

# Recent jet measurements from ALICE

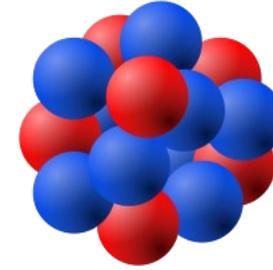
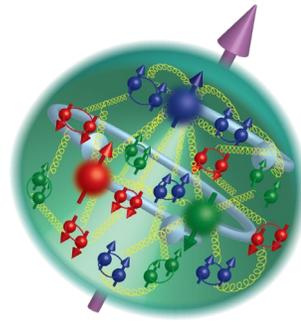
**Ezra D. Lesser**

*UC Berkeley / LBNL*

11 November 2021



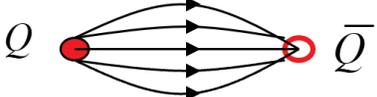
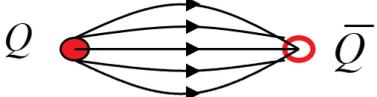
# Introduction



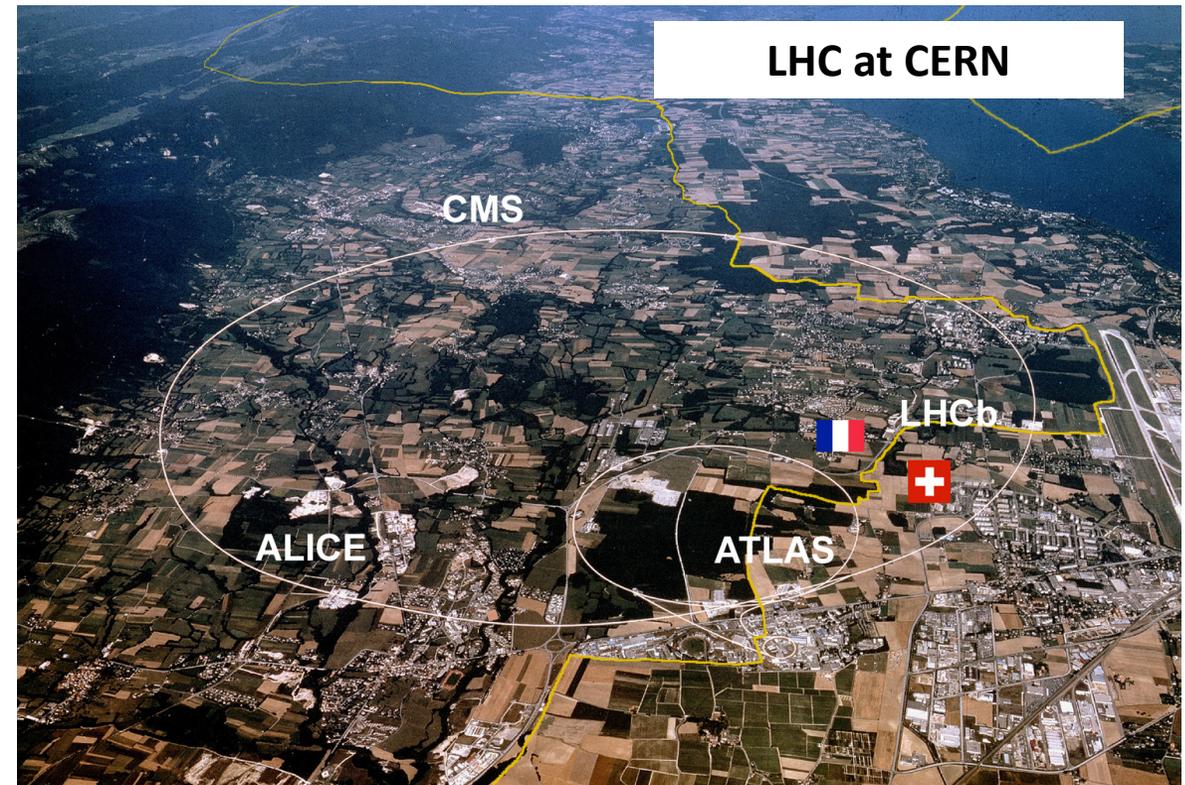
- **Quantum Chromodynamics (QCD)** is the theory of strong interactions

- We study high-energy QCD interactions using collider experiments

- Small length scales ( $\lambda \lesssim \text{fm}$ )

- Color confinement   $q$    $\bar{q}$

- High temperature nuclear matter

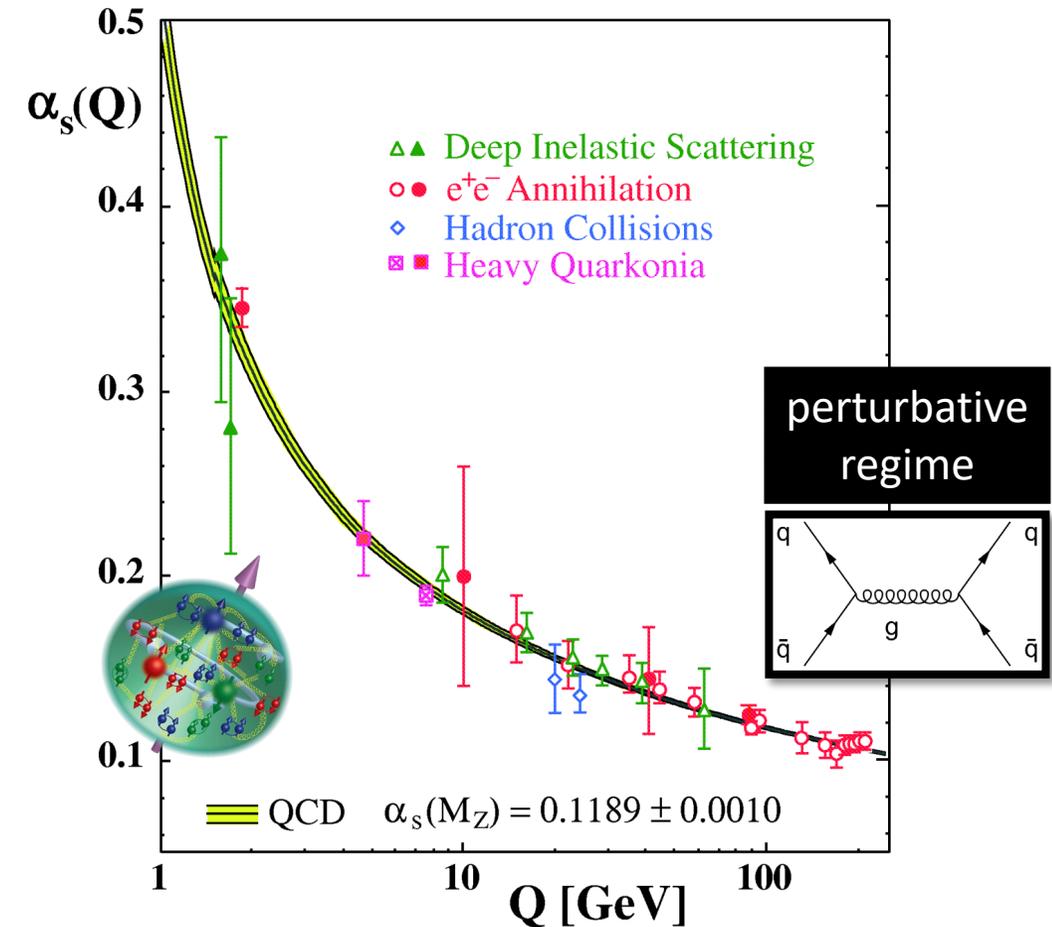


# Theoretical challenges

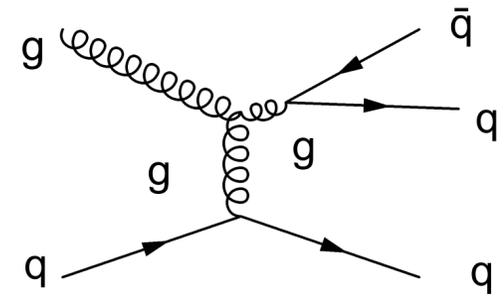
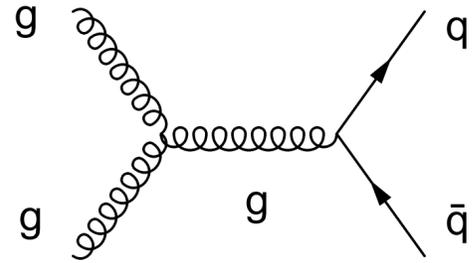
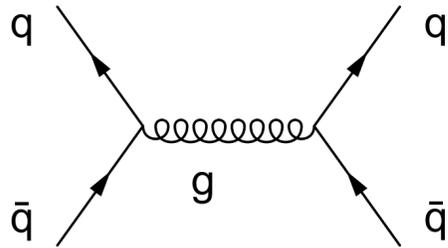
- $\alpha_s$  runs from divergence to  $\Lambda_{\text{QCD}} \approx 200 \text{ MeV}$  to **asymptotic freedom**
- Some physics cannot be calculated via perturbative techniques



Gross/Politzer/Wilczek: 2004 Nobel Prize in Physics



# QCD jets

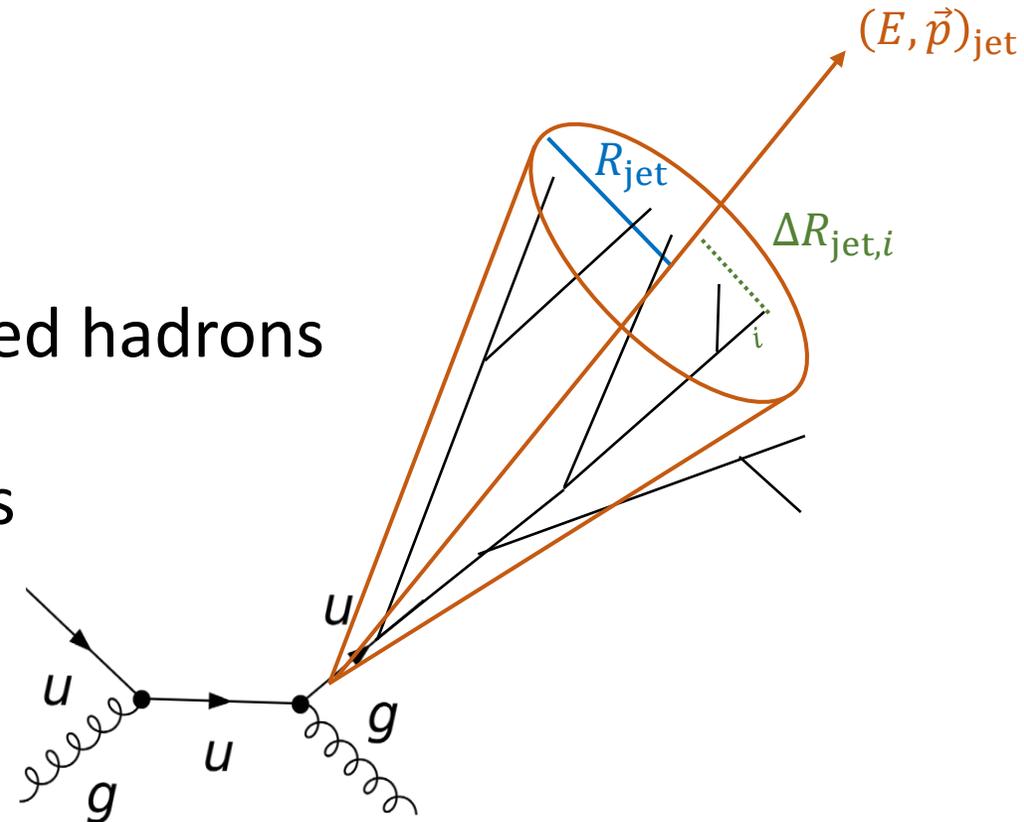


- Interesting probe for various scales of strong interactions:

- Initial, hard (high- $Q^2$ ) scattering
- Parton shower
- Fragmentation into hadrons

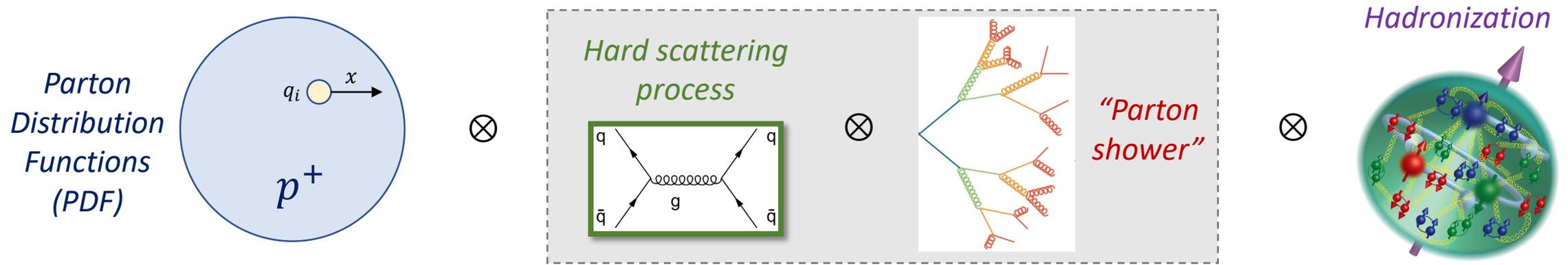
- Experimentally reconstructed from grouped hadrons

- **Dynamically recombined, tunable** objects which can be sensitive to either/both perturbative and nonperturbative physics



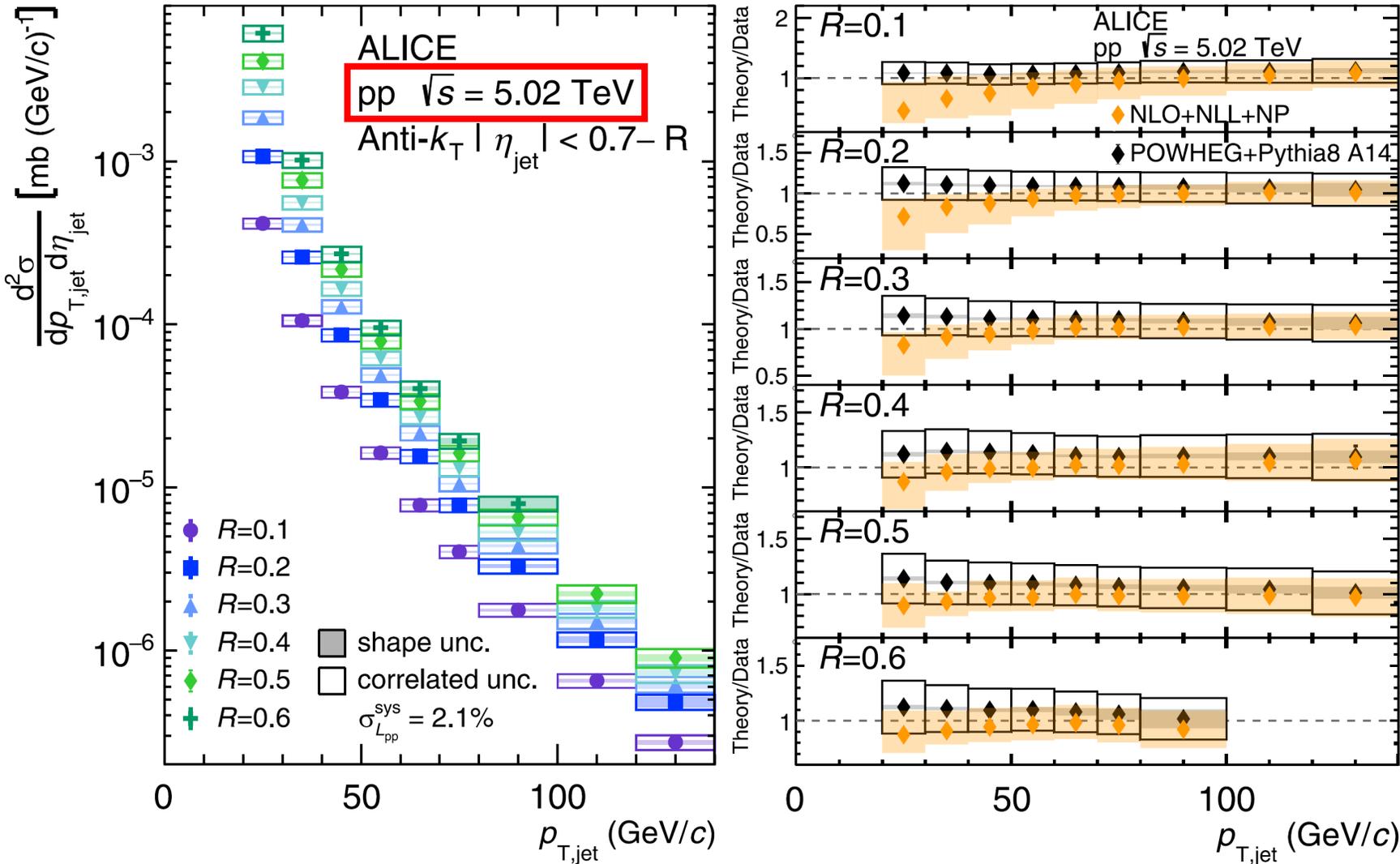
# Calculating jet observables

- Jet observables are useful because they can also be compared to first-principles QCD using **factorization theorems**
  - Ability to calculate physics at different scales separately, then combine



- Proven valid at leading power of  $Q$  <sup>[1]</sup> and for leading power corrections
- Allows tests of **universal physics** throughout various measurements
- These steps can also be implemented into statistical generators for creating Monte Carlo simulations

# Measurements of the inclusive jet cross section

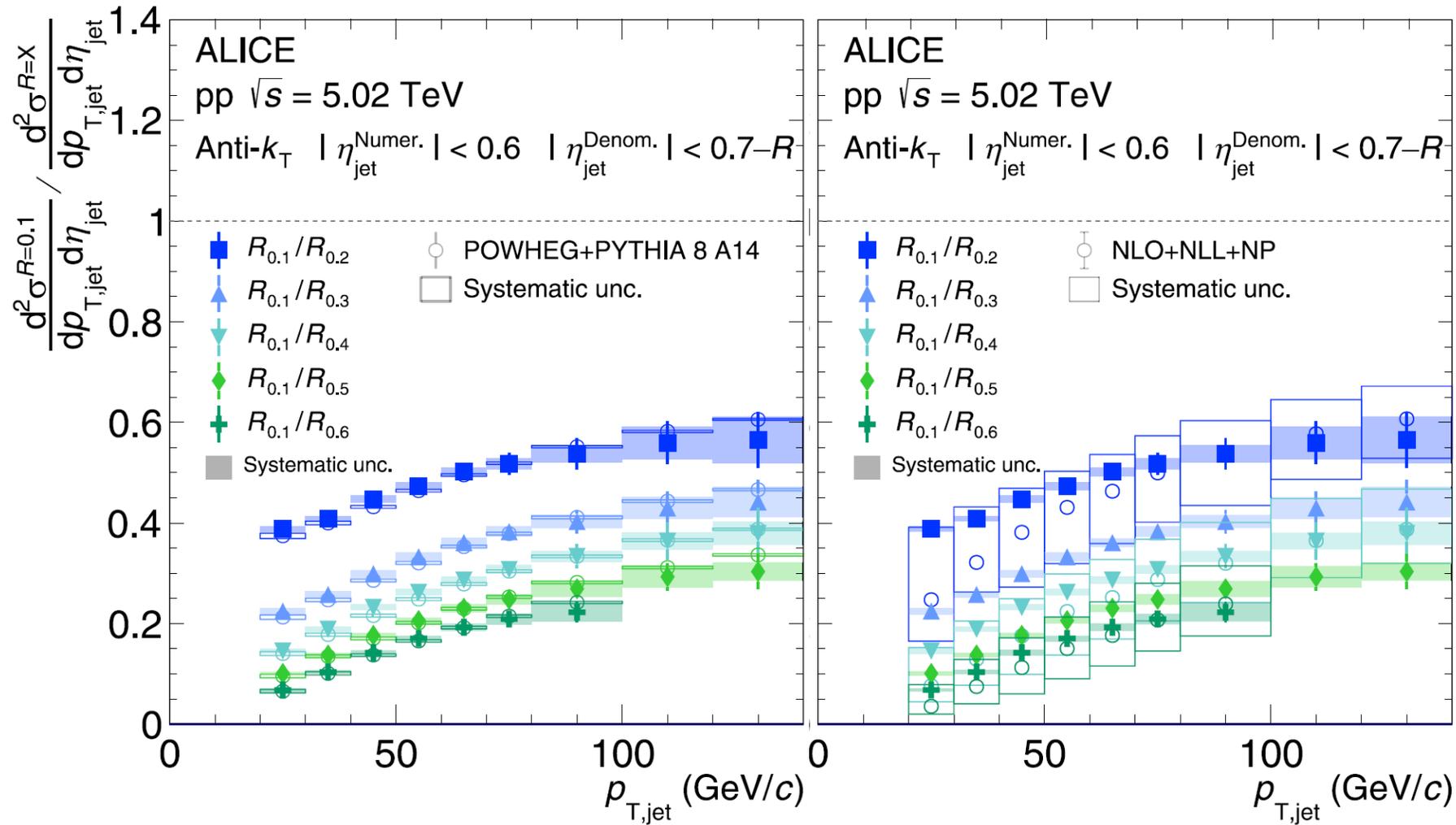


- Jets reconstructed with **small** to **moderate** jet radius  $R$
- Increasing  $R$  shifts spectrum to the right
- Slight tension at low  $p_T$

**Higher-order theoretical predictions work well to describe the data over a range of  $p_T$  and  $R$**

Theory: X. Liu, S. Moch, F. Ringer  
[Phys. Rev. D 97 \(2018\) 056026](#)

# Ratios of the inclusive jet cross section



- Taking ratios allows cancellation of most correlated systematic uncertainties [1]
- Large uncertainties on NLO+NLL+NP from scale variations

**Inclusive jet predictions agree well with experimental data within the given uncertainties**

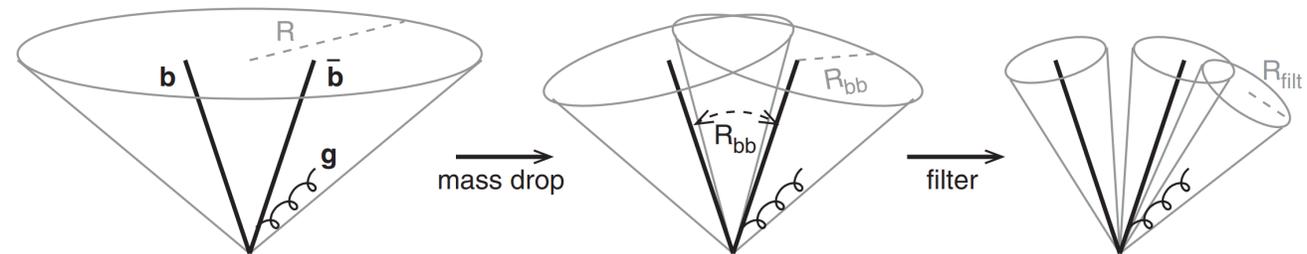
*Higher order calculations can lessen the systematic uncertainty on theory calculations*

# Going deeper using jet substructure

- **Tagging jets** of particular origin

- Boosted objects (Higgs/BSM searches:  $H \rightarrow b\bar{b}$ ) [2]

- Quark vs. gluon jets



- Precision **tests of perturbative QCD** and factorization

- We will discuss this first

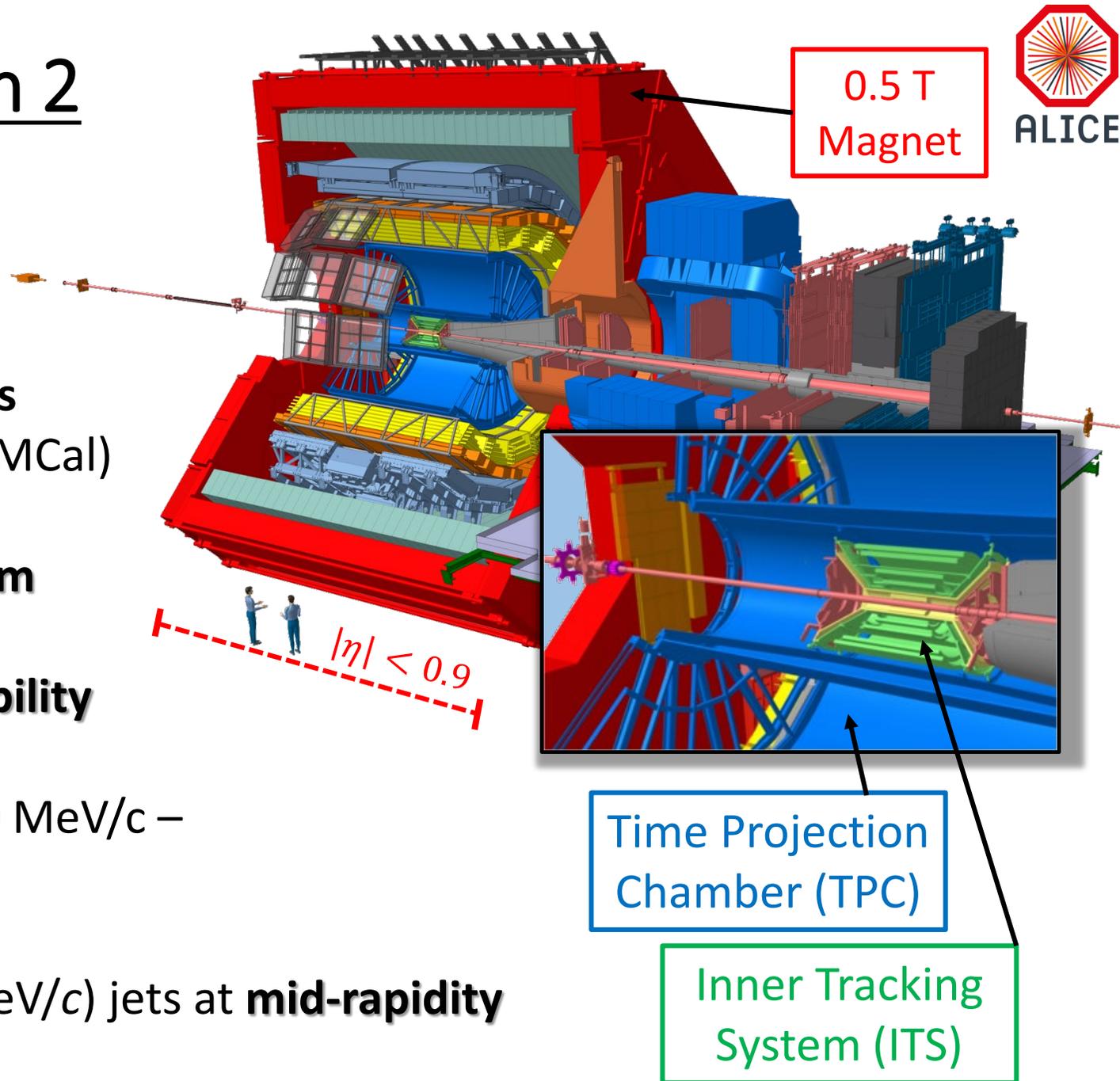
- Probing the **quark-gluon plasma** in heavy-ion collisions

- We will discuss this later

[2] *J. Butterworth, A. Davison, M. Rubin, G. Salam*  
[Phys. Rev. Lett. 100, 242001 \(2008\)](https://arxiv.org/abs/hep-ph/0712316)

# ALICE detector during Run 2

- **Central barrel:** silicon inner tracking system (ITS), gas TPC, EM calos.
- Measurement of **charged-particle jets** (ITS + TPC) and **full jets** (ITS + TPC + EMCal)
- **High-precision spatial and momentum resolution**, excellent for substructure measurements, plus **strong PID capability**
- Measurement of tracks with  $p_T > 150$  MeV/c – study low- $p_T$  tracks at LHC energies
- Great for **low/moderate- $p_T$**  ( $< 150$  GeV/c) jets at **mid-rapidity**

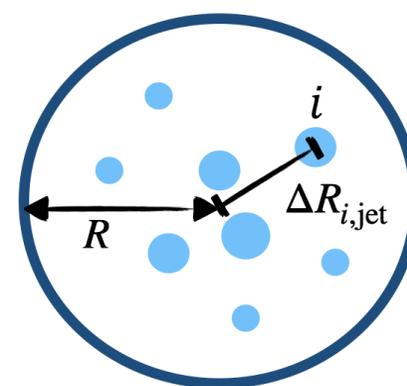


# Generalized jet angularities

- **Class of substructure observables** dependent on  $p_T$  and angular distributions of tracks within jets

$$\lambda_{\alpha}^{\kappa} \equiv \sum_{i \in \text{jet}} \left( \frac{p_{T,i}}{p_{T,\text{jet}}} \right)^{\kappa} \left( \frac{\Delta R_{i,\text{jet}}}{R} \right)^{\alpha}$$

Tunable, continuous parameters for relative weighting  
Constituent angle in  $(\eta, \phi)$  space  
Constituent  $p_T$



- IRC-safe\* observable for  $\kappa = 1, \alpha > 0 \rightarrow$  **directly calculable from pQCD**
- Each  $(\kappa, \alpha)$  defines a different observable capable of probing jet structure and providing systematic constraints on theory
- Can be further varied with jet resolution parameter  $R$

A. Larkoski, J. Thaler, W. Waalewijn  
[JHEP 11 \(2014\) 129](https://arxiv.org/abs/1304.1579)

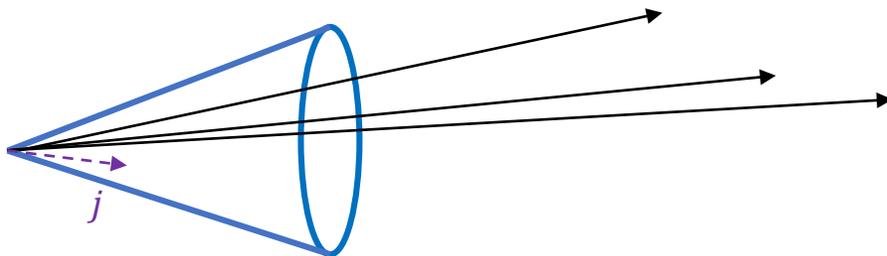
\* track-based observables IRC-unsafe (see backup)

# What is IRC safety?

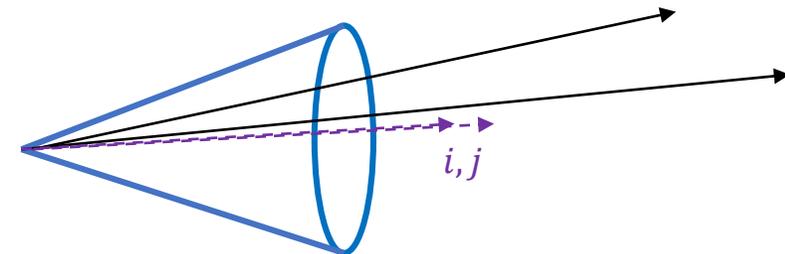
$$\lambda_\alpha^\kappa \equiv \sum_{i \in \text{jet}} \left( \frac{p_{T,i}}{p_{T,\text{jet}}} \right)^\kappa \left( \frac{\Delta R_{\text{jet},i}}{R} \right)^\alpha \equiv \sum_{i \in \text{jet}} z_i^\kappa \theta_i^\alpha$$

- Stands for **I**nfra-**R**ed and **C**ollinear (**IRC**) safety
- Class of reconstruction algorithms & observables which satisfy certain conditions in order to avoid singularities from appearing in a well-defined path towards theoretical calculation

**I**nfra-**R**ed safety: the observable should not change if an infinitely-low-momentum particle is added to the event/jet

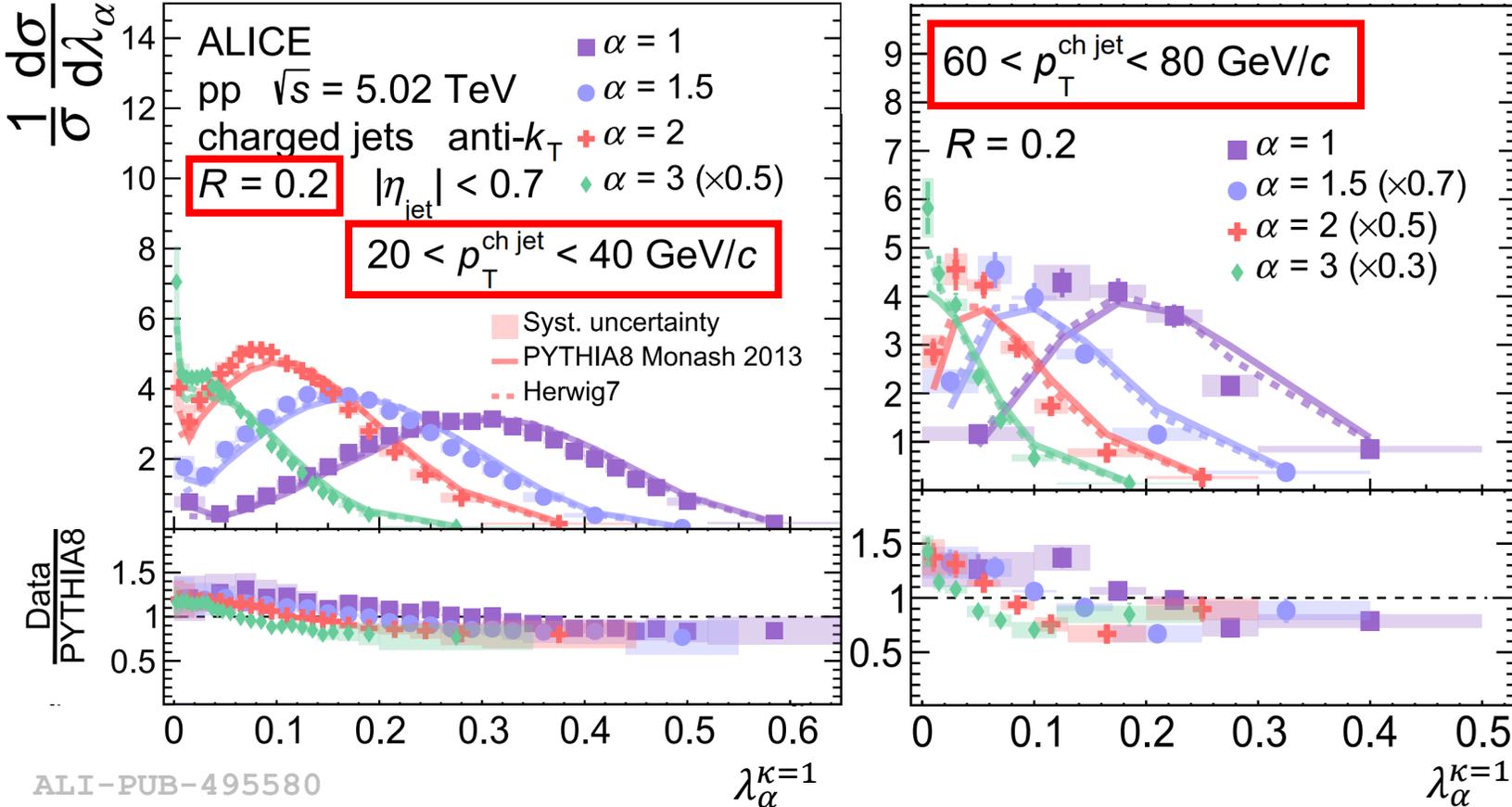


**C**ollinear safety: the observable should not change if one particle splits into two collinear particles



# Some jet angularity measurements

$$\lambda_\alpha^\kappa \equiv \sum_{i \in \text{Jet}} z_i^\kappa \theta_i^\alpha$$



ALI-PUB-495580

all figures available from: ALICE Collab. [arXiv:2107.11303](https://arxiv.org/abs/2107.11303) [nucl-ex]

- Distributions shift to the **left** for **higher  $\alpha$ ,  $p_{T,\text{jet}}^{\text{ch}}$ , and  $R$**
- **Reasonable consistency is seen with MC predictions**
  - Residuals become even smaller with Soft Drop grooming
  - PYTHIA shower + fragmentation function model works in this regime

- Calculable way of **probing the  $p_T$  structure of jets**

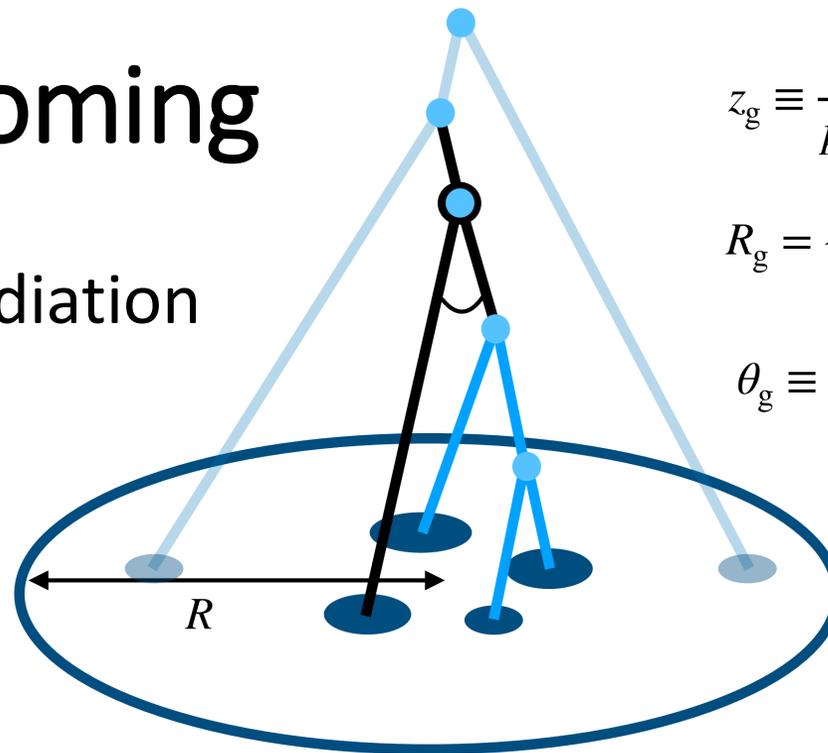
# Going deeper: jet grooming

- Removal of soft, wide-angle radiation to enhance the influence of perturbative effects

- One popular algorithm is **Soft Drop grooming** <sup>[3]</sup>

- Recluster jet into ordered tree using Cambridge-Aachen algorithm and then trim branches until the Soft Drop condition is satisfied

- IRC-safe → **repeatable on theoretical predictions**



$$z_g \equiv \frac{p_{T,\text{subleading}}}{p_{T,\text{leading}} + p_{T,\text{subleading}}}$$

$$R_g = \sqrt{\Delta y^2 + \Delta \phi^2}$$

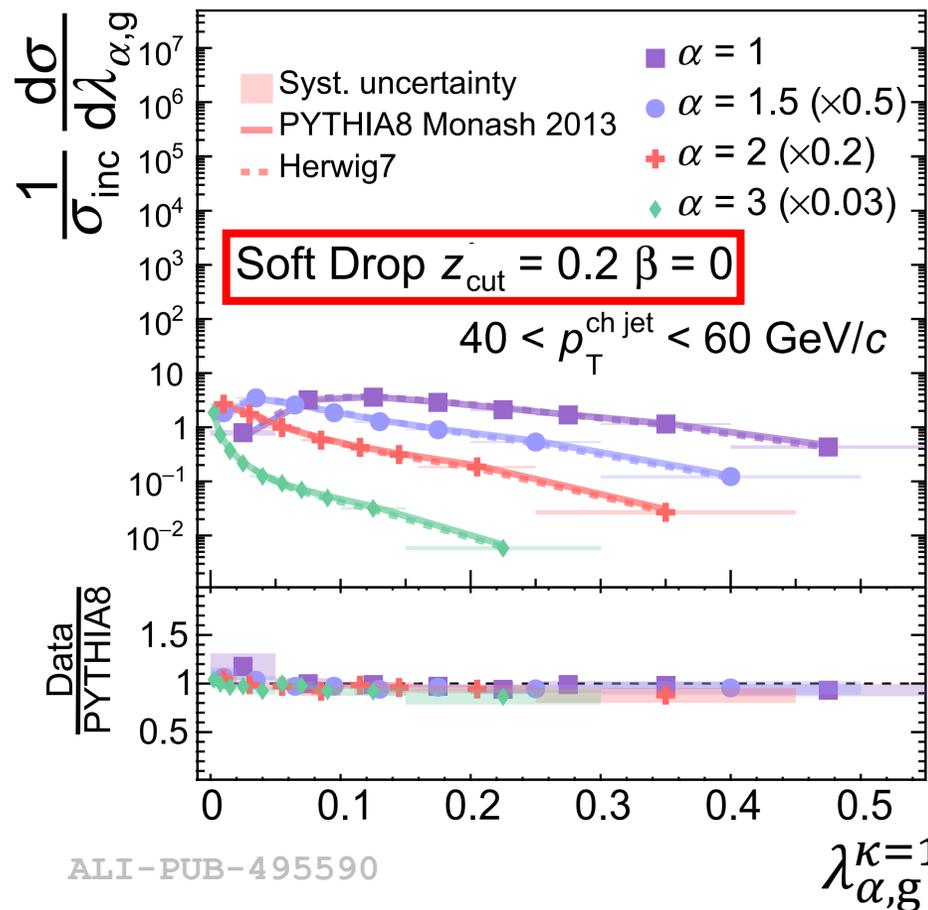
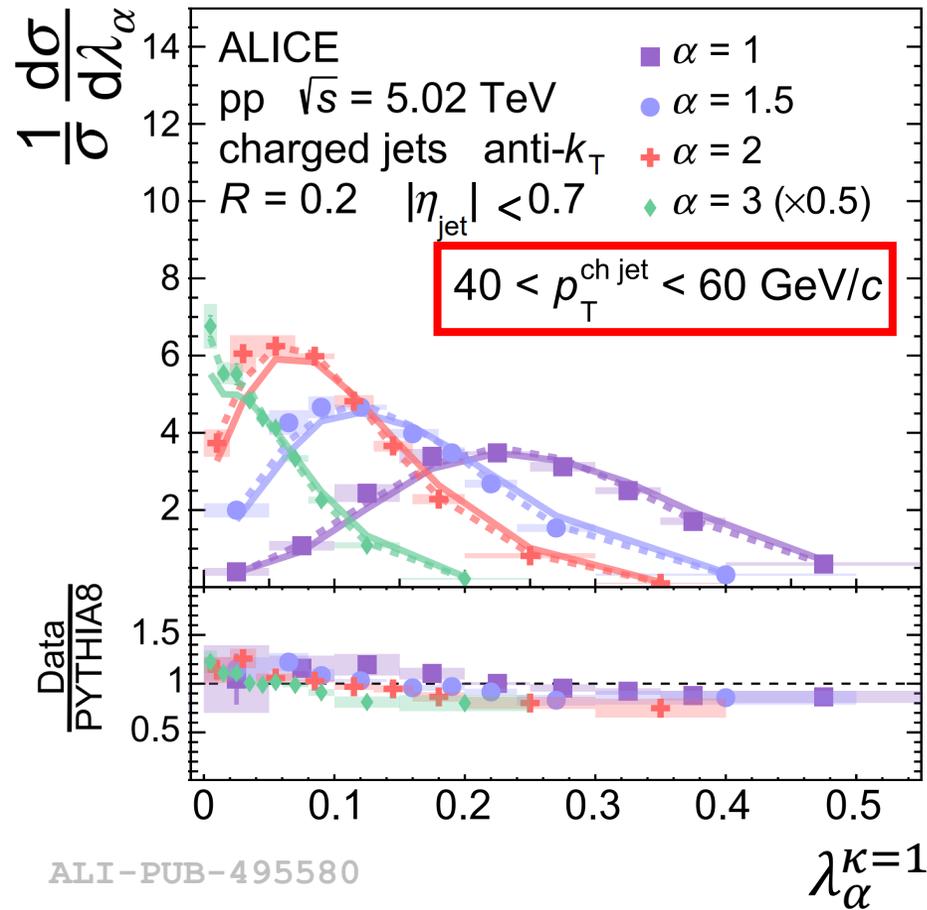
$$\theta_g \equiv \frac{R_g}{R}$$

Soft Drop Condition:

$$\frac{\min(p_{T1}, p_{T2})}{p_{T1} + p_{T2}} > z_{\text{cut}} \left( \frac{\Delta R_{12}}{R_0} \right)^\beta$$

<sup>[3]</sup> A. Larkoski, S. Marzani, G. Soyez, J. Thaler [JHEP 1405 \(2014\) 146](https://arxiv.org/abs/1402.2687)

# Ungroomed vs. Groomed angularities ( $R = 0.2$ )



**Better agreement  
seen after  
grooming**

- Removing some nonperturbative effects from data and models increases the agreement, as would be expected

- Similar improvement in agreement is seen for all  $\alpha$ ,  $R$ , and  $p_T^{ch jet}$  bins

$$\lambda_\alpha^\kappa \equiv \sum_{i \in \text{jet}} z_i^\kappa \theta_i^\alpha$$

$$\lambda_\alpha^\kappa \equiv \sum_{i \in \text{jet}} z_i^\kappa \theta_i^\alpha$$

# Theoretical calculations

- We use theoretical predictions for inclusive **parton** jets [6] calculated at **Next-to-Leading Log (NLL')** perturbative accuracy
  - *New calculations also exist for Z+jets* [7]



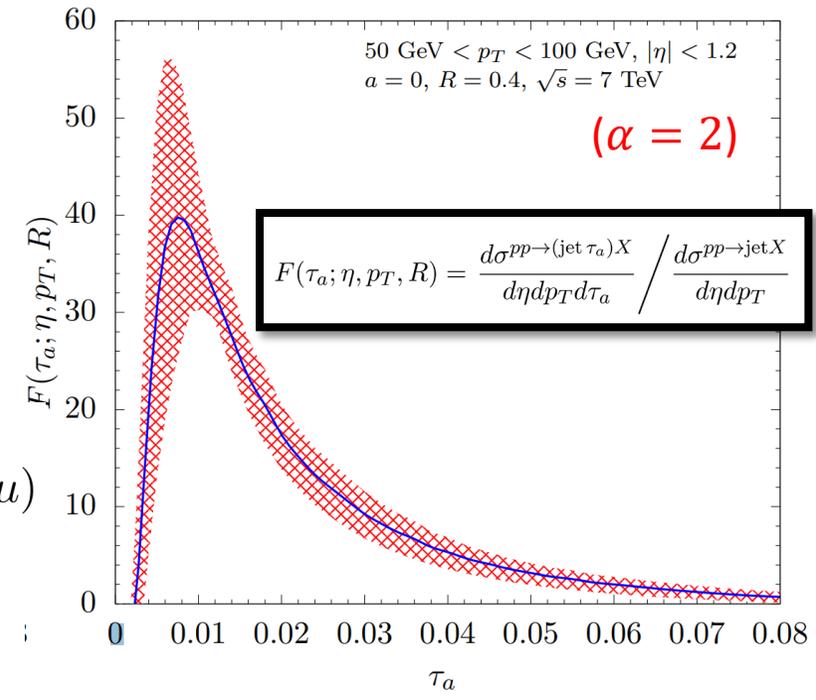
- Carried out in **Soft Collinear Effective Theory**

C. W. Bauer, S. Fleming, M. Luke [Phys. Rev. D 63 \(2000\) 014006](#)

$$\frac{d\sigma^{pp \rightarrow (\text{jet } \tau_a) X}}{d\eta dp_T d\tau_a} = \sum_{abc} \overset{\text{PDFs (NP)}}{f_a(x_a, \mu)} \otimes \overset{\text{PDFs (NP)}}{f_b(x_b, \mu)} \otimes \overset{\text{Hard Function (P)}}{H_{ab}^c(x_a, x_b, \eta, p_T/z, \mu)} \otimes \overset{\text{siAJFs (P / NP)}}{\mathcal{G}_c(z, p_T, R, \tau_a, \mu)}$$

**Definitional difference:**

$$\tau_a \equiv \tau_a^{pp} \equiv \frac{1}{p_T} \sum_{i \in J} p_T^i (\Delta \mathcal{R}_{iJ})^{2-a} \equiv \lambda_{\beta=2-a}^{\kappa=1} * R^{2-a}$$



**We can compare ALICE data to first-principles predictions from theory**

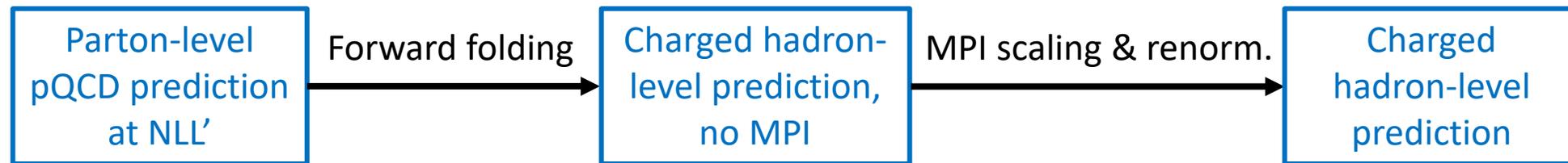
[6] Z. Kang, K. Lee, F. Ringer [JHEP 1804 \(2018\) 110](#)



[7] S. Caletti, O. Fedkevych, S. Marzani, D. Reichelt, S. Schumann, G. Soyez, V. Theeuwes [JHEP 07 \(2021\) 076](#)

# Comparing to pQCD predictions with SCET

- **Parton** jet calculations cannot be directly matched to experimental data
- Must apply a “forward folding” procedure to correct for multi-parton interactions (MPI), hadronization, and **charged-particle** jets



- There is a model dependence introduced, which we address by repeating the folding procedure with both Herwig and PYTHIA

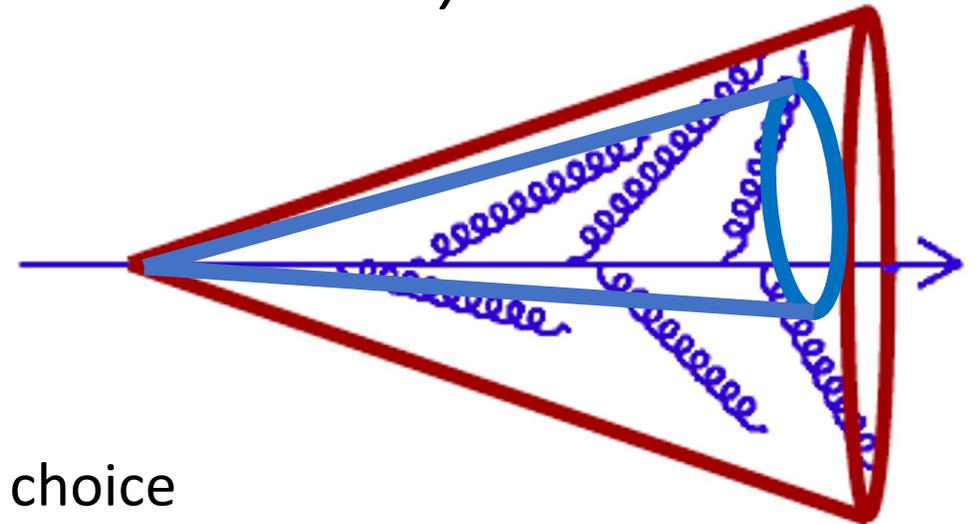
# Determining regions of interest

$$\lambda_\alpha^\kappa \equiv \sum_{i \in \text{jet}} z_i^\kappa \theta_i^\alpha$$

- Nonperturbative effects in the calculation are larger at low  $p_T^{\text{jet}}$  and small  $R$ 
  - Become dominant when soft-collinear scale becomes small:

$$\lambda_\alpha^{\text{NP region}} \lesssim \Lambda / (p_T^{\text{jet}} R) \quad (\text{we use } \Lambda = 1 \text{ GeV})$$

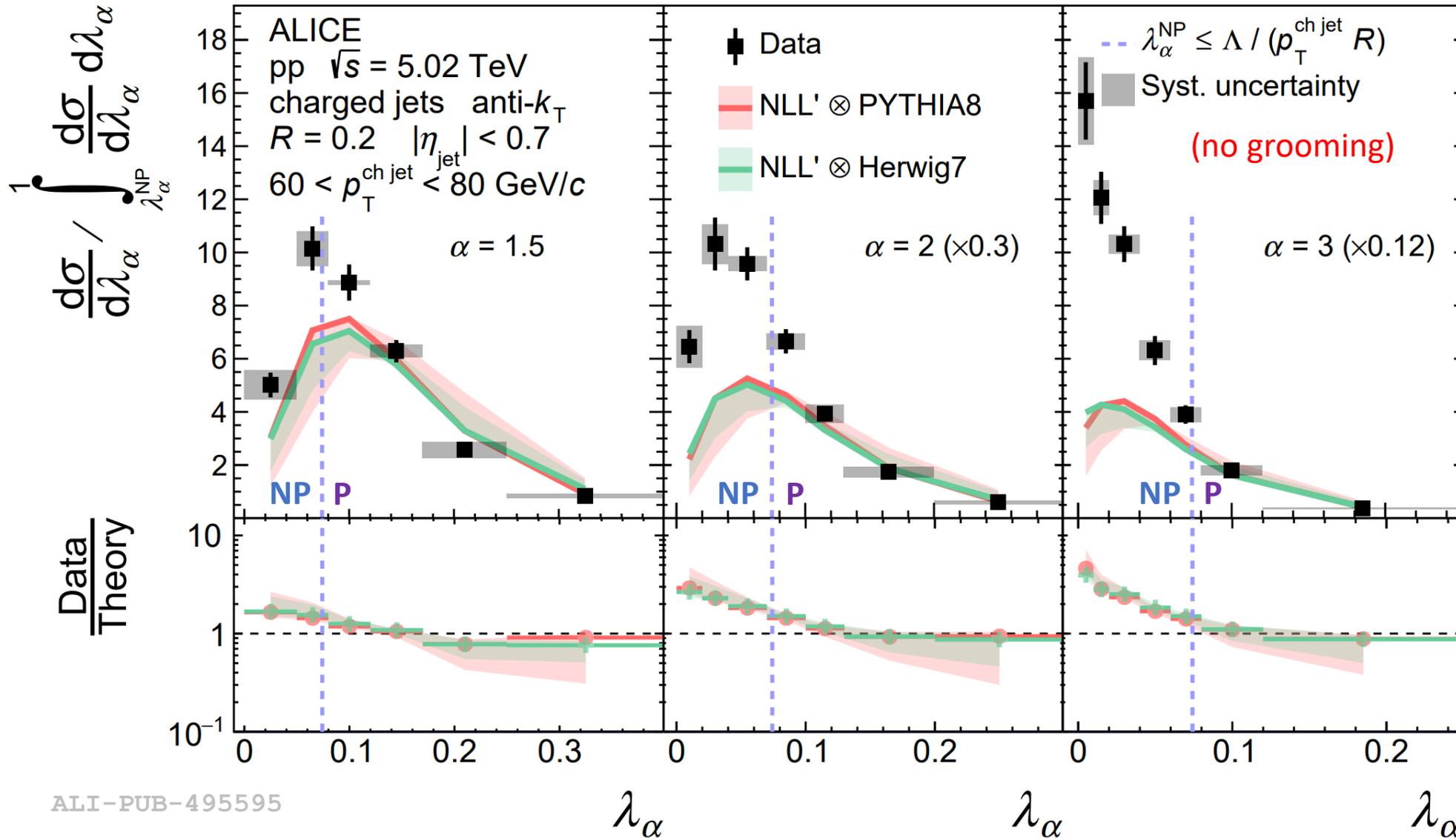
- Parton-to-charged response is largely non-diagonal for **small  $R$ , low  $p_T^{\text{jet}}$** 
  - Due primarily to hadronization
  - Corresponds to an increased dependence on the choice of hadronization model and tuning
  - **These regions** can be used for testing & tuning MC models



***small  $R$  is more susceptible to boundary effects***

# pQCD predictions with SCET ( $R = 0.2$ )

$$\lambda_\alpha^\kappa \equiv \sum_{i \in \text{jet}} z_i^\kappa \theta_i^\alpha$$

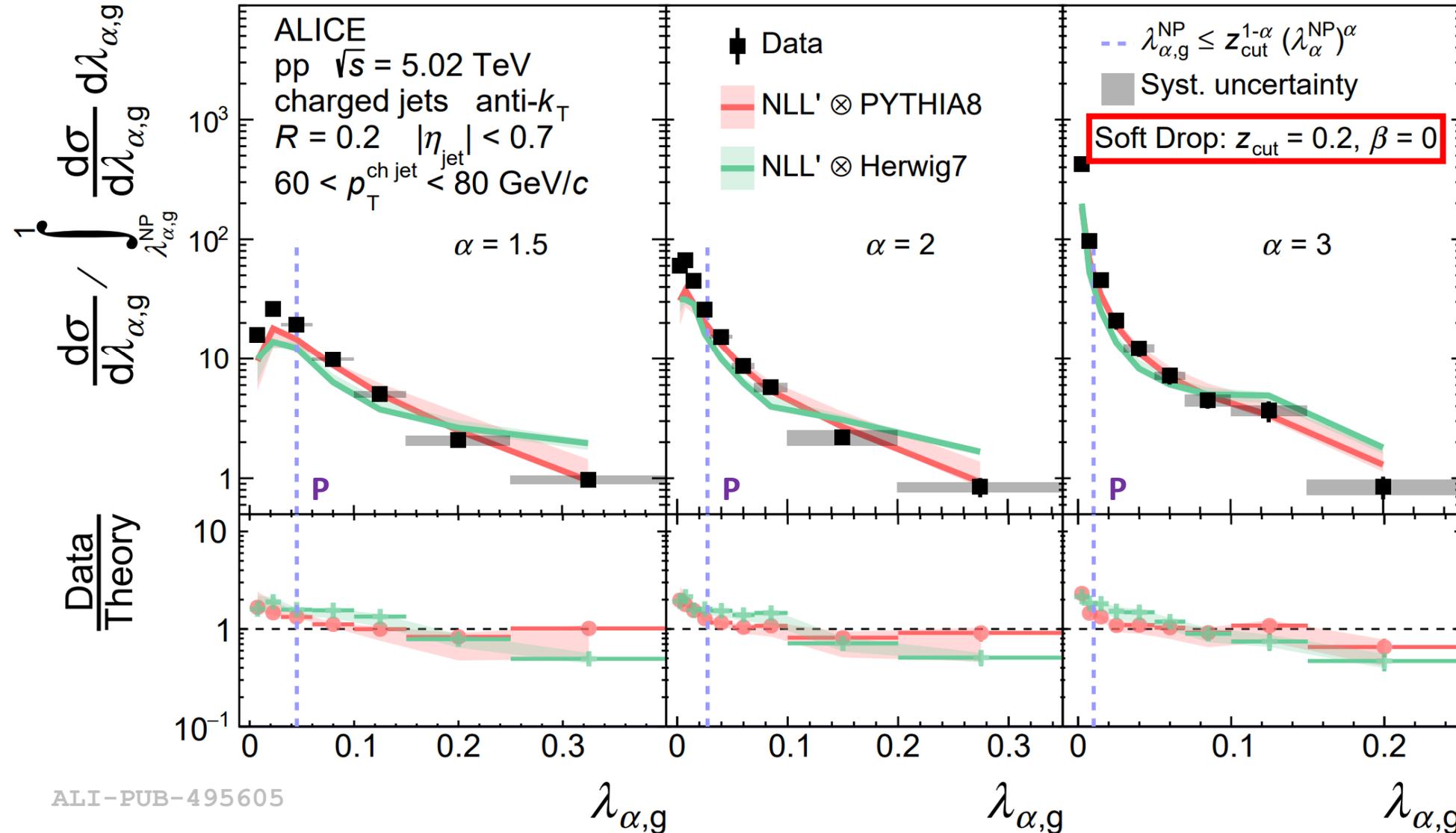


Distributions dominated by nonperturbative effects at large  $\alpha$

Agreement within perturbative region is reasonable

# pQCD predictions with SCET ( $R = 0.2$ )

$$\lambda_{\alpha}^{\kappa} \equiv \sum_{i \in \text{jet}} z_i^{\kappa} \theta_i^{\alpha}$$



SD grooming greatly increases the perturbative region for predictions

Reasonable agreement still seen within uncertainties

# Alternate hadronization correction

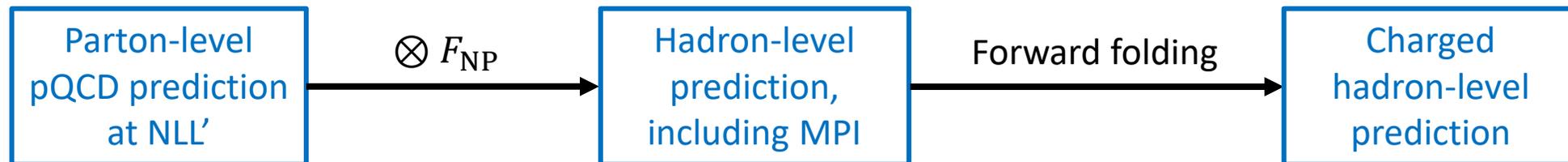
$$\lambda_\alpha^\kappa \equiv \sum_{i \in \text{jet}} z_i^\kappa \theta_i^\alpha$$

- Comparisons to Monte Carlo predictions are limited in interpretation
  - Highly-tuned phenomenological models

- Apply **nonperturbative shape function  $F$**  [8,9] from first principles:  $\Omega_\alpha = \frac{\Omega}{\alpha - 1}$

$$\frac{d\sigma}{dp_T d\lambda_\alpha} = \int dk F(k) \frac{d\sigma^{\text{pert}}}{dp_T d\lambda_\alpha} \left( \lambda_\alpha - \frac{k}{p_T R} \right) \sim \left( F * \frac{d\sigma^{\text{pert}}}{dp_T d\lambda_\alpha} \right) (\lambda_\alpha) \quad \text{where} \quad F(k) = \frac{4k}{\Omega_\alpha^2} \exp\left(-\frac{2k}{\Omega_\alpha}\right)$$

- Single-parameter ( $\Omega$ ) function: hadronization effects should be described by one (unknown to pQCD) parameter, containing **universal effects**
- Still requires folding to charged level, which is mostly well-described  $p_T$  shift

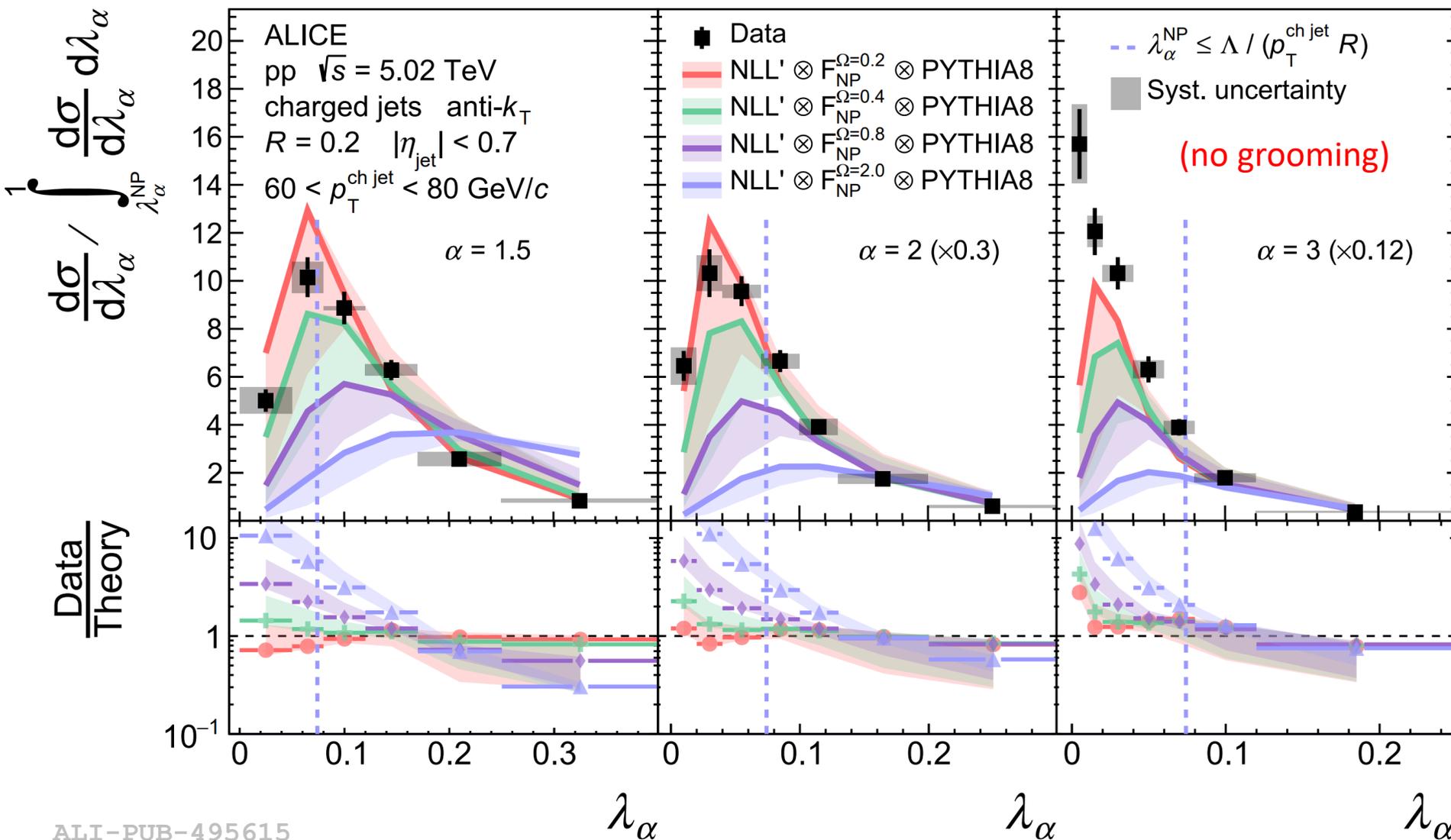


[8] G. Korchemsky, G. Sterman  
[Nuc. Phys. B 555 \(1999\) 335-351](#)

[9] E. Aschenaur, K. Lee, B. Page, F. Ringer  
[Phys. Rev. D 101, 054028 \(2020\)](#)

# pQCD predictions with SCET ( $R = 0.2$ )

$$\lambda_\alpha^\kappa \equiv \sum_{i \in \text{jet}} z_i^\kappa \theta_i^\alpha$$



Best agreement seen with smaller values of  $\Omega = 0.2$  or  $0.4$  GeV/c

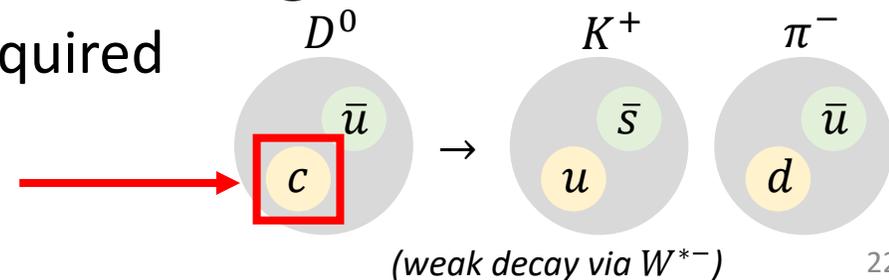
Tension with previous result of  $\Omega = 3.5$  GeV/c ( $R = 0.4$  full jets, higher  $p_T^{\text{jet}}$ , and for jet mass) [10]

$$\left( \lambda_{\alpha=2}^{\kappa=1} \sim \frac{m_{\text{jet}}^2}{p_{T,\text{jet}}^2} \right)$$

# Substructure of “heavy-flavor jets”

- Jets from **quarks of heavy flavor** (e.g. **charm**, **bottom**)
  - Much higher mass ( $m_c = 1.3 \text{ GeV}/c^2$ ,  $m_b = 4.2 \text{ GeV}/c^2 \gg m_{u,d} \sim \text{few MeV}/c^2$ )
- Primarily created from an initial hard scattering
  - Can be used to probe long timescales in the QGP
- Can be used to **boost the proportion of quark jets** over gluon jets
- Candidate jets are “tagged” based on decays and vertexing
  - Nontrivial corrections (efficiency, purity) are often required

*c* and *b* hadronize, then quickly decay into more stable particles

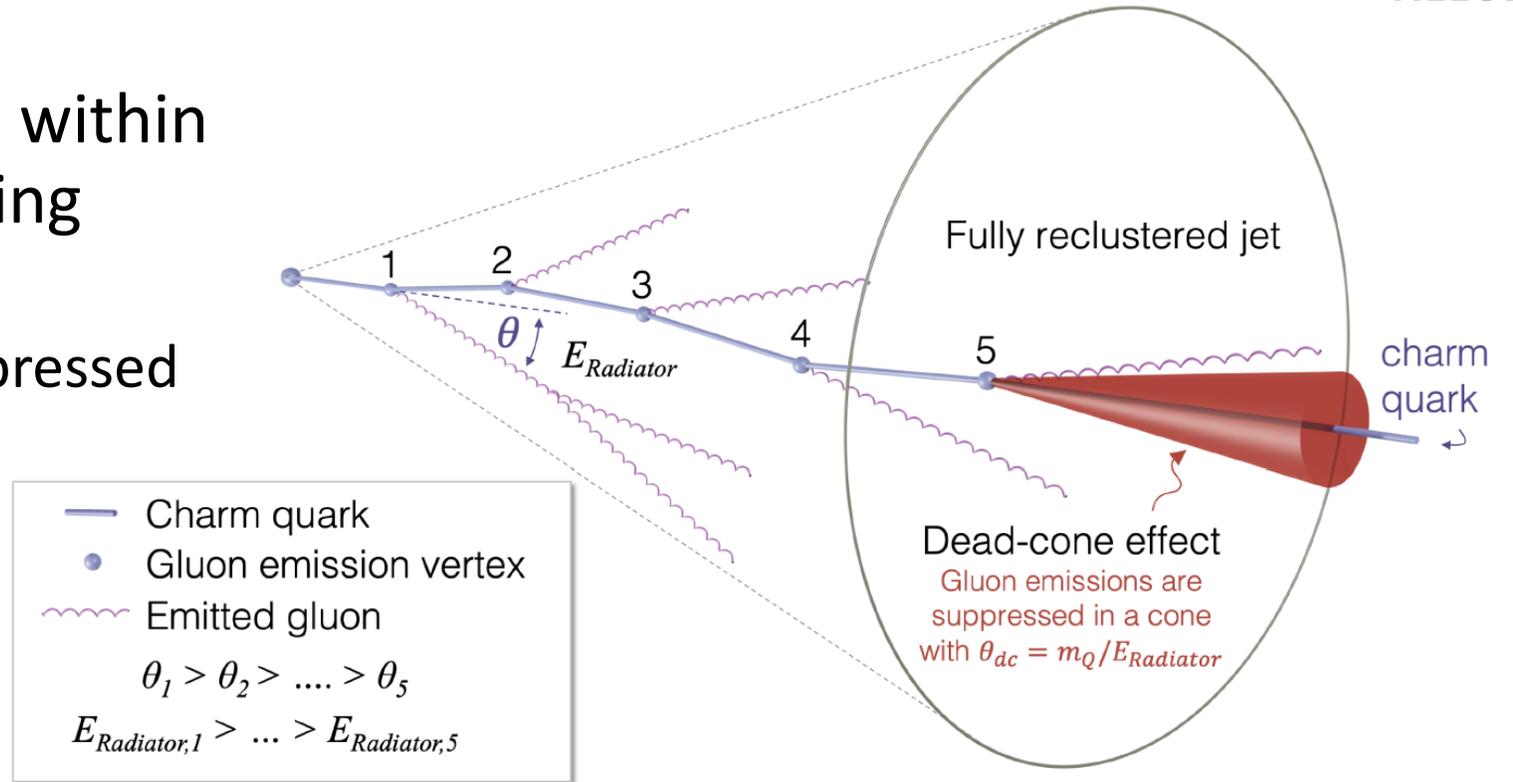


# Measuring the dead-cone effect in QCD

- Gluon radiation is suppressed within an angle  $m/E$  from the emitting particle <sup>[11]</sup>
  - Radiation should be more suppressed for heavy flavor quarks

## Challenges of measurement:

- 1) Identifying gluon radiation
  - Background contributions from hadronization, heavy hadron decays, ...
- 2) Determining dynamic direction of heavy quark throughout the shower



ALICE Collab.: [arXiv:2106.05713](https://arxiv.org/abs/2106.05713) [nucl-ex]

**Solution:** use declustering procedure with Cambridge/Aachen algorithm

<sup>[11]</sup> Y. Dokshitzer, V. Khoze, S. Troyan [J. Phys. G17 \(1991\) 1602](https://arxiv.org/abs/hep-th/9110274)

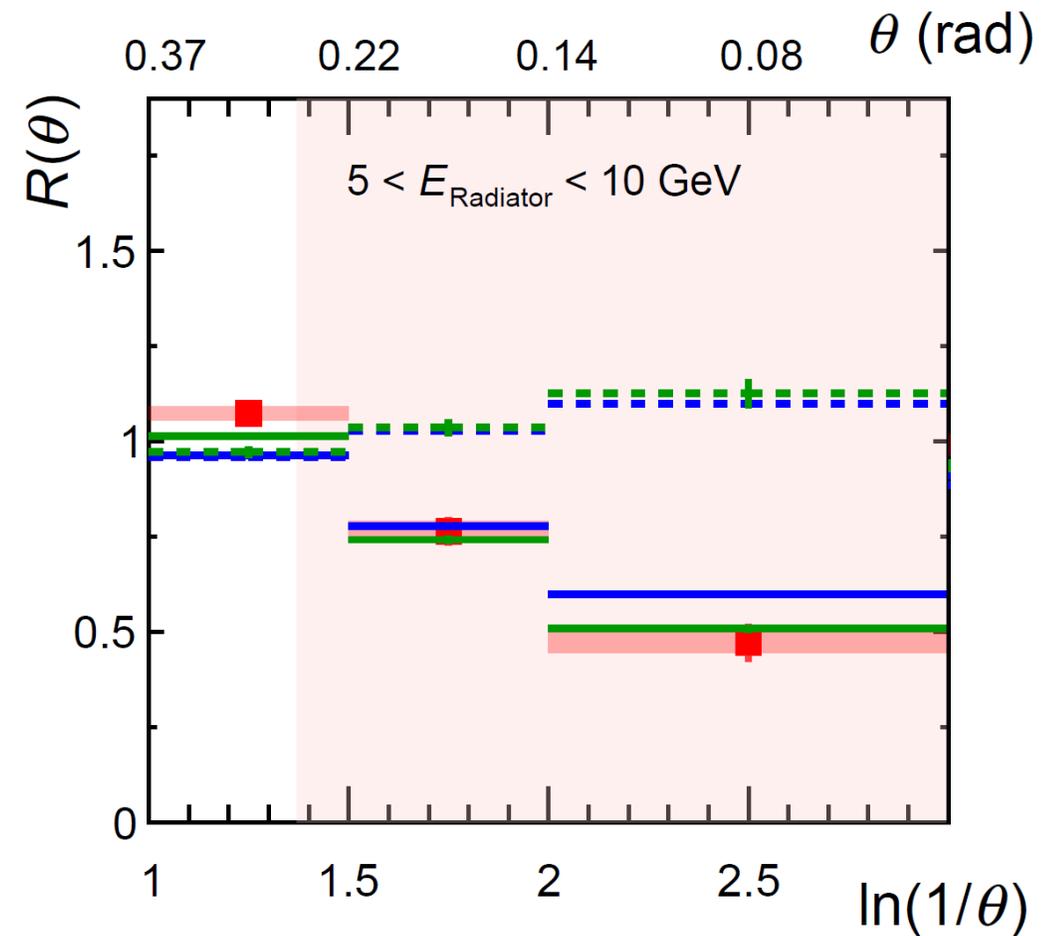
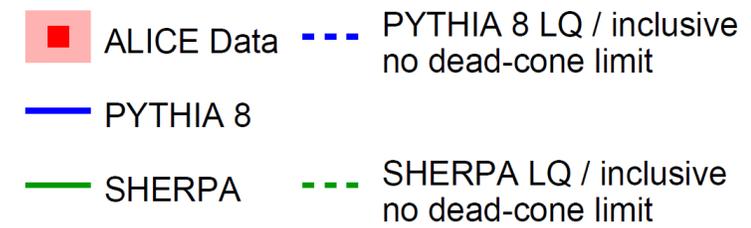
L. Cunqueiro, M. Płoskoń [Phys. Rev. D 99 \(2019\) 074027](https://arxiv.org/abs/1907.07402)

# First direct observation of dead-cone effect

- Calculate ratio of the splitting angle ( $\theta$ ) for  $D^0$ -tagged vs. inclusive jets, vs.  $E_{\text{radiator}}$

$$R(\theta) = \frac{1}{N^{D^0 \text{ jets}}} \frac{dn^{D^0 \text{ jets}}}{d\ln(1/\theta)} \bigg/ \frac{1}{N^{\text{inclusive jets}}} \frac{dn^{\text{inclusive jets}}}{d\ln(1/\theta)} \bigg|_{k_T, E_{\text{Radiator}}}$$

- 1) Reconstruct Lund Plane for **inclusive** and  $D^0$ -tagged jets
- 2) Project onto the angular axis, and take the ratio  $D^0$ -tagged / **inclusive**
- Significant suppression is seen, and is enhanced at lower  $E_{\text{radiator}}$



# Motivation for Pb-Pb studies

- **Quark-Gluon Plasma (QGP)** believed to form in heavy ion collisions
- Modifies jet interactions:
  - Jet quenching (see figure on right)
  - Momentum broadening
- Open questions:
  - Lumpy or smooth? What are the d.o.f.? q / g fraction? Hadronization? Factorization breaking? ...
- How else does the QGP modify the jets we observe?
  - → how can we study the QGP using jet observables?

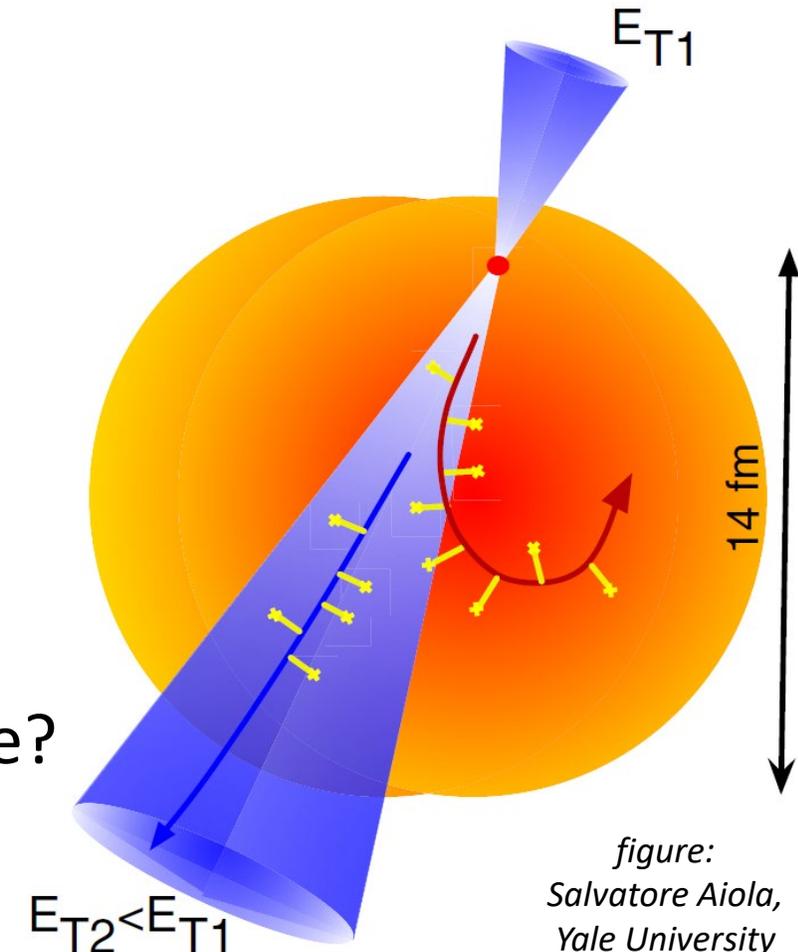
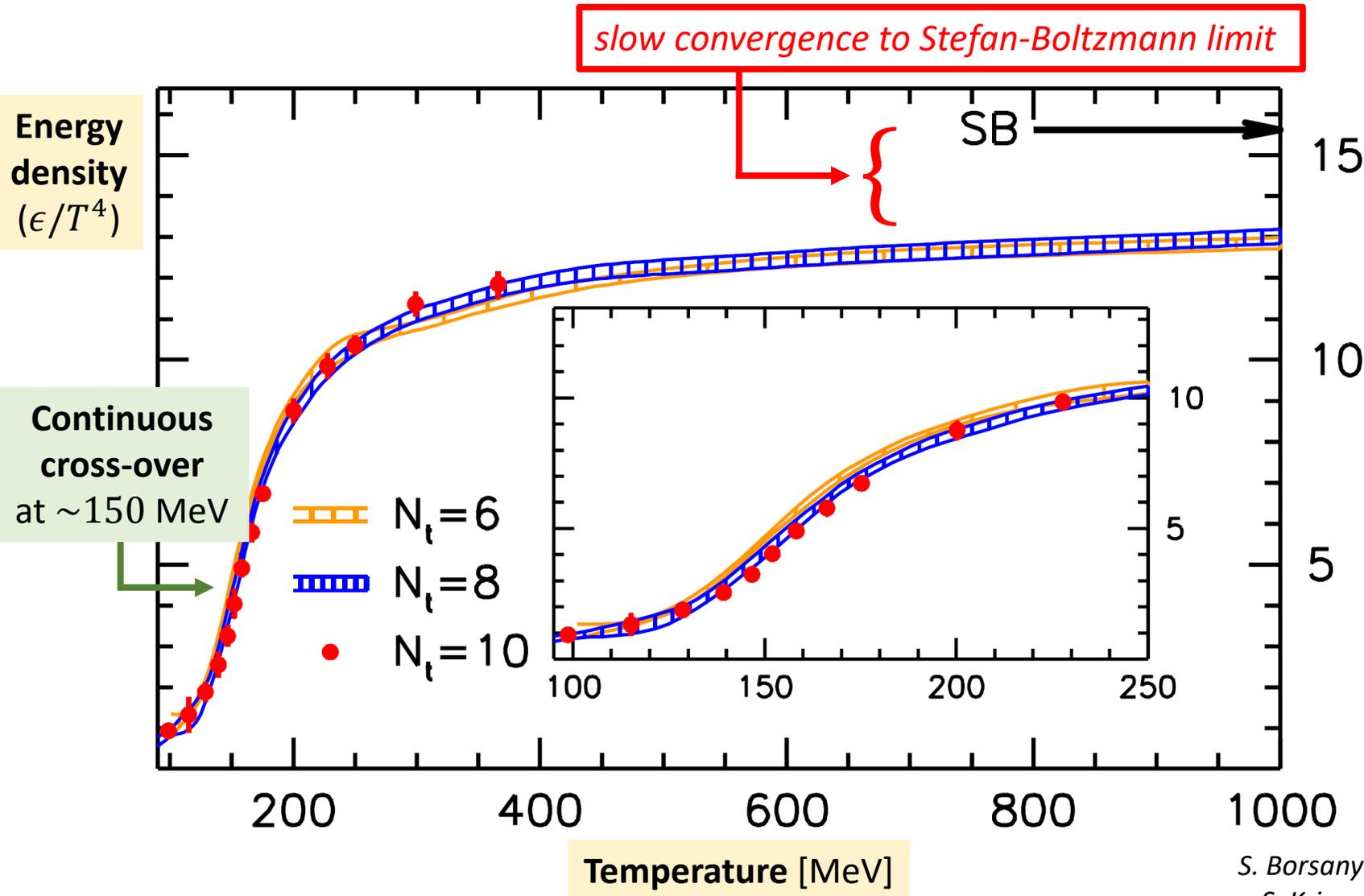


figure:  
Salvatore Aiola,  
Yale University

# Finite temperature QCD on the lattice



- **Lack of sharp phase transition**

- e.g. ionization of an atomic plasma

- **What carries the extra energy?**

- Complex  $q+g$  states?
  - “Strongly coupled” plasma effects?

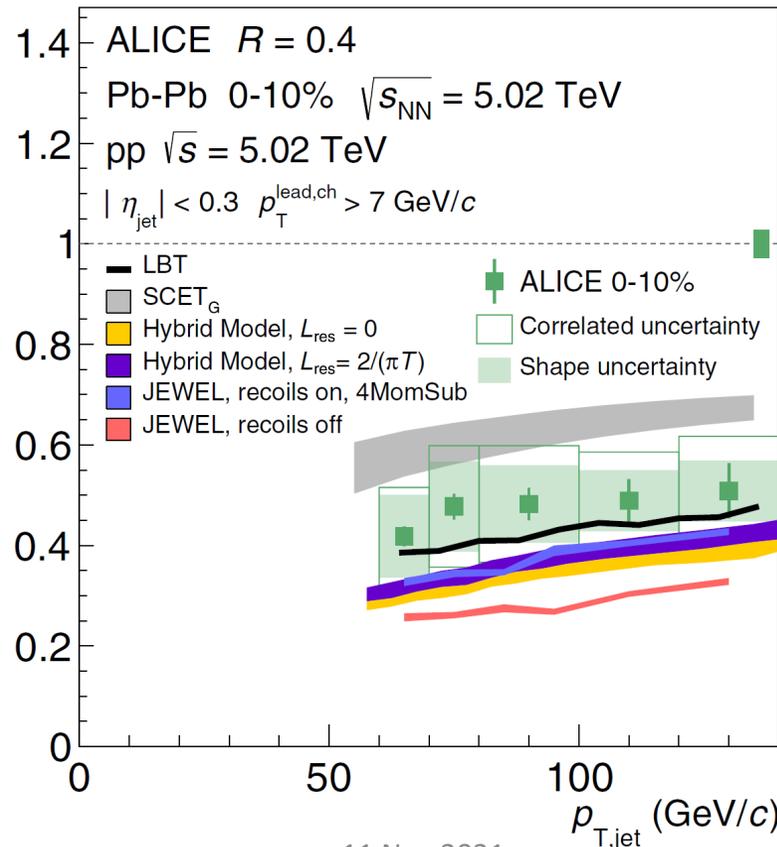
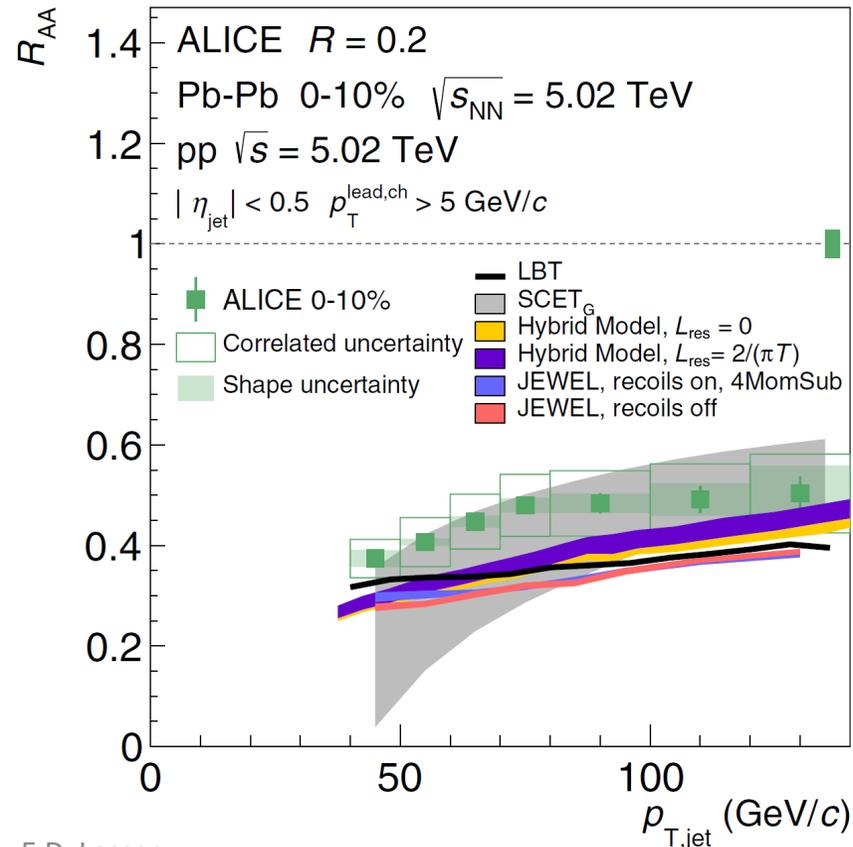
S. Borsanyi, G. Endrodi, Z. Fodor, A. Jakovac, S. Katz, S. Krieg, C. Ratti, K. Szabo [JHEP 1011 \(2010\) 077](https://arxiv.org/abs/1002.4467)

# Modification of jet cross section in Pb-Pb

$$R_{AA}^i(p_T) = \frac{d^2 N_{AA}^i / dp_T d\eta}{\langle T_{AA} \rangle d^2 \sigma_{NN}^i / dp_T d\eta}$$

→ Jet yield in AA (here Pb-Pb) collisions  
→ Jet cross section in pp collisions  
→ Geometry → # NN collisions

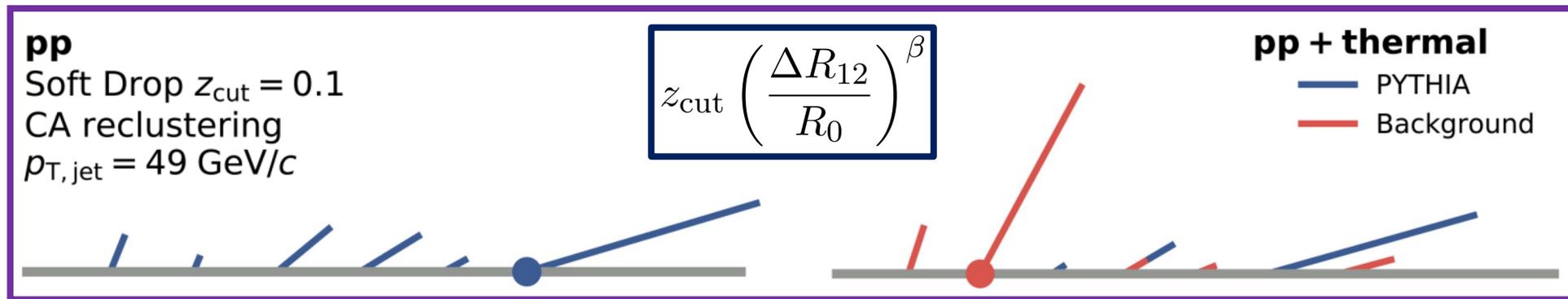
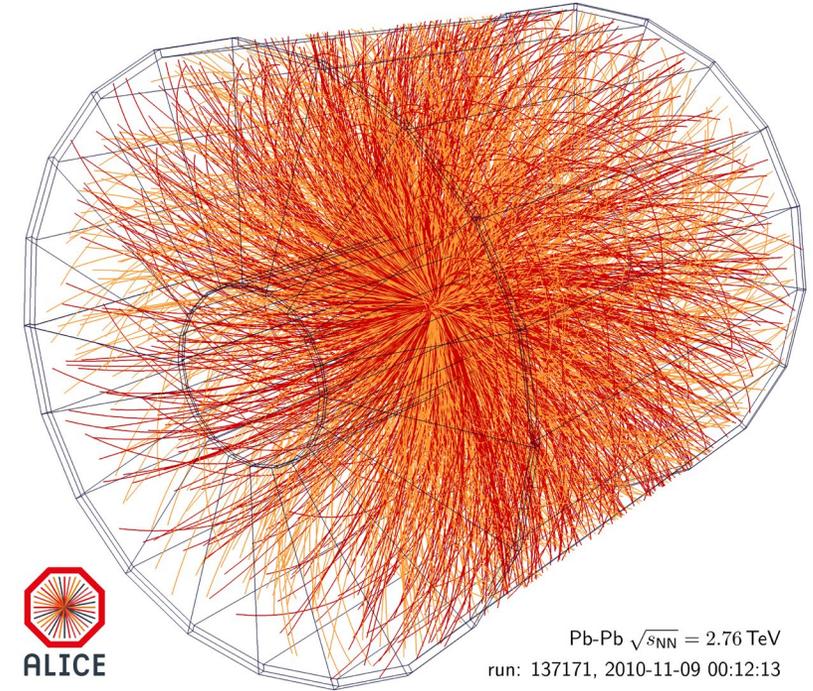
**No modification**  
 $\leftrightarrow R_{AA} = 1$



- **Strong suppression** of jet yield emulated by all of the quenching models
- Hints of disagreement with some models
  - Can we use **substructure measurements** to place stronger limits on some?

# Grooming settings in Pb-Pb

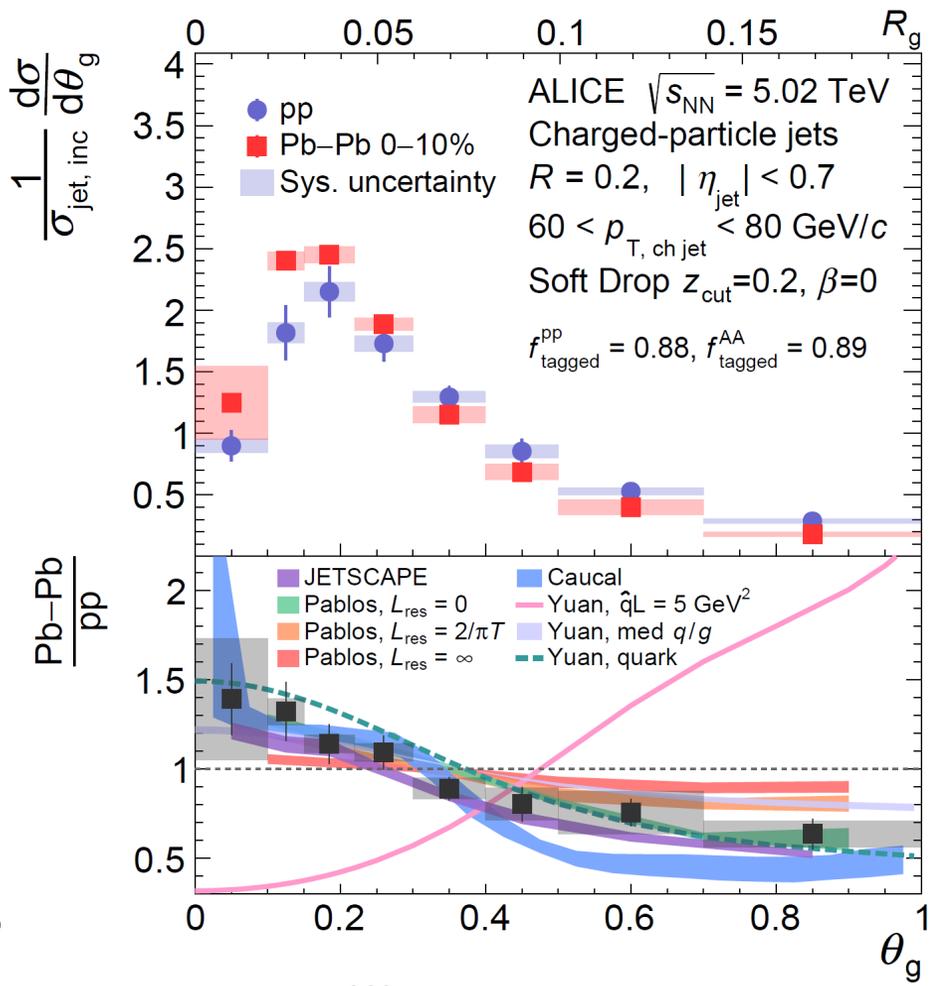
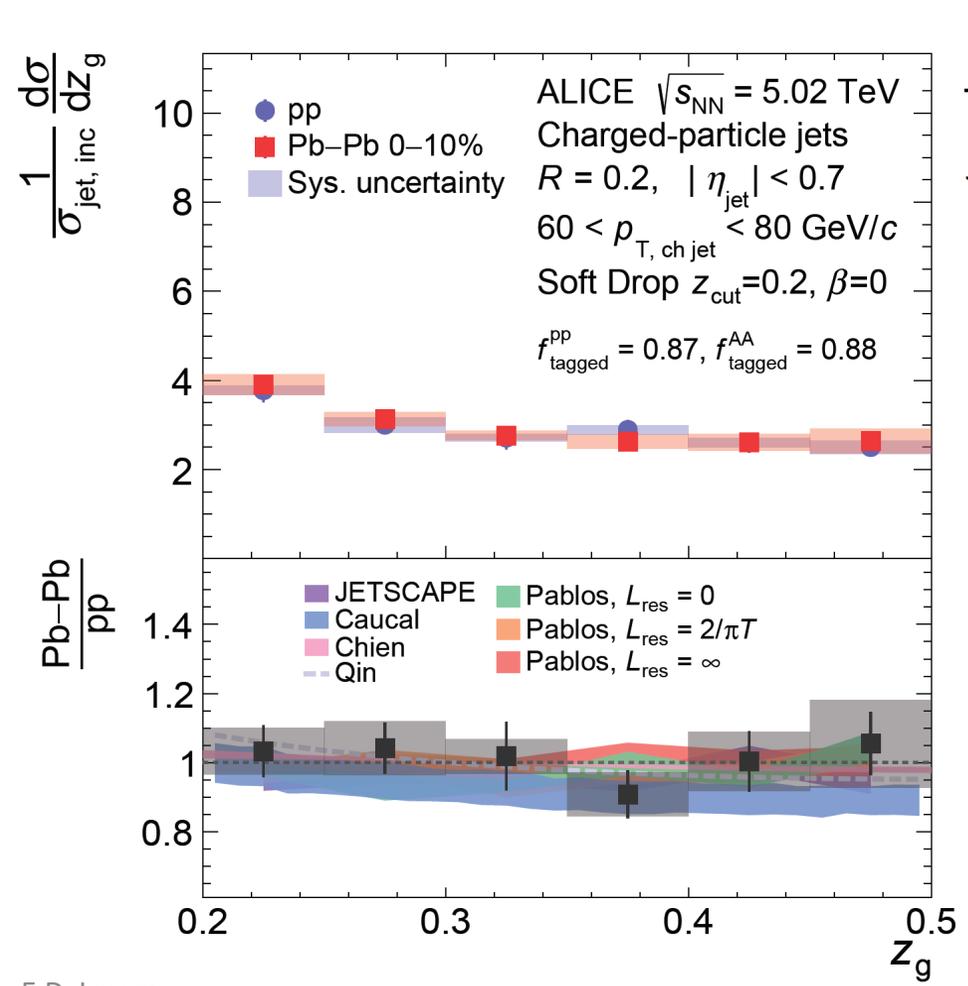
- Mistagging of the primary splitting occurs in jets in heavy-ion collisions due to the increased background
- Higher values of  $z_{\text{cut}} \geq 0.2$  (Soft Drop) increase the tagging purity in high-background environments [12]



[12] J. Mulligan, M. Płoskoń [Phys. Rev. C 102, 044913 \(2020\)](https://arxiv.org/abs/2004.04913)

# $z_g$ and $R_g$ in pp compared to Pb-Pb

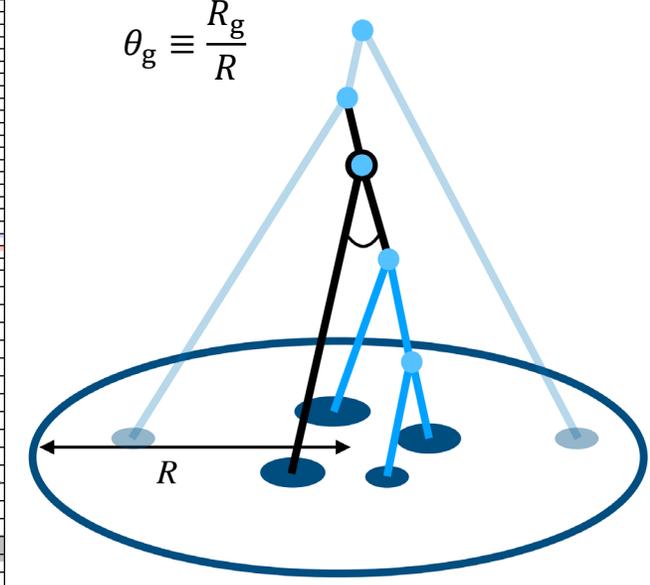
- Stronger grooming conditions ( $z_{\text{cut}} = 0.2$ ) allows fully-corrected groomed jet observables, and enabled the first measurement of  $\theta_g$  in Pb-Pb data



$$z_g \equiv \frac{p_{\text{T, subleading}}}{p_{\text{T, leading}} + p_{\text{T, subleading}}}$$

$$R_g = \sqrt{\Delta y^2 + \Delta \phi^2}$$

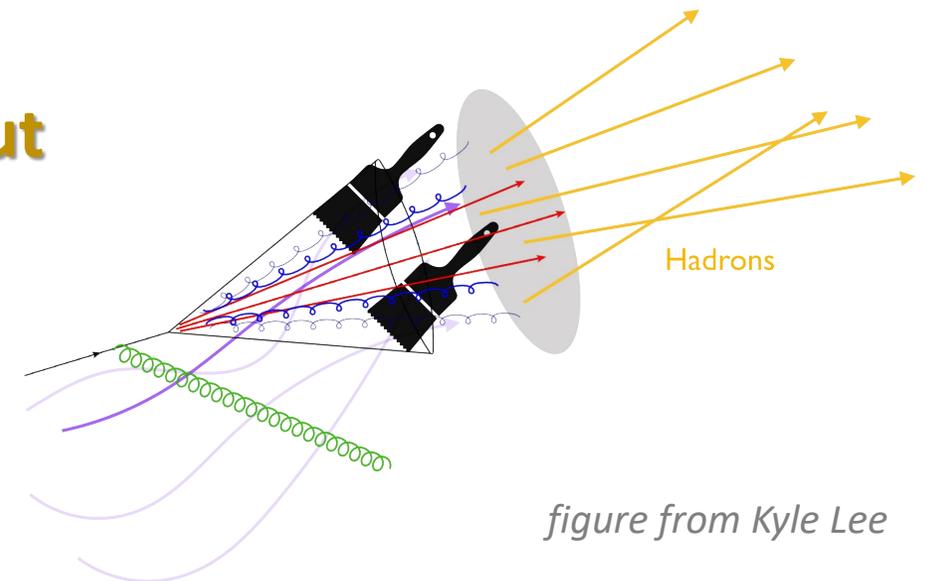
$$\theta_g \equiv \frac{R_g}{R}$$



ALICE Collab.: [arXiv:2107.12984](https://arxiv.org/abs/2107.12984) [nucl-ex]

# Conclusions

- ALICE has many **new and developing analyses** with novel comparisons to first-principles pQCD predictions
  - Stay tuned for new upcoming results!
- **Folding approach to nonperturbative corrections** can be used to constrain theory and Monte Carlo hadronization models
- Some new approaches to **mitigating large backgrounds** which appear in heavy-ion collisions
- Comparing measurements **with and without grooming** allows an approach to study soft effects
  - Grooming settings must be chosen in pp to maximize calculability and Pb-Pb comparisons



*figure from Kyle Lee*



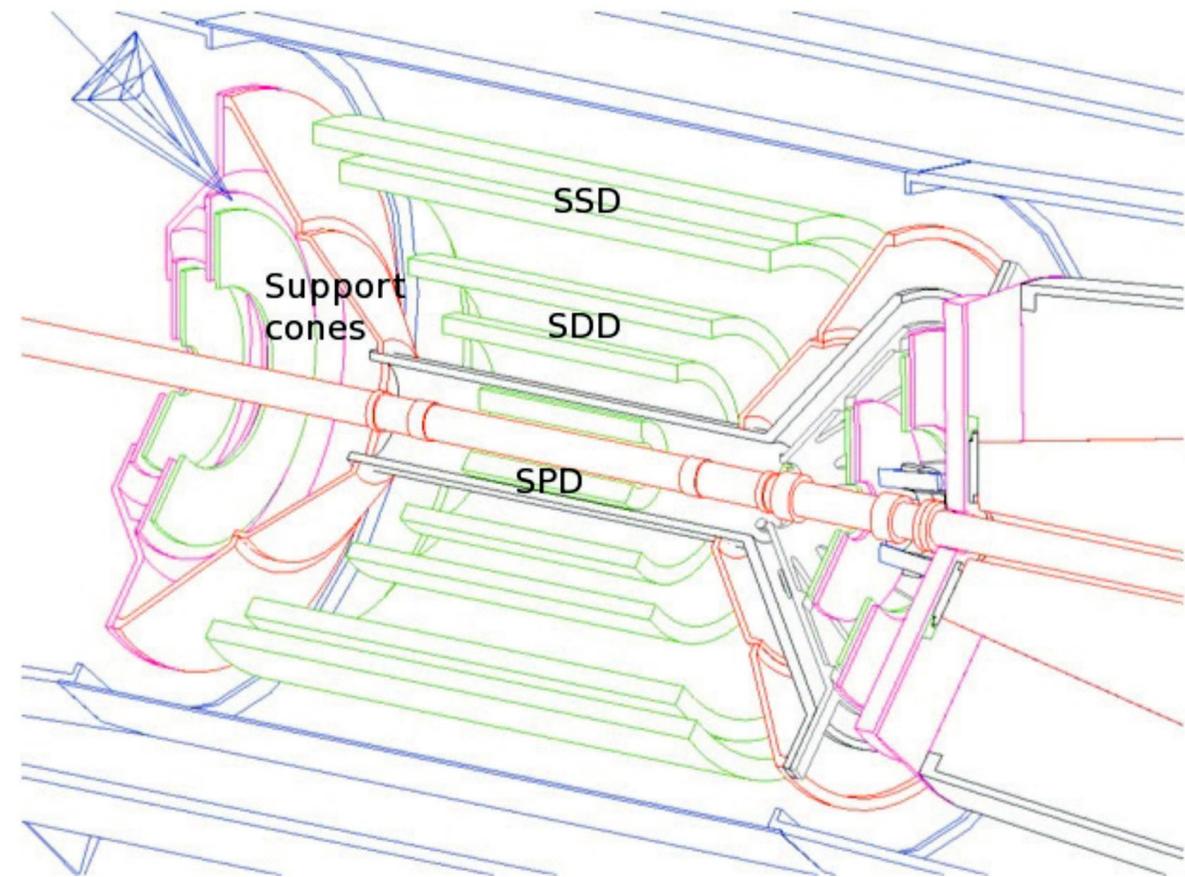
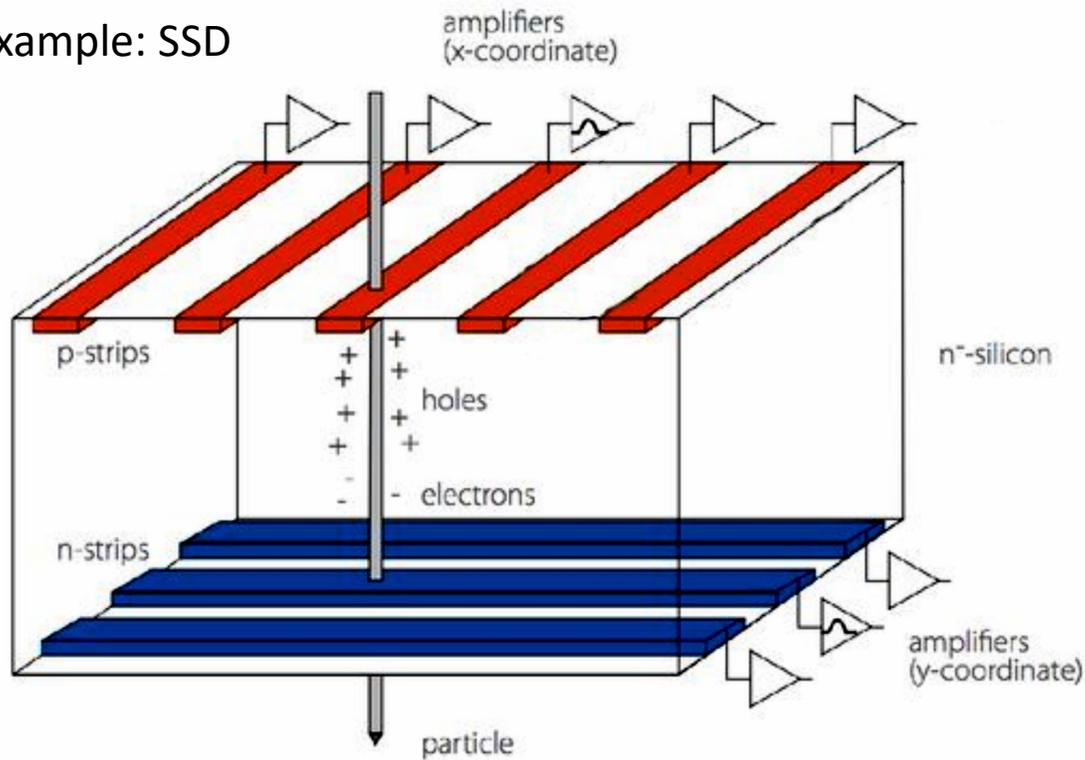
ALICE

# Backup

# ALICE Inner Tracking System (ITS)

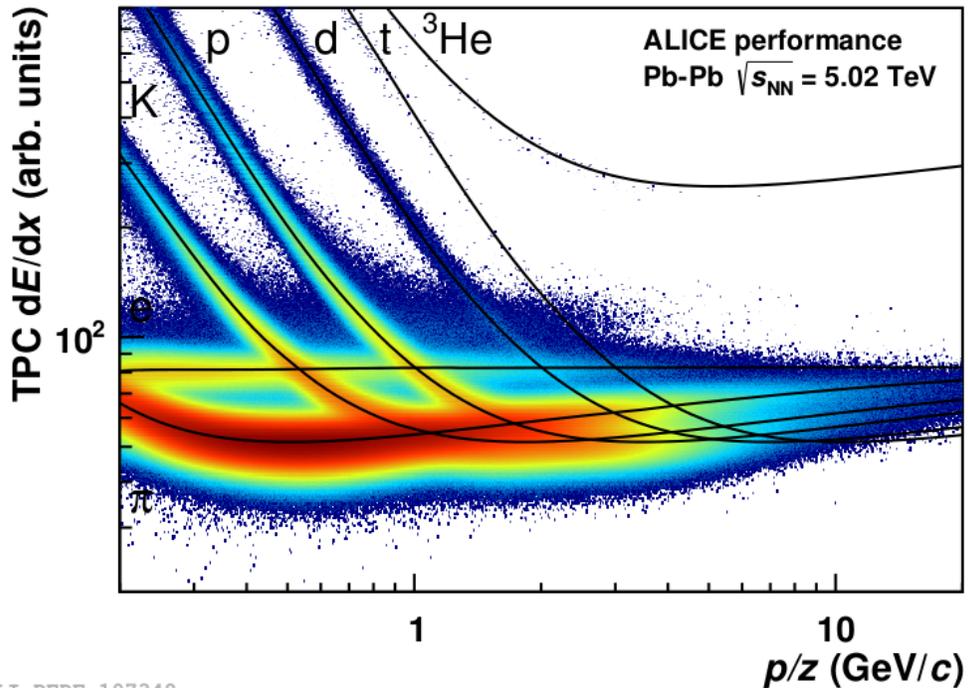
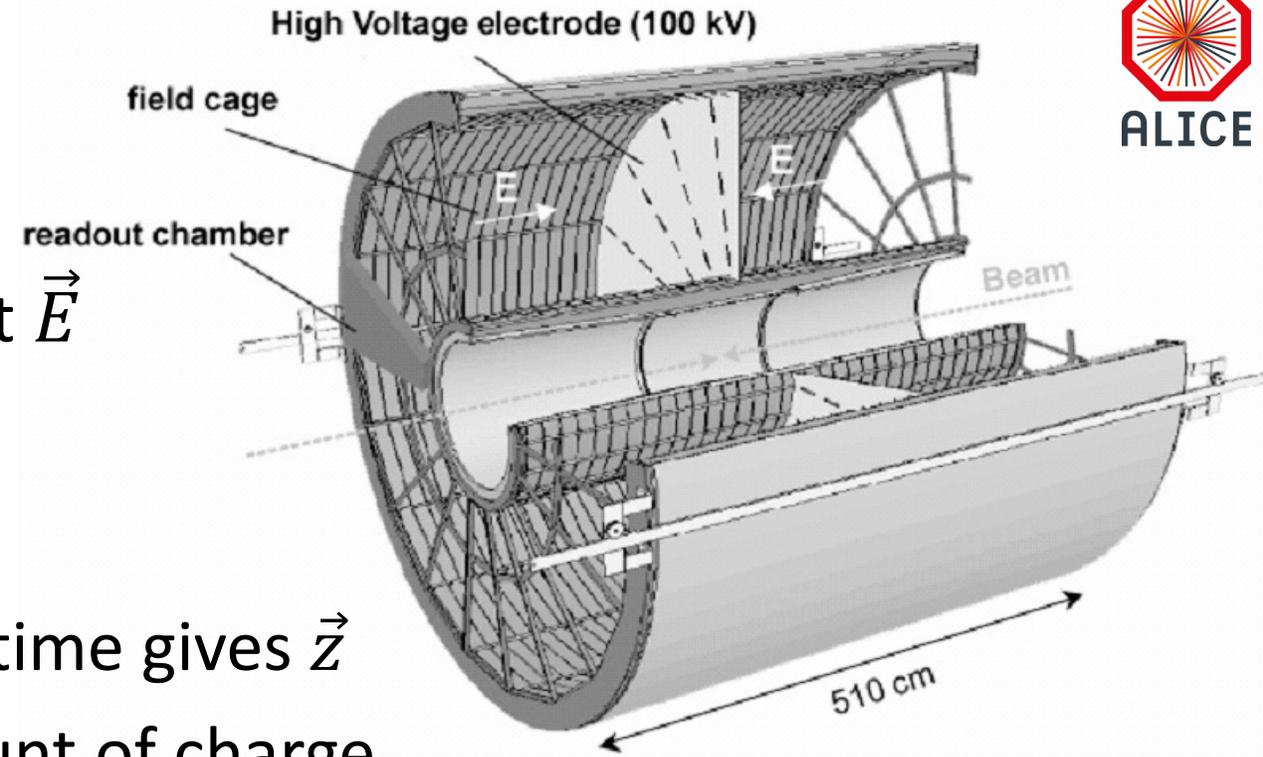
- 6 layers (two each of pixel, drift, and strip detectors)
- SSD & SDD can measure charge  $\rightarrow \frac{dE}{dx}$

Example: SSD

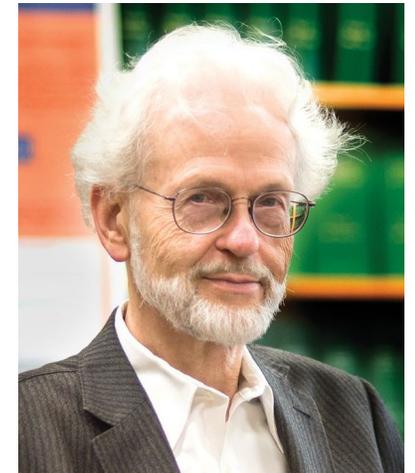


# ALICE TPC

- HV electrode creates high-gradient  $\vec{E}$
- Ionization electrons drift to wire chamber readout



- Drift time gives  $\vec{z}$
- Amount of charge (pulse height) correlates to the energy
- The first TPC was invented by David Nygren at LBNL 



David Nygren

# ALICE data (so far)

System	Year(s)	$\sqrt{s_{NN}}$ (TeV)	$L_{int}$
pp	2009-2013	0.9	200 $\mu\text{b}^{-1}$
		2.76	100 $\text{nb}^{-1}$
		7	1.5 $\text{pb}^{-1}$
		8	2.5 $\text{pb}^{-1}$
	2015, 2017	5.02	1.3 $\text{pb}^{-1}$
	2015-2018	13	36 $\text{pb}^{-1}$
pPb	2013	5.02	15 $\text{nb}^{-1}$
	2016	5.02	3 $\text{nb}^{-1}$
		8.16	25 $\text{nb}^{-1}$
Xe-Xe	2017	5.44	0.3 $\mu\text{b}^{-1}$
Pb-Pb	2010-2011	2.76	75 $\mu\text{b}^{-1}$
	2015, 2018	5.02	800 $\mu\text{b}^{-1}$

*compiled by: Yaxian Mao, Hard Probes 2020*

- As of November 2021, the ALICE Collaboration has 322 physics publications published in refereed journals
- Of those, 29 are published jet measurements ([link](#))
- The large integrated luminosity in **Run 2** allows precise new measurements and new observables

# Recent ALICE pp jet substructure measurements

- Generalized jet angularities (with and without grooming)
- Inclusive jet Lund Plane: <https://alice-figure.web.cern.ch/node/18640>
- First direct observation of the dead-cone effect: [Nucl. Phys. A \(Jan 2021\) 121905](https://arxiv.org/abs/2008.08864)
- Groomed  $z_g$  and  $R_g$  (Soft Drop & dynamical grooming): [ALICE-PUBLIC-2020-006](https://arxiv.org/abs/2006.08864)
- First measurement of  $D^0$ -tagged Soft Drop  $z_g/R_g/n_{SD}$ : [ALICE-PUBLIC-2020-002](https://arxiv.org/abs/2006.08864)
- Jet-axis differences: <https://alice-figure.web.cern.ch/node/19522>
- Fully-corrected  $N$ -subjettiness in pp and Pb-Pb: [CERN-EP-2021-082](https://arxiv.org/abs/2108.08201)
- Inclusive/leading subjet  $z_r$ : <https://alice-figure.web.cern.ch/node/19990>
- Using ML to reduce jet background: <https://alice-figure.web.cern.ch/node/16909>

# Jet reconstruction

- Jets are reconstructed from charged particle tracks using the **anti- $k_T$**  sequential recombination algorithm [5]
  - From an **IRC-safe** class of algorithms
  - **Soft-resilient**: shape is not strongly affected by soft, wide-angle radiation

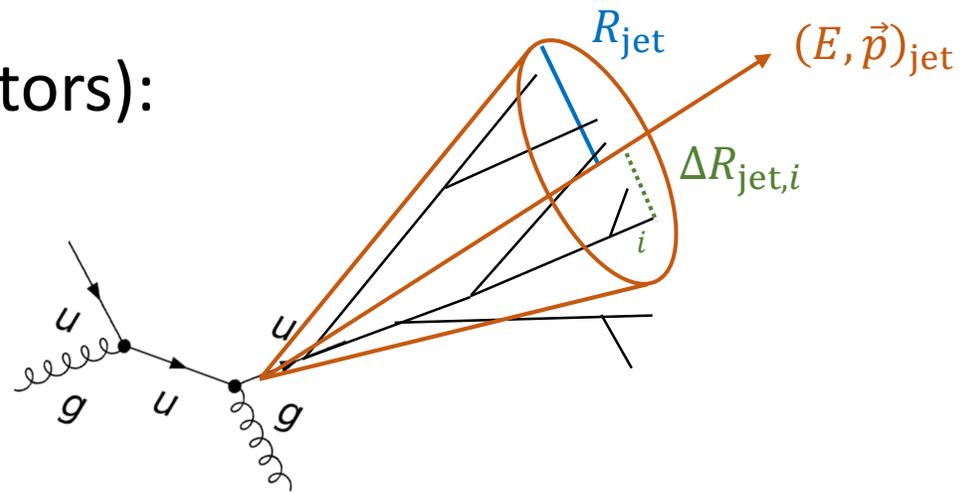
$$d_{ij} = \min \left( k_{Ti}^{2p}, k_{Tj}^{2p} \right) \frac{\Delta_{ij}^2}{R^2}$$

$$d_{iB} = k_{Ti}^{2p}$$

$$p = \begin{cases} 1, & \text{"inclusive"} k_T \\ 0, & \text{Cambridge/Aachen} \\ -1, & \text{anti } k_T \end{cases}$$

- **E-scheme** recombination (adding four vectors):

$$(E, \vec{p})_{\text{jet}} = \sum_{i \in \text{jet}} (E, \vec{p})_i$$



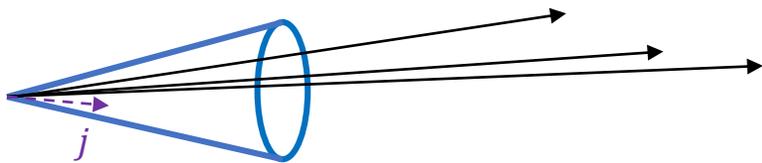
[5] [JHEP 0804:063,2008](https://arxiv.org/abs/0804.063)

# What is IRC safety?

$$\lambda_{\beta}^{\kappa} \equiv \sum_{i \in \text{jet}} \left( \frac{p_{T,i}}{p_{T,\text{jet}}} \right)^{\kappa} \left( \frac{\Delta R_{\text{jet},i}}{R} \right)^{\alpha} \equiv \sum_{i \in \text{jet}} z_i^{\kappa} \theta_i^{\alpha}$$

- Stands for **I**nfra-**R**ed and **C**ollinear (**IRC**) safety
- Class of reconstruction algorithms & observables which satisfy certain conditions in order to avoid singularities from appearing in a well-defined path towards theoretical calculation

**Infra-Red safety:** the observable should not change if an infinitely-low-momentum particle is added to the event/jet



$$\lambda_{\alpha,\text{new}}^{\kappa} = \sum_{i \in \text{jet}} z_i^{\kappa} \theta_i^{\alpha} + z_j^{\kappa} \theta_j^{\alpha}$$

$$z_j = 0 \rightarrow z_j^{\kappa} \theta_j^{\alpha} = 0 \quad (\kappa > 0)$$

$$\lambda_{\alpha,\text{new}}^{\kappa} = \lambda_{\alpha,\text{old}}^{\kappa}$$

**Collinear safety:** the observable should not change if one particle splits into two collinear particles

$$\lambda_{\alpha,\text{new}}^{\kappa} = \sum_{(i \neq j) \in \text{jet}} z_i^{\kappa} \theta_i^{\alpha} + (\lambda z_j)^{\kappa} \theta_j^{\alpha} + [(1 - \lambda) z_j]^{\kappa} \theta_j^{\alpha}$$

$$\text{Need } \lambda^{\kappa} + (1 - \lambda)^{\kappa} = 1 \quad \forall \{\lambda \in [0,1]\} \rightarrow \kappa = 1$$

Consider 1-particle jet:  $\lambda_{\alpha,\text{new}}^{\kappa} = (\lambda z_j)^{\kappa} \theta_j^{\alpha} + [(1 - \lambda) z_j]^{\kappa} \theta_j^{\alpha}$

$$\theta_j = 0 \rightarrow z_j^{\kappa} \theta_j^{\alpha} = 0 \quad (\alpha > 0)$$

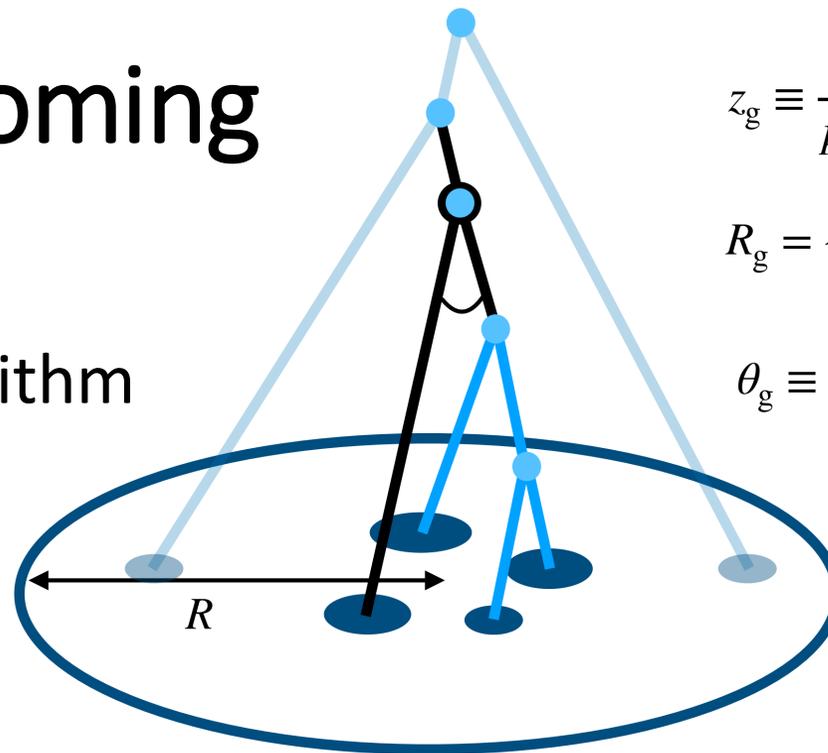
# Charged-particle jet observables

- Charged-particle jets are useful for substructure observables since tracking detectors give **enhanced spatial precision**
- However, track-based observables are IRC-unsafe
- Formalism to calculate these observables using **track functions** <sup>[5]</sup>
- Currently we use the IRC-safe observables to motivate our measurements, and then apply nonperturbative corrections using different methods

<sup>[5]</sup> *H. Chang, M. Procura, J. Thaler, W. Waalewijn*  
[Phys. Rev. Lett. 111 \(2013\) 102002](#)

# Going deeper: jet grooming

- Recluster jet into ordered tree using Cambridge-Aachen algorithm
- Trim branches, using one of two different algorithms:
  - **Soft Drop grooming** [3]
    - Removes soft, wide-angle radiation
  - **Dynamical grooming** [4]
    - Identifies the “hardest” splitting
- IRC or Sudakov safe [5]
  - Repeatable on theoretical predictions



$$z_g \equiv \frac{p_{T,\text{subleading}}}{p_{T,\text{leading}} + p_{T,\text{subleading}}}$$

$$R_g = \sqrt{\Delta y^2 + \Delta \phi^2}$$

$$\theta_g \equiv \frac{R_g}{R}$$

Soft Drop Condition:

$$\frac{\min(p_{T1}, p_{T2})}{p_{T1} + p_{T2}} > z_{\text{cut}} \left( \frac{\Delta R_{12}}{R_0} \right)^\beta$$

[3] A. Larkoski, S. Marzani, G. Soyez, J. Thaler [JHEP 1405 \(2014\) 146](#)

“Hardness”:

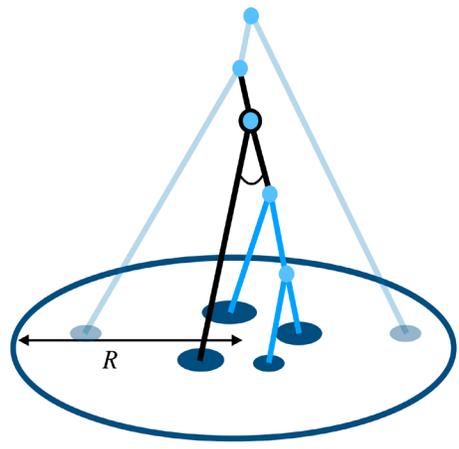
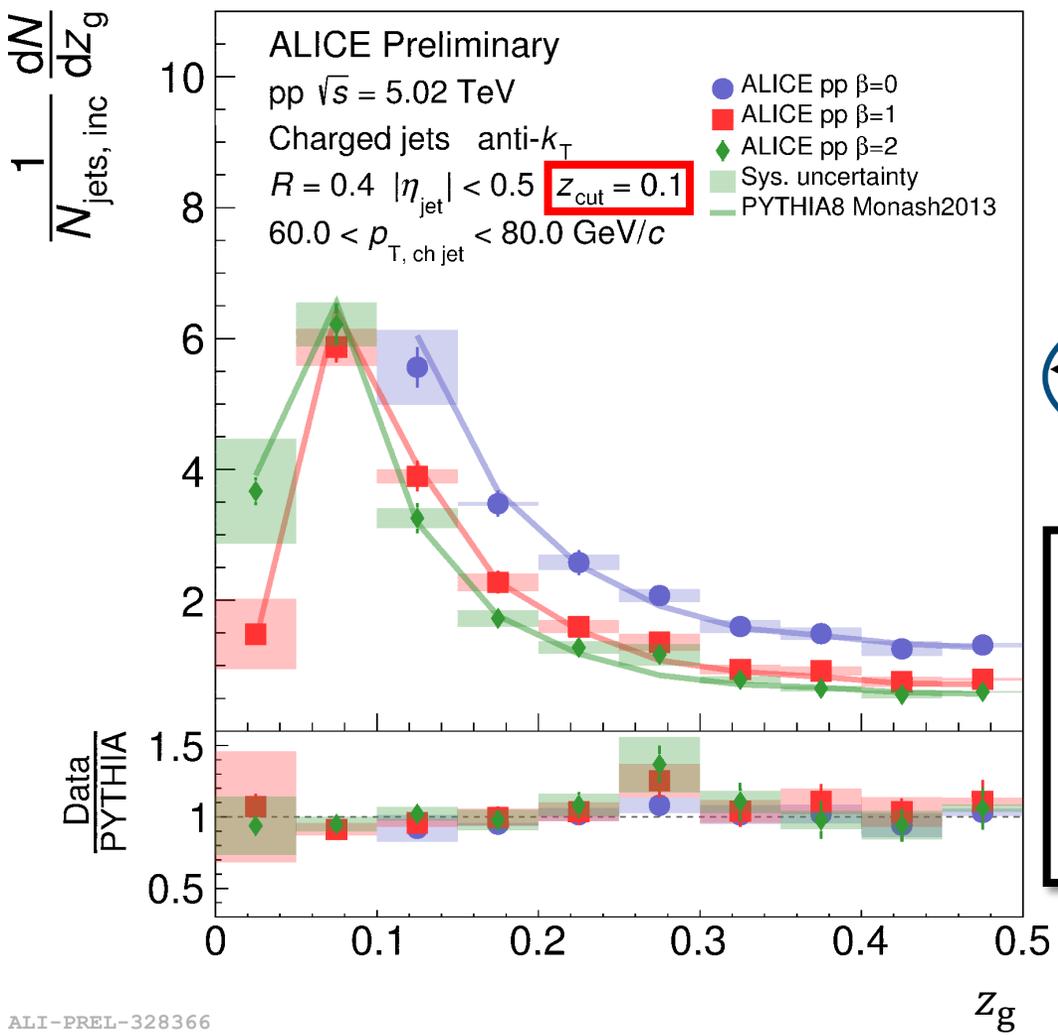
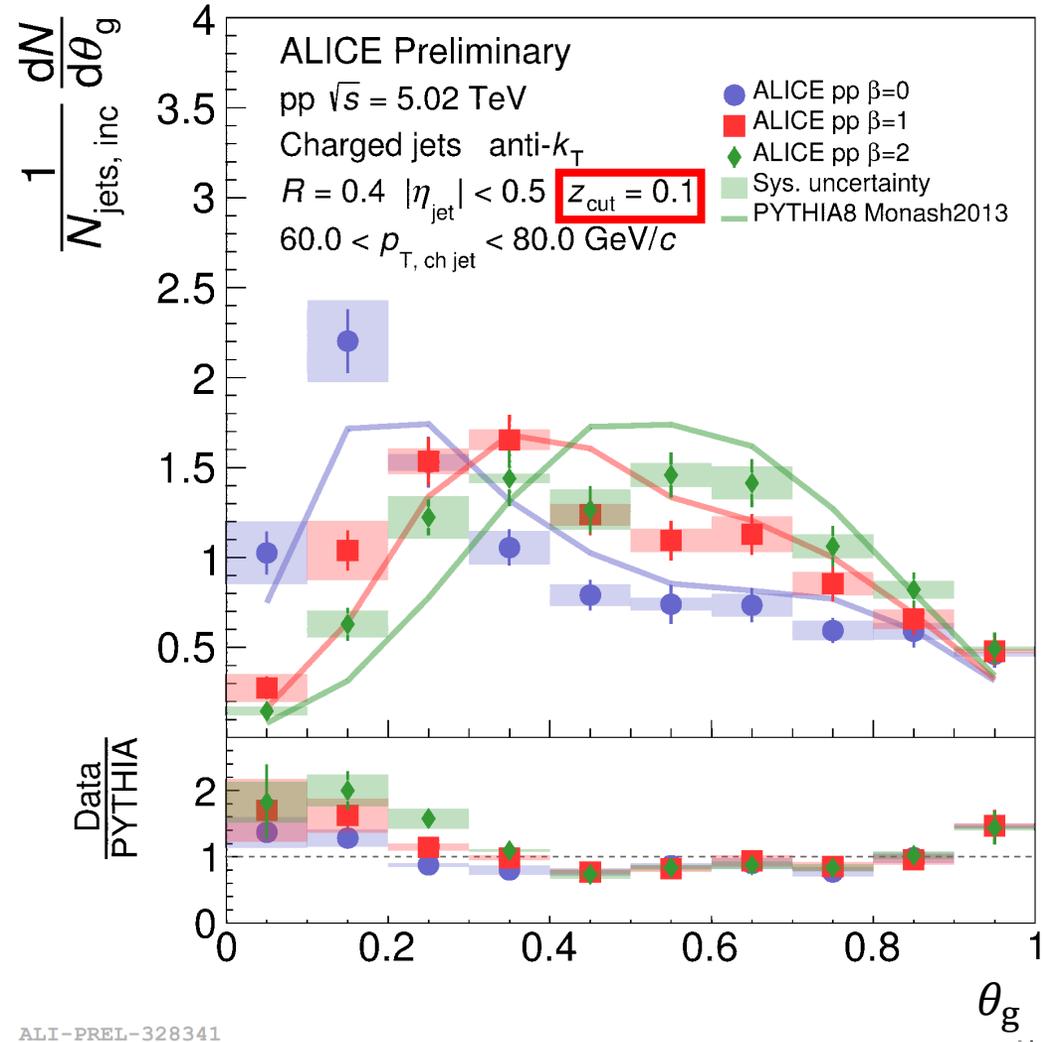
$$\kappa^{(a)} = \frac{1}{p_T} \max_{i \in \text{C/A seq.}} \left[ z_i (1 - z_i) p_{T,i} \left( \frac{\theta_i}{R} \right)^a \right]$$

[4] Y. Mehtar-Tani, A. Soto-Ontoso, K. Tywoniuk [Phys. Rev. D 101 \(2020\) 034004](#)

[5] A. Larkoski, S. Marzani, J. Thaler [Phys. Rev. D 91 \(2015\) 111501](#)

# $z_g$ and $R_g$ with Soft Drop grooming

- Comparisons to PYTHIA show stronger modification with larger  $\beta$

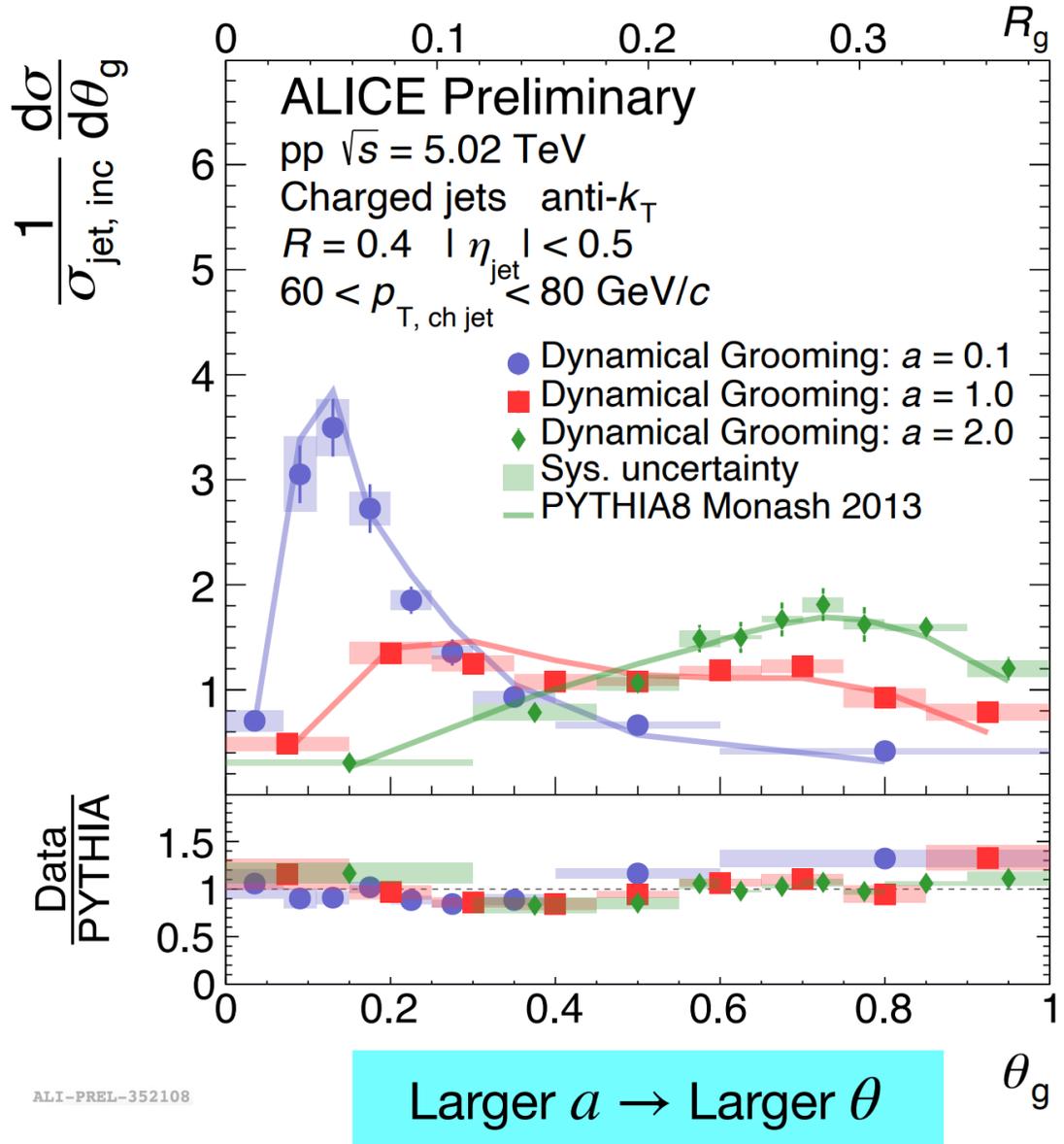


$$z_g \equiv \frac{p_{T, subleading}}{p_{T, leading} + p_{T, subleading}}$$

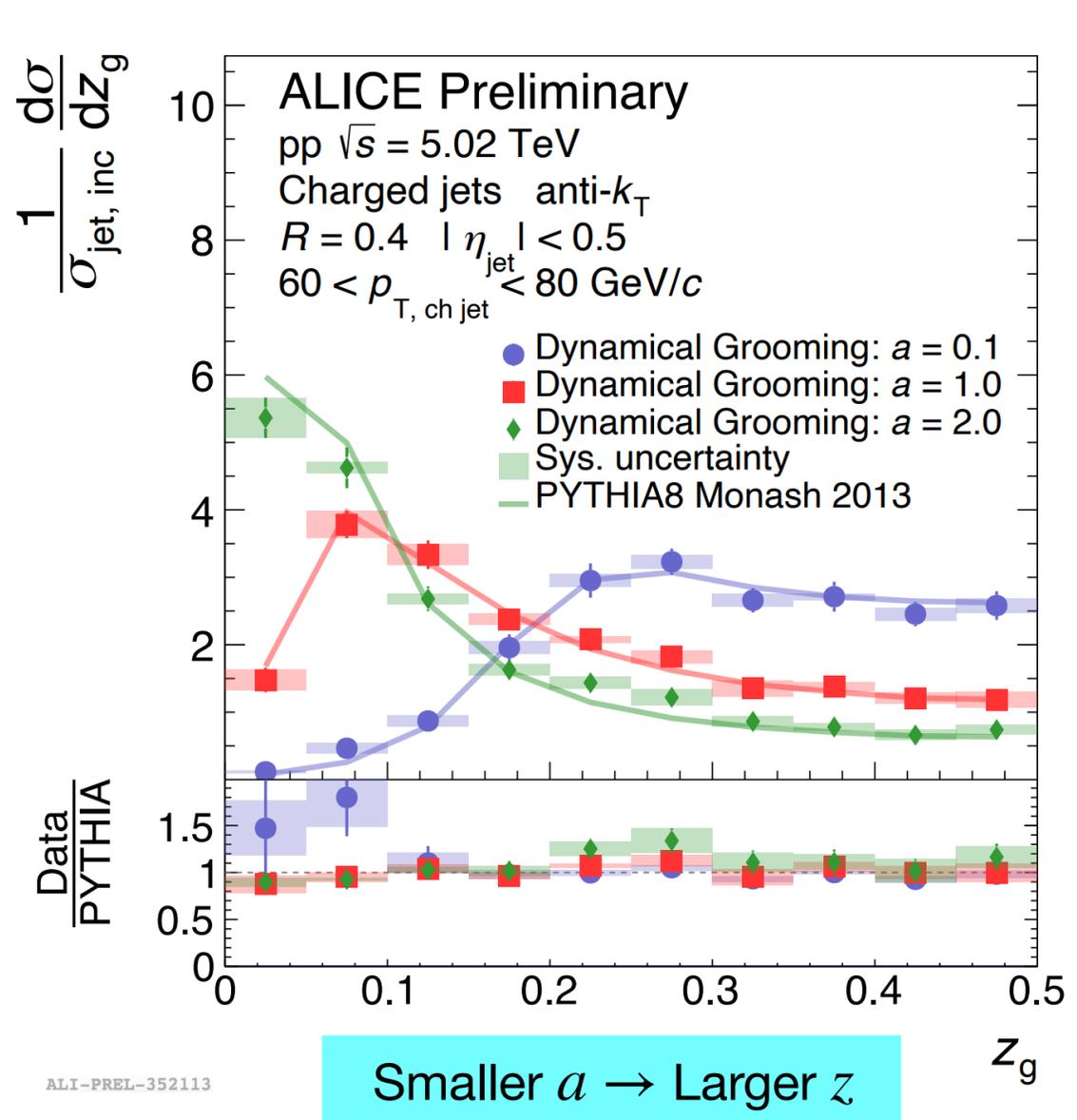
$$R_g = \sqrt{\Delta y^2 + \Delta \phi^2}$$

$$\theta_g \equiv \frac{R_g}{R}$$

# First measurement with Dynamical Grooming

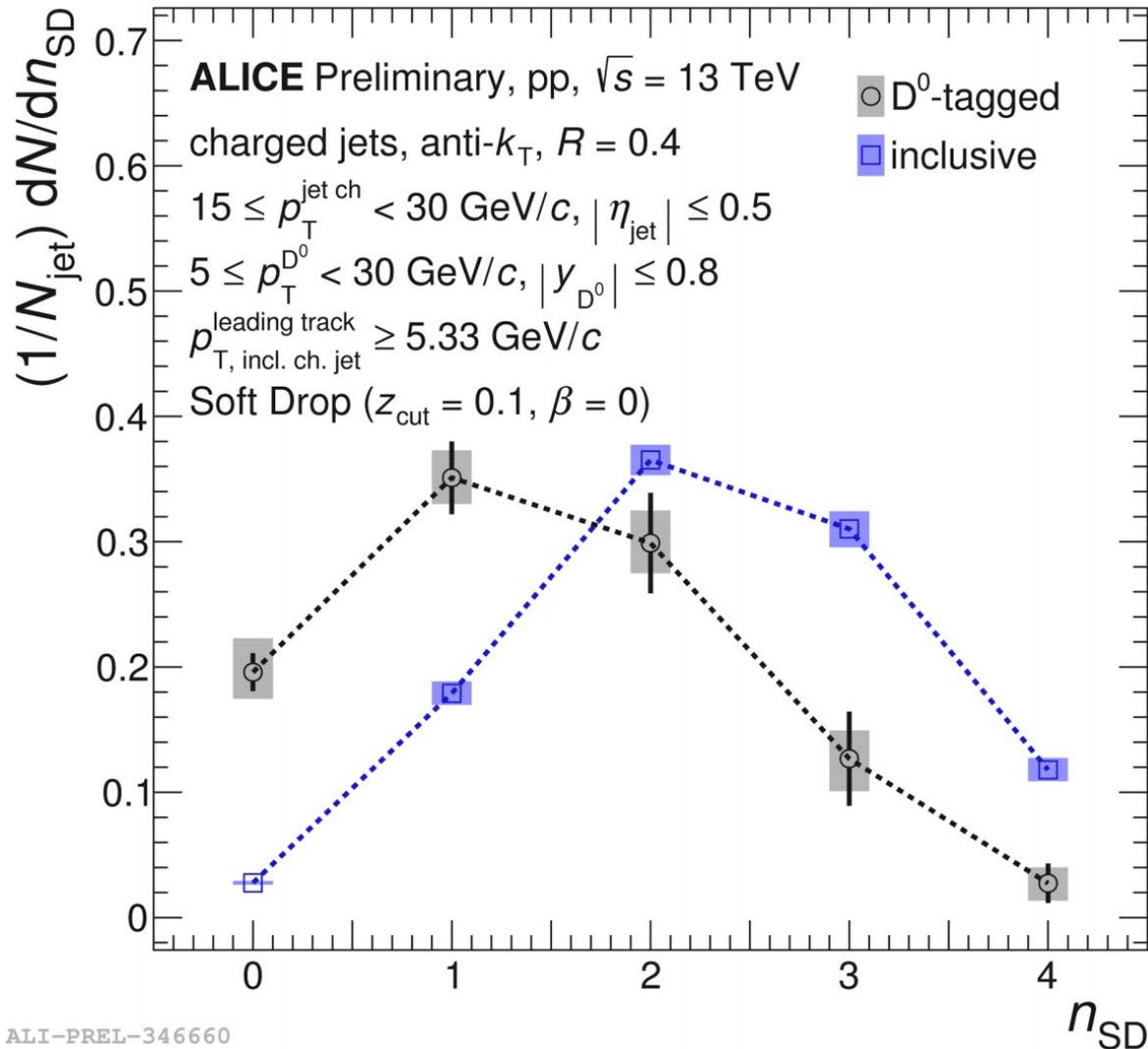


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ALI-PREL-352113

# First measurement of $z_g/R_g/n_{SD}$ in $D^0$ -tagged jets

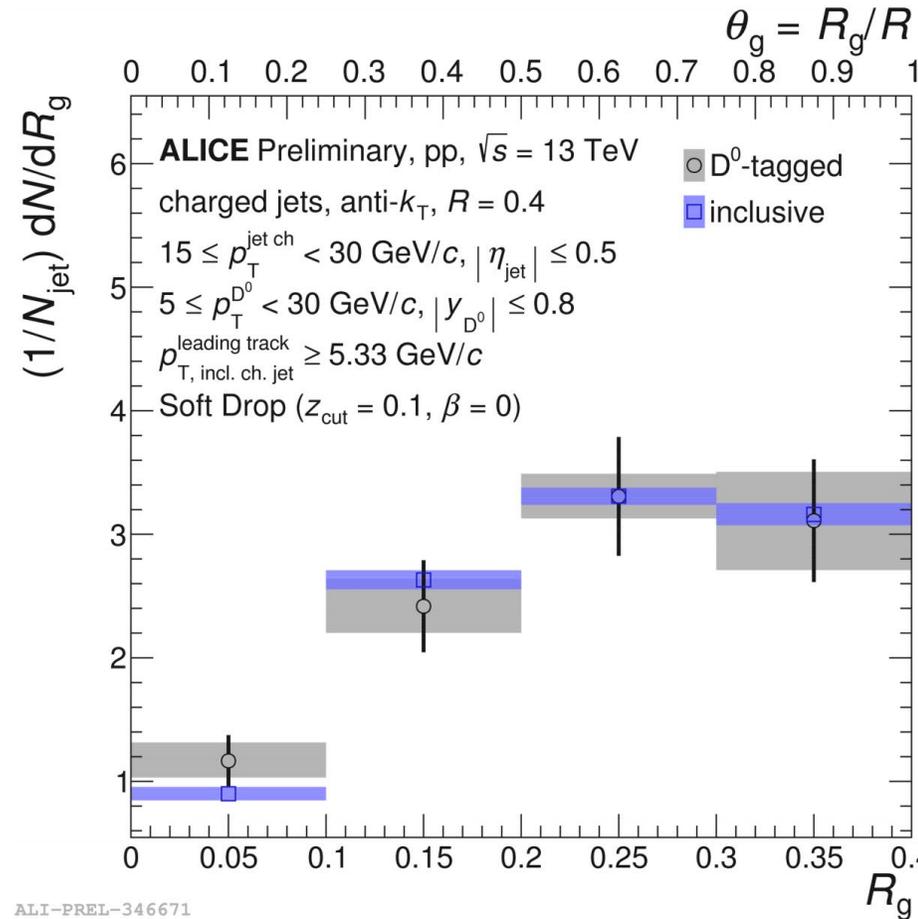
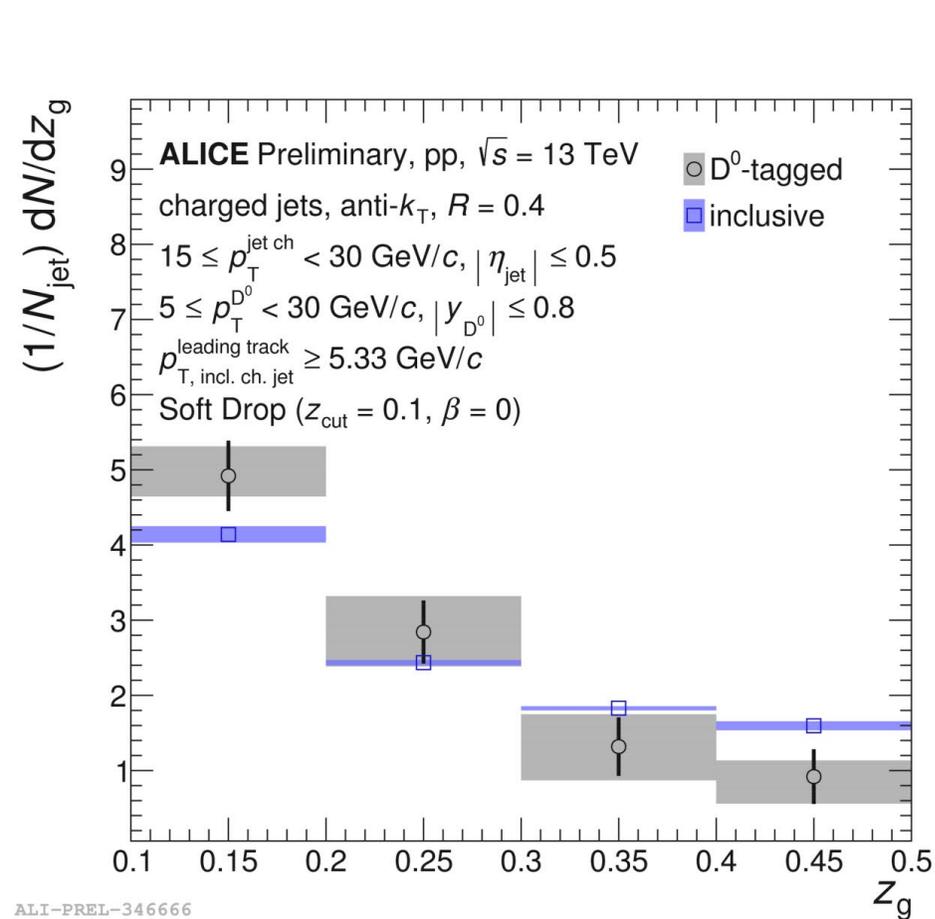


ALI-PREL-346660

- $n_{SD}$  is the number of splittings which pass the Soft Drop grooming condition
  - Follows the hardest branch
- **$D^0$ -tagged jets have fewer splittings** than inclusive jets
- Consistent with quark jets being **harder with fewer emissions** than gluon jets

# First measurement of $z_g/R_g/n_{SD}$ in $D^0$ -tagged jets

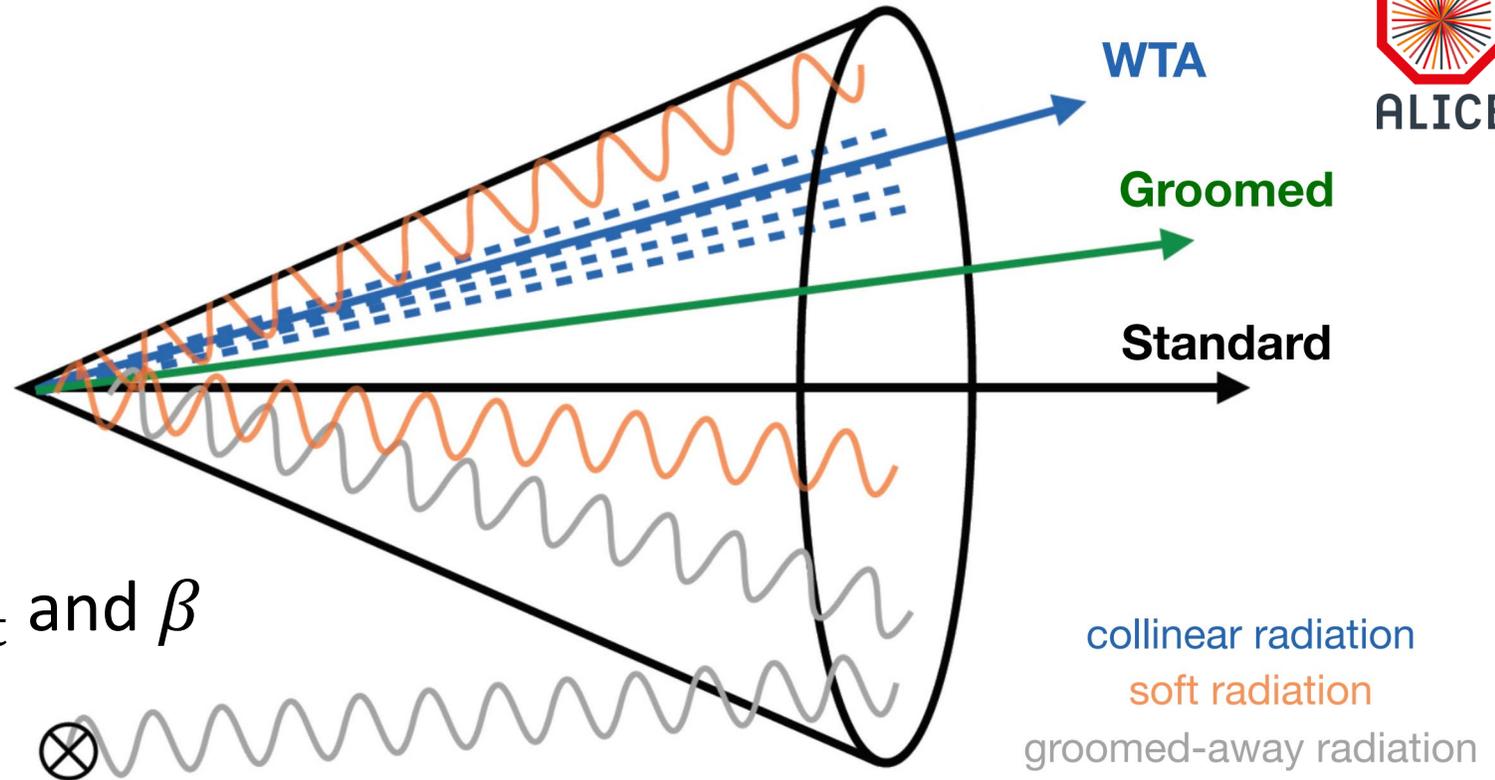
- Reconstruct  $D^0$  mesons through  $D^0 \rightarrow K^- \pi^+$  decay channel
- Calculate substructure observable in signal and both sideband regions



- Apply **statistical subtraction** to obtain the measurement for “pure” signal
- Any differences probe influence of **heavy quark mass** and **parton flavor** of the jet

# Jet-axis differences

- **Standard:** anti- $k_T$  jet with  $E$ -scheme recombination
- **Groomed:** apply Soft Drop with different values of  $z_{\text{cut}}$  and  $\beta$
- **Winner-Take-All (WTA):** jet axis is given by its leading constituent

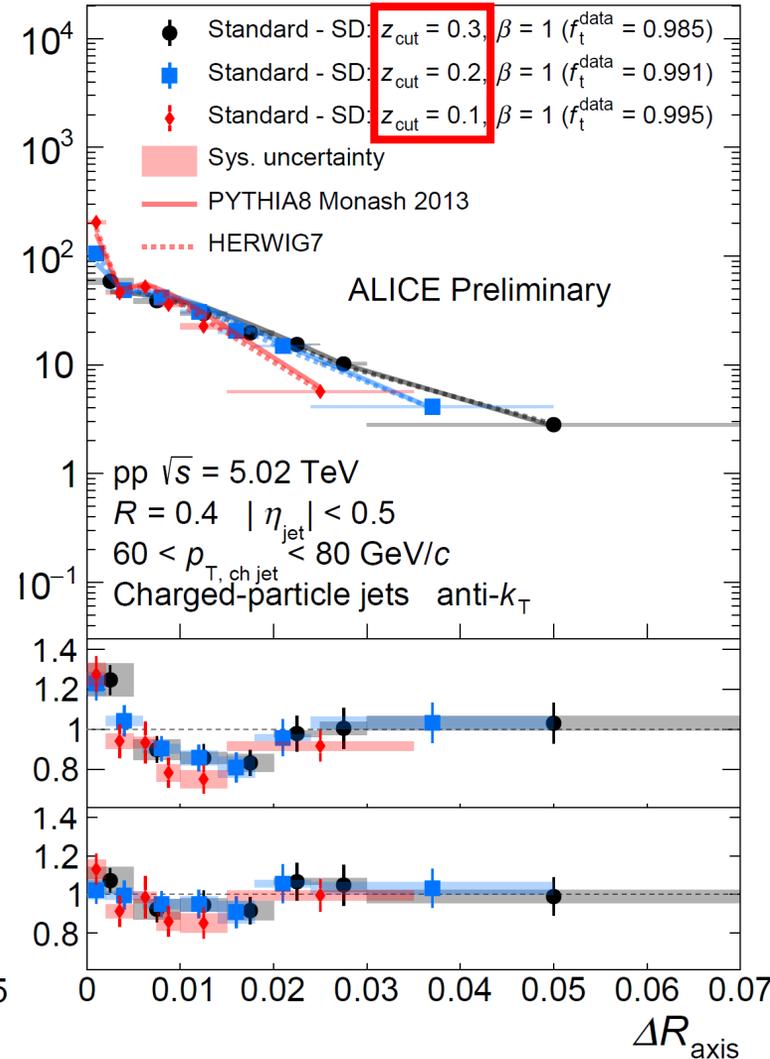
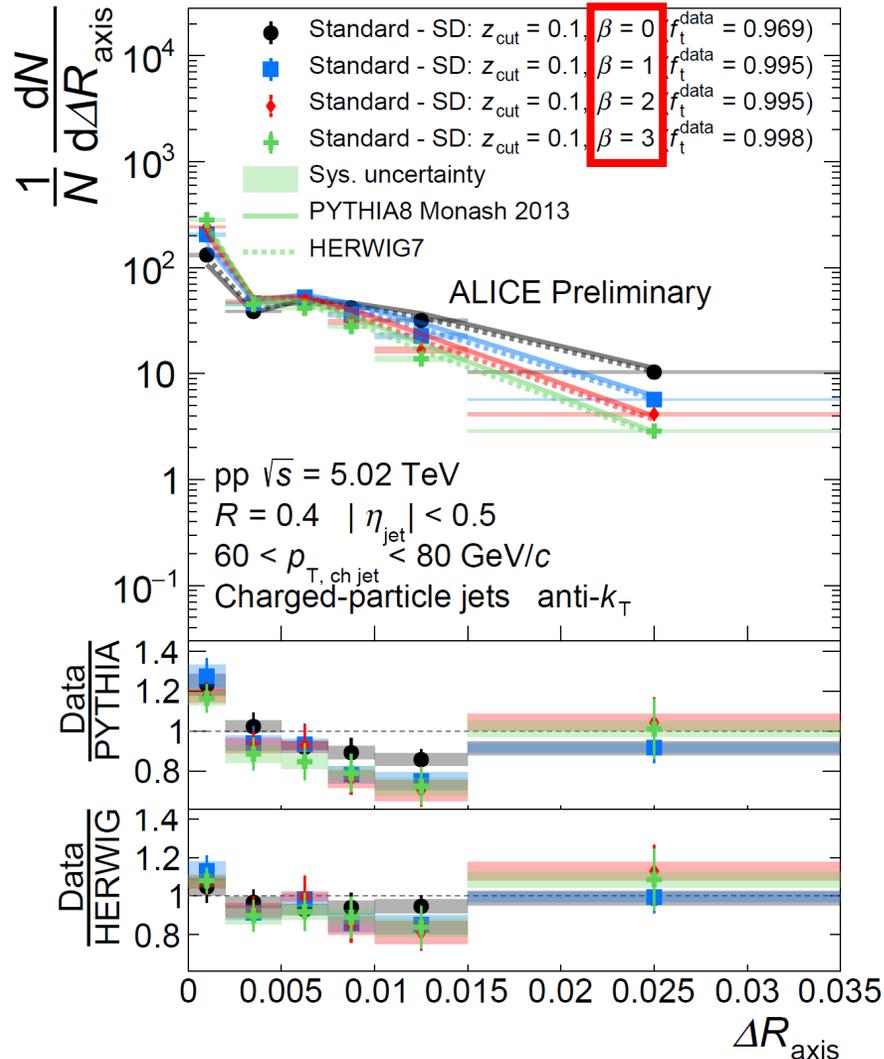


- Calculate the angular separation:  $\Delta R_{\text{axis}} = \sqrt{\Delta y^2 + \Delta \phi^2}$
- IRC-safe observable sensitive to **soft radiation, TMDs, and PDFs** [5]

[5] Cal, Neill, Ringer, Waalewijn [JHEP 04 \(2020\) 211](https://arxiv.org/abs/1908.07551)

# First measurement of the jet-axis differences

- Slight tension seen between data and MC for standard versus SD axis

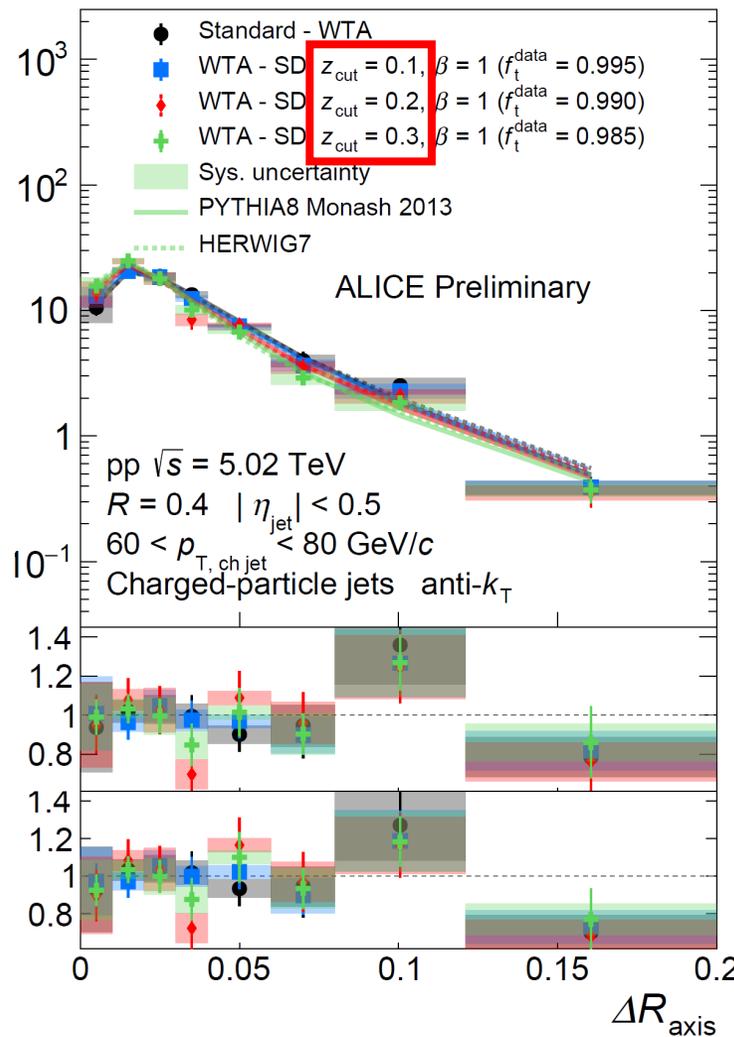
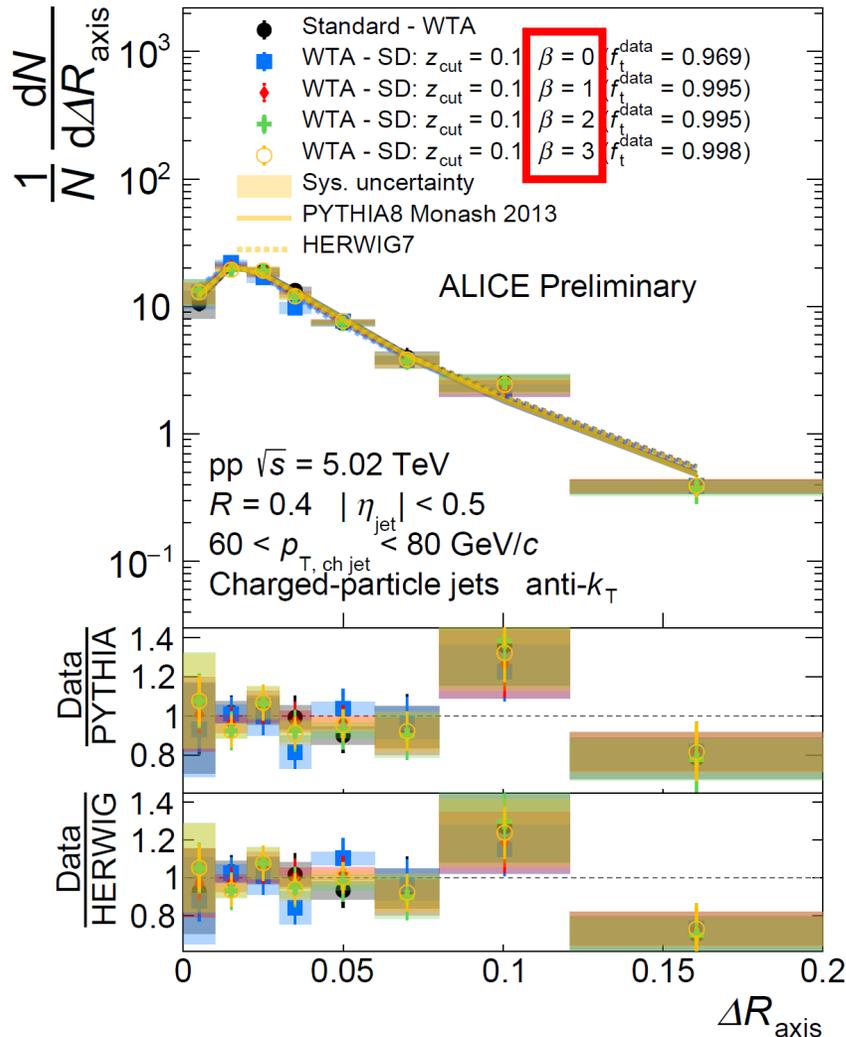


**Standard and SD axes are strongly correlated**

- Seems mostly independent of grooming parameters
- Will be useful for tuning MC generators
- pQCD comparisons are coming soon!

# First measurement of the jet-axis differences

- Good agreement seen with MC for a wide range of SD parameters



• **WTA and standard/SD axes are less strongly aligned/correlated**

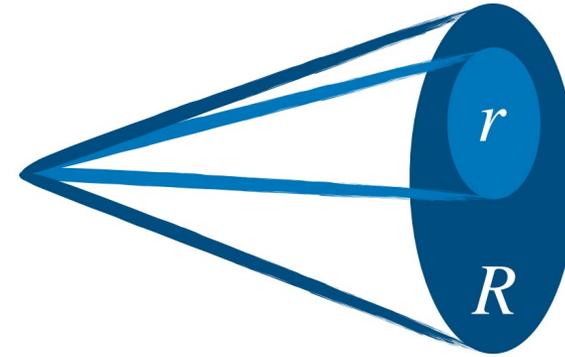
•  $p_T$  is distributed more broadly within the jet, rather than collimated along a single axis

• PYTHIA and Herwig reproduce this trend

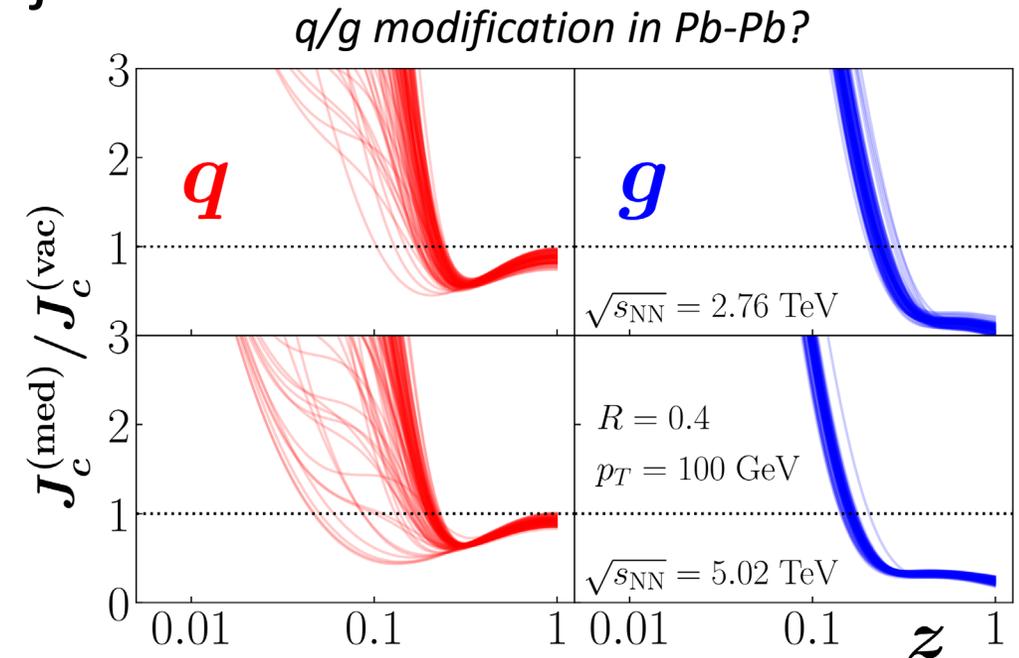
• Note: every curve uses the same sample of jets

# Measurement of subjets

- Reconstruct inclusive jets with radius  $R$ , then recluster using anti- $k_T$  with smaller radius  $r$
- Can either study **inclusive** or **leading** subjets
- Sensitive to jet quenching effects from the hot, dense QCD medium formed in heavy-ion collisions
- Test of **universality of jet functions**: compare extraction of  $J_{r,med}(z)$  to  $J_{med}(z)$  from  $R_{AA}$  [6]



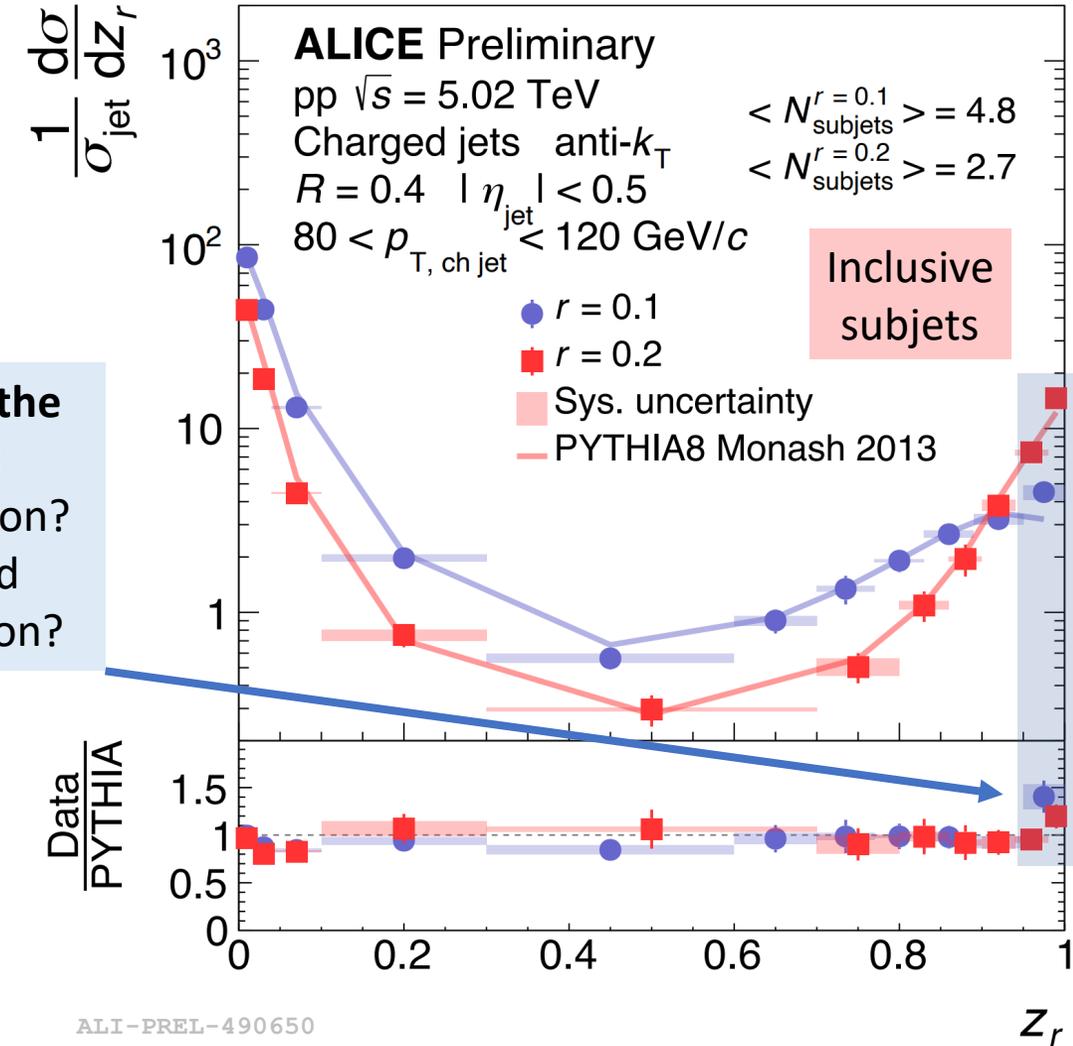
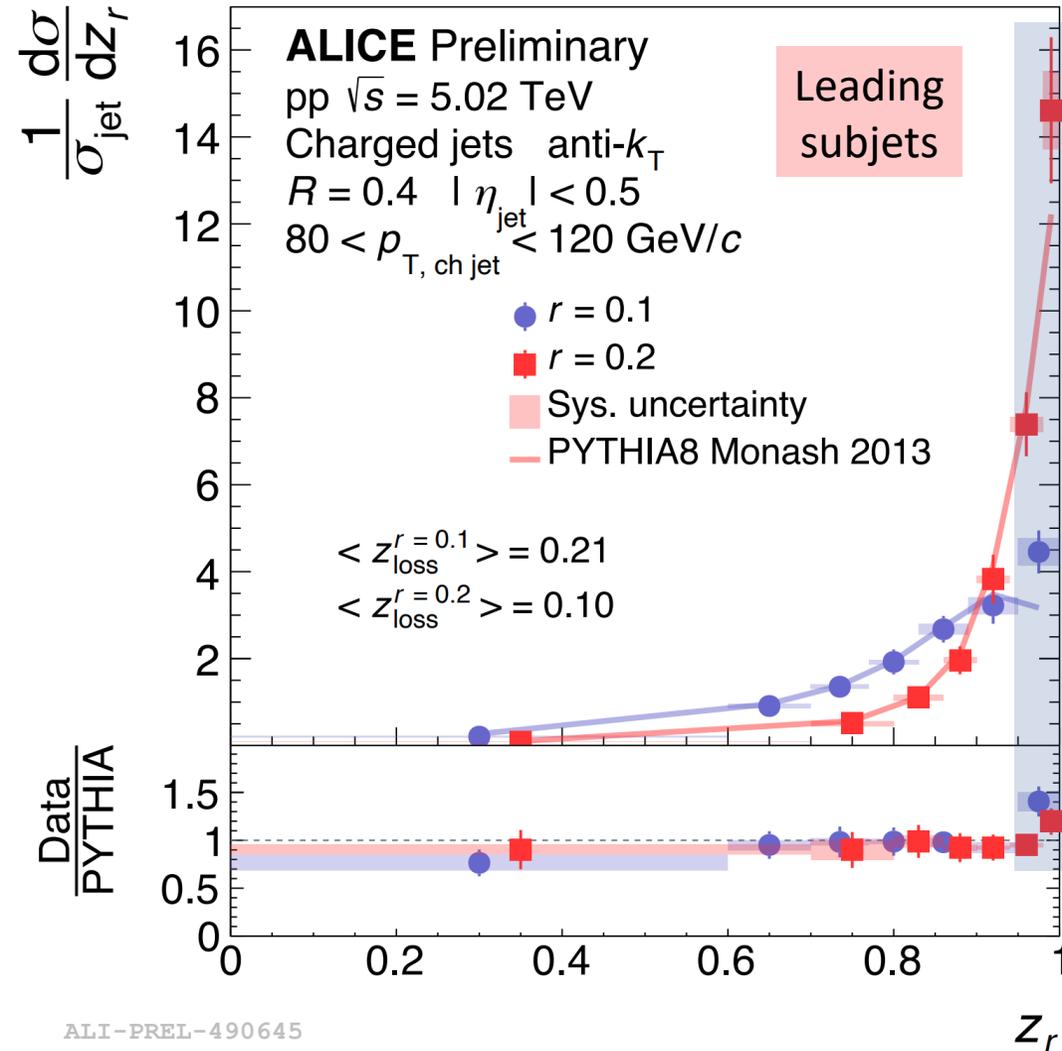
$$z_r = \frac{p_T^{\text{ch subjet}}}{p_T^{\text{ch jet}}}$$



[6] Qiu, Ringer, Sato, Zurita [PRL 122 \(2019\) 25](#)

# New subjet measurements in pp

- Reasonable agreement is observed with respect to MC generators



# Inclusive jet (primary) Lund Plane

- Triangular diagram populated by each primary splitting after Cambridge-Aachen reclustering

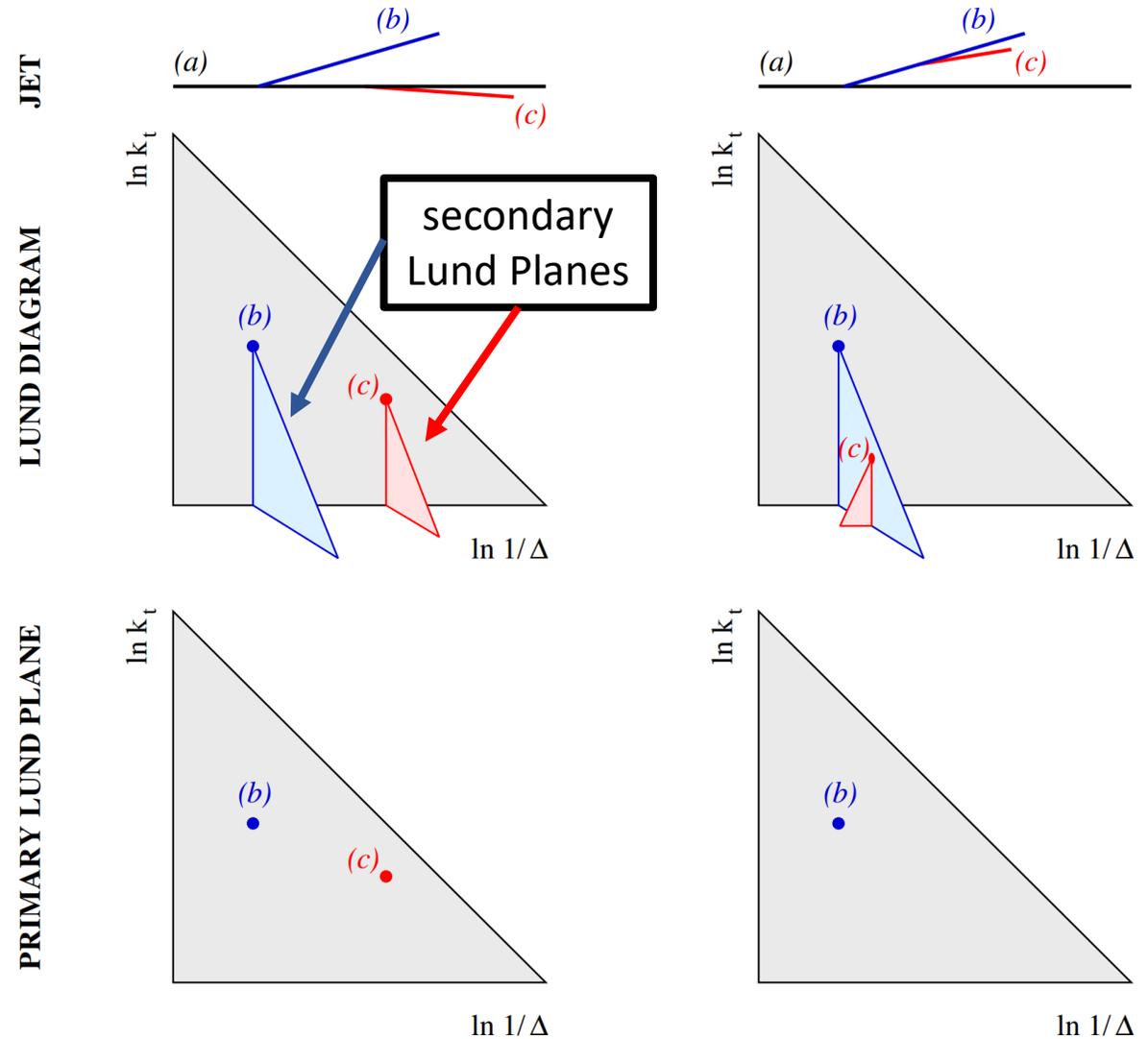
- Axes are related to angle and  $p_T$ :

$$\Delta \equiv \Delta_{ab} = \sqrt{(y_a - y_b)^2 + (\phi_a - \phi_b)^2}$$

$$k_t \equiv p_{T,b} \Delta_{ab}$$

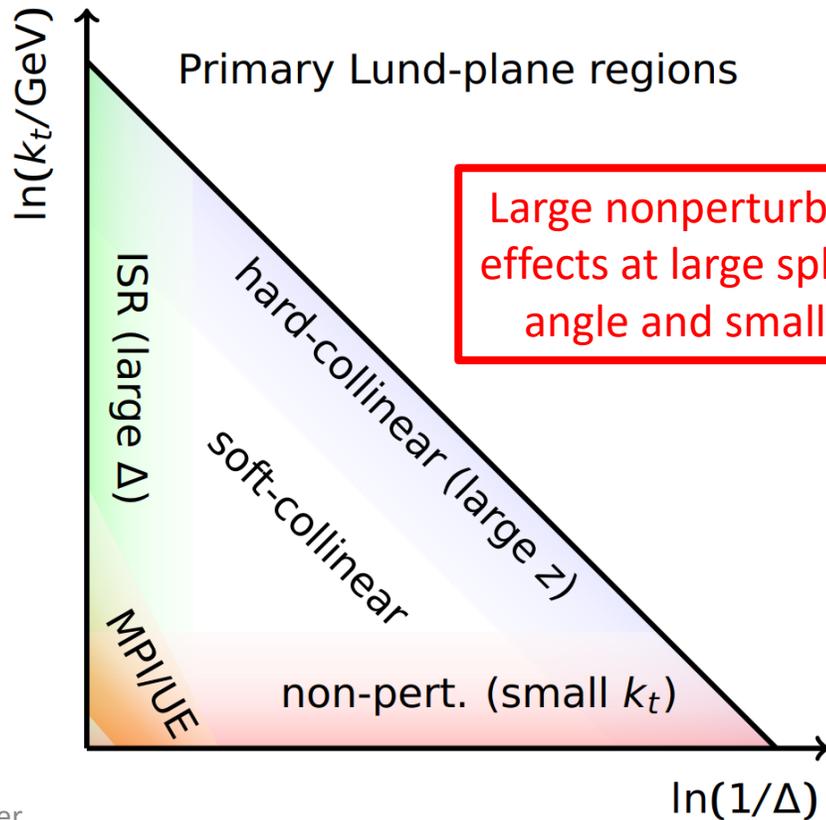
- Not generally IRC-safe; perturbatively amenable for

$$k_t \gg \Lambda_{\text{QCD}}$$

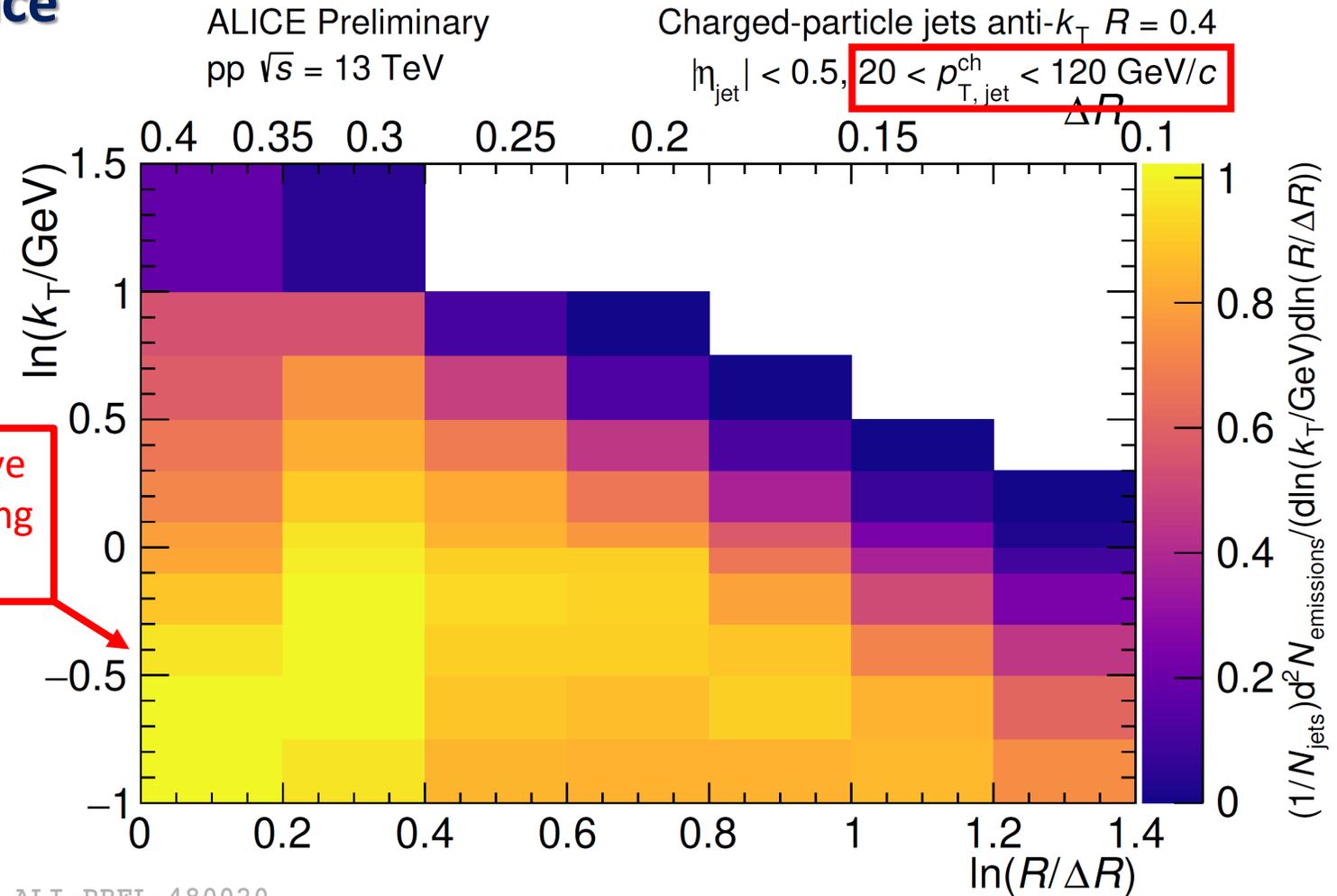


# Inclusive jet (primary) Lund Plane

- Illustrates **branching phase space**
- Has been also measured by ATLAS [7] at higher jet  $p_T$  ( $> 675$  GeV/c)



Large nonperturbative effects at large splitting angle and small  $k_T$

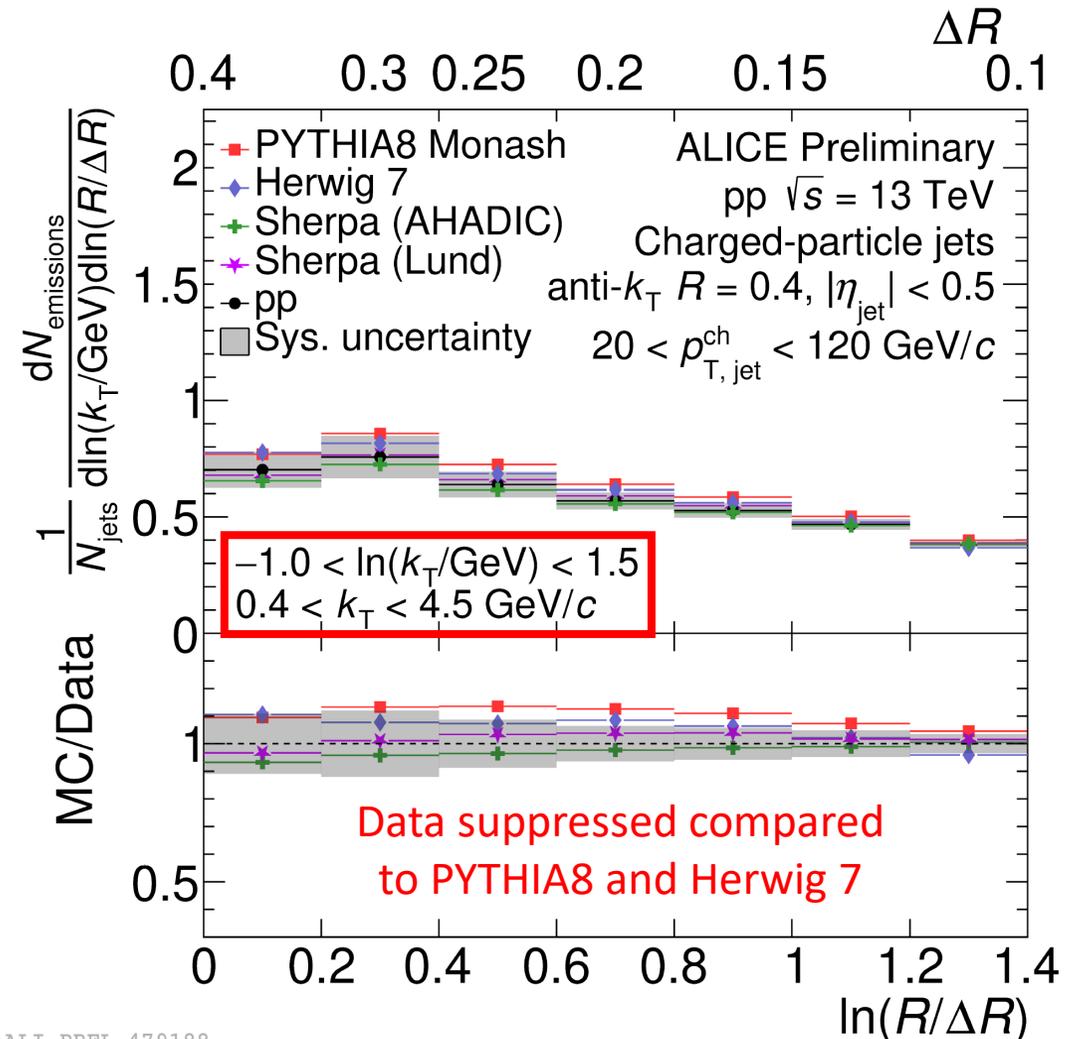
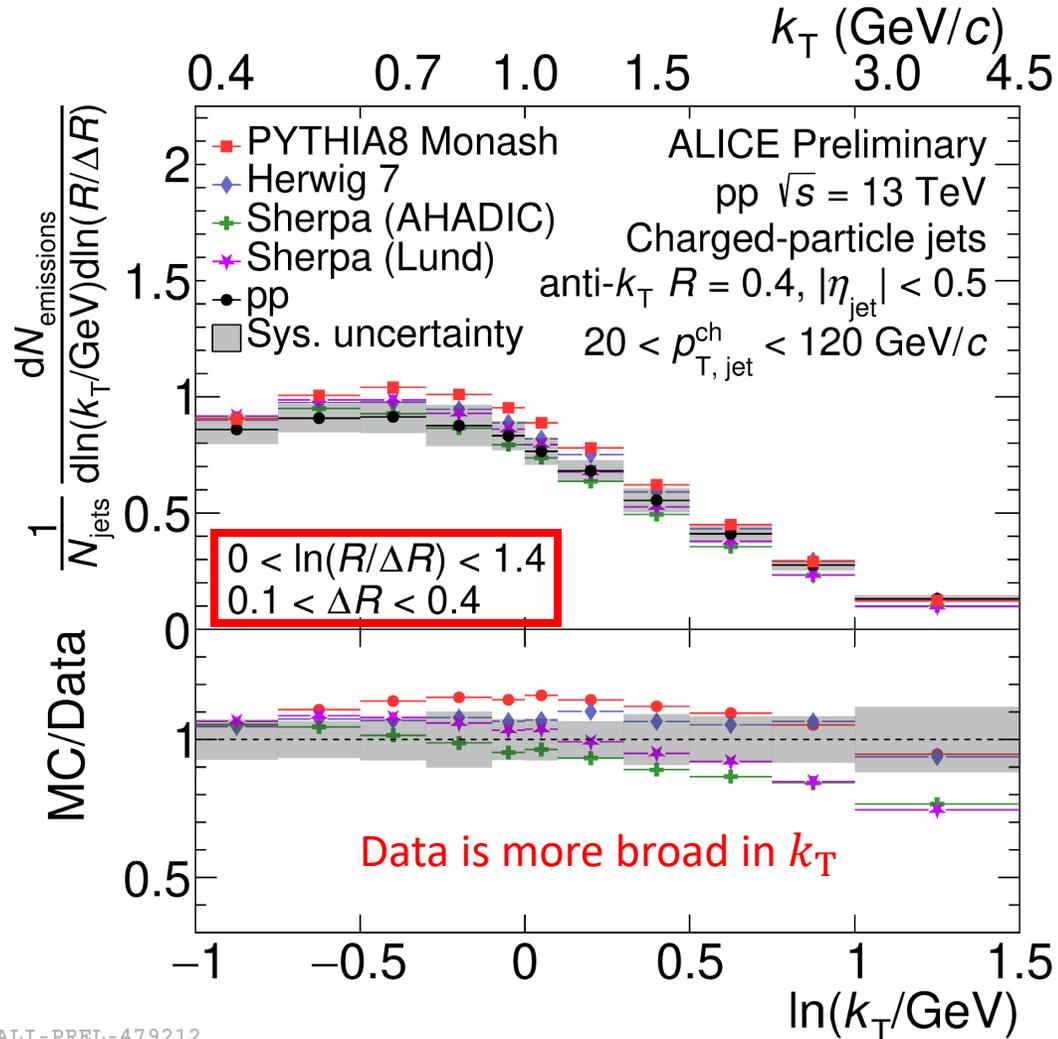


ALI-PREL-480020

[7] ATLAS Collab.: [Phys. Rev. Lett. 124 \(2020\) 222002](https://arxiv.org/abs/1908.07551)

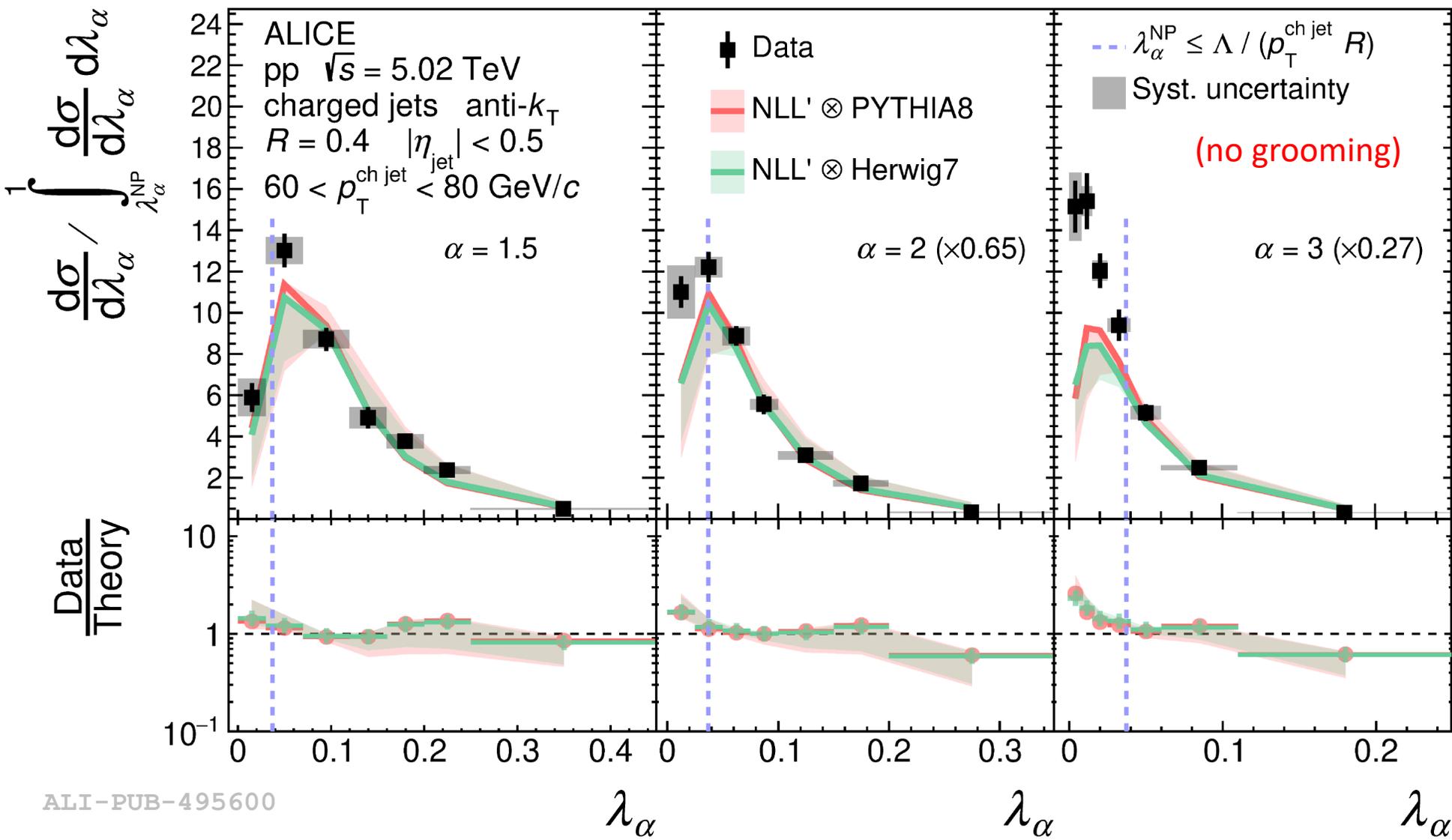
# Comparing Lund Plane projections to models

- Slight tension seen with some models in different regions of phase space



# pQCD predictions with SCET ( $R = 0.4$ )

$$\lambda_\alpha^\kappa \equiv \sum_{i \in \text{jet}} z_i^\kappa \theta_i^\alpha$$

For larger  $R$  we see increased tension at large values of  $\lambda_\alpha$

This could hint at the importance of higher-order terms (for example, power corrections in  $\lambda_\alpha$ )

# Choosing grooming settings

- **Soft Drop**: higher values of  $z_{\text{cut}} \geq 0.2$  increase the leading branch tagging purity in high-background environments [5]

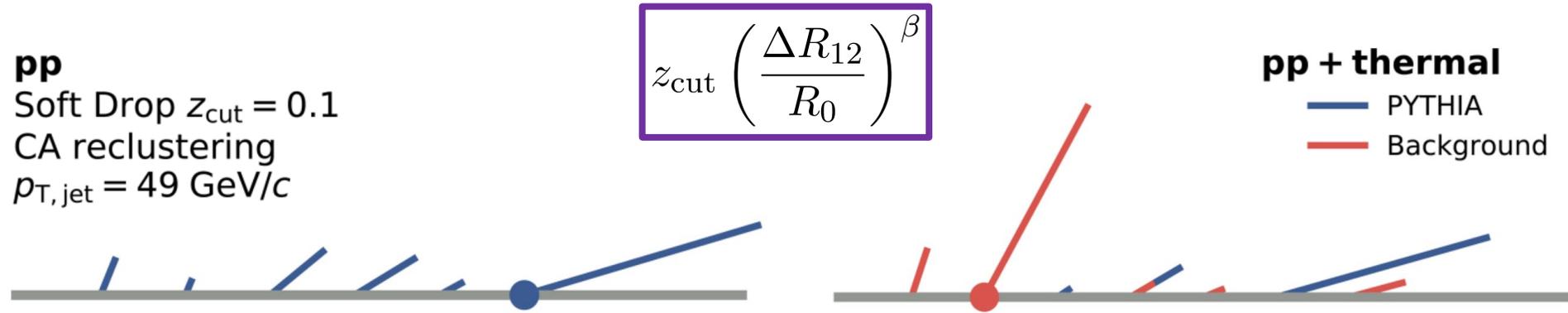


figure: J. Mulligan, LBNL

- **Dynamical**: same is true for lower  $a \rightarrow 0$

$a \rightarrow 0$

hardest  $z$

$z_{\text{cut}} \approx e^{-a\pi/\alpha_s C_F}$

$a = 1$

hardest  $k_T$

$\ln k_t \approx -\sqrt{a}$

$a = 2$

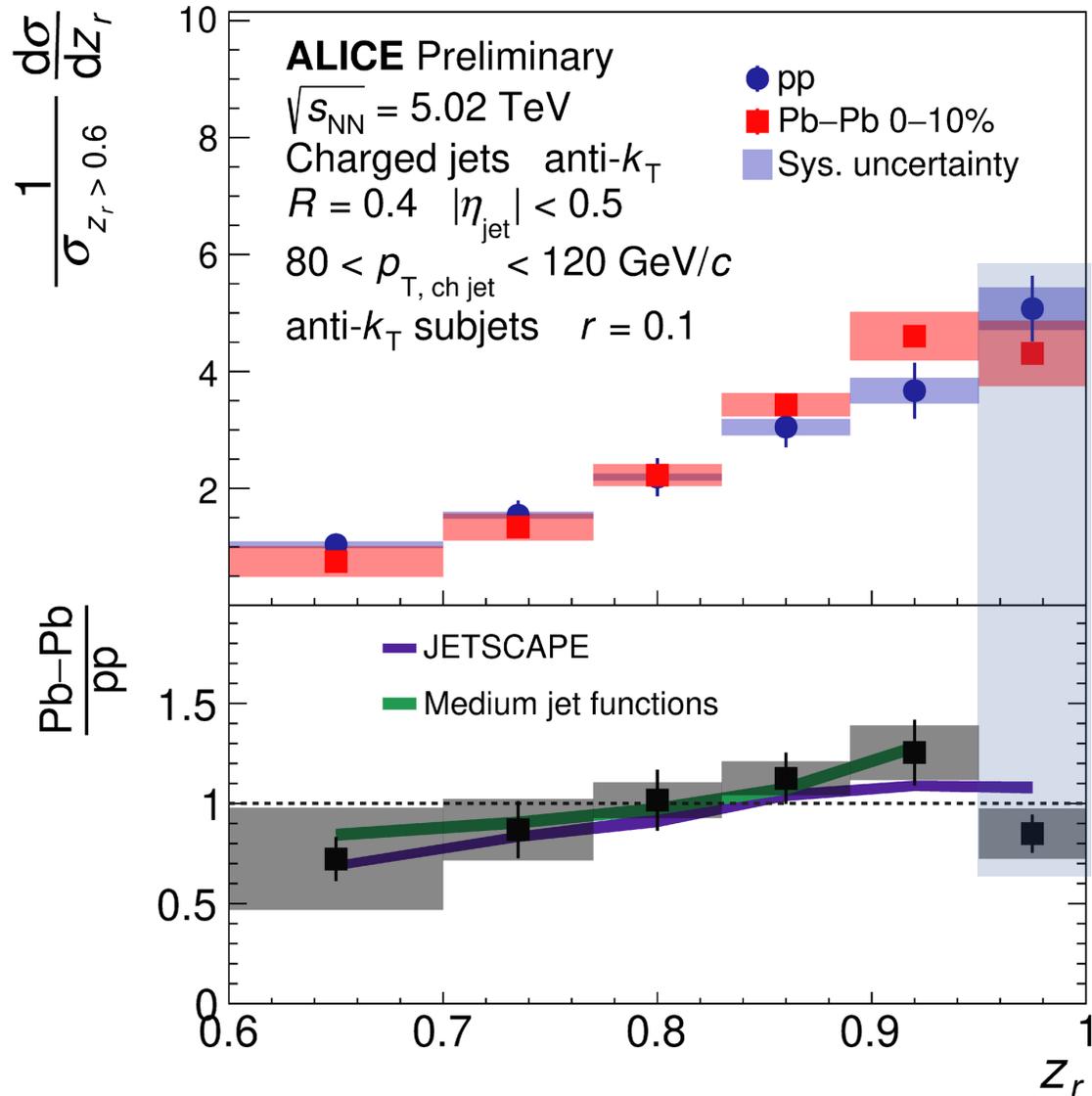
smallest  $t_f$

$\ln k_t(R_{\text{jet}}) \approx -\sqrt{a}$

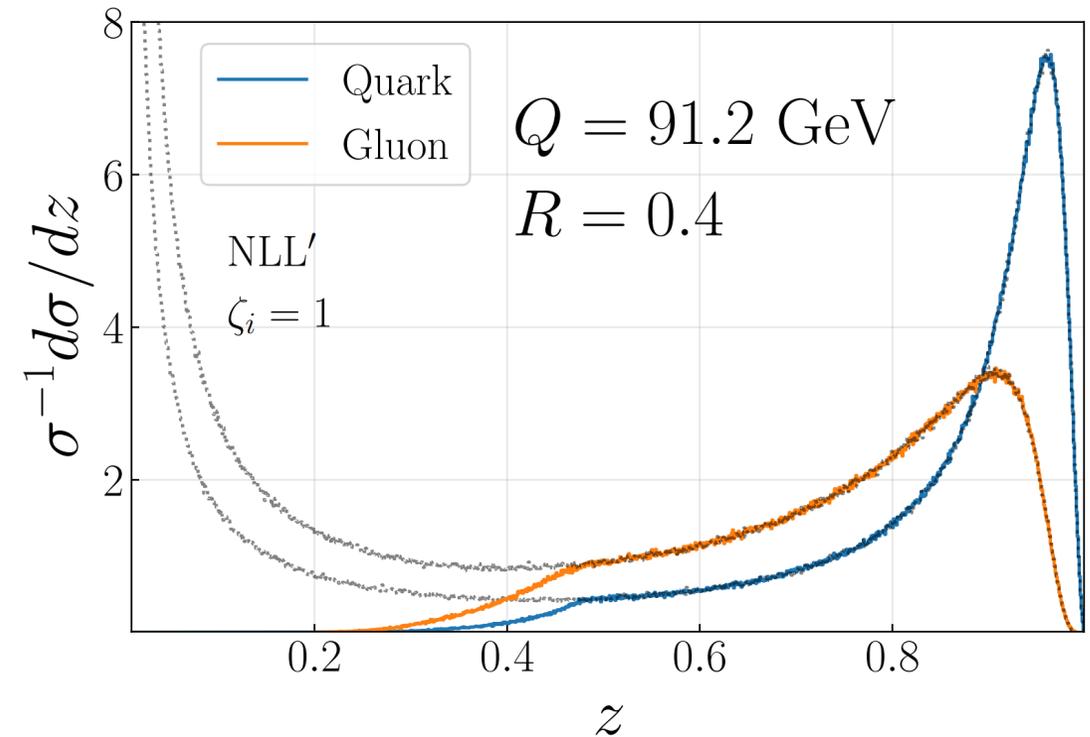
$z_i(1 - z_i) p_{T,i} \left( \frac{\theta_i}{R} \right)^a$

[5] Mulligan, Płoskoń [Phys. Rev. C 102, 044913 \(2020\)](https://arxiv.org/abs/2004.04491)

# Modification in Pb-Pb collisions?



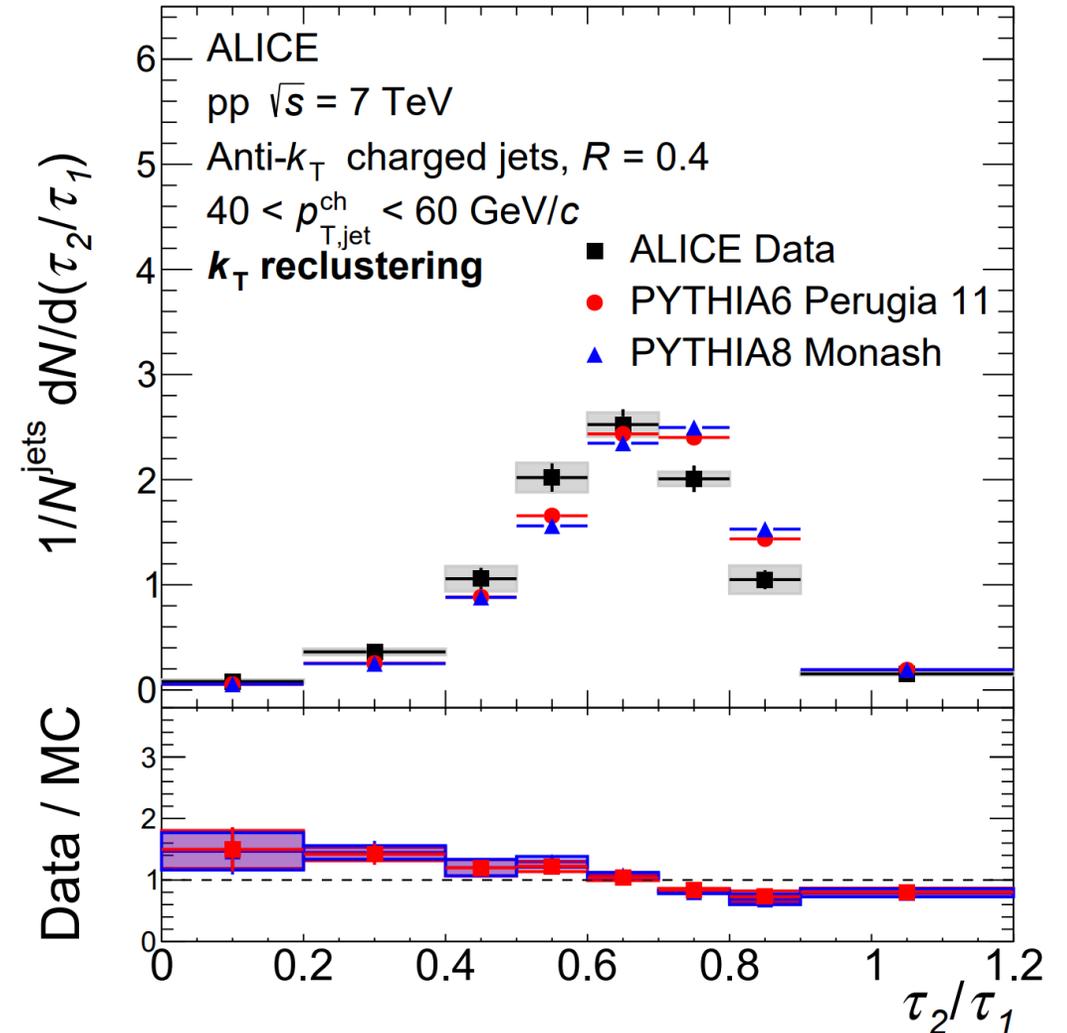
- Hardening at mid- $z_r$  could point to quark/gluon fraction modification
- Soft radiation enhanced at small  $z_r$   
 → competing normalization effect



# Measuring the $N$ -subjettiness in pp

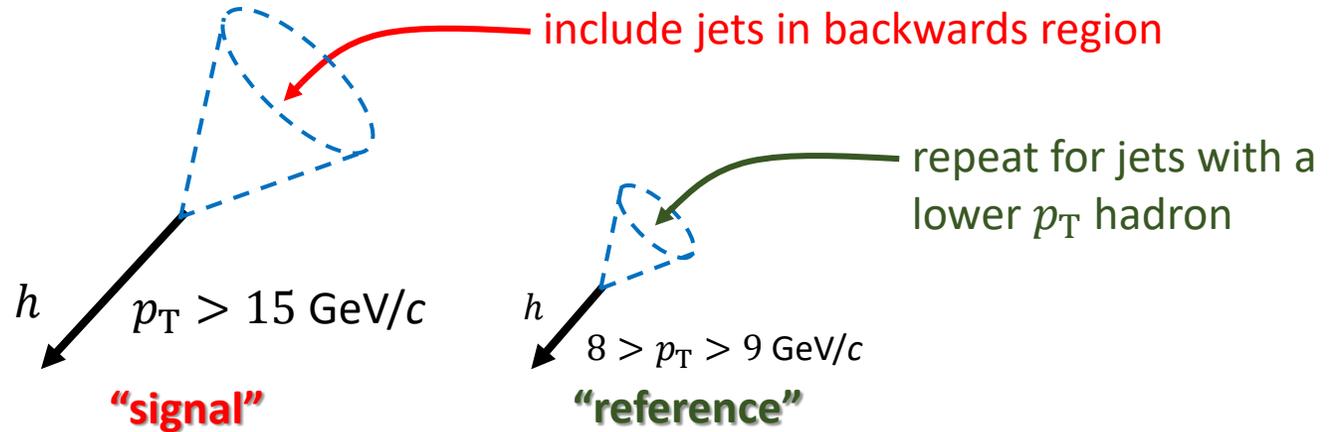
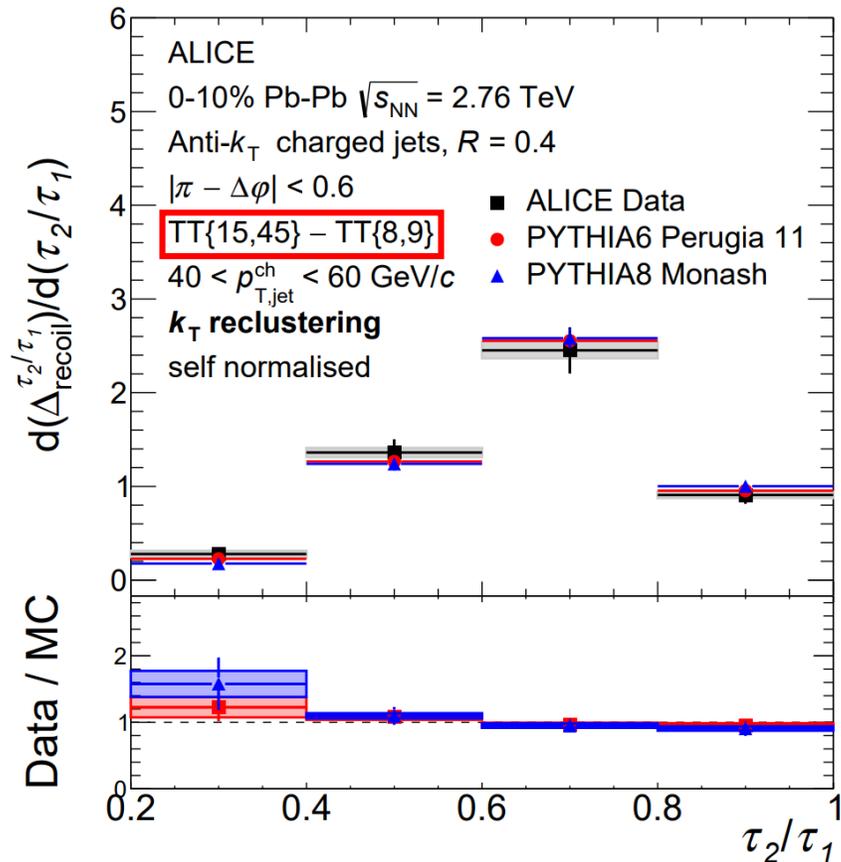
- Used for **tagging 1- or 2-pronged jets**
  - Originally designed to tag boosted decays such as  $W^\pm \rightarrow \bar{q}q$  or  $t \rightarrow W^+b$
- $\tau_N \rightarrow 0$  means correlation to  $N$  subjets;  
 $\tau_N \rightarrow 1$  means no strong correlation and suggests at least  $N + 1$  subjets
- Low values of  $\tau_N/\tau_{N-1}$  are used to **discriminate  $N$ -prongness**
- $\tau_2/\tau_1$  is peaked at intermediate values  $\rightarrow$  pp jets are found to be **mostly single-cored**, as two hard substructures are not well-separated and defined

$$\tau_N = \frac{1}{p_{T,\text{jet}} \times R} \sum_k p_{T,k} \text{minimum}(\Delta R_{1,k}, \Delta R_{2,k}, \dots, \Delta R_{N,k})$$



# Fully corrected $N$ -subjettiness in Pb-Pb

- Using the **semi-inclusive hadron-jet recoil technique** <sup>[9]</sup> for the first time in a substructure measurement ([CERN-EP-2021-082](https://cds.cern.ch/record/2781082))

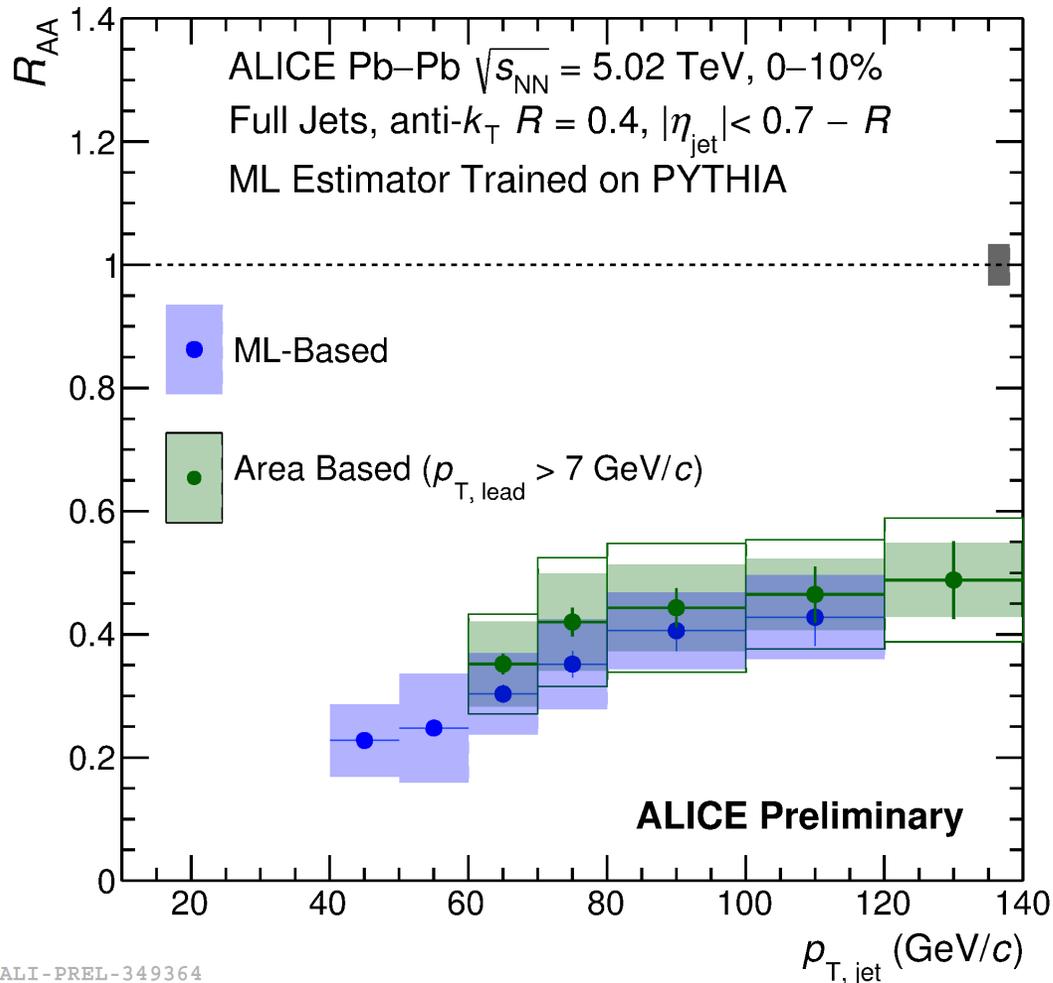


- Reduce contamination from combinatorial jets via requirement of a back-to-back high- $p_T$  hadron, then subtracting the observable shape from a reference Trigger Track (TT) bin

[9] ALICE Collab. [JHEP 09 \(2015\) 170](https://arxiv.org/abs/1503.07546)

# Using ML to reduce jet background [10]

- May allow studying jets with lower jet  $p_T$  and larger  $R$  than before



ALI-PREL-349364

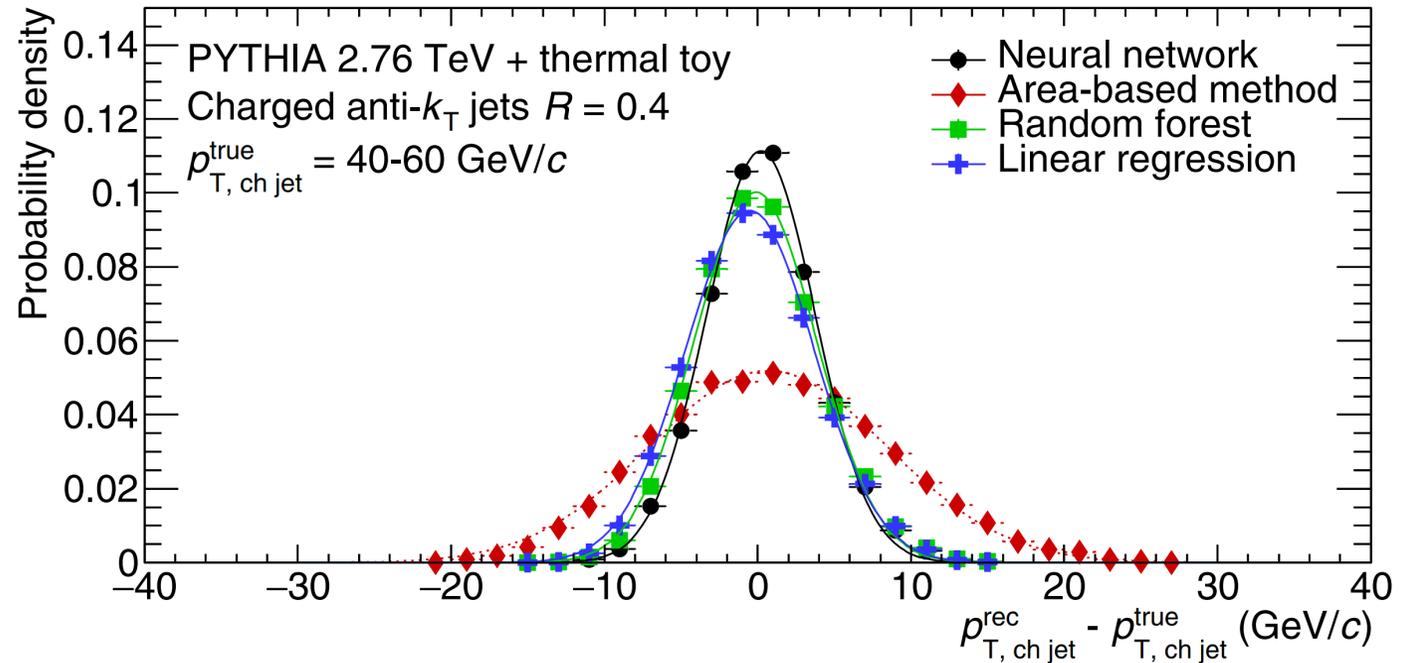


FIG. 2. Residual distributions for several background estimators in  $40 \leq p_{T, ch jet}^{true} < 60$  GeV/c.