



Two-Particle Correlations of Hadrons in e^+e^- Collisions at Belle

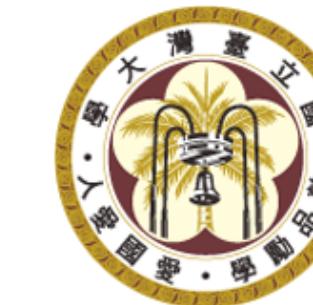
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^b Massachusetts Institute of Technology

on behalf of the Belle Collaboration

ICHEP 2022, Jul. 9th, Bologna Italy



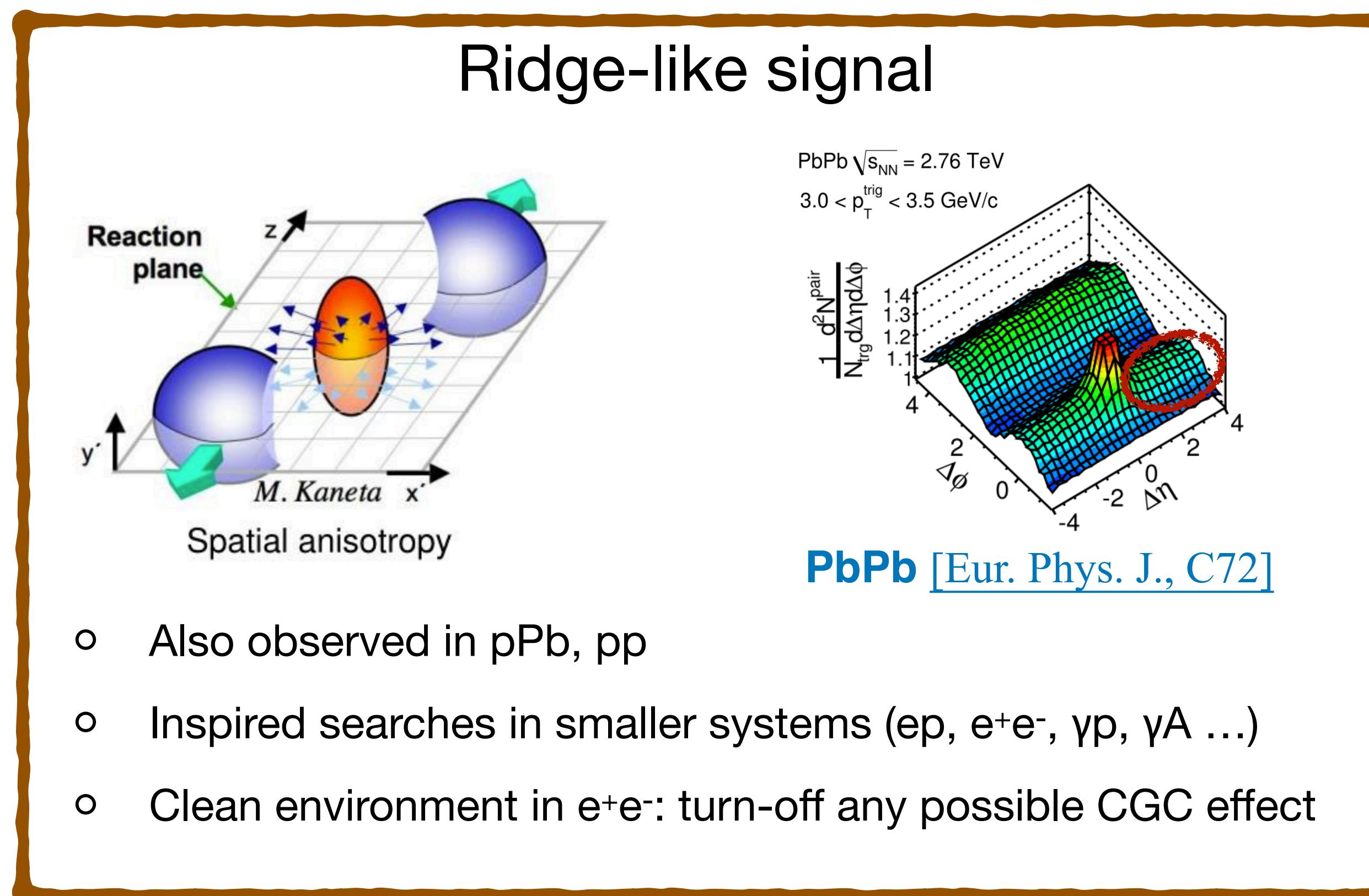
國立臺灣大學
National Taiwan University



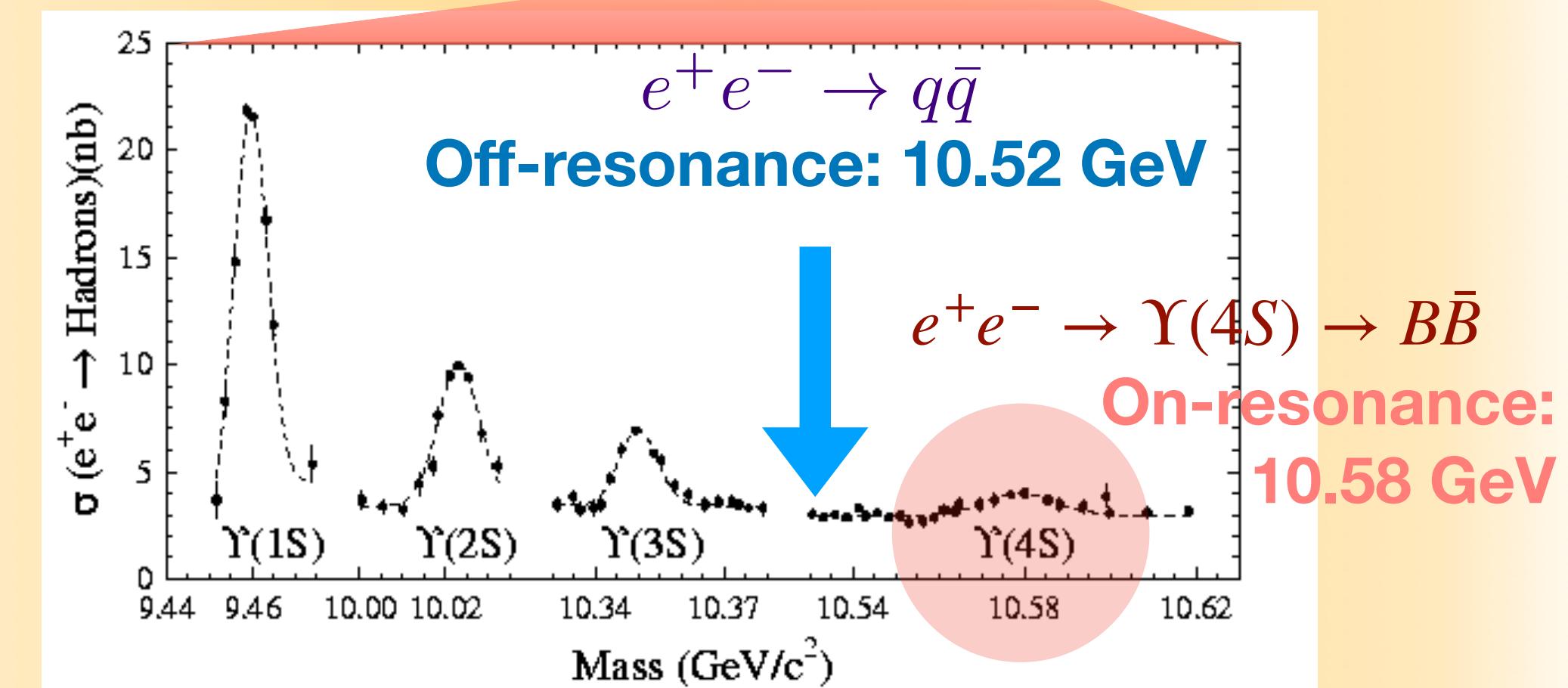
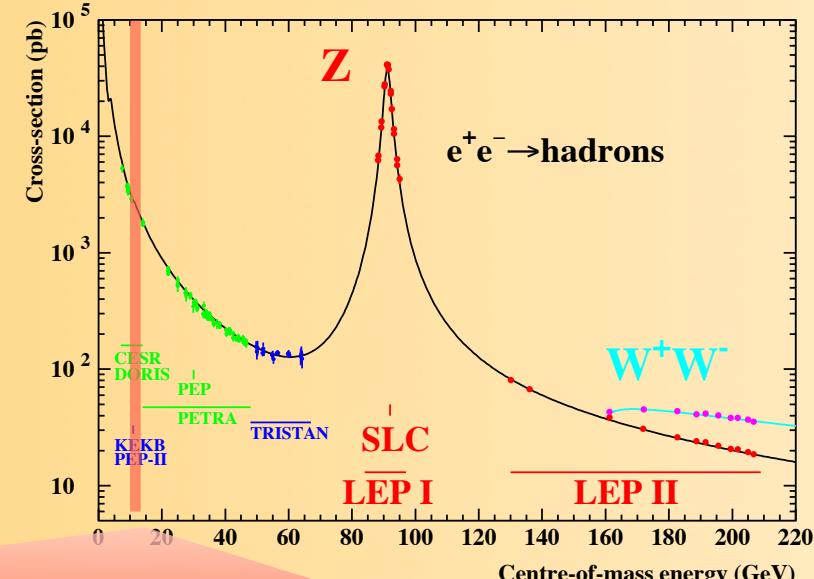
[\[Phys. Rev. Lett. 128 \(2022\) 142005\]](#)
[arXiv:2206.09440, submitted to JHEP](#)

Small system (e^+e^-): minimal condition for azimuthal anisotropy

Two-particle correlation: soft probe for Quark-Gluon Plasma (QGP) in heavy ion collisions

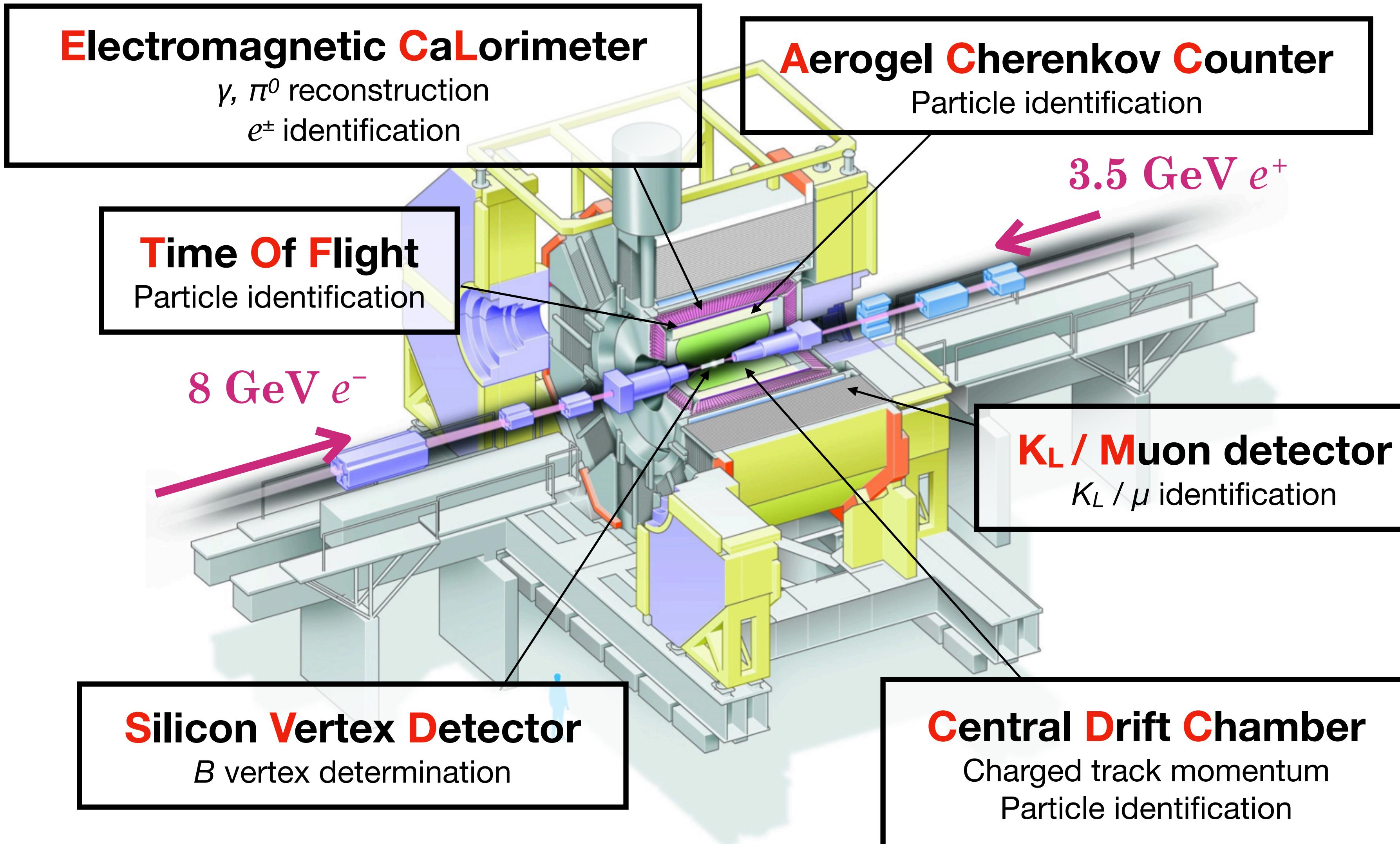


Exploring low-energy region



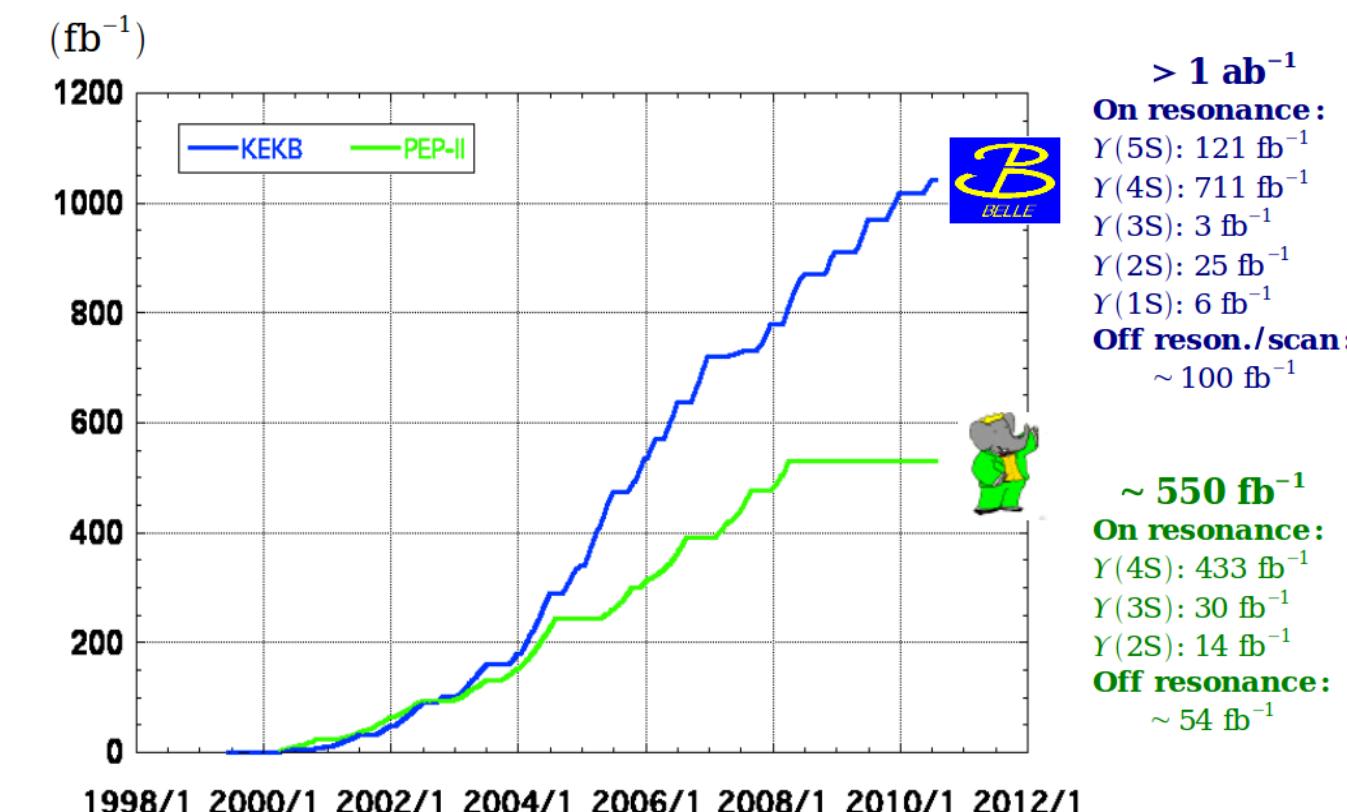
Compared w/ event generators

- Thrust-axis two-particle correlation:
Search for medium expanding transverse to the out-going quark directions
- New inputs to the phenomenological fragmentation models at low collision energy

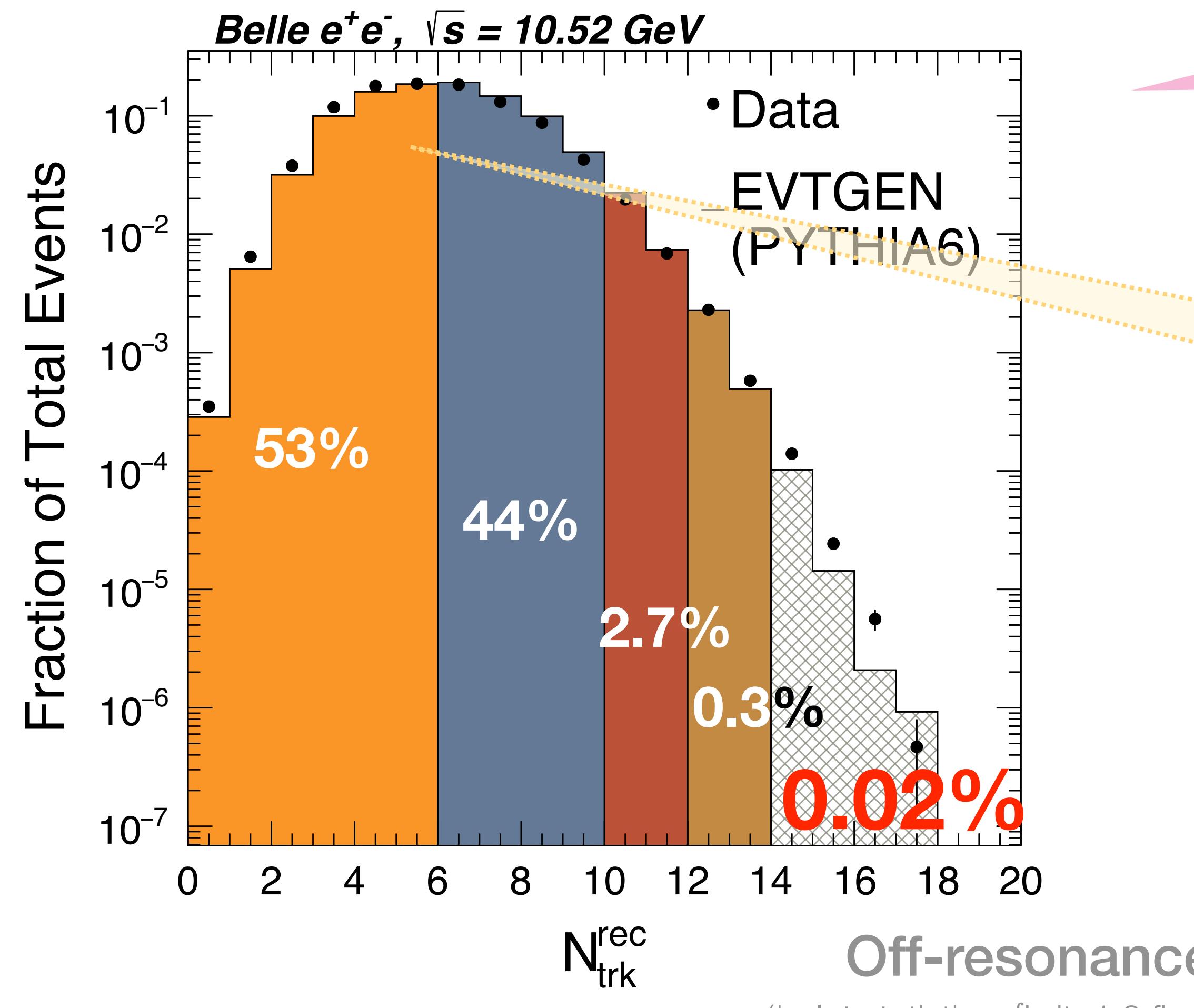


(KEK)

Boost to the C.M. frame
for the correlation study!



Studying two-particle correlations as a function of multiplicity



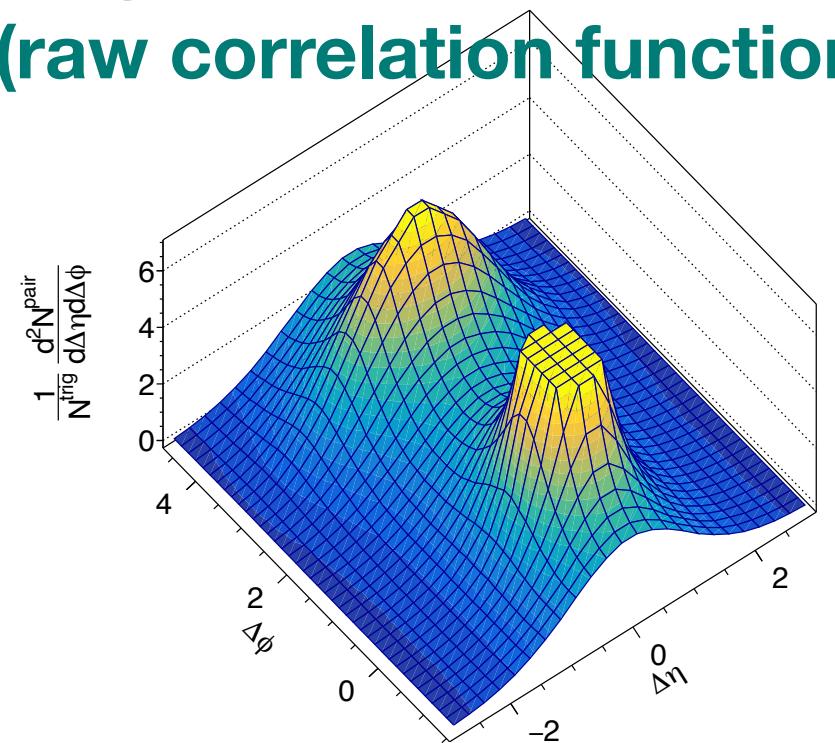
- $q\bar{q}$ ($q = u, d, c$ and s) fragmentation
- $\Upsilon(4S) \rightarrow B\bar{B}$ in on-resonance sample

Low-multiplicity background

- Radiative Bhabha events
- $e^+e^- \rightarrow l^+l^-$ ($l = e, \mu$)
- Two-photon processes

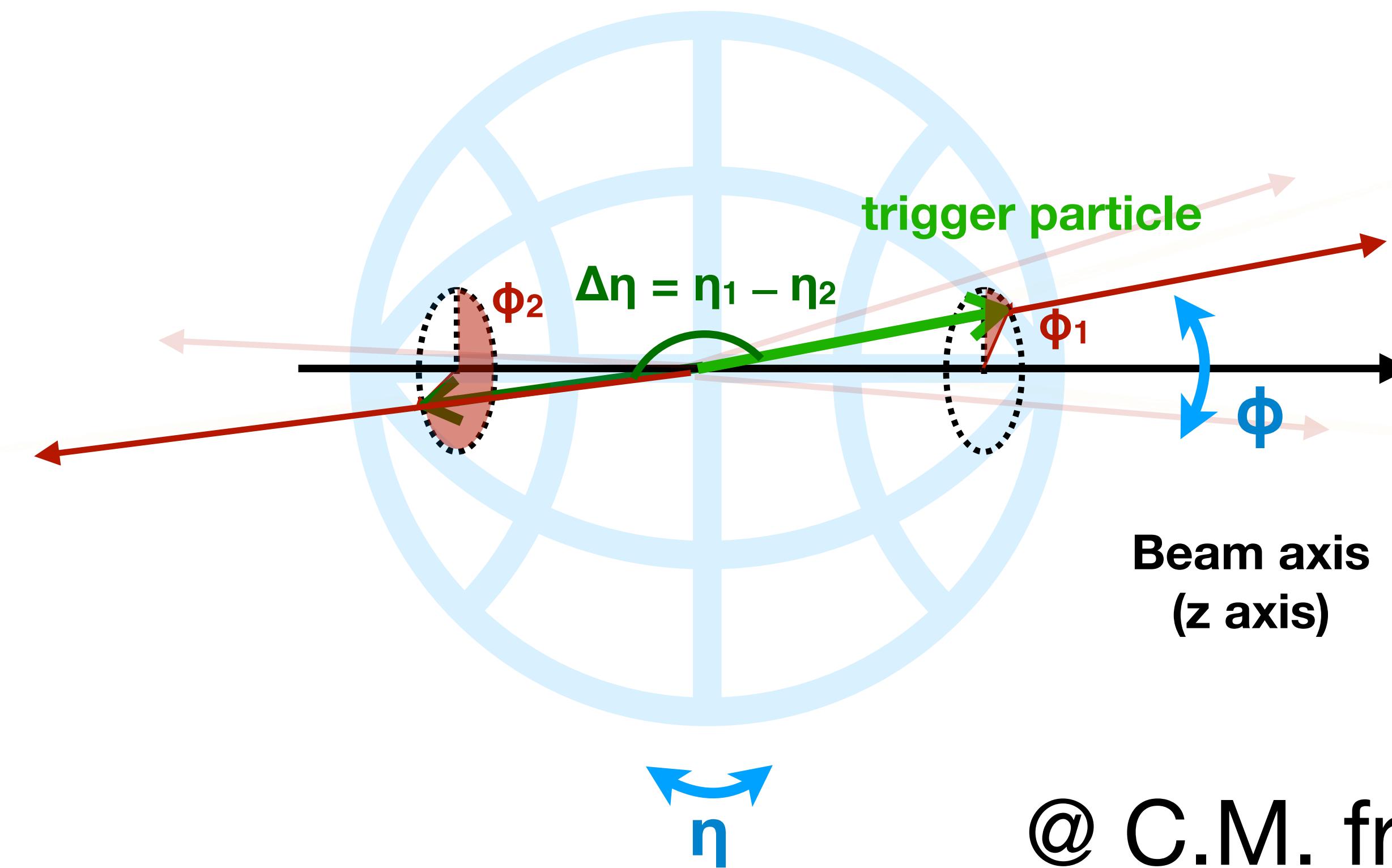
on-resonance see [backup](#)

Signal (raw correlation function)



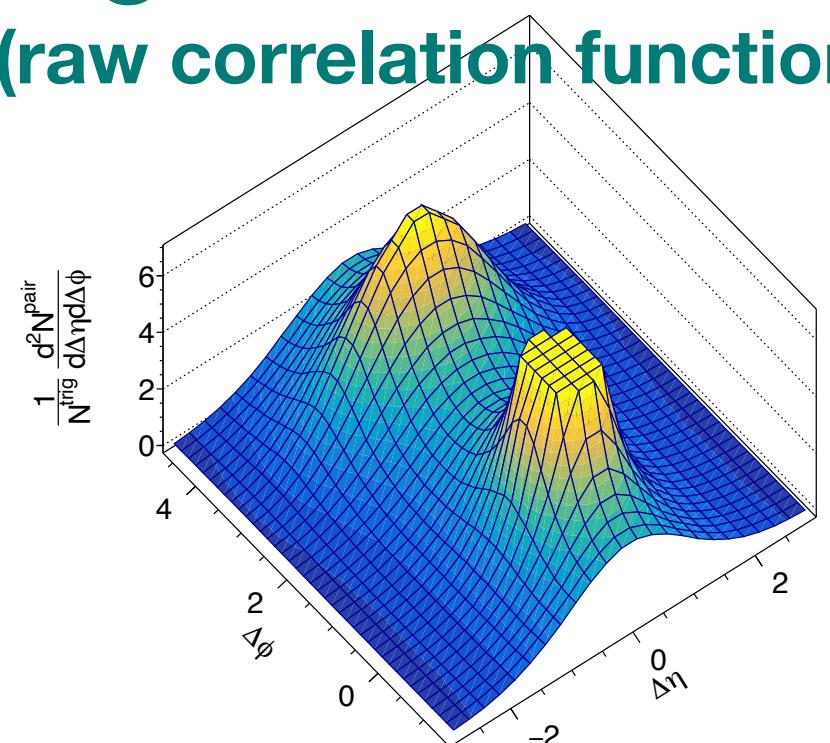
$$S(\Delta\eta, \Delta\phi) = \frac{1}{N_{\text{corr}}^{\text{trk}}} \frac{d^2 N^{\text{same}}}{d\Delta\eta d\Delta\phi}$$

Track pairs' angular difference in
 η (pseudorapidity), ϕ (azimuthal angle)

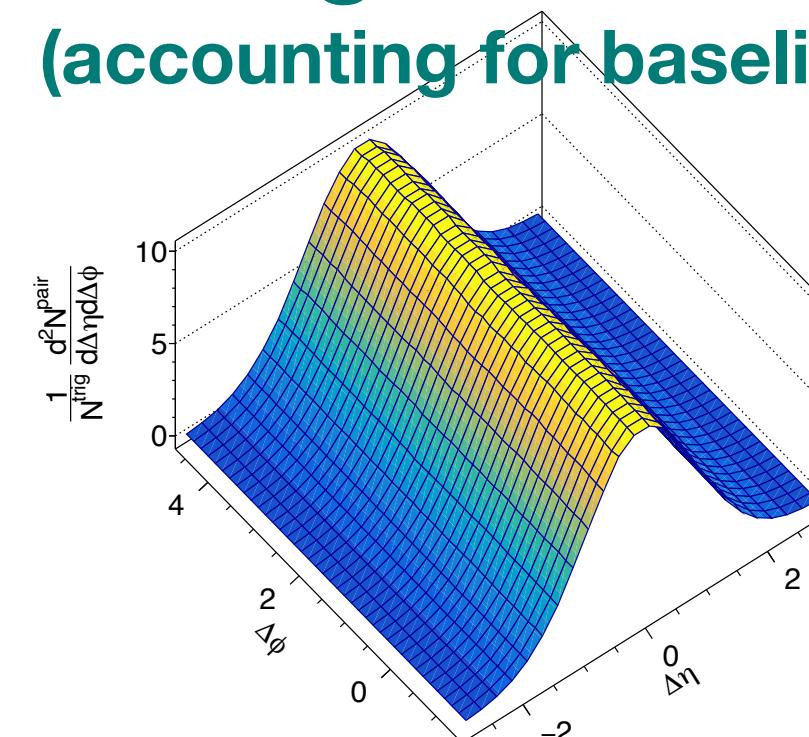


@ C.M. frame

Signal
(raw correlation function)

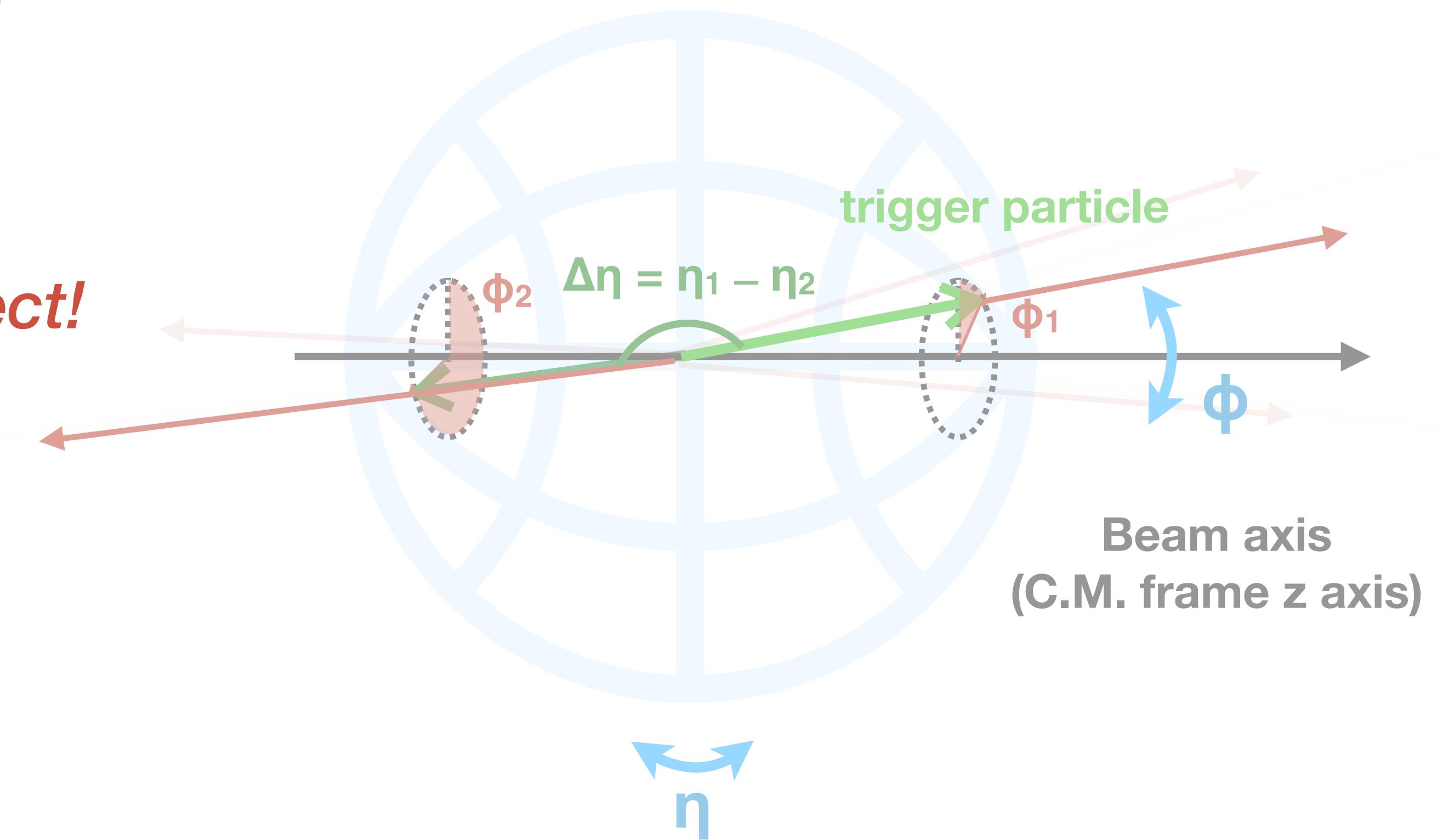


Background
(accounting for baseline of random pairing)



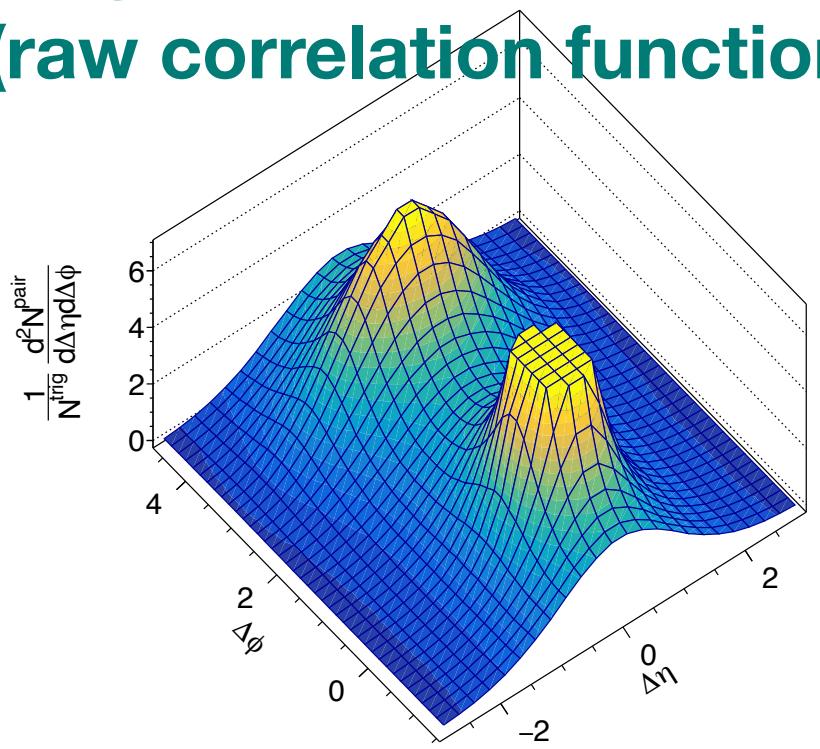
Track pairs' angular difference in
 η (pseudorapidity), ϕ (azimuthal angle)

Factoring out the random pairing effect!

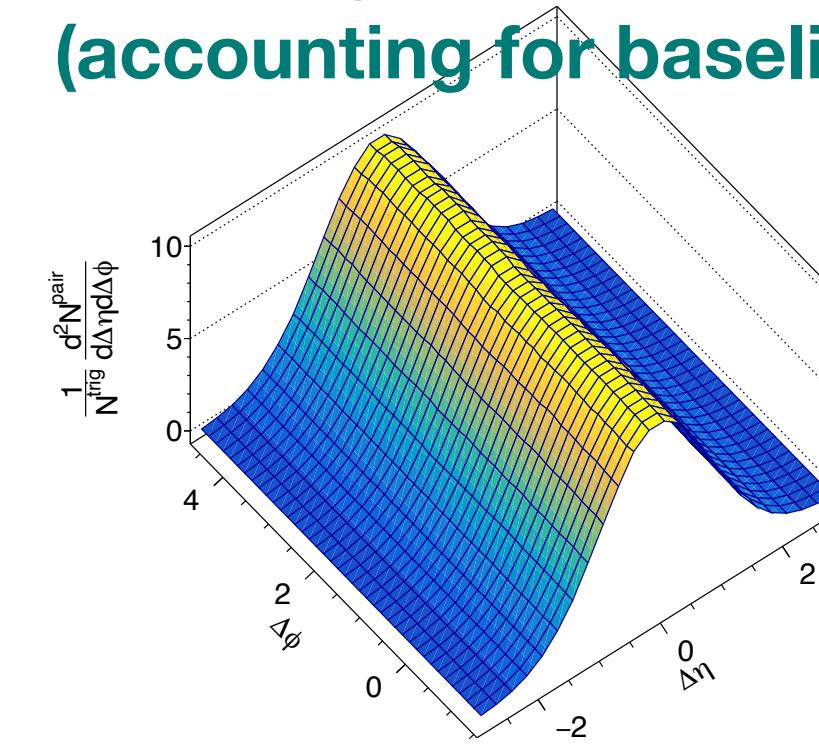


Signal

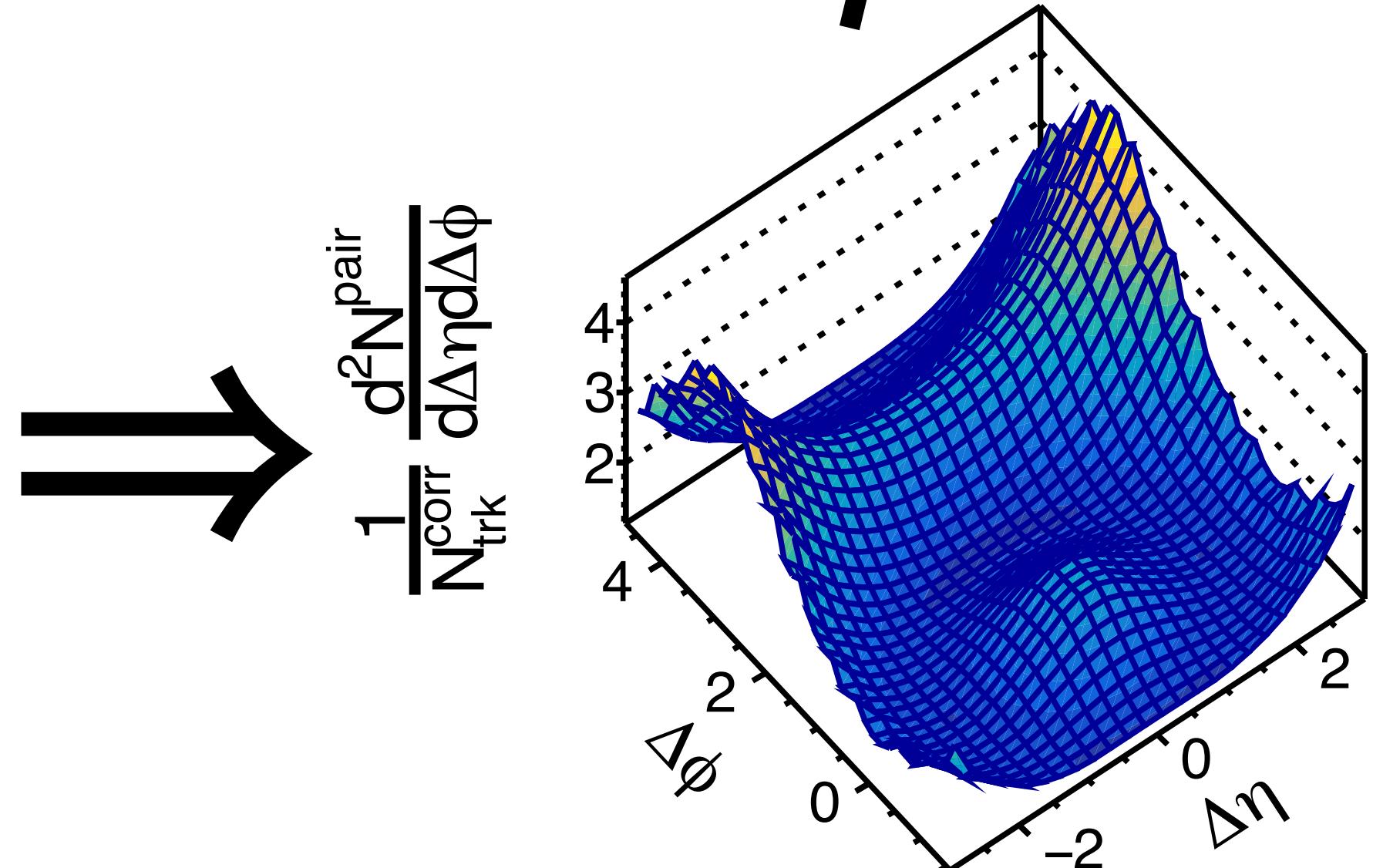
(raw correlation function)

**Background**

(accounting for baseline of random pairing)



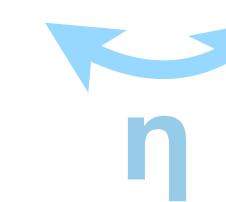
Track pairs' angular difference in
 η (pseudorapidity), ϕ (azimuthal angle)



Two-particle correlation function
(per-trigger-particle associated yield)

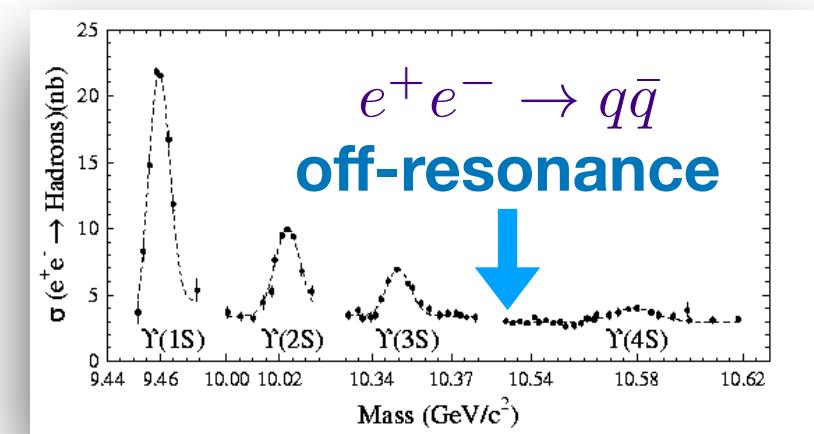
$$\frac{1}{N_{\text{corr}}} \frac{d^2N^{\text{pair}}}{d\Delta\eta d\Delta\phi} = B(0,0) \times \frac{S(\Delta\eta, \Delta\phi)}{B(\Delta\eta, \Delta\phi)}$$

Beam axis
(C.M. frame z axis)

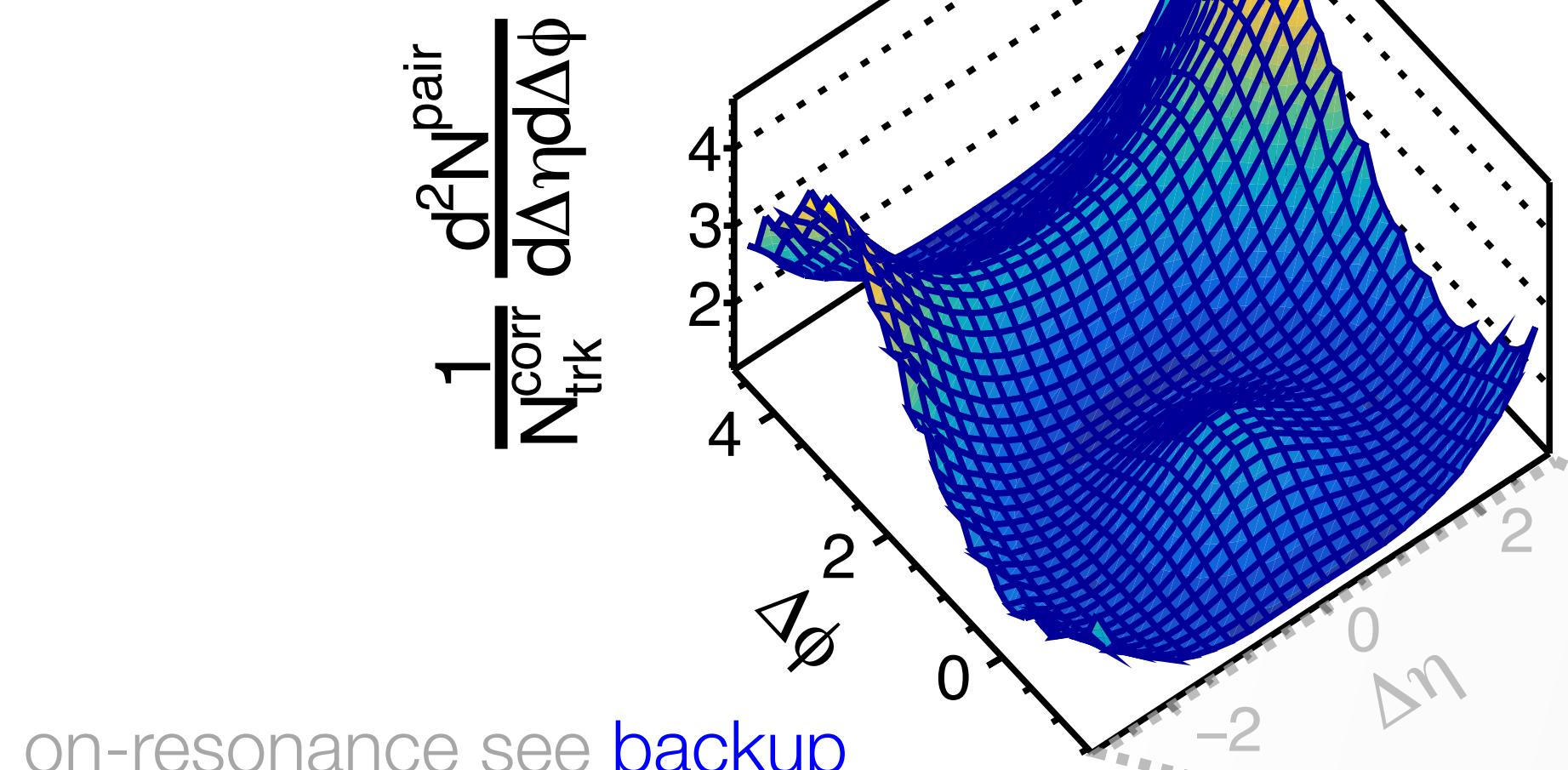


trigger particle

Reasonable data and MC agreements!



█ Data
— PYTHIA6



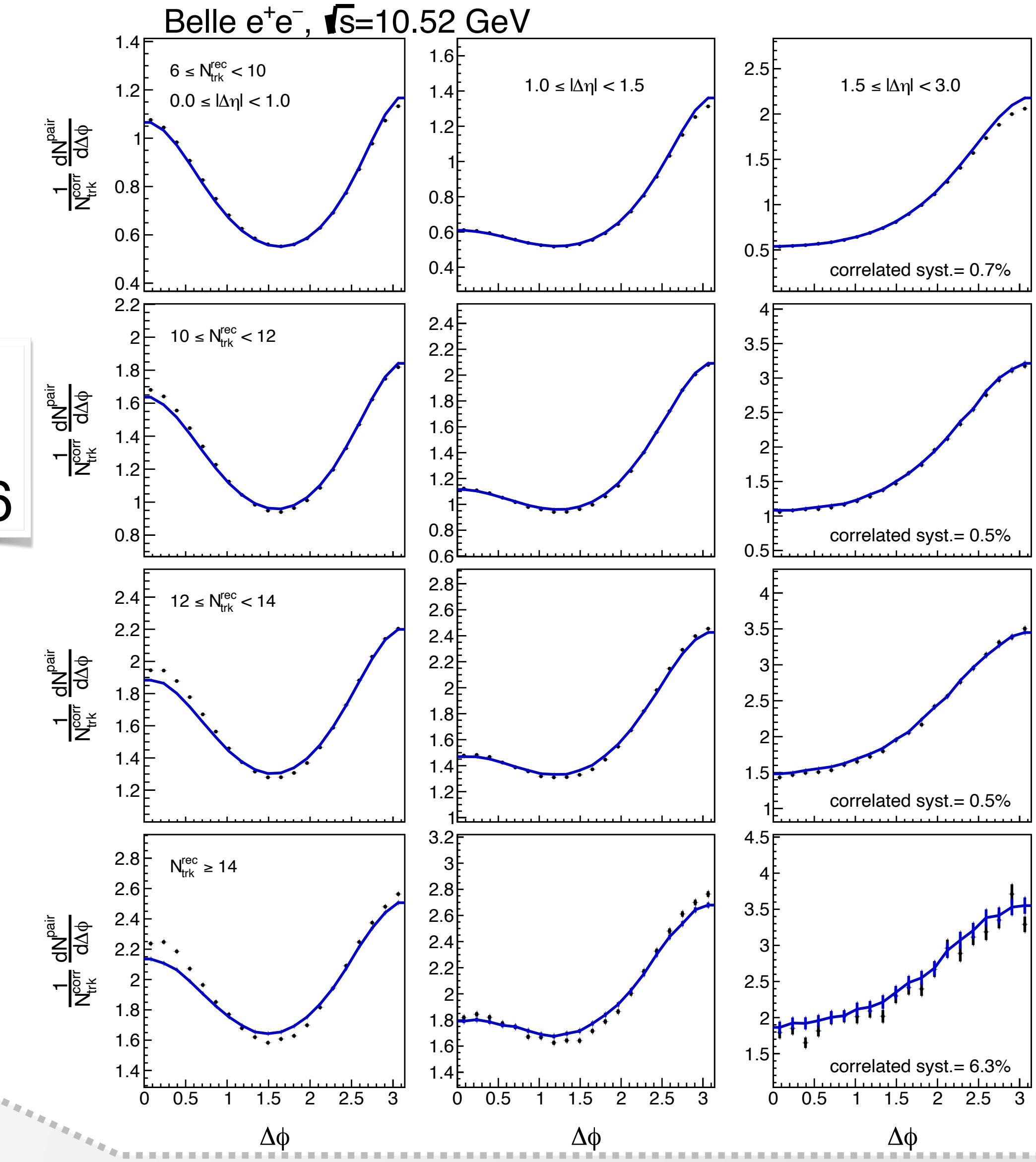
on-resonance see [backup](#)

arXiv:2201.01694

[Phys. Rev. Lett. 128
(2022) 142005]

$$12 \leq N_{\text{trk}}^{\text{rec}} < 14$$

High-multiplicity



Short Range
($0 \leq |\Delta\eta| < 1$)

Middle Range
($1 \leq |\Delta\eta| < 1.5$)

Long Range
($1.5 \leq |\Delta\eta| < 3.0$)

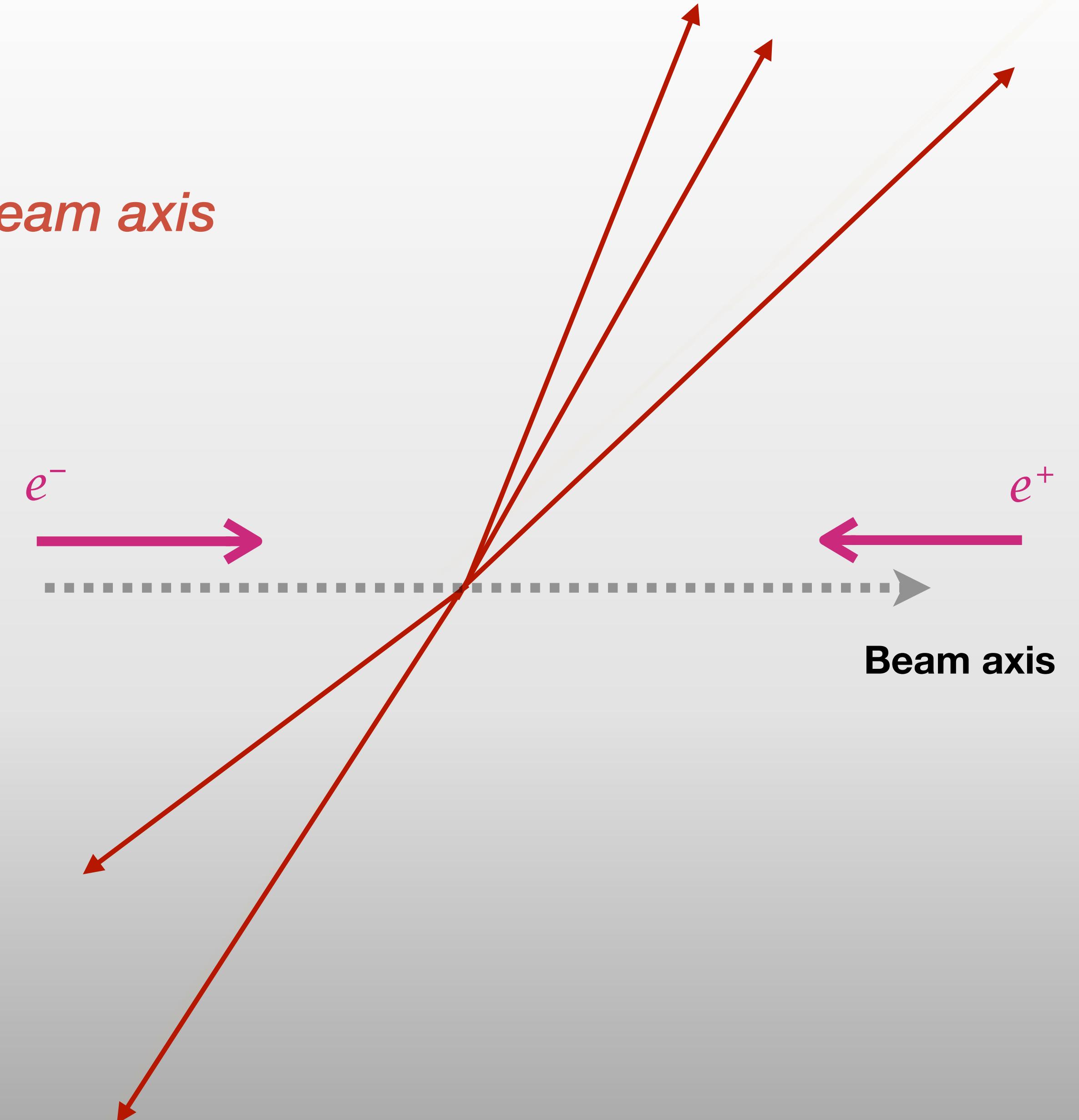
Thrust-axis two-particle correlation

Out-going direction of e^+e^- event \neq beam axis

$$T = \max_{\hat{n}} \frac{\sum_i |\vec{p}_i \cdot \hat{n}|}{\sum_i |\vec{p}_i|}$$

($i \in$ charged, neutral particles and MET)

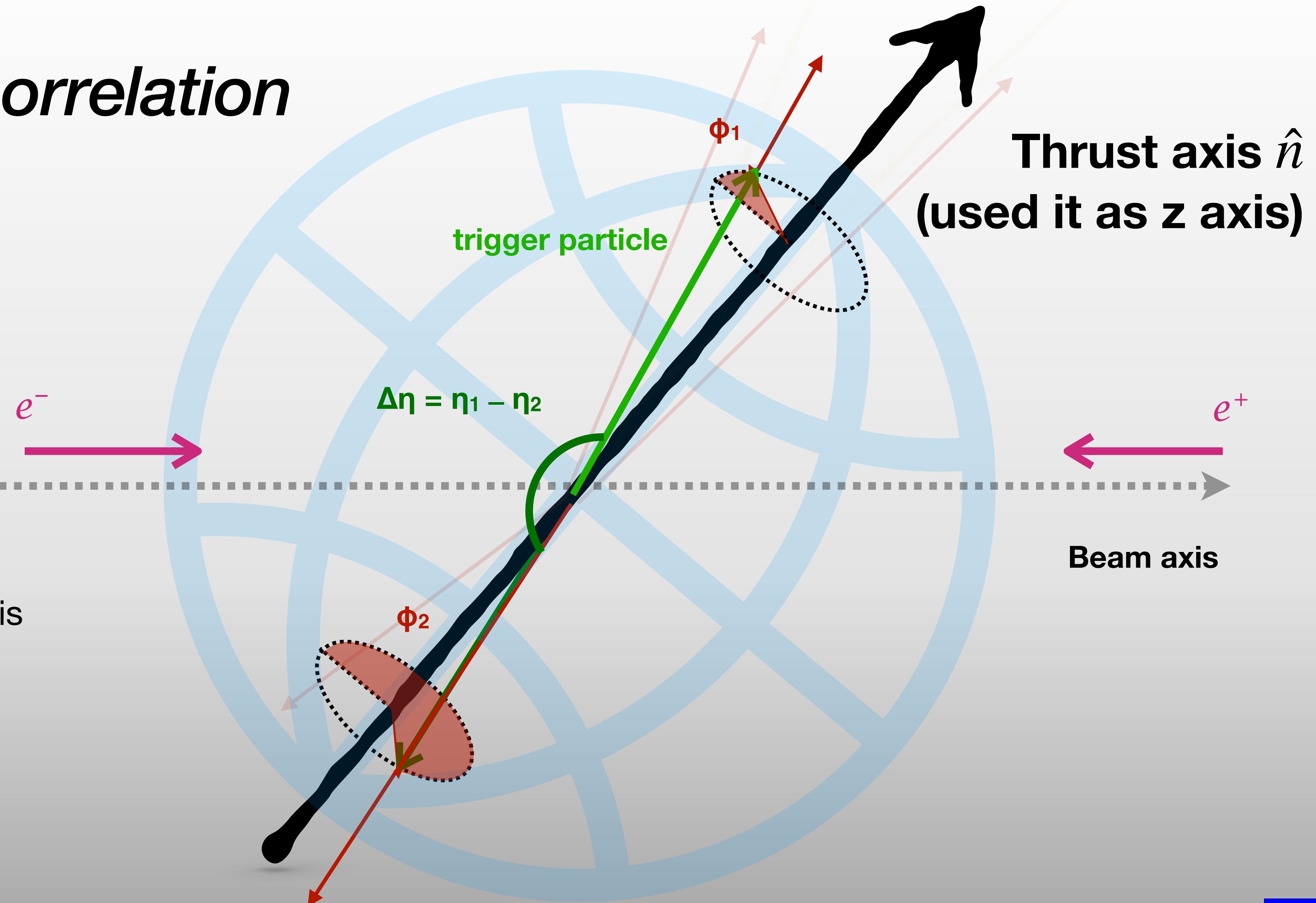
$$\vec{p}_{\text{MET}} = - \sum_{\text{neu,chg}} \vec{p}$$



Thrust-axis two-particle correlation

$$T = \max_{\hat{n}} \frac{\sum_i |\vec{p}_i \cdot \hat{n}|}{\sum_i |\vec{p}_i|}$$

Particles (p_T, η, ϕ) are re-calculated w.r.t. thrust axis

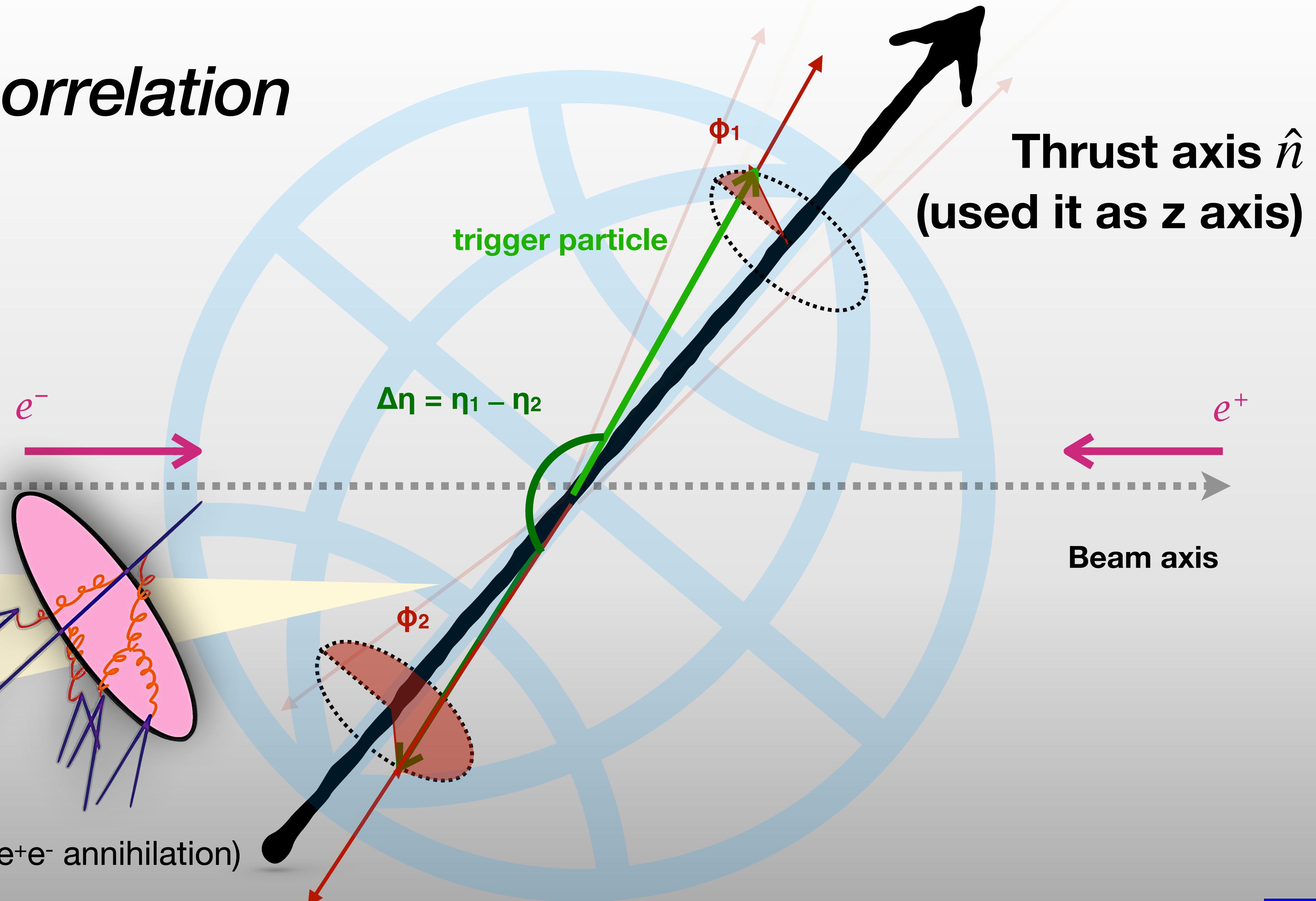


Thrust-axis two-particle correlation

$$T = \max_{\hat{n}} \frac{\sum_i |\vec{p}_i \cdot \hat{n}|}{\sum_i |\vec{p}_i|}$$

If high energy quarks can form some medium, looking from the thrust axis is sensitive to the azimuthal anisotropy of this “imaginary medium.”

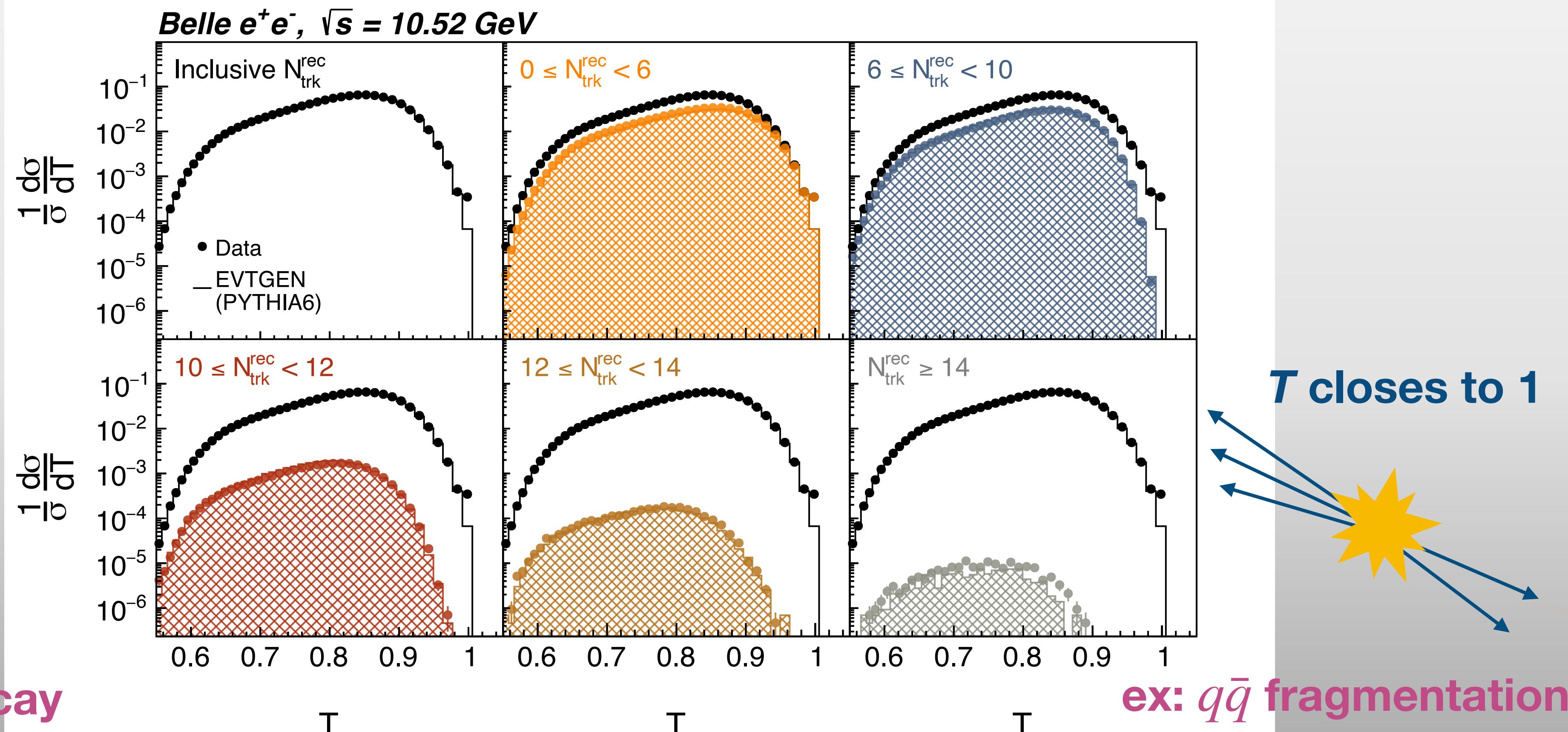
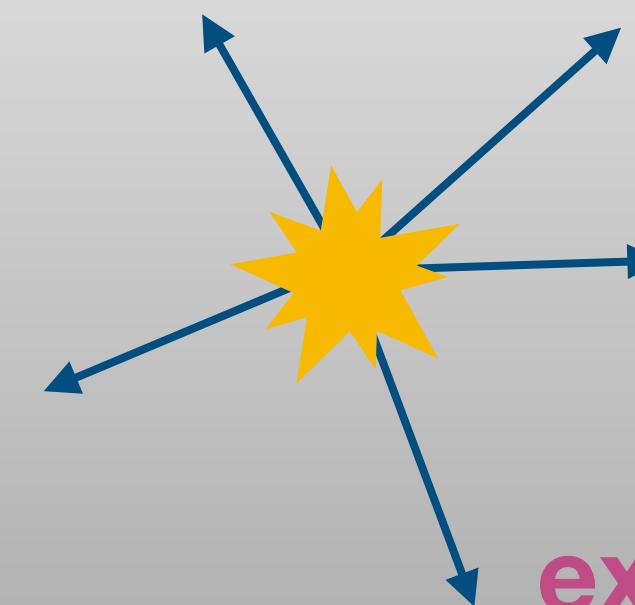
(quark from e^+e^- annihilation)



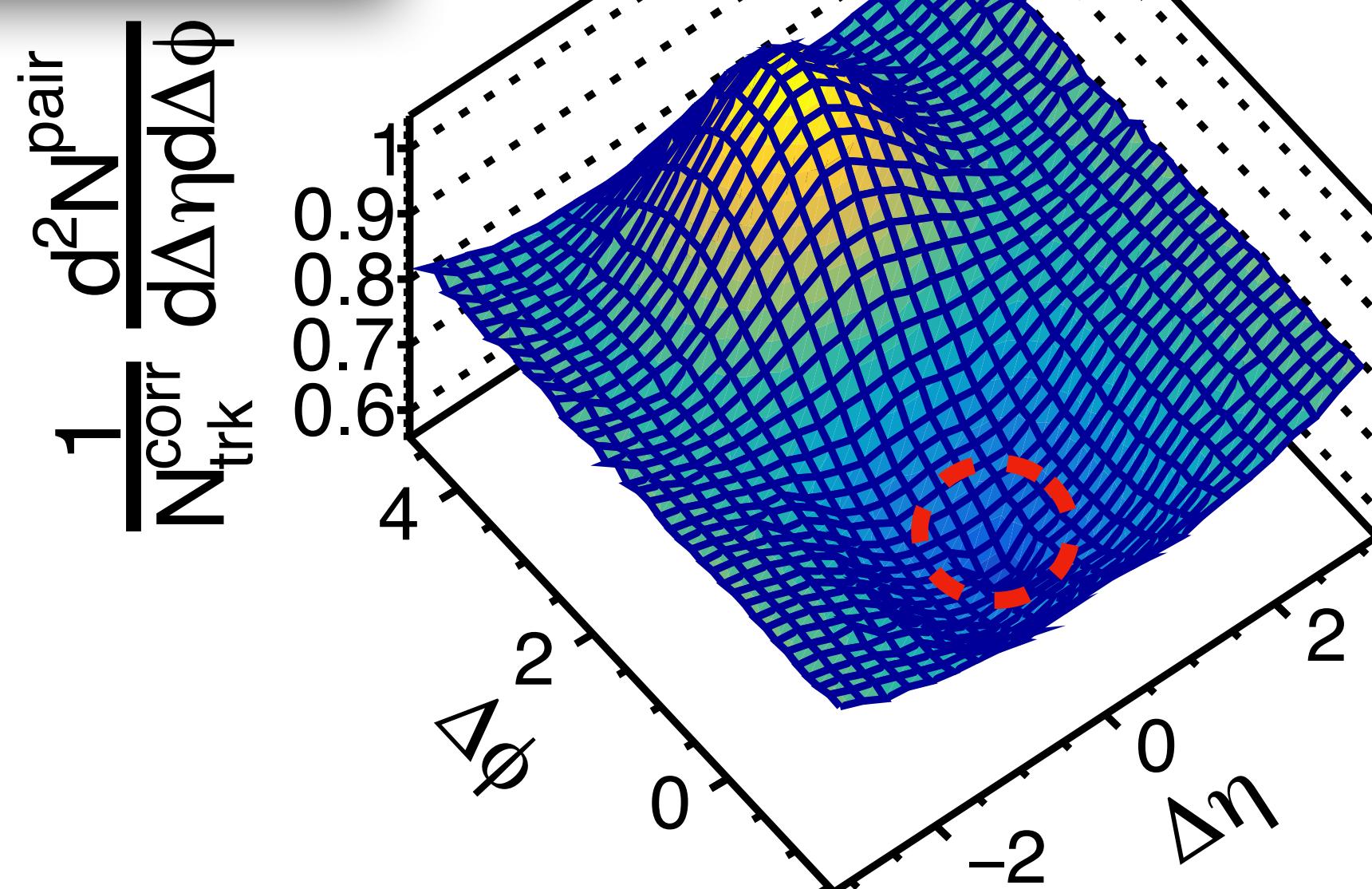
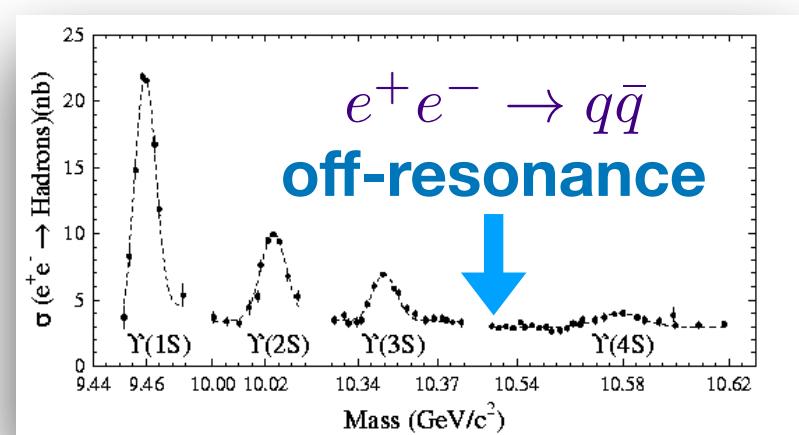
Thrust distribution

$$T = \max_{\hat{n}} \frac{\sum_i |\vec{p}_i \cdot \hat{n}|}{\sum_i |\vec{p}_i|}$$

T closes to 0.5

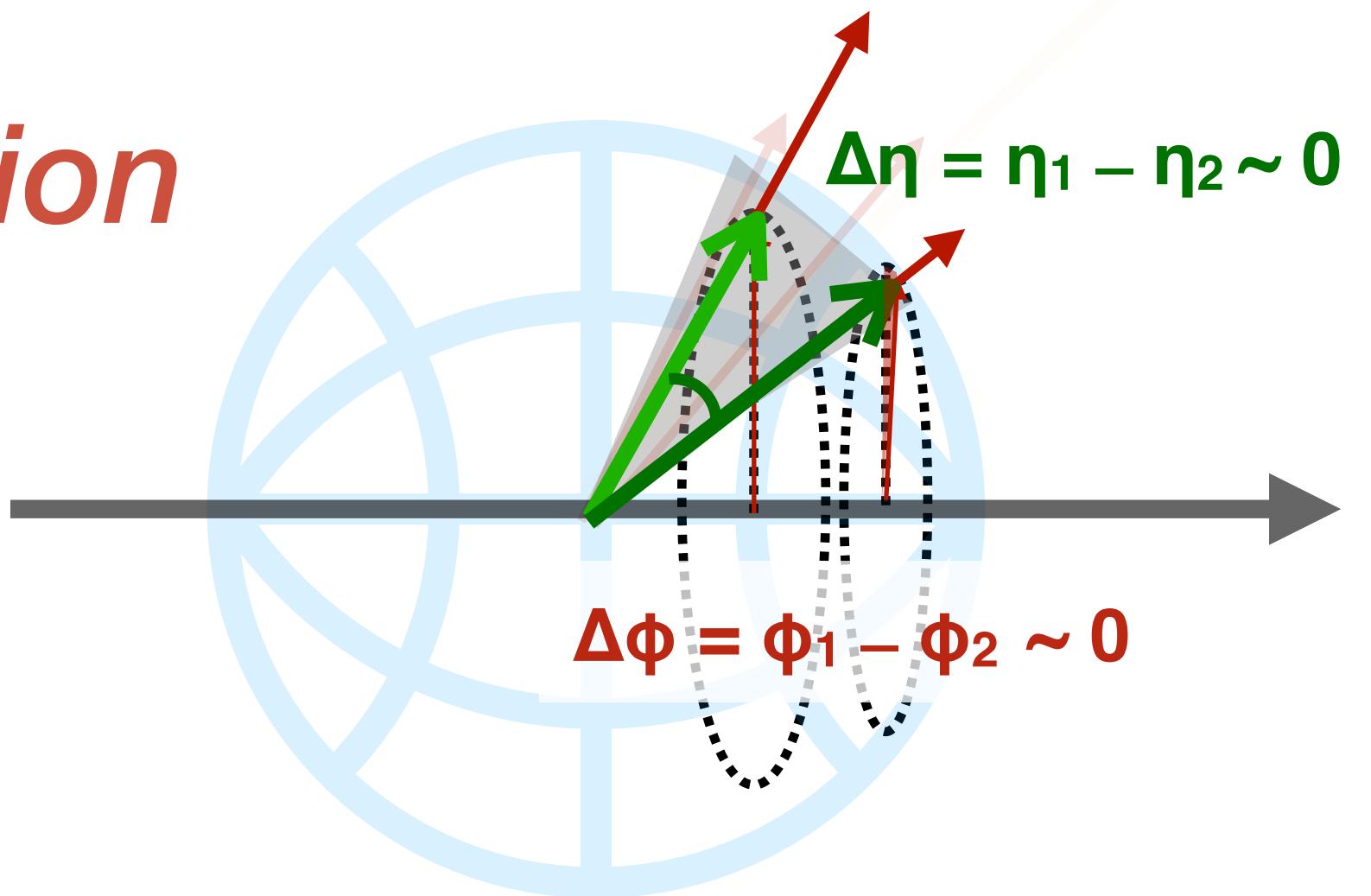


Lack of origin-peak jet correlation

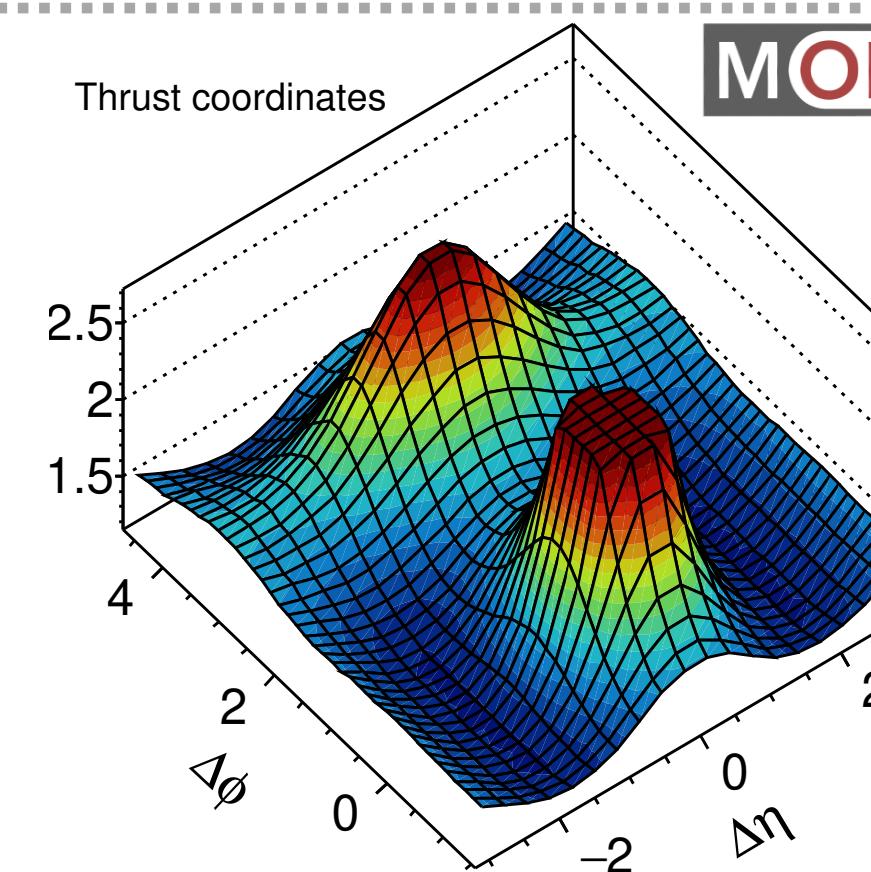


arXiv:2201.01694
PRL ref.

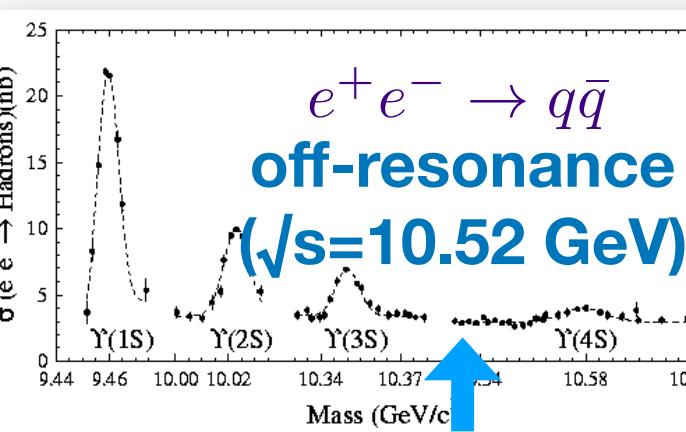
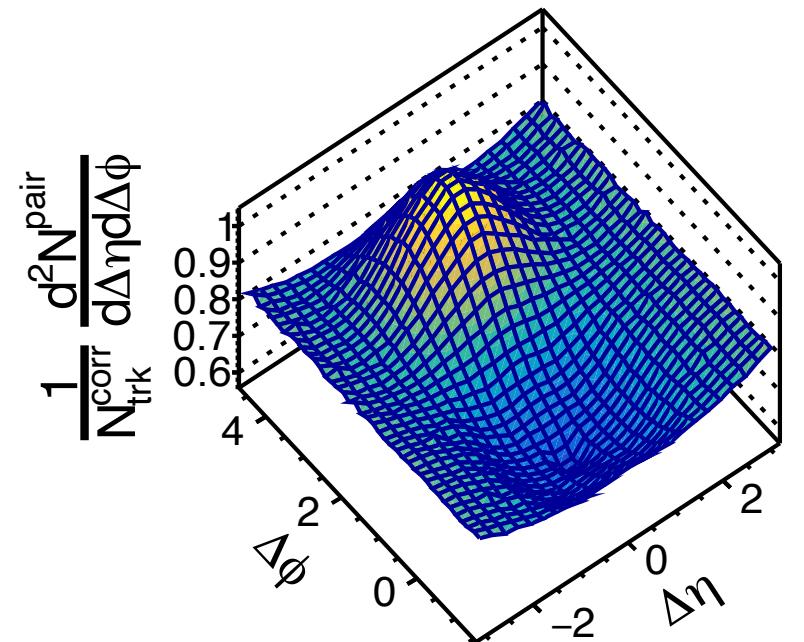
$$12 \leq N_{\text{trk}}^{\text{rec}} < 14$$



c.f. e^+e^- @ LEP1 (Z-pole energy)
[\[Phys. Rev. Lett. 123, 212002 \(2019\)\]](#)



- Simulate w/ Sherpa @ different \sqrt{s}



$\sqrt{s} = 15 \text{ GeV}$

- Sharp origin-peak correlation is recovered as \sqrt{s} goes high
- Thrust-axis analysis: from null to significant intra-jet correlation!

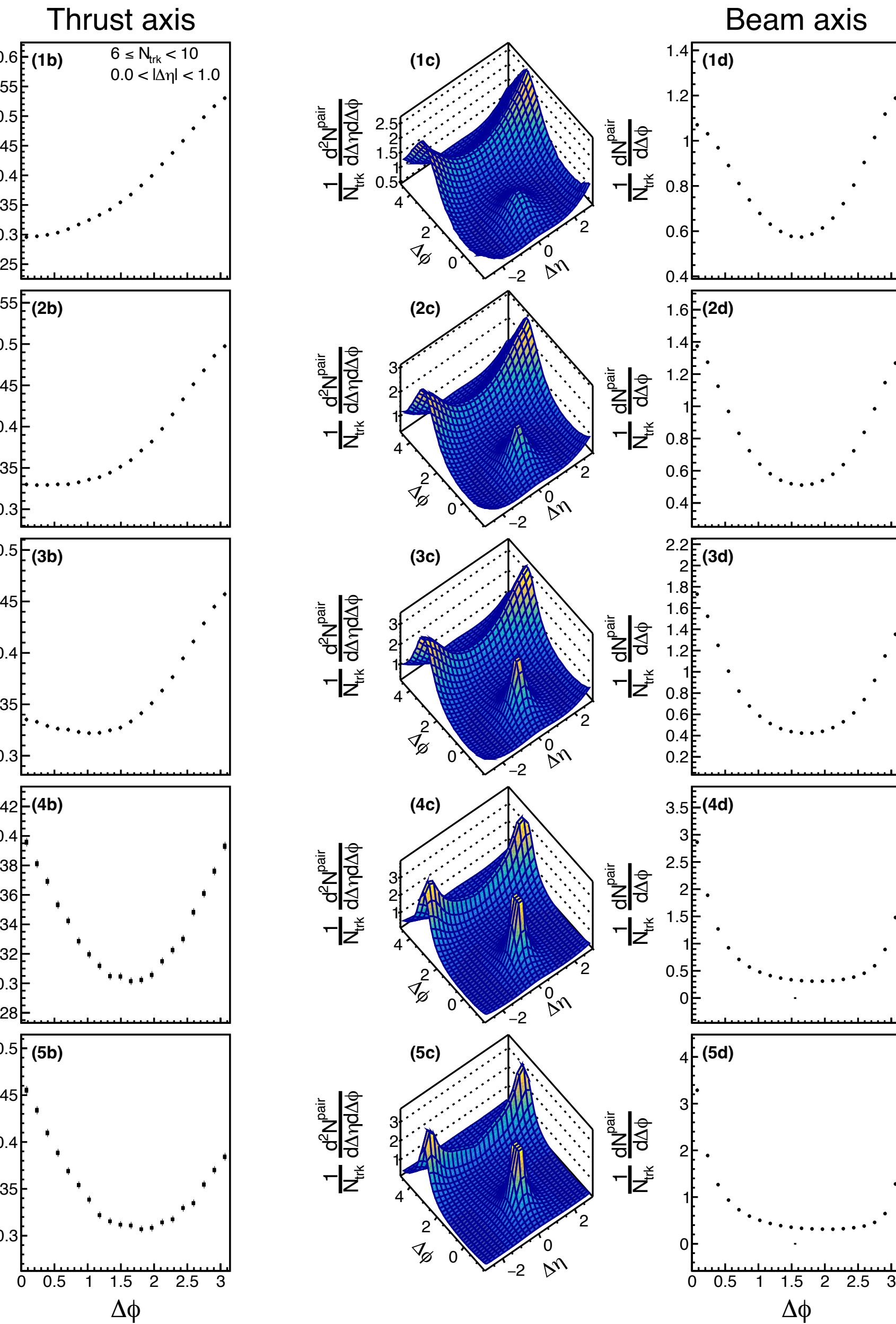
$\sqrt{s} = 20 \text{ GeV}$

$\sqrt{s} = 50 \text{ GeV}$

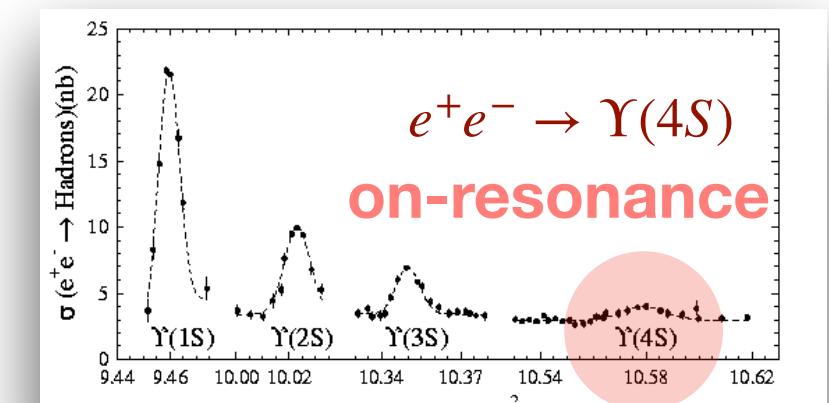
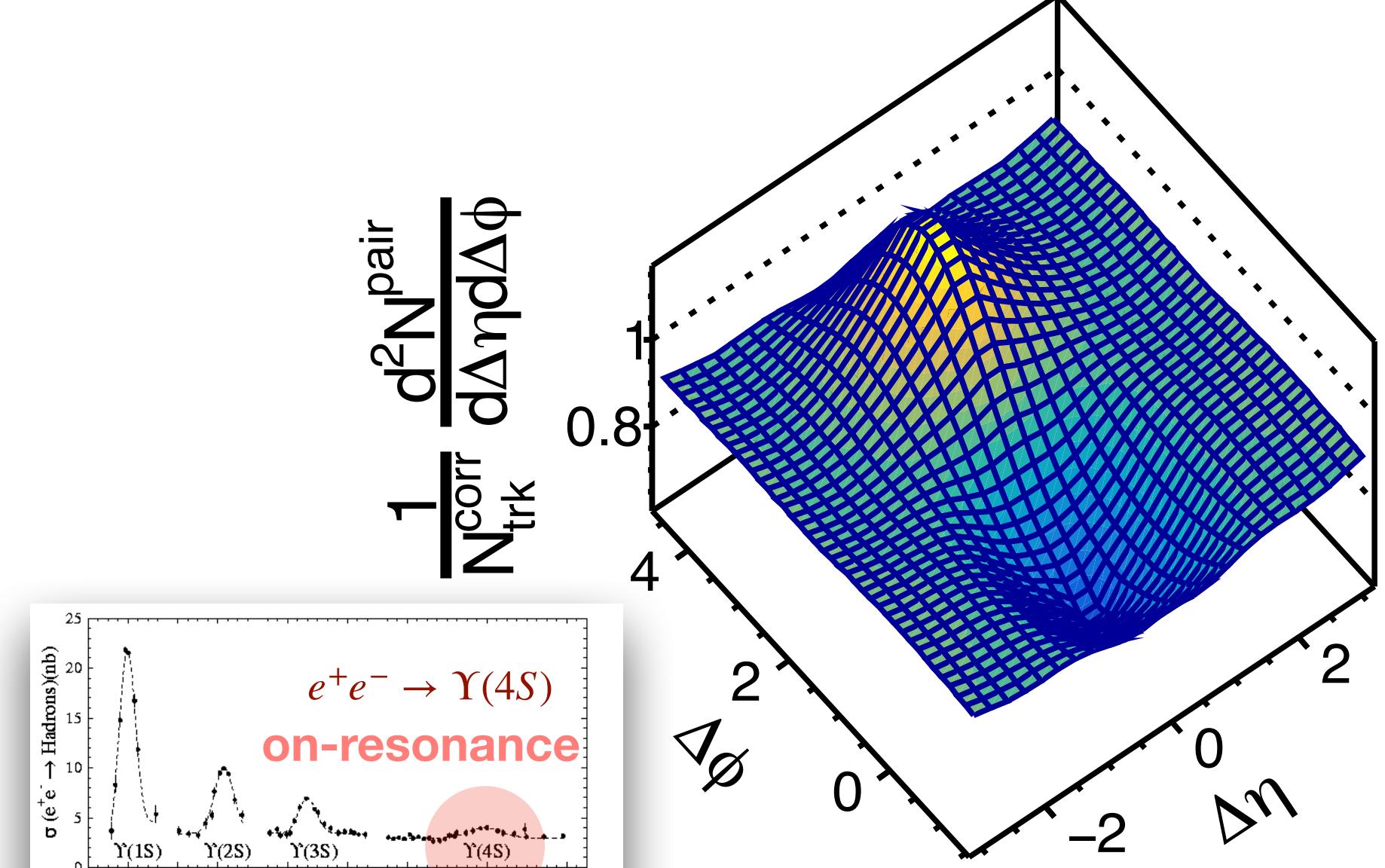
$\sqrt{s} = 91.2 \text{ GeV}$
(LEP1 energy)

* Demonstrated with $6 \leq N_{\text{trk}} < 10$
This phenomenon is seen in all multiplicity ranges

Larger origin peak correlation is found



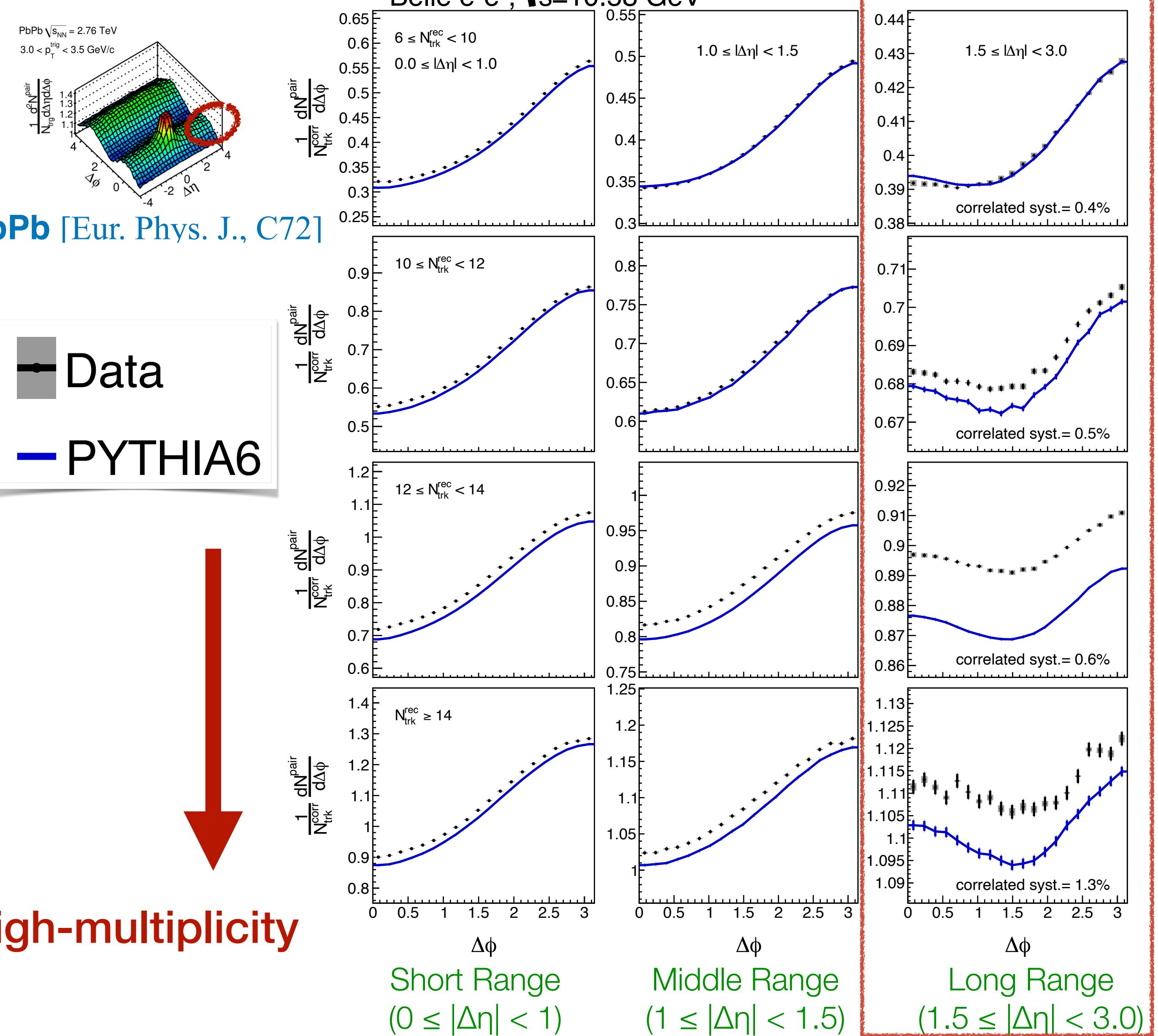
- Enhanced long-range near-side correlation, but does NOT resemble to typical ridge structure
- Similar enhancement seen in MC

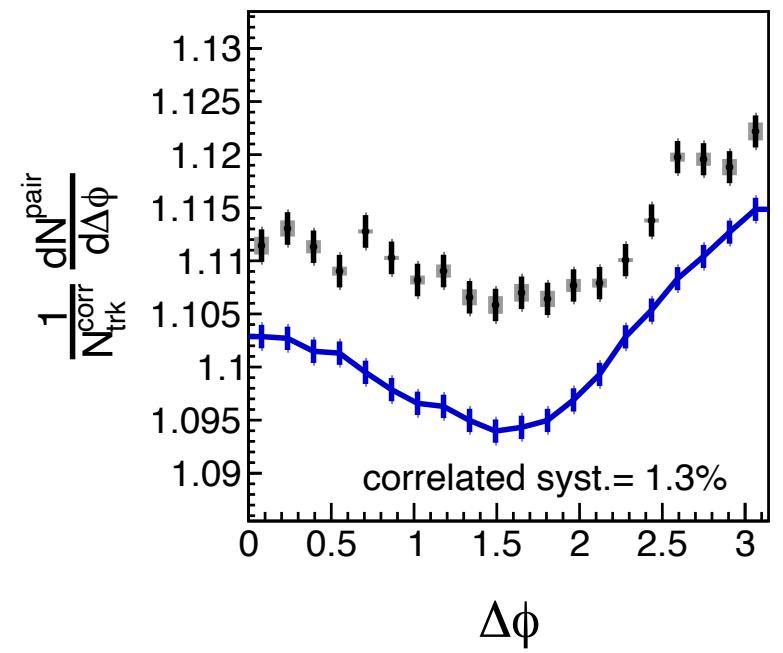


arXiv:2206.09440
submitted to JHEP

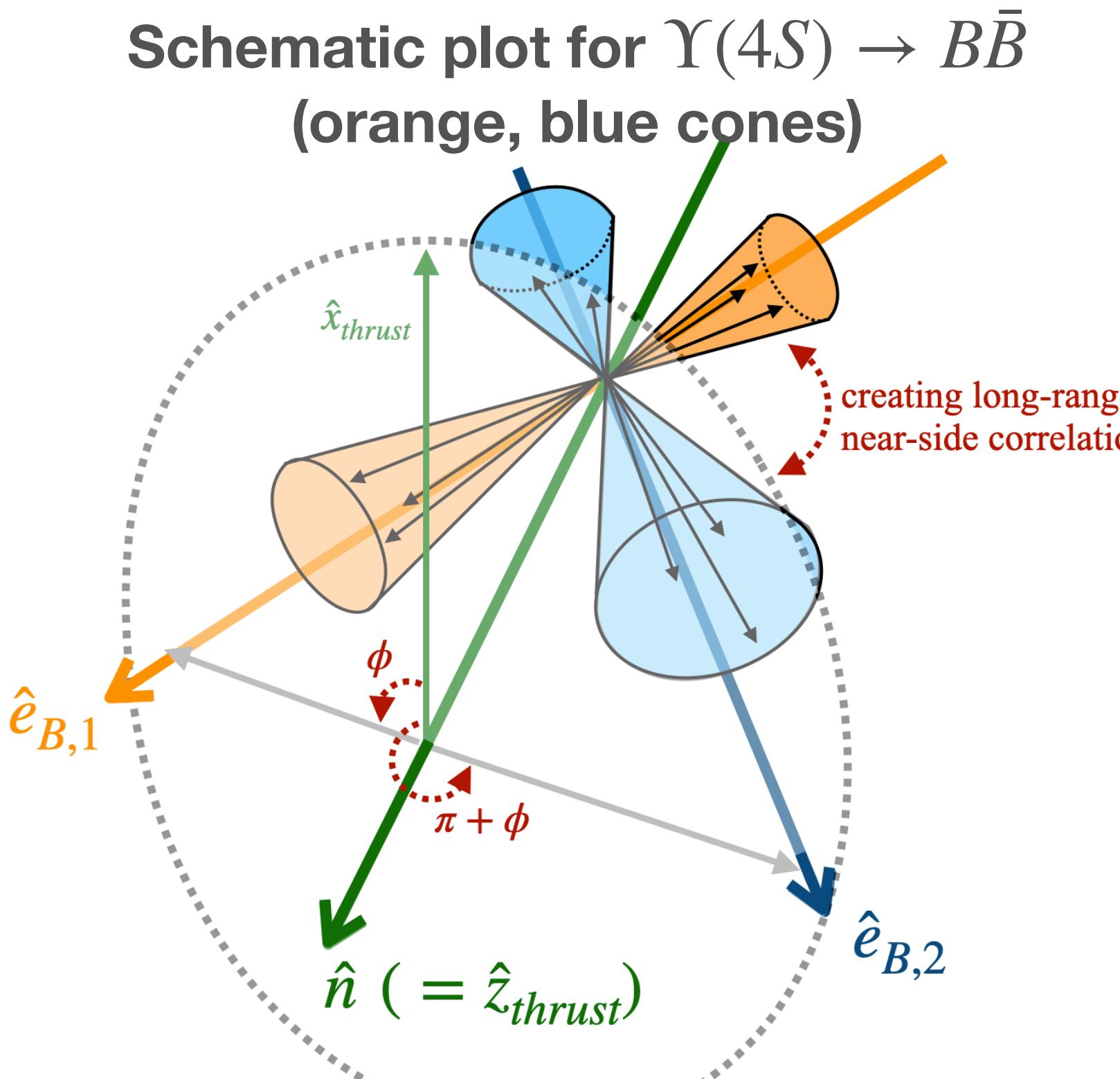
$$12 \leq N_{\text{trk}}^{\text{rec}} < 14$$

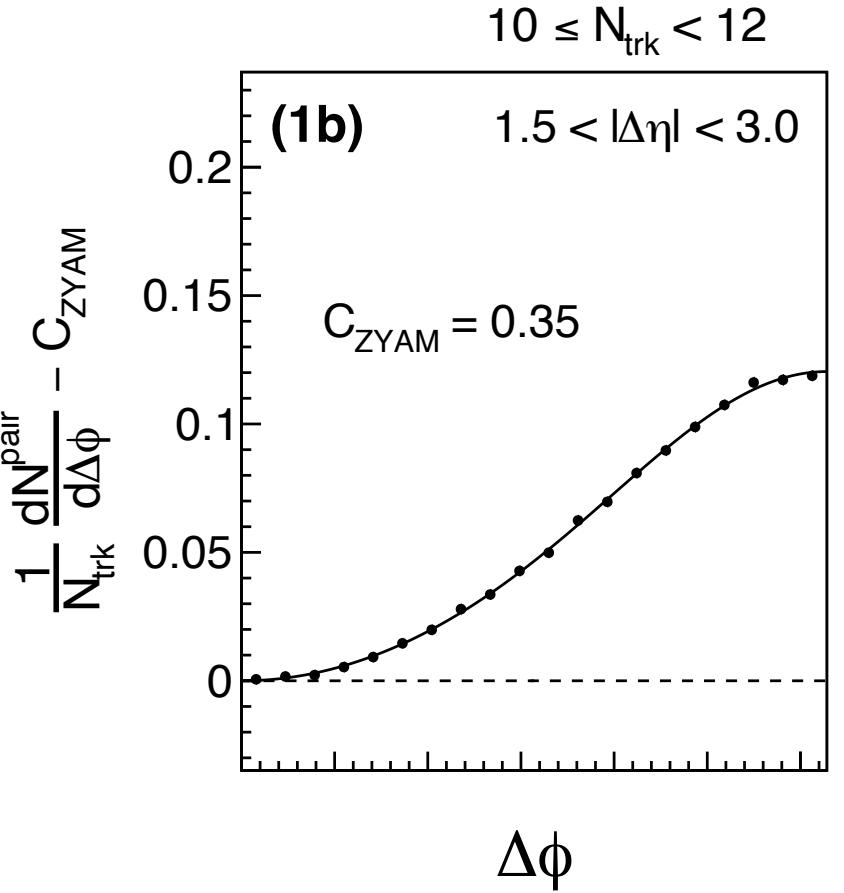
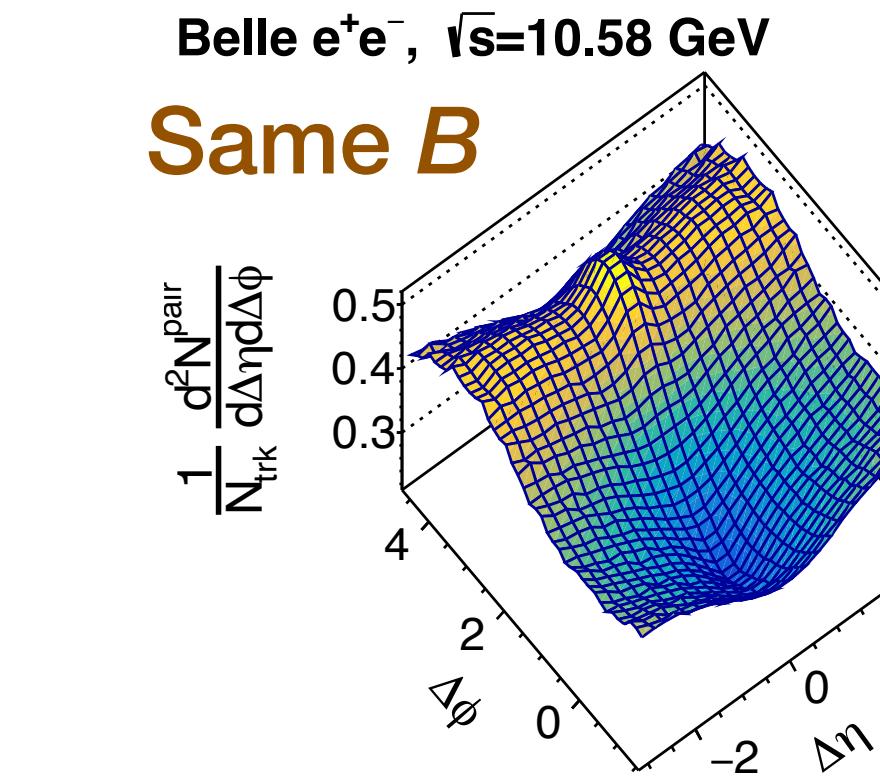
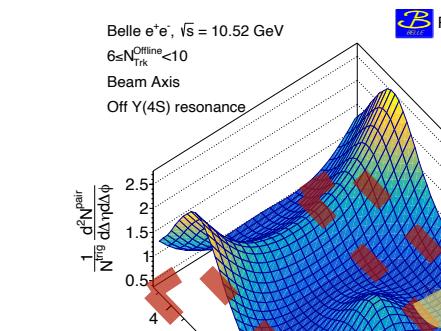
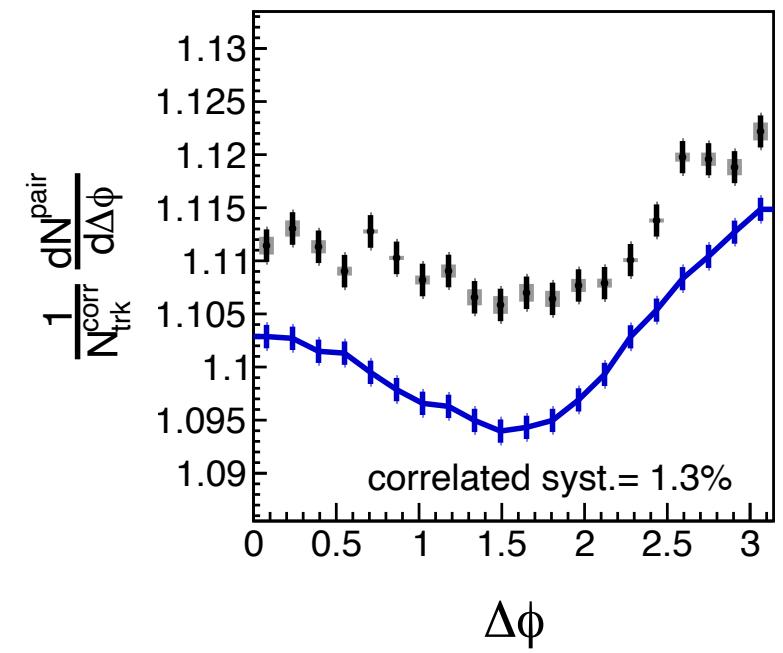
High-multiplicity



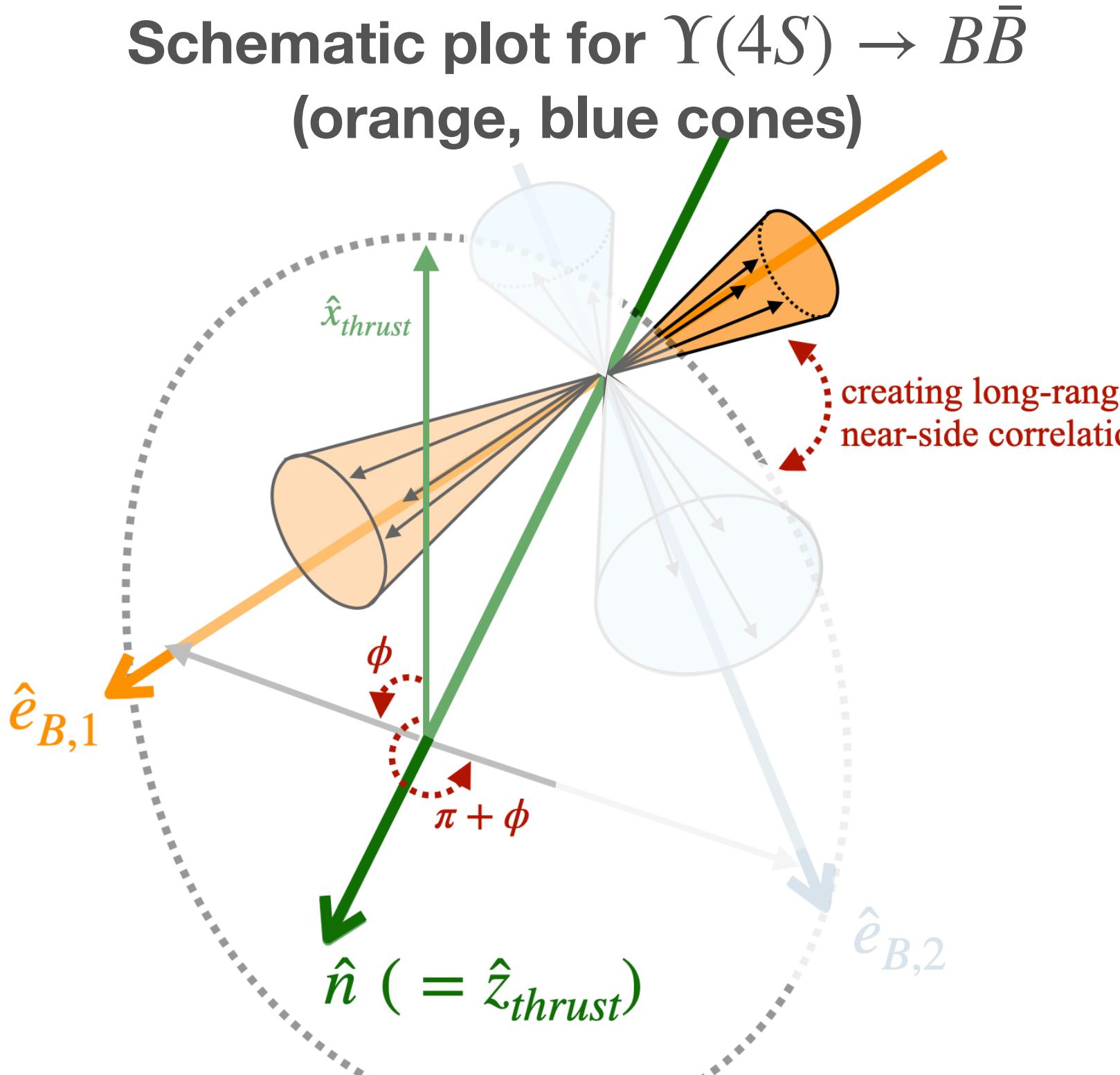


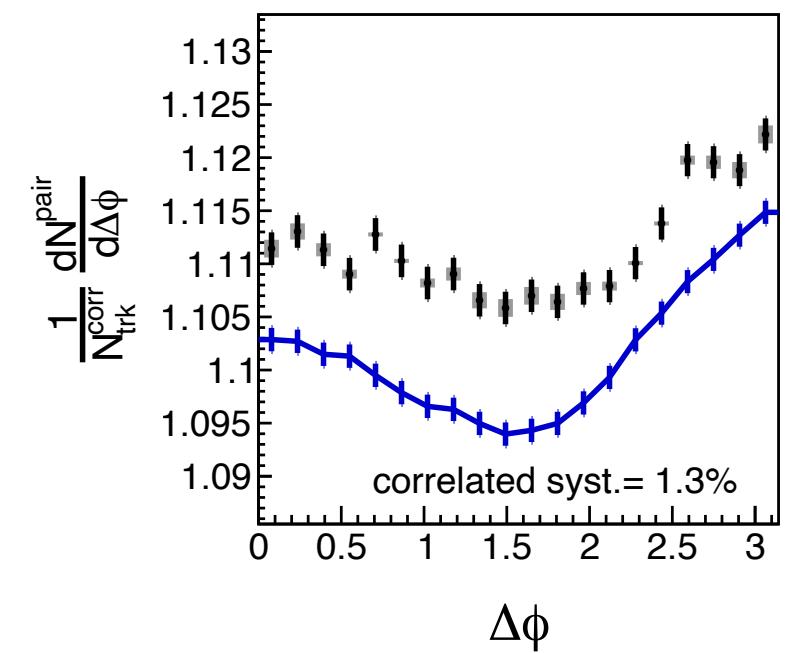
- Two B -meson decays:
special event topology
thrust axis alignment



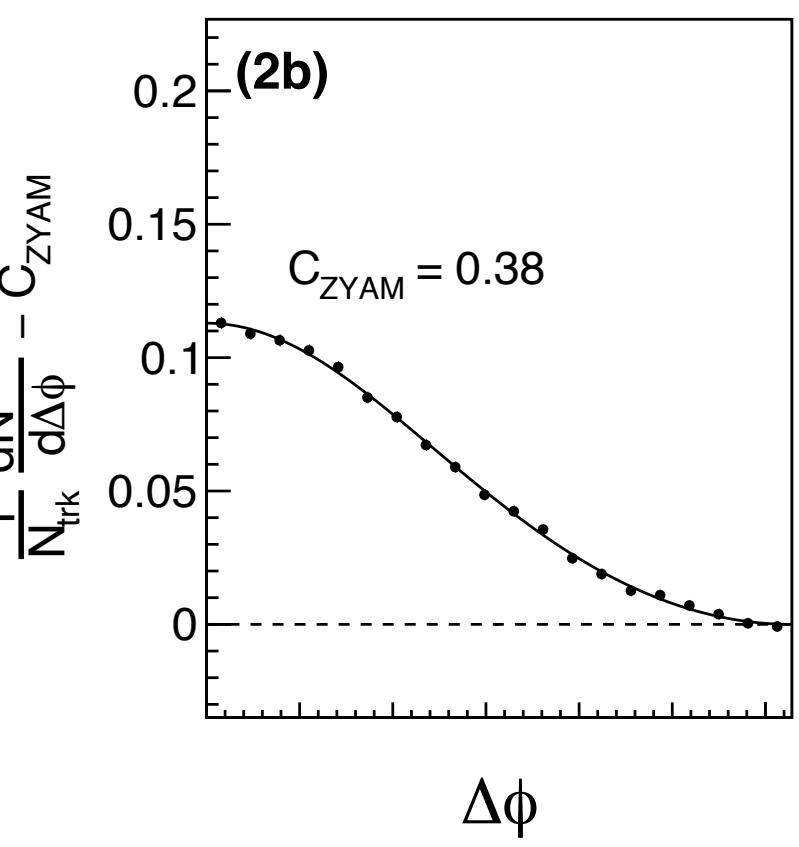
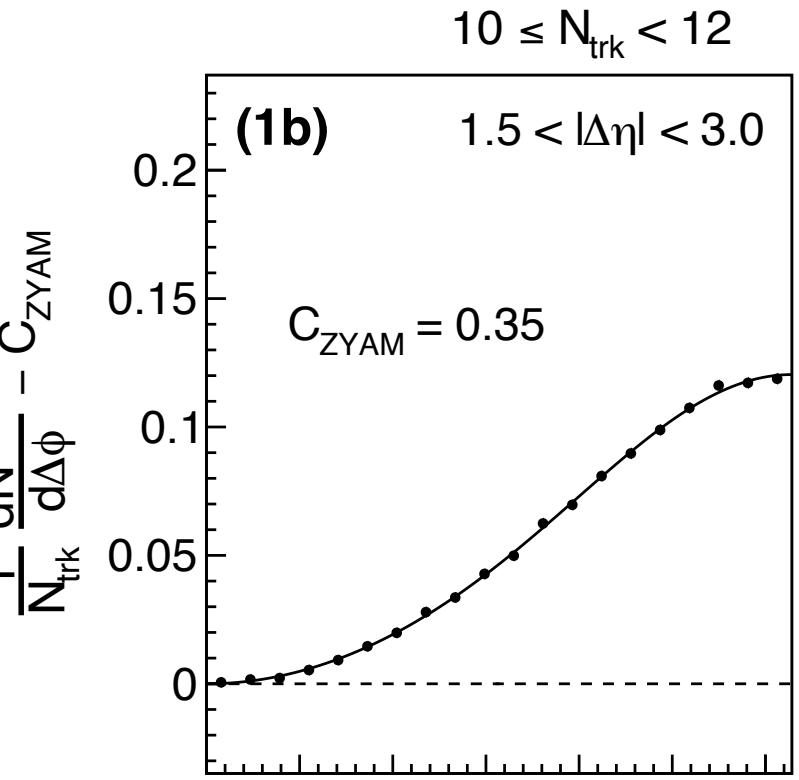
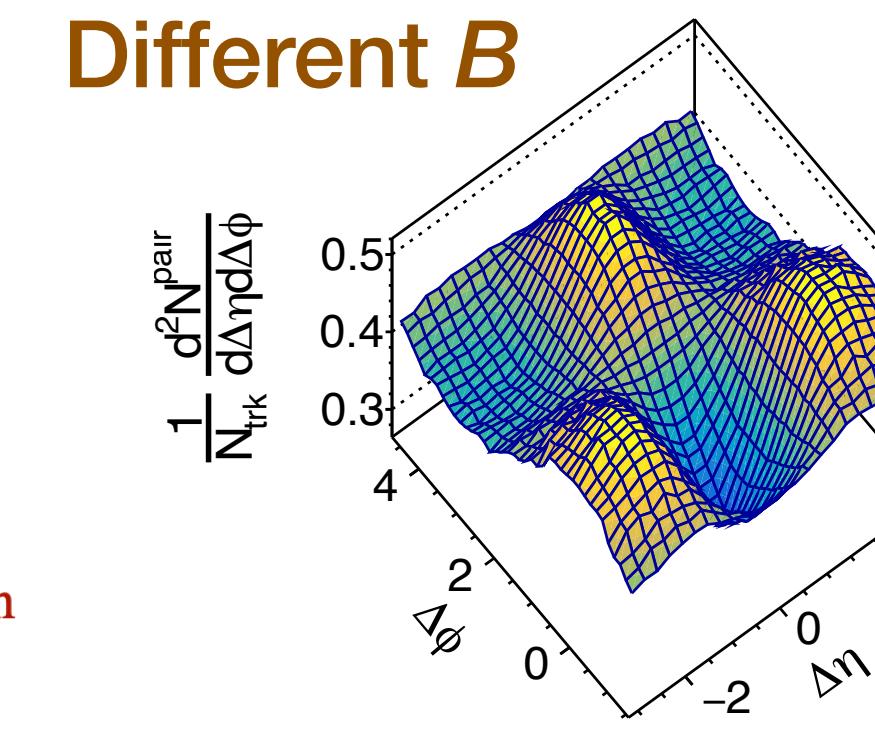
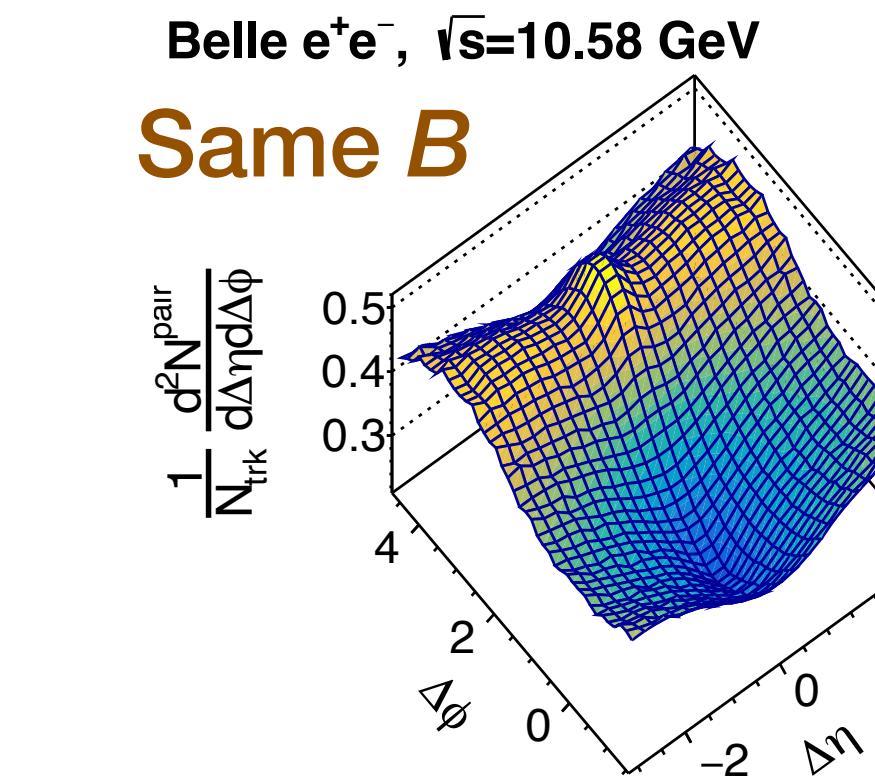
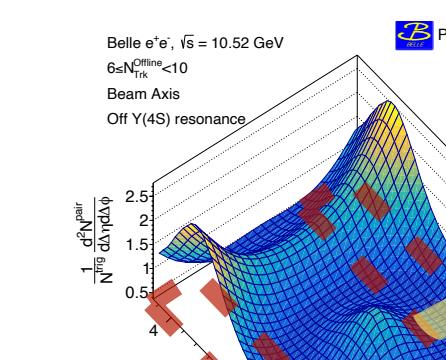
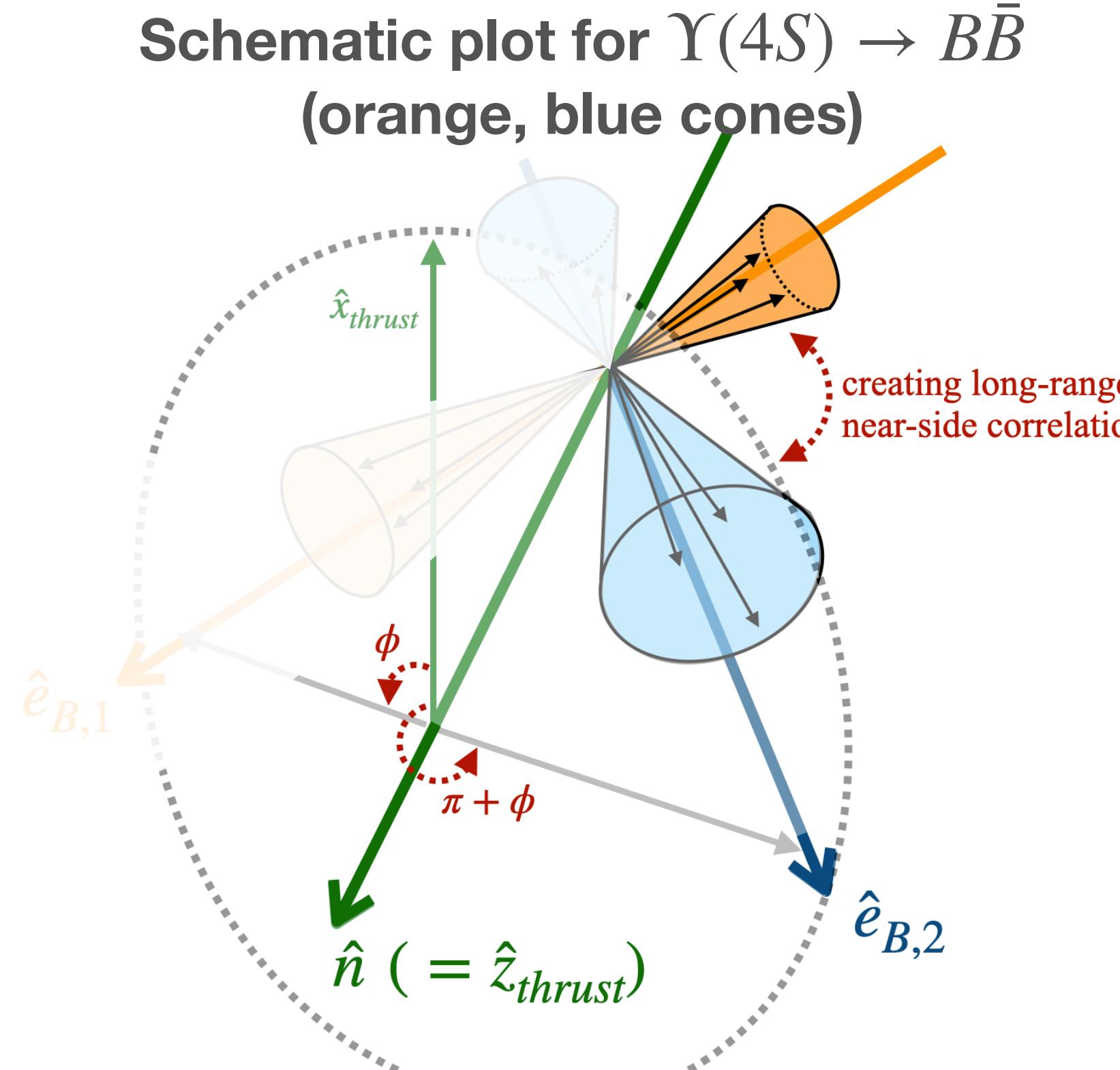


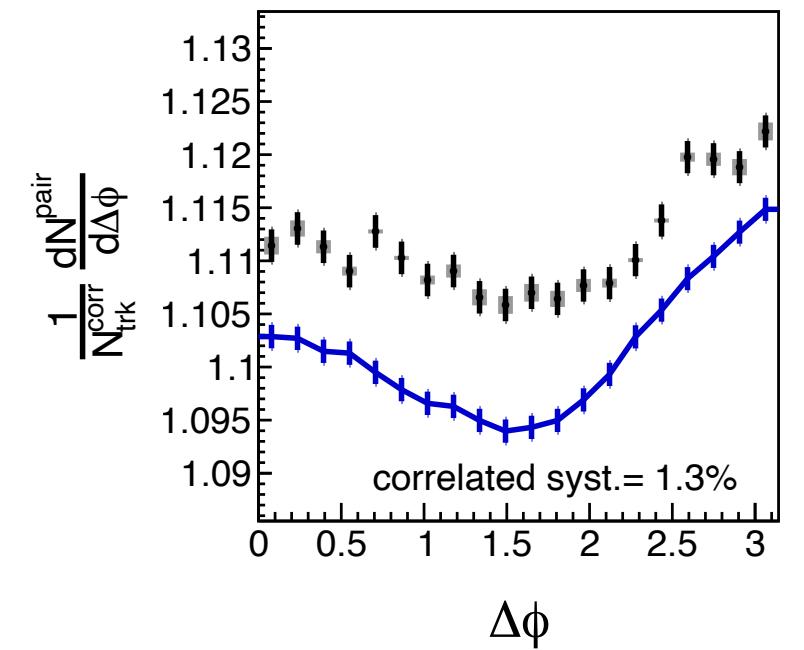
- Two B -meson decays: special event topology thrust axis alignment



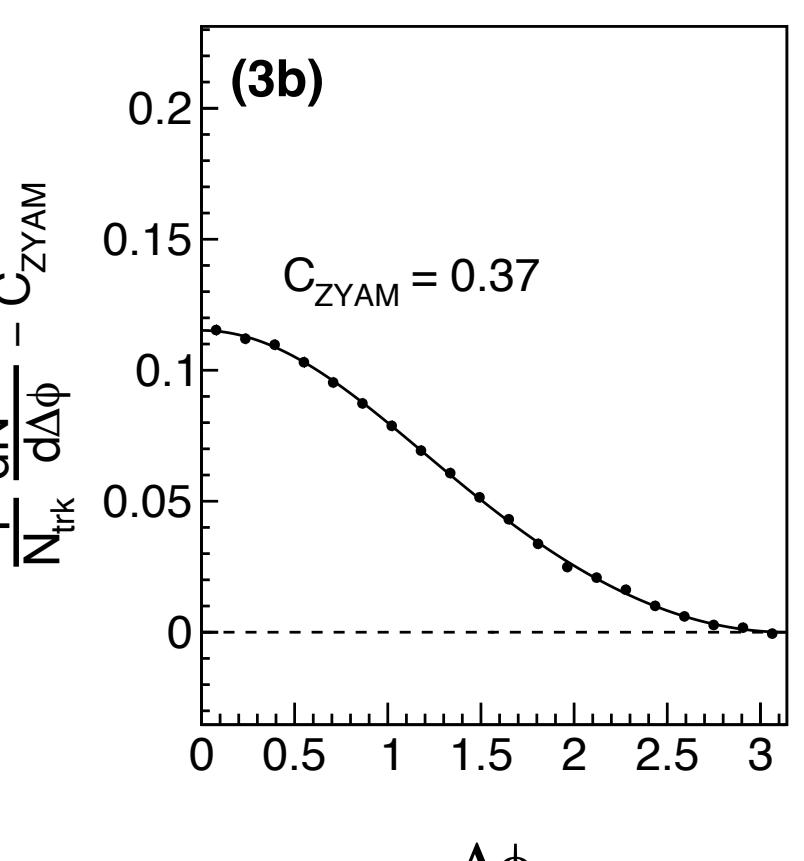
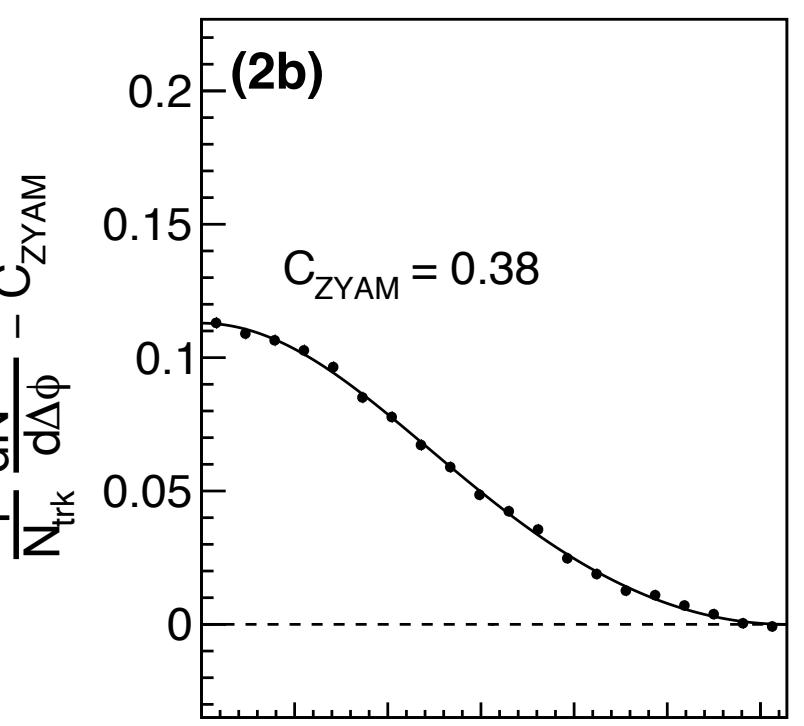
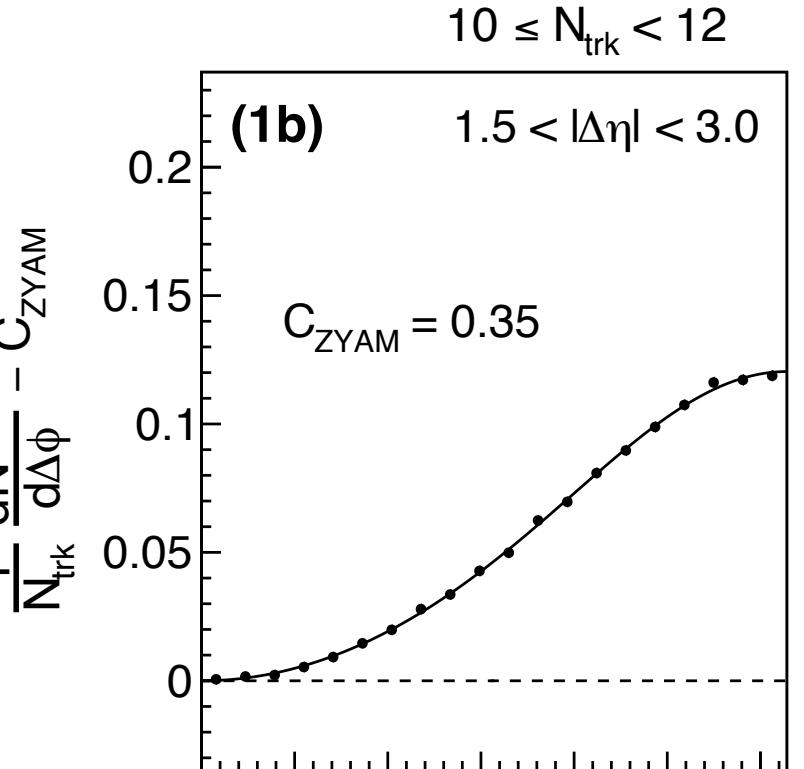
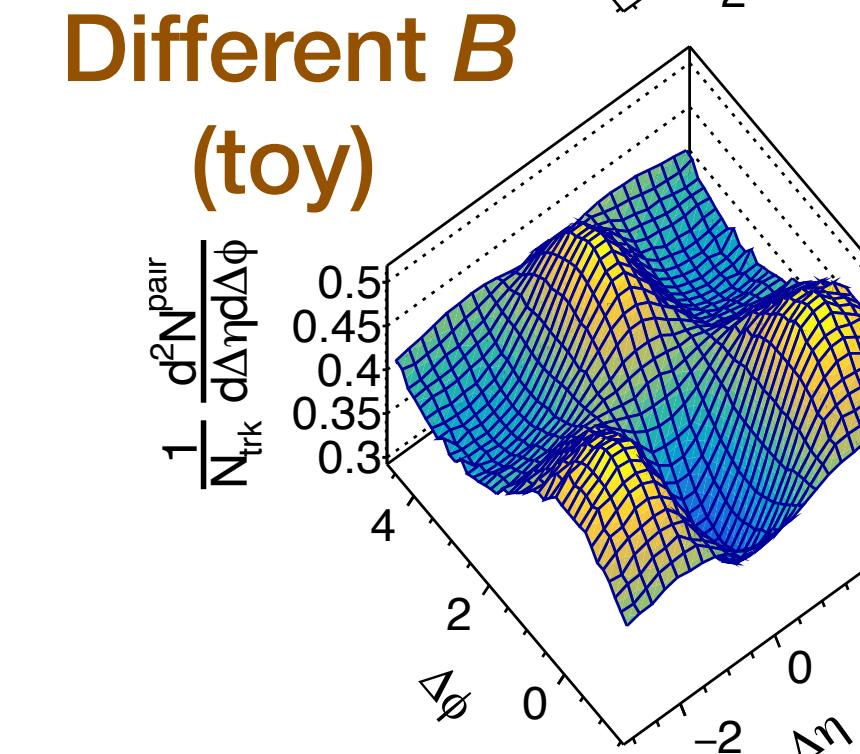
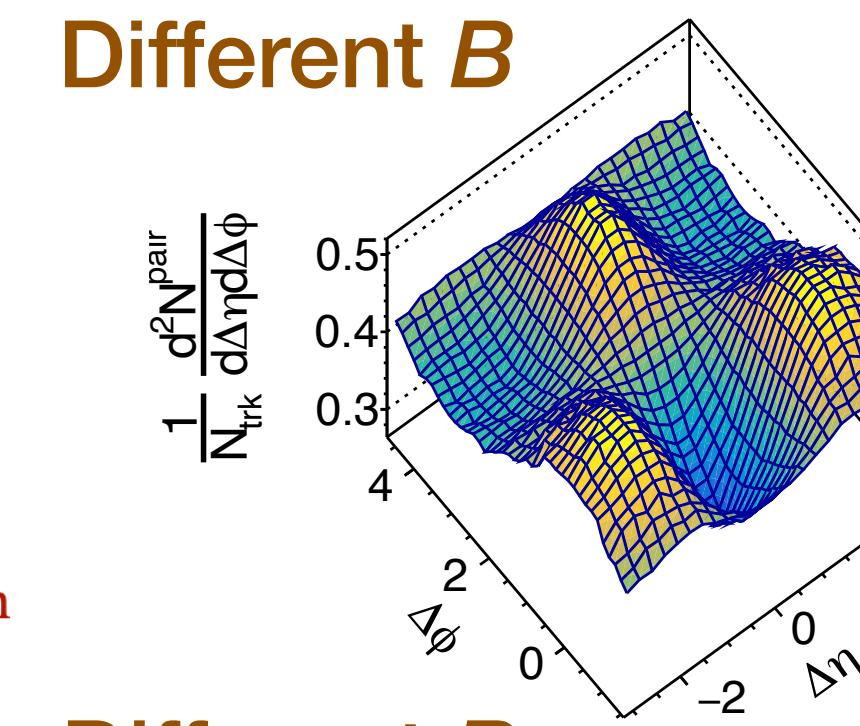
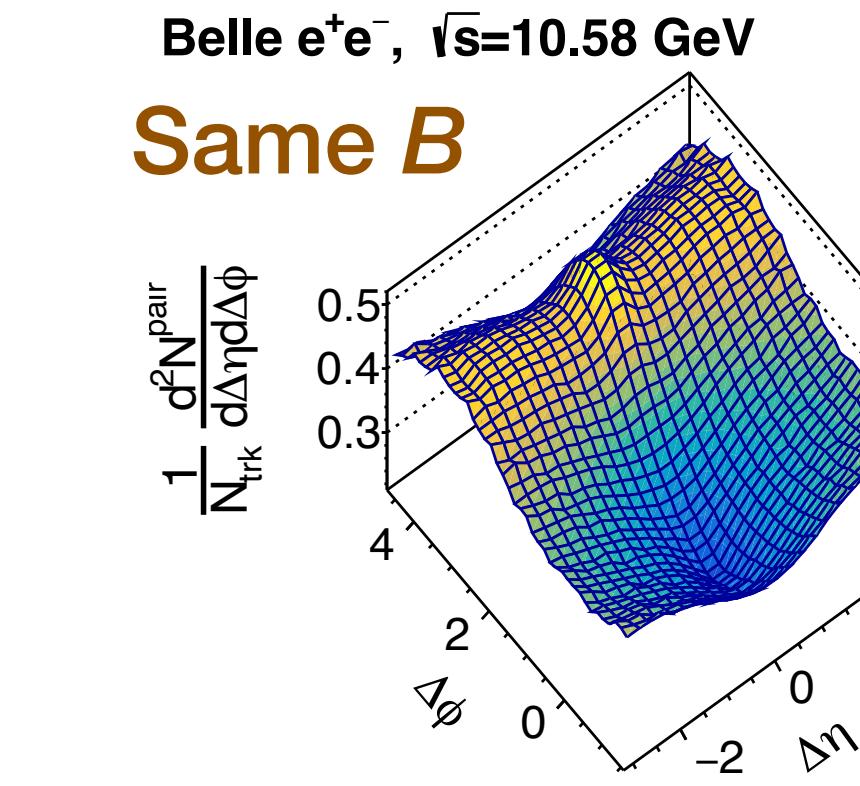
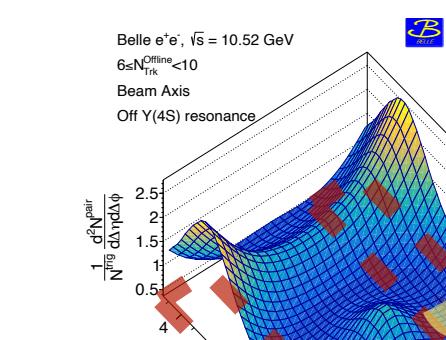
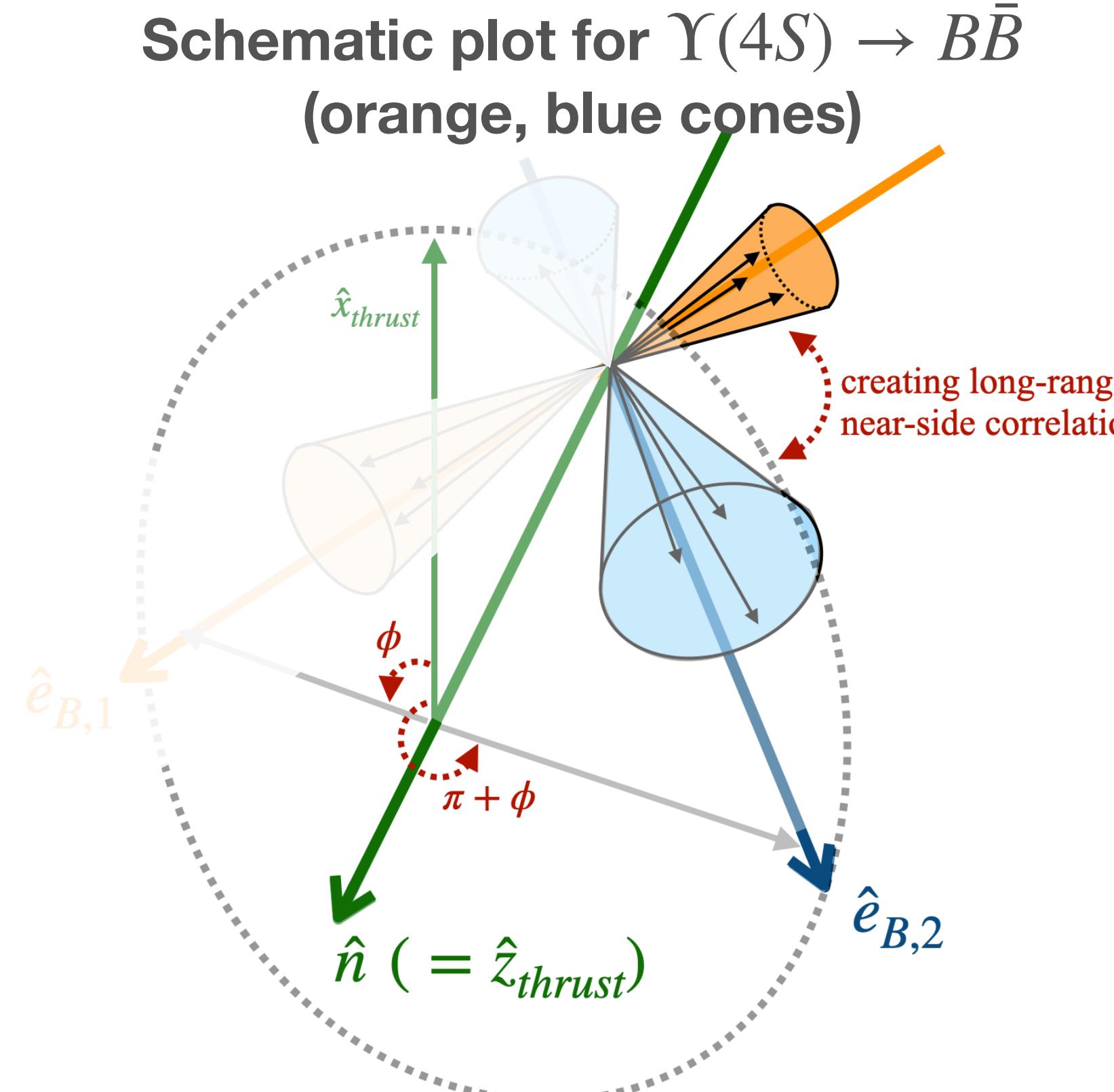


- Two B -meson decays:
special event topology
thrust axis alignment

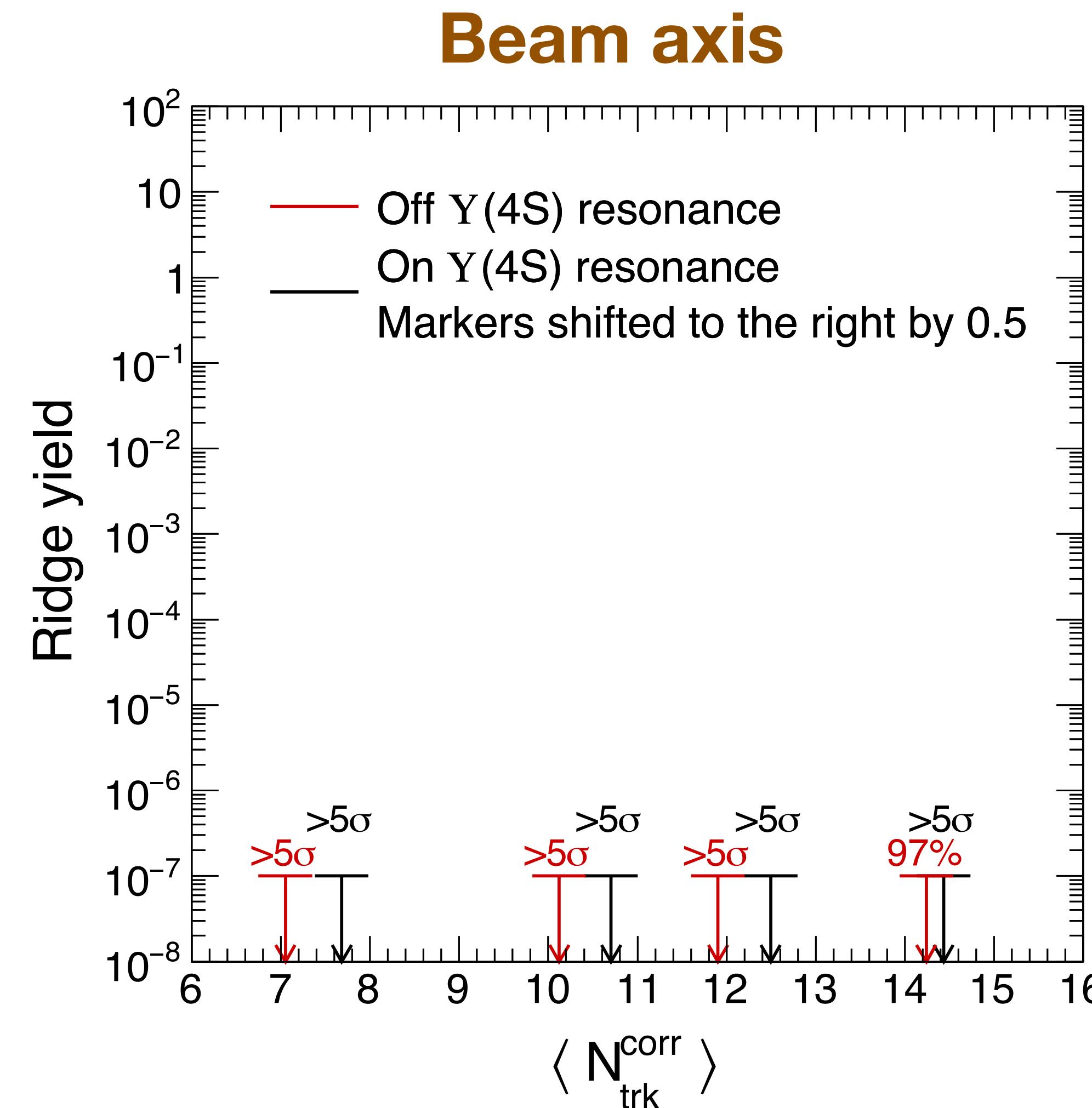




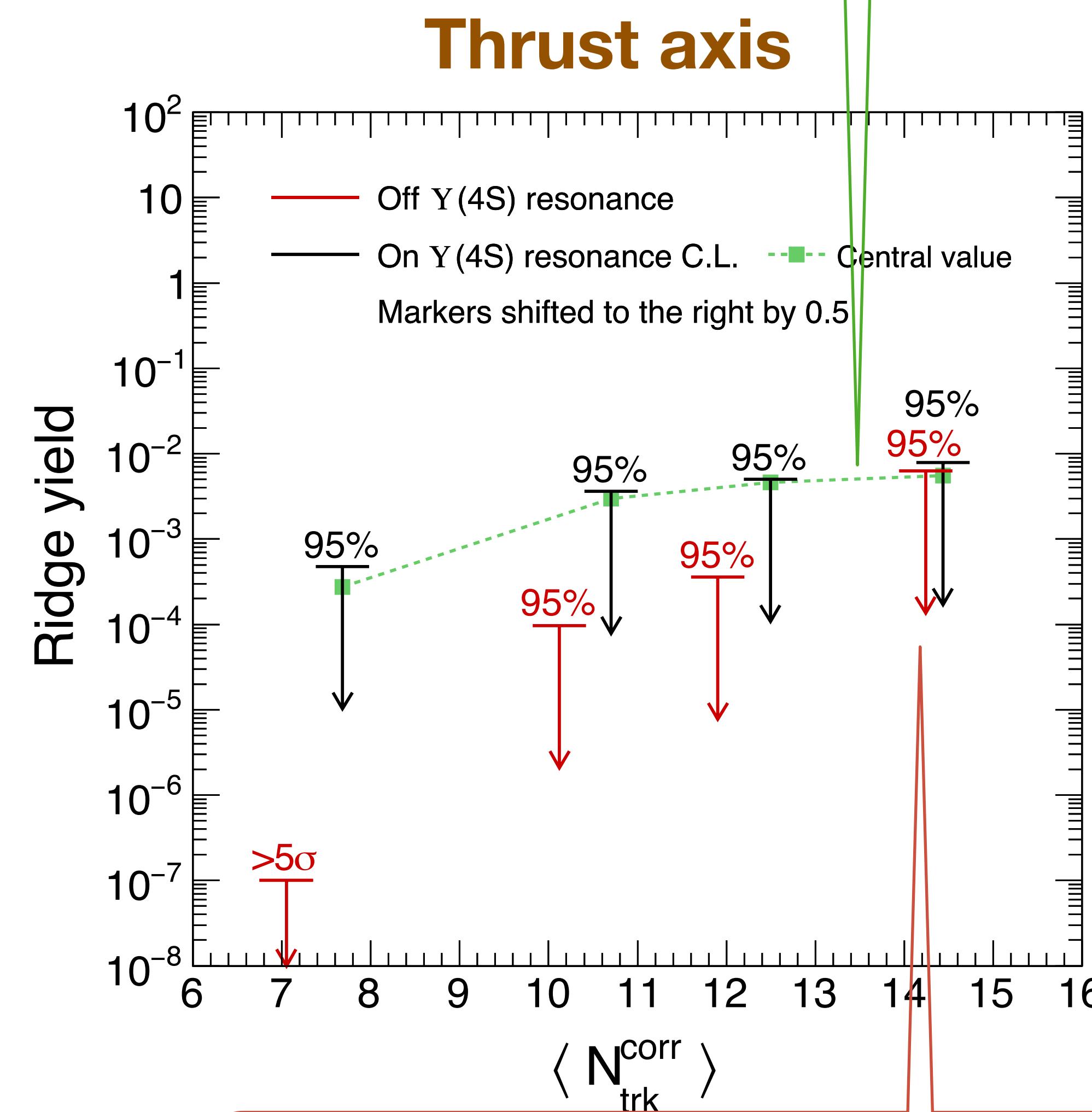
- Two B -meson decays: special event topology thrust axis alignment
- Toy sample pairing uncorrelated B 's from different events shows similar enhancement!



On-resonance:
Low-scale long-range enhancement



>5σ exclusion of ridge signal!

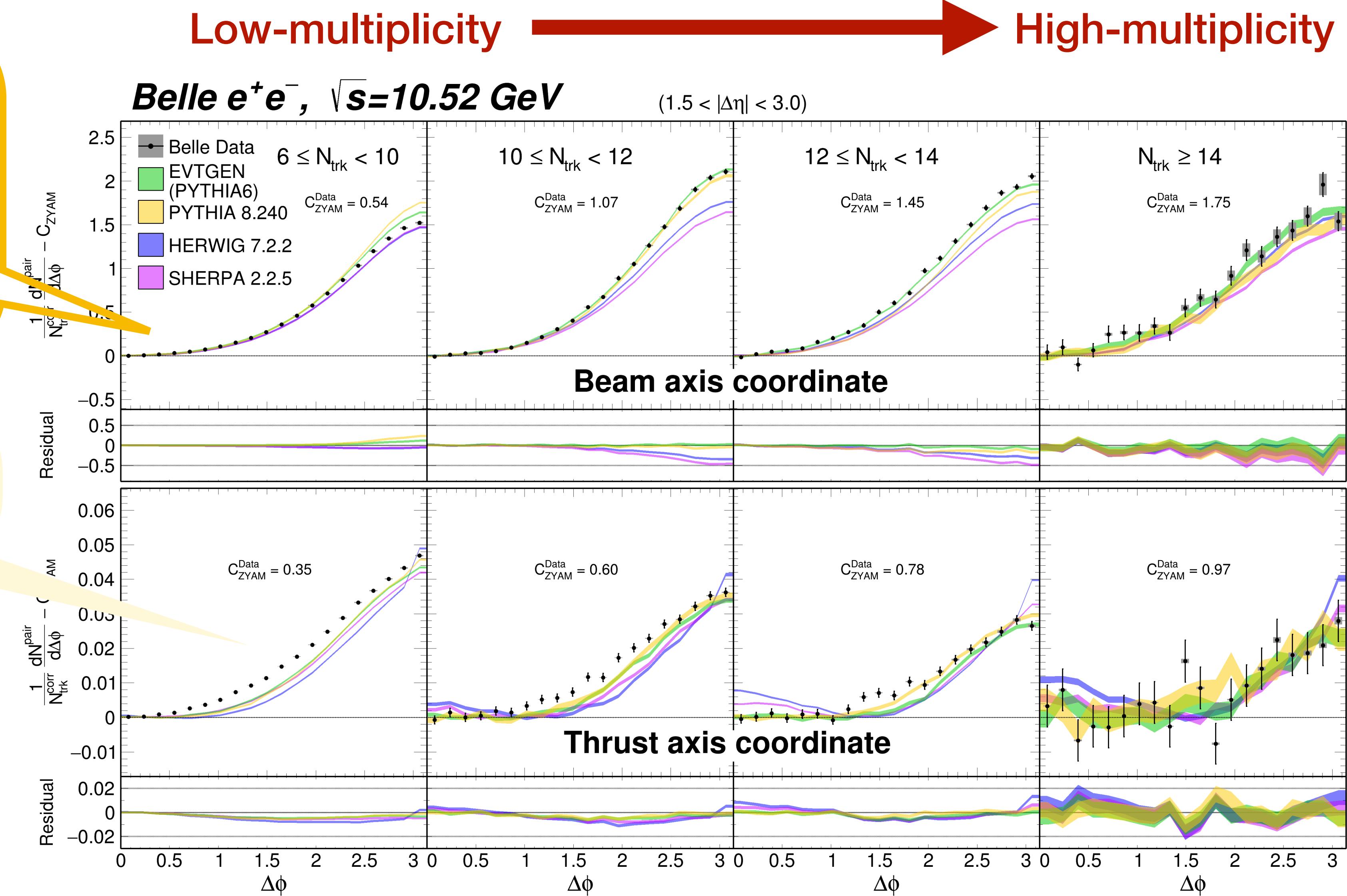


Off-resonance: No significant ridge signal
C.L. limited by statistics

- MCs consistent with data in near side
- Discrepancies in the away-side magnitude

Differences in data & MC correlation shapes

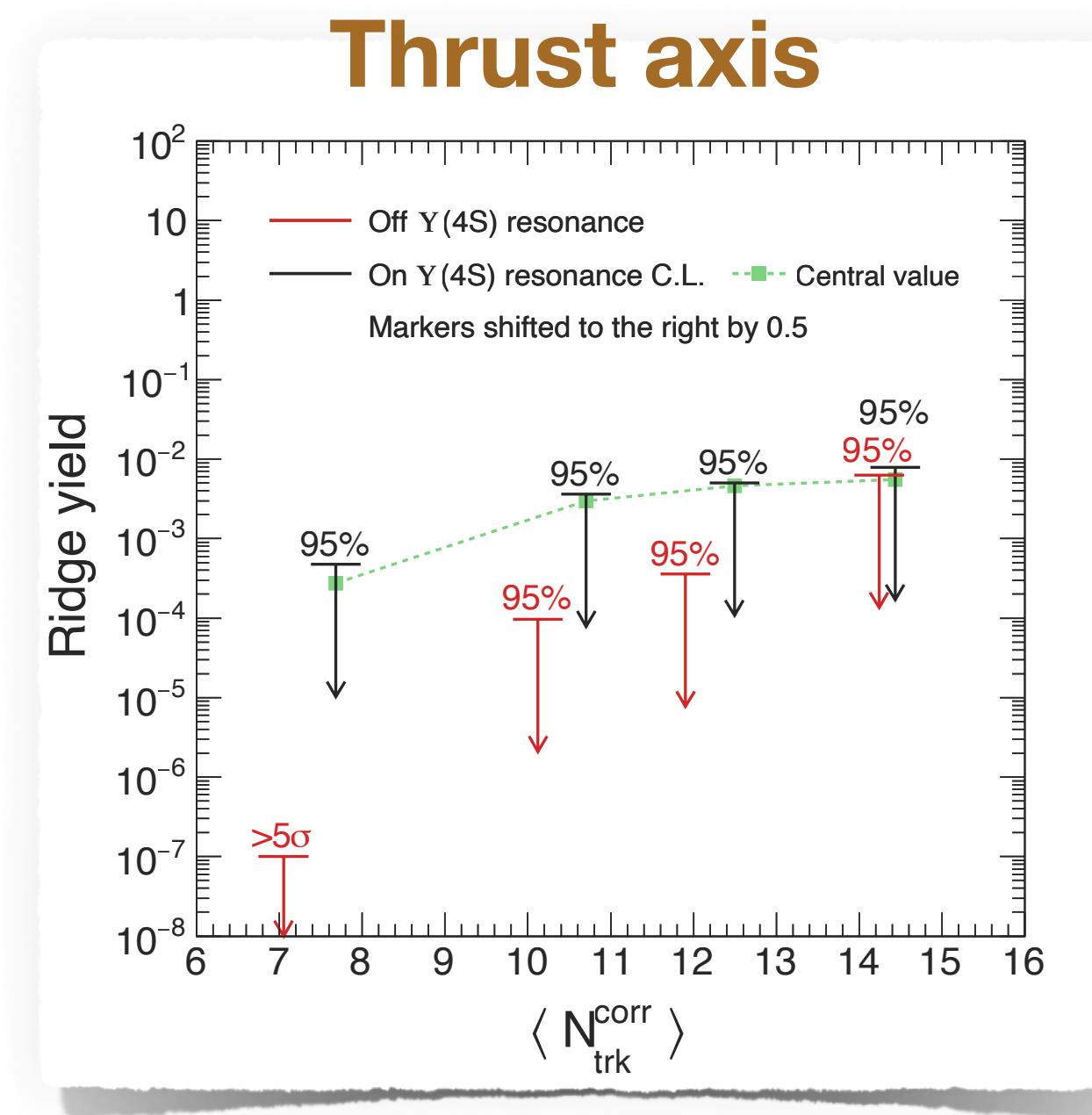
- PYTHIA6 agrees better with data than HERWIG & SHERPA
- PYTHIA8 has similar behavior as PYTHIA6



on-resonance see backup

e⁺e⁻ system & minimal condition

- Upper limits for exclusion of ridge-like signals



Exploring low-energy region (Thrust axis analysis)

- Off-resonance:
no significant ridge signal,
origin-peak jet correlation
scales with collision energy
- On-resonance:
low-scale long-range near-
side enhancement due to
special decay topology of
 $\Upsilon(4S) \rightarrow B\bar{B}$ system

Compared w/ event generators

- PYTHIA is in better
agreement with data
than SHERPA &
HERWIG

MITHIG group's work was supported by US DOE-NP



Backup



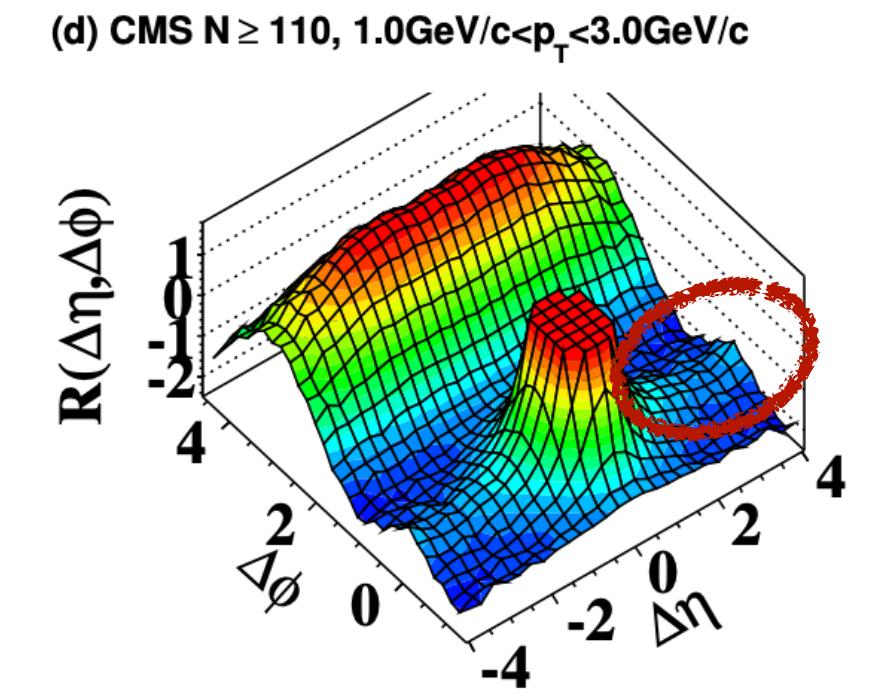
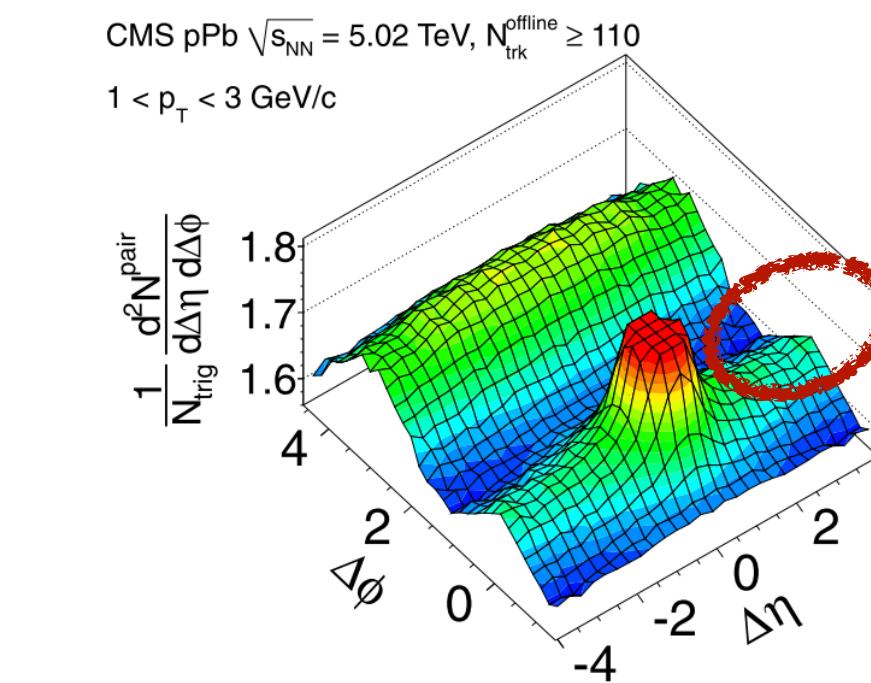
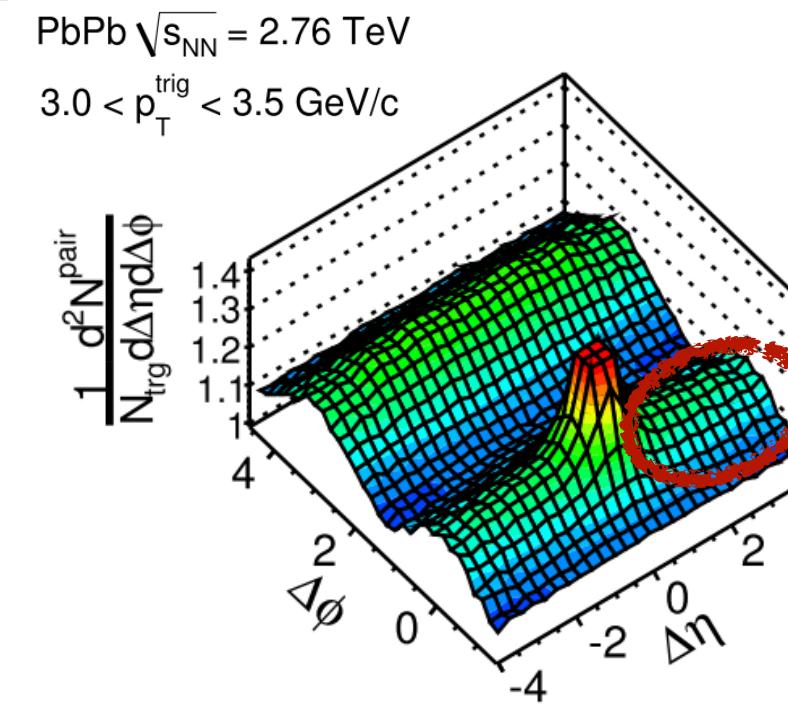
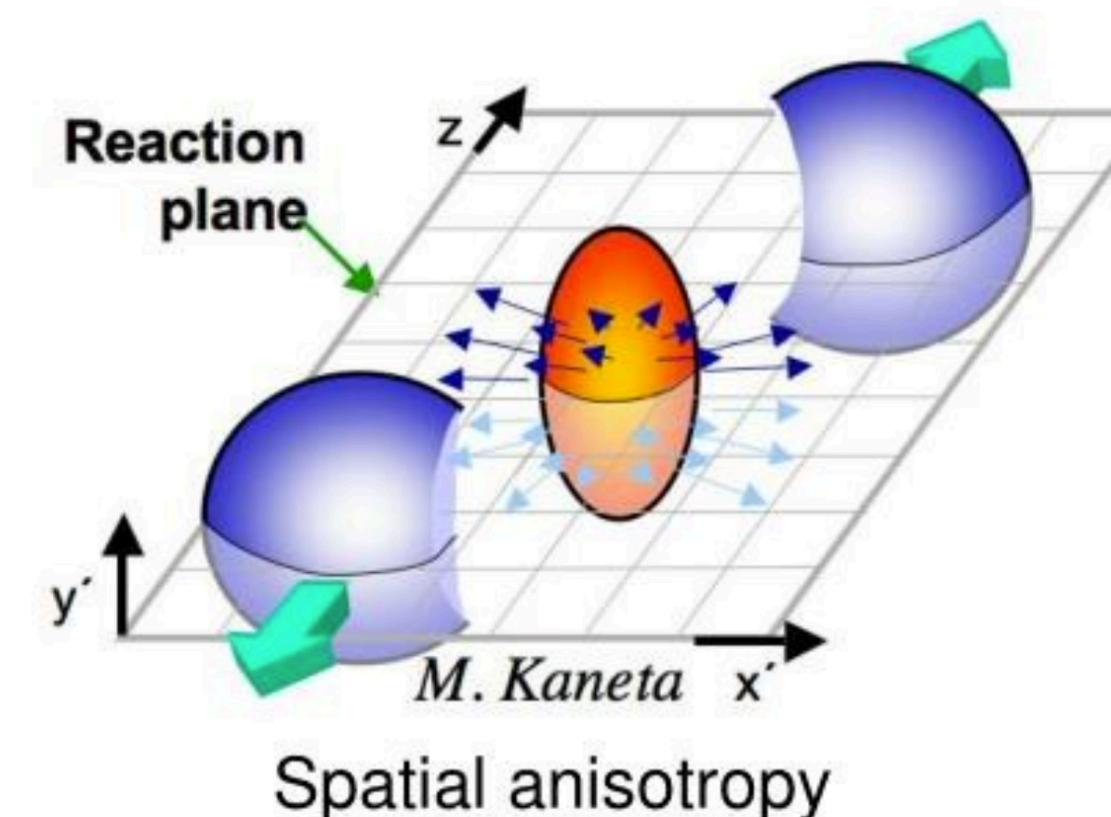
Yu-Chen (Janice) Chen

ICHEP 2022



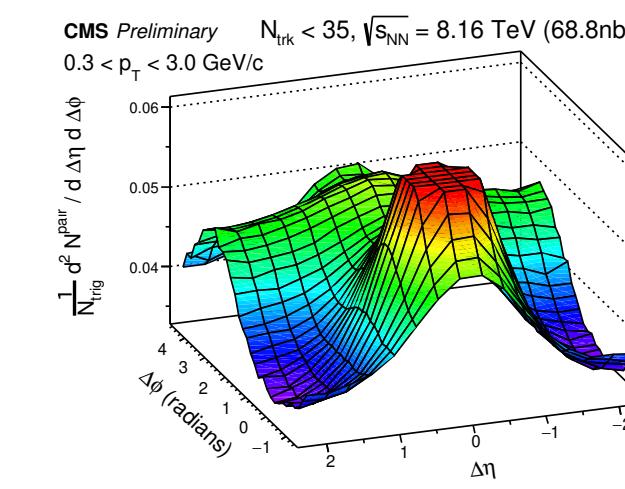
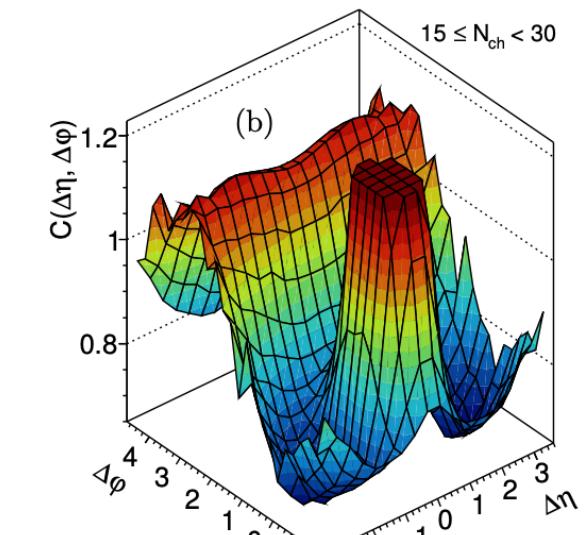
- Collectivity signal

Two-particle correlation: soft probe for Quark-Gluon Plasma (QGP) in heavy ion collisions



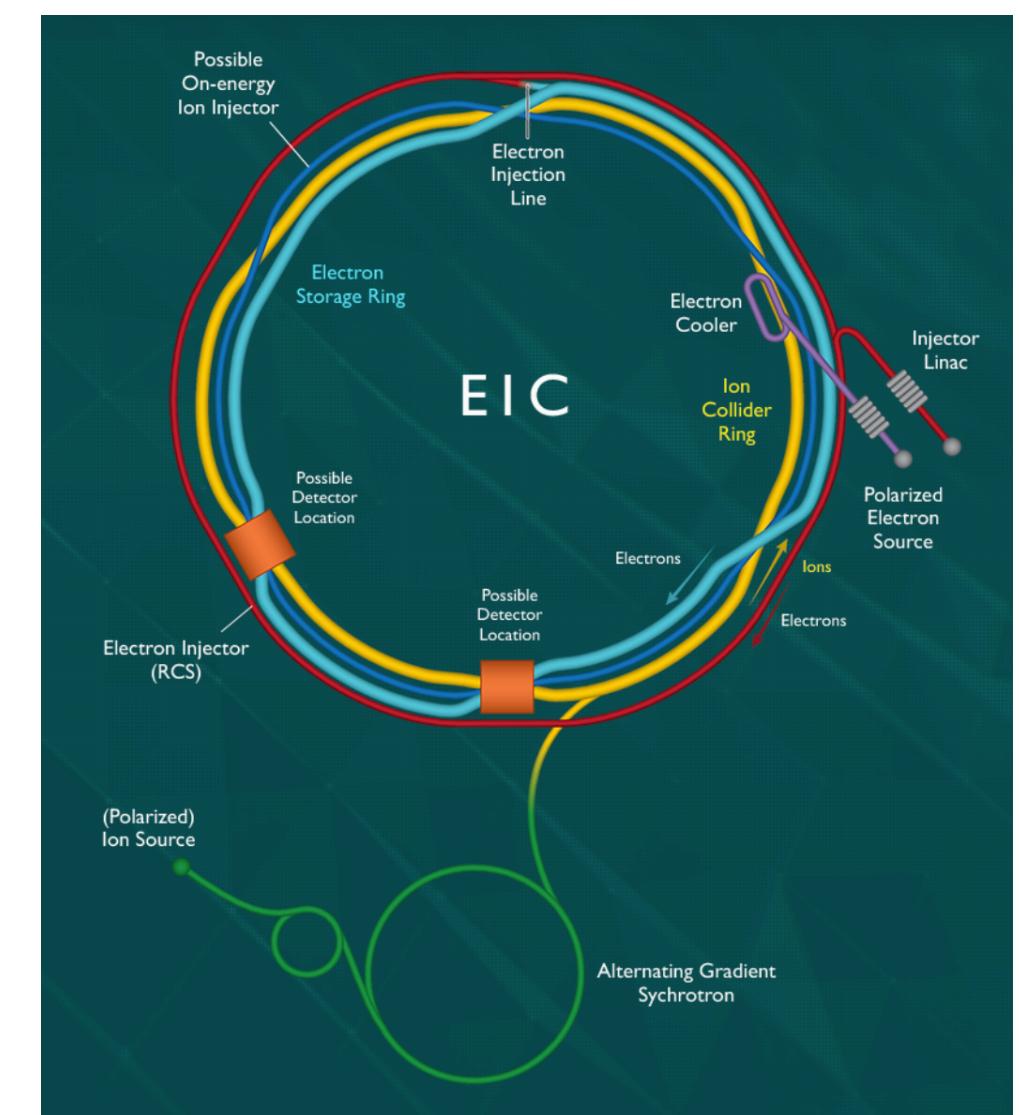
- Minimal conditions for collectivity behavior [\[nucl-th:1707.02307\]](#)

Smaller collision systems such as ep, e⁺e⁻, γp, γA, to the future EIC!

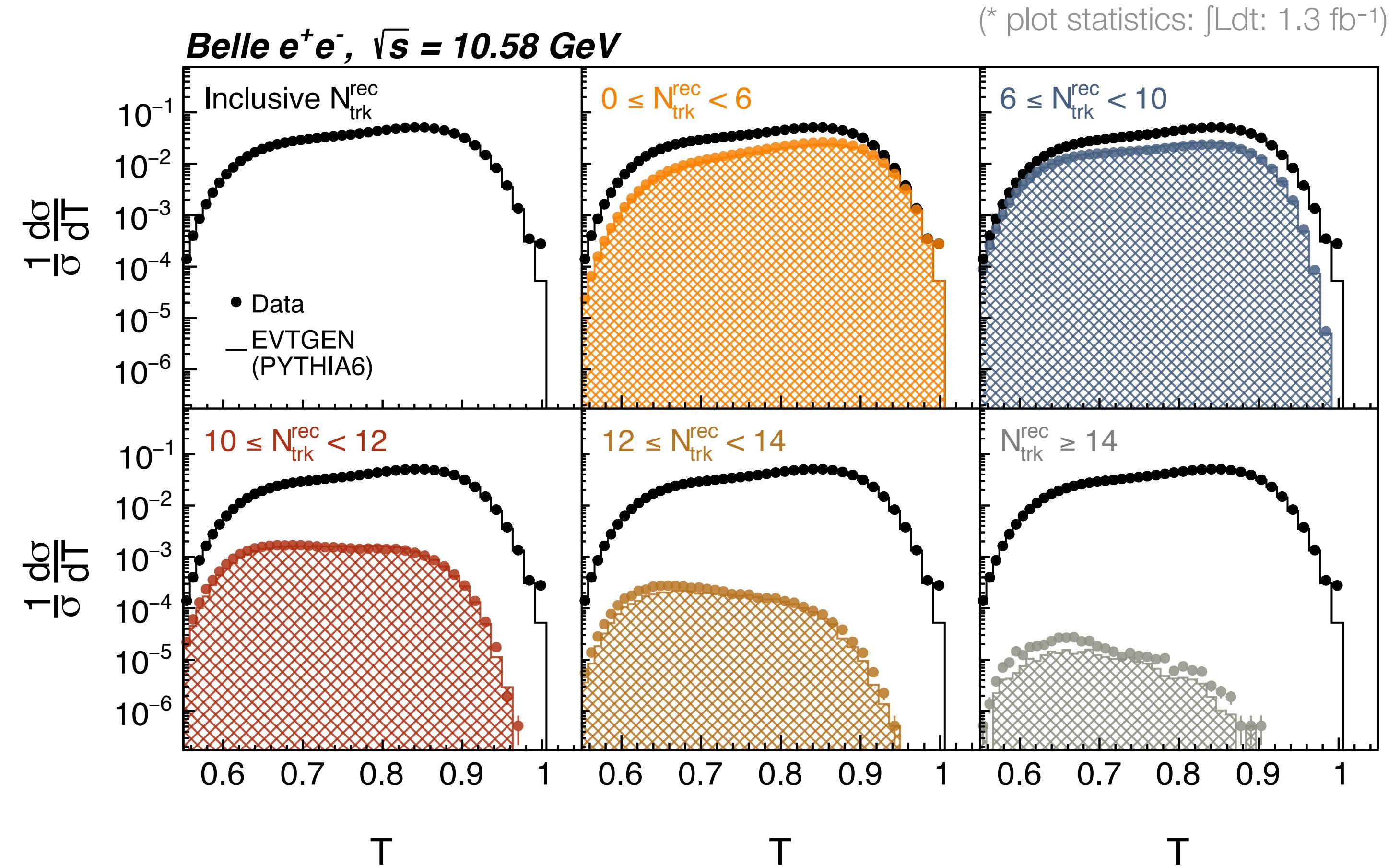
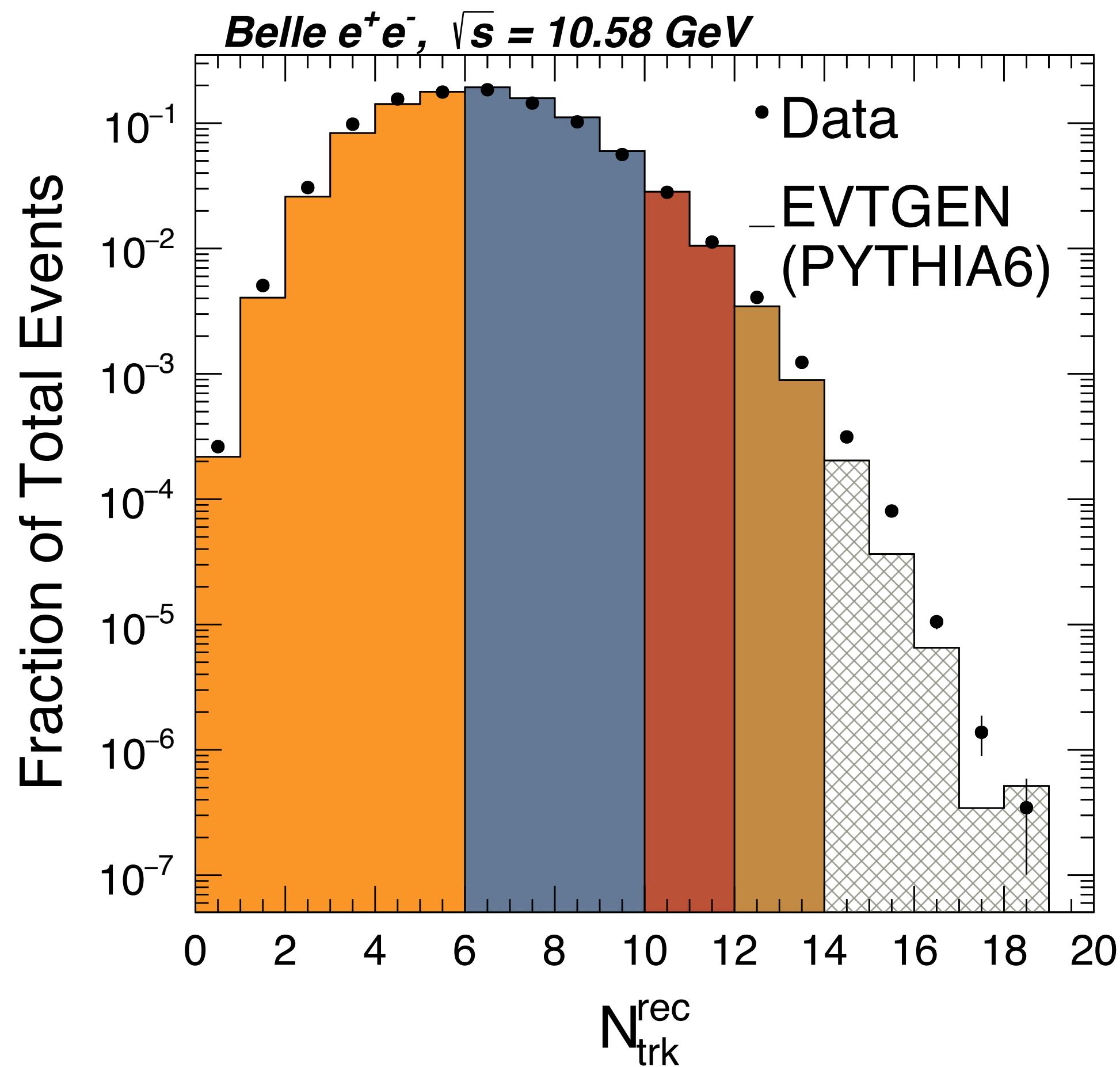


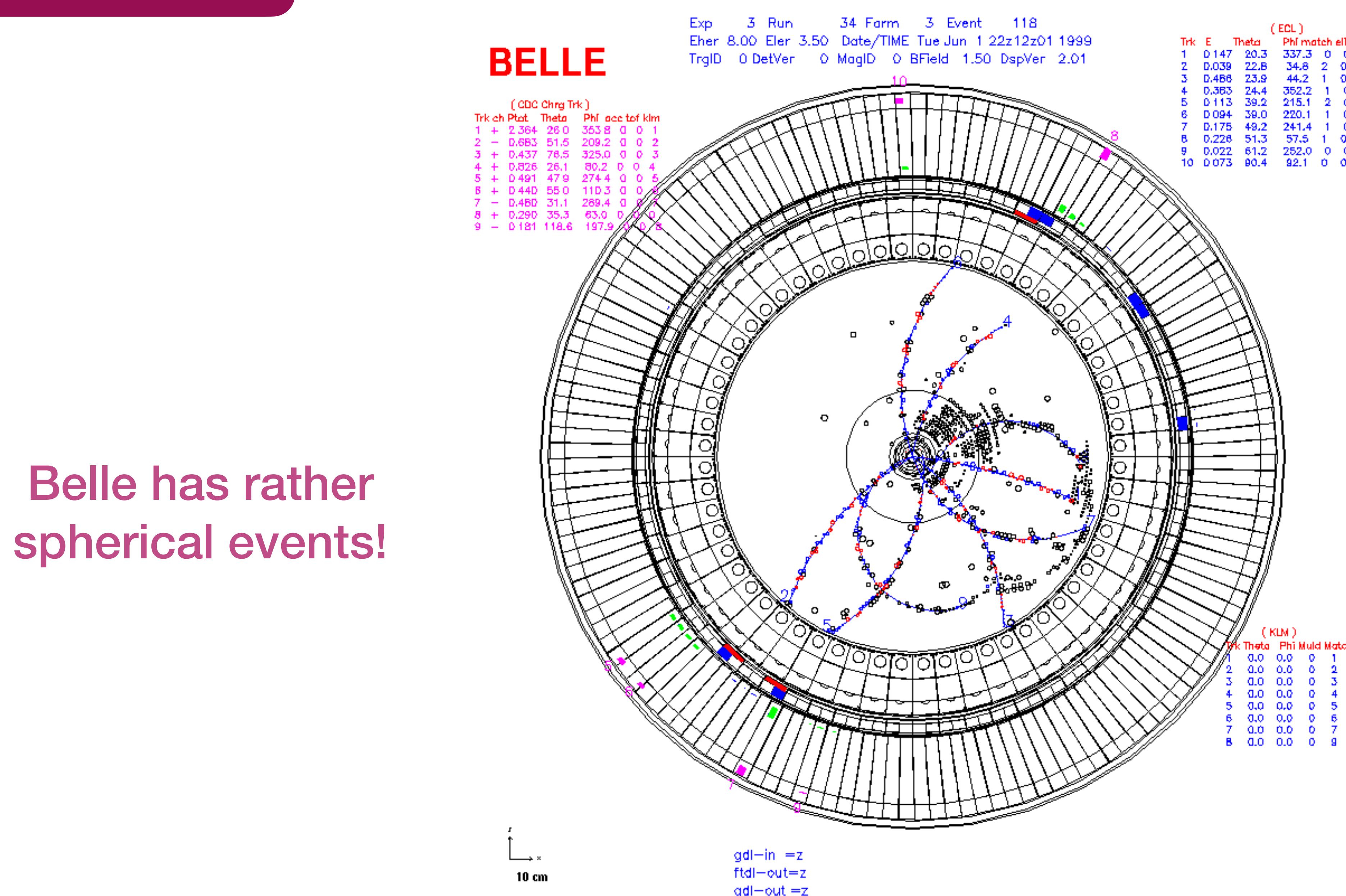
ALEPH e⁺e⁻ [\[Phys. Rev. Lett. 123, 212002 \(2019\)\]](#)

ATLAS γA [\[Phys. Rev. C. 104, 014903\]](#)



Charged particles	
Primary tracks	<ul style="list-style-type: none"> [reconstructed] the distance in the transverse plane of the decay vertex from the primary vertex $< 1 \text{ cm}$ [MC-truth] decay promptly or from particles with proper lifetime $\tau \leq 1 \text{ cm}/c$
Acceptance	$17^\circ \leq \theta \leq 150^\circ$
High quality tracks	$p_T \geq 0.2 \text{ GeV}$
Impact parameter	$ \Delta r < 2, \Delta z < 5$
Duplicate track removal	veto the softer track of a low-momentum pair ($p_T < 0.4 \text{ GeV}$) travelling with a small open angle δ : <ol style="list-style-type: none"> same-sign charges with $\cos \delta > 0.95$ opposite-sign charges with $\cos \delta < -0.95$
Photon conversion veto	veto track pairs which can form common vertices (V^0 objects) with <ol style="list-style-type: none"> z distance between two tracks $< 10 \text{ cm}$ reconstructed V^0's mass $< 0.25 \text{ GeV}$ decay-vertex radius $> 1.5 \text{ cm}$
Neutral particles (for thrust calculation)	
Cluster selection	No direct track-matching and tracks matched at cluster edges
Acceptance	$17^\circ \leq \theta \leq 150^\circ$
Energy cut	Forward endcap: $E < 0.10 \text{ GeV}$ Backward endcap: $E < 0.15 \text{ GeV}$ Barrel: $E < 0.05 \text{ GeV}$





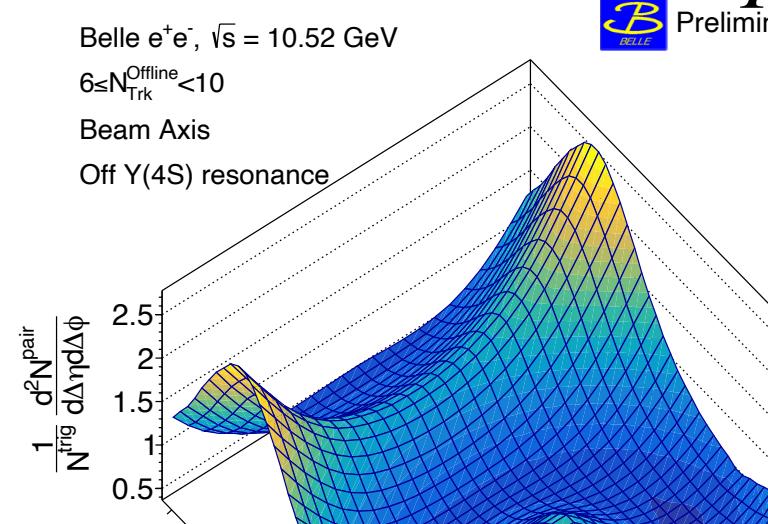
Belle has rather spherical events!

**Two-particle correlation function
(per-trigger-particle
associated yield)**

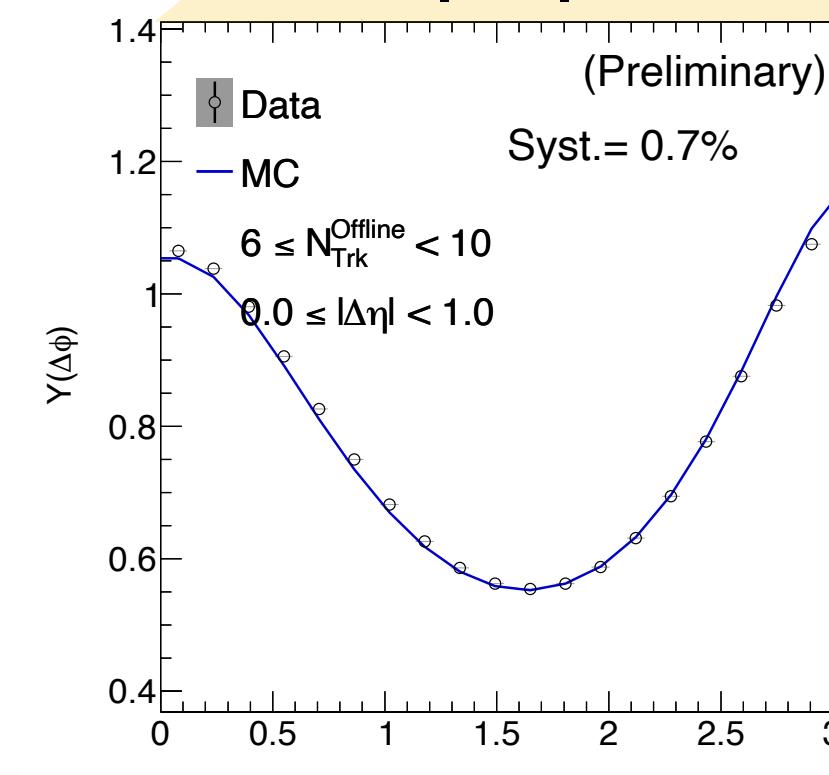
$$\frac{1}{N_{\text{trig}}} \frac{d^2 N^{\text{pair}}}{d\Delta\eta d\Delta\phi}$$

Associated yield vs. $\Delta\phi$

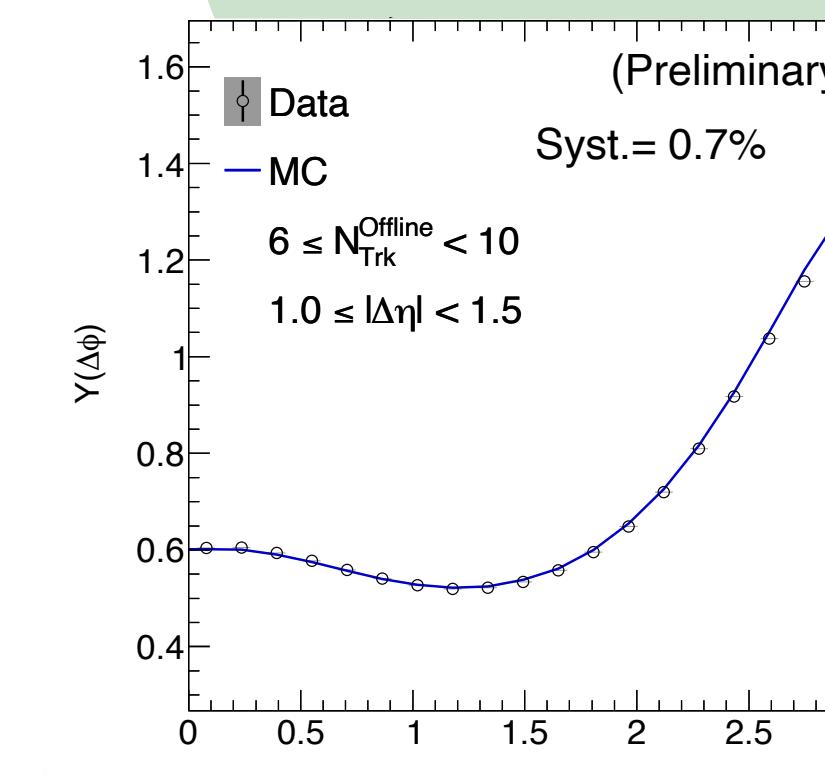
$$Y(\Delta\phi) = \frac{1}{N_{\text{trig}}} \frac{dN^{\text{pair}}}{d\Delta\phi} = \frac{1}{\Delta\eta_{\text{max}} - \Delta\eta_{\text{min}}} \int_{\Delta\eta_{\text{min}}}^{\Delta\eta_{\text{max}}} \frac{1}{N_{\text{trig}}} \frac{d^2 N^{\text{pair}}}{d\Delta\eta d\Delta\phi} d\Delta\eta$$



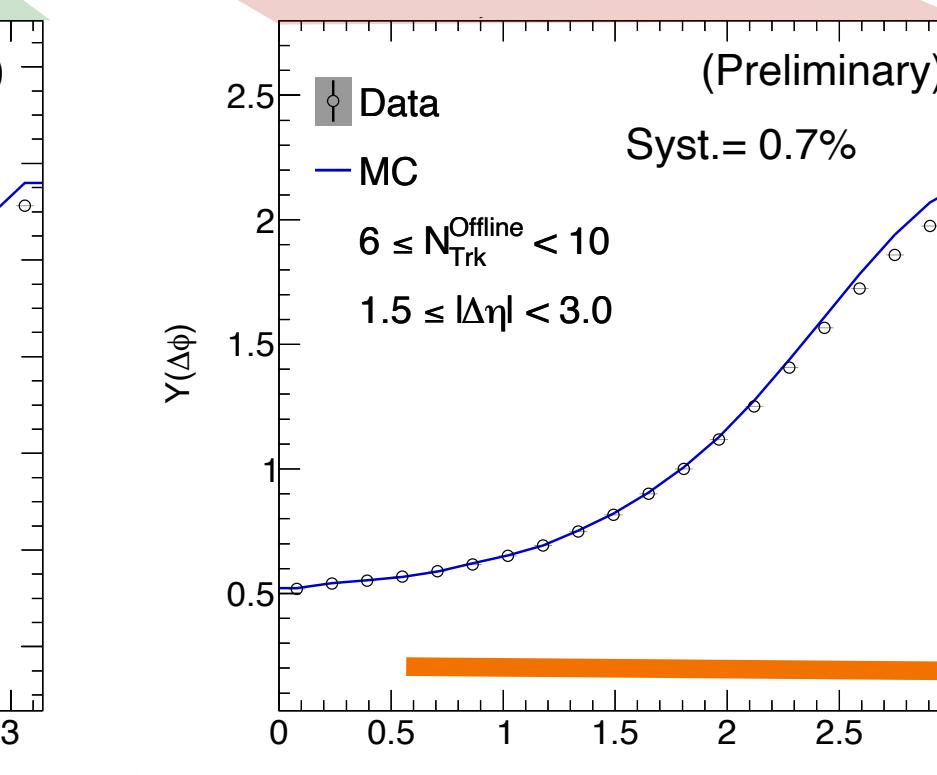
**Short Range
($0 \leq |\Delta\eta| < 1$)**



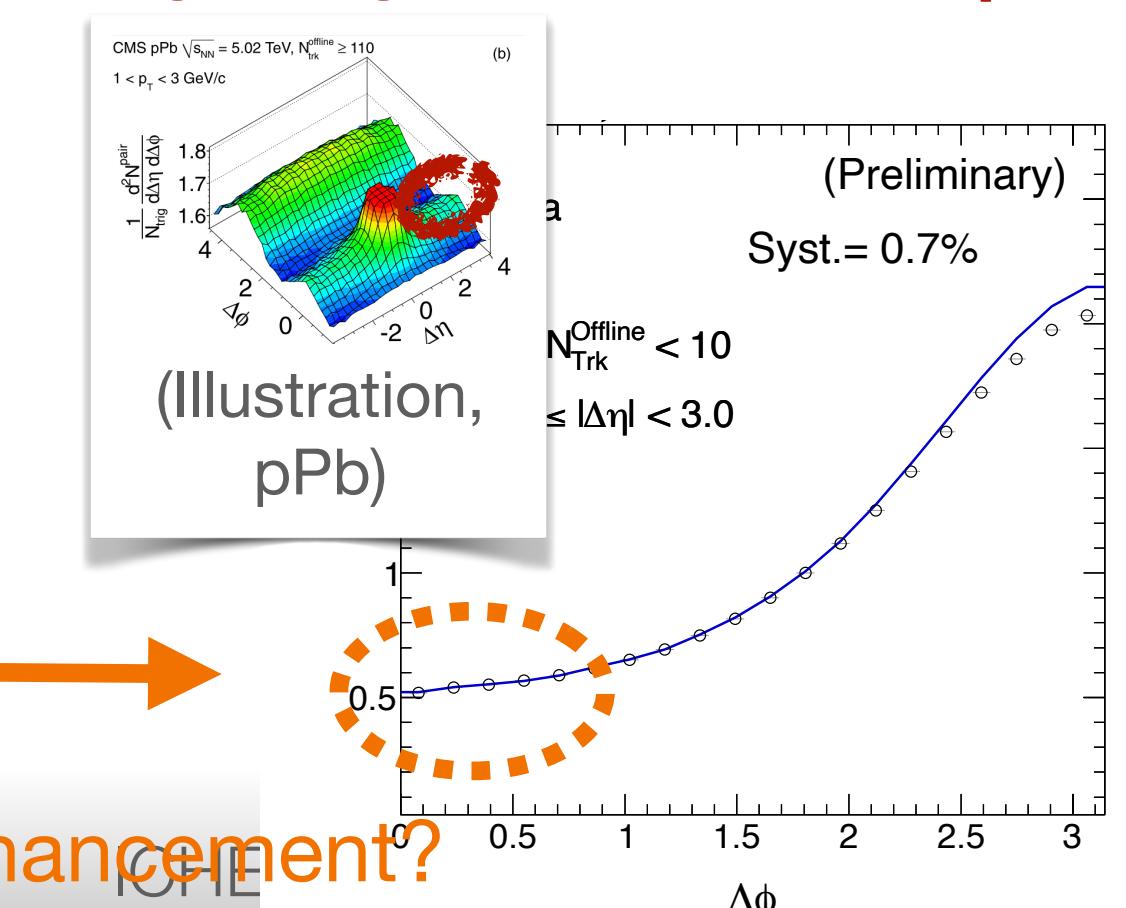
**Middle Range
($1 \leq |\Delta\eta| < 1.5$)**



**Long Range
($1.5 \leq |\Delta\eta| < 3.0$)**



**Ridge Signal
(long-range, near-side ($\Delta\phi \sim 0$))**

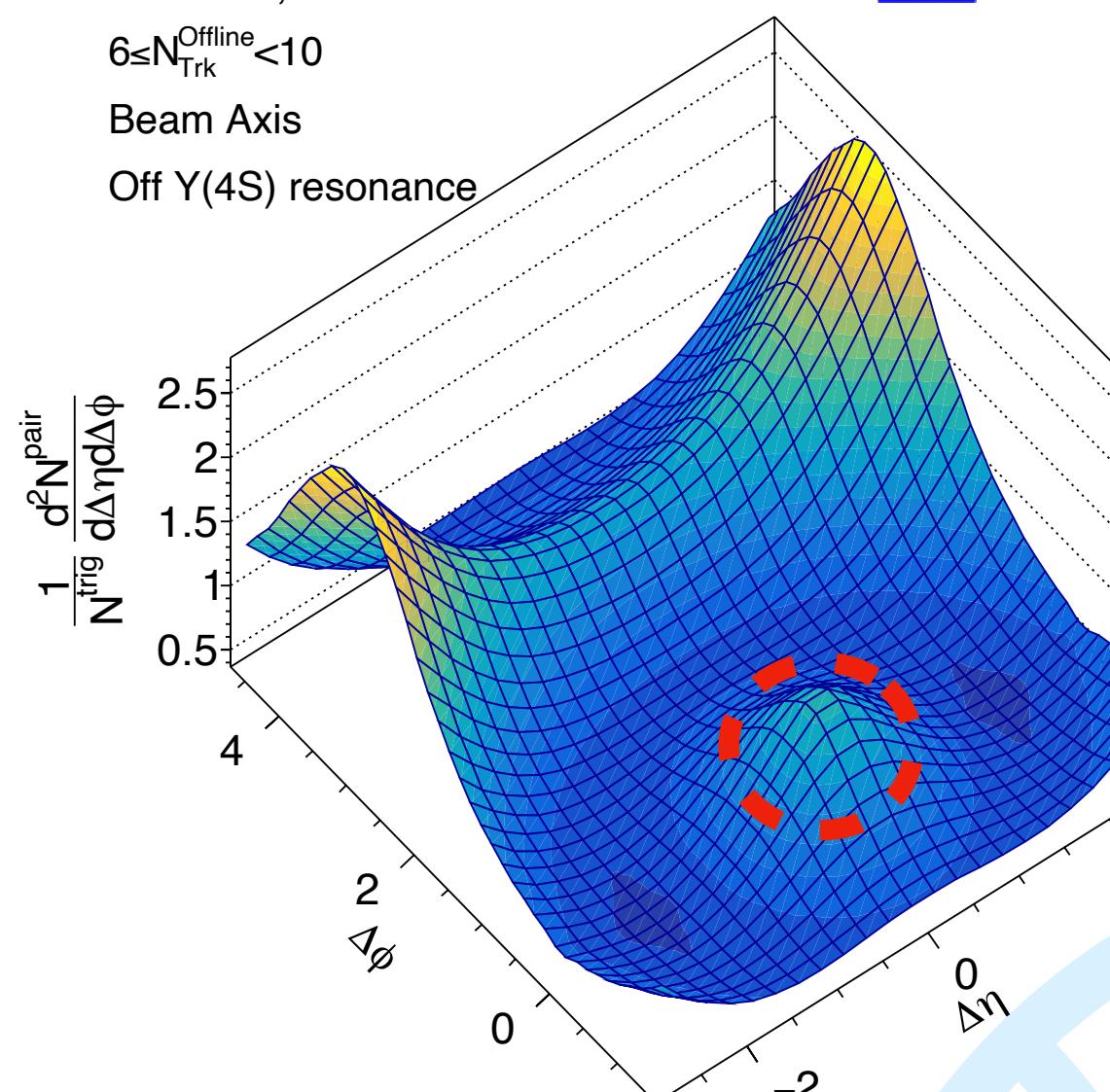


**Two-particle correlation function
(per-trigger-particle
associated yield)**

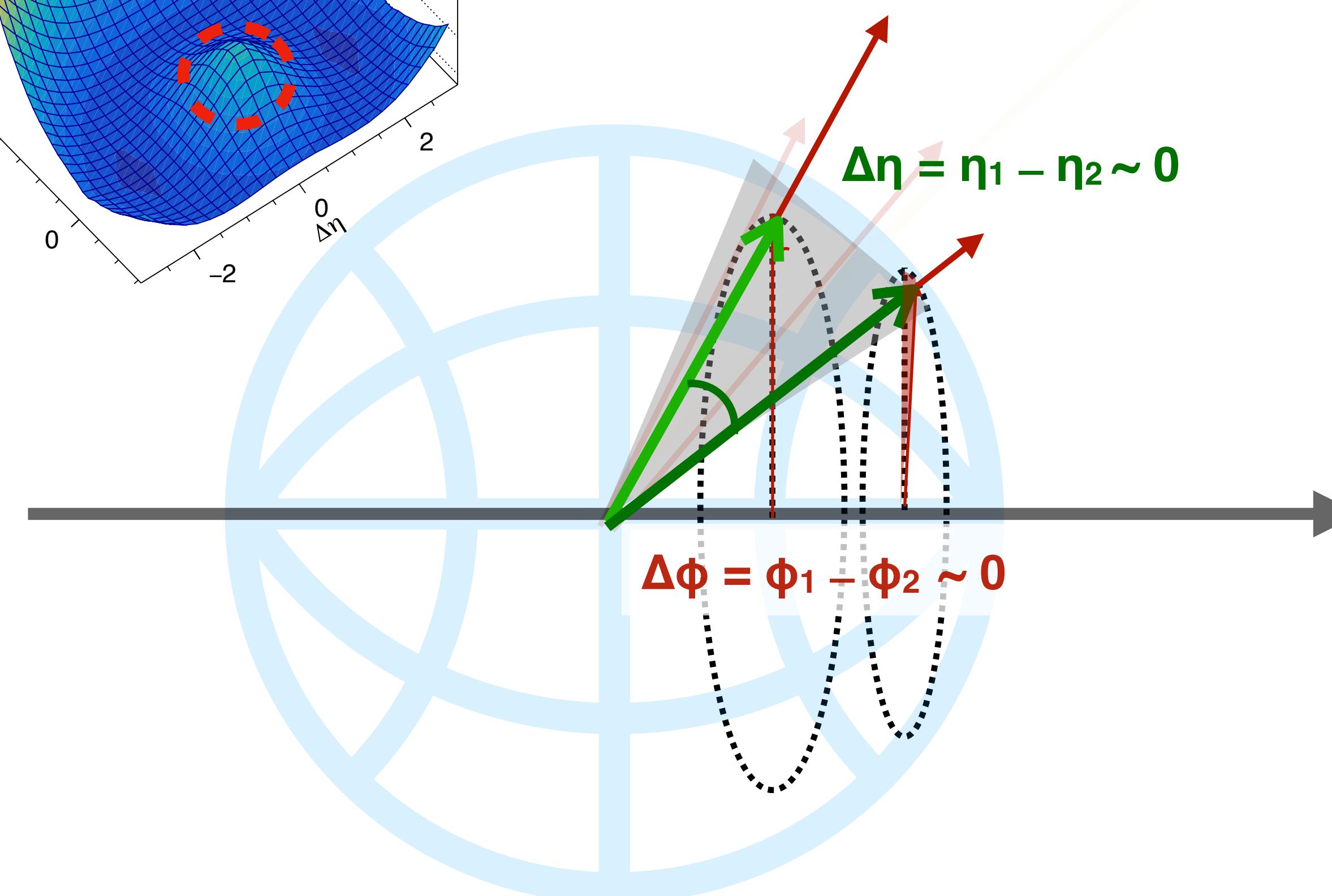
$$\frac{1}{N_{\text{trig}}} \frac{d^2N^{\text{pair}}}{d\Delta\eta d\Delta\phi}$$

Belle e^+e^- , $\sqrt{s} = 10.52$ GeV
 $6 \leq N_{\text{Trk}}^{\text{Offline}} < 10$
Beam Axis
Off $\Upsilon(4S)$ resonance

 Preliminary

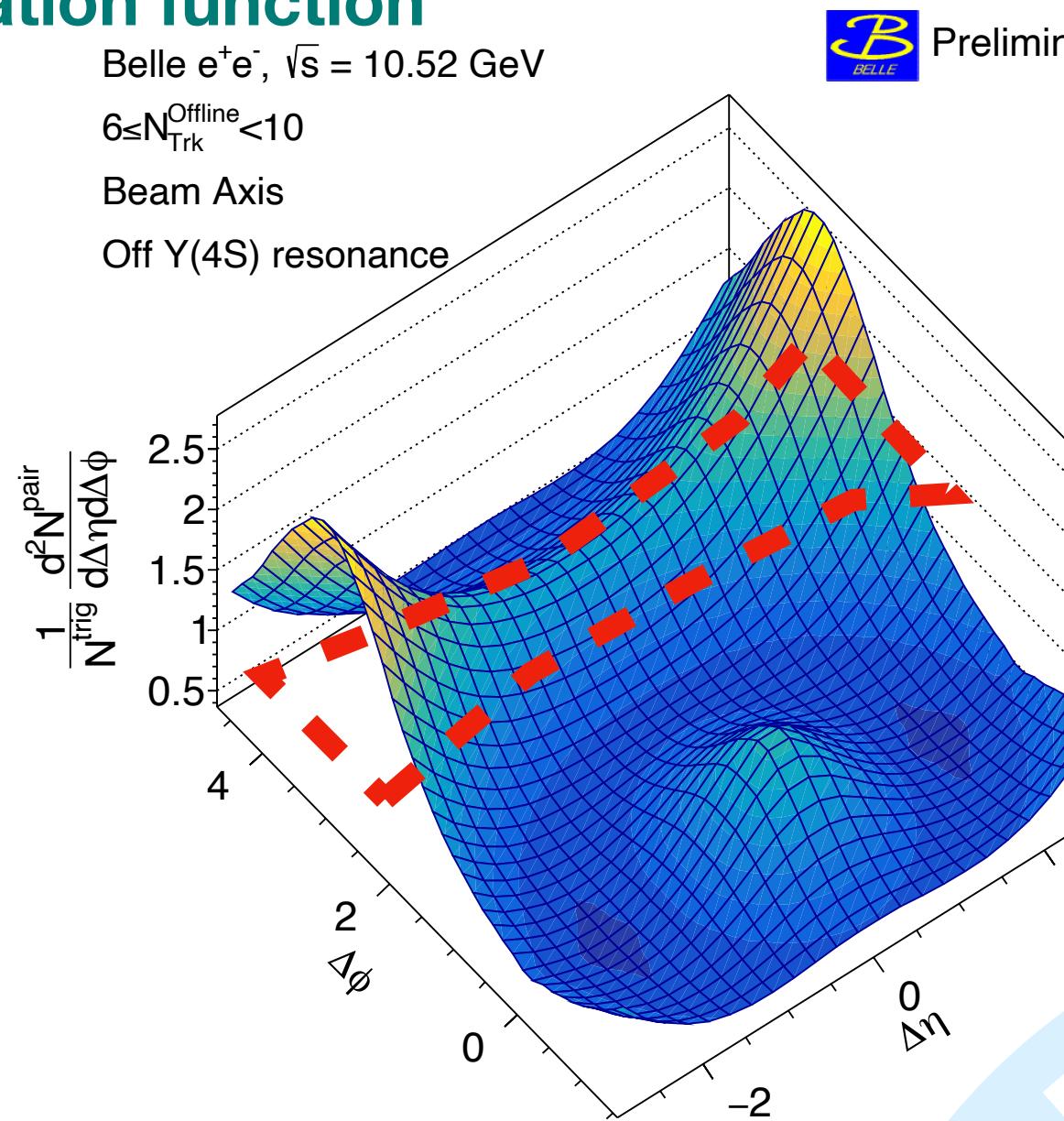


**Origin-peak intra-jet correlations
@ near side $(\Delta\eta, \Delta\phi) \sim (0,0)$**

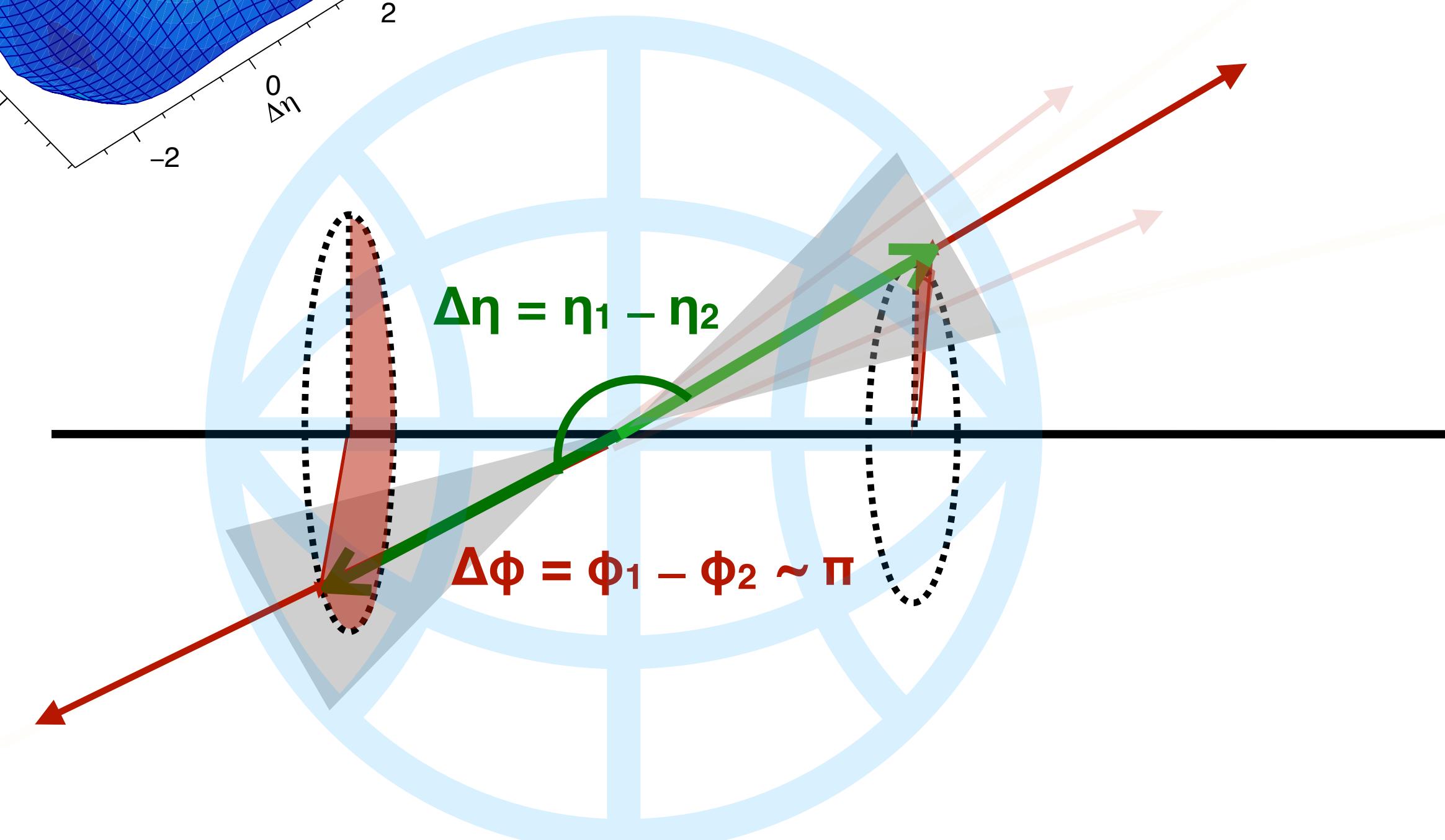


**Two-particle correlation function
(per-trigger-particle
associated yield)**

$$\frac{1}{N_{\text{trig}}} \frac{d^2N^{\text{pair}}}{d\Delta\eta d\Delta\phi}$$

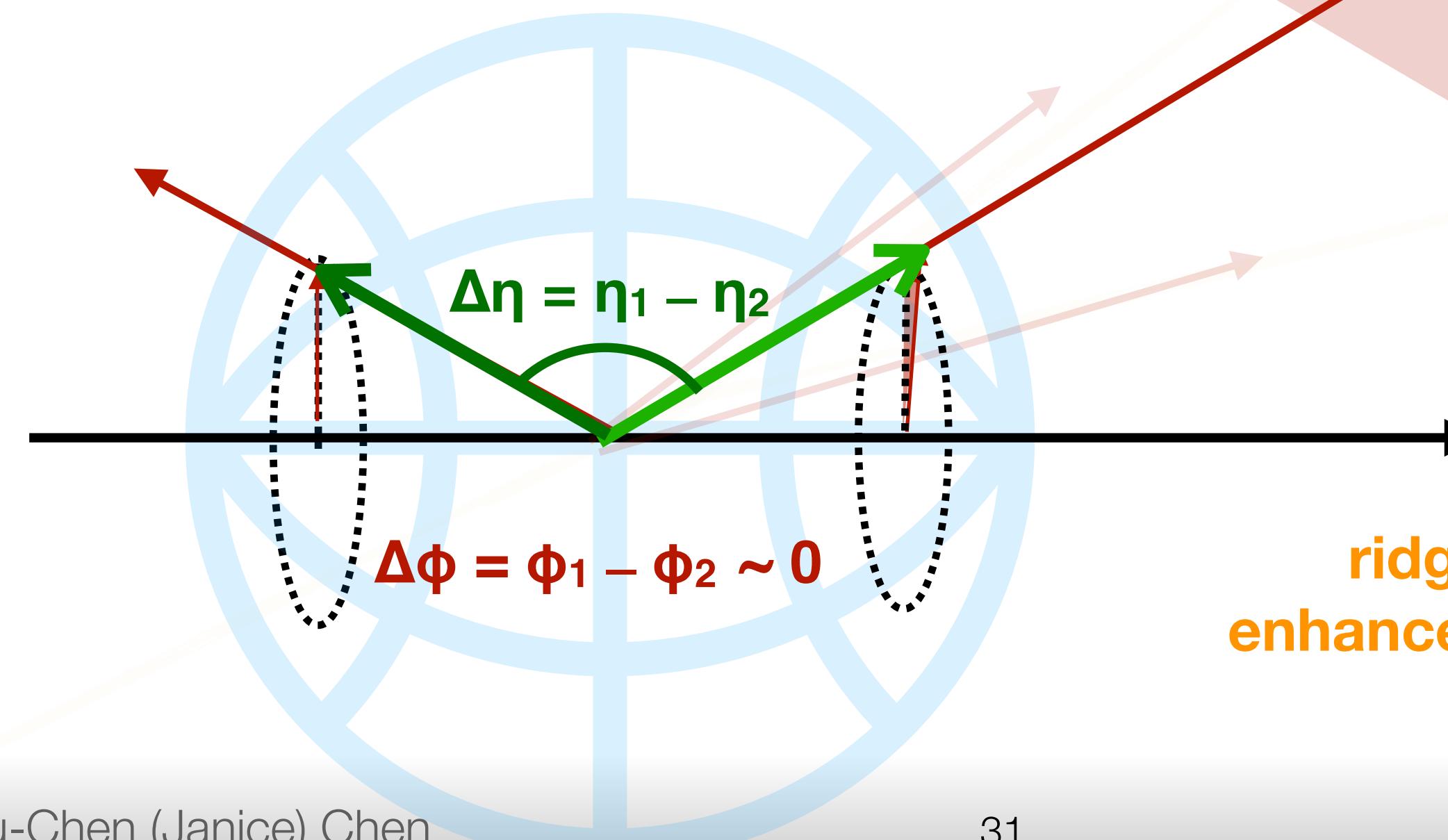
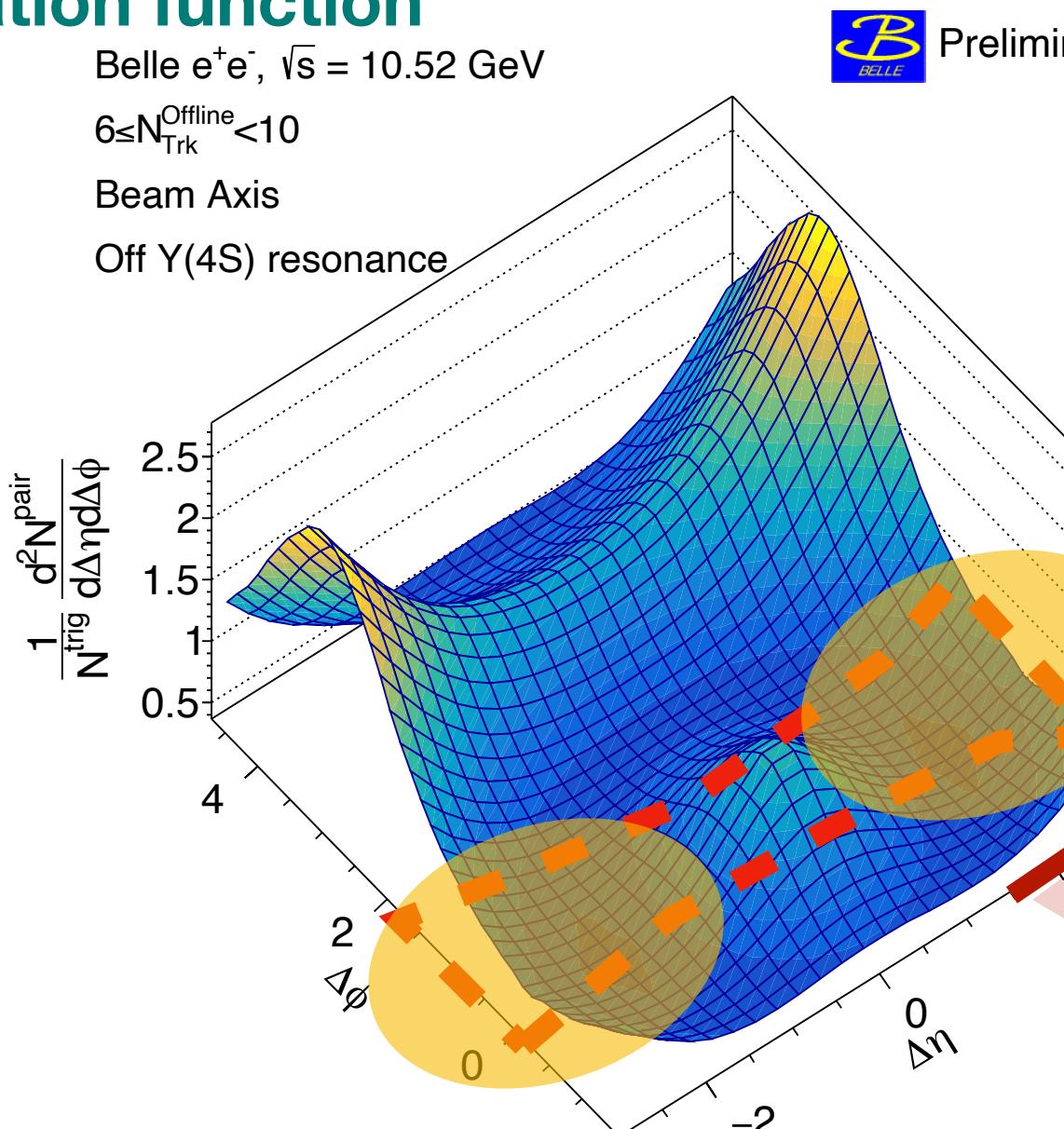


**Back-to-back jet correlations
@ away side ($\Delta\phi \sim \pi$)**

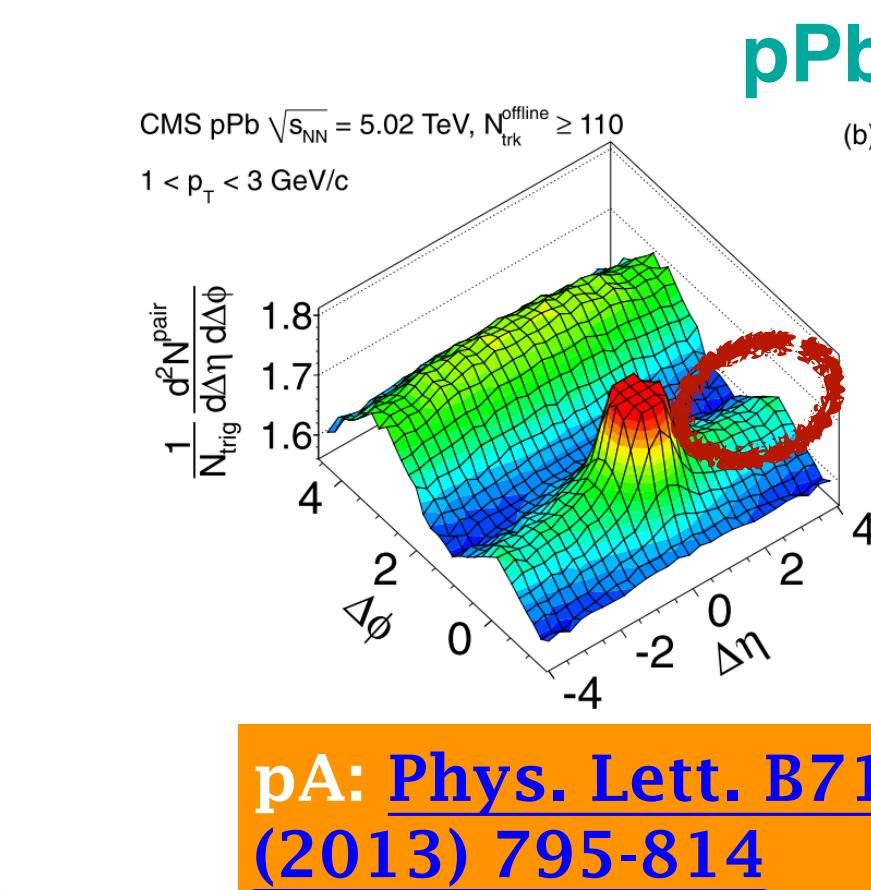


**Two-particle correlation function
(per-trigger-particle
associated yield)**

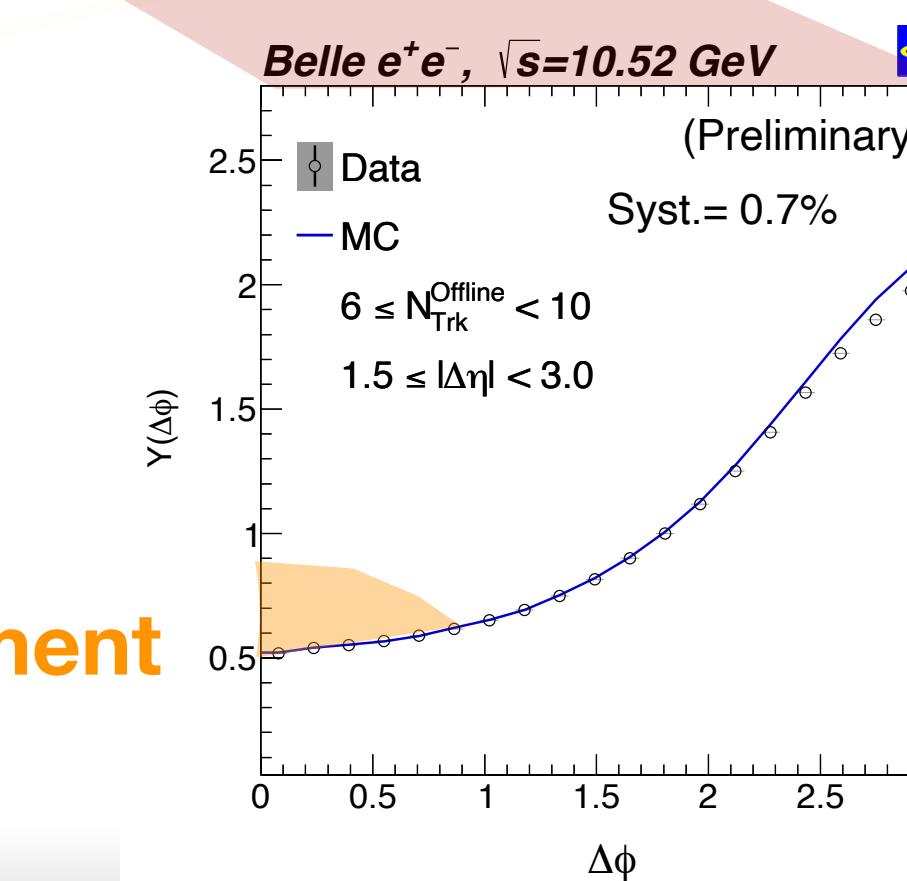
$$\frac{1}{N_{\text{trig}}} \frac{d^2N^{\text{pair}}}{d\Delta\eta d\Delta\phi}$$

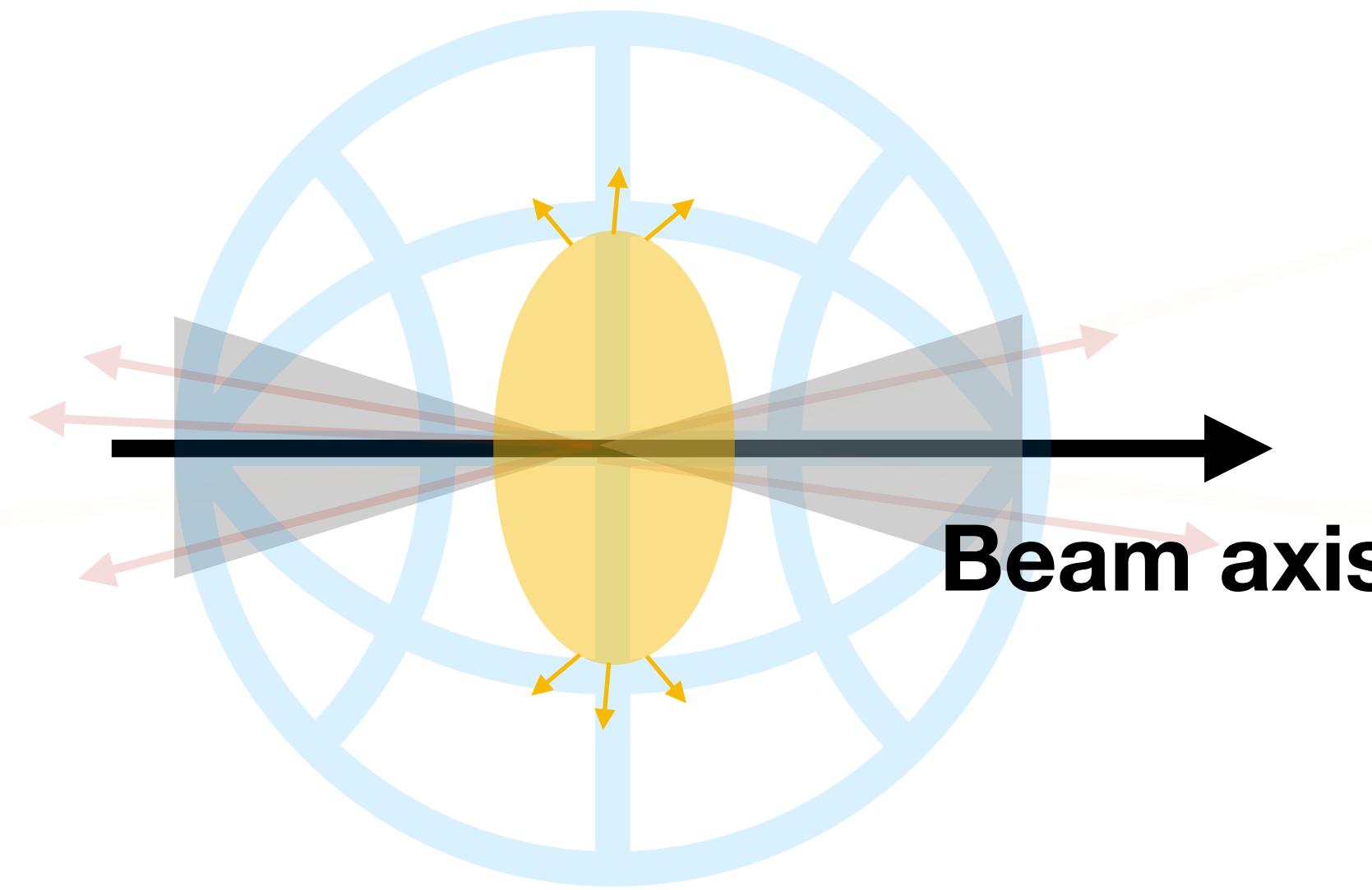


**Ridge correlations
@ long range, near side**



pA: [Phys. Lett. B718 \(2013\) 795-814](#)

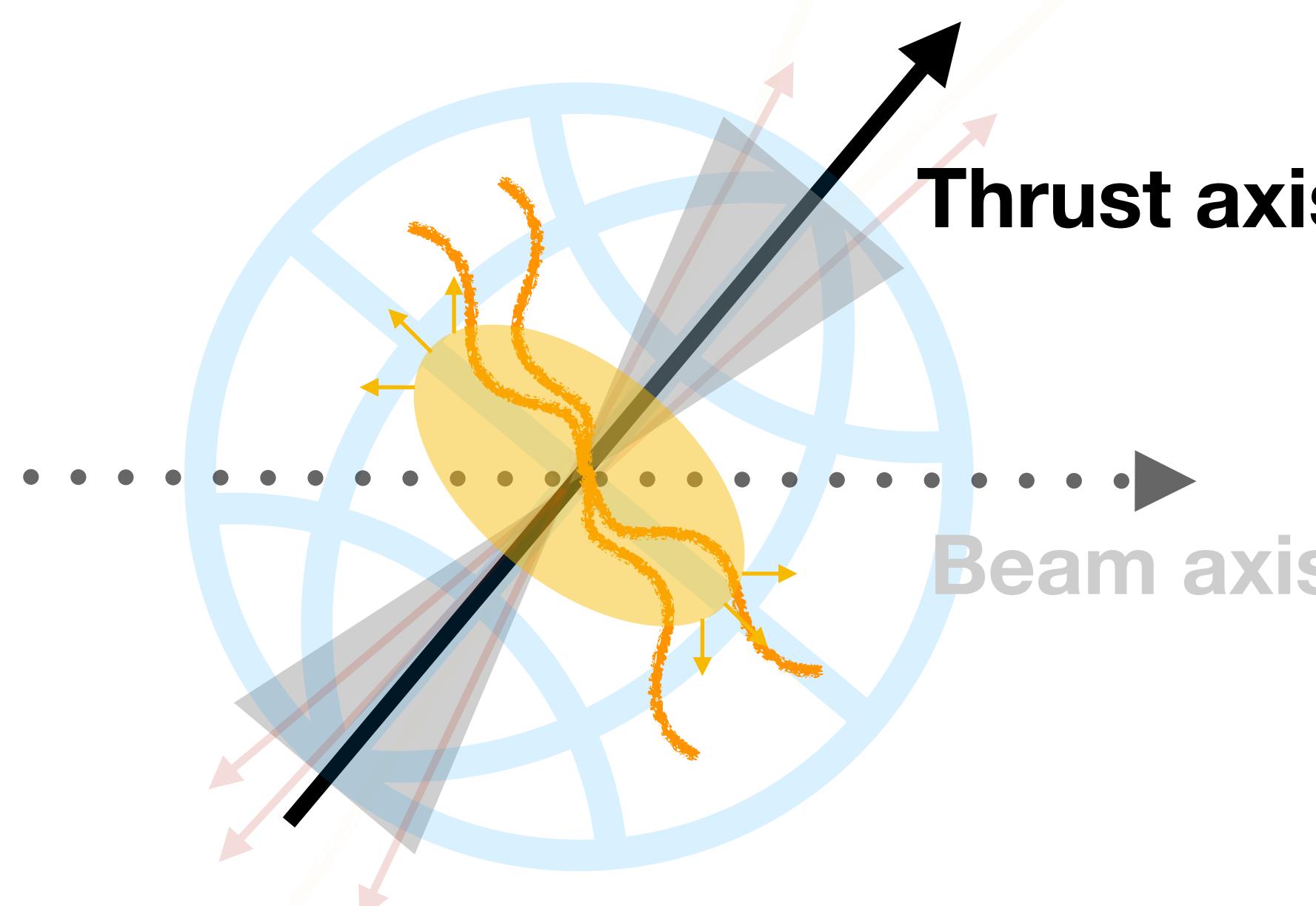
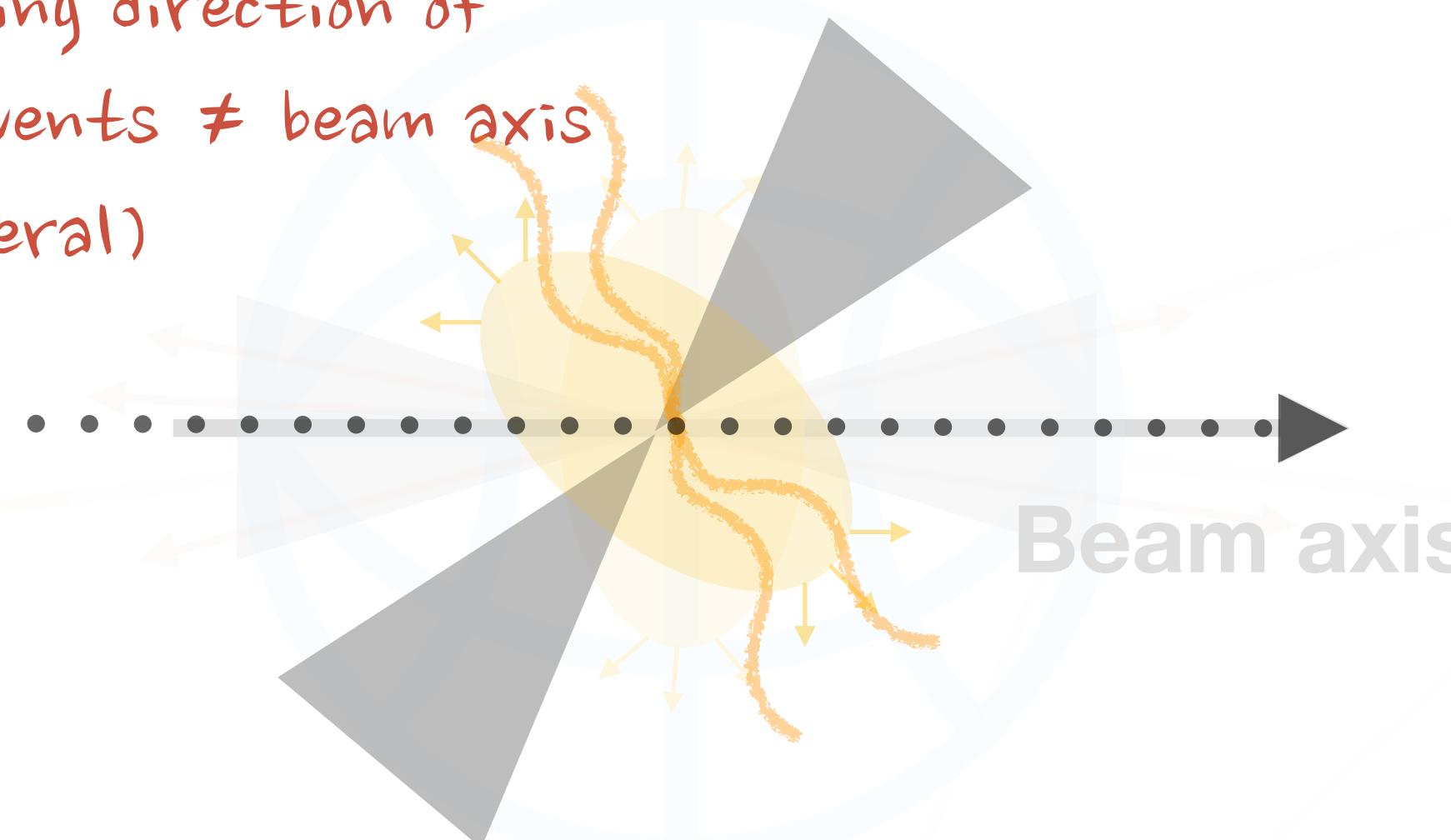




The **mid rapidity region** is where a correlation function sensitive to:

- Beam axis analysis:
hydrodynamic expansion of possible QGP medium in HI collisions

out-going direction of
 e^+e^- events \neq beam axis
(in general)

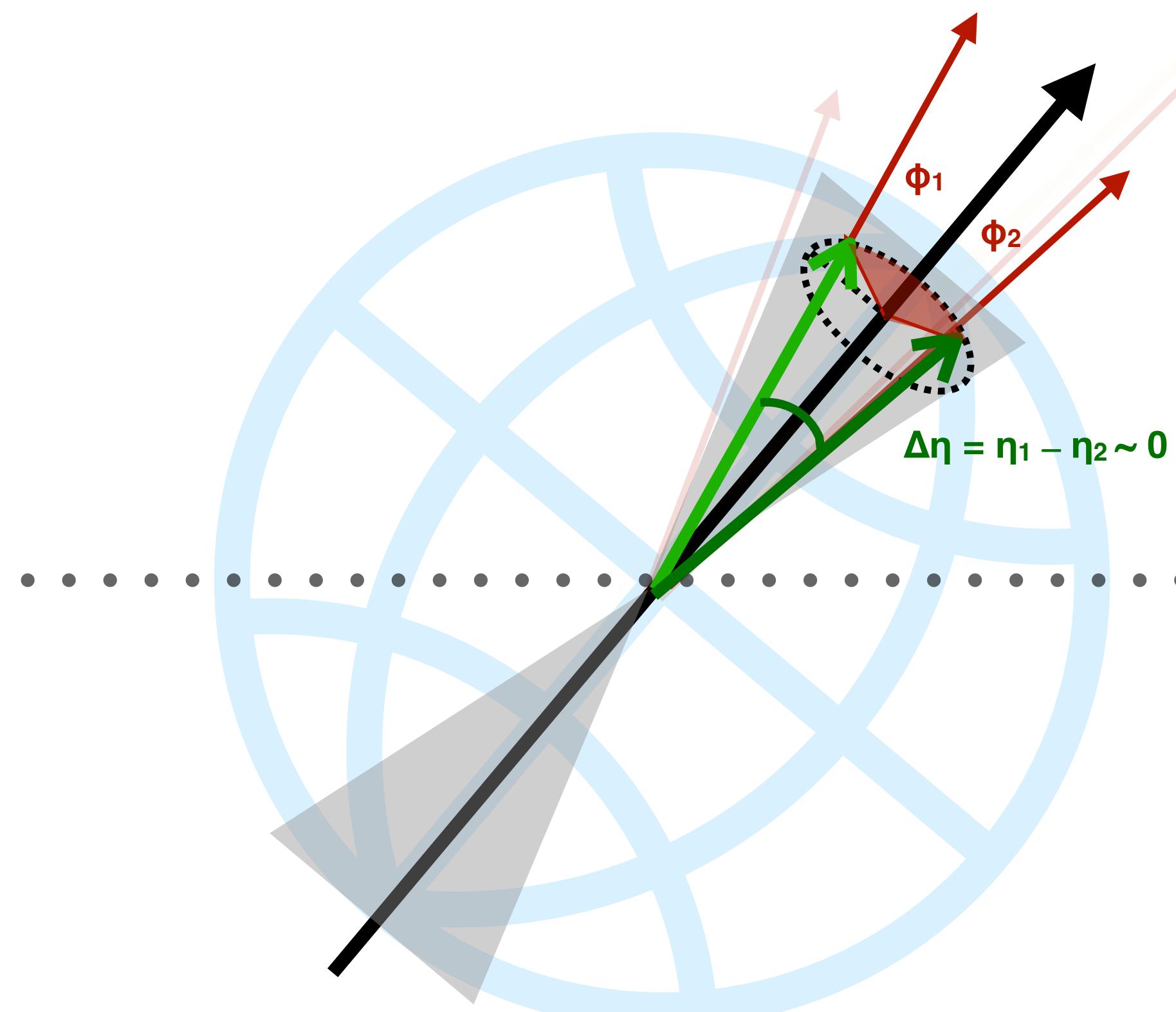


The **mid rapidity region** is where a correlation function sensitive to:

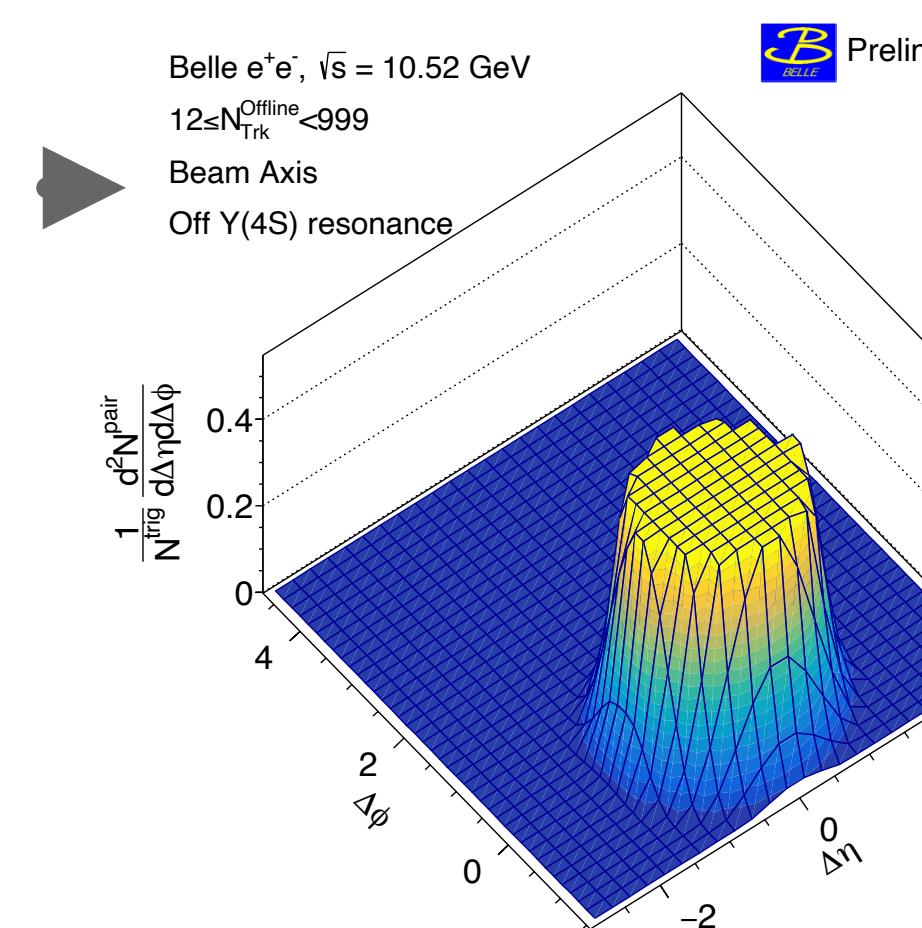
- Beam axis analysis:
hydrodynamic expansion of possible QGP medium in HI collisions
- Thrust axis analysis:
soft emissions or QGP in e^+e^- annihilation

How to understand correlation function in thrust axis coordinate?

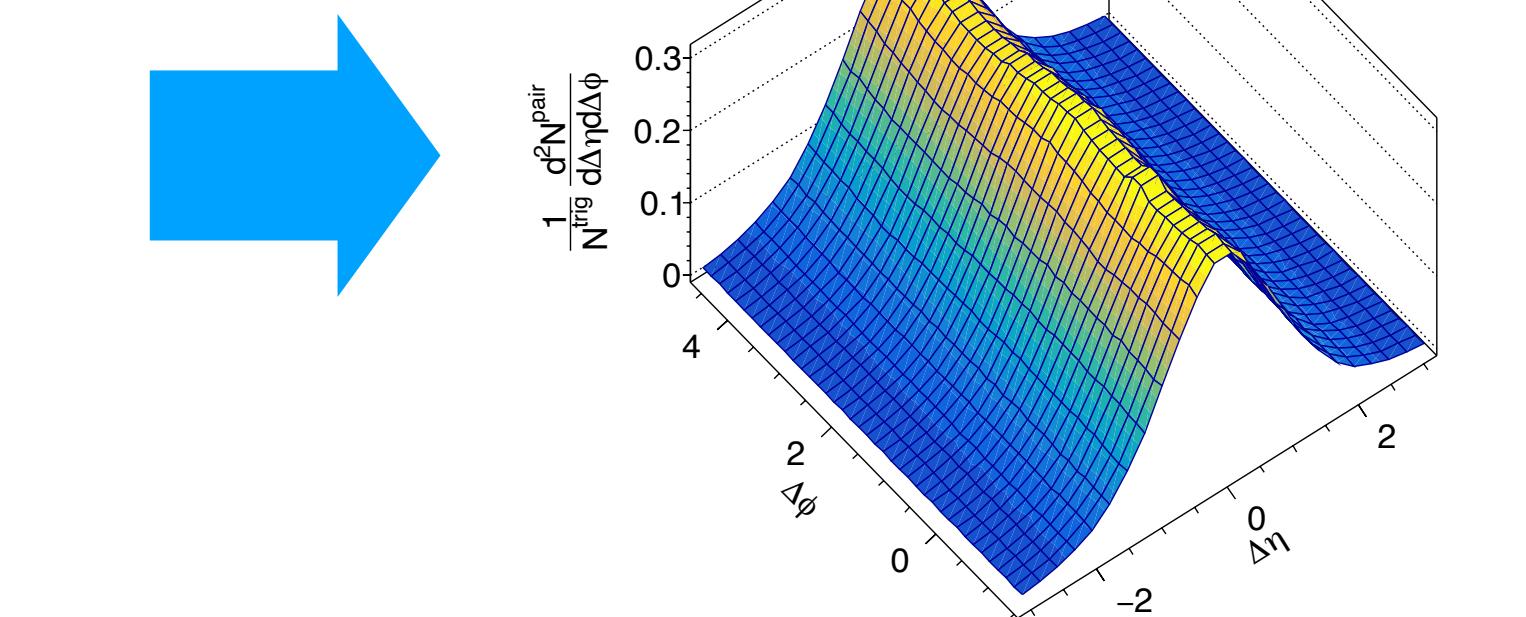
- Intra-jet correlation of on-axis jets is diluted!



Collinear leading intra-jet
correlation dilutes along $\Delta\phi$



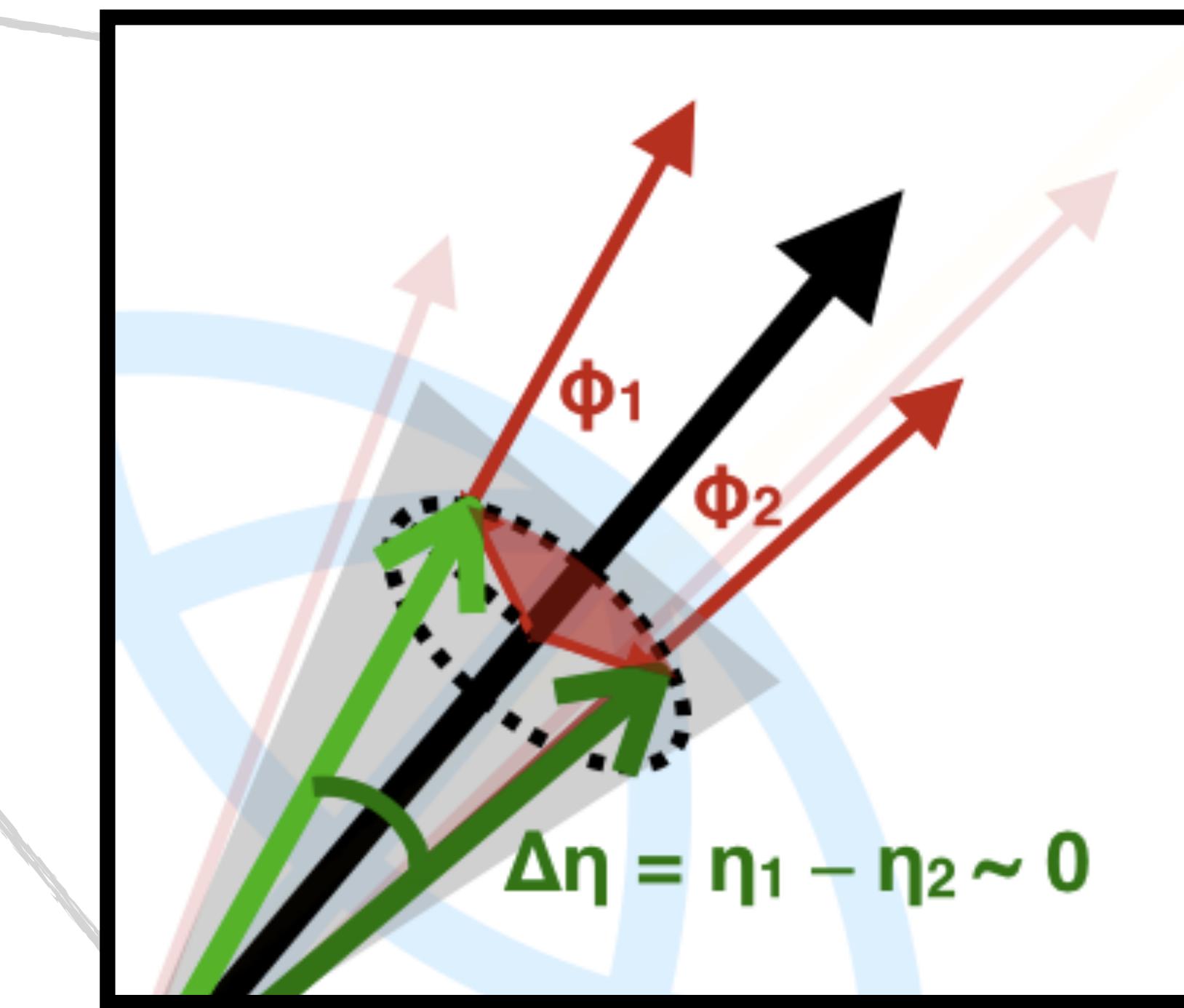
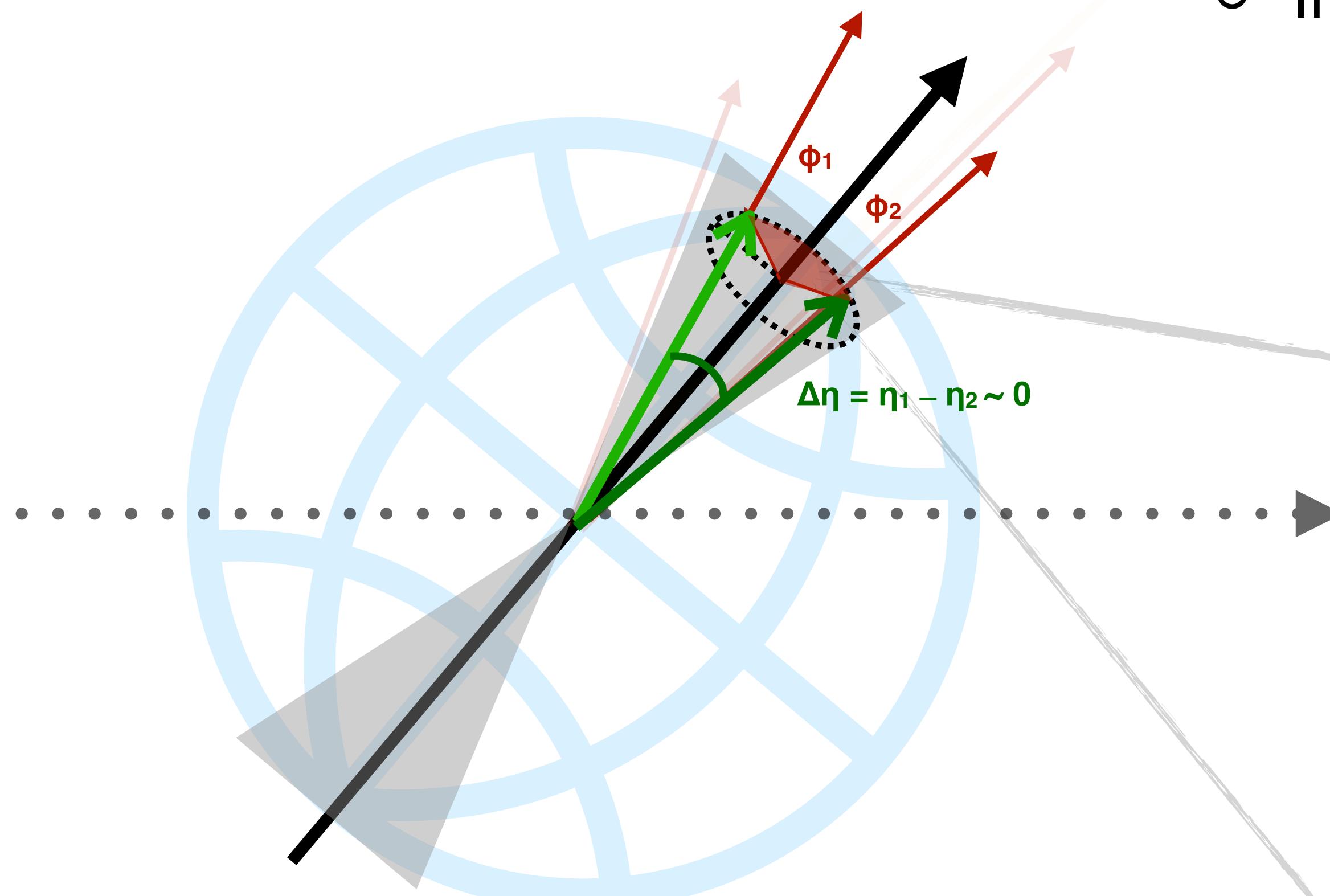
leading intra-jet correlation viewed
@ beam coordinate



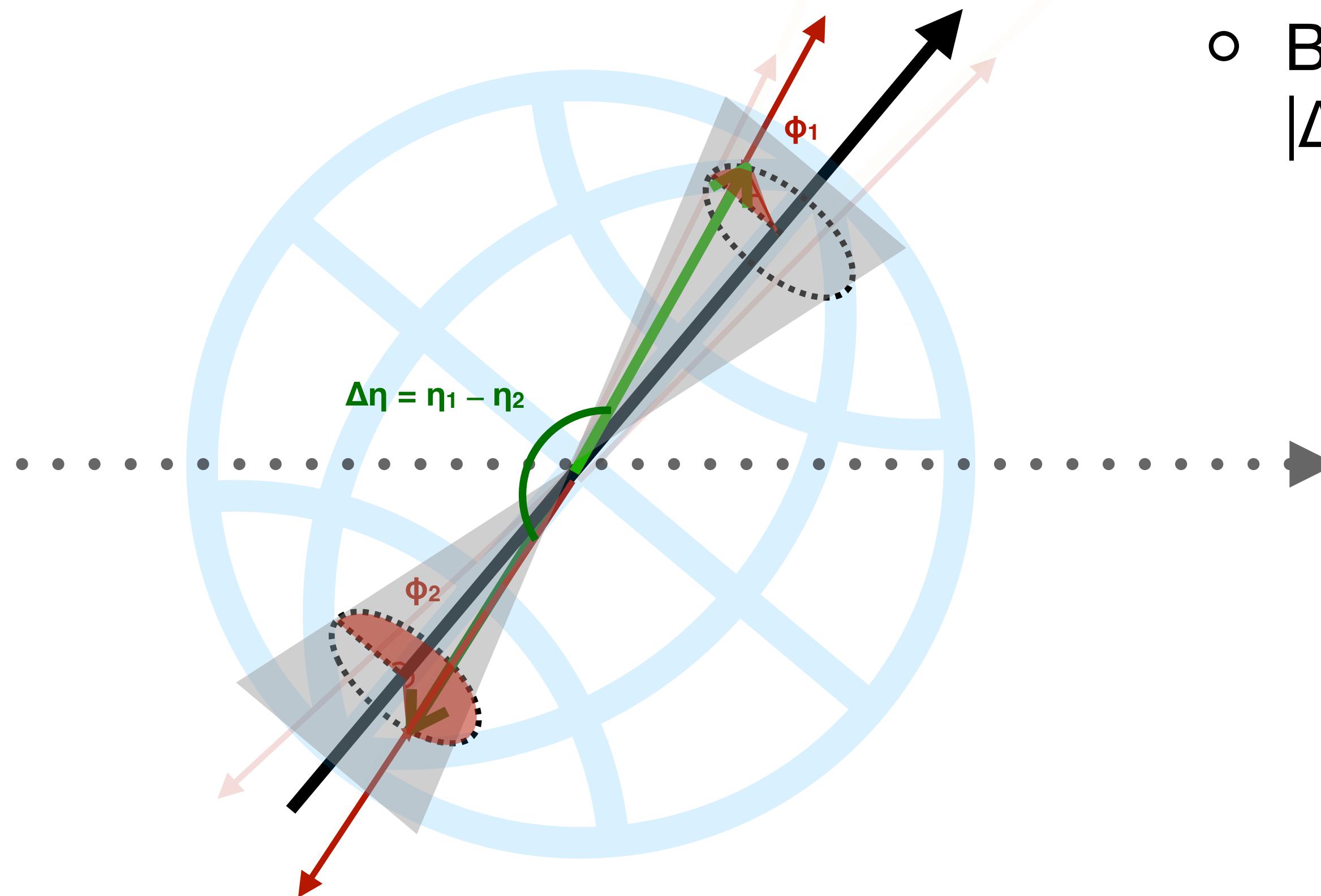
leading intra-jet correlation viewed
@ thrust coordinate

A weakened jet correlation

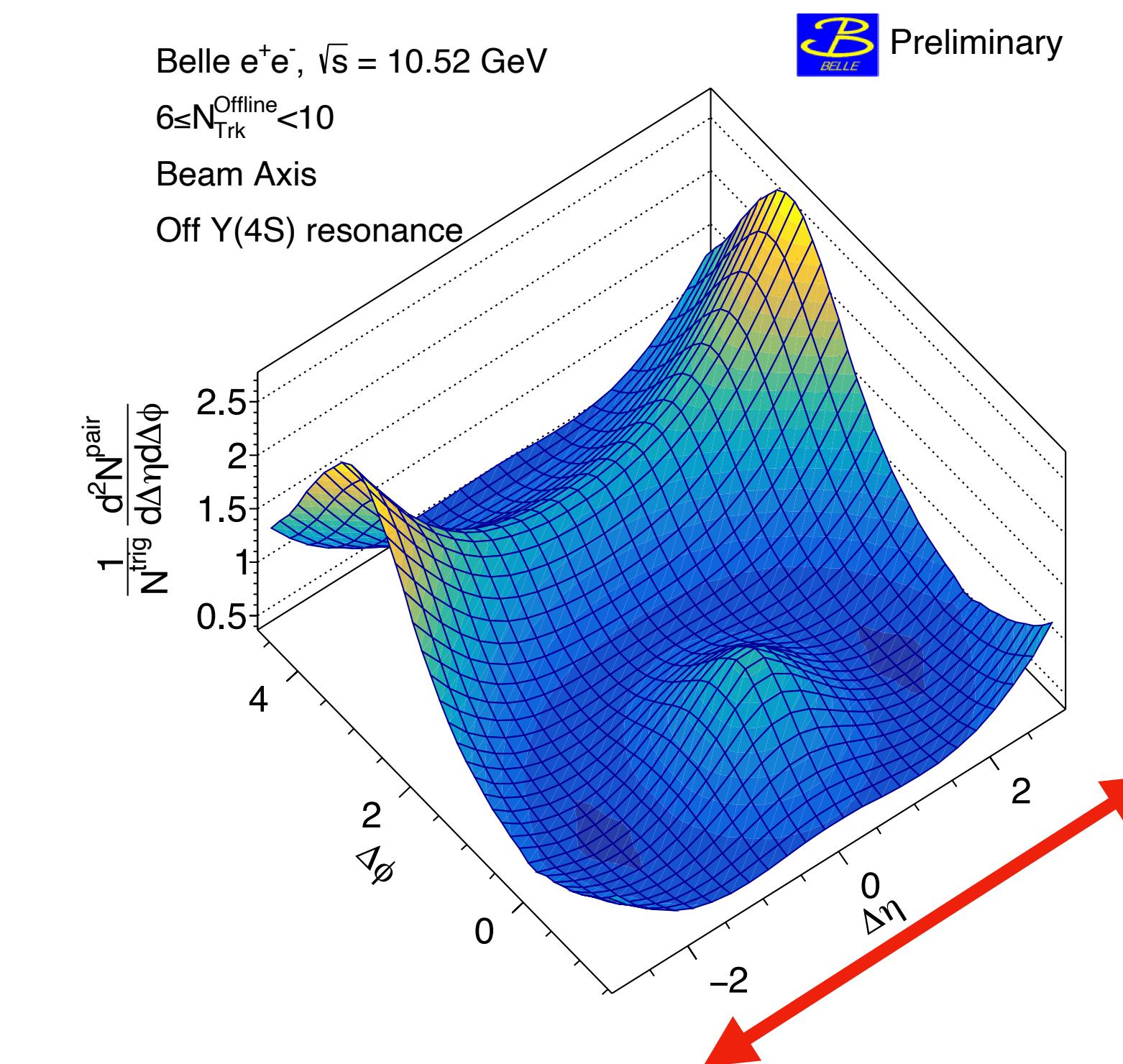
- Intra-jet correlation of on-axis jets is diluted!



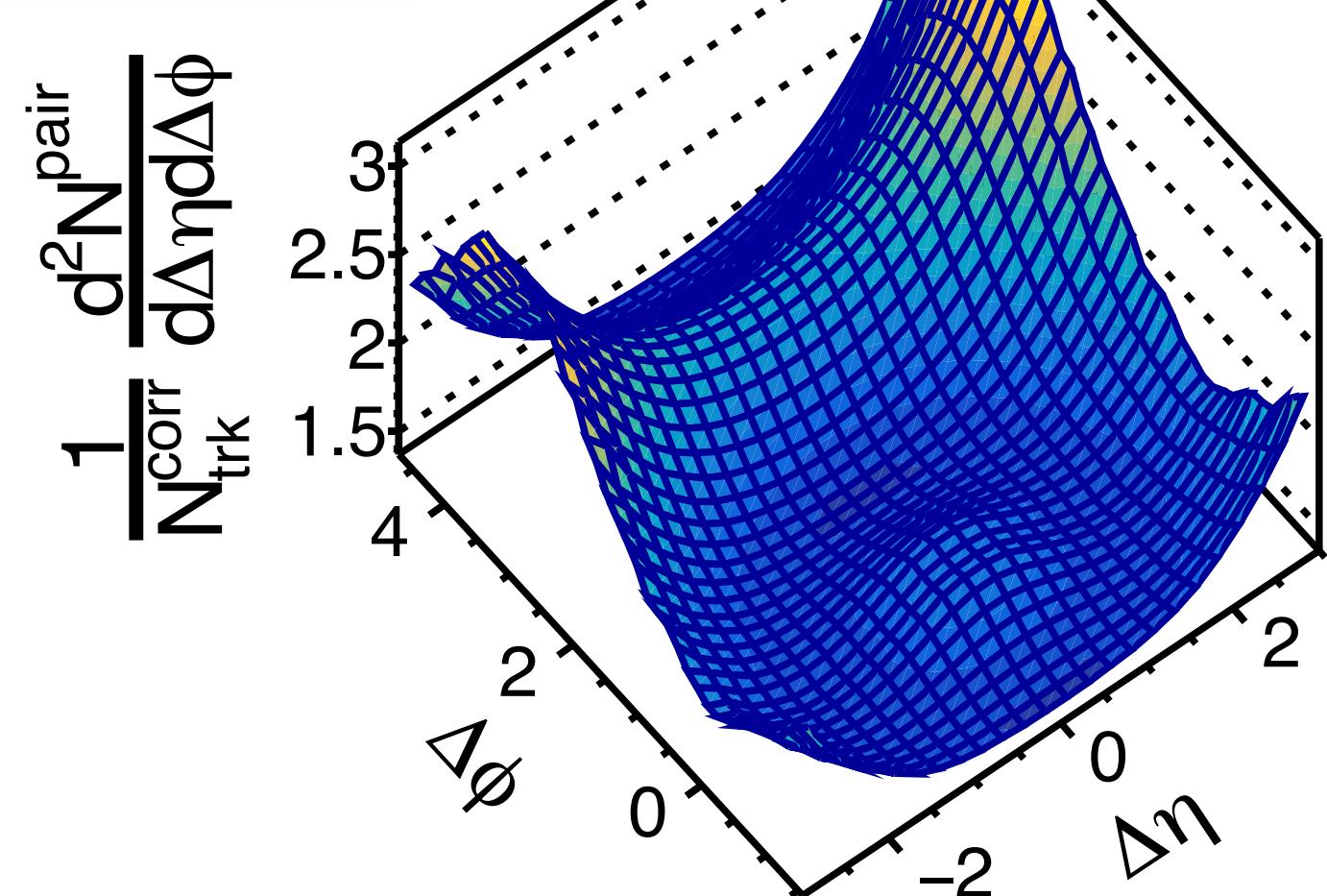
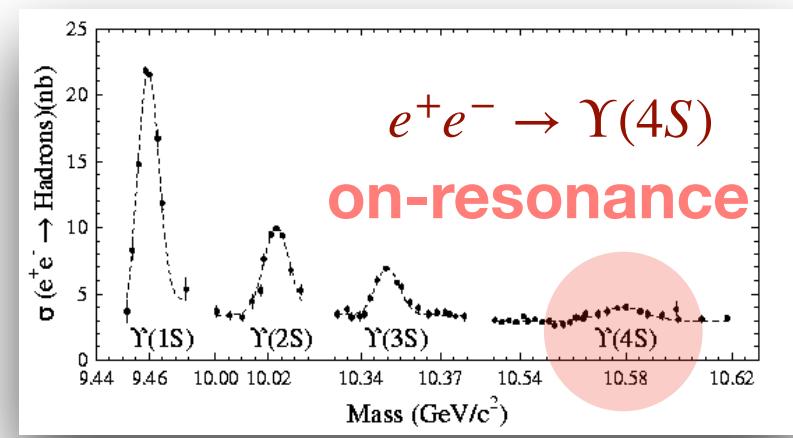
A weakened jet correlation



- Intra-jet correlation of on-axis jets is diluted!
- Back-to-back-jet correlation is excluded at finite $|\Delta\eta|$ region of interest

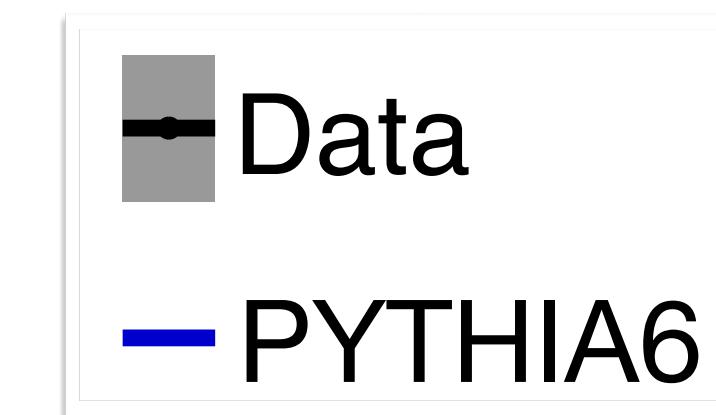


- Larger discrepancies are observed btw data and PYTHIA6 in the near-side ($\Delta\phi \approx 0$) and away-side ($\Delta\phi \approx \pi$) peak values

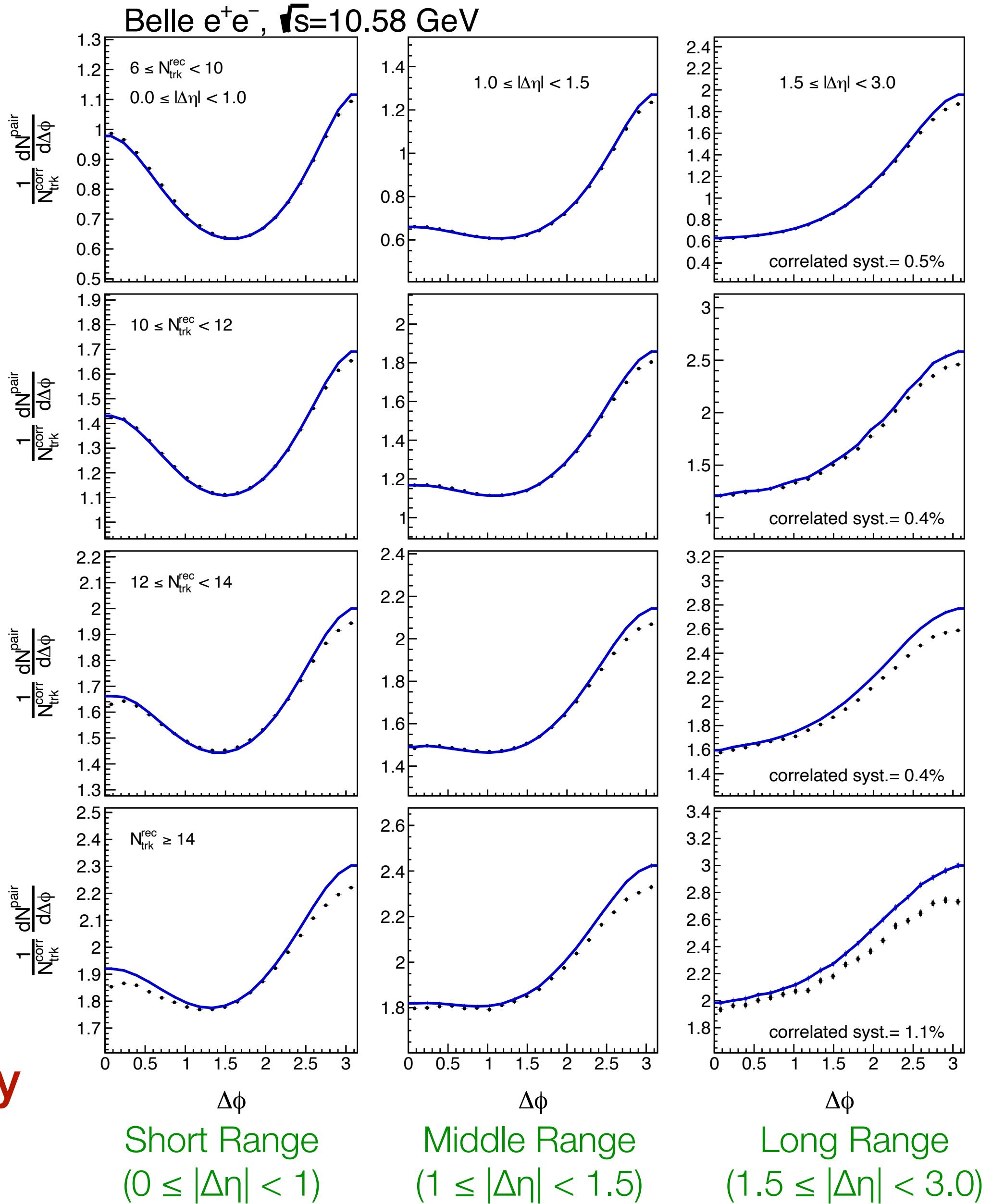


[arXiv:2206.09440](https://arxiv.org/abs/2206.09440)
submitted to JHEP

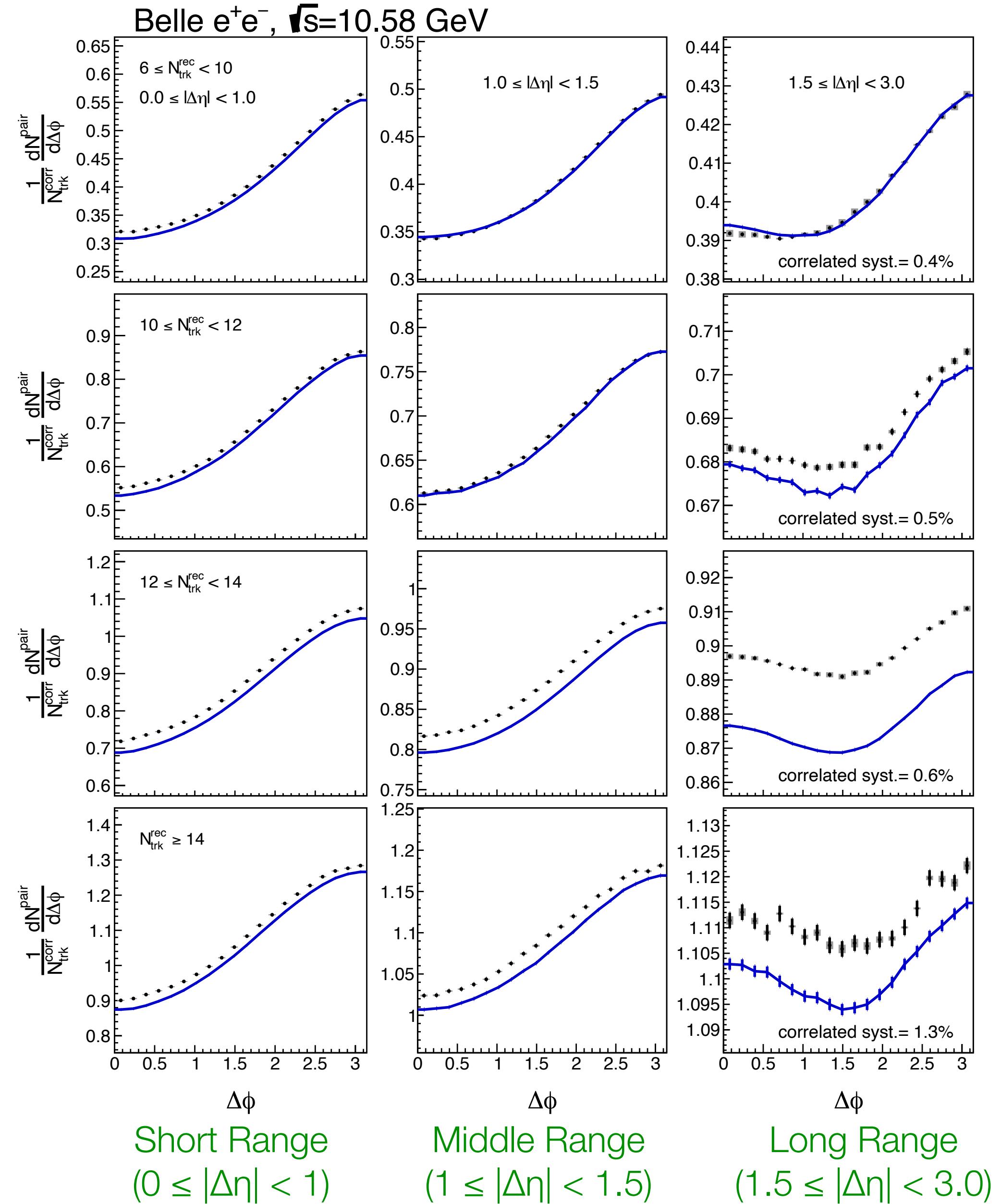
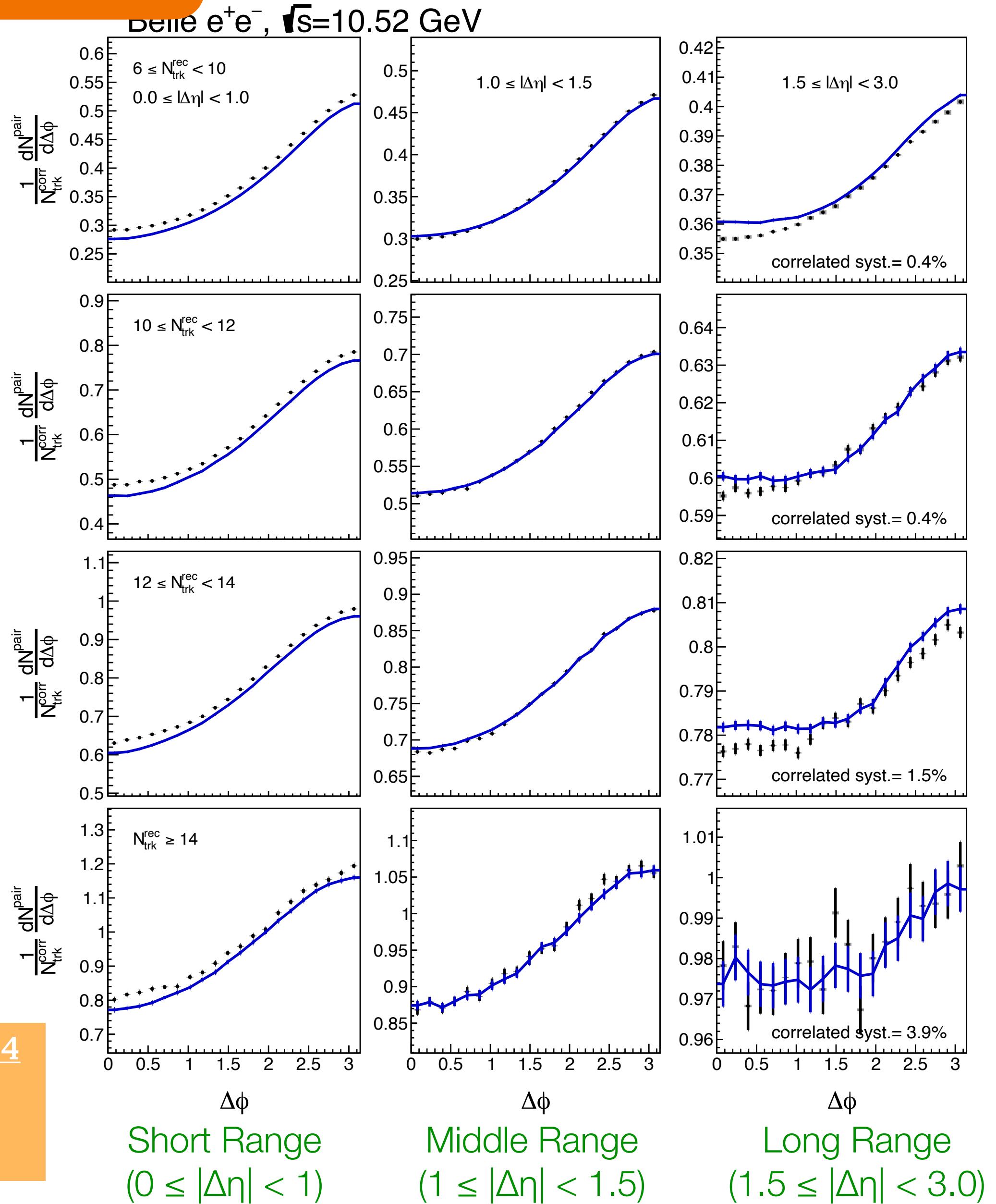
$$12 \leq N_{\text{trk}}^{\text{rec}} < 14$$



High-multiplicity



Thrust-axis two-particle correlations



arXiv:2201.01694

Phys. Rev. Lett.
128 (2022)
142005

Selections

1. Primary particle selection

Vary the primary particle definition between the proper lifetime cut $\tau < 1 \text{ cm}/c$ and the vertex cut $V_r < 1 \text{ cm}$

2. Tracking efficiency

Universal 0.35% uncertainty quoted for high p_T ($> 200 \text{ MeV}/c$) tracks

3. Event selection

Vary the energy sum in ECL from $> 0.18 \sqrt{s}$ to $> 0.23 \sqrt{s}$

Histogramming imperfection

4. $B(0,0)$ extrapolation and long-range correlation scaling

Corrections of bin-size effect on the $B(0,0)$ scaling factor and the magnitude of the long-range correlations are applied. Uncertainties of the correction factors are considered as sources of systematics

5. $\Delta\phi$ bin width

Reweighting

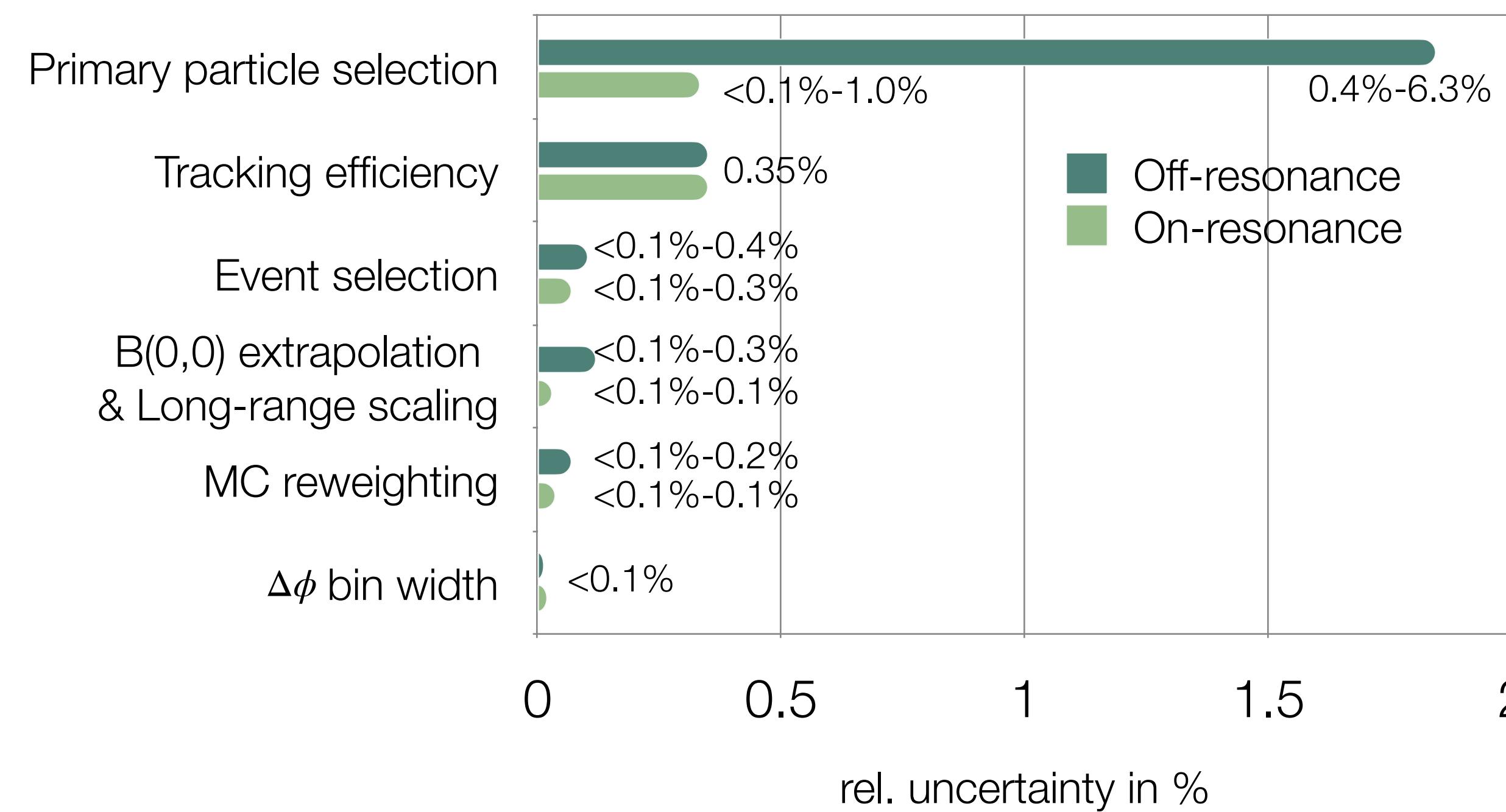
Accessing by reweighting factors with the alternative parametrization

6. MC reweighting

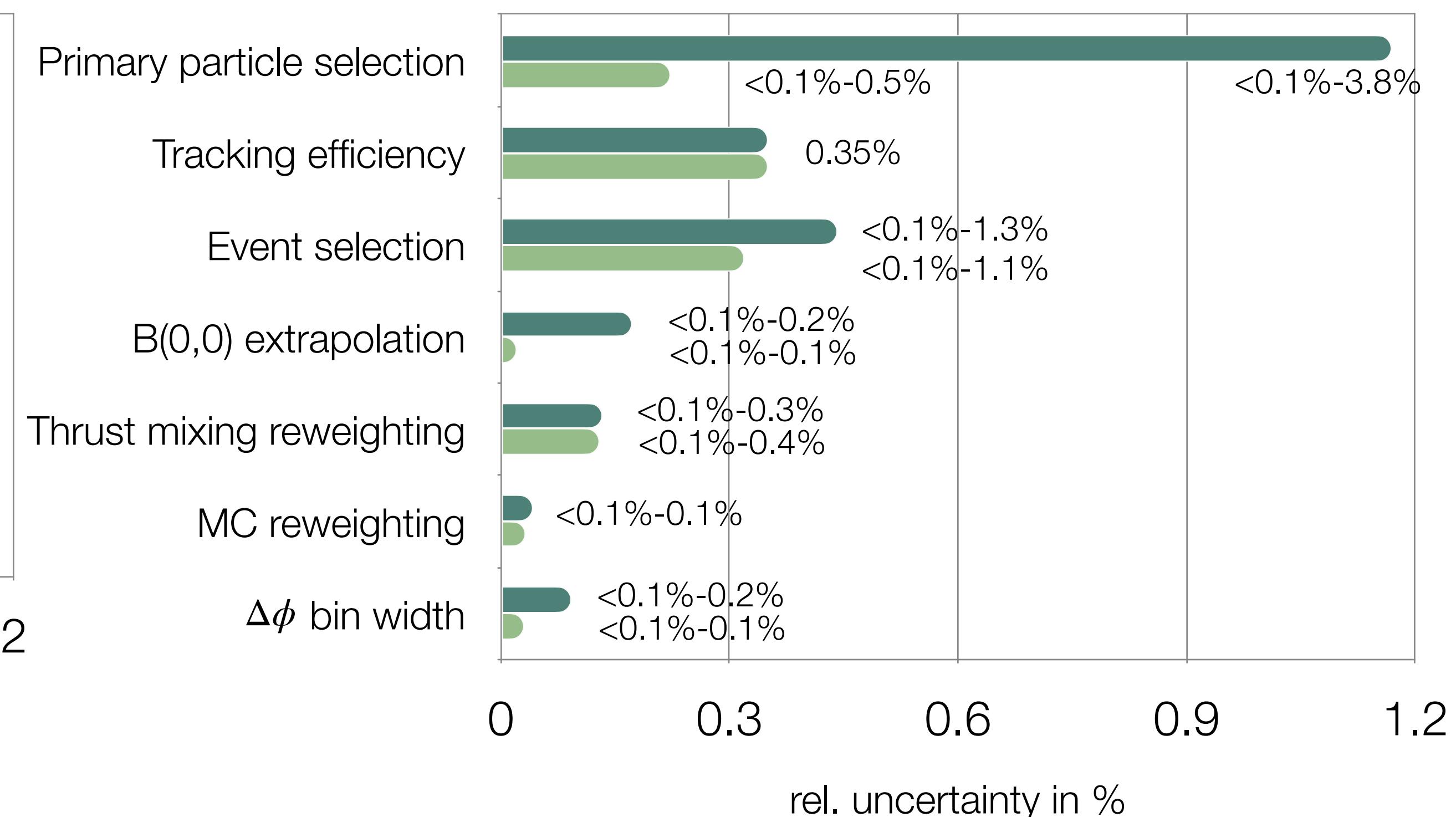
7. Thrust mixing reweighting

- Selections (primary particle, tracking, and event selections) are the dominant systematics sources
- Others are comparably small: $O(10^{-4})$ up to 0.5%

Beam axis analysis



Thrust axis analysis



- ZYAM method (zero yield at minimum) is applied to calculate “ridge yield”

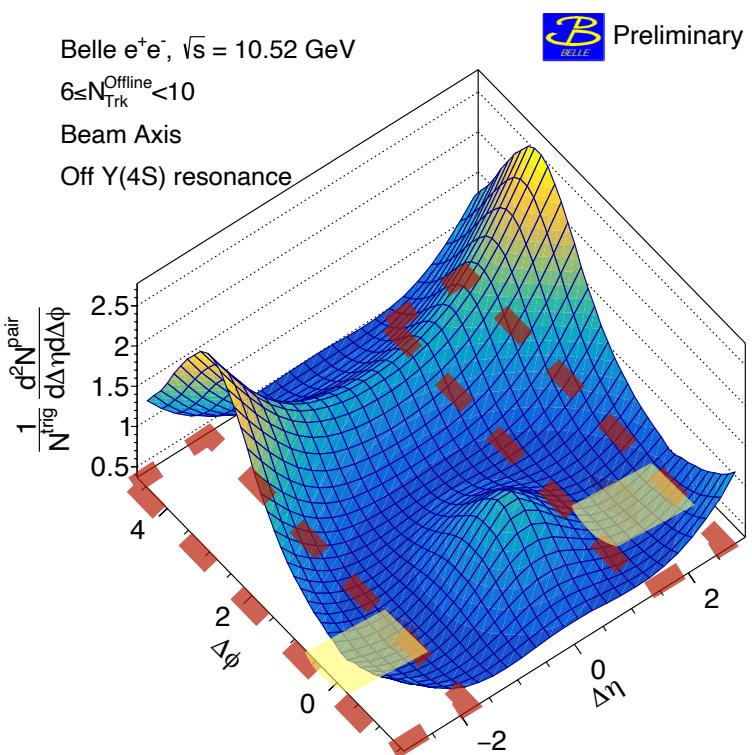
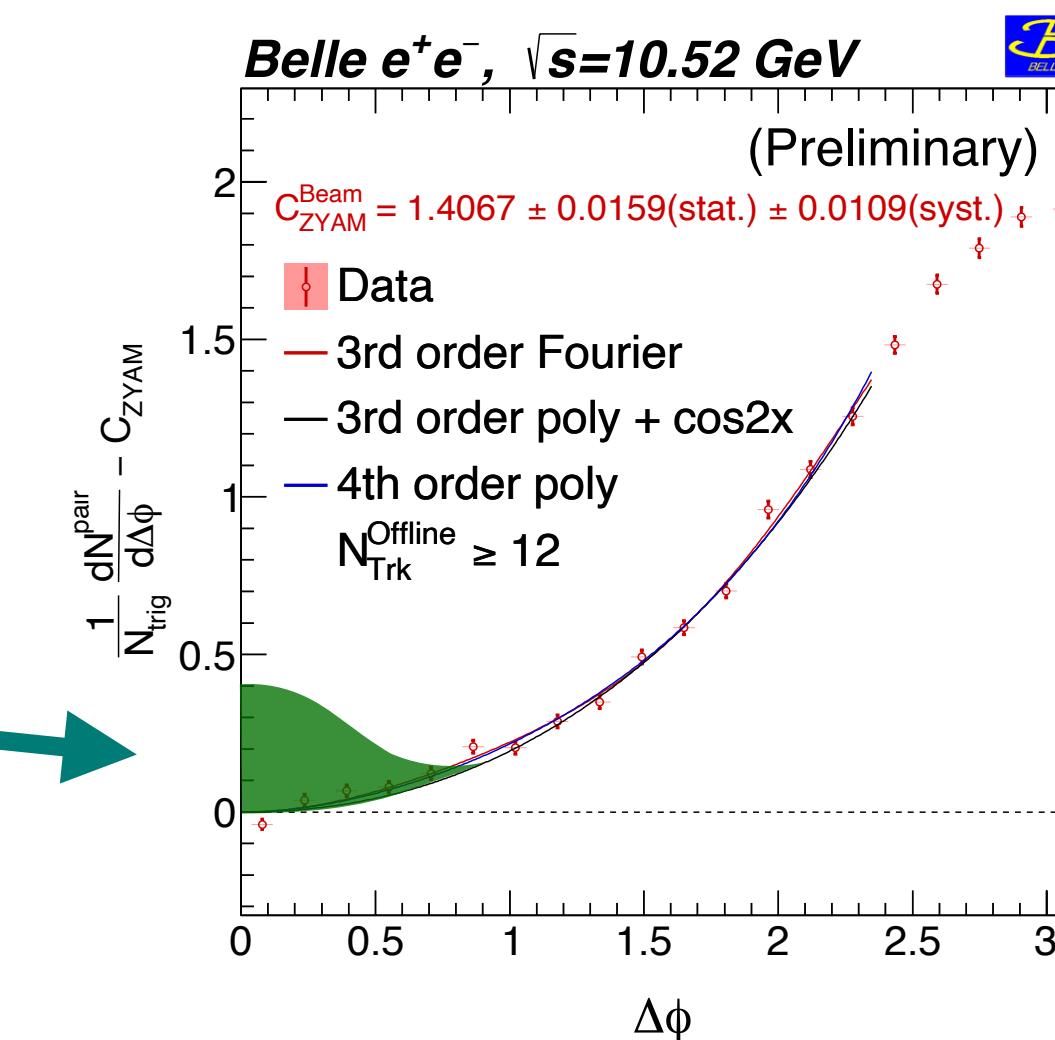
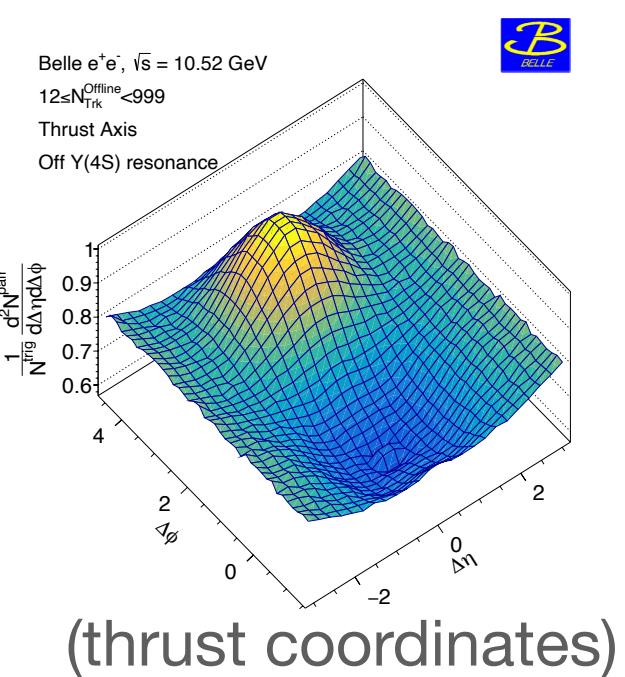
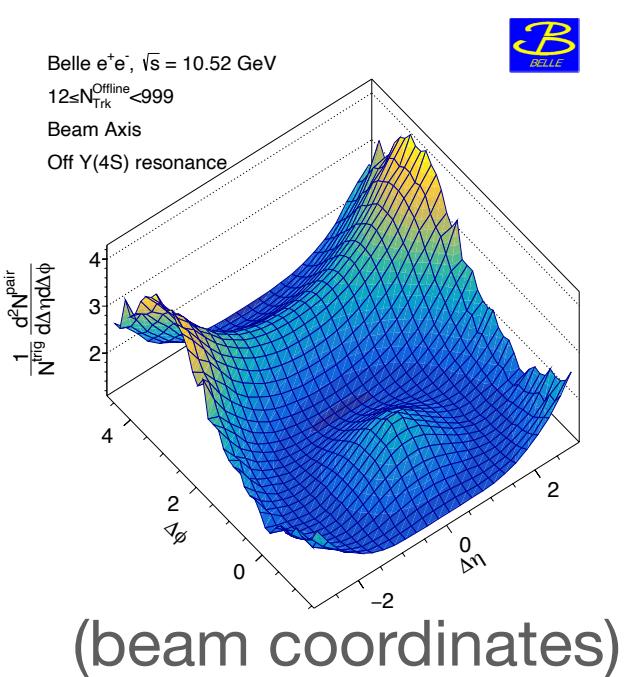


illustration of an enhanced ridge signal



- No significant ridge signals are observed in both beam, thrust axis coordinates
- Upper limits of ridge yield by the bootstrap method reported

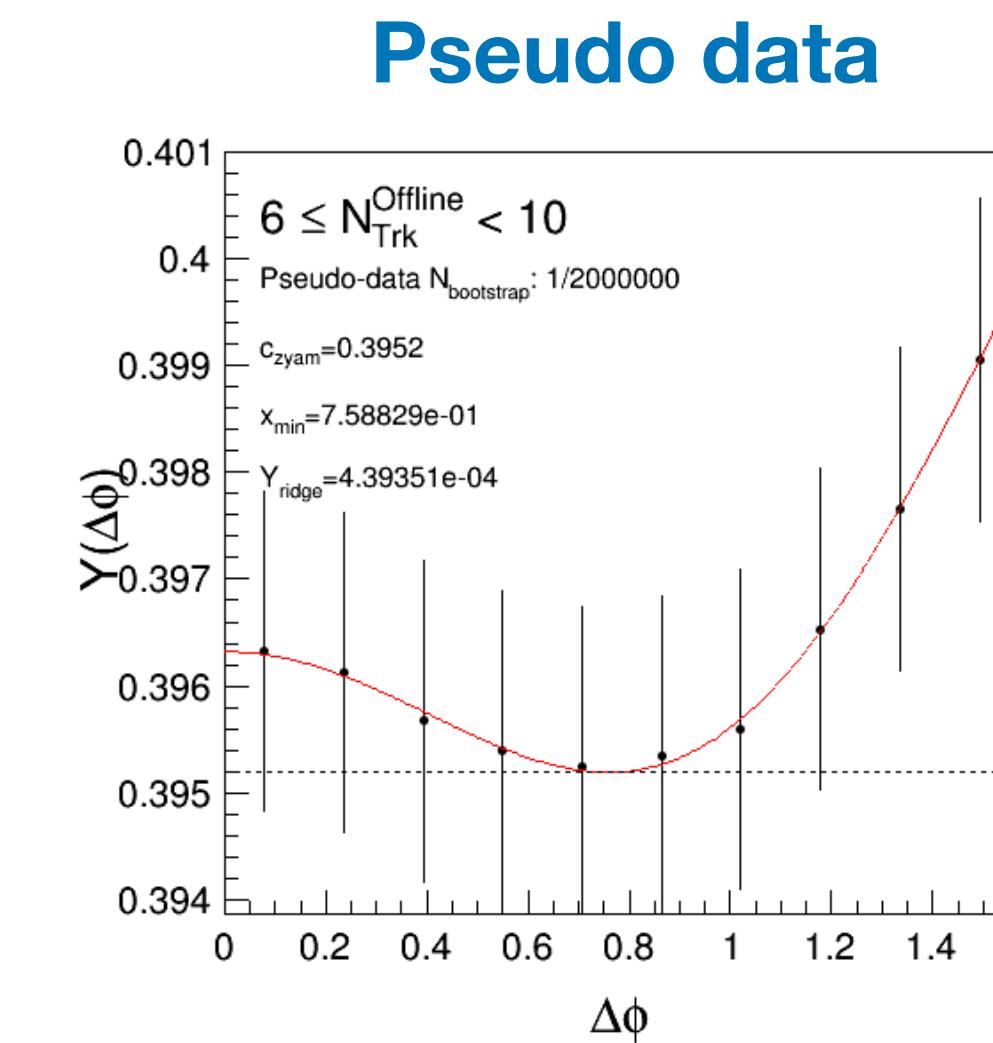
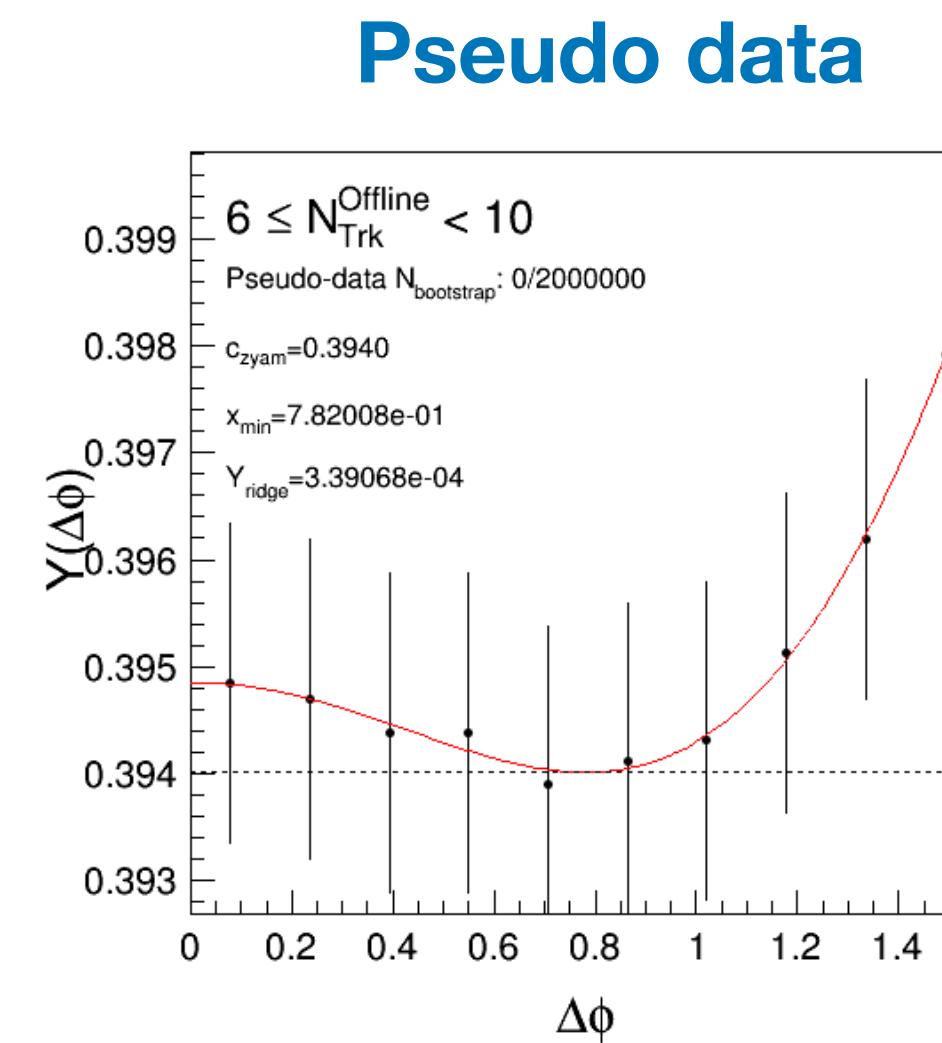
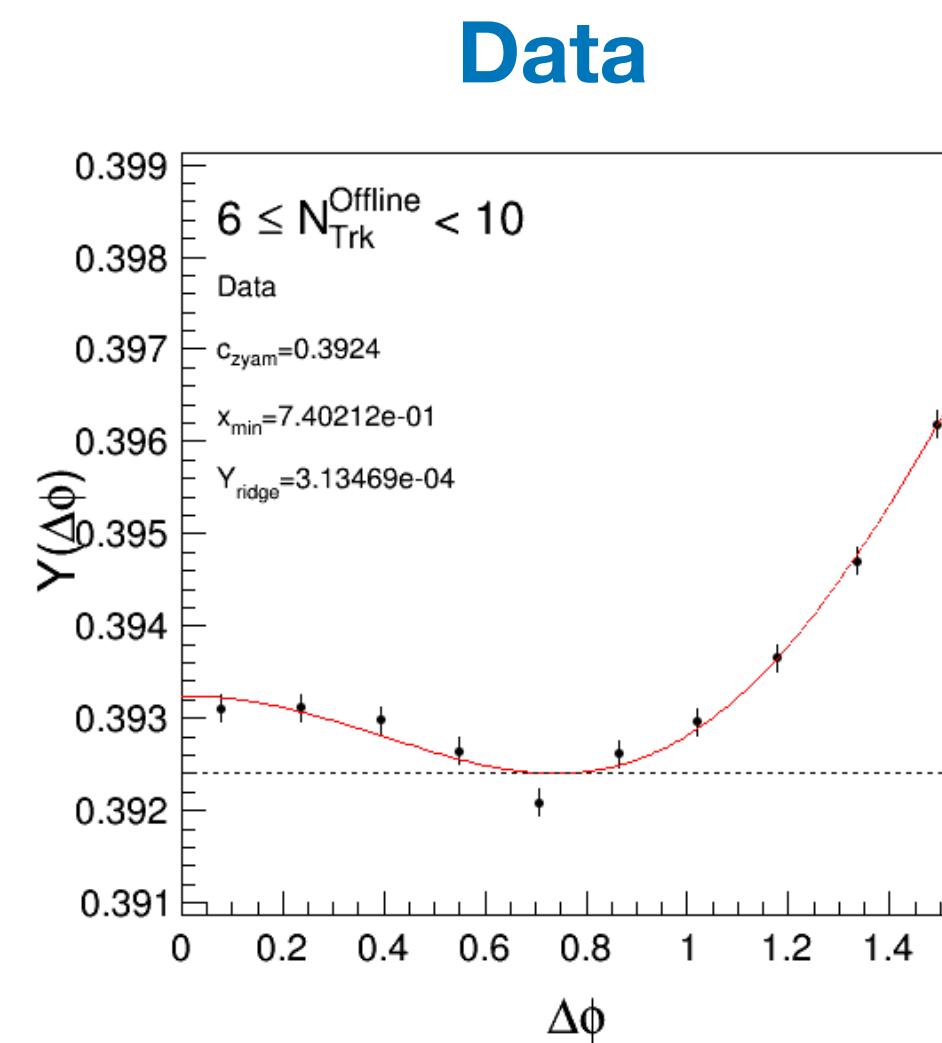


ZYAM
Phys.Rev. C72 (2005)
011902

bootstrap: [bootstrap]

Bootstrap method

- Fit the long-range yield distribution $Y(\Delta\phi)$.
- Vary the functional distribution by statistical and systematic uncertainties to construct a pseudo data.
- Refit the distribution with the same function and get a new ridge yield from this smeared distribution.
- Total 2M pseudo data are constructed.



Ref: [\[bootstrap\]](#)

Belle e^+e^- , $\sqrt{s}=10.58 \text{ GeV}$ (1.5 < $|\Delta\eta|$ < 3.0)