### **Diquarks on the Lattice**

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based on: [2203.16583][2203.03230] JHEP 05 (2022) 062 [2106.09080] Heavy spectrum - a precision tool and challenge to theory

Many new and exotic hadrons observed, e.g. 62 at the LHC

4-/5-quark states not expected in quark models. Many predicted quark model states not found.



... many not explained in theory QCD often approximated in models ~> many extensions possible ~> many interpretations ~> often contradictory statements

model	building blocks
" plain"	$q_{(i,c)}, \bar{q}_{(i,c)}$
diquark	$[qq]_{(i,j,c)} \& q/\bar{q}$
triquark	$[qq\bar{q}]_{(i,j,k,c)}$ & $q/\bar{q}$
hydro-onium	$[Q\bar{Q}]_{(i,j)}, \ [q\bar{q}]_{(i,j)},$
molecular	$[qqq]_{(i,j,k)}$ $[Q\bar{q}]_{(i,j)}, [q\bar{Q}]_{(i,j)},$ $[qqQ]_{(i,j,k)},$

One goal: Non-perturbative insights into exotic hadrons in full QCD

Diquarks - attractive building blocks for ordinary and exotic hadrons

### Diquarks - an attractive concept

"The concept of diquarks is almost as old as the quark model, and actually predates QCD [1]" ~ arXiv:2203.16583; [1] PR 155, 1601 (1967)

Successful for low-lying baryons and exotic hadrons.
 Well founded in QCD with many predictions.
 But, experimental evidence has been elusive.

• Light diquarks:

 $\circ$  special "good" ( $\bar{3}_F, \bar{3}_c, J^P = 0^+$ ) configuration

- $\circ~$  quarks on "good" diquarks attract each other
- o large mass splitting in good, bad and not-even-bad
- o non-vanishing size or compact?
- HQSS-limit: A diquark acts as an antiquark  $[QQ] \leftrightarrow \overline{Q}$ .  $\rightsquigarrow$  currently one motivation for  $T_{QQ}$ -type hadrons, next slide



In the following:

- $\circ~$  new work on diquarks as possible effective d.o.f's in QCD
- was motivated by our studies of doubly heavy tetraquarks

Phys.Rev.D 102 (2020) 114506 [2006.14294] Phys.Rev.D 99 (2019) 5, 054505 [1810.10550] Phys.Rev.Lett. 118 (2017) 14, 142001 [1607.05214]

# The case for doubly heavy tetraquarks - Diquarks and $qq'\bar{Q}\bar{Q}'$

Revisit ideas for stable multiquarks based on diquarks

- $\circ~$  Effective q-q interaction in "good" diquarks
- $\circ\;\; \mathsf{HQS}\;(Q\sim b)\;\mathsf{relates}\;[ar{Q}ar{Q}]_3\leftrightarrow Q$
- Combine (HH)+(II) diquarks into tetraquarks:  $\left[ \{ ag' \} [\bar{Q}\bar{Q}'] = (qC\gamma_5 g')(\bar{Q}C\gamma_i \bar{Q}') \right]$
- PDG mesons/baryons provide constraints



→Ader et al. ('82); Manohar, Wise ('93); .



<sup>→</sup>Mathur et al.'19

### Diquarks on the lattice - a gauge invariant probe

• A problem for the lattice is that diquarks are colored, i.e. not-gauge invariant. • Could fix a gauge, but then properties are gauge-dependent (masses, sizes,...)

 $\rightsquigarrow$  lattice and Dyson-Schwinger, see e.g. [15-20] in 2106.09080

Alternative: Static spectator quark Q (m<sub>Q</sub> → ∞) cancels in mass differences.
 Diquark properties exposed in a gauge-invariant way.

 $\rightsquigarrow$  hep-lat/0510082, hep-lat/0509113, hep-lat/0609004, arxiv:1012.2353

$$C_{\Gamma}(t) \sim \exp\left[-t\left(m_{D_{\Gamma}}+m_{Q}+\mathcal{O}(m_{Q}^{-1})
ight)
ight]$$

 $\rightsquigarrow t \rightarrow$  large,  $m_Q \rightarrow$  large



 $<sup>\</sup>leadsto$  picture of baryons from Hosaka, 2013

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• Lattice correlator: Diquark embedded in a static-light-light baryon

$$C_{\Gamma}(t) = \sum_{\vec{x}} \left\langle [D_{\Gamma}Q](\vec{x},t) \ [D_{\Gamma}Q]^{\dagger}(\vec{0},0) \right\rangle$$

$$\xrightarrow{\sim} \text{ static quark} = Q \text{ and } D_{\Gamma} = q^{c}C\Gamma q$$

$$\xrightarrow{\sim} \text{ flavor combinations } ud, \ \ell s, \ ss'$$

$$\xrightarrow{\sim} \text{ static-light mesons } [\bar{Q}\Gamma q]$$

Towards a clearer understanding and footing in QCD using lattice calcs

- spectrum: [diquark] mass differences are fundamental characteristics of QCD (Jaffe '05, arXiv:hep-ph/0409065)
- 2. spatial correlations: study attraction and special status of the "good" diquark
- 3. structure: estimate size and shape of the "good" diquark

Diquark spectroscopy



$$(1^+ - 0^+)_{qq'}$$
 splitting



We consider mass differences of qq'Q baryons:

$$C^{qq'Q}_{\Gamma}(t)-C^{qq'Q}_{\gamma_5}(t)$$

 $\rightsquigarrow Q$  drops out

 $\rightsquigarrow$  measures diquark-diquark mass difference

Bad-good diquark splitting:

- $\circ~$  Special status of good diquark observed
- $\circ~{\rm Good}~0^+$  ud diquark lies lowest in the spectrum
- $\circ~$  Bad  $1^+$   $\mathit{ud}$  diquark 100-200 MeV above
- $\circ~0^-$  and  $1^ \mathit{ud}$  diquarks  $\sim 0.5~GeV$  above
- $\circ~$  Pattern repeated in  $\ell s$  and ss'

 $\Delta m_{qq'Q}(m_{\pi})$  dependence:

- $\circ~$  Chiral limit:  $\sim {\rm const}$
- $\circ$  Heavy-quark limit: decreases  $\sim 1/(m_{q_1}m_{q_2})$ , with  $m_\pi \sim (m_{q_1}+m_{q_2})$

$$\delta(1^+ - 0^+)_{q_1q_2} = A / \left[1 + (m_\pi/B)^{n \in 0,1,2}\right]$$

# Lattice spectroscopy - diquark-quark differences

We consider mass differences of a qq'Q baryon and a light-static meson:

$$\begin{array}{|c|c|}\hline C_{\Gamma=\gamma_5}^{qq'Q}(t) - C_{\gamma_5}^{q'\bar{Q}}(t) \\ \hline & & \sim Q \text{ drops out} \\ & & \sim \text{ diquark-quark mass difference} \end{array}$$

 $\Delta m_{qq'Q}(m_{\pi})$  dependence:

 Chiral vs. heavy-quark limiting behaviours, as before

$$\delta(Q[q_1q_2]_{0^+} - \bar{Q}q_2) = C \left[1 + (m_{\pi}/D)^{n \in 0,1,2}\right]$$

Diquark-quark splitting:

- $\circ~$  Established mass differences between a good diquark and an <code>[anti]quark</code>
- $\circ~$  May prove useful in identifying favourable tetra-, pentaquark channels
- $\circ\,$  Omits possible distortions through additional light quarks, Pauli-blocking, spin-spin interactions  $\ldots\,$



### Diquark spectroscopy - comparing results

• We want to compare our results with phenomenology

 $\rightsquigarrow$  more details in extra info slides

- $\circ\,$  Key resource: (Jaffe '05, arXiv:hep-ph/0409065), updated with PDG 2021 input
- $\circ~$  For pheno estimates combine charm and bottom hadron masses such that leading  $\mathcal{O}(1/m_Q)~(Q=c,b)$  cancel
- The main spectroscopy results are summarised as:

All in [MeV]	$\delta E_{\text{lat}}(m_{\pi}^{\text{phys}})$	$\delta E_{\rm pheno}$	$\delta E_{\rm pheno}^{\rm bottom}$	$\delta E_{\rm pheno}^{\rm charm}$
$\delta(1^+-0^+)_{ud}$	198(4)	206(4)	206	210
$\delta(1^+ - 0^+)_{\ell s}$	145(5)	145(3)	145	148
$\delta(1^+ - 0^+)_{ss'}$	118(2)			
$\delta(Q[ud]_{0^+} - \overline{Q}u)$	319(1)	306(7)	306	313
$\delta(Q[\ell s]_{0^+}-ar{Q}s)$	385(9)	397(1)	397	398
$\delta(\textit{Q}[\ell s]_{0^+} - ar{\textit{Q}}\ell)$	450(6)			

 $\leadsto$  use the bottom estimate for static

 $\sim$  use charm-bottom difference as estimate for deviation from static

 $\Rightarrow \lesssim \mathcal{O}(7) \text{MeV}$  deviation

• Overall, very good agreement observed.

Diquark structure

#### Diquarks - spatial correlations

We access (good) diquark structure information through density-density correlations:



Main tool: Correlations between two light quarks' relative positions to the static quark. Note, when S and  $r_{ud}$  fixed, distance between static quark Q and light quarks q, q' is

- $\circ~$  Minimized for  $\phi=\pi,$  possible disruption due to  ${\it Q}$  is largest
- Maximized for  $\phi = \pi/2$ , possible disruption due to Q is smallest

# Good diquark attraction



Setting  $\phi = \pi/2$ :

- $|\vec{x}_1| = |\vec{x}_2| = R$ , use  $R, \Theta$ :  $\rho_2^{\perp}(R, \Theta) = \rho_2(r_{ud}, S, \pi/2)$
- Attraction visible through increase in  $\rho_2^{\perp}$  for small  $\Theta$  at any fixed R

Two limiting cases for the two quarks:  $\circ \cos(\Theta) = 1$  on top of each other  $\circ \cos(\Theta) = -1$  opposite each other

"Lift" as qualitative criterion:

$$\frac{\rho_2^{\perp}(R,\Theta=0,\Gamma)}{\rho_2^{\perp}(R,\Theta=\pi/2,\gamma_5)}$$

Increase observed in good diquark only

# Spatial correlation over $\Theta$



# Good diquark size

1 0e-04



• Distance between quarks:  $r_{ud} = R_{\sqrt{2(1 - \cos(\Theta))}}$ 

→ different visualisation

- $\rho_2^{\perp}(R, r_{ud}) \sim \exp(-r_{ud}/r_0)$  $\rightsquigarrow$  "characteristic size"  $r_0$
- Need to control:
  - o interference from Q
     → we limit analysis to r<sub>ud</sub> < R</li>
     o periodicity effects
    - $\rightarrow$  in practice we find  $L = 5r_0$
- Further checks:  $A(R, r_{ud} = 0) \sim \exp(-R/R_0)$

Data well described by (single) exponential Ansatz





 $\circ$  all R shown simultaneously

2

 $\circ$  combined fits over  $\forall R$  with shared  $r_0$ 

r<sub>ud</sub>/a 10

8





Good diquark size:

- Agreement w/ prev. quenched and dynamical
- Refinement through our results
- $r_0 \simeq \mathcal{O}(0.6)$ fm weak  $m_{\pi}$  dependence  $\rightarrow \sim r_{\text{meson, barvon, arXiv:1604.02891}}$

 $r_0(m_\pi)$  dependence:

- $\circ \ m_{q,q'} \uparrow \text{should produce more compact} \\ \text{object}$
- But, diquark attraction↓ works opposite
- Former effect dominates at large  $m_{\pi}$ ?
- But, in quenched diquarks definitely larger...

Shape of good diquarks - studying wavefunction "oblateness"



Tangential and radial spatial correlation decay

As opposed to before  $R \neq fixed$ :  $\circ \phi = \pi$ : radial correlation,  $size \rightsquigarrow r_0^{\parallel}$   $\circ r_0^{\perp}/r_0^{\parallel}$  gives information on shape: = 1, spherical  $\neq 1$ , prolate/oblate  $ize \rightsquigarrow r_0^{\perp}$ 

- Probe J = 0 nature of good diquark (spherical, S-wave expectation)
- Diquark polarisation through static quark?



• Goal: •  $r_0^{\perp}$ ,  $r_0^{\parallel}$  at fixed *S* 

Technical issue:

◦ (||) as before: R = S◦ (⊥) different:  $R = \sqrt{(r^{\perp})^2 + S^2}$ 

Solution:

- $\circ$  Introduce "nuisance" paremeter  $R_0$
- $\circ~$  Adjusted in figure
- Parallel lines  $\rightsquigarrow r_0^{\perp} = r_0^{\parallel}$
- $r_0^{\perp}/r_0^{\parallel}(m_{\pi})$  dependence:
  - $\circ~$  Ratio  $\simeq 1$  for all  $m_\pi$
  - $\,\circ\,$  Consistent w/ scalar, J= 0, shape
  - No diquark polarisation through Q observed

## Summary - Diquarks on the lattice

Gauge invariant approach to diquarks in  $n_f = 2 + 1$  lattice QCD

 $\circ~$  Lattice setup with short chiral extrapolations, continuum limit still required

Diquark spectroscopy

- Special status of "good" diquark confirmed, attraction of 198(4)MeV over "bad"
- $\circ~$  Chiral and flavor dependence modelled through simple Ansatz
- $\circ~$  Very good agreement with phenomenological estimates

#### Diquark structure

- $\circ q q$  attraction in good diquark induces compact spatial correlation
- $\circ$  Good diquark size  $r_0 \simeq \mathcal{O}(0.6)$ fm  $\sim r_{
  m meson, \ baryon}$ , weakly  $m_\pi$  dependent
- o Good diquark shape appears nearly spherical

#### Outlook

- $\circ\,$  Results provide clear, quantitative support for the good diquark picture
- $\circ~$  Hope to refine diquark model parameters
- $\circ~$  Insights for studies of exotic tetraquarks (esp. doubly heavy), heavy-baryons, etc.
- $\circ~$  Refinement towards diquarks in light baryons? Tetraquark diquark content?  $\ldots$

Thank you for your attention.



Further material

#### A gauge invariant probe - lattice calculation details

• Lattice correlator: Diquark embedded in a static-light-light baryon

$$C_{\Gamma}(t) = \sum_{\vec{x}} \left\langle [D_{\Gamma}Q](\vec{x},t) \ [D_{\Gamma}Q]^{\dagger}(\vec{0},0) \right\rangle$$

→ static quark=Q and  $D_{\Gamma} = q^{c}C\Gamma q$ → flavor combinations ud,  $\ell s$ , ss'→ static-light mesons  $[\bar{Q}\Gamma q]$ 

setting up on the lattice - we recycle

 $one m_f = 2 + 1$  full QCD,  $32^3 × 64$ , a = 0.090 fm,  $a^{-1} = 2.194$  GeV (PACS-CS gauges)  $one m_π = 164, 299, 415, 575, 707$  MeV ,  $m_s ≃ m_s^{phys}$ , propagators re-used from before

 $\circ~$  Quenched gauge a  $\simeq 0.1 {\rm fm},~~m_\pi^{\rm valence}=909\,{\rm MeV}$  , to match hep-lat/0509113

## Diquark spectroscopy - phenomenological estimates

We want to compare our results with phenomenology

- $\circ\,$  Key resource: (Jaffe '05, arXiv:hep-ph/0409065), updated with PDG 2021 input
- $\circ~$  For pheno estimates use charm and bottom hadron masses where leading  $\mathcal{O}(1/m_Q)~(Q=c,b)$  can be cancelled

Four estimates considered:

$$\circ \ \delta(1^{+} - 0^{+})_{ud} : \boxed{\frac{1}{3} \left(2M(\Sigma_{Q}^{*}) + M(\Sigma_{Q})\right) - M(\Lambda_{Q})}$$
  

$$\circ \ \delta(1^{+} - 0^{+})_{us} : \boxed{\frac{2}{3} \left(M(\Xi_{Q}^{*}) + M(\Sigma_{Q}) + M(\Omega_{Q})\right) - M(\Xi_{Q}) - M(\Xi_{Q}')}$$
  

$$\circ \ \delta(Q[ud]_{0^{+}} - \bar{Q}u) : \boxed{M(\Lambda_{Q}) - \frac{1}{4} \left(M(P_{Qu}) + 3M(V_{Qu})\right)}$$
  

$$\longrightarrow P_{Qu}, V_{Qu} \text{ are the ground-state, heavy-light mesons}$$
  

$$\circ \ \delta(Q[us]_{0^{+}} - \bar{Q}s) :$$

$$M(\Xi_Q) + M(\Xi'_Q) - \frac{1}{2}(M(\Sigma_Q) + M(\Omega_Q)) - \frac{1}{4}(M(P_{Qs}) + 3M(V_{Qs}))$$

 $\rightsquigarrow P_{\mathit{Qs}}, V_{\mathit{Qs}}$  are the ground-state, heavy-strange mesons

## $\Delta$ -Nucleon mass difference



Measured the mass difference of  $\Delta - N$ 

- Prediction:  $\delta(\Delta N) = 3/2 \times \delta(1^+ 0^+)_{ud}$
- $\circ~$  Same Ansatz as before
- $\circ$  Prediction holds well, even at fairly large  $m_{\pi}$

### A tunable system - opportunity together with pheno





 $\circ$  E.g. scans in  $m_{b'}$  map out the heavy quark mass dependence.

 $\circ$  Away from physical masses the binding mechanism can be probed.

 $\rightarrow$  Mass dependence can be confronted with model predictions.

 $\rightarrow$  System can be tuned continuously from the bound to the resonant or non-interacting regimes.

 $\rightarrow$  Requires robust control of finite volume spectrum.

Review of doubly heavy tetraquarks in lattice QCD

### Confirm and predict doubly heavy tetraquarks non-perturbatively

Tetraquarks as ground states? What would their binding mechanism/properties be?

# HQS-GDQ picture, consequences for $qq'\bar{Q}'\bar{Q}$ tetraquarks:

- $\circ J^P = 1^+$  ground state tetraquark below meson-meson threshold
- $\,\circ\,$  Deeper binding with heavier quarks in the  $\bar{Q}'\,\bar{Q}$  diquark
- $\circ~$  Deeper binding for lighter quarks in the qq' diquark

Ideal for lattice: Diquark dynamics and HQS could enable  $J^P = 1^+$  ground state doubly heavy tetraquarks with flavor content  $qq'\bar{Q}\bar{Q}'$ .

**Goal:**  $\Delta E = E_{\text{tetra}} - E_{\text{meson-meson}}$ , e.g. in  $bb\bar{u}\bar{d}$ ,  $bb\bar{\ell}\bar{s}$  and others  $\Rightarrow$  Verify, quantify predictions of binding mechanism in mind.

#### Lattice point of view

Hidden flavor qQq̄'Q̄ are tetraquark candidates as excitations of QQ̄'.
 → technical difficulty for lattice calculations, need to resolve many f.vol states.
 → qq'Q̄Q̄', i.e. ground state candidates would be better to handle.

In the following

- $\circ~$  Tetraquarks with two heavy (c, b) and two light ( $\ell,s)$  quarks.
- $\circ~{\sf Lattice}$  evidence for  $bb\bar u\bar d$  ,  $bb\bar\ell\bar s$  .
- $\circ~$  Recent updates on systematics.
- $\circ~$  Survey of candidates status.

## Lattice tetraquarks - 4 main approaches

<ol> <li>Static quarks (m<sub>Q</sub> = ∞) Fitted potentials used to predict bound states and resonances.</li> <li>Allows for potential formulation.</li> <li>Ansatz fitted to lattice data.</li> <li>Plug into Schrödinger Eq. for E<sub>n</sub>.</li> </ol>	<ul> <li>3. Finite volume energy levels Lattice energies equated to (un)observed states. <ul> <li>Operator matrix (GEVP) gives λ<sub>i</sub> ∝ E<sub>i</sub></li> <li>⇒ Finite volume states.</li> <li>&gt; Binding? Get ΔE = E<sub>0</sub> - E<sub>thresh</sub>.</li> <li>&gt; Mechanism? Vary quark masses.</li> <li>~→ AF et al. ('17,'18, '20), Hughes et al. ('17), Junnarkar et al. ('18), Leskovec et al. ('19), Mohanta et al. ('20)</li> </ul></li></ul>
<ul> <li>2. HAL QCD method</li> <li>Lattice potentials studied for scattering properties.</li> <li>Expansion of energy dependent potential (systematics?).</li> <li>Method under debate, best motivated for heavy systems.</li> </ul>	<ul> <li>4. Scattering analysis</li> <li>Lattice energies studied in terms of scattering phase shifts.</li> <li>○ Excited state energies via GEVP.</li> <li>○ Analyse fvol spectrum ⇒ Resonant, bound, virtual bound, free.</li> <li>~&gt;Hadron Spectrum Coll. ('18,'20)</li> </ul>

### Lattice tetraquarks - 4 step recipe

### The main tool is to adopt a variational approach

Lattice GEVP gives access to finite volume energy states (masses, overlaps).

**Beware:** Operator overlaps do not necessarily connect to the naively expected structures. Be careful when equating lattice correlators with trial-wave functions.

Step I: Set up a basis of operators, here  $J^P = 1^+$ 

Diquark-Antidiquark:

$$D = \left( (q_a)^T (C\gamma_5) q'_b \right) \times \left[ \bar{Q}_a (C\gamma_i) (\bar{Q'}_b)^T - a \leftrightarrow b \right]$$

Dimeson:

$$M = (\bar{b}_a \gamma_5 u_a) (\bar{b}_b \gamma_i d_b) - (\bar{b}_a \gamma_5 d_a) (\bar{b}_b \gamma_i u_b)$$

Step II: Solve the GEVP and fit the energies

$$\begin{aligned} F(t) &= \begin{pmatrix} G_{DD}(t) & G_{DM}(t) \\ G_{MD}(t) & G_{MM}(t) \end{pmatrix}, \quad F(t)\nu = \lambda(t)F(t_0)\nu , \\ G_{\mathcal{O}_1\mathcal{O}_2} &= \frac{C_{\mathcal{O}_1\mathcal{O}_2}(t)}{C_{PP}(t)C_{VV}(t)} , \ \lambda(t) = Ae^{-\Delta E(t-t_0)} . \\ &\simeq \Delta E = E_{\text{lotra}} - E_{\text{hresch}} \text{ in case of binding correlator } (C_{\mathcal{O}_1\mathcal{O}_2}(t))/(C_{PP}(t)C_{VV}(t)). \end{aligned}$$

Most use these operators, but a larger basis has been worked out.

 $\Rightarrow$  Need to be used by more groups.

→ HadronSpectrum Coll. ('17)

Step III: Finite volume corrections

Large energy shifts are possible due to the finite lattice volume.



With a single volume available:

- $\circ$  In a bound state corrections are  $\sim \exp(binding momentum)$ 
  - $\rightsquigarrow$  strong supp.  $\mathit{m}_{had}$  =heavy
- In a scattering state expect large deviation around threshold

With multiple volumes available:

- $\circ$  Track mass dependence  $\leadsto$  decide bound/scatt. state
- Power law corrections might be too small to resolve

Step IV: Finite volume / Scattering analysis

Limitation: Small GEVP without f.vol analysis ok for deeply bound states. Insufficient to tell apart free, resonant or virtual bd. states.

**Extension:** Connect energies to scattering phase shifts via finite volume quantisation conditions (Lüscher-formalism).



 $\circ\,$  connect (many) f.vol states to scattering parameters (sketch: BW)

 $\circ\,$  resonance: extra state(s) appear, lowest state close to threshold

What we know: A review of recent lattice studies

# What we know: Deeply bound $J^P = 1^+ bb\bar{u}\bar{d}$ and $bb\bar{\ell}\bar{s}$ tetraquarks





· Colquhoun, AF, Hudspith, Lewis, Maltman ('17, '18, '20)

## Overview -possible doubly heavy tetraquark candidates

observed (>1 group) no deep binding observed (1 group) not confirmed (>1 grou	ıp)
channel	deeply bound
$J^P = 1^+$	bbūd bcūd bbls bcls bsūd csūd bbūc bbsc ccūd ccls bbbb
$J^{P} = 0^{+}$	bbūū ccūū bbūd bcūd bbls bcls bbsīs ccīs bsūd csūd bbūc bbsīc bbūc ccūd bbbīb

Surveying candidates

Deeply bound states
Focus: strong interaction stable
('17), Junnarkar et al. ('18), Leskovec et al. ('19), Mohanta et al. ('20)
States above threshold, resonances?
$ \begin{array}{l} \rightarrow bb\bar{u}\bar{d} \mbox{ in } J^P = 1^+ \mbox{ /w static quarks find a} \\ \mbox{ resonance just above threshold. } & \sim_{\rm Bicudo \mbox{ et al. ('19)}} \\ \rightarrow \mbox{ No results from other approaches. } \\ \rightarrow \mbox{ What about } cs\bar{u}\bar{d} \mbox{ ?} \end{array} $

#### Shallow binding?

 $\circ cc\bar{u}\bar{d}$  now observed by LHCb, robust lattice post-diction?

 $\rightarrow$  Work to remove current limitations.