Electromagnetic interaction of baryon resonances in the timelike region studied via the reaction

 $\pi N o N e^+ e^-$

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Outline

- Introduction
- $\pi N
 ightarrow N e^+ e^-$ in helicity formalism
 - Polarization & anisotropy from symmerties
- Effective Lagrangian model
- Comparison to new results from HADES

Introduction

EM transition form factors of baryon resonances



Resonance polarization - density matrices

Creation and decay of a resonance:

$$\mathcal{M}_{fi} = \sum_{\lambda} \left\langle f \left| T_{R
ightarrow f}
ight| R(\lambda)
ight
angle \left\langle R(\lambda) \left| T_{i
ightarrow R}
ight| i
ight
angle^{-i}$$
 .

Squared amplitude (weighted average over initial polarization):

$$\sum_{i} P_{i} |\mathcal{M}_{fi}|^{2} = \sum_{\lambda,\lambda'}
ho_{\lambda\lambda'}^{\mathrm{cre}}
ho_{\lambda\lambda'}^{\mathrm{dec}} \quad \text{ c.f. } \langle \mathcal{O}
angle = \mathrm{Tr}\left(
ho \, \mathcal{O}
ight) \quad
ho \sim
ho_{\lambda\lambda'}^{\mathrm{cre}} \quad rac{\mathrm{polarization state}}{\mathrm{of \ the \ resonance}}$$

Polarization density matrices:

$$\mathcal{O} \sim
ho_{\lambda'\lambda}^{
m dec}$$

 $R(\lambda)$

measured quantity → angular distribution of decay products

$$egin{aligned} &
ho_{\lambda\lambda'}^{ ext{cre}} = \sum_i P_i \left\langle R(\lambda) \left| T_{i
ightarrow R}
ight| i
ight
angle \left\langle i \left| T_{i
ightarrow R}^{\dagger}
ight| R(\lambda')
ight
angle \ &
ho_{\lambda'\lambda}^{ ext{dec}} = \left\langle R(\lambda') \left| T_{R
ightarrow f}^{\dagger}
ight| f
ight
angle \left\langle f \left| T_{R
ightarrow f}
ight| R(\lambda)
ight
angle \end{aligned}$$

The process $\pi N o N e^+ e^-$



Important contribution: baryon resonance in the *s*-channel

3 steps - 2 intermediate resonances

- baryon resonance R (N* or Δ)
- vector particle (ϱ or γ^*)

each of the 3 steps is a 1 \rightarrow 2 or 2 \rightarrow 1 process $\pi + N \rightarrow R$ preparation of resonance state $R \rightarrow N + \gamma^*$ E.M. transition of resonance $\gamma^* \rightarrow e^+e^-$ "analyser"







Two independent helicity amplitudes:

$$egin{aligned} &A_0\equiv F^1_{rac{1}{2},rac{1}{2}}=F^1_{-rac{1}{2},-rac{1}{2}}\ &A_1\equiv F^1_{rac{1}{2},-rac{1}{2}}=F^1_{-rac{1}{2},rac{1}{2}} \end{aligned}$$

They satisfy the QED relation:

$$rac{A_0}{A_1} = -\sqrt{2}rac{m_e}{m_{\gamma^*}}$$

$$egin{aligned} & \gamma^*
ightarrow e^+ e^- & - ext{decay density matrix:} \ &
ho_{\lambda',\lambda}^{ ext{dec}} \propto egin{pmatrix} 1 + \cos^2 heta_e + lpha & -\sqrt{2}\cos heta_e\sin heta_e e^{-i\phi_e} & \sin^2 heta_e e^{-2i\phi_e} \ -\sqrt{2}\cos heta_e\sin heta_e e^{i\phi_e} & 2(1 - \cos^2 heta_e) + lpha & \sqrt{2}\cos heta_e\sin heta_e e^{-i\phi_e} \ & \sin^2 heta_e e^{2i\phi_e} & \sqrt{2}\cos heta_e\sin heta_e e^{i\phi_e} & 1 + \cos^2 heta_e + lpha \end{pmatrix} \qquad lpha = rac{2m_e^2}{|\mathbf{k}_e|^2} \end{aligned}$$

Angular distribution of the lepton pair:

$$\sum_{\lambda,\lambda'} \rho_{\lambda\lambda'}^{cre} \rho_{\lambda\lambda'}^{dec} \propto (1 + \cos^2 \theta_e) \left(\rho_{1,1}^{cre} + \rho_{-1,-1}^{cre} \right) + 2 \sin^2 \theta_e \rho_{0,0}^{cre}$$

$$+ \sqrt{2} \sin 2\theta_e \left[\cos \phi_e (\operatorname{Re} \rho_{1,0}^{cre} - \operatorname{Re} \rho_{-1,0}^{cre}) \right]$$

$$+ \sin \phi_e (\operatorname{Im} \rho_{1,0}^{cre} + \operatorname{Im} \rho_{-1,0}^{cre}) \right]$$

$$+ 2 \sin^2 \theta_e \left(\cos 2\phi_e \operatorname{Re} \rho_{1,-1}^{cre} + \sin 2\phi_e \operatorname{Im} \rho_{1,-1}^{cre} \right)$$

$$we can obtain \rho_{\lambda\lambda'}^{cre} via fitting the experimental angular distribution to the experimental angular di$$

$$\begin{array}{l} 1 \longrightarrow 2 \text{ processes} \\ \text{Wigner-Eckart theorem for transition amplitude } R \longrightarrow 1+2: \\ & \left\langle \mathbf{p}s_{1}\lambda_{1}; -\mathbf{p}s_{2}\lambda_{2} \left| T_{R \rightarrow 1+2} \right| \mathbf{p}_{R} = 0, \ JM \right\rangle = \sqrt{\frac{2J+1}{4\pi}} F_{\lambda_{1}\lambda_{2}}^{J} D_{M,\lambda_{1}-\lambda_{2}}^{J}(\Omega)^{*} \\ \text{Restrictions on helicity amplitudes:} \\ & \text{from Wigner matrix } D_{M,\lambda_{1}-\lambda_{2}}^{J}(\Omega): \ -J \leq \lambda_{1} - \lambda_{2} \leq J \\ & \text{from parity conservation:} \ F_{\lambda_{1}\lambda_{2}}^{J} = \eta_{R}\eta_{1}\eta_{2}(-1)^{J-s_{1}-s_{2}}F_{-\lambda_{1},-\lambda_{2}}^{J} \\ R \rightarrow N + \gamma^{*}: \\ \text{3 independent} \\ & \text{helicity amplitudes} \\ & \text{for J} \geq 3/2 \text{ resonances:} \end{array} \right. \begin{array}{l} \text{Migner matrix } D_{M,\lambda_{1}-\lambda_{2}}^{J}(\Omega) = \pm F_{0,\frac{1}{2}}^{J} \\ & \text{C}_{1/2} \equiv F_{1,\frac{1}{2}}^{J} = \pm F_{-1,-\frac{1}{2}}^{J} \\ & \text{C}_{1/2} \to 0 \quad \text{when} \quad m_{\gamma^{*}} \rightarrow 0 \\ & \text{(real photons are transverse)} \end{array}$$

0.2

0

 $\cos \theta_{\gamma^\star}$

0.4 0.6 0.8

1

$$\begin{split} R &\to N + \gamma^* \quad \text{- creation density matrix:} \\ \rho_{\lambda\lambda'}^{\text{cre}} &\propto \sum_{\lambda_R,\lambda_N} F_{\lambda\lambda_N}^J F_{\lambda'\lambda_N}^{J*} P_{\lambda_R} D_{\lambda_R,\lambda-\lambda_N}^J(\Omega)^* D_{\lambda_R,\lambda'-\lambda_N}^J(\Omega) \\ \text{Unpolarized } J &= 3/2^- \text{ baryon resonance [e.g. $N(1520)]:} \\ \rho_{\lambda,\lambda'}^{\text{cre},3/2} &= \mathcal{N} \begin{pmatrix} A_{1/2}^2 + 3\left(A_{1/2}^2\cos^2\theta + A_{3/2}^2\sin^2\theta\right) & -\sqrt{3}A_{3/2}C_{1/2}\sin 2\theta & 2\sqrt{3}A_{1/2}A_{3/2}\sin^2\theta \\ -\sqrt{3}A_{3/2}C_{1/2}\sin 2\theta & C_{1/2}^2(5 + 3\cos 2\theta) & \sqrt{3}A_{3/2}C_{1/2}\sin 2\theta \\ 2\sqrt{3}A_{1/2}A_{3/2}\sin^2\theta & \sqrt{3}A_{3/2}C_{1/2}\sin 2\theta & A_{1/2}^2 + 3\left(A_{1/2}^2\cos^2\theta + A_{3/2}^2\sin^2\theta\right) \\ \text{E.g. if } A_{3/2} &= A_{1/2} = C_{1/2}: \end{split}$$

 $\cos\theta_{\gamma^{\star}}$

 $7/2^{-}$

0.6 0.8

1

0.2 0.4

 $\cos \theta_{\gamma^{\star}}$

⁻¹

-0.8 -0.6 -0.4 -0.2 0

All contributions to the process $\pi N
ightarrow N e^+ e^-$:

Born terms





Consistent interaction scheme for $J \ge 3/2$ resonances:

$$egin{aligned} \mathcal{L}_{R_{3/2}N
ho}^{(1)} &= rac{ig_1}{4m_N^2} ar{\Psi}_R^{\mu} ec{ au} \, \Gamma \gamma^{
u} \psi_N \cdot ec{
ho}_{
u \mu} + ext{h.c.} \ \mathcal{L}_{R_{3/2}N
ho}^{(2)} &= -rac{g_2}{8m_N^3} ar{\Psi}_R^{\mu} ec{ au} \, \Gamma \partial^{
u} \psi_N \cdot ec{
ho}_{
u \mu} + ext{h.c.} \ \mathcal{L}_{R_{3/2}N
ho}^{(3)} &= -rac{g_3}{8m_N^3} ar{\Psi}_R^{\mu} ec{ au} \, \Gamma \psi_N \partial^{
u} \cdot ec{
ho}_{
u \mu} + ext{h.c.}, \end{aligned}$$

• coupling constants from
$$R o N
ho$$
 branching ratios (HADES, $\pi N o N\pi\pi$ [Phys. Rev. C 102 (2020) 024001])

- analogous Lagrangians for $RN\gamma$ coupling
- VMD1: relative phase of ρ and direct γ contribution is not fixed \rightarrow various interference patterns
- ρ contribution is important although we are below threshold

$$\Psi^{\mu}_{R}=i\gamma_{
u}(\partial^{\mu}\psi^{
u}_{R}-\partial^{
u}\psi^{\mu}_{R})$$

[V. Pascalutsa, Phys. Rev. D 58 (1998) 096002;T. Vrancx, et al. Phys. Rev. C 84 (2011) 045201]



Differential cross section of e^+e^- production

- dominant sources are Born and N(1520)
- error bands: uncertainty of resonance widths and branching ratios
- relative phase of *ρ* and direct *γ* has a strong influence



Density matrix elements



- Born and N(1520) contributions have similar shapes
- longitudinal polarization disappears as $\, m_{
 m inv}
 ightarrow 0 \,$

HADES results

Quasifree $\pi^- p ightarrow n e^+ e^-$ by HADES

[R. Abou Yassine et al., e-Print: 2205.15914 [nucl-ex] (2022)]

Polarization density matrix elements:

- extracted from experiment via fitting $d^4\sigma/d\cos\theta_{\gamma^*} dM_{e^+e^-} d\cos\theta_e d\phi_e$ for $M_{e^+e^-} > 300 \,\mathrm{MeV}/c^2$ and 3 bins in $\cos\theta_{\gamma^*}$
- ~ consistent with effective Lagr. model (dominance of N(1520) and Born terms)



HADES results

Quasifree $\pi^- p ightarrow n e^+ e^-$ by HADES



Differential cross section vs. models

- large excess compared to QED [pointlike N(1520) and N(1535)] for M_{e+e-} > 200 MeV
- ▲ and ▼: reconstructed from π⁻p → nρ⁰ [known from PWA of π⁻p → nπ⁺π⁻] using two versions of VMD
- Covariant Spectator Quark model
 [G. Ramalho, T. Pena, Phys. Rev. D 95, 014003 (2017)]
- effective Lagrangian model with φ_{ρNR} = 90°
 (~ incoherent sum)
 [M. Z., D. Nitt, M. Buballa, T. Galatyuk, Phys. Rev. C 104, 015201 (2021)]

Summary

- Quasifree $\pi^- p
 ightarrow ne^+e^-$ measured at $\sqrt{s}=$ 1.49 GeV $\,$ by HADES
- Related to $\pi^- p
 ightarrow n \pi^+ \pi^-$ by vector meson dominance (VMD)
- Spin density matrix elements (= polarization state) of γ^* accessible in the experiment
- Differential cross section confronted with various models
 - timelike e.m. transition of the relevant baryon resonances
 - various versions of VMD
- Plans for higher energies

Thank You!

R. Abou Yassine et al. (HADES Collaboration & M.Z.), e-Print: 2205.15914 [nucl-ex] (2022)
M. Z., D. Nitt, M. Buballa, T. Galatyuk, Phys. Rev. C 104, 015201 (2021)
E. Speranza, M. Z., B. Friman, Phys. Lett. B 764, 282 (2017)
M. Z., Gy. Wolf, Phys. Rev. C 86, 065209 (2012)
B. Zhang, M. Z., in preparation

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Members of HADES: Piotr Salabura, Beatrice Ramstein, Tetyana Galatyuk **HADES** results

Quasifree $\pi^- p ightarrow n e^+ e^-$ by HADES

[R. Abou Yassine et al., e-Print: 2205.15914 [nucl-ex] (2022)]

- π^- beam: p_{π} = 0.658 GeV ($\sqrt{s_{\pi N}}$ = 1.49 GeV)
- targets: polyethylene (CH₂), carbon (C)
- missing mass cut: select exclusive ne^+e^-
- difference of CH₂ and C \rightarrow free $\pi^- p \rightarrow n e^+ e^-$
- low statistics for carbon target \rightarrow quasifree $\pi^- p \rightarrow n e^+ e^-$: $\pi^- + CH_2$ & effective proton number



HADES results

Quasifree $\pi^- p ightarrow n e^+ e^-$ by HADES



Differential cross section vs. models

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- ▲ and ▼: reconstructed from π⁻p → nρ⁰ [known from PWA of π⁻p → nπ⁺π⁻
 (Bonn-Gatchina, HADES data)], via

$$\circ$$
 VMD1: $\Gamma(M_{e^+e^-})=\Gamma_0rac{M_{e^+e^-}}{M_0}$

$$\circ$$
 VMD2: $\Gamma(M_{e^+e^-})=\Gamma_0igg(rac{M_0}{M_{e^+e^-}}igg)^3$