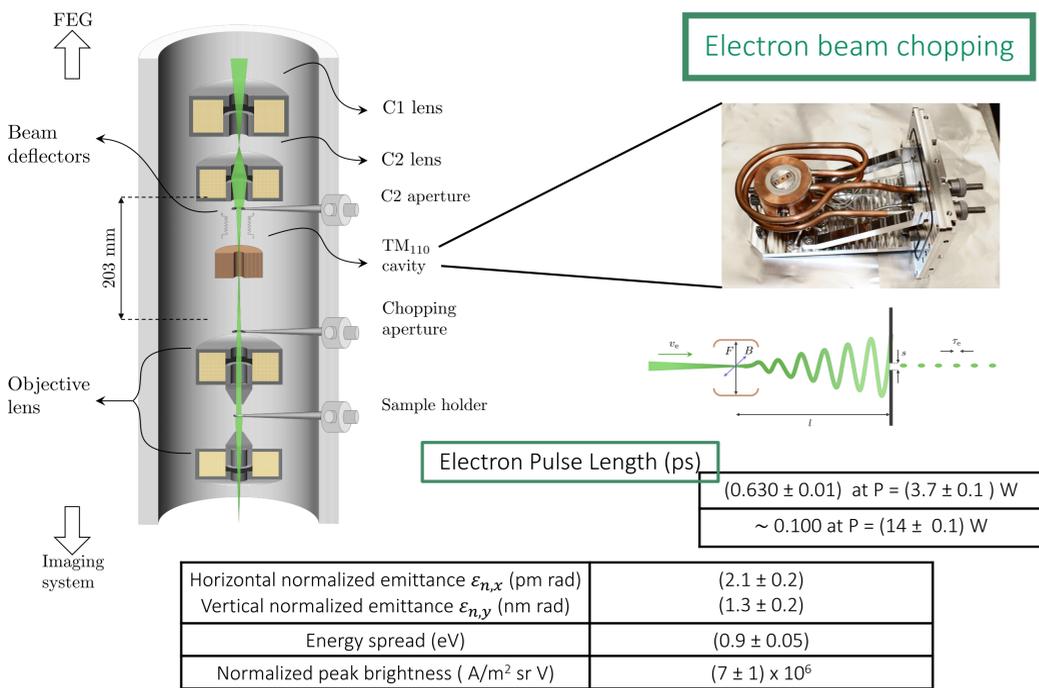


Phase shaping of the free-electrons wavefunction with fs-laser pulses in an RF-cavity-based UTEM

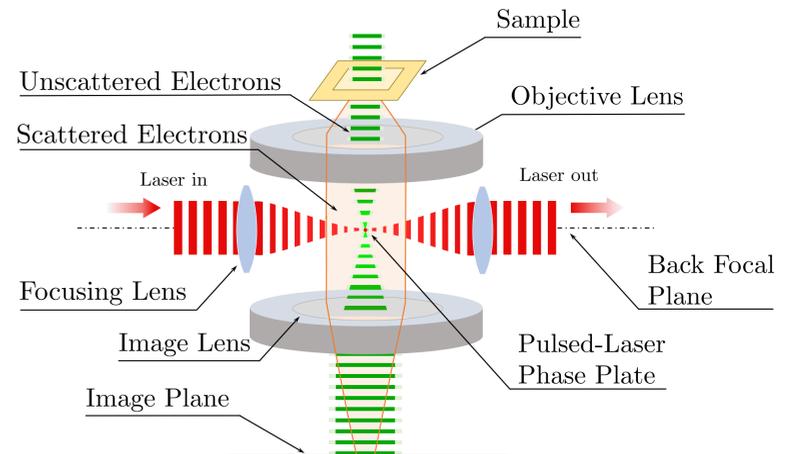
S. Borrelli, S.T. Kempers, W. Schaap, P.H.A. Mutsaers, E. Kieft, B. Buijsse, O.J. Luiten and K.A.H. van Leeuwen

RF-cavity-based ultrafast transmission electron microscope



Electron wavefunction's phase shaping with Light

Phase Plate based on ponderomotive interaction between a tightly focused pulsed laser and the pulsed zero-order electron (unscattered) beam transmitted by a sample.



$\frac{\pi}{2}$ - phase shift between scattered and scattered electrons

Theoretical Framework

Interaction between laser and electron pulses modeled using the relativistic ponderomotive potential

$$U_p = \frac{e^2}{c \epsilon_0 \gamma m \omega_0^2} \frac{W}{\pi^{3/2} w(z)^2 \tau} e^{-\frac{(t-z/c)^2}{\tau^2}} e^{-2\frac{x^2+y^2}{w(z)^2}}$$

Phase Shift on an electron crossing the laser spot $w(z)$ at $\vec{r} = (z, y)$ at time t_0

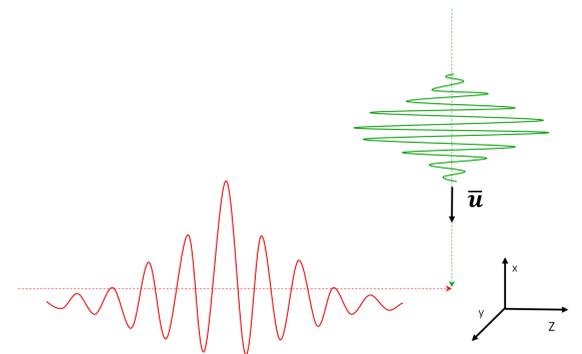
$$\Delta\phi = -\frac{1}{\hbar} \int_{-\infty}^{+\infty} dt U_p(u(t-t_0), y, z, t)$$

Maximum Phase Shift for perfect space-time synchronization between laser and electron pulses ($t_0 = y = z = 0$)

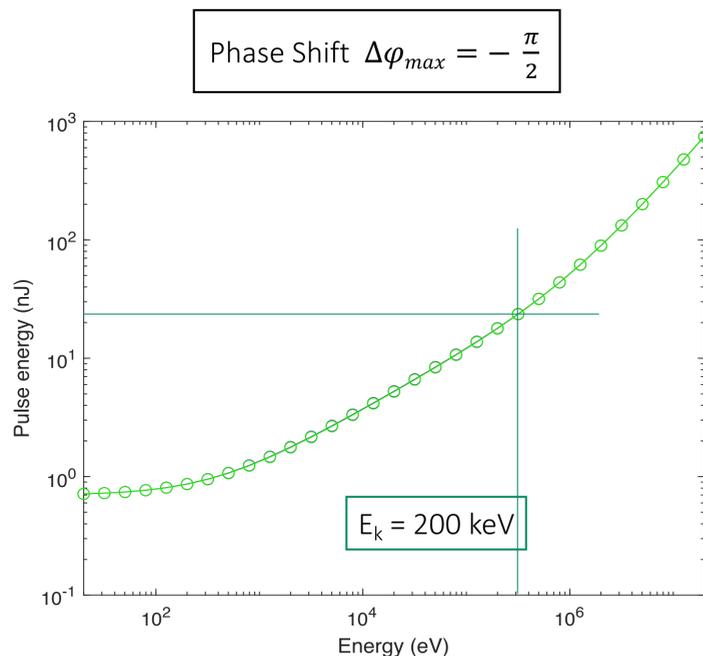
Long pulse limit

$$\Delta\phi_{max} \sim -\frac{e^2}{\hbar c \epsilon_0 \gamma m \omega_0^2} \frac{W}{\pi w_0^2} \frac{\tau_t}{\tau}$$

Phase shift depends on the synchronization between laser and electron pulses, on the laser parameters (pulse energy W , duration τ , waist w_0) and electron pulse length



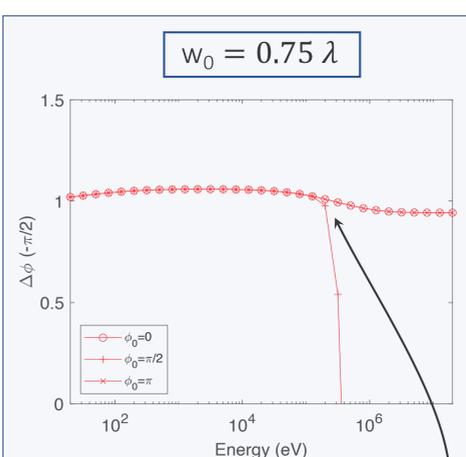
Experimental Parameters



Laser waist $w_0 = 2\lambda = 1.6 \mu\text{m}$
Laser pulse duration $\tau = 100 \text{ fs}$

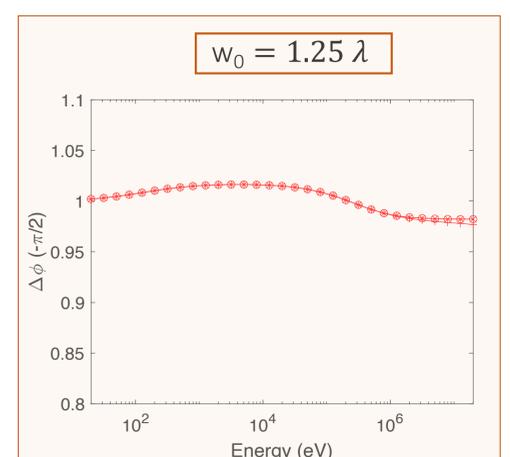
Realistic Field Model

$$\Delta\phi = \frac{1}{\hbar} \int_P dt L(x, y, z, t) = \int_P dt \left(-\frac{mc^2}{\gamma} - e \frac{\mathbf{p} \cdot \mathbf{A}}{m\gamma} - \frac{e^2 \mathbf{A} \cdot \mathbf{A}}{m\gamma} + eV \right)$$



Phase shift at high electron energies depends on:

- field phase
- field polarization
- field model chosen



Agreement between ponderomotive approximation and real field model