

From nuclear interactions to binary neutron star mergers

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University of Pisa

QFC2022- Quantum gases, fundamental interactions and cosmology

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UNIVERSITÀ DI PISA

Results in collaboration with:

- I. Bombaci (University of Pisa)
- I. Vidaña (INFN Catania)
- A. Perego (University of Trento)
- D. Radice (Penn State University)
- S. Bernuzzi (Jena University)
- A. Prakash (Penn State University)...

Hopefully very soon: results from new collaborations...

- EOS for neutron star matter
- Nuclear interactions and nuclear matter calculations
- The nuclear many-body problem
- EOS for cold nucleonic and hyperonic matter
- Open problems: Hyperon-puzzle in neutron stars and connection with hypernuclei
- Applications to binary neutron star mergers

- What do we mean by EOS?
- A relation between: $(n_B, T, P, \epsilon, \{X_i\})$
- n_B : baryonic density
- T : temperature
- P : pressure
- ϵ : energy density
- $\{X_i\}$: composition

- What do we mean by EOS of neutron star matter?
- A relation between: $(n_B, T, P, \epsilon, \{X_i\})$
- n_B : range: $(10^{-13} - 1.5) \text{ fm}^{-3}$
- T : range: $(0 - 100) \text{ MeV}$
- P : range: $(\sim 0 - 10^{38}) \text{ dyne cm}^{-2}$
- ϵ : range: $(1 - 10^{17}) \text{ g cm}^{-3}$
- $\{X_i\}$: n, p, e^- , μ^- , hyperons(?), quarks(?)

Brute force lattice QCD calculation

- In principle the best way \Rightarrow really ab-initio
- Problems:
- \Rightarrow no unique way to define a "potential"
- \Rightarrow extremely challenging from a computational point of view

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Phenomenological interactions

- Describe very well NN-phase shifts and several nuclear observables
- "Problems":
- \Rightarrow Phenomenological...not very satisfactory from a theoretical point of view
- \Rightarrow Many-body forces "seem" included just as a way to improve models

Derivation of nuclear interaction

Brute force lattice QCD calculation: HAL QCD

- In principle the best way \Rightarrow really ab-initio
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Phenomenological interactions

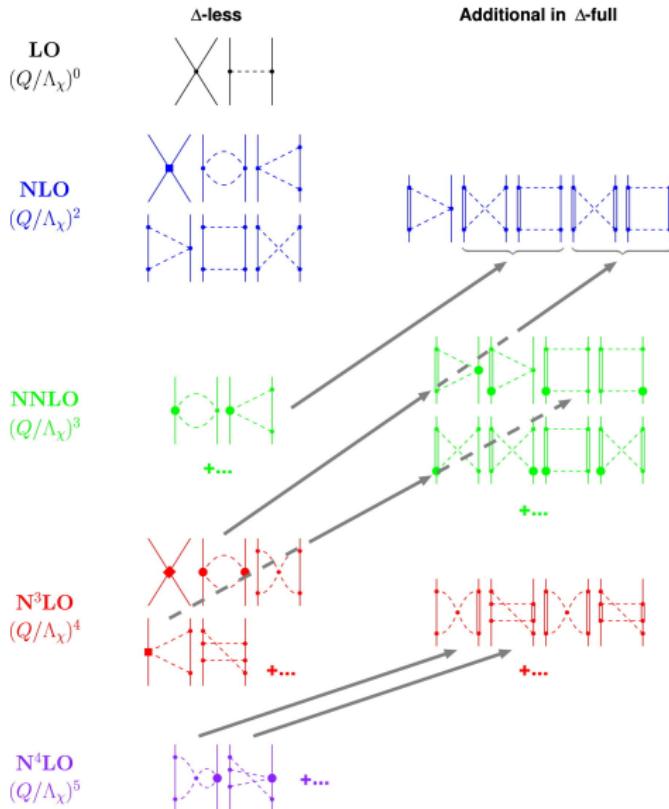
- Describe very well NN-phase shifts and several nuclear observables
- "Problems":
- \Rightarrow Phenomenological or based on one meson exchange...not very satisfactory from a theoretical point of view
- \Rightarrow Many-body forces "seem" included just as a way to improve models

Interactions from ChEFT

- Developed on a well defined theoretical framework
- Many-body forces appear naturally in the theory
- "Problems":
- \Rightarrow Treatment of many-body forces quite involving
- \Rightarrow Issues about renormalization of the theory...



Chiral 2N Force



Chiral 3N Force

LO
 $(Q/\Lambda_\chi)^0$

Δ -less

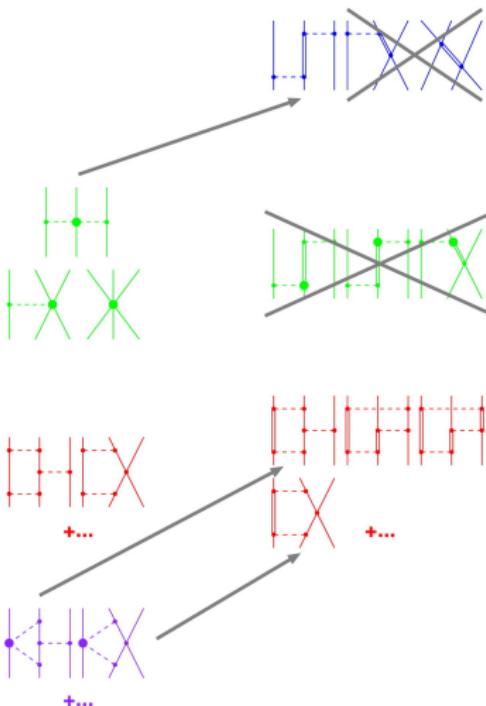
Additional in Δ -full

NLO
 $(Q/\Lambda_\chi)^2$

NNLO
 $(Q/\Lambda_\chi)^3$

N^3LO
 $(Q/\Lambda_\chi)^4$

N^4LO
 $(Q/\Lambda_\chi)^5$



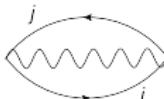
Ladder diagrams summation:

$$i \circlearrowleft \cdots \circlearrowleft j + i \circlearrowleft \bar{k} \bar{l} \bar{j} \circlearrowright + i \circlearrowleft \bar{m} \bar{n} \bar{j} \circlearrowright + i \circlearrowleft \bar{m} \bar{n} \bar{p} \bar{q} \bar{j} \circlearrowright + \dots = i \circlearrowleft \text{wavy line} \circlearrowright j$$

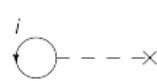
1st-order, 2nd-order and 3rd-order contributions:



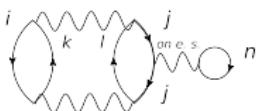
(a)



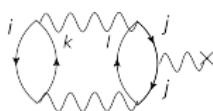
(b)



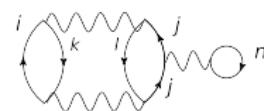
(c)



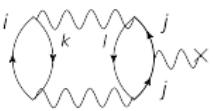
(d)



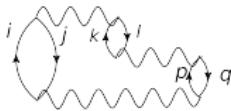
(e)



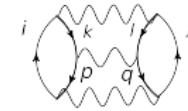
(f)



(g)



(h)



(i)

The Brueckner-Hartree-Fock approach

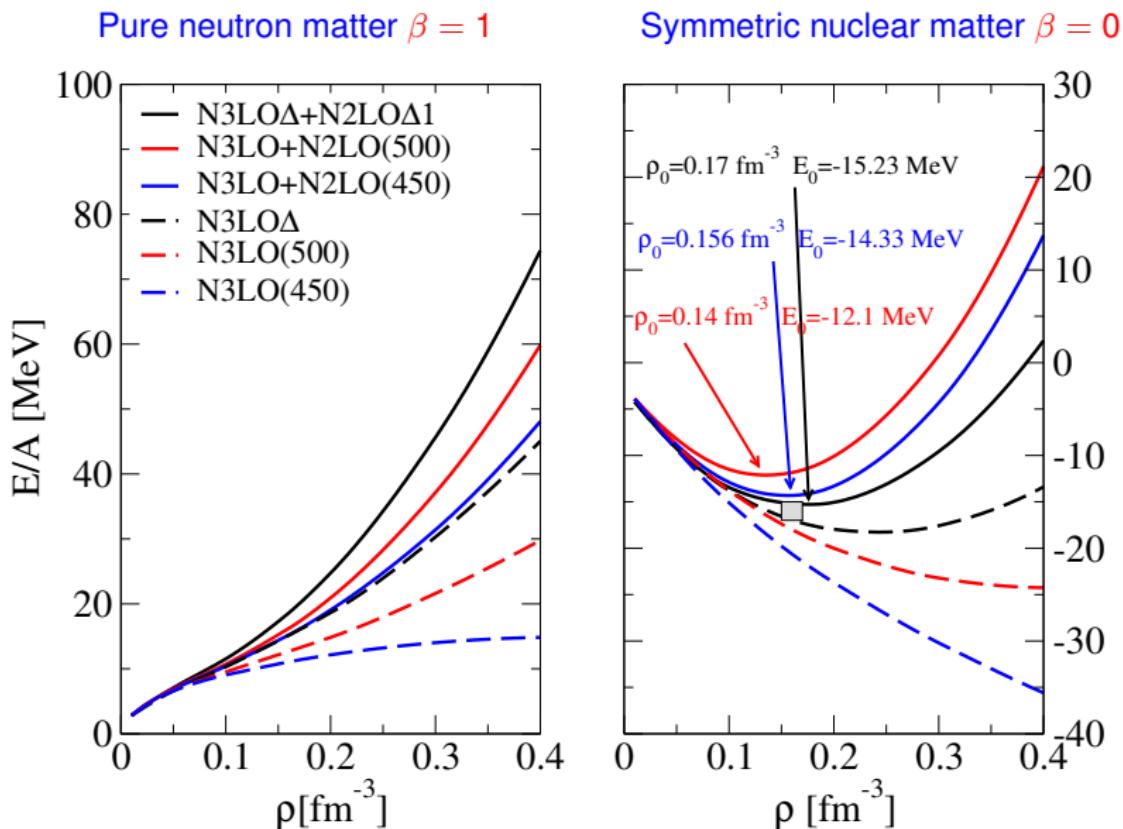
- Starting point: the Bethe-Goldstone equation

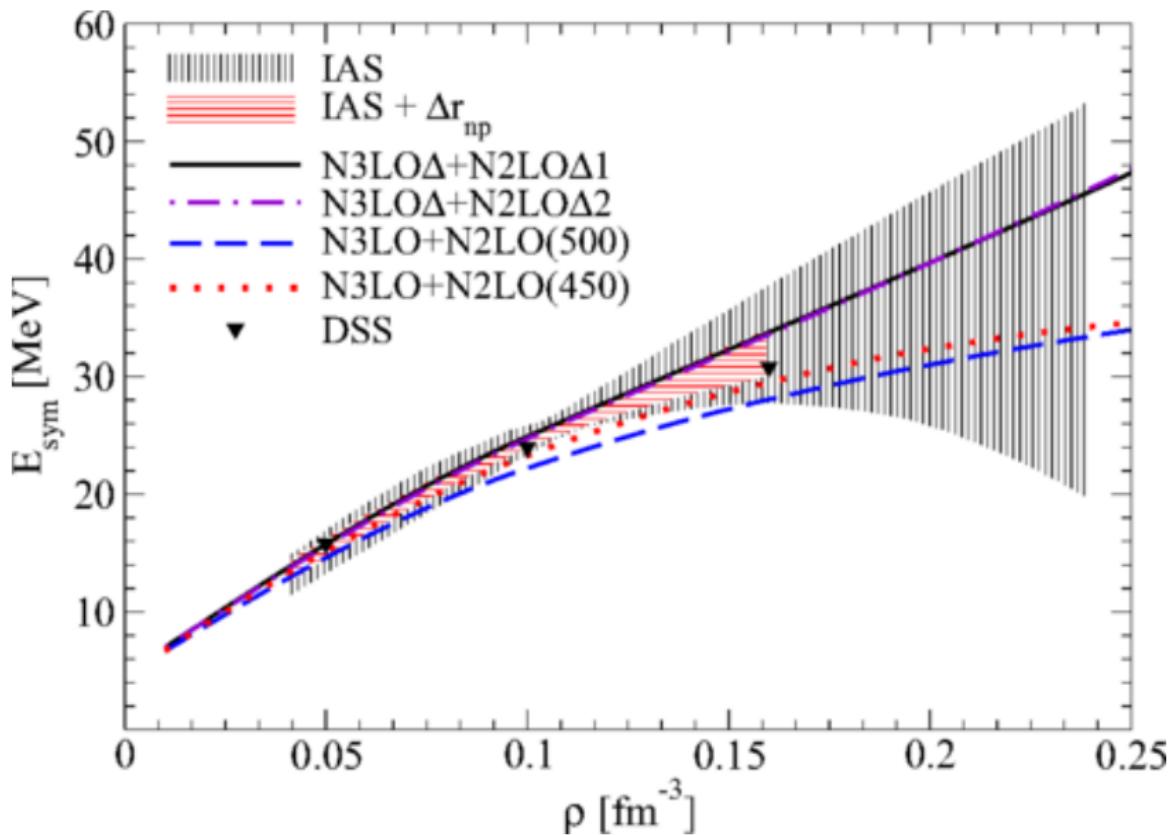
$$G(\omega)_{B_1 B_2, B_3 B_4} = V_{B_1 B_2, B_3 B_4} + \sum_{B_i B_j} V_{B_1 B_2, B_i B_j} \times \frac{Q_{B_i B_j}}{\omega - E_{B_i} - E_{B_j} + i\eta} G(\omega)_{B_i B_j, B_3 B_4}$$

$$U_{B_i}(k) = \sum_{B_j} \sum_{\vec{k}'} n_{B_j}(|\vec{k}'|) \times \langle \vec{k} \vec{k}' | G(E_{B_i}(\vec{k}) + E_{B_j}(\vec{k}'))_{B_i B_j, B_i B_j} | \vec{k} \vec{k}' \rangle_{\mathcal{A}}$$

$$E_{B_i}(k) = M_{B_i} + \frac{\hbar^2 k^2}{2M_{B_i}} + Re[U_{B_i}(k)]$$

$$\frac{E}{A_{BHF}} = \frac{1}{AV} \sum_{B_i} \sum_{k \leq k_{F_i}} \left[M_{B_i} + \frac{\hbar^2 k^2}{2M_{B_i}} + \frac{1}{2} Re[U_{B_i}(k)] \right]$$





Equation of state for cold neutron stars (T=0)

$$E/A(\beta, n_B) = E/A_{snm}(n_B) + E_{sym}(n_B)\beta^2 \quad \beta = \frac{n_n - n_p}{n_n + n_p}$$

$$E_{sym}(n_B) = E/A_{pnm}(n_B) - E/A_{snm}(n_B)$$

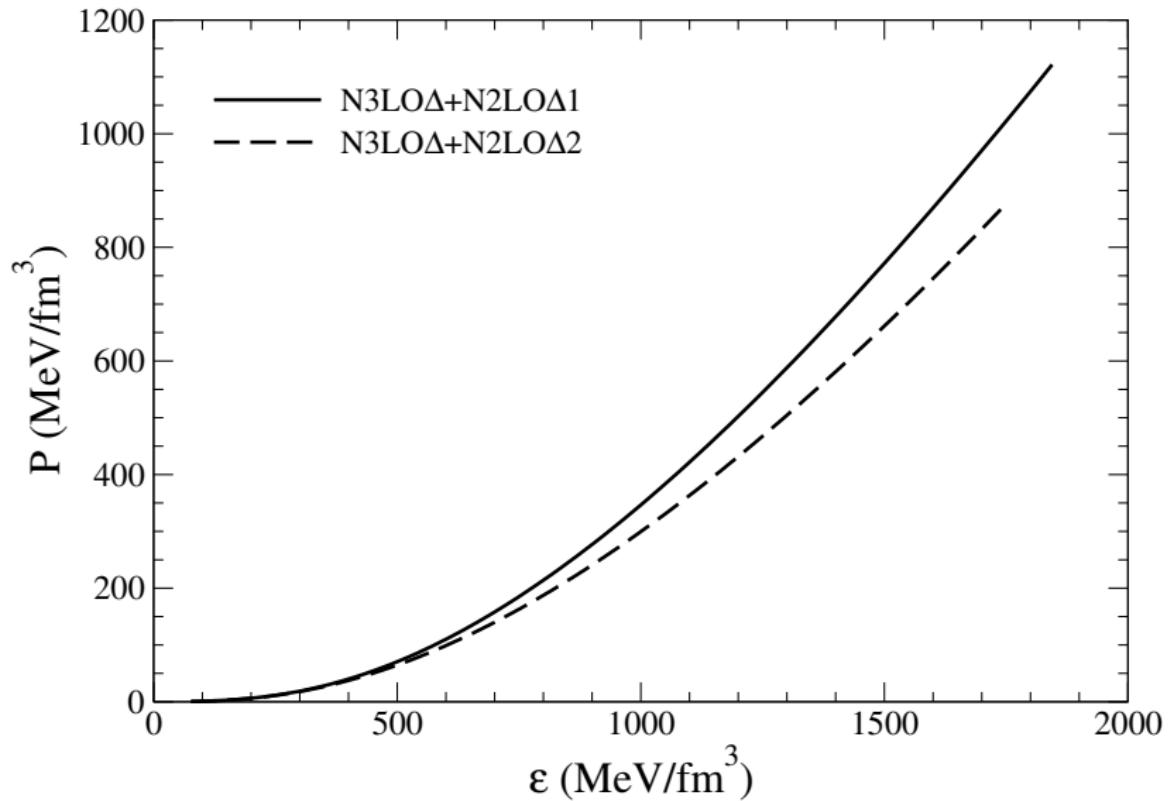
$$\mu_i = \frac{\partial(n_B E/A(\beta, n_B))}{\partial n_i} \quad n_B = n_n + n_p$$

- Chemical equilibrium:

$$\mu_n - \mu_p = \mu_e \quad \mu_e = \mu_\mu$$

- Charge neutrality:

$$n_p - n_\mu - n_e = 0.$$

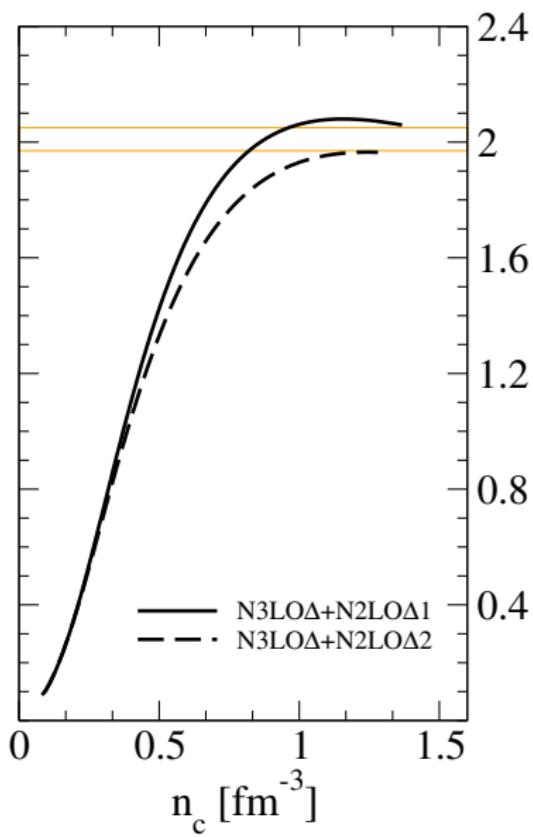
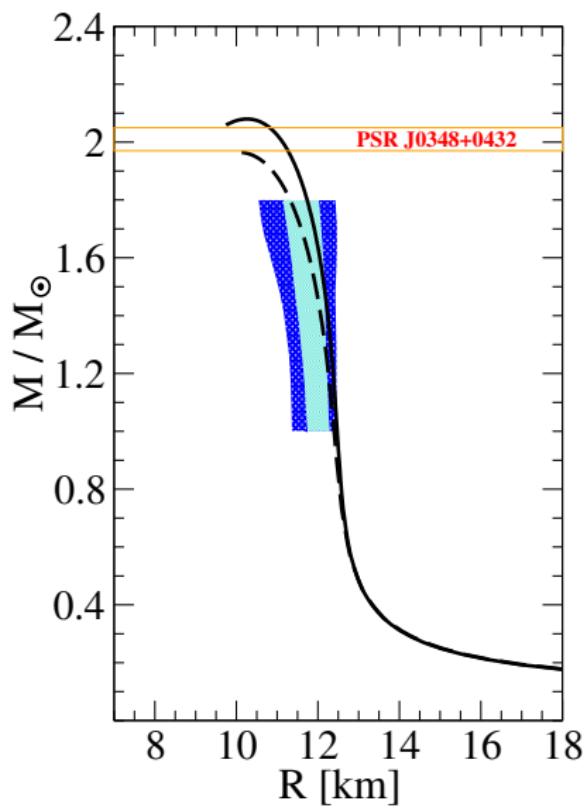


- Neutron stars have a very strong gravitational field \Rightarrow their structure is described by General theory of relativity.
- Equations of hydrostatic equilibrium in general relativity of Tolman-Oppenheimer-Volkoff (TOV):

$$\frac{dP}{dr} = -\frac{G\rho m}{r^2} \left(1 + \frac{P}{\rho c^2}\right) \left(1 + \frac{4\pi Pr^3}{mc^2}\right) \left(1 - \frac{2Gm}{rc^2}\right)^{-1},$$
$$\frac{dm(r)}{dr} = 4\pi r^2 \rho.$$

- Fixed an EOS and a value of the central pressure value P_c TOV equations are solved numerically.
- Output $\Rightarrow M_G(R)$, $M_G(P_c)$ (or $M_G(M_B)$)
- $M_B = m_u \int n_B(r)dV$, $m_u = (m_n + m_p)/2$

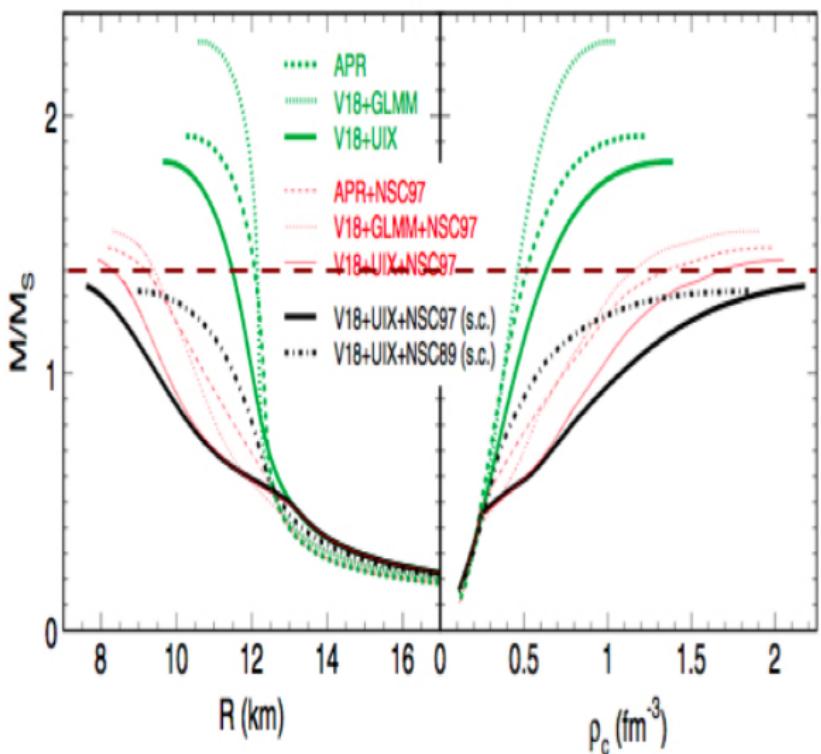
Neutron stars based on N3LO Δ +N2LO Δ (case of nucleonic matter)



I. Bombaci and D. Logoteta **A&A 609, A128 (2018)**

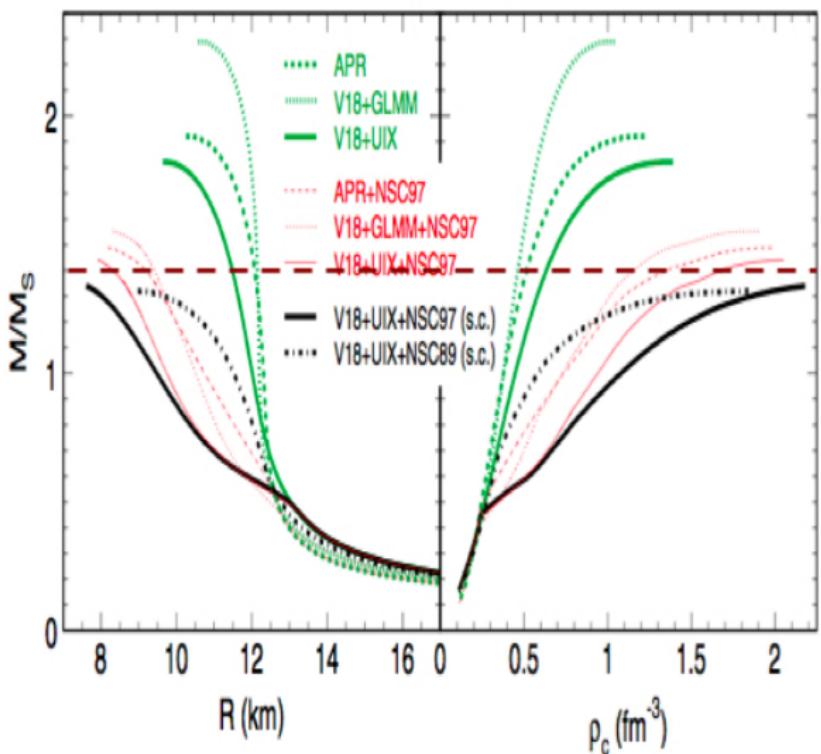
The problem of the maximum mass of neutron stars with microscopic approaches

H.-J. Schulze et al. Phys. Rev. C 73, 058801 (2006)



The problem of the maximum mass of neutron stars with microscopic approaches

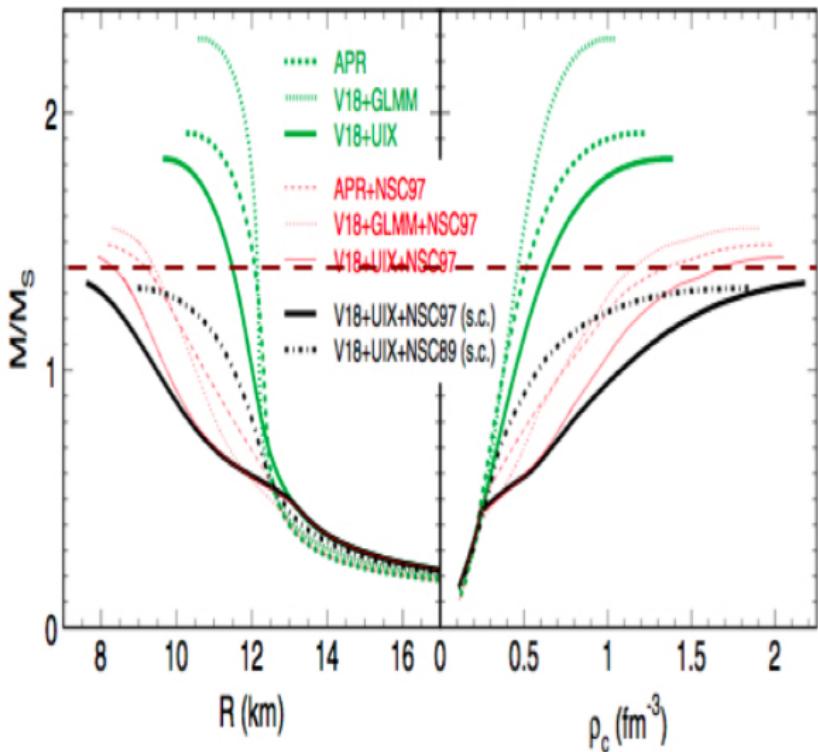
H.-J. Schulze et al. Phys. Rev. C 73, 058801 (2006)



- $n + n \rightarrow n + \Lambda$
- $n + n \rightarrow p + \Sigma^-$
- $p + e^- \rightarrow \Lambda + \nu_{e^-}$
- $n + e^- \rightarrow \Sigma^- + \nu_{e^-}$

The problem of the maximum mass of neutron stars with microscopic approaches

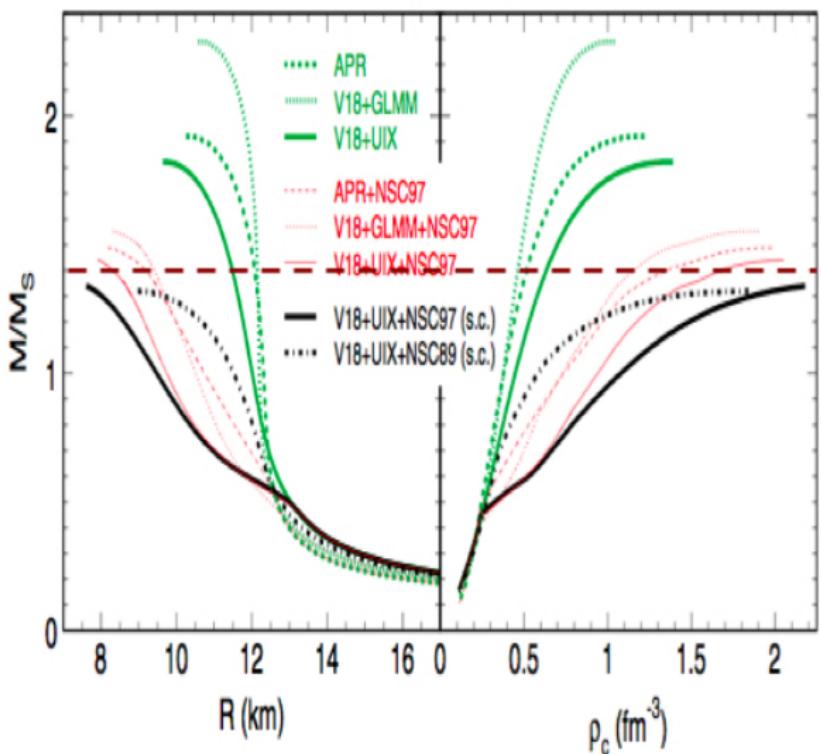
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- Recent measurements:
- $M^{J1614-2230} = 1.97 \pm 0.04 M_{\odot}$
- $M^{J0348+0432} = 2.01 \pm 0.04 M_{\odot}$
- $M^{J0740+6620} = 2.14^{+0.20}_{-0.18} M_{\odot}$

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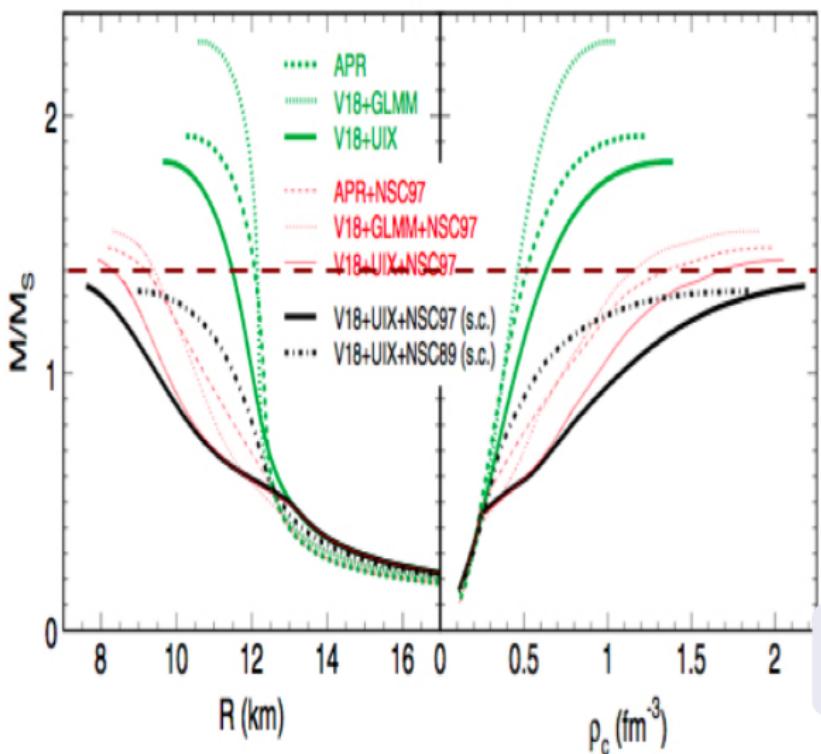
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DRAMMATIC SCENARIO!!

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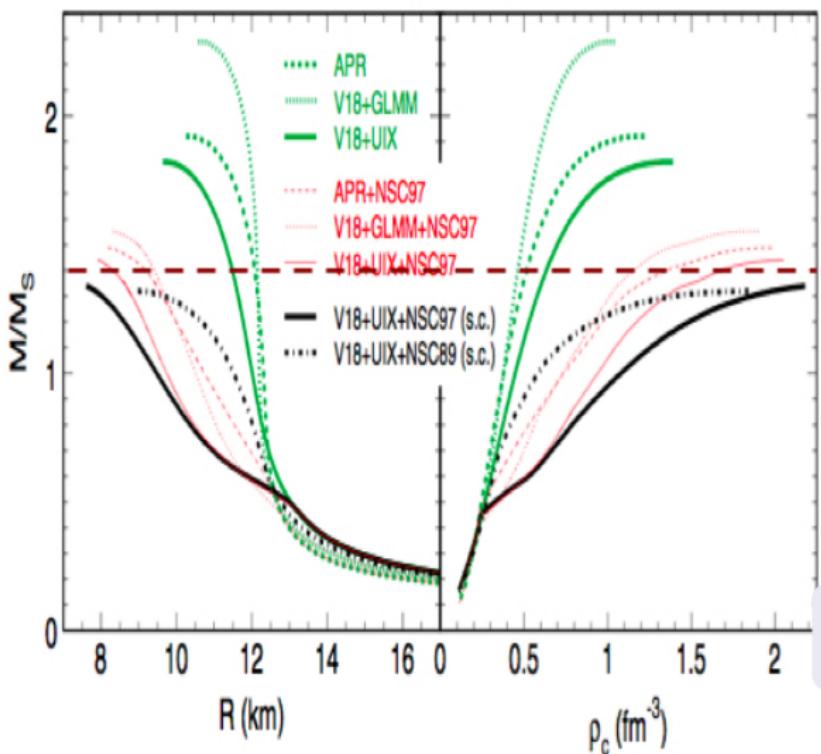


DRAMMATIC SCENARIO!!

NNY, NYY and YYY may help??

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H.-J. Schulze et al. Phys. Rev. C 73, 058801 (2006)

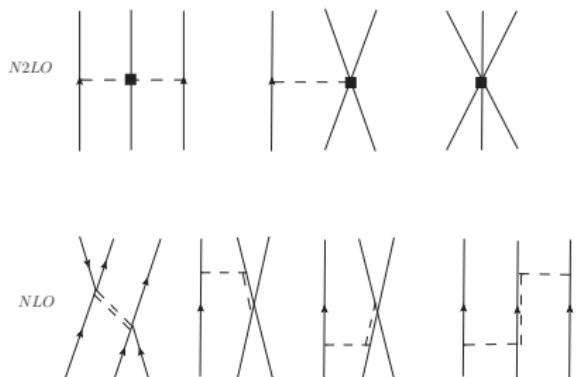


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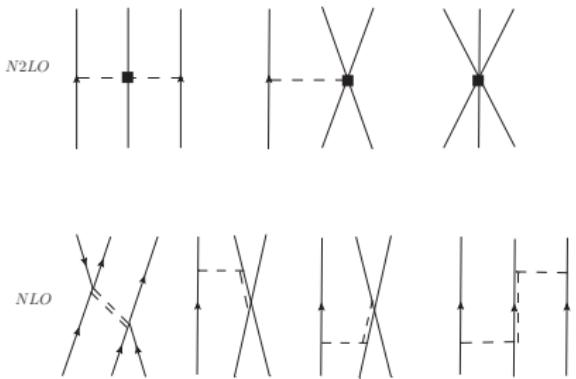
DRAMMATIC SCENARIO!!

We focused on the **NNA** interactions



- Up to N2LO just 1 LEC \Rightarrow fixed to $U_\Lambda(k=0) = (-28, -30)$ MeV

- Following Petschauer (2013)
- Baryonic three-body forces from chiral effective field theory
- Nonvanishing leading order contributions at order NLO and N2LO
- Same strategy used for nuclear matter
- Effective NN Λ interaction from bare NN Λ force
- Low energy constants estimated from decuplet saturation



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- Separation energies of heavy hypernuclei improve!

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- Effective NN Λ interaction from bare NN Λ force
- Low energy constants estimated from decuplet saturation

- Asymmetric matter:

$E/A(\beta, \rho)$ calculated for several values of $\beta = \frac{n_n - n_p}{n_n + n_p}$

$$\mu_i = \frac{\partial(n_B E/A(\beta, n_B))}{\partial n_i} \quad n_B = n_n + n_p + n_\Lambda$$

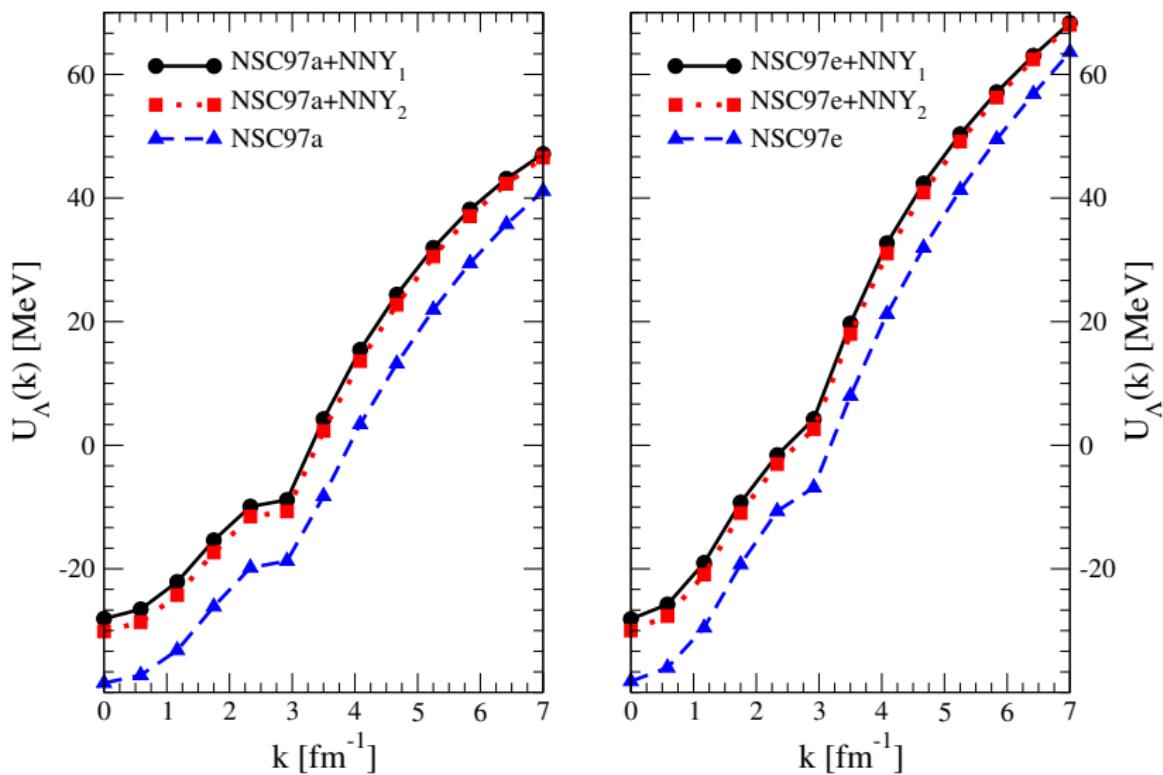
- Chemical equilibrium:

$$\mu_n - \mu_p = \mu_e \quad \mu_e = \mu_\mu \quad \mu_n = \mu_\Lambda$$

- Charge neutrality:

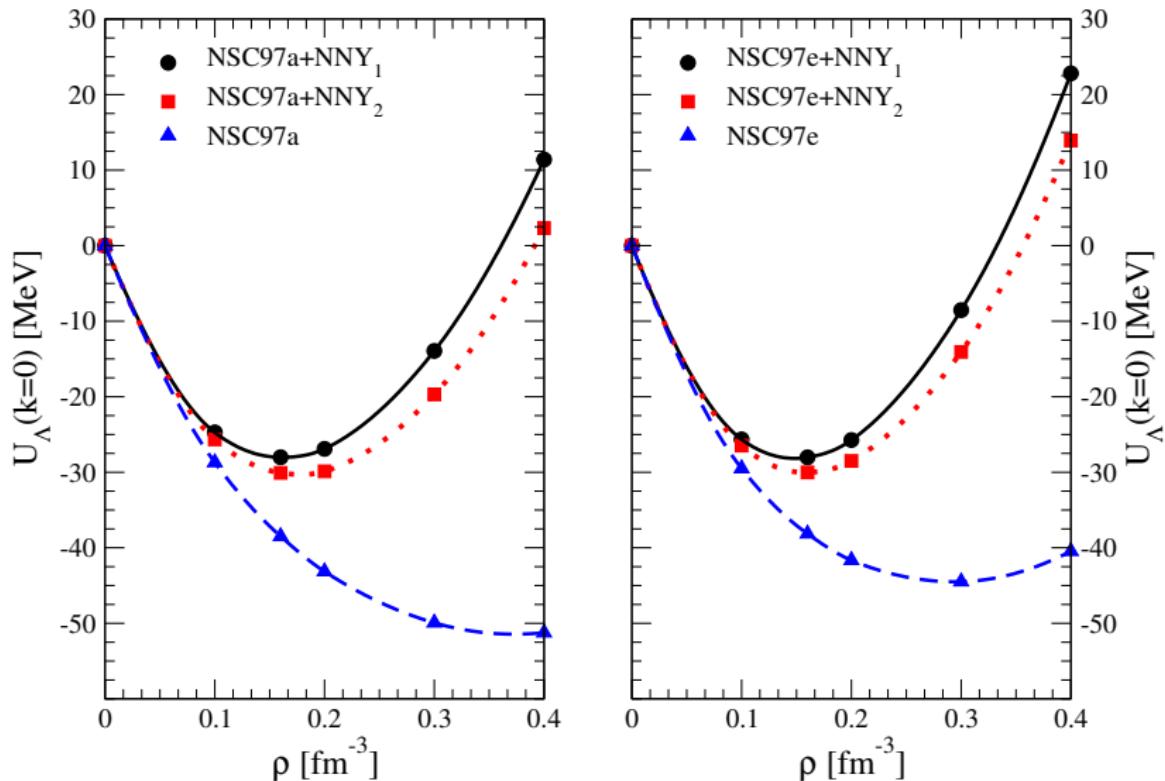
$$n_p - n_\mu - n_e = 0.$$

Λ -single particle potential



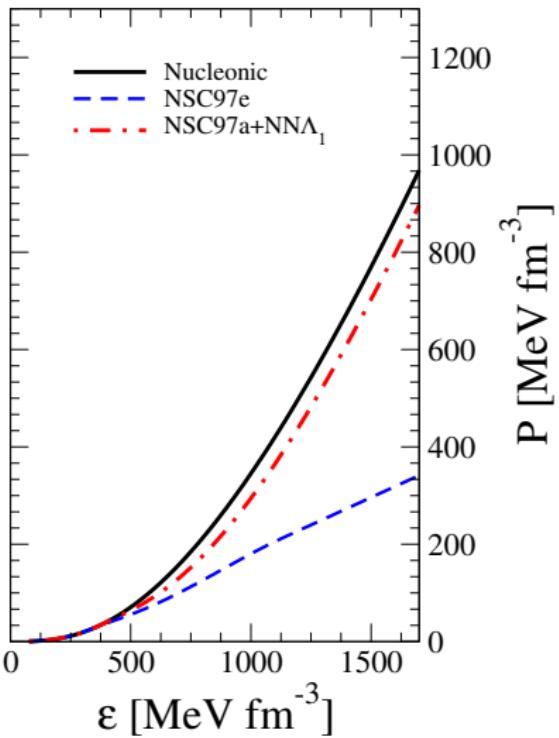
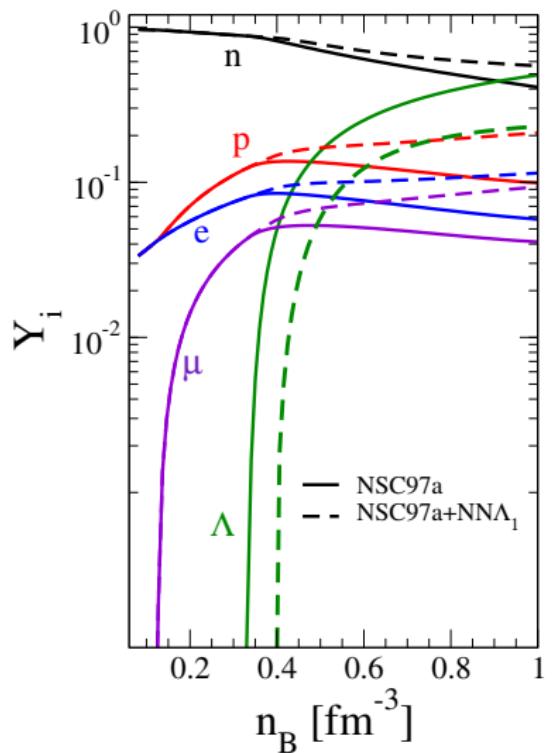
D. Logoteta, I. Vidaña and I. Bombaci [Eur. Phys. J. A, 55 11 \(2019\) 207](#)

$U_\Lambda(k=0)$ as function of baryonic density



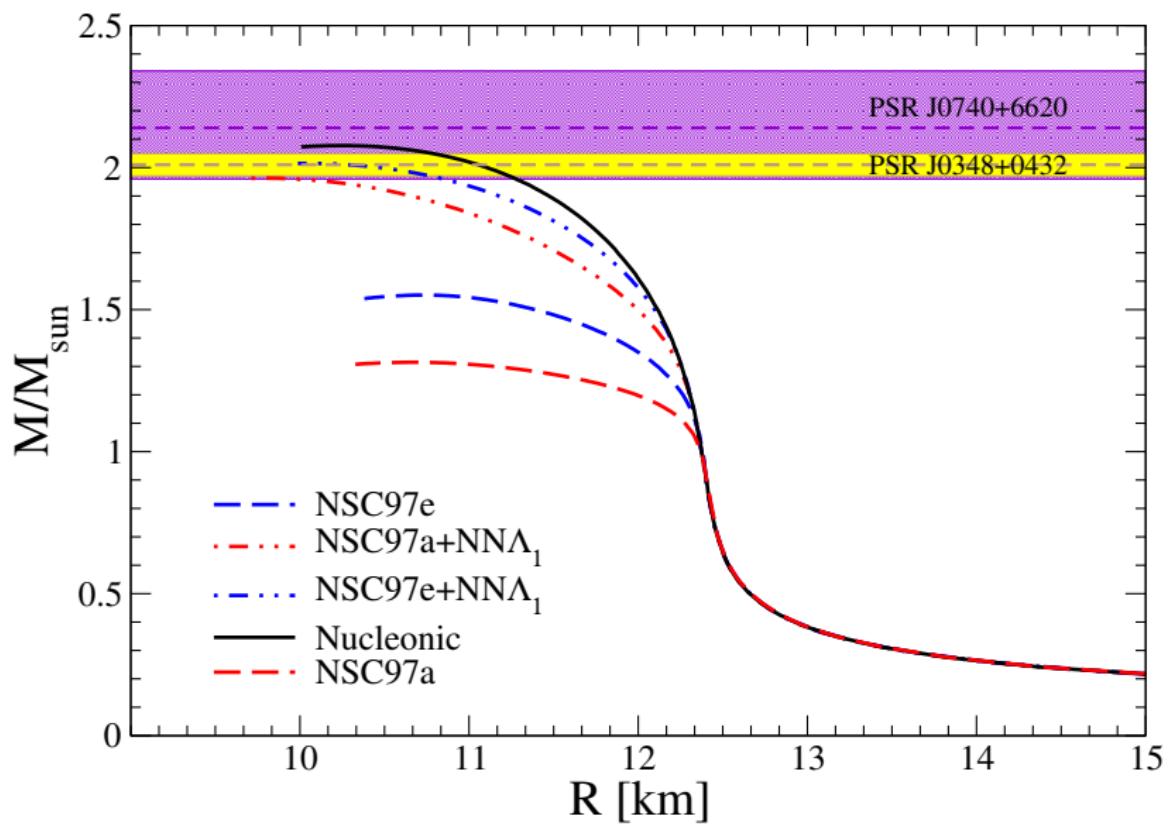
D. Logoteta, I. Vidaña and I. Bombaci [Eur. Phys. J. A, 55 11 \(2019\) 207](#)

Composition of hyperonic matter



D. Logoteta, I. Vidaña and I. Bombaci [Eur. Phys. J. A, 55 11 \(2019\) 207](#)

Neutron stars structure including Λ -hyperon



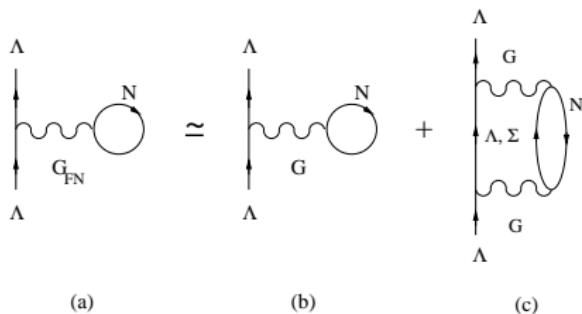
D. Logoteta, I. Vidaña and I. Bombaci [Eur. Phys. J. A, 55 11 \(2019\) 207](#)

Improved description of the separation energies of Λ -hypernuclei

	$^{41}\Lambda\text{Ca}$	$^{91}\Lambda\text{Zr}$	$^{209}\Lambda\text{Pb}$
NSC97a	23.0	31.3	38.8
NSC97a+NN Λ_1	14.9	21.1	26.8
NSC97a+NN Λ_2	13.3	19.3	24.7
NSC97e	24.2	32.3	39.5
NSC97e+NN Λ_1	16.1	22.3	27.9
NSC97e+NN Λ_2	14.7	20.7	26.1
Exp.	18.7(1.1)	23.6(5)	26.9(8)

D. Logoteta, I. Vidaña and I. Bombaci [Eur. Phys. J. A, 55 11 \(2019\) 207](#)

Λ separation energies in hypernuclei



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D. Logoteta, I. Vidaña and I. Bombaci Eur. Phys. J. A, 55 11 (2019)

- **EOS** $\Rightarrow P, \varepsilon, T, n_B, X_i$
- **TOV** \Rightarrow gravitational masses M_1 and M_2 you want to use in your simulation
- **Initial data:** LORENE \Rightarrow solves problem of the two (M_1 and M_2) NSs orbiting ~ 45 km away in quasicircular orbit
- **Evolution:** Whisky THC \Rightarrow describes temporal evolution of the system: solves Einstein equations coupled to hydrodynamics

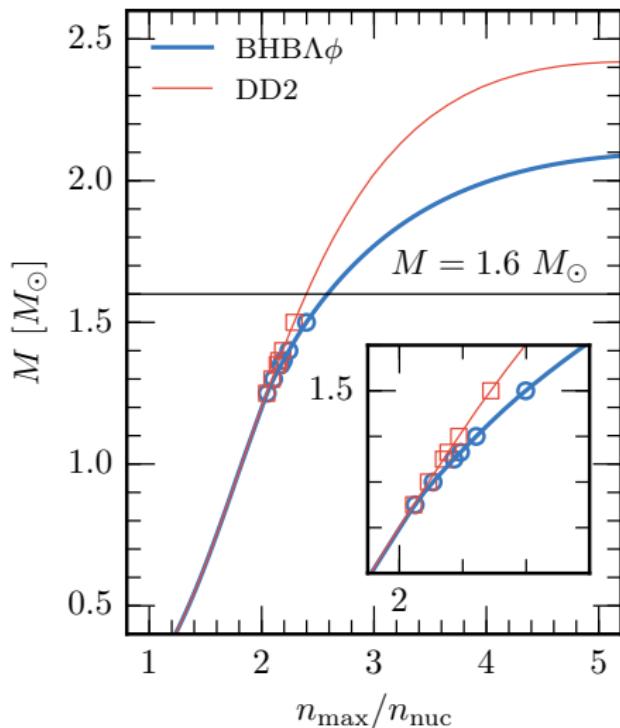
Once all these stuff is done...(thousand of CPU hours)

Output:

Extraction of GWs signal, mass ejected, nucleosynthesis ...

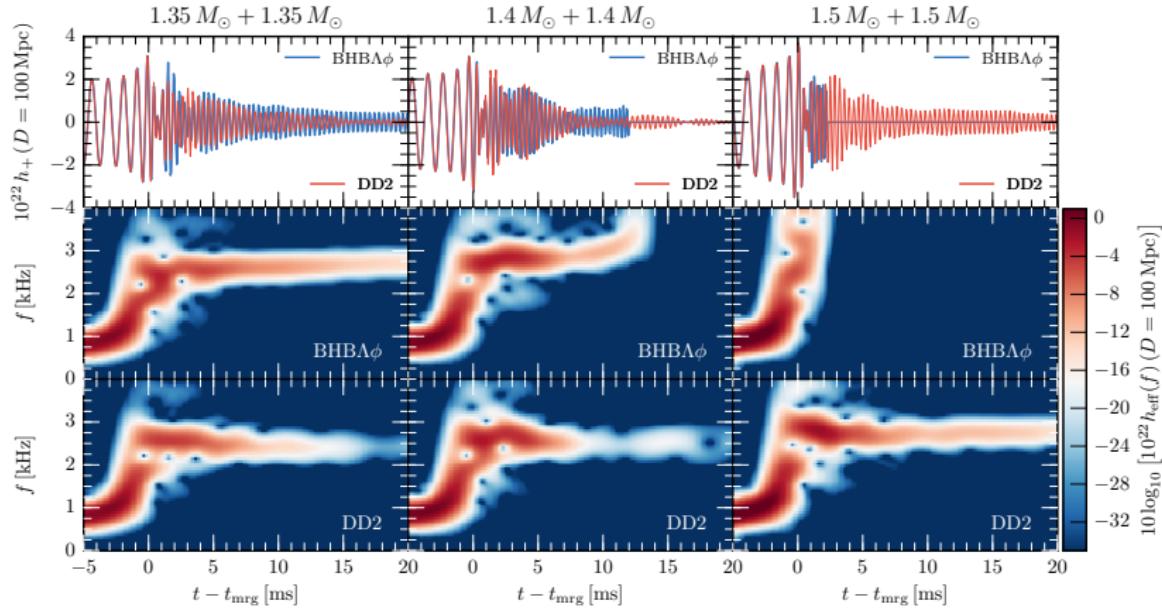
...and very important:

Constraints on the EOS of neutron star matter

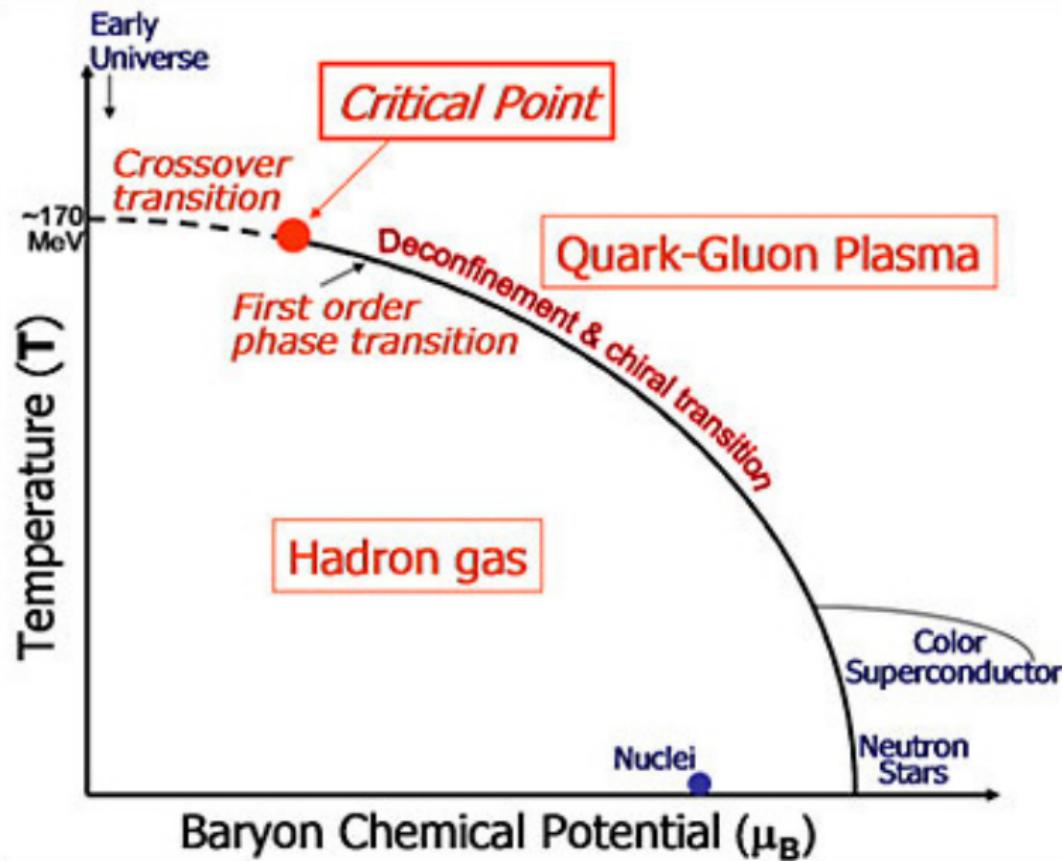


D. Radice et al. ApJL 842 L10 (2017)

GWs spectrum with hyperons and without



D. Radice et al. ApJL 842 L10 (2017)



- Gibbs conditions for phase coexistence:

$$\mu_H(P_H, T_H) = \mu_Q(P_Q, T_Q), \quad T_H = T_Q, \quad P_H(\mu_H, T) = P_Q(\mu_Q, T) = P_T.$$

- Charge neutrality is not imposed locally but globally.
- Hadronic and quark phase are not separately neutral.
- The whole system satisfies:

$$\chi \rho_c^Q + (1 - \chi) \rho_c^H + \rho_c^I = 0.$$

- Energy density and baryonic density in the mixed phase read:

$$\langle \epsilon \rangle = (1 - \chi) \epsilon_H - \chi \epsilon_Q,$$

$$\langle n \rangle = (1 - \chi) n_H - \chi n_Q.$$

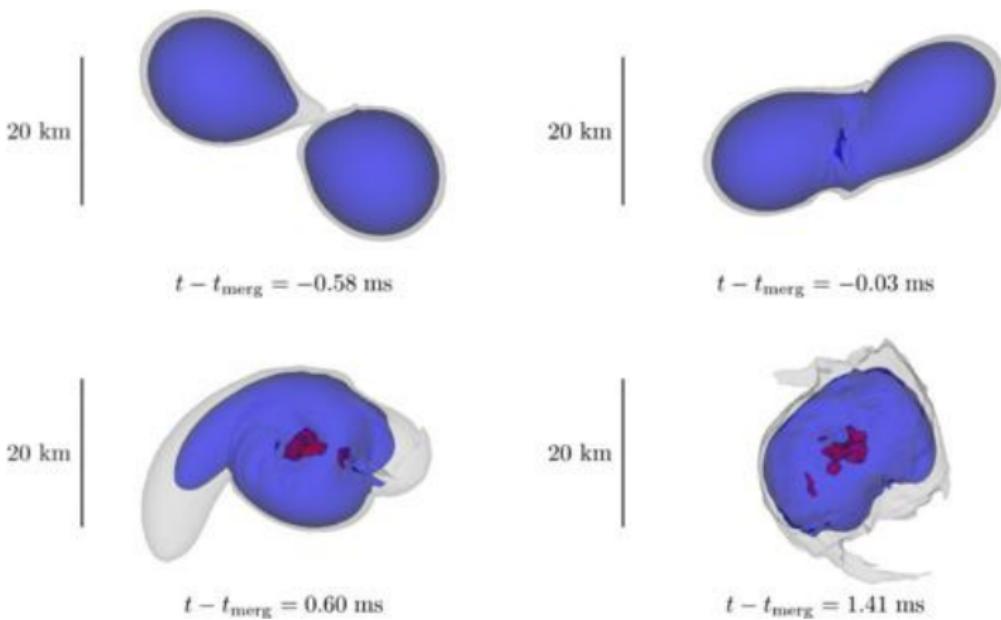
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A. Prakash, D. Radice, D. Logoteta, A. Perego, V. Nedora, I. Bombaci, R. Kashyap, S. Bernuzzi, and A. Endrizzi **Phys. Rev. D 104, 083029 (2021)**

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A. Prakash, D. Radice, D. Logoteta, A. Perego, V. Nedora, I. Bombaci, R. Kashyap, S. Bernuzzi, and A. Endrizzi **Phys. Rev. D 104, 083029 (2021)**

Snapshots of the merger



A. Prakash, D. Radice, D. Logoteta, A. Perego, V. Nedora, I. Bombaci, R. Kashyap, S. Bernuzzi, and A. Endrizzi **Phys. Rev. D 104, 083029 (2021)**



Choose your favourite EOS, fix M_1, M_2

$$M_{tot} = M_1 + M_2$$

$$q = M_1/M_2$$

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Possible scenarios:

- Long lived
- Short lived (delayed collapse)
- Prompt collapse (PC)

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Questions:

- Can we relate this behavior to some specific properties of the EOS?
- For fixed q , is there a threshold value of M_{tot} (M_{th}) to get a PC?

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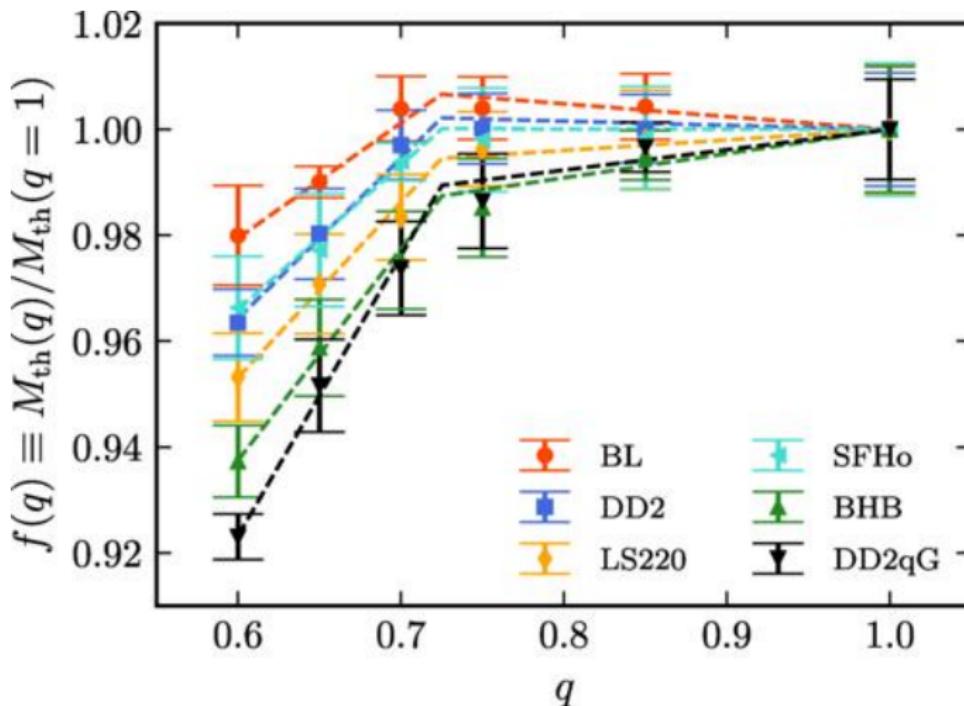
Questions:

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Key quantity

$$K^\infty(n_B^{max}) = 9(n_B^{max})^2 \frac{\partial^2 E/A}{\partial n_B^2} \Big|_{n_B^{max}}$$

Role of incompressibility of nuclear matter in BNSM



A. Perego, D. Logoteta, D. Radice, S. Bernuzzi, R. Kashyap, A. Das, S. Padamata, and A. Prakash **Phys. Rev. Lett. 129, 032701 (2022)**

- Taking into account the correct degrees of freedom is crucial for a realistic description of astrophysical system like NSs, BNSM and CCSNe
- Future GW detectors (ET, KAGRA, LISA) will provide the chance to observe the postmerger GW signal \Rightarrow strong constraints on the EOS of dense hadronic matter
- We need finite temperature microscopic EOSs with hyperons based on realistic interactions between nucleons and hyperons (and/or quarks)
- **EQUALLY IMPORTANT:** strong experimental efforts are required to improve the quality of NY, YY and many-body hyperonic interactions