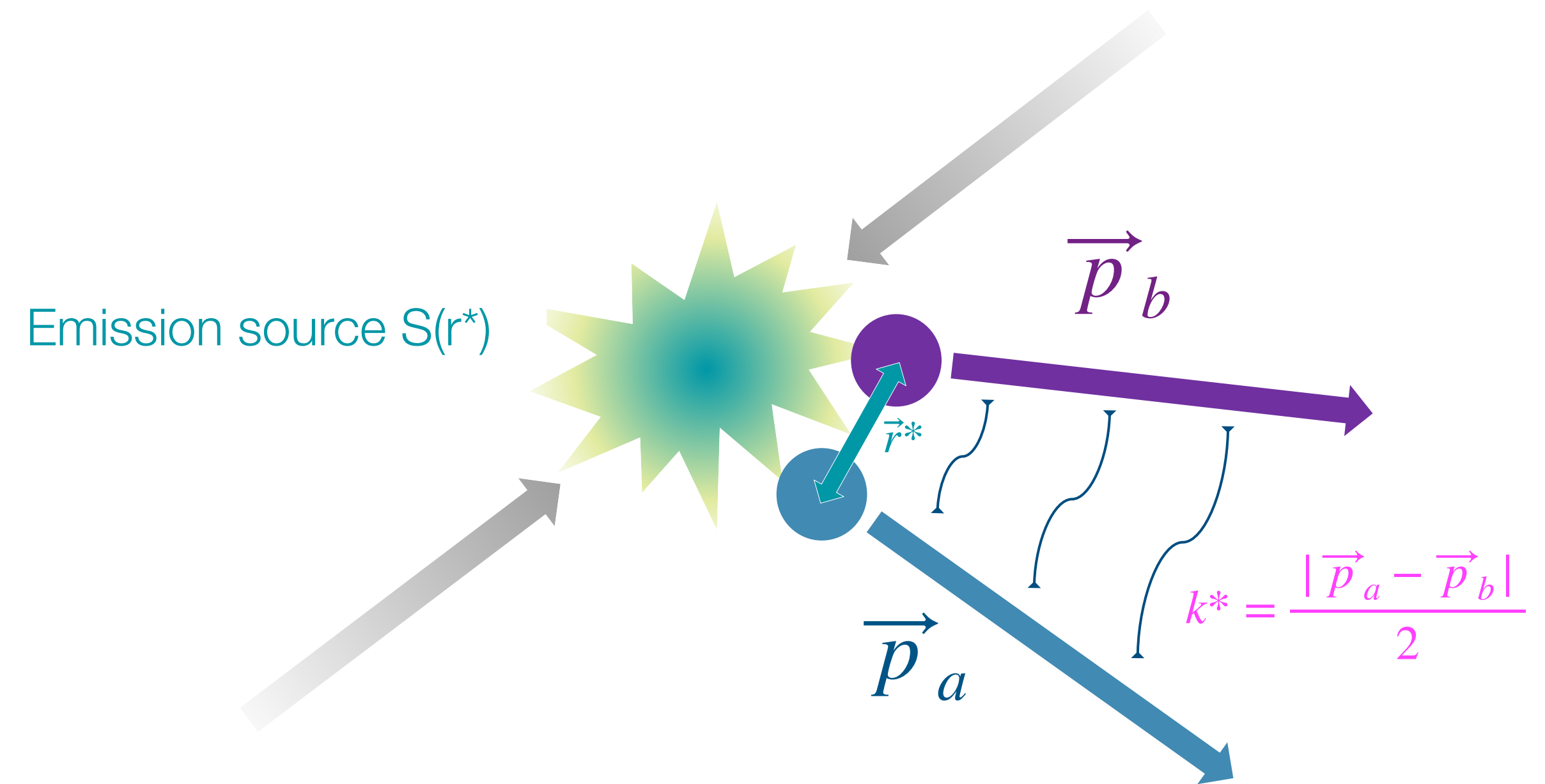
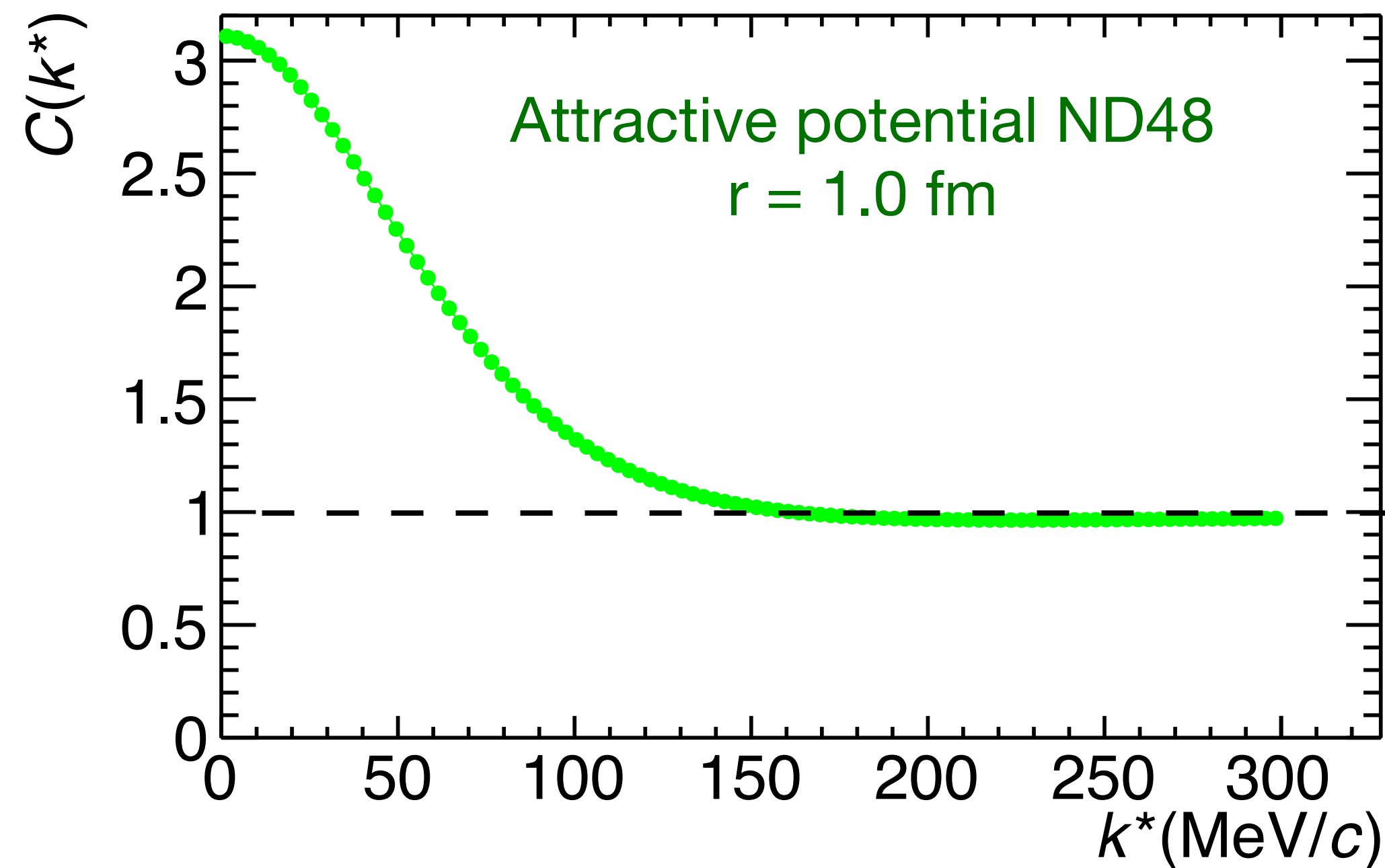
**Koonin-Pratt Equation**

$$C(k^*) = \underbrace{\int S(\vec{r}^*) \left| \psi(\vec{k}^*, \vec{r}^*) \right|^2 d^3\vec{r}^*}_{\text{theoretical definition}} = \underbrace{\mathcal{N} \frac{N_{\text{same}}(k^*)}{N_{\text{mixed}}(k^*)}}_{\text{experimental definition}} \xrightarrow{k^* \rightarrow \infty} 1$$

*CATS Framework: D. Mihaylov et al., EPJ. C78 (2018) 394  
S.E. Koonin PLB 70 43 (1977)*



- Correlation rises above 1 for attractive potentials

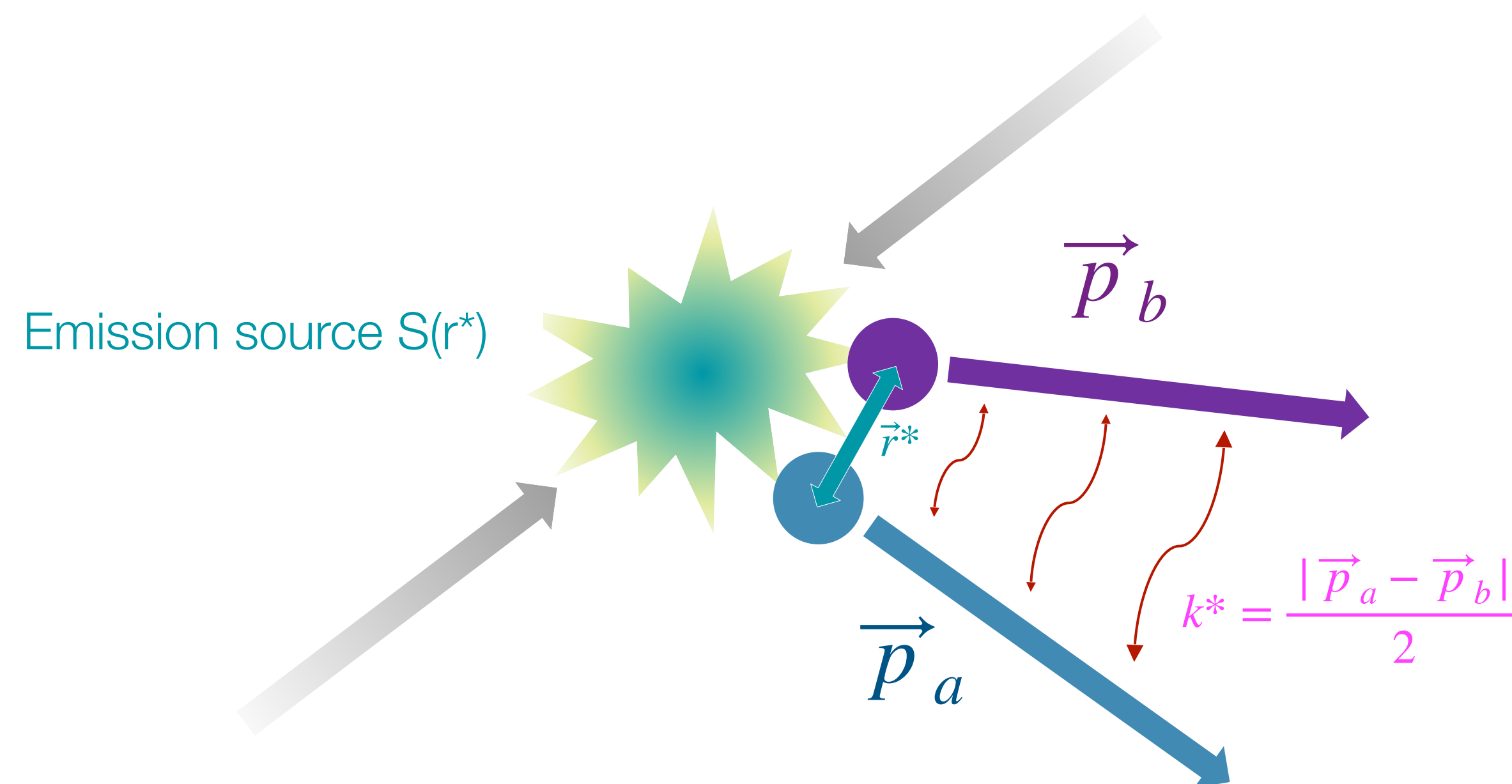
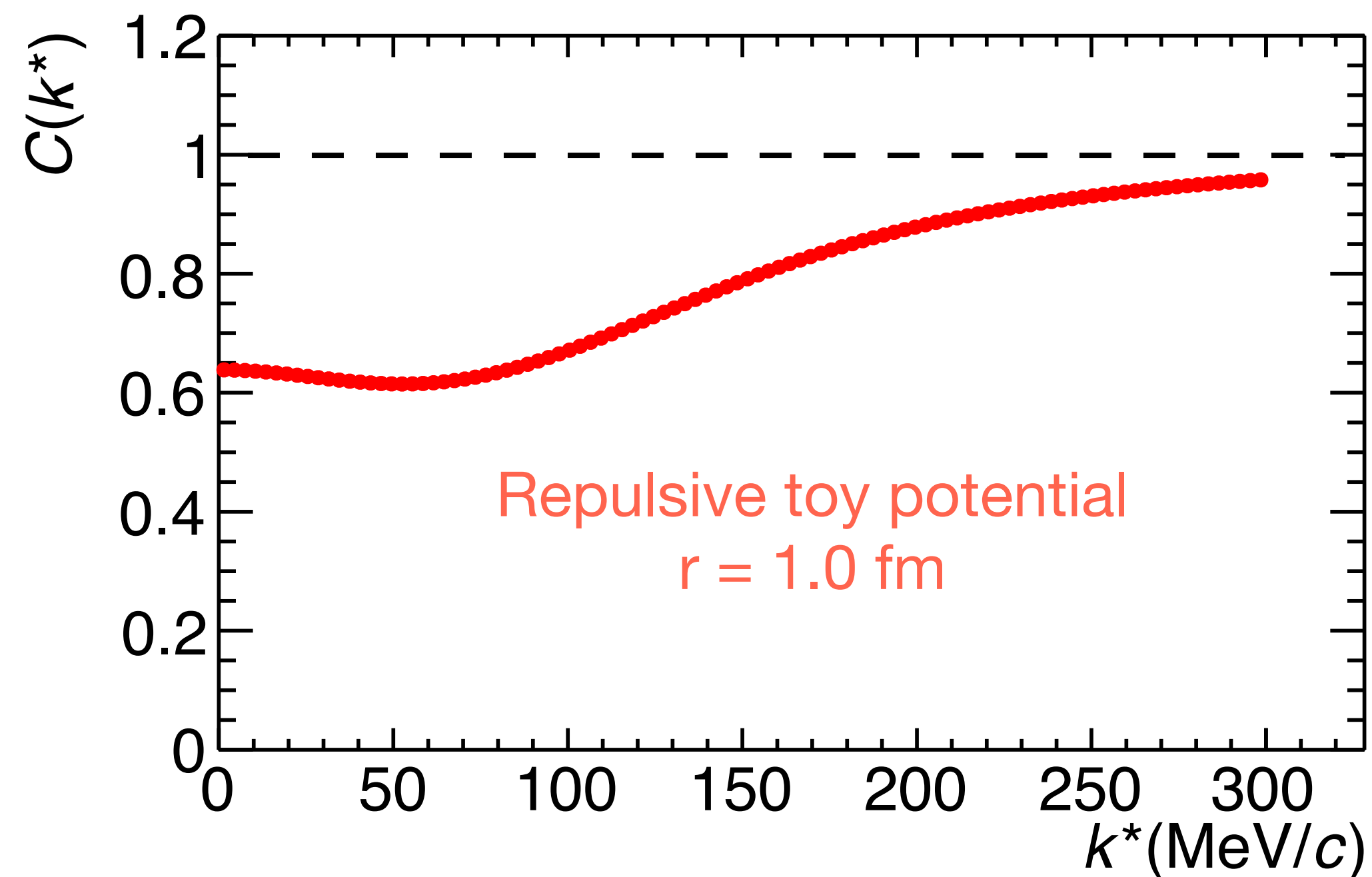


Koonin-Pratt Equation

$$C(k^*) = \underbrace{\int S(\vec{r}^*) \left| \psi(\vec{k}^*, \vec{r}^*) \right|^2 d^3 \vec{r}^*}_{\text{theoretical definition}} = \underbrace{\mathcal{N} \frac{N_{\text{same}}(k^*)}{N_{\text{mixed}}(k^*)}}_{\text{experimental definition}} > 1$$

CATS Framework: D. Mihaylov et al., EPJ. C78 (2018) 394  
S.E. Koonin PLB 70 43 (1977)

- Repulsive interaction brings correlation below 1



**Koonin-Pratt Equation**

$$C(k^*) = \underbrace{\int S(\vec{r}^*) \left| \psi(\vec{k}^*, \vec{r}^*) \right|^2 d^3 \vec{r}^*}_{\text{theoretical definition}} = \underbrace{\mathcal{N} \frac{N_{\text{same}}(k^*)}{N_{\text{mixed}}(k^*)}}_{\text{experimental definition}} < 1$$

*CATS Framework: D. Mihaylov et al., EPJ. C78 (2018) 394  
S.E. Koonin PLB 70 43 (1977)*



- General purpose heavy-ion experiment

- Excellent particle identification (PID)
- Most suited LHC experiment for studying femtoscopic correlations

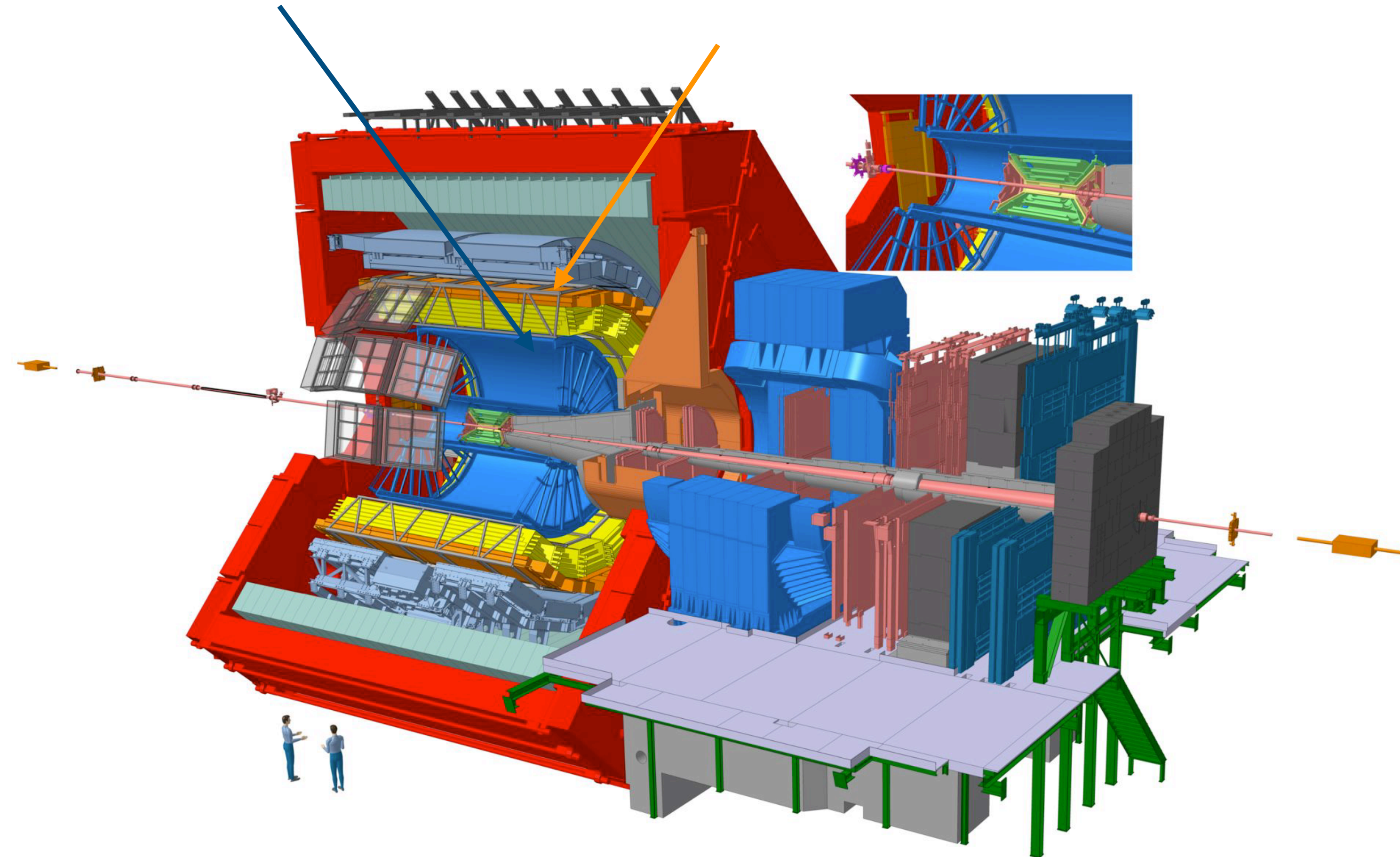
- Run 2 high-multiplicity data

- Number of events:  $\sim 1 \times 10^9$

- Particle selection with TPC + TOF

- p(anti-p) : **98.30% (98.76%)**
- d(anti-d) :  **$\sim 100\%$**

Time Projection Chamber (TPC)    Time of Flight (TOF)





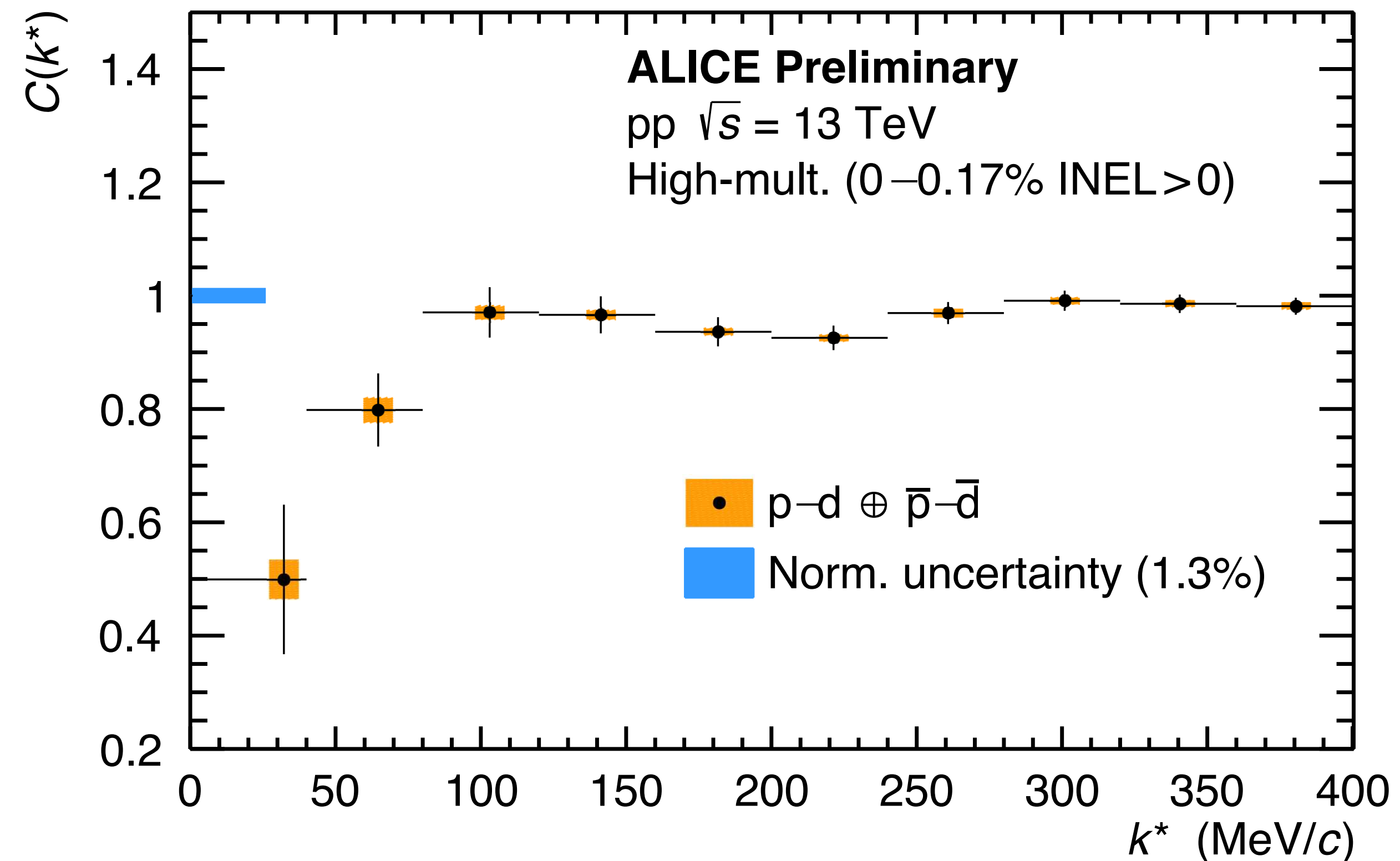
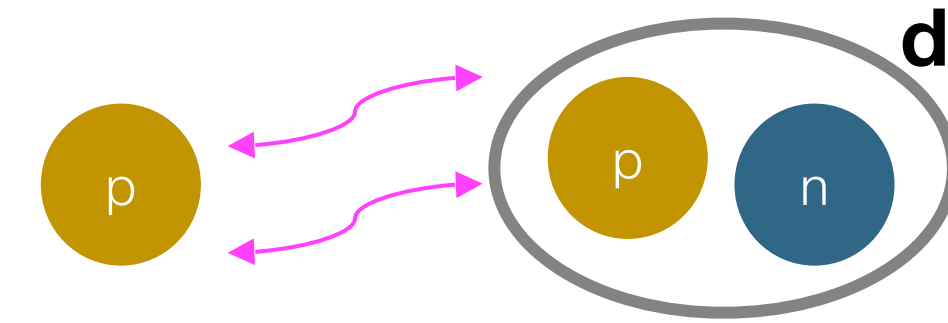
# First measurement of proton-deuteron

- $p-d \oplus \bar{p}-\bar{d}$  correlation

- Measured p-d correlation not flat, shows depletion at low  $k^*$
- Repulsive type of interaction
- Accessing spin-isospin dependence of NNN

- Pairs below  $k^* < 200$  MeV/c

- p-d: 1747
- p-d: 1250

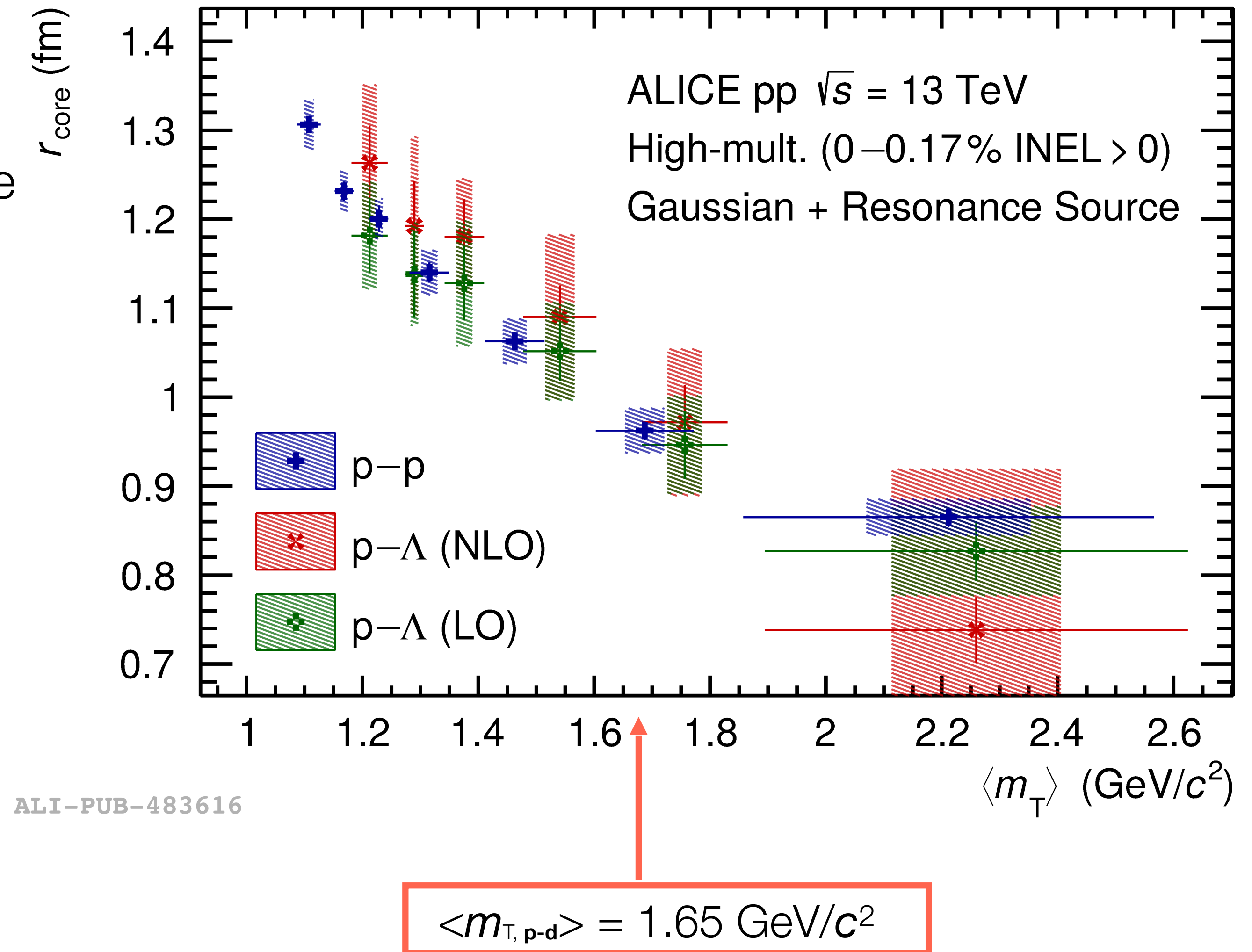


ALI-PREL-486400

# The source

- Short distances in pp and p—Pb collisions
- Particle emission from **Gaussian core** source

Source size	mean value
$r_{\text{core}}$	$0.97 \pm 0.04$ fm

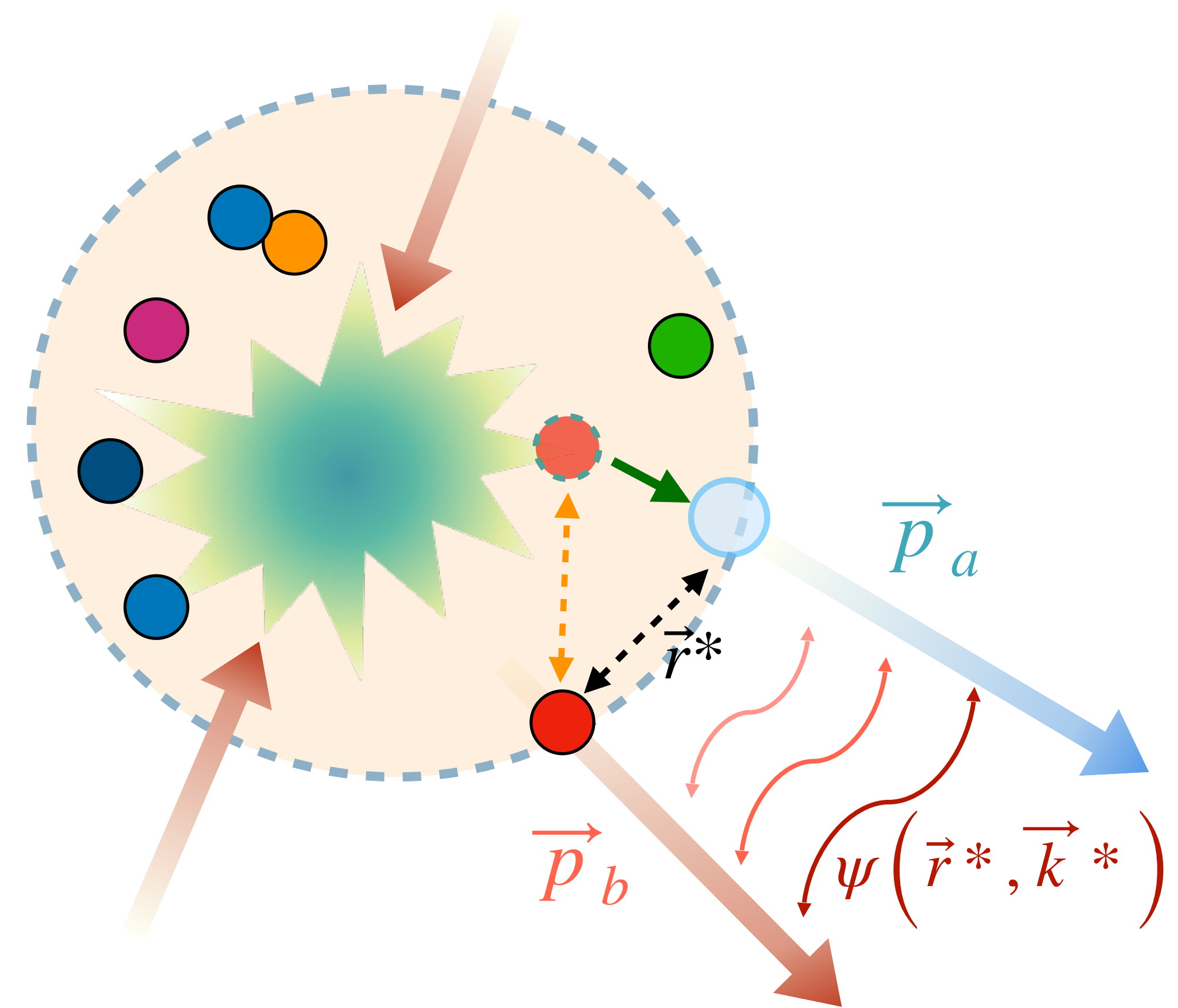


ALICE Coll. PLB 811 135849 (2020)



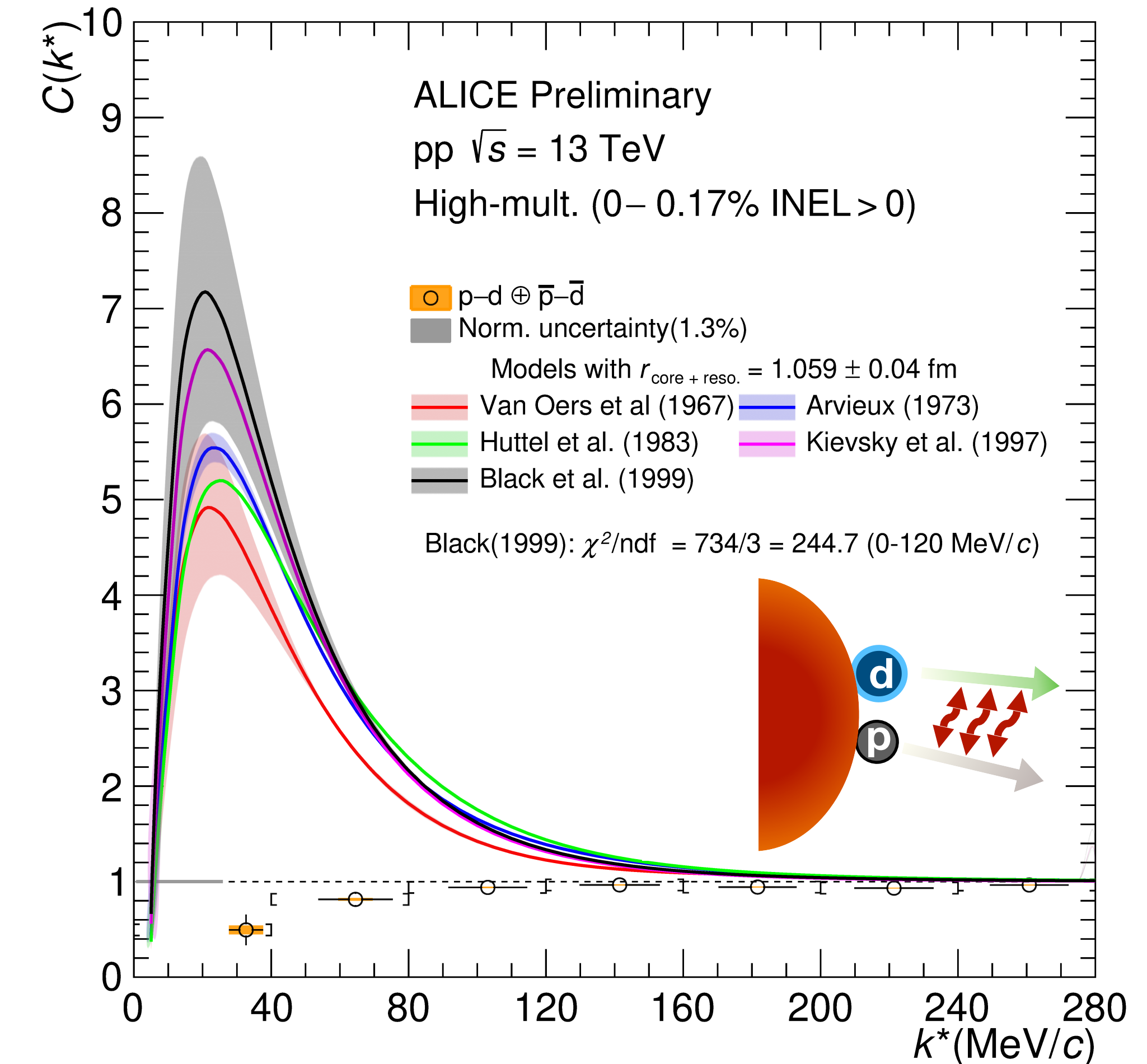
- Short distances in pp and p—Pb collisions
- Particle emission from **Gaussian core** source
- The source radius is effectively increased by **short-lived strongly decaying resonances** ( $c\tau \approx r_{\text{core}}$ ) e.g.  $\Delta$ -resonances in case of protons

Source size	mean value
$r_{\text{core}}$	$0.97 \pm 0.04$ fm
$r_{\text{eff}}$	$1.06 \pm 0.04$ fm



ALICE Coll. PLB 811 135849 (2020)

- Two-particle s-wavefunction accounting for Coulomb and strong interaction<sup>1</sup>
  - Coulomb + strong interaction ( $S = 1/2$  and  $S = 3/2$ )
  - Assumption: p and d are point-like particles!
  - Theoretical model constrained to scattering p–d experiments



ALI-PREL-501009

Van Oers, Brockmann et al. Nucl. Phys. A 561-583 (1967)

J. Arvieux et al. Nucl. Phys. A 221 253-268 (1973)

E. Huttel et al. Nucl. Phys. A 406 443-455 (1983)

A. Kievsky et al. PLB 406 292-296 (1997)

T.C. Black et al. PLB 471 103-107 (1999)

Ref	Quartet $^4S_{3/2}$	Doublet $^2S_{1/2}$
Oers, Brockmann et al. (1967)	$11.4^{+1.8}_{-1.2}$	$1.2^{+0.2}_{-0.2}$
Arvieux et al. (1973)	$11.88^{+0.4}_{-0.1}$	$2.73^{+0.1}_{-0.1}$
Huttel et al. (1983)	11.1	4.0
Kievsky et al. (1997)	13.8	0.024
Black et al. (1999)	$14.7^{+2.3}_{-2.3}$	$-0.13^{+0.04}_{-0.04}$

<sup>1</sup>R. Lednicky, Phys. Part. Nuclei 40, 307–352 (2009)

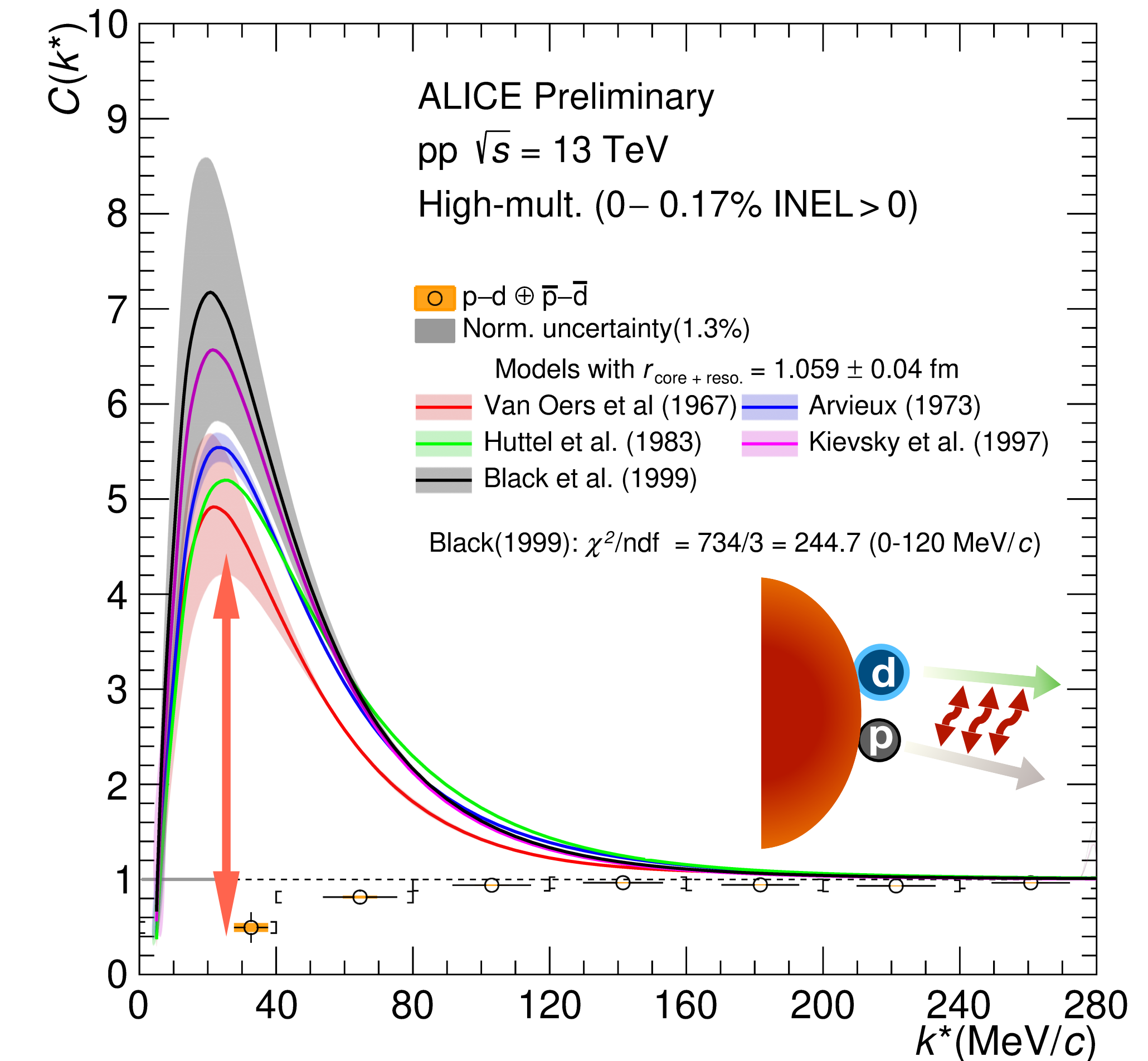


- Two-particle s-wavefunction accounting for Coulomb and strong interaction<sup>1</sup>
  - Coulomb + strong interaction ( $S = 1/2$  and  $S = 3/2$ )
  - Assumption: p and d are point-like particles!
  - Theoretical model constrained to scattering p–d experiments

Ref	Quartet $^4S_{3/2}$	Doublet $^2S_{1/2}$
Oers, Brockmann et al.(1967)	$11.4^{+1.8}_{-1.2}$	$1.2^{+0.2}_{-0.2}$
Arvieux et al.(1973)	$11.88^{+0.4}_{-0.1}$	$2.73^{+0.1}_{-0.1}$
Huttel et al.(1983)	11.1	4.0
Kievsky et al.(1997)	13.8	0.024
Black et al. (1999)	$14.7^{+2.3}_{-2.3}$	$-0.13^{+0.04}_{-0.04}$

**Model and data disagree for source size =  $1.06 \pm 0.04$  fm!**

<sup>1</sup>R. Lednicky, Phys. Part. Nuclei 40, 307–352 (2009)



ALI-PREL-501009

Van Oers, Brockmann et al. Nucl. Phys. A 561-583 (1967)

J. Arvieux et al. Nucl. Phys. A 221 253-268 (1973)

E. Huttel et al. Nucl. Phys. A 406 443-455 (1983)

A. Kievsky et al. PLB 406 292-296 (1997)

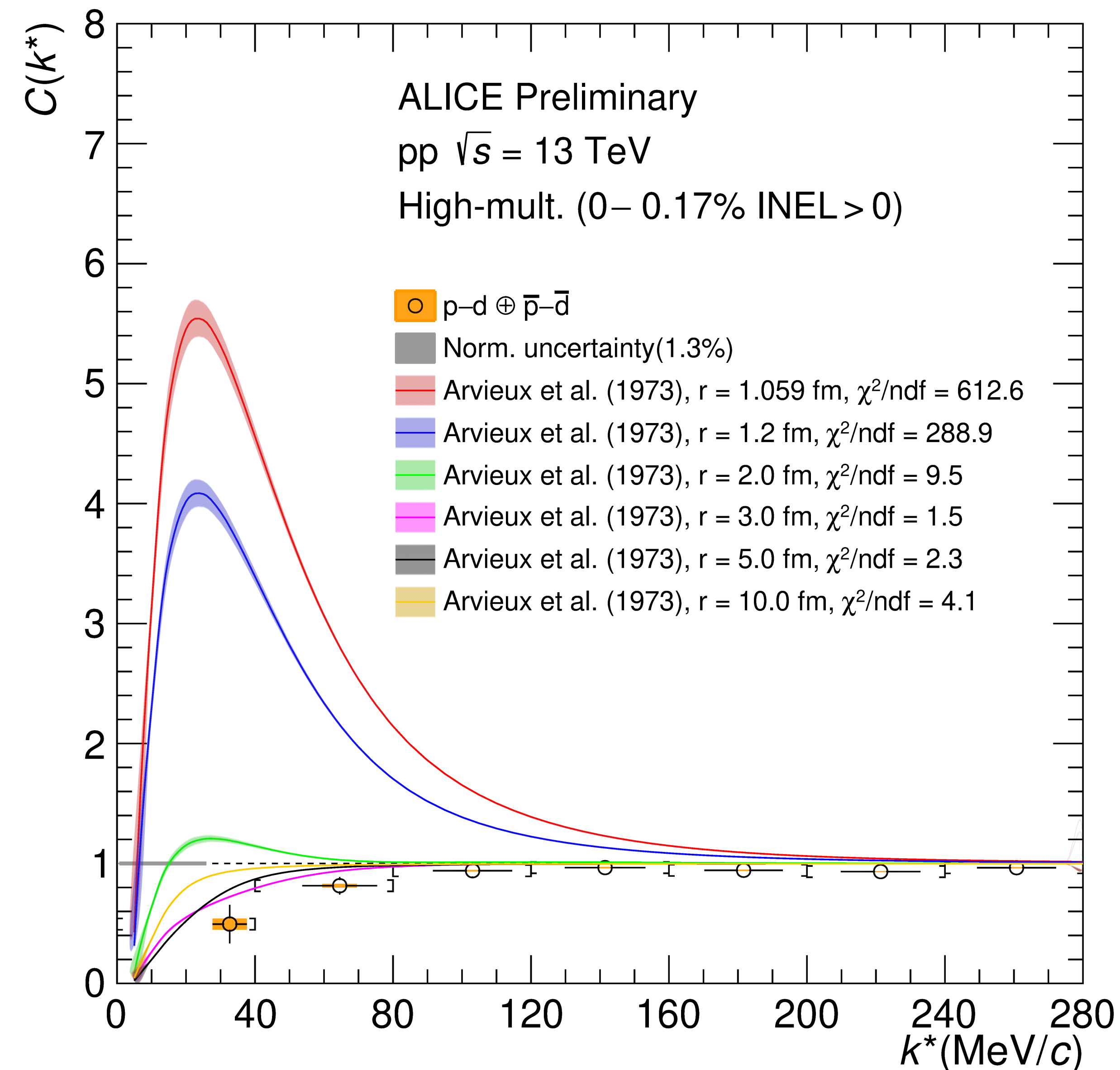
T.C. Black et al. PLB 471 103-107 (1999)

# Increased source size deuteron(antideuteron)

- Improved agreement with larger source sizes
- CF becomes flat at larger source size
- The effect of attractive strong interaction in the CF is diluted

## Assumptions

- ➔ Model does not account for p-(p-n) interaction
- ➔ Deuteron as point like particle



ALI-DER-500988



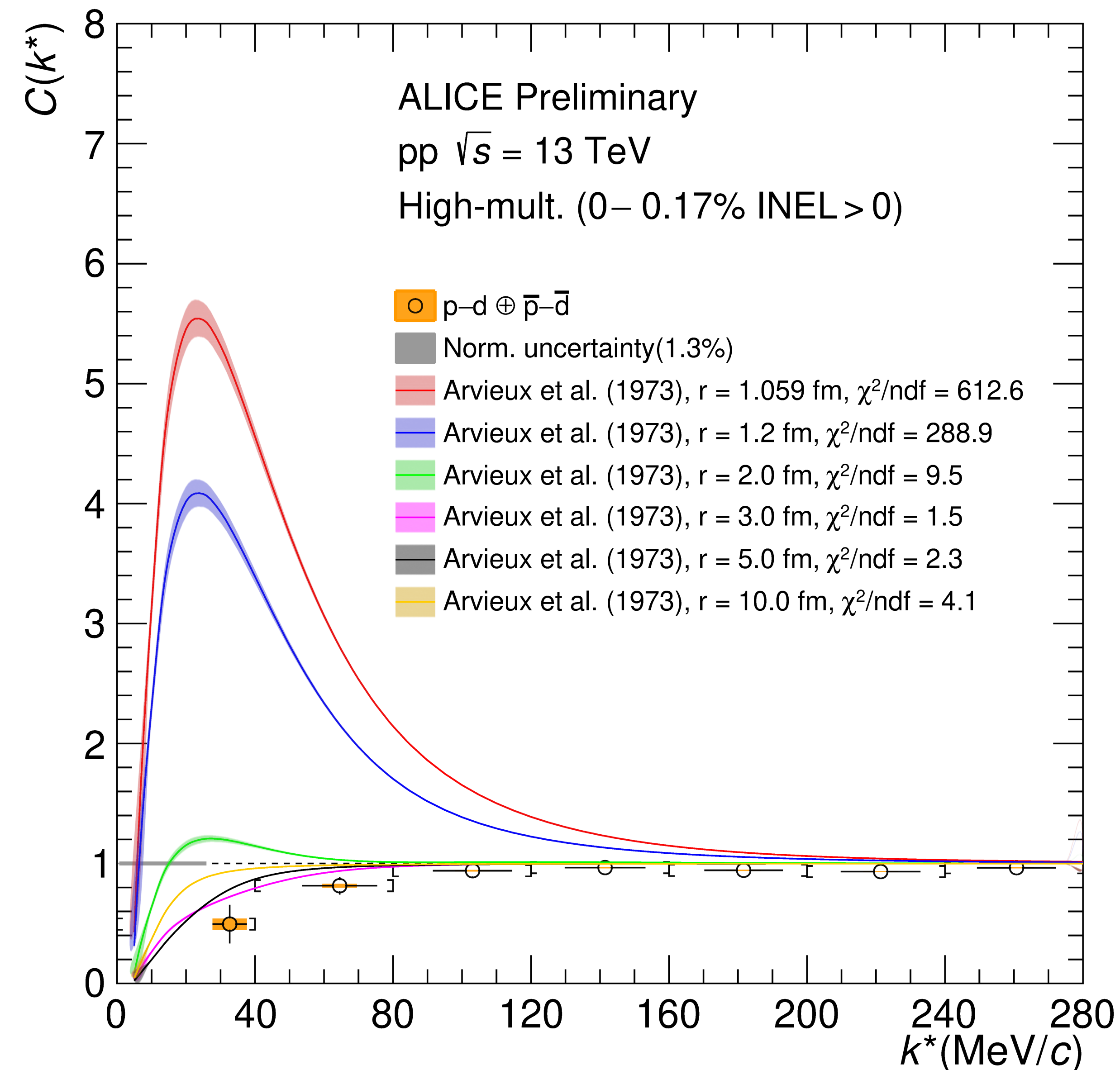
# Increased source size deuteron(antideuteron)

- Improved agreement with larger source sizes
- CF becomes flat at larger source size
- The effect of attractive strong interaction in the CF is diluted

## Assumptions

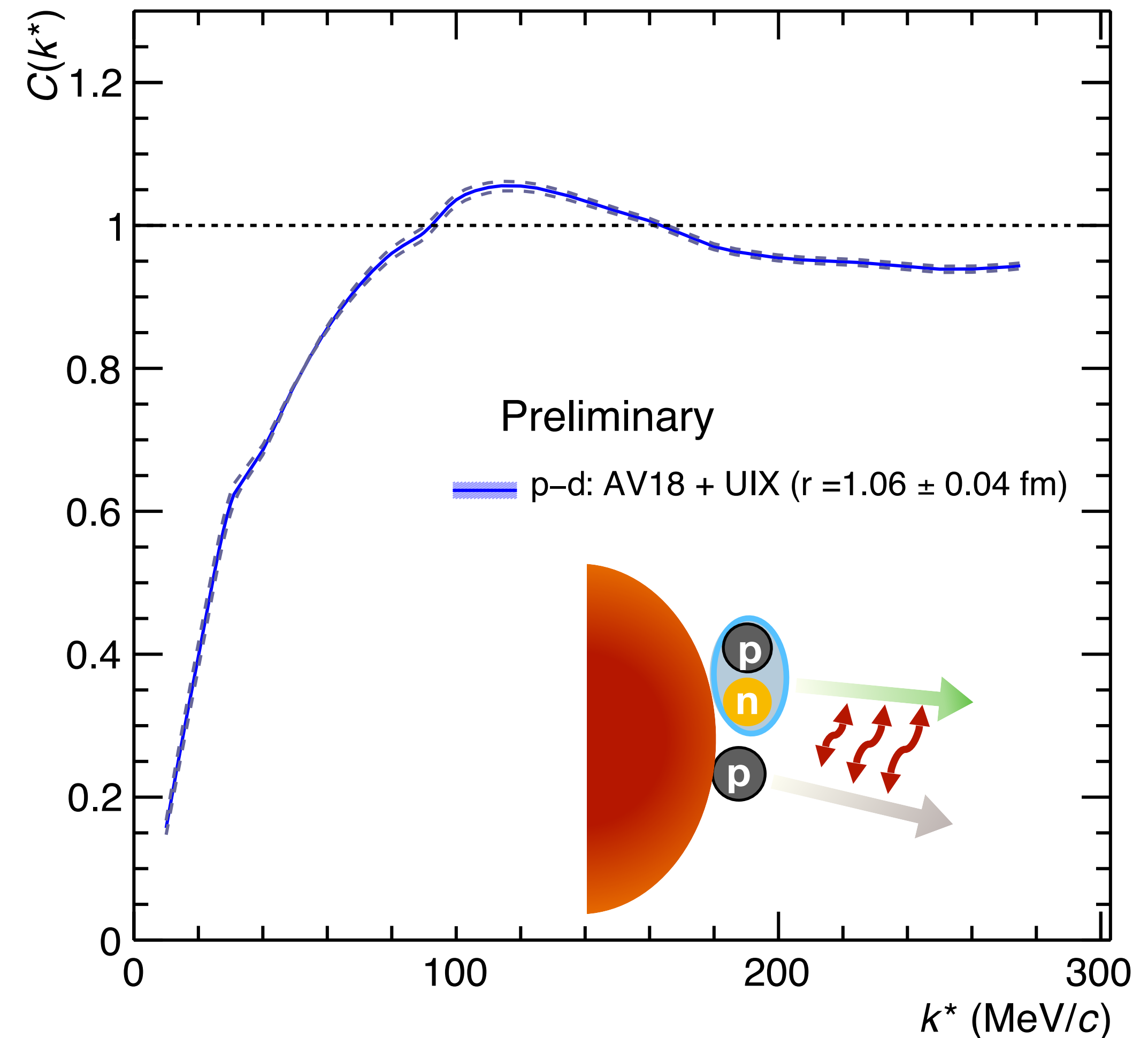
- ➔ Model does not account for p-(p-n) interaction
- ➔ Deuteron as point like particle

Work in progress: project the pair-wise and genuine three-body interaction of p-(p-n) on the p-d correlations



ALI-DER-500988

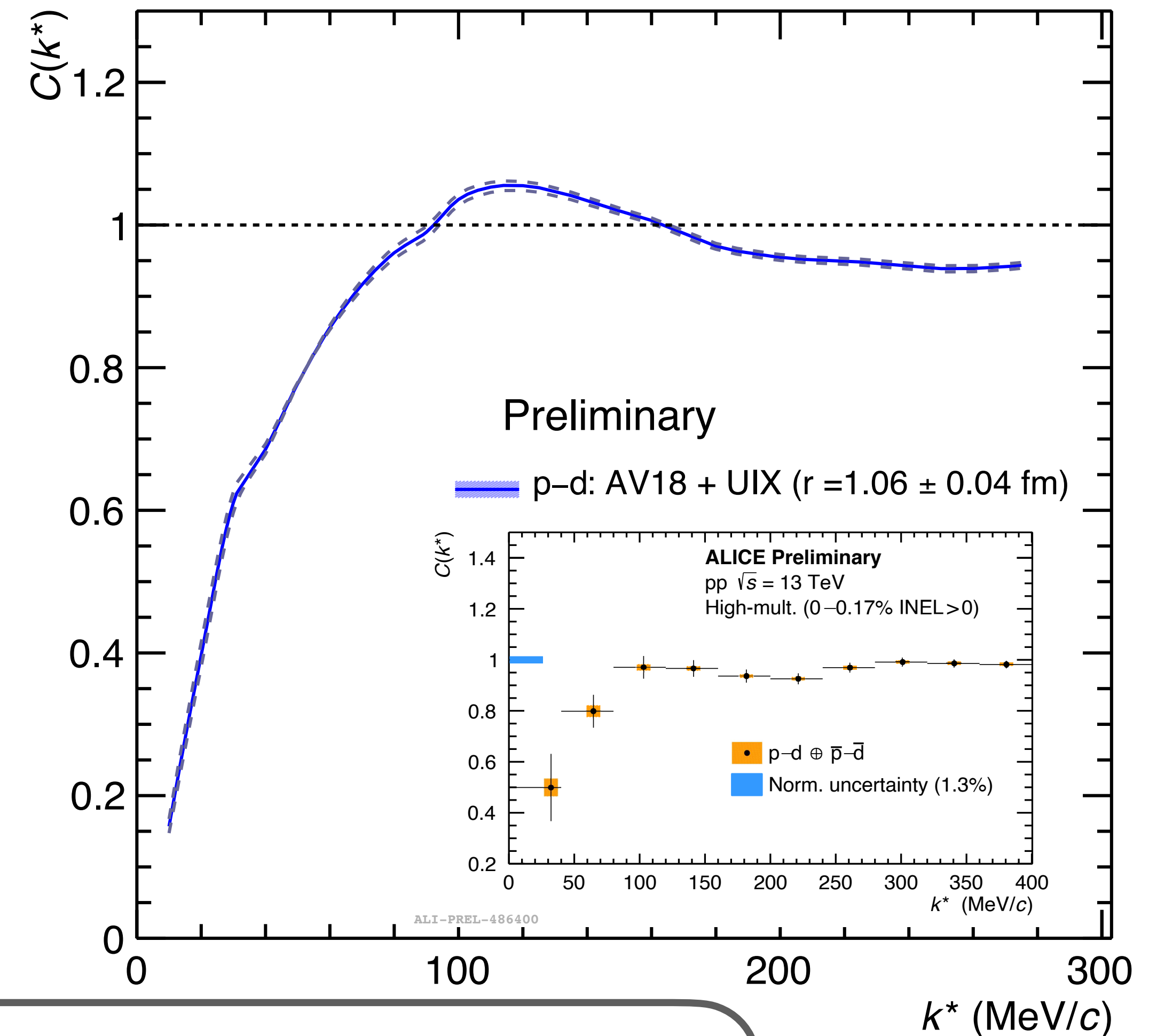
- **Model:** based on three-body dynamics calculation done by PISA theory group: **Michele Viviani**, **Alejandro Kievesky** and **Laura Marcucci**
- Relevant potentials:
  - Two-body interaction with Argonne V18 (AV18) and three-body interaction using Urbana XI (UIX) potential
  - Used a deuteron wavefunction from AV18 NN interaction
  - Demanding that deuteron is formed at the same time as the proton



Calculation: provided in a private communication



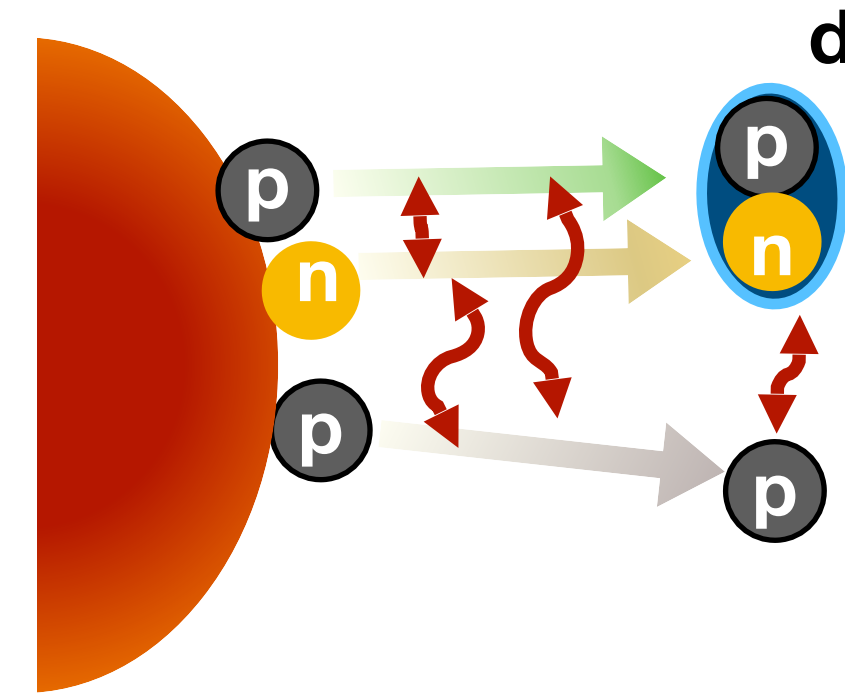
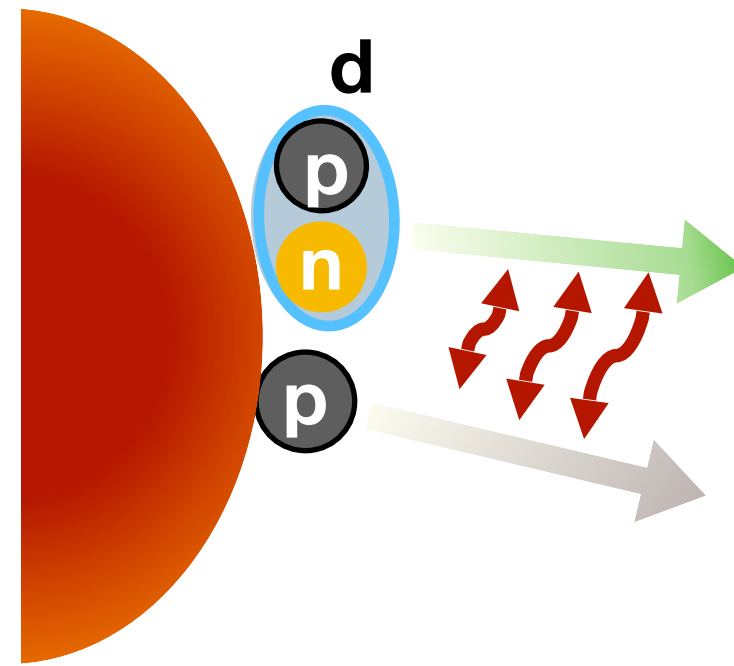
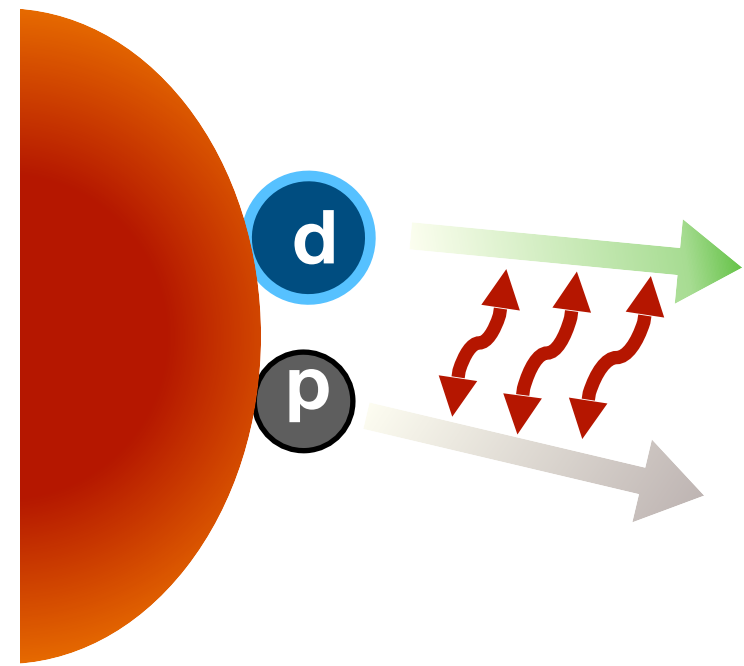
- **Model:** based on three-body dynamics calculation done by PISA theory group: **Michele Viviani**, **Alejandro Kievesky** and **Laura Marcucci**
- Relevant potentials:
  - Two-body interaction with Argonne V18 (AV18) and three-body interaction using Urbana XI (UIX) potential
  - Used a deuteron wavefunction from AV18 NN interaction
  - Demanding that deuteron is formed at the same time as the proton



➔ **Model calculation qualitatively reproduces the data**

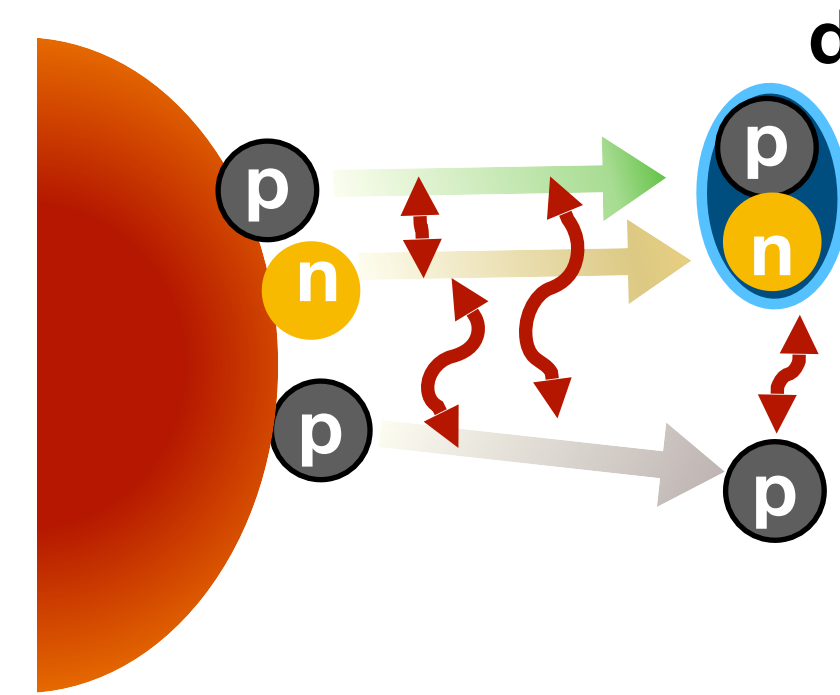
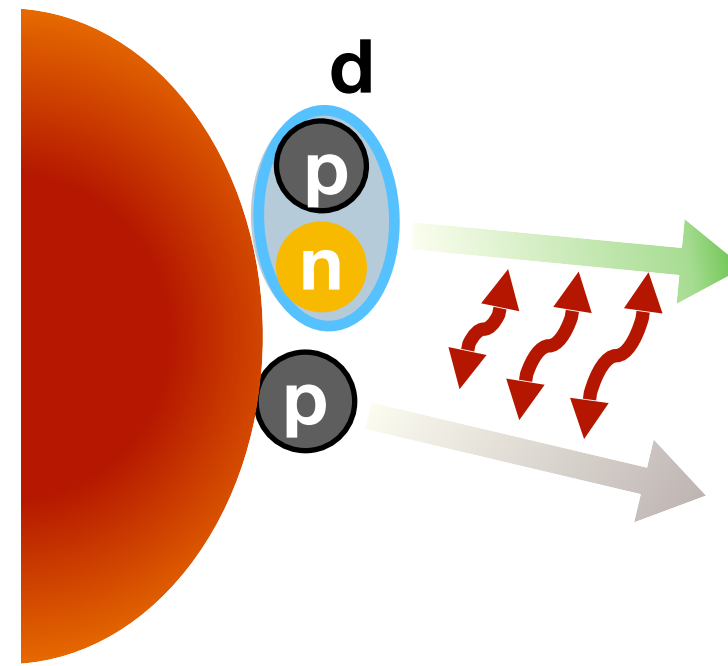
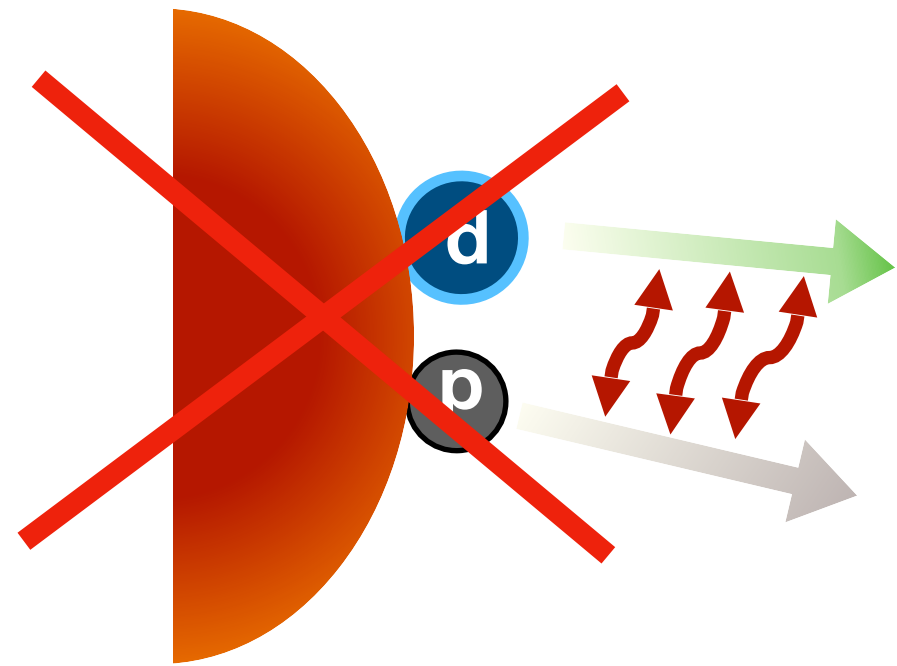
➔ **The p-d correlation should be affected by two + three-body p-p-n interactions!**

# Summary & Outlook

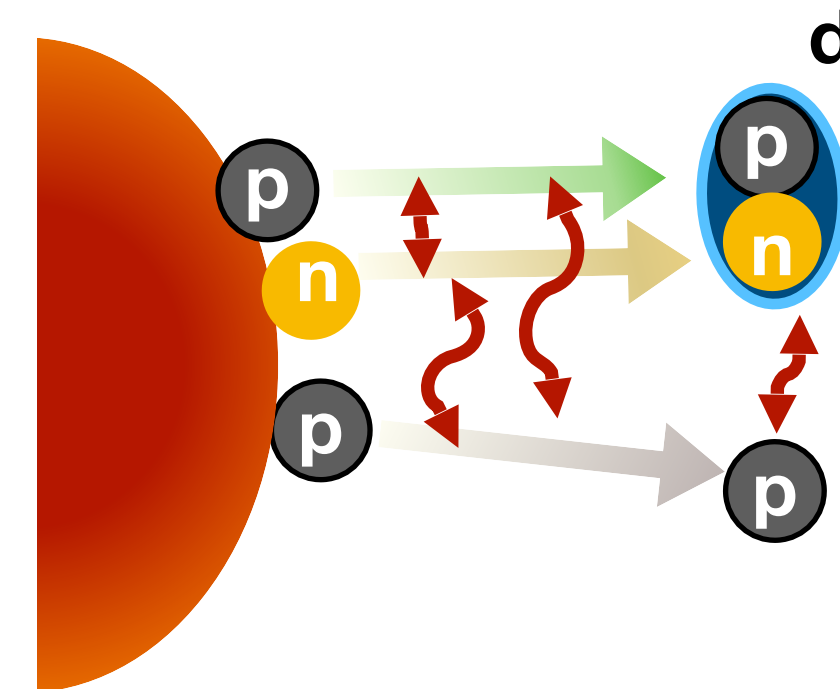
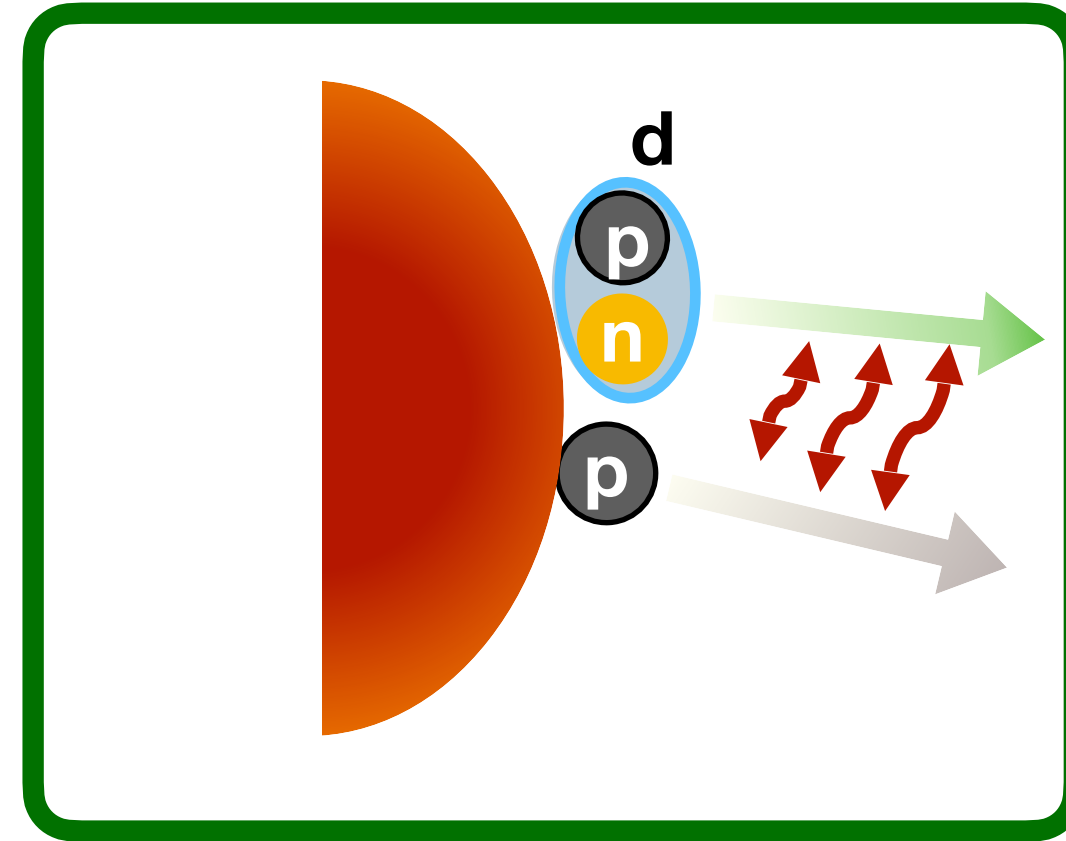
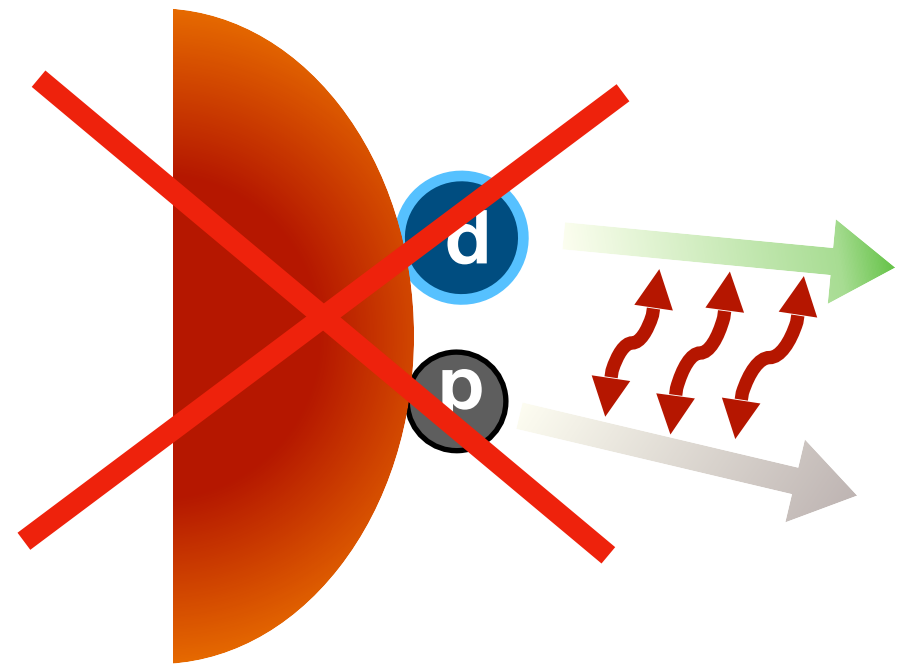




# Summary & Outlook



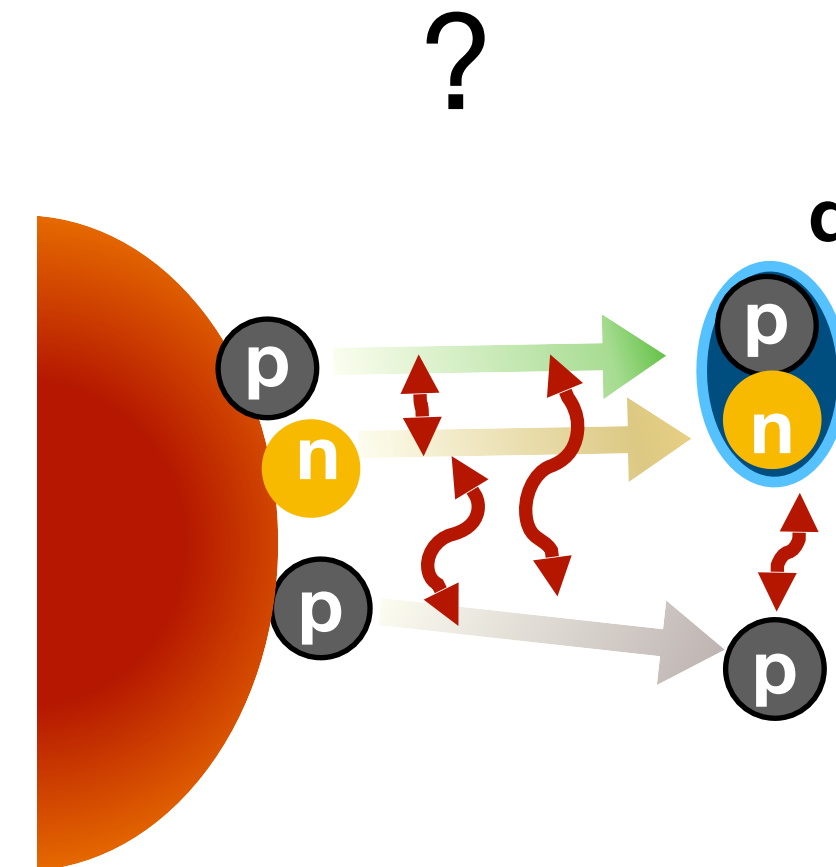
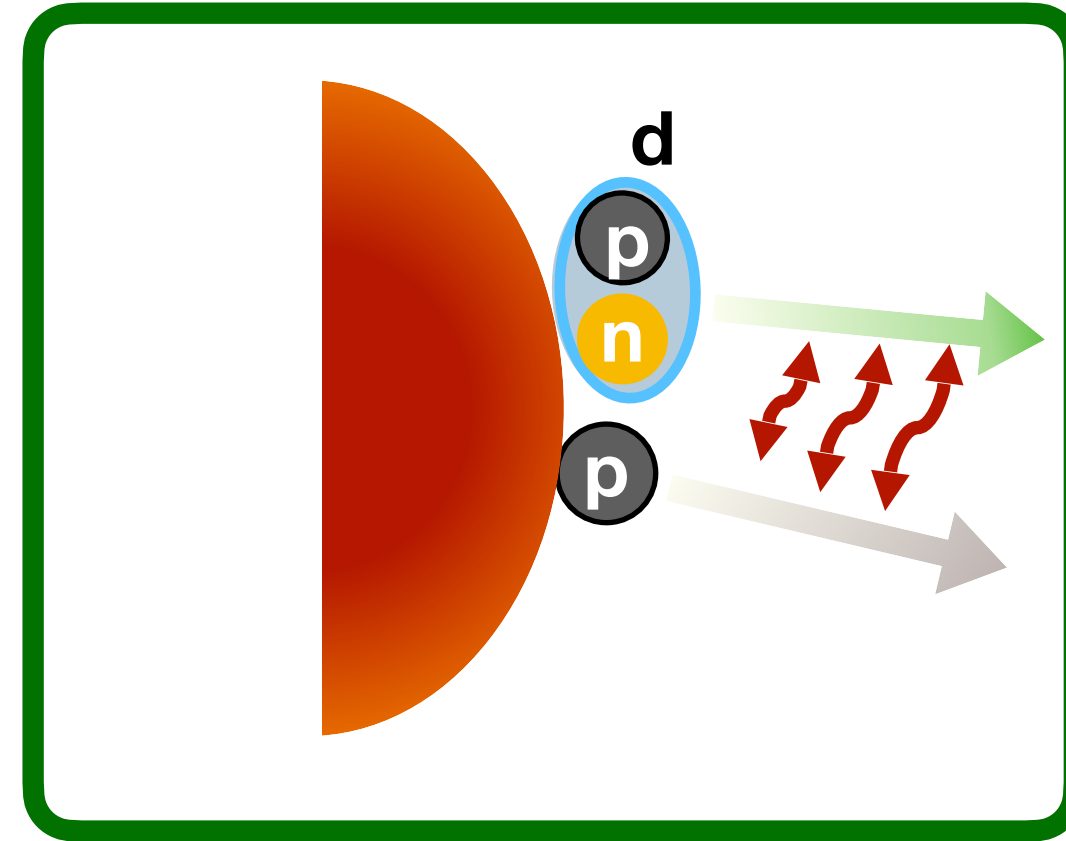
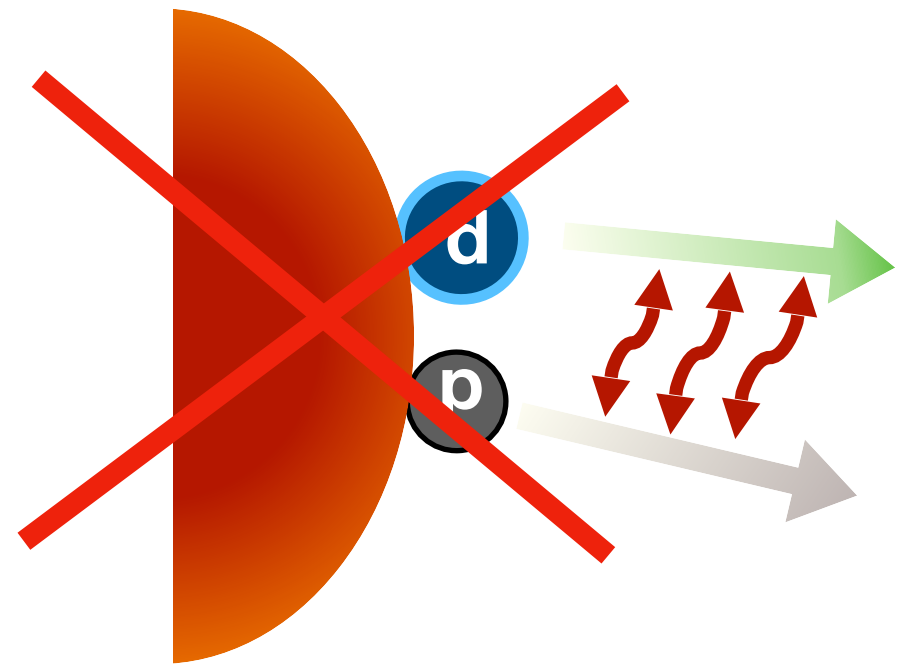
Looks promising!



- Work in progress:
  - Include the projections of the contributions of pair-wise and genuine three-body p-p-n interactions to the p-d correlation
  - p-d potential models based on three-body dynamics

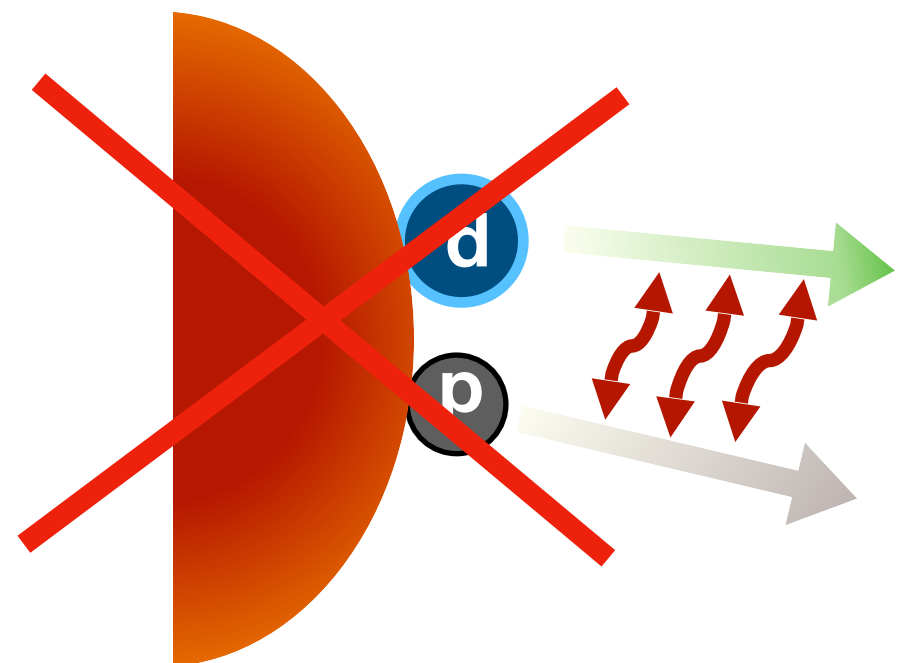


Looks promising!

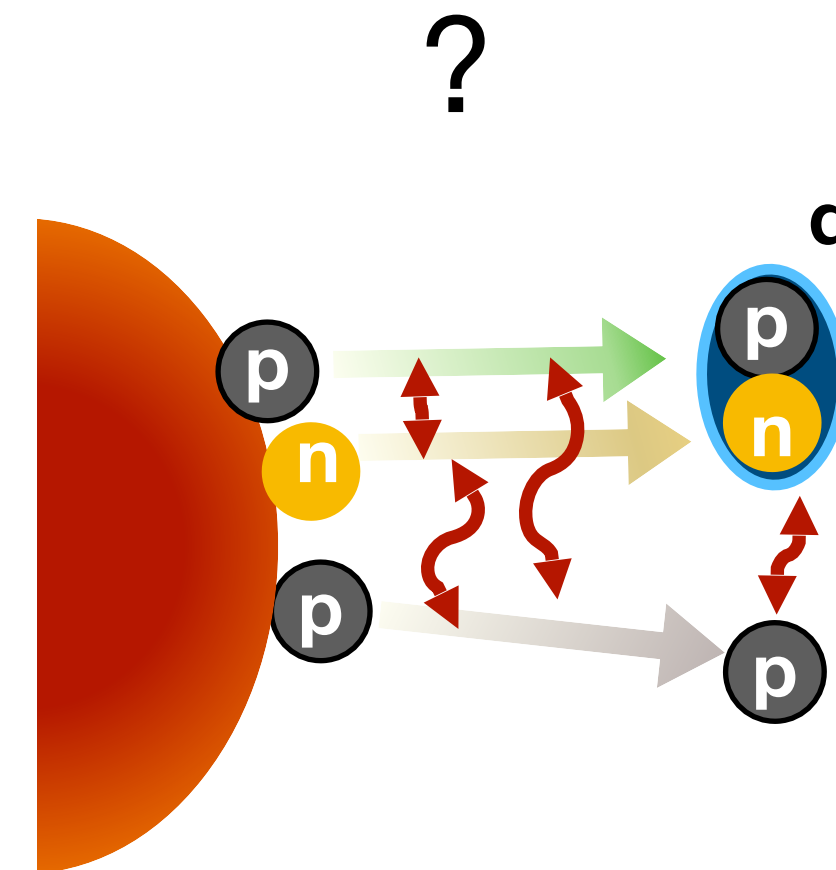
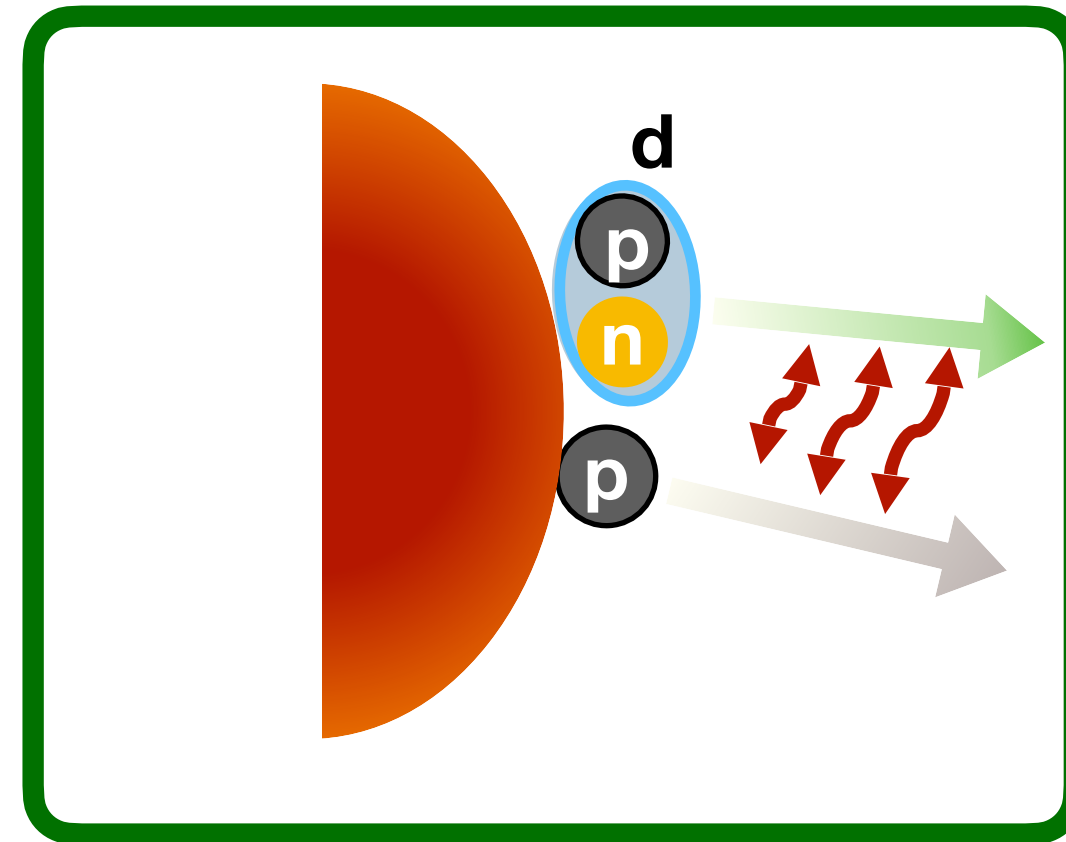


- Work in progress:

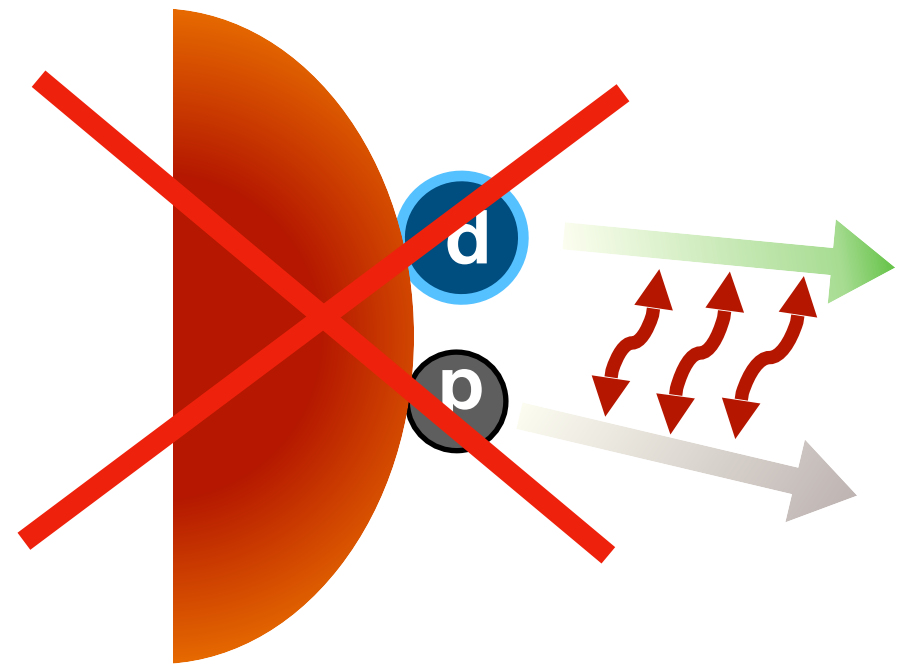
- Include the projections of the contributions of pair-wise and genuine three-body p-p-n interactions to the p-d correlation
- p-d potential models based on three-body dynamics



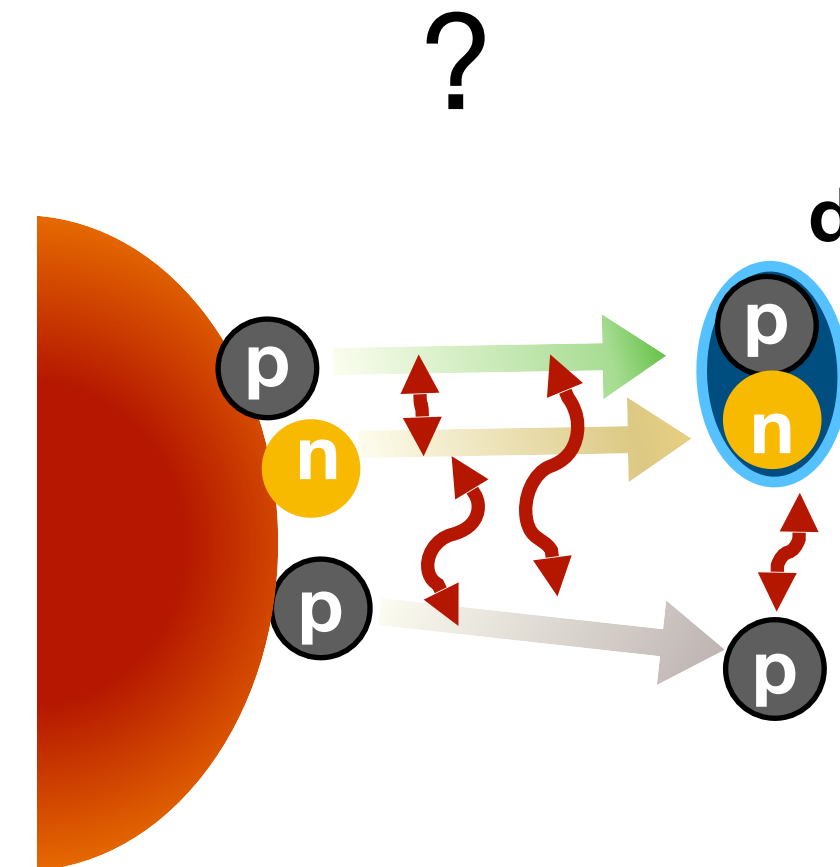
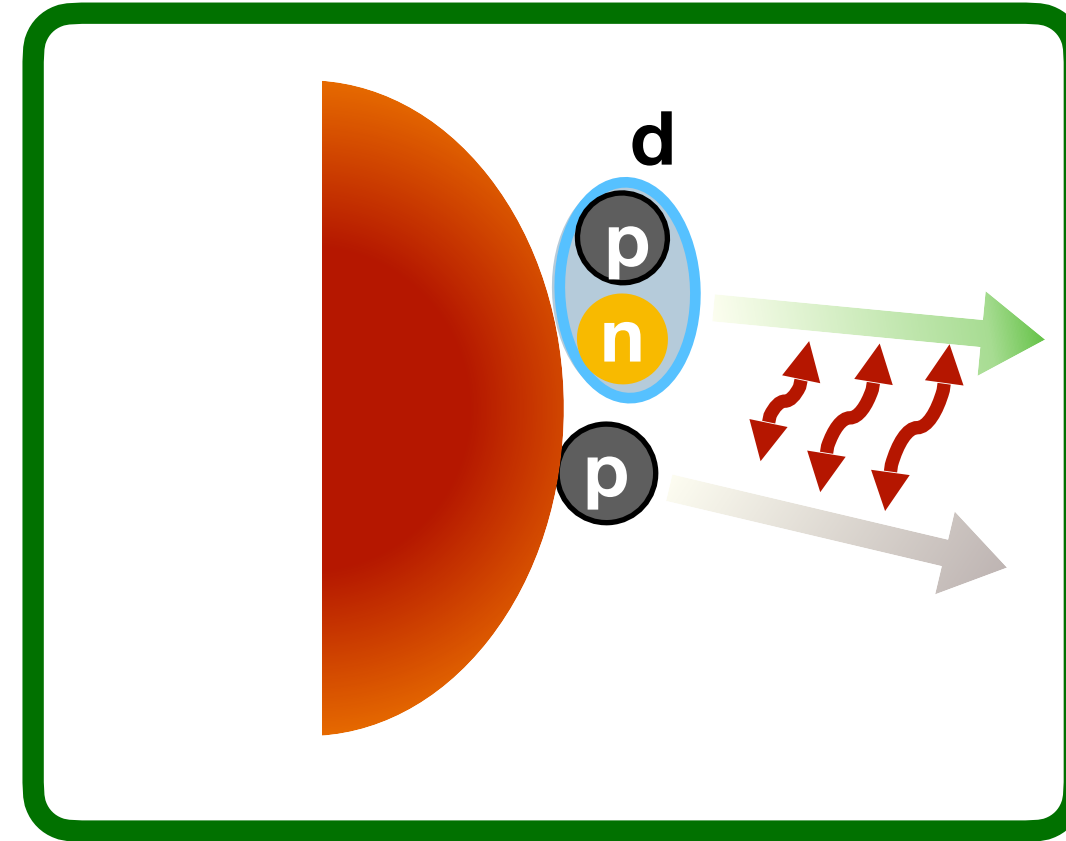
Looks promising!



- Work in progress:
  - Include the projections of the contributions of pair-wise and genuine three-body p-p-n interactions to the p-d correlation
  - p-d potential models based on three-body dynamics
- Outlook:
  - More precision studies within reach with the large data samples in Run 3



Looks promising!



- Work in progress:

- Include the projections of the contributions of pair-wise and genuine three-body p-p-n interactions to the p-d correlation
- p-d potential models based on three-body dynamics

- Outlook:

- More precision studies within reach with the large data samples in Run 3

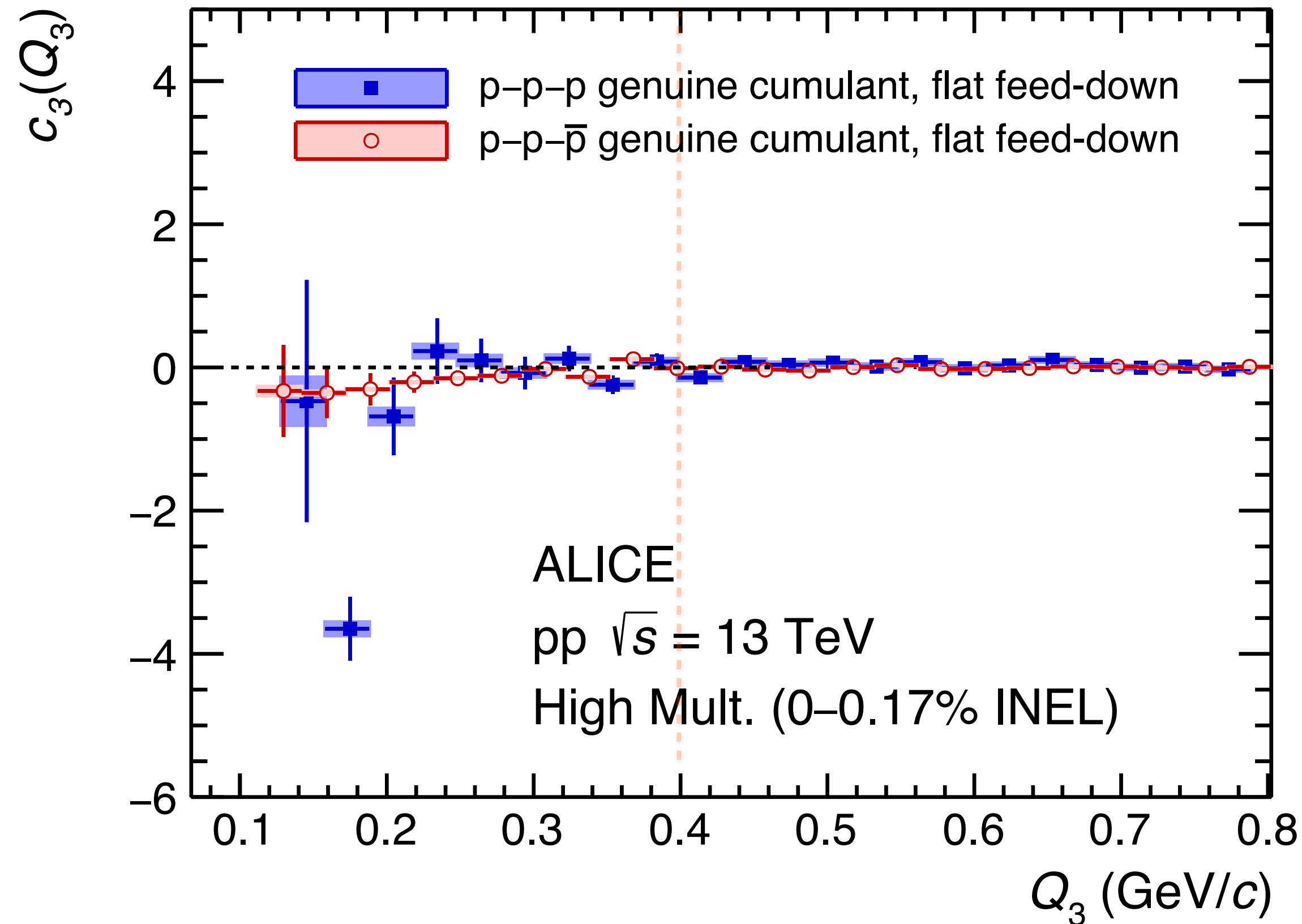
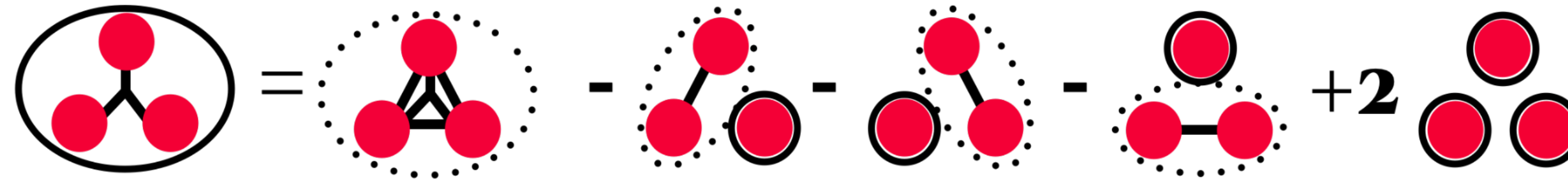
Thank you for your attention!



# Additional slides

# The p-p-p cumulant

Talk: Laura Šerkšnytė  
29/06/2022, 11:15



**Statistical significance:**

**p-p-p:  $n_\sigma = 6.7$  for  $Q_3 < 0.4$  GeV/c**

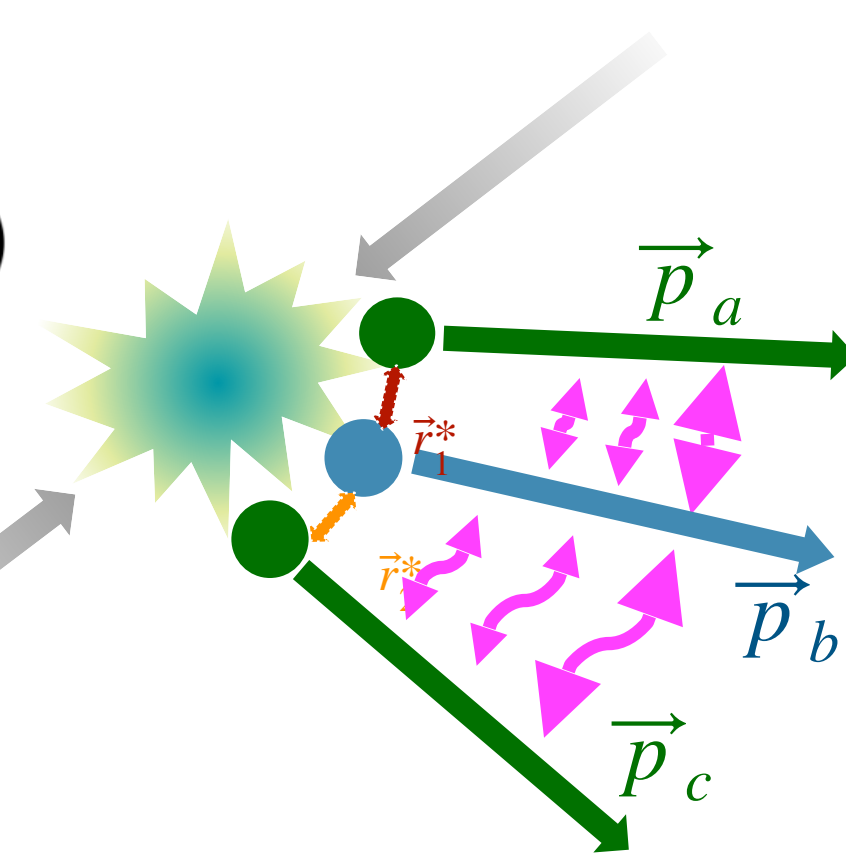
**Conclusion:**

**Presence of a genuine three-body effect in p-p-p!**

**Possible interpretations:**

- Pauli blocking at the three-particle level
- long-range Coulomb interaction effects
- three-body strong interaction

**New**  
**[arXiv:2206.03344](https://arxiv.org/abs/2206.03344)**



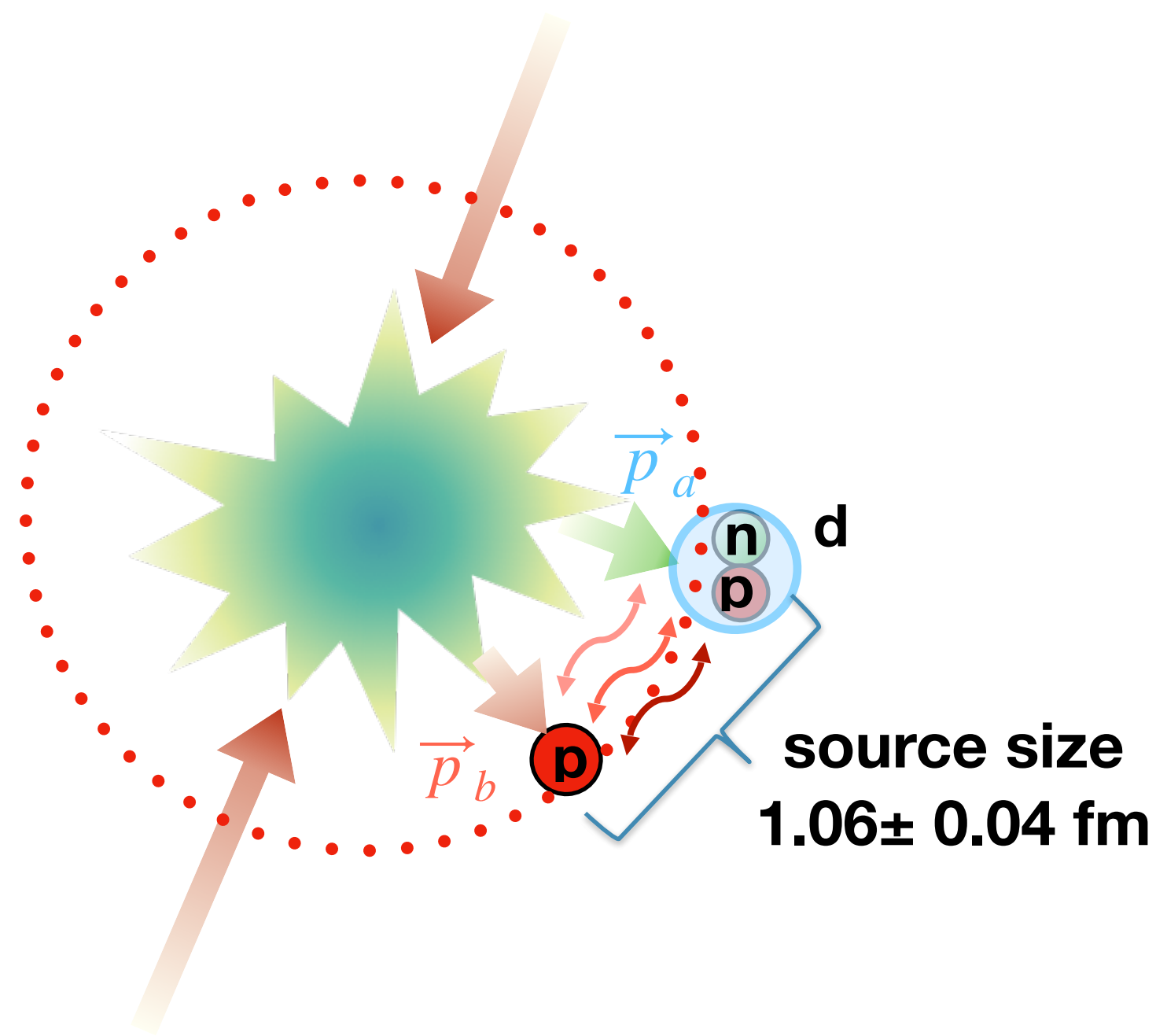
**The p-d correlation should be affected by two + three-body p-p-n interactions!**



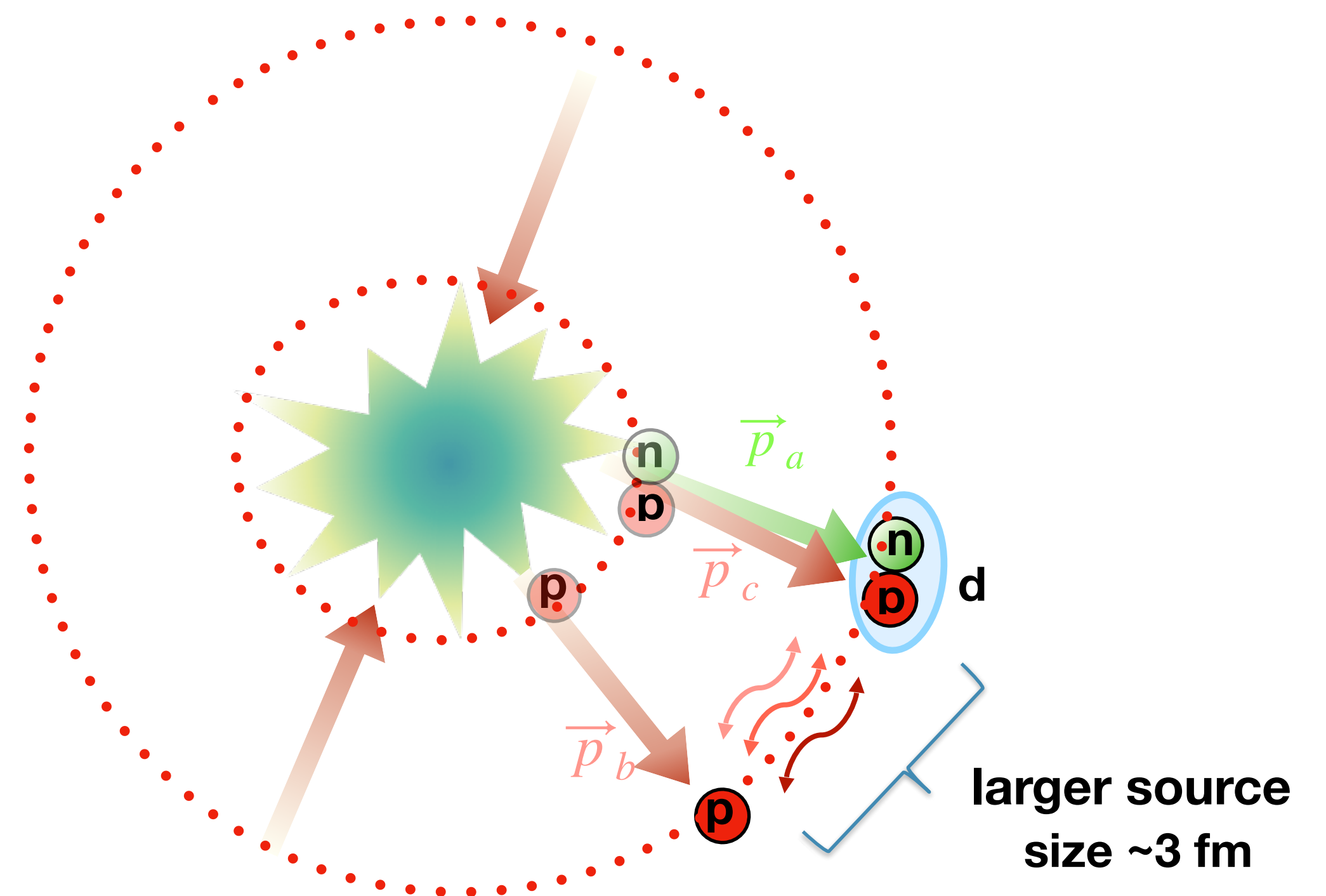
# What if the deuteron is formed later?

- Source size increases due to **late formation** of deuteron
  - As a result the measured interaction between proton and deuteron weakens

Case I : p and d are formed at the same time

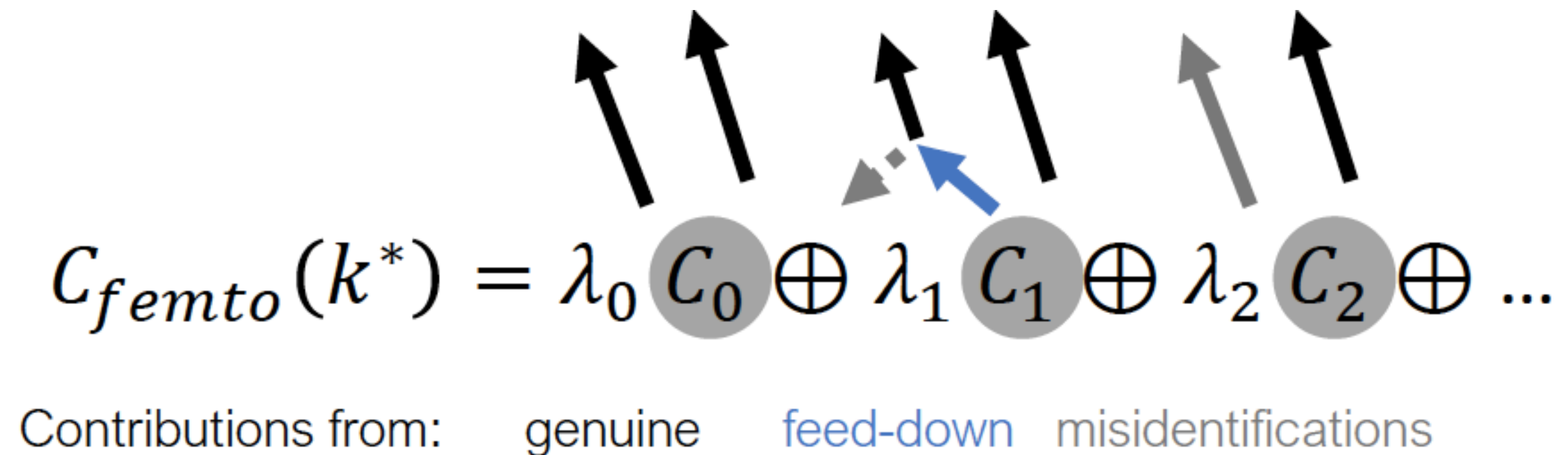


Case II : delayed formation of d



- The femtoscopic correlation may have background/contributions from

- Particles from weak decays
- Particles from material knock-outs
- Misidentifications


$$C_{femto}(k^*) = \lambda_0 C_0 \oplus \lambda_1 C_1 \oplus \lambda_2 C_2 \oplus \dots$$

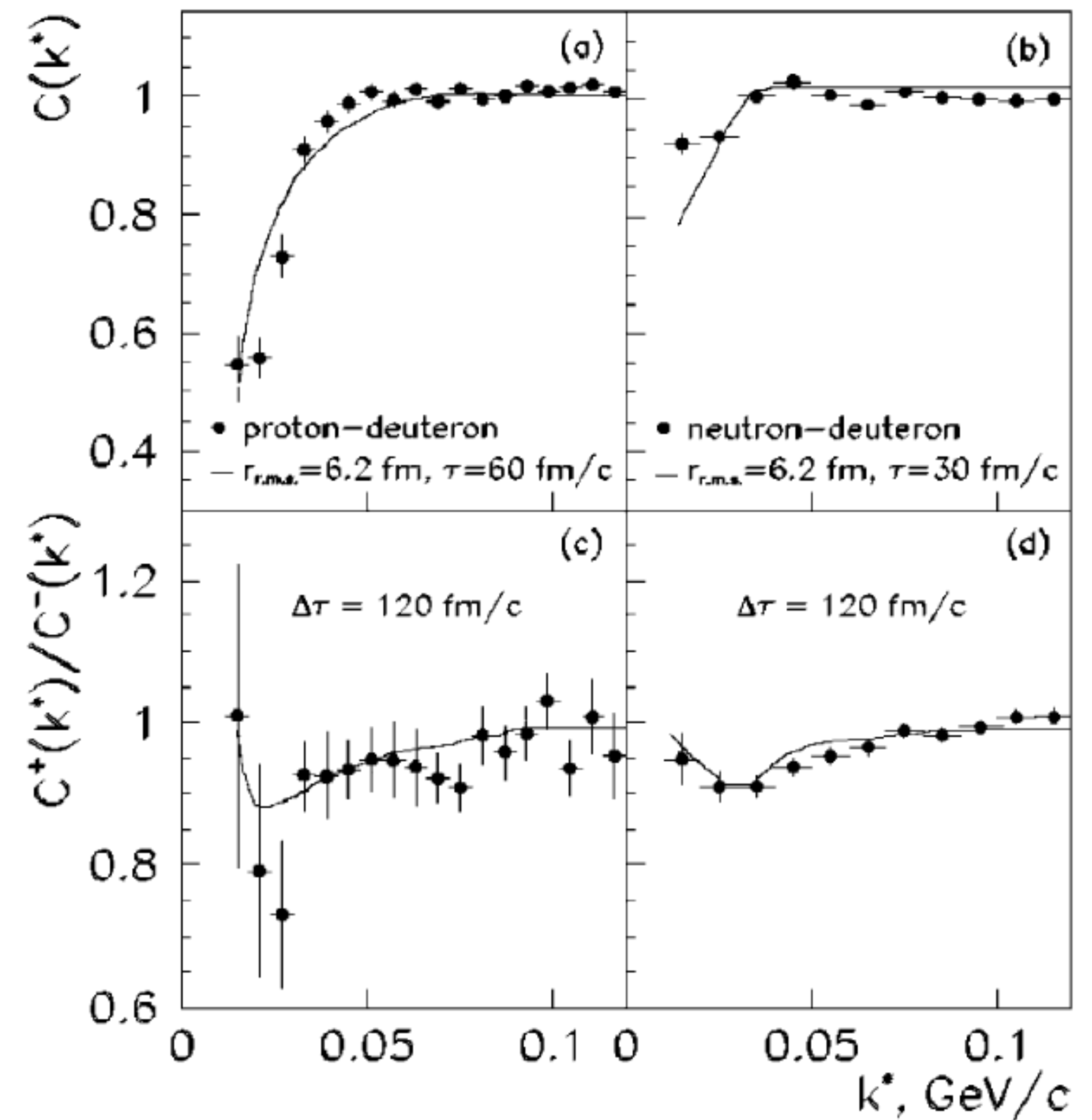
Contributions from:    genuine    feed-down    misidentifications

- Quantification of the contributions to the pairs done by the lambda parameters  $\lambda_{ij} = \mathcal{P}_i \cdot f_i \times \mathcal{P}_j \cdot f_j$ 
  - Purity of the individual particles ( $\mathcal{P}_i$ )
  - Feed-down fractions ( $f_i$ )



- **Status:**

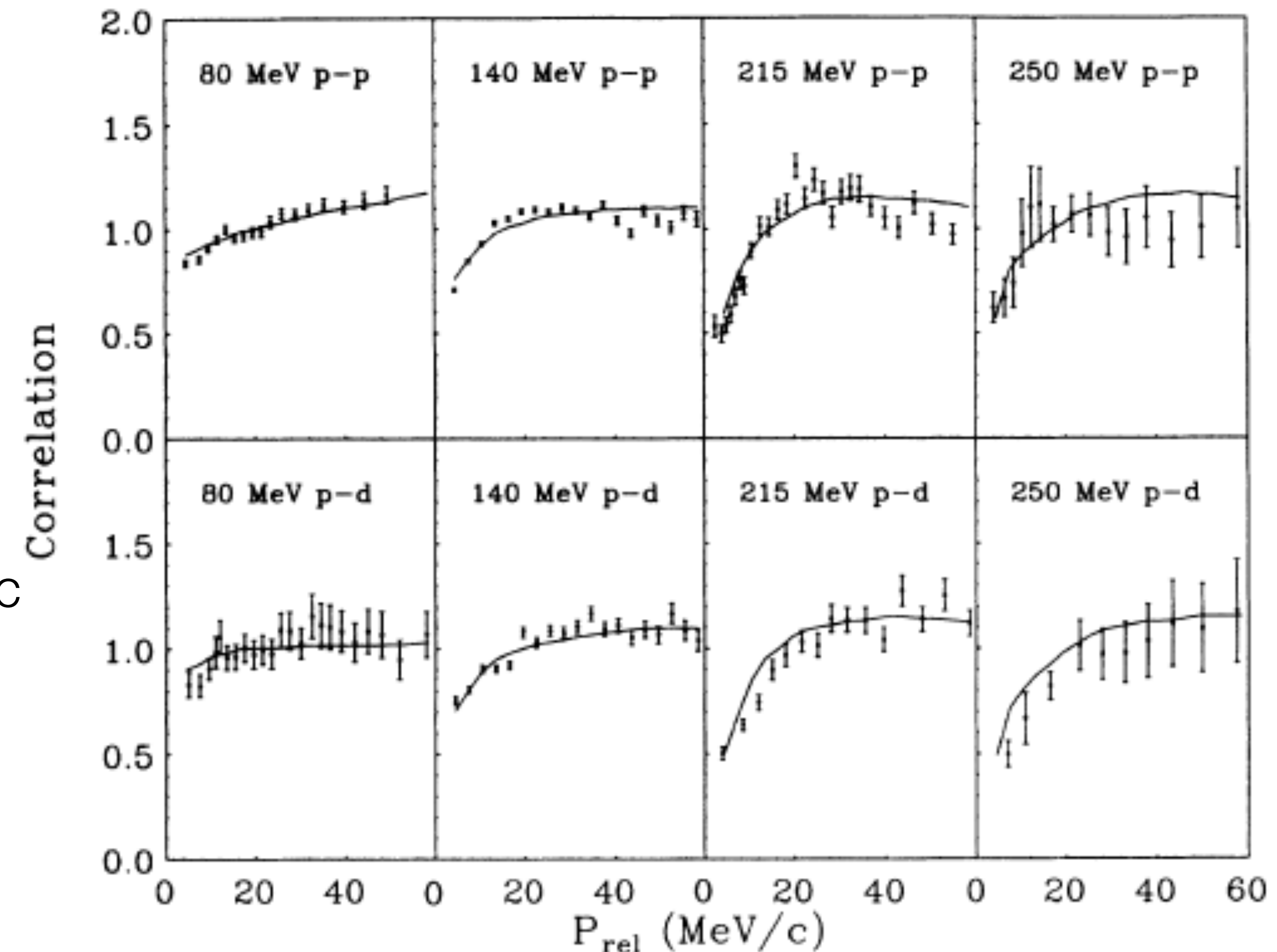
- p-d correlation function from 2006
- GANIL(Grand Accélérateur National d'Ions Lourds):
  - $^{40}\text{Ar}-^{58}\text{Ni}$  reaction at 77 MeV/u
  - Show a clear depletion
  - Only unto 100 MeV/c in relative momentum



[1] Wosińska, K., Pluta, J., Hanappe, F. *et al. Eur. Phys. J. A* 32, 55–59 (2007)

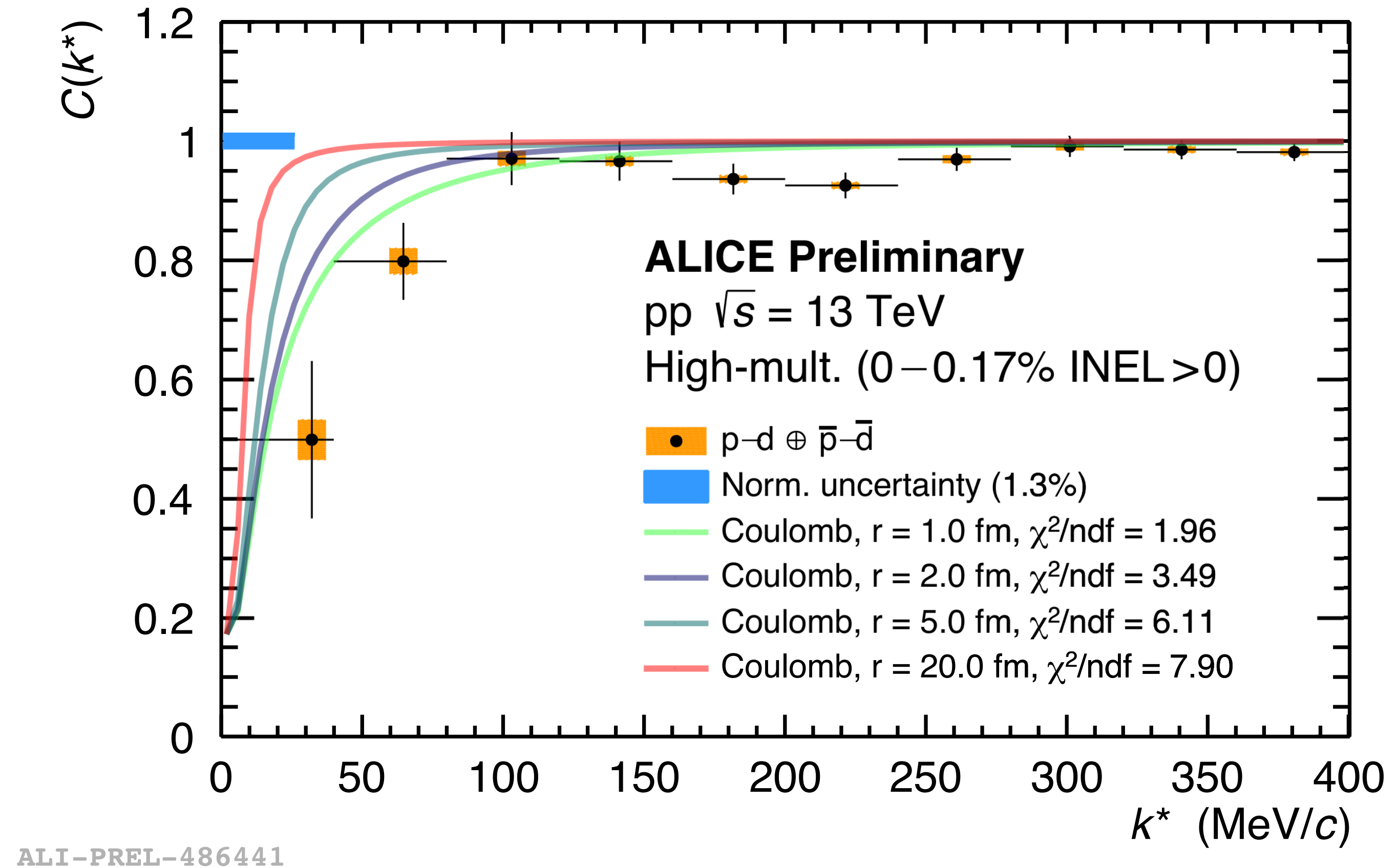
# proton-deuteron correlation measurement so far

- **Status:** Measurement by *P. A. DeYoung et al* in 1990
  - Measurements for 80 and 140 MeV/c  $^{16}\text{O}$  -  $^{27}\text{Al}$  reaction were performed at the Stony Brook Linac
  - Measurements for 215 and 250 MeV/c  $^{16}\text{O}$  -  $^{27}\text{Al}$  reaction were performed at the ATLAS facility of the Argonne National Laboratory.
  - In the relative momentum range [0-60] MeV/c
  - Show a clear depletion
  - Solid line coulomb prediction from Koonin model



*P. A. DeYoung et al. PRC 41, R1885 (1990)*

- Coulomb-corrected wave function for charged particles Lednický, R. *Phys. Part. Nuclei* 40, 307–352 (2009)
  - Coulomb + strong interaction ( $S = 1/2$  and  $S = 3/2$ )
  - Only for s wave interaction
  - Theoretical models constrained to scattering p—d experiments
  - Coulomb-interaction only does not describe the data





- Coulomb-corrected wave function for final-state interactions (Lednický): [arxiv.org/abs/nucl-th/0501065](https://arxiv.org/abs/nucl-th/0501065)

$$\psi_{-k^*}(r^*) = e^{i\delta_c} \sqrt{A_c(\eta)} \left[ e^{-ik^*r^*} F(-i\eta, 1, i\zeta) + f_c(k^*) \frac{\tilde{G}(\rho, \eta)}{r^*} \right]$$

- $f_c$  is the Coulomb-corrected strong scattering amplitude
- $F(-i\eta, 1, i\zeta)$  is the confluent hypergeometric function and  $\tilde{G}(\rho, \eta)$  is the regular Coulomb function
- It is an approximated wave function for two near-threshold charged particles:
- The two-particle correlation: we can use Koonian-Pratt formula

$$C(k) = \int S(\mathbf{r}) |\psi_k(\mathbf{r})|^2 d^3r, \quad \text{with source function} \quad S(r) = \frac{1}{(4\pi r_0^2)^{3/2}} \exp\left(-\frac{r^2}{4r_0^2}\right)$$

- Hadron-Deuteron Correlations and Production of Light Nuclei in Relativistic Heavy-Ion Collisions:  
[arxiv.org/abs/1904.08320](https://arxiv.org/abs/1904.08320)
  - hadron-deuteron correlation function which carries information about the source of the deuterons
  - Allows one to determine whether a deuteron is directly emitted from the fireball or if it is formed afterwards
  - Conclusion:
    - The theoretical p-d correlation function is strongly dependent on the source size

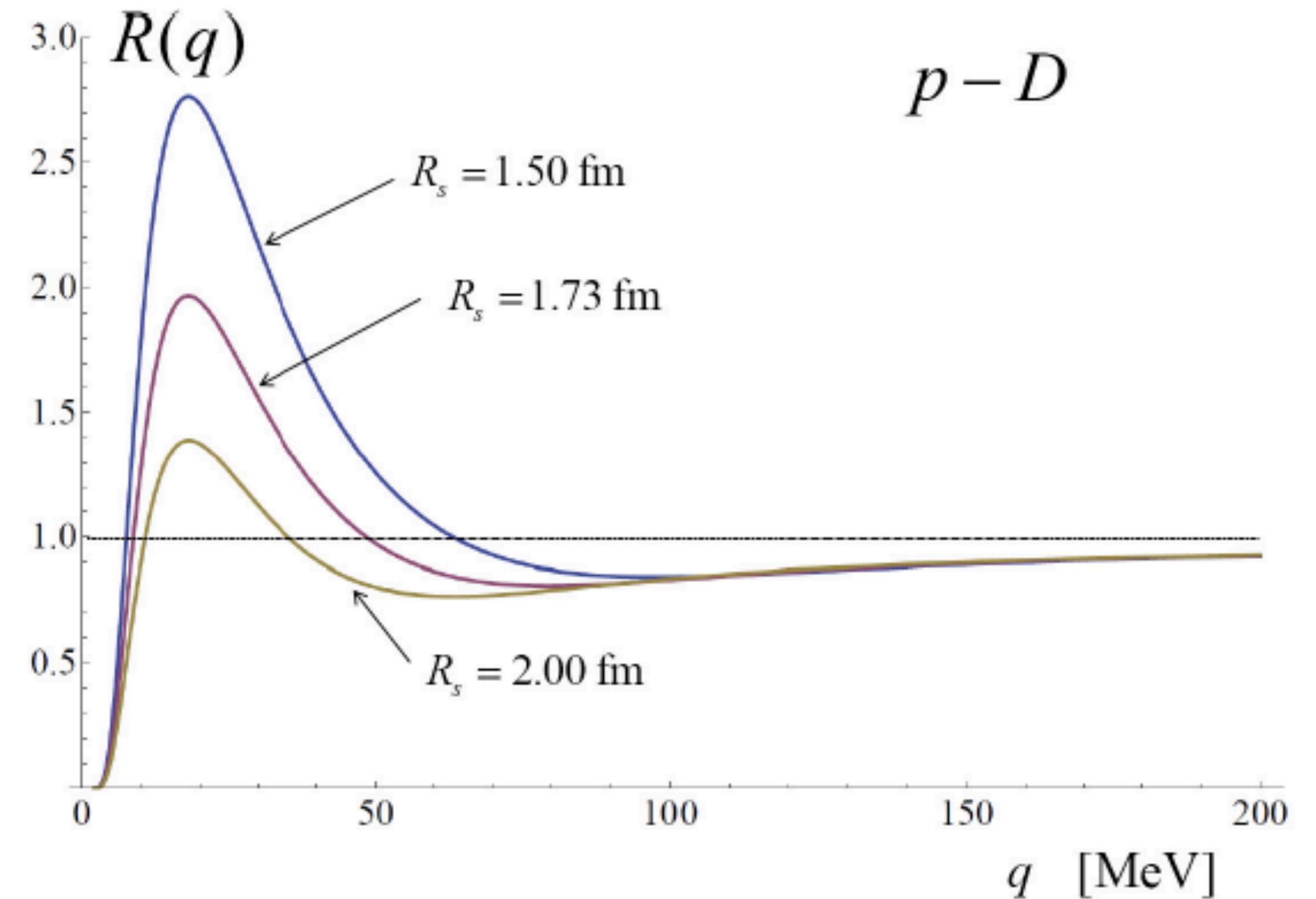


Fig. 2.  $p-D$  correlation function