









# Mitigation of the onset of hosing in the linear regime through plasma frequency detuning

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## An instability with many faces

#### **Growth rate - it's a spectrum**

• "a long-wavelength hosing instability in laser-plasma interactions" has been studied some time ago\*\*\*\*



FIG. 2. The growth rate for hosing vs wave number for  $\tilde{x}_R = 256.$ 

- disruptive instability that modulates the bunch centroid at the plasma wavelength
- competes with the self-modulation instability (for long drivers)

### **The bogeyman of wakefield acceleration**

### **Suppressing hosing in particle drivers**

- a lot of research towards mitigation has focused on the short-bunch, nonlinear regime\*
- fewer options for mitigation in the long-beam, linear-wakefield regime\*\* exist (relevant for single-stage TeV-level PWFA schemes)

 $\Rightarrow$  what does this seed frequency dependence look like for beam hosing?



1



<sup>\*</sup> [T. J. Mehrling, et al., Phys. Rev. Accel. Beams 22, 031302 \(2019\)](https://doi.org/10.1103/PhysRevAccelBeams.22.031302) [R. Lehe, et al., Phys. Rev. Lett 119, 244801 \(2017\)](https://doi.org/10.1103/PhysRevLett.119.244801) \*\* [J. Vieira, et al., Phys. Rev. Lett. 112, 205001 \(2014\)](https://doi.org/10.1103/PhysRevLett.112.205001)

### **The hosing growth rate as a function of seed frequency**

### **A novel approach to hosing mitigation**

### **Conclusion**





### Methods and parameters

### **Theory**

$$
\frac{d^2y_c}{dz^2} = \frac{m_e}{\gamma M_b} \left\langle F_y \right\rangle =
$$

First-order evolution of certains for  $y_c(\zeta, z) = y_{c0}(\zeta) + \text{RHS}(y_{c0})$ 

Bunch centroid equation:

### plasma response

For a Gaussian transverse bunch profile (2D Cart.):

- electron bunch
- bunch profile: longit. cosine and transv. Gaussian
- cold beam  $(\varepsilon_N = 0)$
- head of beam, window length  $L = 140 k_p^{-1} (\sim 22 \lambda_p)$

$$
\left\langle F_y \right\rangle = \sqrt{\frac{\pi}{8}} \frac{n_{b0}}{n_0} \left( \frac{q_b}{e} \right)^2 \sigma_y \exp(\sigma_y^2) \int_{\zeta}^{\infty} d\zeta' \sin(\zeta - \zeta') f(\zeta')
$$
  

$$
\left\{ \exp \left[ y_c(\zeta') - y_c(\zeta) \right] \text{erfc} \left[ \frac{y_c(\zeta') - y_c(\zeta) + 2 \sigma_y^2}{2 \sigma_y} \right] - \exp \left[ y_c(\zeta) - y_c(\zeta') \right] \text{erfc} \left[ \frac{y_c(\zeta) - y_c(\zeta') + 2 \sigma_y^2}{2 \sigma_y} \right] \right\}
$$



### $RHS(y_c)$

troid (valid for 
$$
z \leq k_{\beta}^{-1}
$$
):

\n $\int \frac{1}{2} z^2$ 

#### **Parameters**

$$
n_0 = 0.5 \cdot 10^{14} \text{ cm}^{-3}
$$
  
\n
$$
\gamma_b = 480
$$
  
\n
$$
\sigma_r = 200 \text{ }\mu\text{m} \qquad \approx 0.27 \text{ } k_p^{-1}
$$
  
\n
$$
\sigma_z = 12 \text{ cm} \qquad \approx 160 \text{ } k_p^{-1}
$$
  
\n
$$
M_b = m_e \qquad \Rightarrow k_\beta^{-1} / k_p^{-1} \approx 980
$$
  
\n
$$
n_{b0} / n_0 = 0.001 \Rightarrow N_b = (1.9-3.8) \cdot 10^9
$$

- 1) initial centroid perturbation:  $y_{c0}(\zeta) = 0.05 \sin(k \zeta)$
- 2) obtain evolution of  $y_c(\zeta, z)$
- 3) measure the **amplitude** response:

 $\Pi(z) =$  $\int d\zeta \left[ y_c(\zeta, z) \right]$  $\int d\zeta \, |y_c(\zeta,0)|$ 

#### **How?**

with

- theoretical model
- simulations

$$
k_{\beta}^{2} = \frac{1}{2 \gamma_{b}} \left( \frac{\omega_{b}}{c} \right)^{2} = \frac{1}{2 \gamma_{b}} \frac{q_{b}^{2} n_{b0}}{\varepsilon_{0} M_{b}} \frac{1}{c^{2}}
$$





## How does the HI growth rate depend on the seed frequency?









## Each growth regime is associated with a phase shift

- the phase shift can be measured with a crosscorrelation method\*
- phase shift "spectrum" confirms three growth regimes



\* For the theoretical curve, *L* and  $\sigma_z$  are scaled for each k such that the same number of wavelengths is considered in the analysis (  $\sim 22 \lambda_p$ ).









### Behaviour is analogous with a harmonic oscillator





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- hosing: growing centroid and centroid velocity  $v_c/c = dy_c/dz$
- initially,  $y_c$  and  $v_c$  are phase-shifted by  $\pi/2$ 
	- $y_c(\zeta, z) = A \sin[k\zeta \varphi(z)]$ 2.5 • assume the centroid evolves as
	- $v_c(\zeta, z)/c = A \varphi'(z) \sin(k\zeta \varphi(z) \frac{\pi}{2})$ bulc • the centroid velocity would be
- $\frac{1}{2}$ • different phase shifts to plasma response  $\left\langle F_{y}\right\rangle$ **⇒** detuning impacts both quantities differently
- $n = \frac{1}{2}$ • solution: alternate between  $k < k_p$  and  $k > k_p$



0 0.5 1 1.5 2

z = 0:5 k!<sup>1</sup> z = 1:0 k!<sup>1</sup> z = 2:0 k!<sup>1</sup>



## Can this knowledge be used to mitigate hosing?

### **Simply staying in damping regime does not work**



control local plasma density *np*

control ratio of seed  $k$  (initial perturbation) to local  $k_p$ 

*Amplitude response as a function of local plasma density*





- the total transverse energy is almost two orders of magnitude smaller than the case without steps
- instability picks up in the resonant plasma density
- a second set of steps prolongs the suppressive effect

### Hosing can be mitigated with plasma density steps

• for small centroids  $(y_c \ll 1)$ :

#### **Measuring the mitigation effectiveness A proof-of-concept density step configuration**

$$
\left(\frac{d^2}{dz^2} + k_{\text{HO}}^2(\zeta, z)\right) y_c(\zeta, z) = F(\zeta, z, y_c)
$$

• multiply by  $v_c$ :

$$
\frac{d}{dz} \left( \frac{1}{2} v_c^2 + \frac{1}{2} k_{\text{HO}}^2 y_c^2 \right) = v_c F
$$

#### transverse energy

• initial centroid displacement at  $k_{p,0}$ :  $y_{c0}(\zeta) = 0.05 \sin(k_{p,0}\zeta)$ 





### 3D OSIRIS simulations



## Hosing can be mitigated with plasma density steps















### Does the mitigation set-up destroy a self-modulated bunch?

### **Methodology There is significant impact on the accelerating field amplitude**

• preliminary study indicates a **large drop** in the amplitude of  $E<sub>z</sub>$  (~ -40%)

#### **Virtually no effect on bunch charge**





• the SMI can be **optimised** with a small, early density step\*

• similar impact on this configuration ("opt.")



\* [K. V. Lotov, Phys. Plasmas 18, 024501 \(2011\);](https://doi.org/10.1063/1.3558697) [K. V. Lotov, Phys. Plasmas 22, 103110 \(2015\)](https://doi.org/10.1063/1.4933129)





## The self-modulation instability obeys similar physics



㱺 **Poster session tonight!**



### **#49 - "Early dynamics of the self-modulation instability growth rate"**



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2.5

-2

0

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## **Conclusions**

#### $\boldsymbol{\varsigma}$ **The hosing growth rate depends on the perturbation wavelength**

- the amplitude response evolves along the propagation
- the amplitude "spectrum" can be probed via plasma density detuning (such as a density step)





### **A hosing seed can be suppressed through a series of plasma density steps**

- however, set-up may significantly impact the wakefield amplitude driven by a self-modulated bunch
- implications for the control of the growth of transverse beam-plasma instabilities in general
- a small amount of detuning (either  $\Delta k$  or  $\Delta n_{p}^{}$ ) can lead to very different growth regimes
- these growth regimes are associated with a characteristic phase shift between the radius and the plasma response

#### **There is a particular amplitude response early in the development of hosing**



#### 㱺 **For more information:** <https://doi.org/10.48550/arXiv.2207.14763>







