

# TMD studies at JLab: present and future

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Sar WorS 2021 Sardinian Workshop on Spin

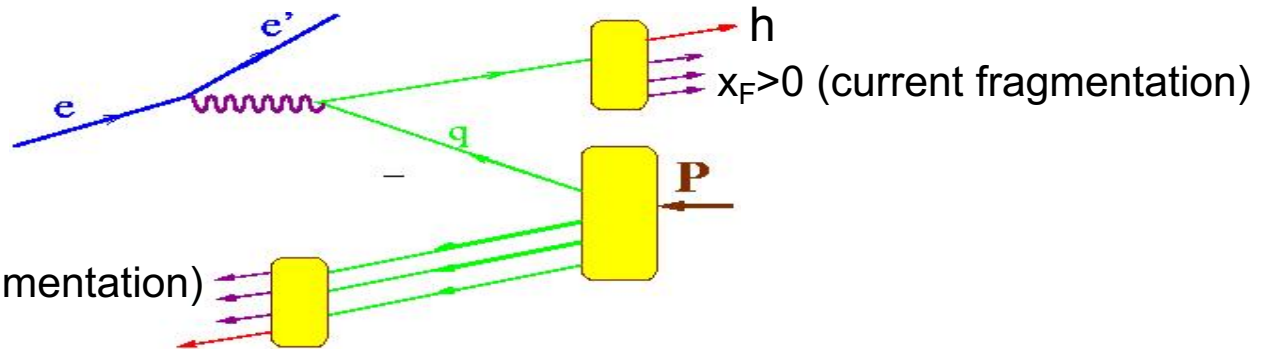
Sep 6-8, 2021

- Introduction
- SIDIS program at JLab
- Present some CLAS12 data
- Studies of transverse momentum of hadrons
  - multiplicities
  - azimuthal modulations
- Interpretations & challenges
- Future measurements
- Summary

**\* In collaboration with Harut Avakian (JLab)**

# Electroproduction: extending 1D PDFs

$x_F$  – fractional momentum in the CM frame

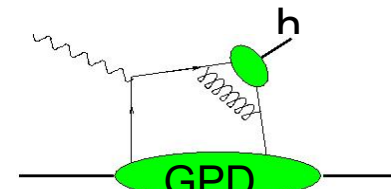
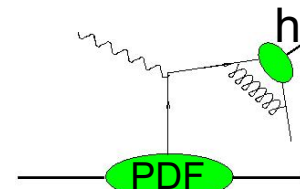
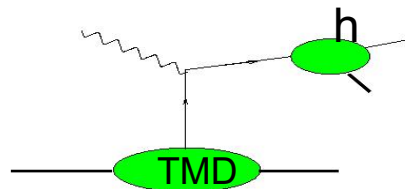
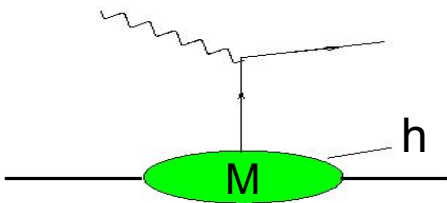


$x_F < 0$  (target fragmentation)

$x_F > 0$  (current fragmentation)

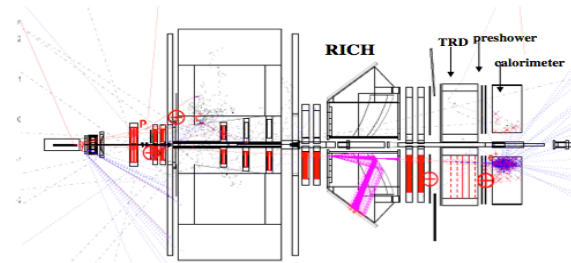
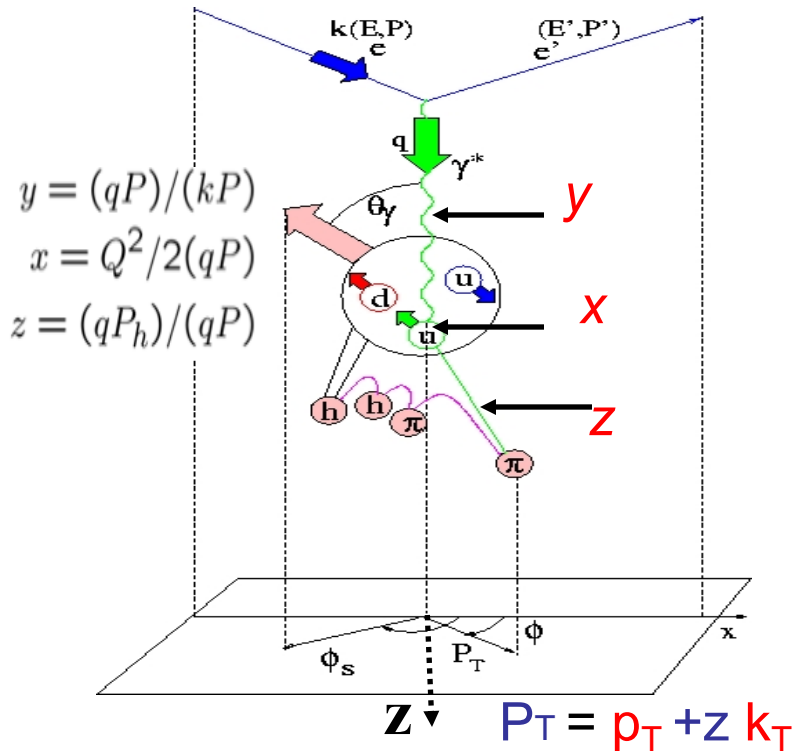
Target fragmentation

Current fragmentation

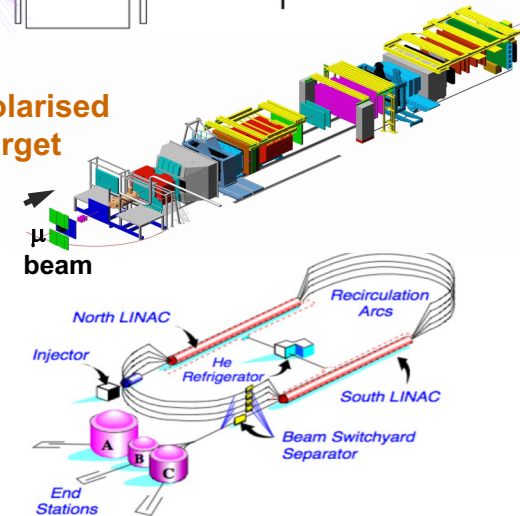


Wide kinematic coverage of large acceptance detectors allows studies of semi-inclusive and exclusive processes simultaneously

# Semi Inclusive DIS



Polarised Target



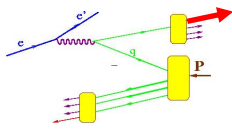
Azimuthal modulations depend on structure functions, providing information on underlying correlations of spins with partonic momentum distributions

$$\sigma = F_{UU} + P_t F_{UL}^{\sin \phi} \sin 2\phi + P_b F_{LU}^{\sin \phi} \sin \phi \dots$$

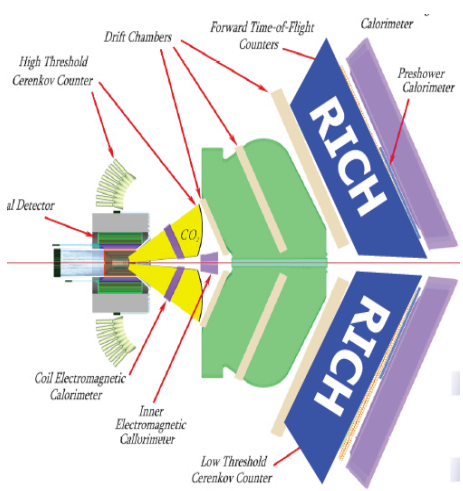
$$F_{XY}^h(x, z, P_T, Q^2) \propto \sum H^q \times f^q(x, k_T, \dots) \otimes D^{q \rightarrow h}(z, p_T, \dots) + \dots$$

beam polarization  
 target polarization

Distribution & Fragmentation Functions



# SIDIS at JLab12



CLAS12

E12-06-112:  $\pi^+, \pi^-, \pi^0$   
E12-09-008:  $K^+, K^-, K^0$

E12-07-107:  $\pi^+, \pi^-, \pi^0$   
E12-09-009:  $K^+, K^-, K^0$

C12-11-111:  $\pi^+, \pi^-, \pi^0$   
 $K^+, K^-$

$H_2, NH_3, HD$

CLAS12

E09-008:  $\pi^+, \pi^-, \pi^0$   
 $K^+, K^-, K^0$

E07-107:  $\pi^+, \pi^-, \pi^0$   
E09-009:  $K^+, K^-, K^0$

$D_2, ND_3$

**Proton** Quark spin polarization

	$N^q$	U	L	T
Nucleon polarization	U	$f_1$		$h_1^\perp$
	L		$g_1$	$h_{1LL}^\perp$
	T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

Hall C Hall A

E12-09-017:  $\pi^+, \pi^-, K^+, K^-$   
C12-11-102:  $\pi^0$

HMS SHMS

C12-11-108:  $\pi^+, \pi^-$

Solid

$H_2, NH_3$

Hall C

E12-09-017:  $\pi^+, \pi^-, K^+, K^-$   
C12-11-102:  $\pi^0$

HMS SHMS

$D_2$

**$^3He$**  Quark spin polarization

	$N^q$	U	L	T
Nucleon polarization	U	$f_1$		$h_1^\perp$
	L		$g_1$	$h_{1LL}^\perp$
	T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

Hall A

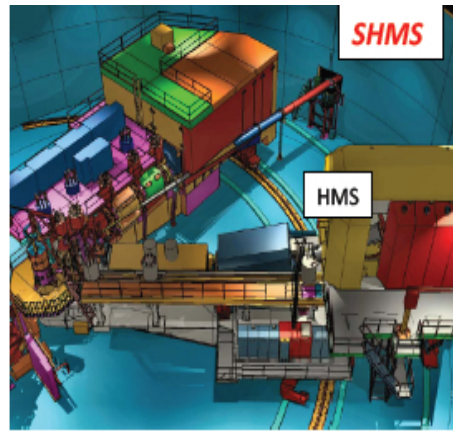
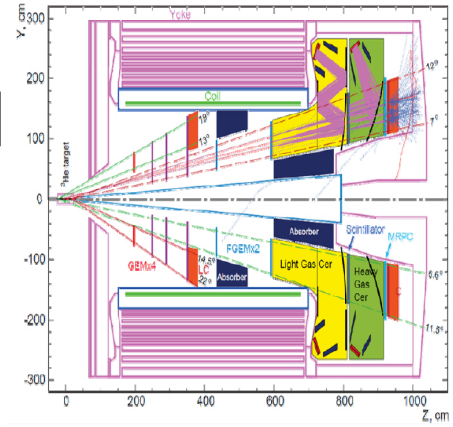
E12-07-007:  $\pi^+, \pi^-$

Solid

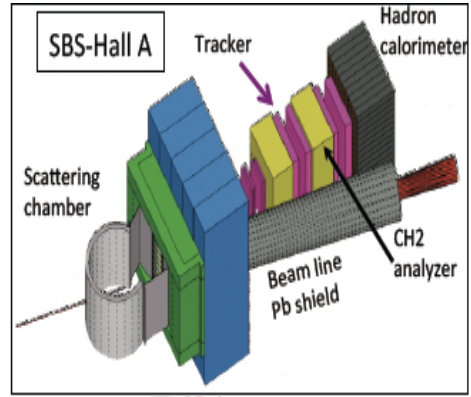
E10-006:  $\pi^+, \pi^-$   
E12-09-018:  $\pi^+, \pi^-, K^+, K^-$

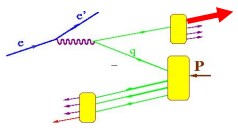
Solid SBS

$^3He$



C12-20-002  
 $\pi^+, \pi^-, \pi^0, K^+$

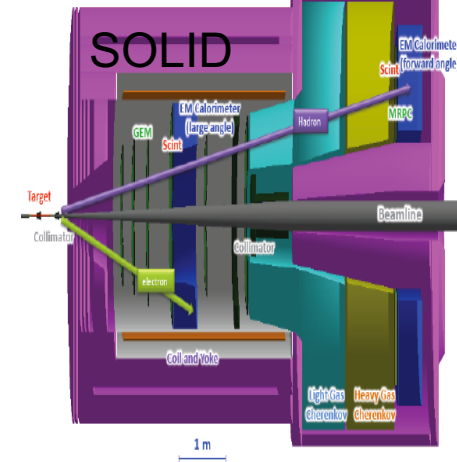
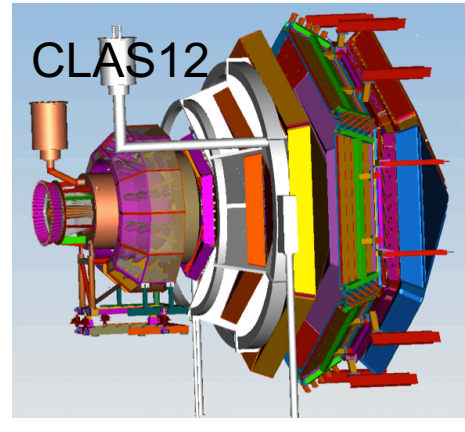
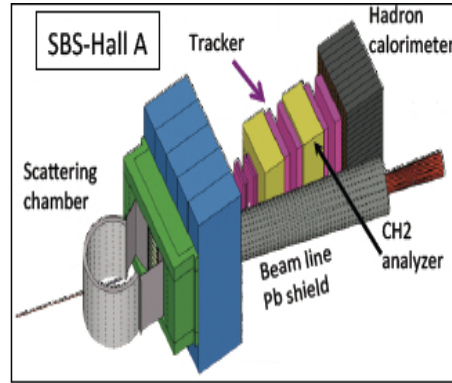
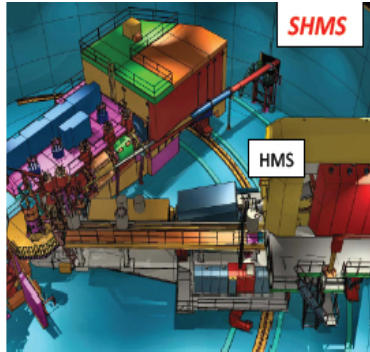




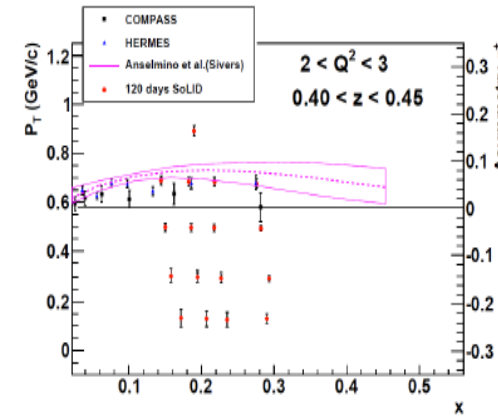
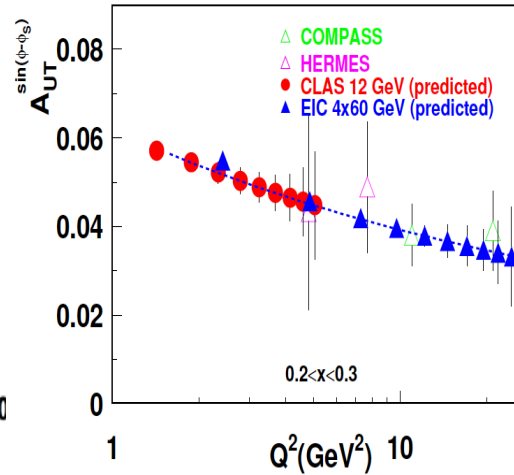
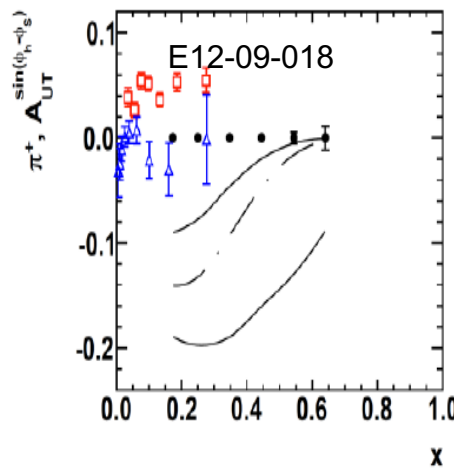
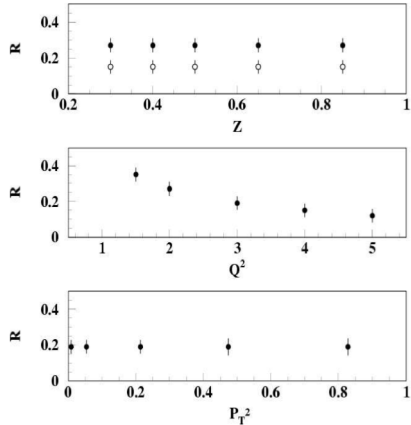
# SIDIS at JLab12

	$U$	$L$	$T$
$U$	$f_1$		$h_1^\perp$
$L$		$g_{1L}$	$h_{1TL}^\perp$
$T$	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

Complementary measurements with different targets



L/T-separation



Combination of high resolution measurements from spectrometers combined with large acceptance data from CLAS12 and SOLID would allow to study TMDs in details in the valence region

# 12 GeV Approved Experiments by Physics Topics



Topic (status: May 2021)	Hall A	Hall B	Hall C	Hall D	Other	Total
Hadron spectra as probes of QCD	0	2	1	4	0	7
Transverse structure of the hadrons	7	4	3	1	0	15
longitudinal structure of the hadrons	1	3	7	1	0	12
3D structure of the hadrons	5.5	9	6.5	0	0	21
Hadrons and cold nuclear matter	9	6	7	1	0	23
Low-energy tests of the Standard Model and Fundamental Symmetries	3	1	0	1	1	6
<b>Total</b>	<b>25.5</b>	<b>25</b>	<b>24.5</b>	<b>8</b>	<b>1</b>	<b>84</b>
<b>Total Experiments Completed</b>	<b>9.0</b>	<b>9.7</b>	<b>7.3</b>	<b>1.5</b>	<b>0</b>	<b>27.5</b>
<b>Total Experiments Remaining</b>	<b>16.5</b>	<b>15.3</b>	<b>17.2</b>	<b>6.5</b>	<b>1.0</b>	<b>56.5</b>

~10 years

JLab 2015 Science & Technology review closeout bullets:

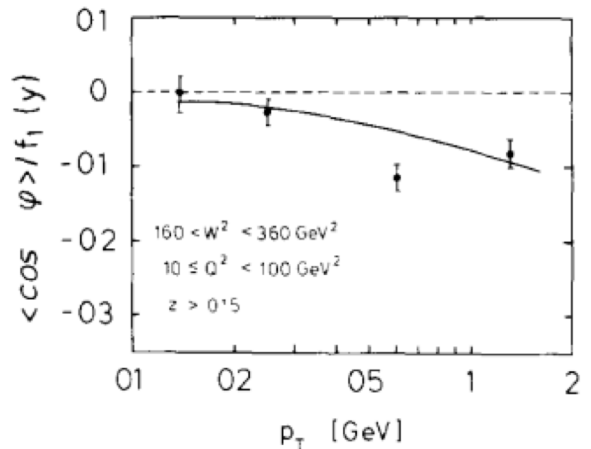
- develop an integrated picture of what measurements are necessary and will be conducted in determining the GPDs and TMDs
- develop milestones for extraction of GPDs and TMDs from experiment

# Azimuthal distributions in SIDIS (unpolarized)

$$\frac{d\sigma}{dx_B dy d\psi dz d\phi_h dP_{h\perp}^2} = \frac{\alpha^2}{x_B y Q^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x_B}\right) \left\{ \begin{array}{l} F_{UU,T} + \epsilon F_{UU,L} + \sqrt{2\epsilon(1+\epsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} \\ + \epsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\epsilon(1-\epsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} \end{array} \right\}$$

H.T. ↓
H.T. ↓
H.T. ↙

EMC-1983 (PL,v130,118)



**Observables: - Azimuthal Moments - Multiplicity**

$$\frac{d^4 M^{\pi^\pm}(x, Q^2, z, P_T^2)}{dx dQ^2 dz dP_T^2} = \left( \frac{d^4 \sigma^{\pi^\pm}}{dx dQ^2 dz dP_T^2} \right) / \left( \frac{d^2 \sigma^{DIS}}{dx dQ^2} \right)$$

$$m^h(x, z, P_T^2, Q^2) = \frac{\pi F_{UU,T}(x, z, P_T^2, Q^2) + \pi \epsilon F_{UU,L}(x, z, P_T^2, Q^2)}{F_T(x, Q^2) + \epsilon F_L(x, Q^2)}$$

- Quark-gluon correlations are significant in electro production experiments (even if at high energy).
- Large  $\cos\phi$  modulations observed in electroproduction (EMC, COMPASS, HERMES) may be a key in understanding of the QCD dynamics.

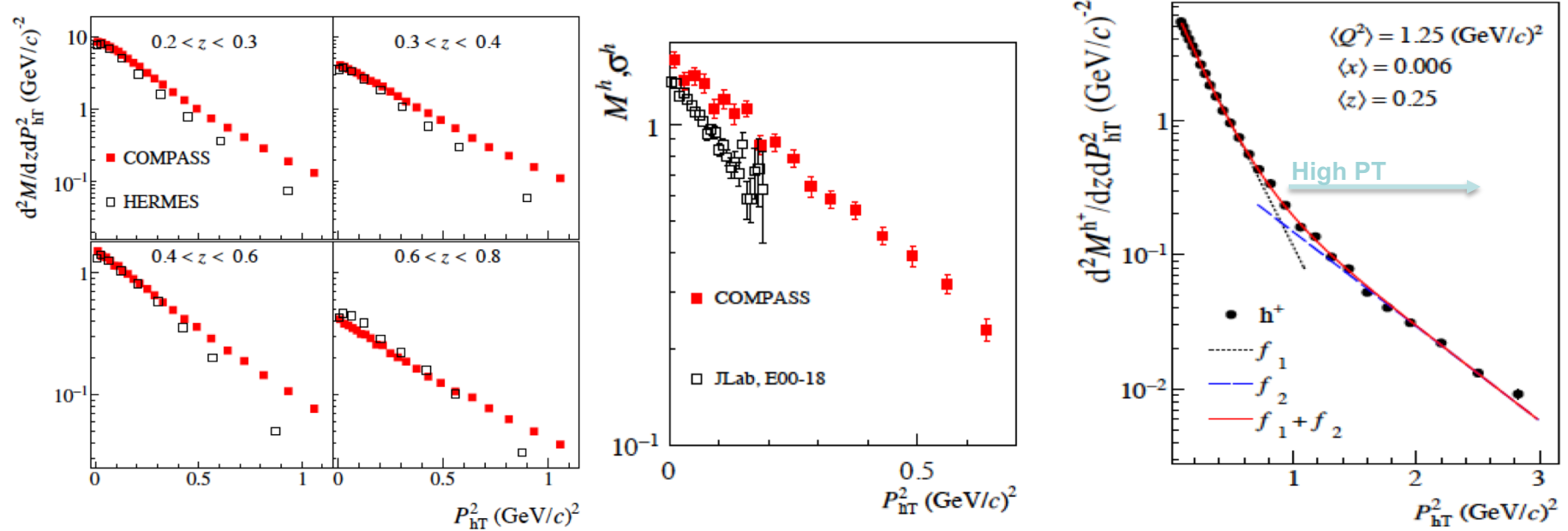
# Multiplicities of hadrons in SIDIS

Gaussian Ansatz

$$f_1^q \otimes D_1^{q \rightarrow h} = x f_1^q(x) D_1^{q \rightarrow h}(z) \frac{e^{-P_{hT}^2 / \langle P_{hT}^2 \rangle}}{\pi \langle P_{hT}^2 \rangle}$$

TMDs universal, so what is the origin of the differences observed ?

COMPASS:1709.07374



- TMDs evolution makes distribution wider
- Lower the beam energy, less phase space for high  $P_T$

- What is the origin of the “high PT tail”?
  - 1) Perturbative contributions?
  - 2) Non perturbative contributions? (TMDs dependence not 1 Gaussian)

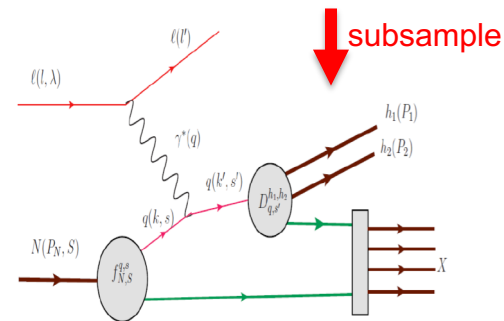
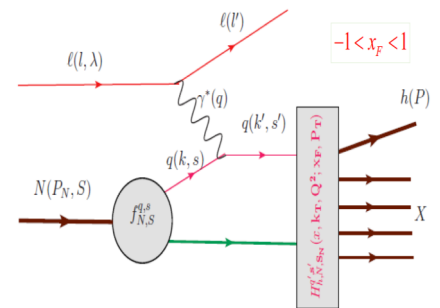
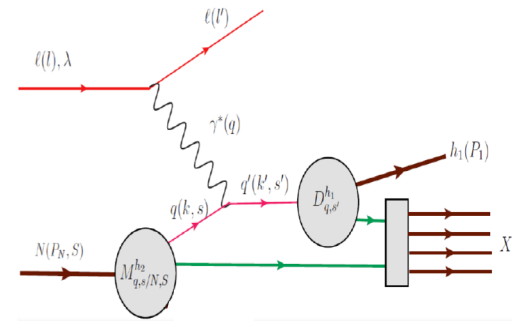


# MC simulations: Why LUND works?

- A single-hadron MC with the SIDIS cross-section where widths of  $k_T$ -distributions of pions are extracted from the data is not reproducing well the data.
- LUND fragmentation based MCs were successfully used worldwide from JLab to LHC, showing good agreement with data.

So why the LUND-MCs are so successful in description of hard scattering processes, and SIDIS in the first place?

- The hadronization into different hadrons, in particular Vector Mesons is accounted (full kinematics)
- Accessible phase space properly accounted
- The correlations between hadrons, as well as target and current fragments accounted
- ....



To understand the measurements we should be able to simulate, at least the basic features we are trying to study ( $P_T$  and  $Q^2$ ,-dependences in particular)

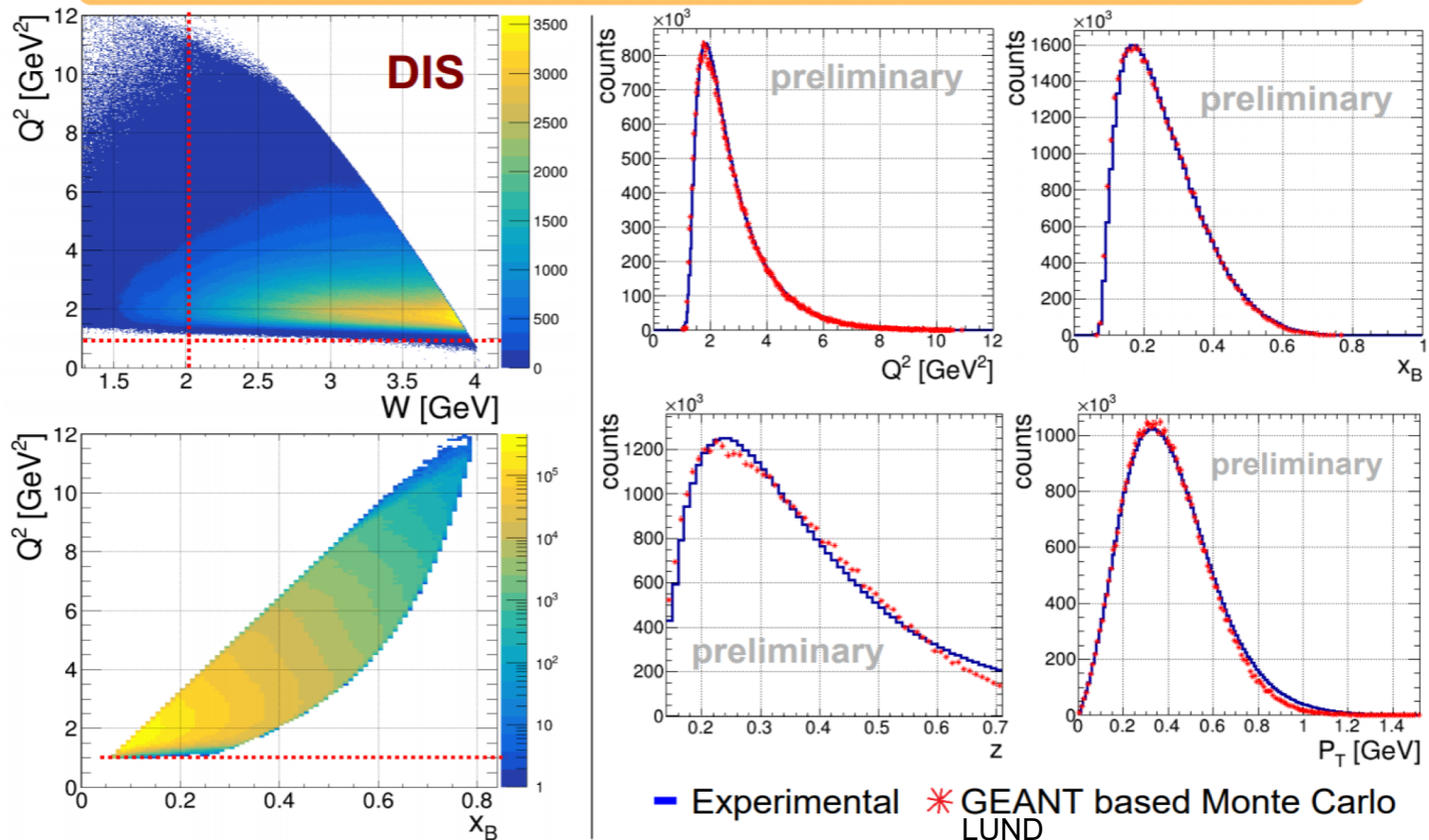
The studies of correlated hadron pairs in SIDIS may be a key for proper interpretation !!!

# SIDIS ehX: CLAS12 data

CLAS12 single hadron distributions  $ep \rightarrow e' \pi^+ X$

7

**Kinematic coverage for  $\pi^+$  (similar for  $\pi^-$  and  $\pi^0$ )**



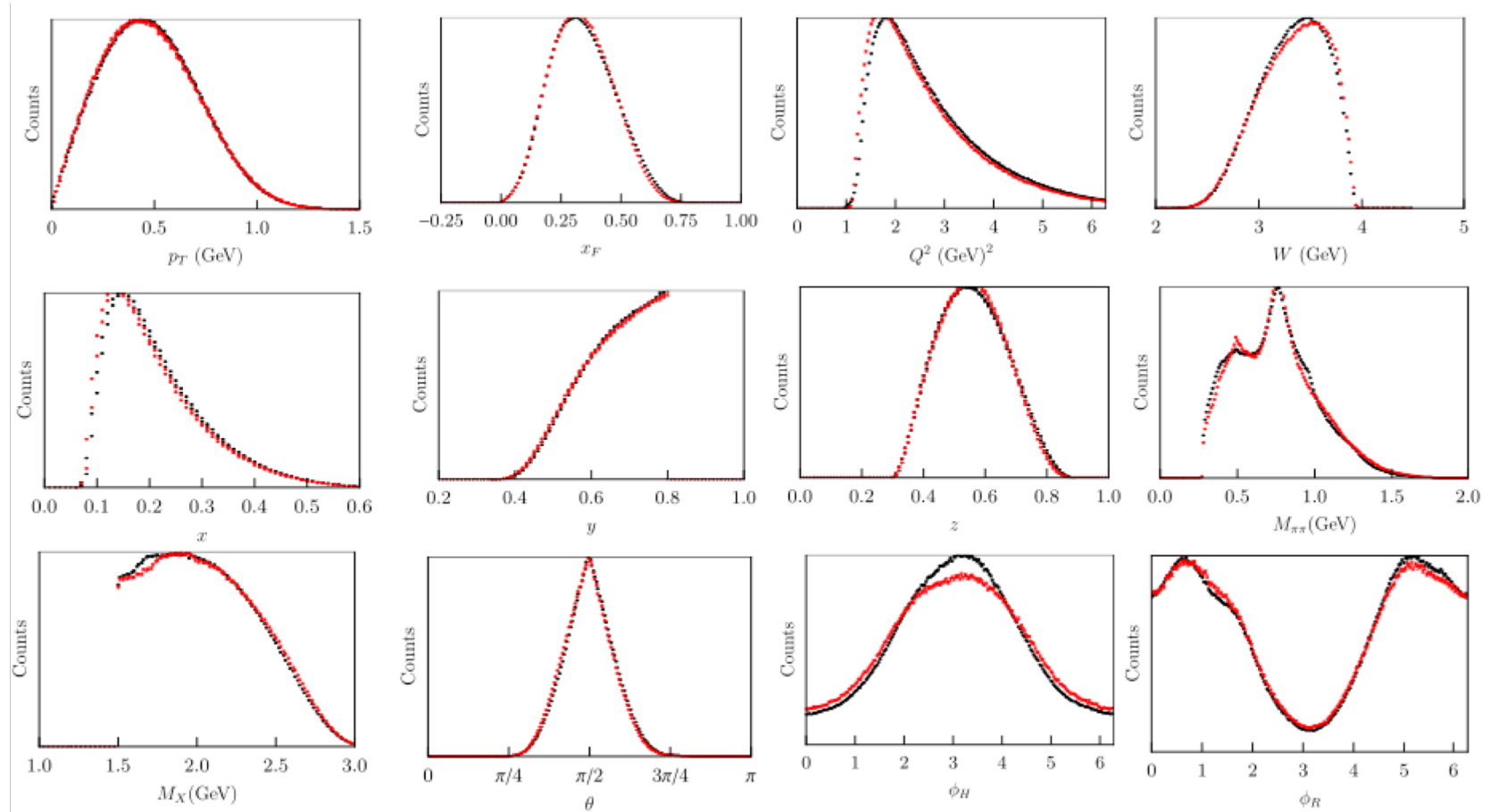
Stefan Diehl, JLU + UCONN

2020 JLUO Annual Meeting

06/24/2020

# SIDIS ehhX: CLAS12 data vs MC

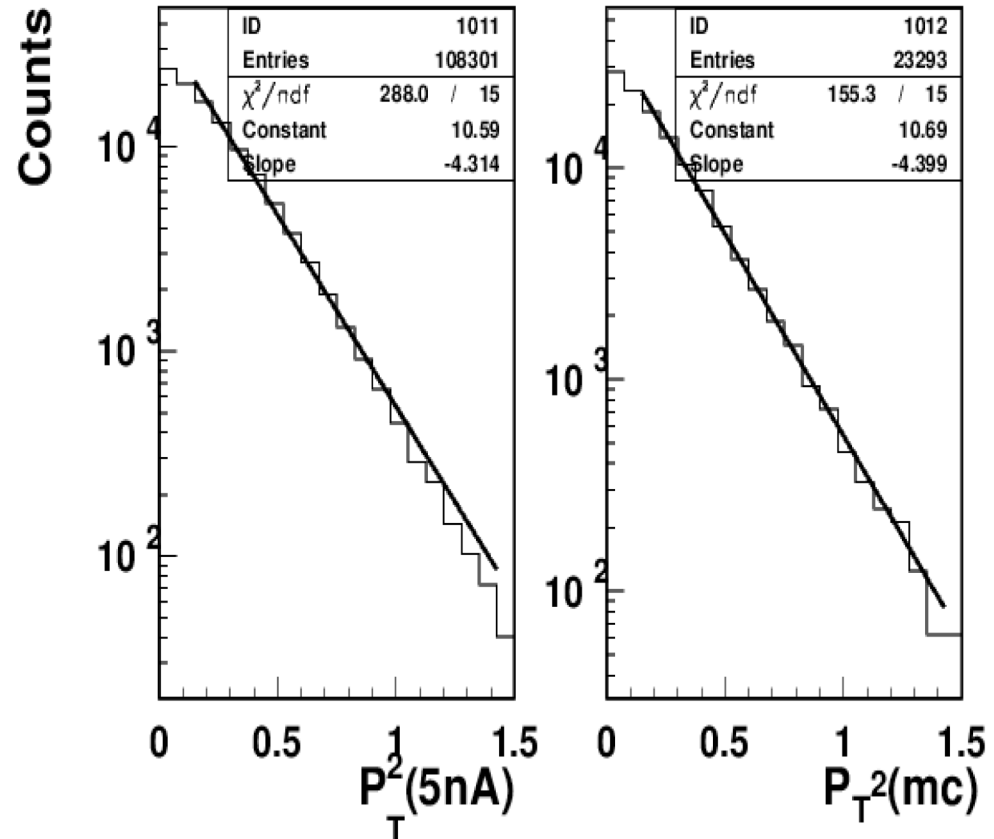
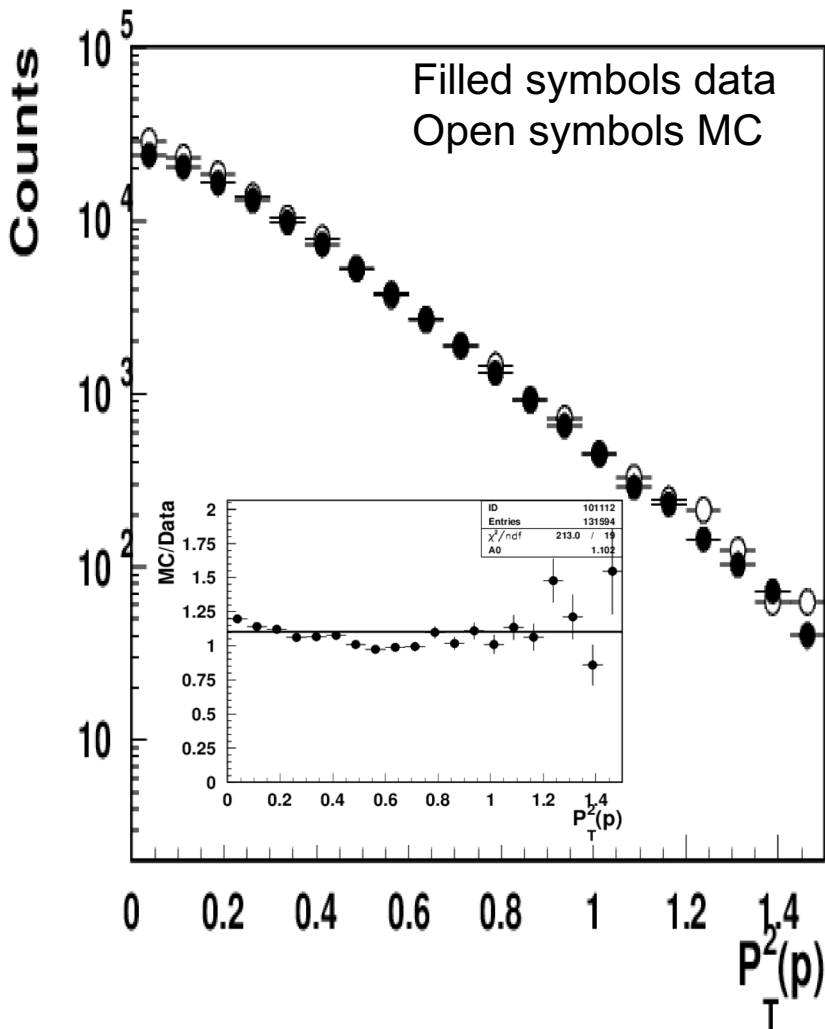
## CLAS12 dihadron production $ep \rightarrow ehhX$



CLAS12 MC, based on the PEPSI(LEPTO) simulation with most parameters "default" is in a good agreement with CLAS12 measurements for all relevant distributions

# CLAS12 Studies: Data vs MC

Using PEPSI (LUND) generator

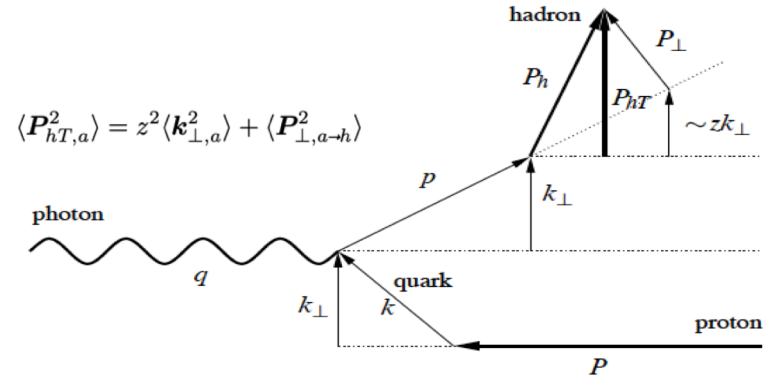
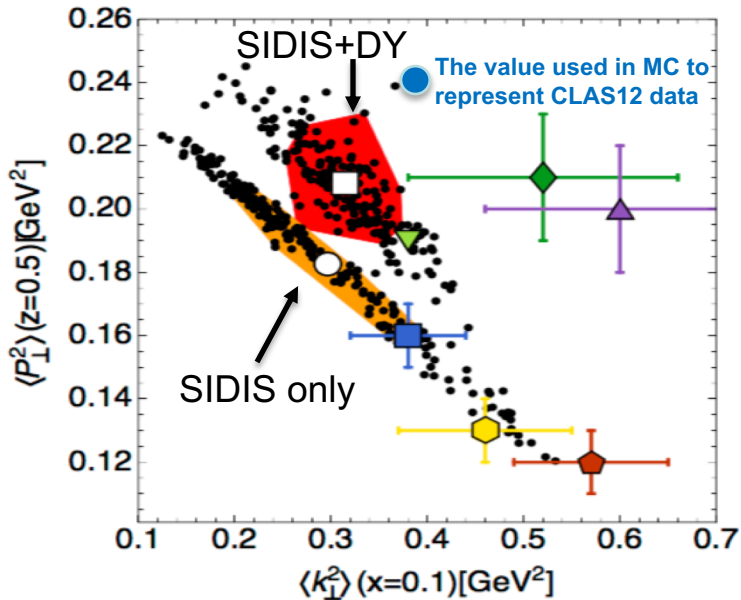


- $P_T$ -distributions of protons, and widths are in good agreement with LEPTO
- May be a source for widths in hadronization

# Extracting the average transverse momenta

Andrea Signori,<sup>1,\*</sup> Alessandro Bacchetta,<sup>2,3,†</sup> Marco Radici,<sup>3,‡</sup> and Gunar Schnell<sup>4,5,§</sup> [10.1007/JHEP11\(2013\)194](https://arxiv.org/abs/10.1007/JHEP11(2013)194)

$$F_{UU,T}^h(x, z, P_{hT}^2, Q^2) = \sum_a \mathcal{H}_{UU,T}^a(Q^2; \mu^2) \int dk_{\perp} dP_{\perp} f_1^a(x, k_{\perp}^2; \mu^2) D_1^{a-h}(z, P_{\perp}^2; \mu^2) \delta(zk_{\perp} - P_{hT} + P_{\perp}) + Y_{UU,T}(Q^2, P_{hT}^2) + \mathcal{O}(M/Q).$$



- Extraction very sensitive to input (replicas)
- Why DY gives higher values ?
- How to reconcile data with 1 pion MC?

- Theory: FFs include all possible sources of a given hadron, including fragmentation and diffractive VMs!
- How do we get the TMD FFs and what are their  $P_{\perp}$  and  $Q^2$  dependence?

$$m_N^h(x, z, P_{hT}^2) = \frac{\pi}{\sum_a e_a^2 f_1^a(x)} \times \sum_a e_a^2 f_1^a(x) D_1^{a-h}(z) \frac{e^{-P_{hT}^2 / (z^2 \langle k_{\perp,a}^2 \rangle + \langle P_{\perp,a-h}^2 \rangle)}}{\pi (z^2 \langle k_{\perp,a}^2 \rangle + \langle P_{\perp,a-h}^2 \rangle)}$$

Sea is not divided to perturbative and non-perturbative

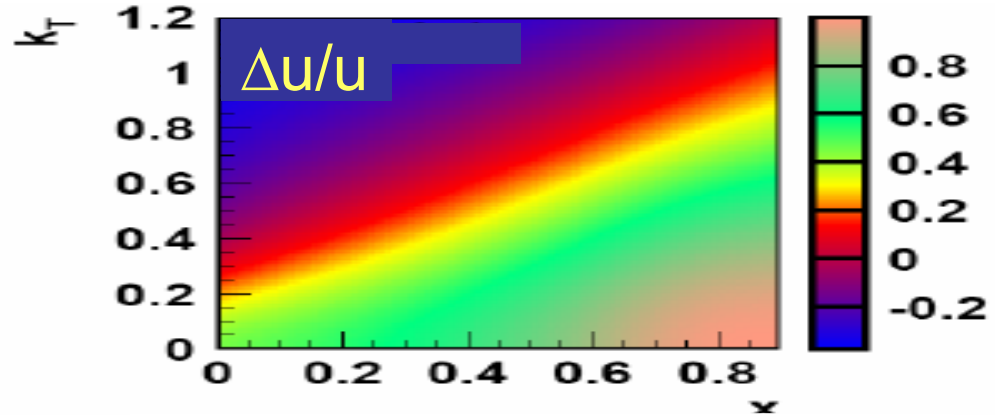
# Unknown “known” $f_1, g_1$ TMDs

$$u^+(x, k_T) = f_1^u(x, k_T^2) + g_1^u(x, k_T^2)$$

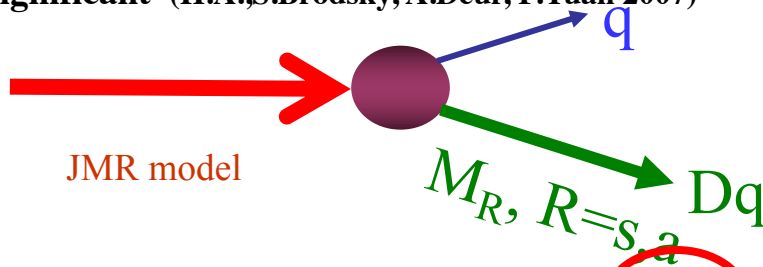
$$u^-(x, k_T) = f_1^u(x, k_T^2) - g_1^u(x, k_T^2)$$

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

(dipole formfactor), J.Ellis, D-S.Hwang, A.Kotzinian

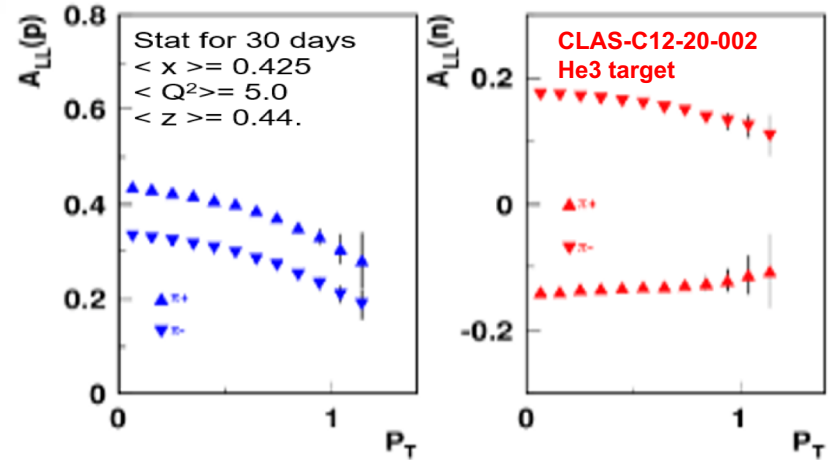


Effect of the orbital motion on the  $q$ - may be significant (H.A.,S.Brodsky, A.Deur, F.Yuan 2007)



$$f_1(x, k_T^2) = A \frac{(xM + m)^2 + k_T^2}{(k_T^2 + \lambda_R^2)^{2\alpha}}$$

$$g_1(x, k_T^2) = A \frac{(xM + m)^2 - k_T^2}{(k_T^2 + \lambda_R^2)^{2\alpha}}$$



Models and lattice predict very significant spin and flavor dependence for TMDs  
 Large transverse momenta are crucial to access the large  $k_T$  of quarks  
 A dedicated to  $g_1(x, k_T)$ -studies CLAS12 proposal with He3 target approved by PAC

# Flavor dependent TMD Fragmentation functions

<https://www.phy.anl.gov/nsac-lrp/Whitepapers/StudyOfFragmentationFunctionsInElectronPositronAnnihilation.pdf>

$$F_{UU} \propto \sum_q f_{1,q}(x, k_{\perp}) \otimes D_1^{q \rightarrow h}(z, p_{\perp})$$

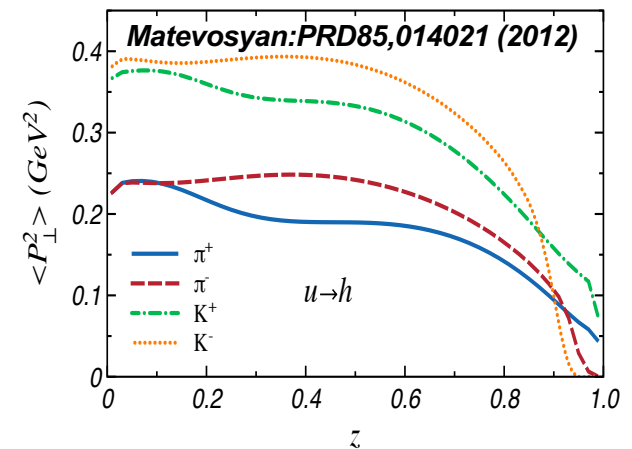
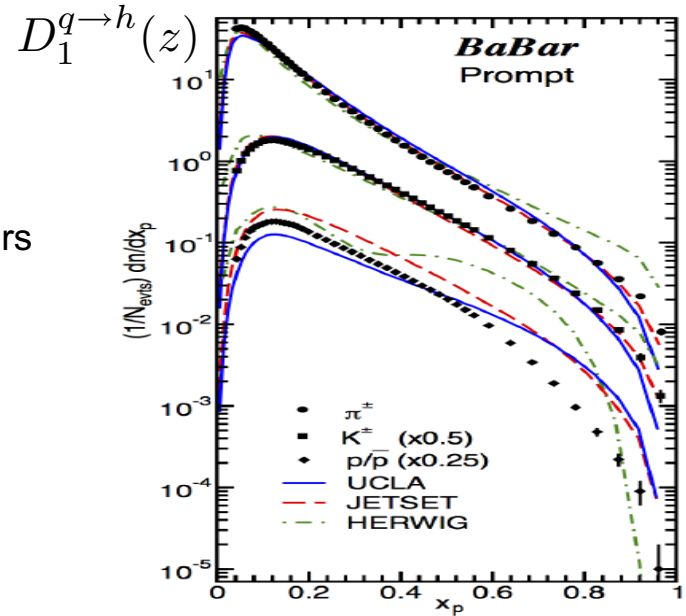
Even simple approximations require an additional set of parameters

$$D_1^{q \rightarrow h, fav}(z, p_{\perp}) = D_1^{q \rightarrow h}(z) \times \frac{e^{-\frac{p_{\perp}^2}{\langle p_{\perp}^2, fav(z) \rangle}}}{\pi \langle p_{\perp}^2, fav(z) \rangle}$$

$$D_1^{q \rightarrow h, unf}(z, p_{\perp}) = D_1^{q \rightarrow h}(z) \times \frac{e^{-\frac{p_{\perp}^2}{\langle p_{\perp}^2, unf(z) \rangle}}}{\pi \langle p_{\perp}^2, unf(z) \rangle}$$

$$\langle p_{\perp}^2, unf(z) \rangle > \langle p_{\perp}^2, fav(z) \rangle$$

Measurements of flavor and spin dependence of transverse momentum dependent fragmentation functions will provide critical input to TMD extraction



# CLAS12 (JLAB) Detector

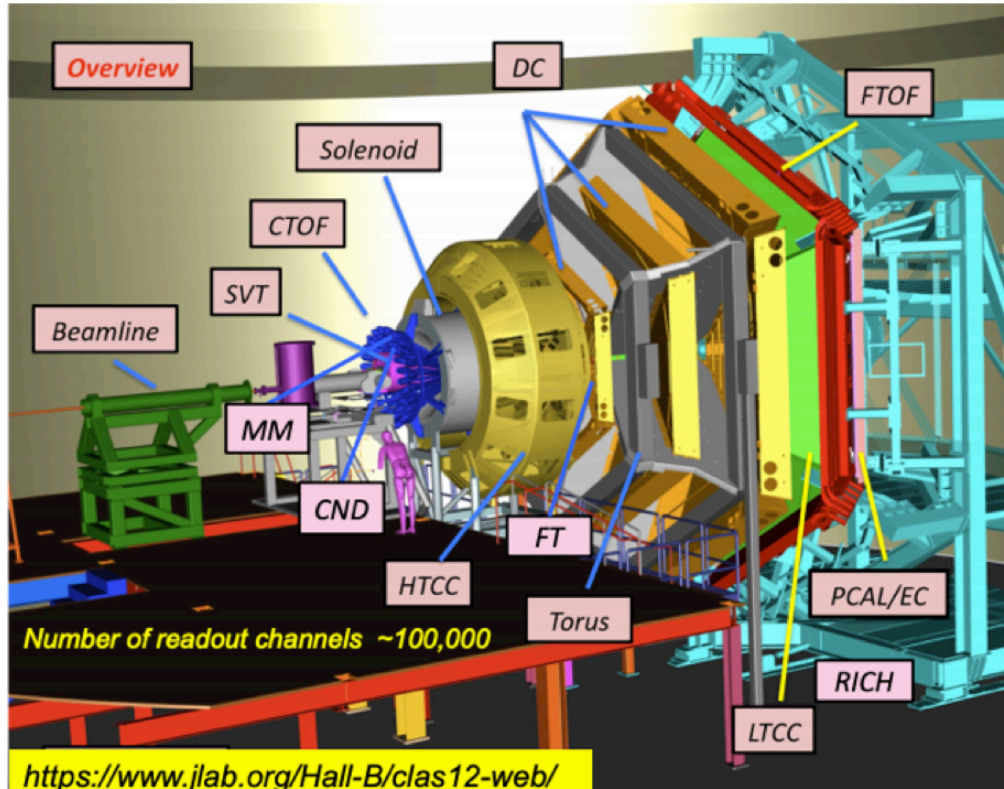
**CLAS allows measuring multi-particle final state detection, opening unique possibilities to study correlation in hadron production.**

## Forward Detector:

- TORUS magnet
- HT Cherenkov Counter
- Drift chamber system
- LT Cherenkov Counter
- RICH detector
- Forward ToF System
- Pre-shower calorimeter
- E.M. calorimeter (EC)
- Forward Tagger

## Central Detector:

- SOLENOID magnet
- Barrel Silicon Tracker
- Micromegas
- Central ToF system
- Neutron detector
- Backward Angle Neutron detector



The CLAS12 Spectrometer at Jefferson Laboratory, V.D. Burkert, et al. Nucl. Instrum. Meth. A, *Volume 959*, 2020, 163419

## PID @ CLAS12

GeV	1	2	3	4	5	6	7	8	9	10
	FTOF									
$\pi/K$			LTCC			HTCC				
			RICH							
$\pi/p$	FTOF		LTCC			HTCC				
			RICH							
$K/p$	FTOF							LTCC		
			RICH							
$e/\pi$			ECAL							
	HTCC									

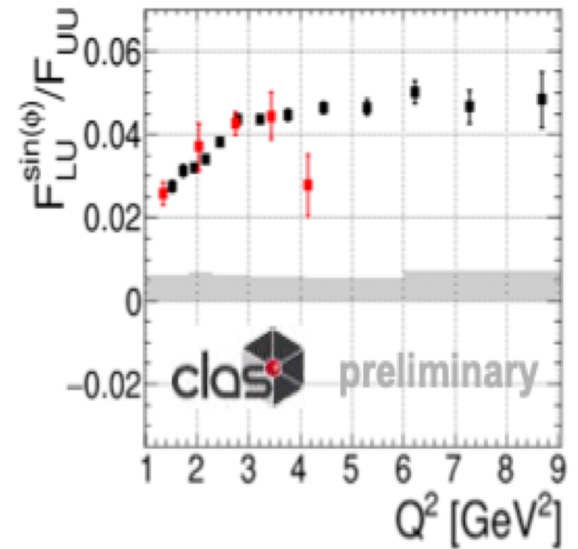
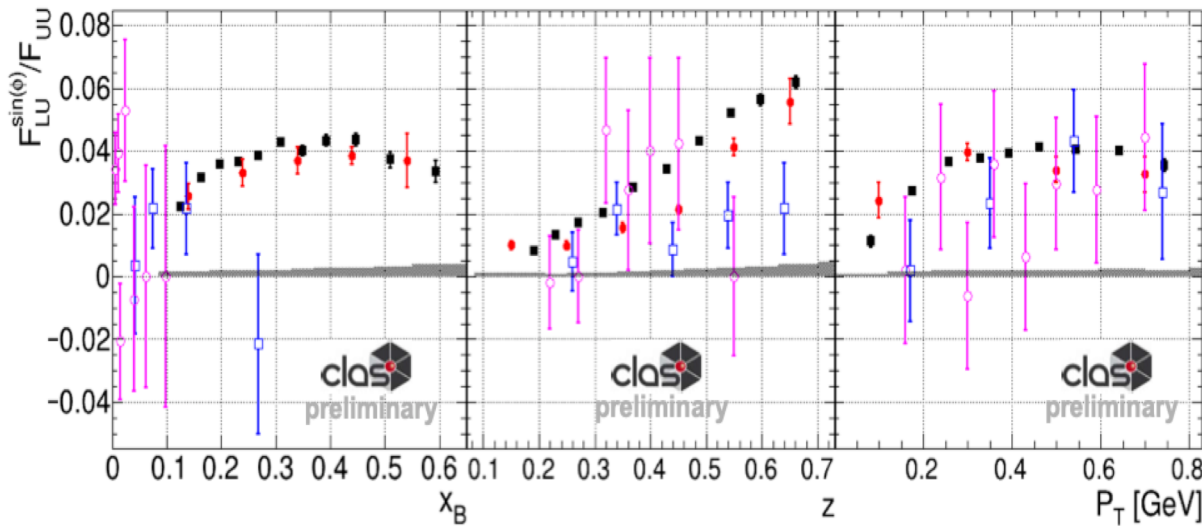
- Large acceptance detector
- Polarized beam (85% average polarization)
- Operates with polarized and unpolarized targets.
- Luminosity up to  $10^{35} \text{ cm}^{-2} \text{ s}^{-1}$
- Beam energy up to 10.6 GeV



# SSA from CLAS12

S. Diehl et al (in publication) [arXiv:2101.03544](https://arxiv.org/abs/2101.03544)

$$BSA_i = \frac{1}{P_e} \cdot \frac{N_i^+ - N_i^-}{N_i^+ + N_i^-} \quad \langle \sin \phi \rangle \propto F_{LU}^{\sin \phi} / F_{UU} \propto 1/Q$$

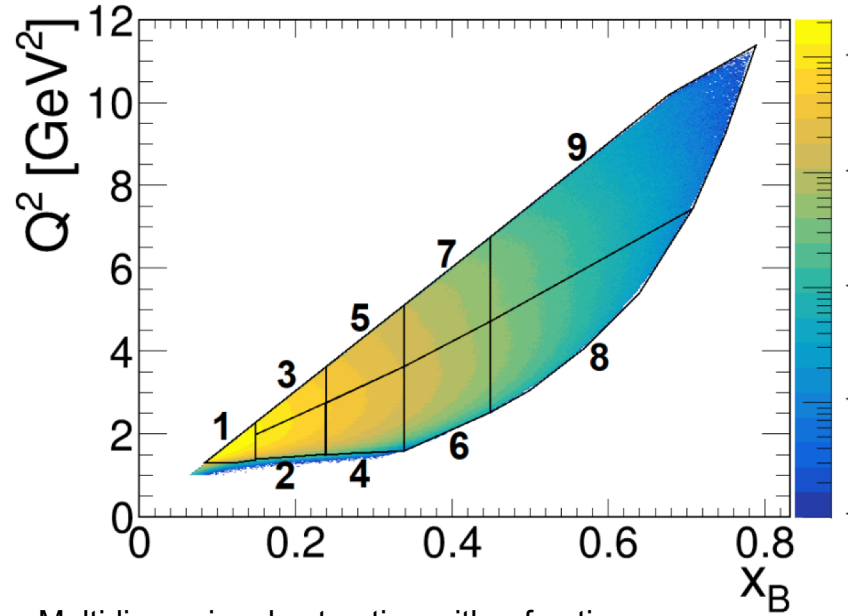


- CLAS12 [this work]
- CLAS [PRD 98 (2014)]
- HERMES [Phys. Let. B 648 (2007)]
- COMPASS [Nucl. Phys. B 886 (2014)]

- Superior statistics in large x-region most relevant for spin-orbit correlation studies
- Unexpected  $Q^2$ -dependence is under study in fine multidimensional bins  $x, z, P_T$

# SSA from CLAS12

S. Diehl et al (in publication) [arXiv:2101.03544](https://arxiv.org/abs/2101.03544)

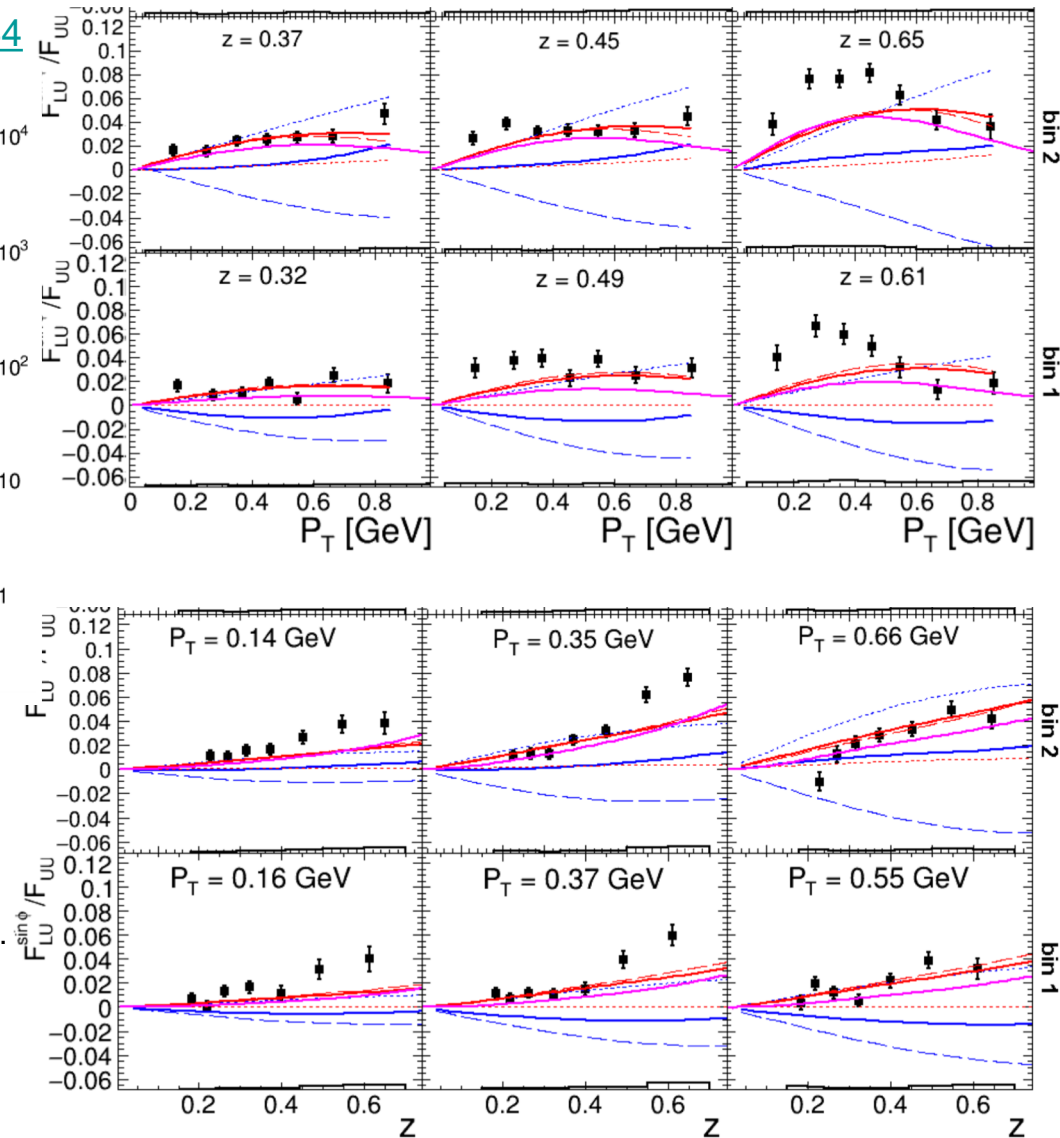


Multidimensional extraction with a fraction of the total approved statistics for the experiment.

Model 1: W. Mao and Z. Lu, Eur. Phys. J. C 73, 2557 (2013)

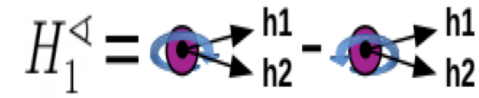
Model 2: W. Mao and Z. Lu, Eur. Phys. J. C 74, 2910 (2014).

$e\bar{H}_1^\perp$  (dashed line) and  $g^\perp D_1$  (dotted line)



# Observation of SSAs in $ep \rightarrow e' \pi^+ \pi^- X$

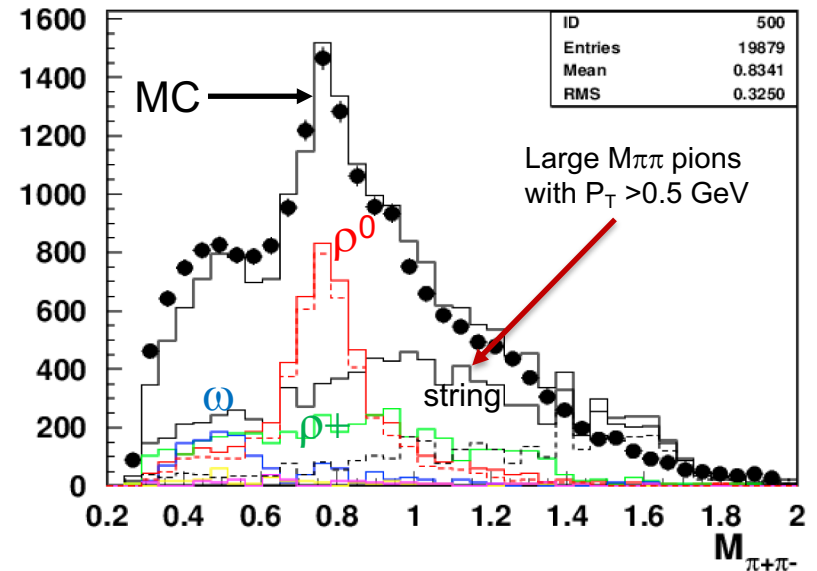
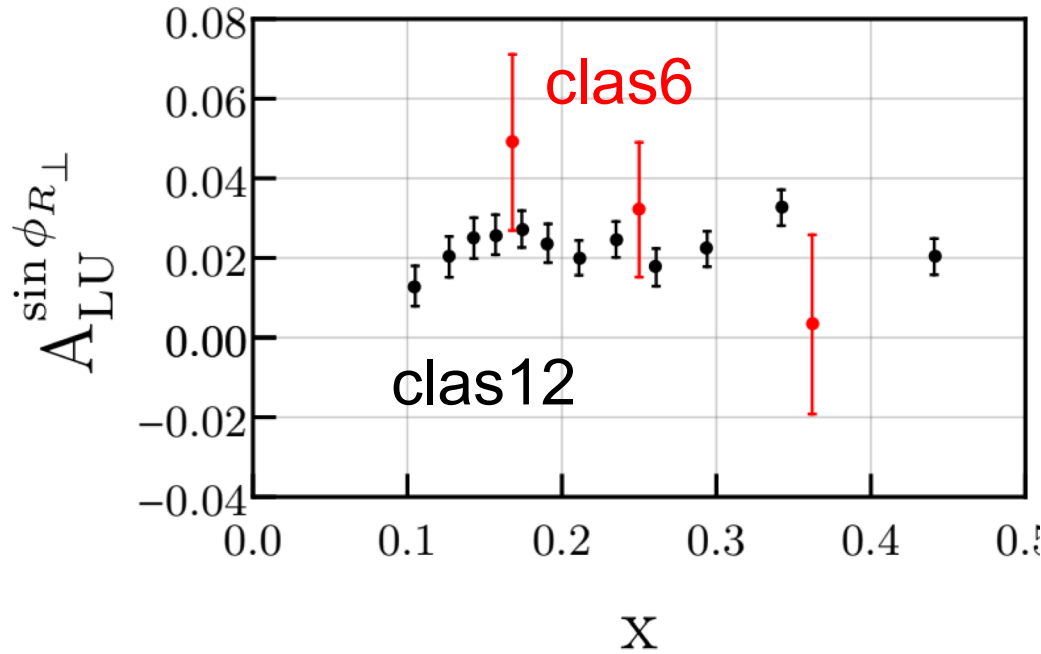
T. Hayward et al. Phys. Rev. Lett. 126, 152501 (2021)



$$d\sigma_{LU} \propto \lambda_e \sin(\phi_{R\perp}) \left( x e(x) H_1^{\Delta}(z, M_h) + \frac{1}{z} f_1(x) \tilde{G}^{\Delta}(z, M_h) \right)$$

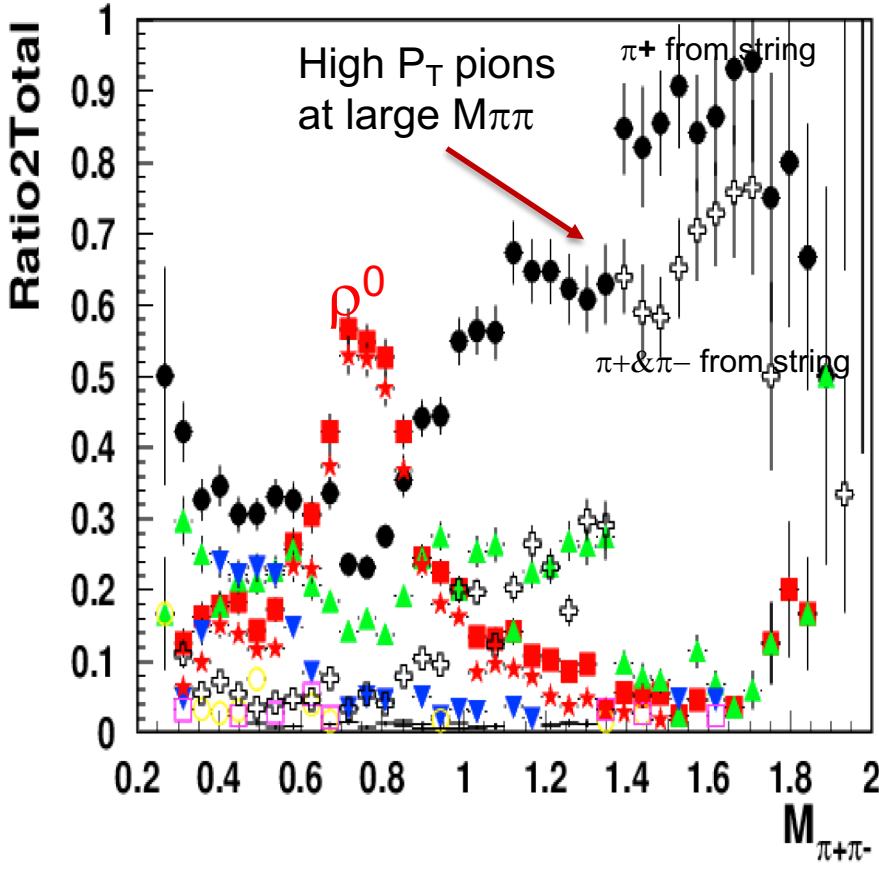
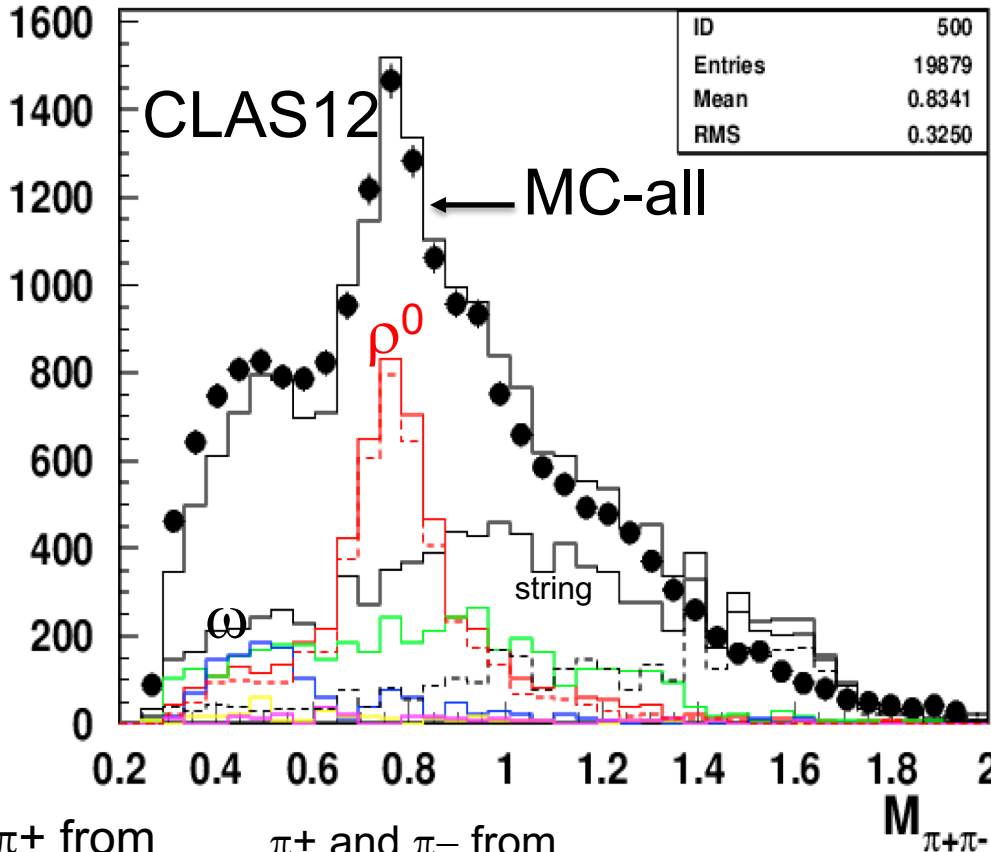
PDF  $e$  describes the force on the transversely polarized quark after scattering

Bacchetta&Radici: arXiv:hep-ph/0311173



- Spin-azimuthal correlations in hadron pair production are very significant
- Hadron pairs in SIDIS (true from JLab to LHC) are dominated by VM decays (therefore single hadron channel too)

# Sources of inclusive pions: CLAS12 vs MC



$\pi^+$  from  $\rho^0$  (red solid line)  
 $\pi^+$  and  $\pi^-$  from string (black solid line)  
 $\rho^+$  (green solid line)  
 $\omega$  (blue solid line)

$\pi^+$  and  $\pi^-$  from  $\rho^0$  (dashed red line)  
 $\pi^+$  and  $\pi^-$  from string (dashed black line)

- Dominant fraction of inclusive pions come from VM decays
- Relative fraction by default in JETSET ~50%

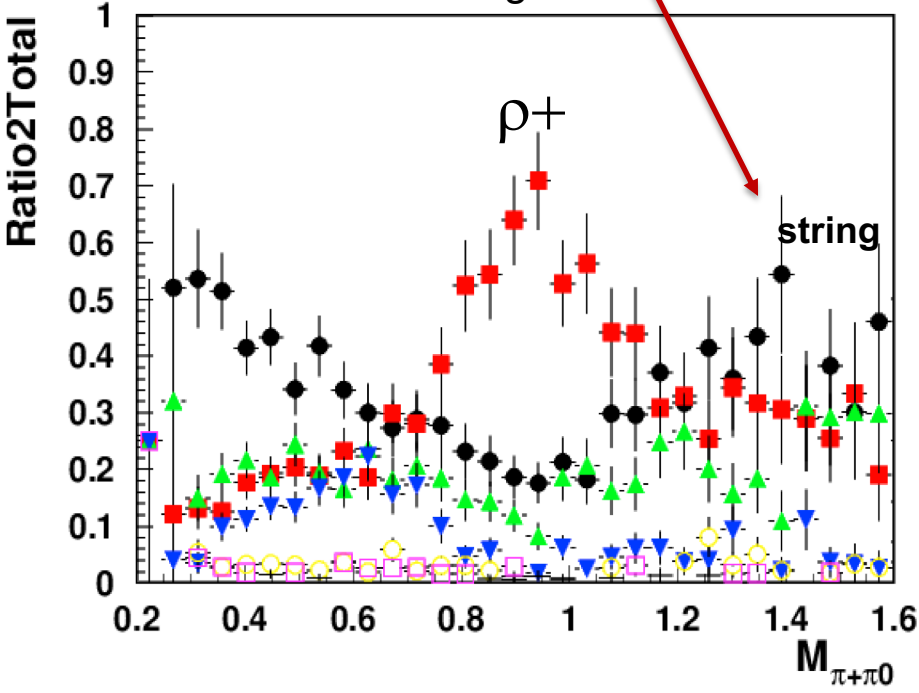
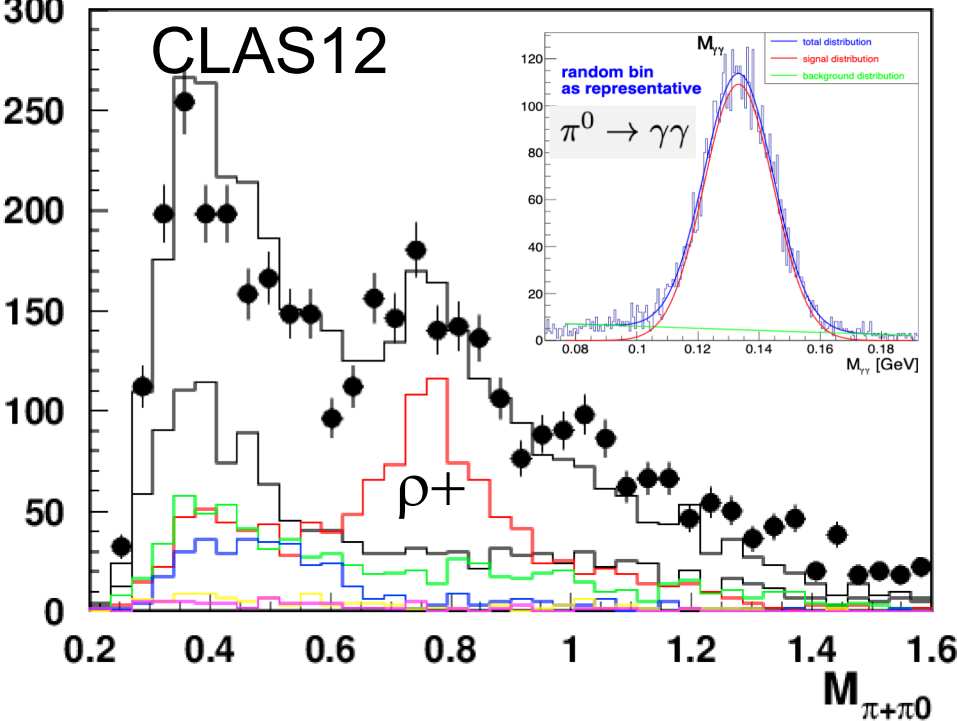
Very important to have multidimensional TMD Fragmentation Functions!

# Sources of inclusive pions: CLAS12 vs MC

$$\rho^\pm \rightarrow \pi^0 + \pi^\pm$$

Detection of  $\pi^0$ s allows studies of  $\rho^\pm$

High  $P_T$  pions at large  $M_{\pi\pi}$



- $\rho^+$
- string
- $\rho^0$
- $\omega$

Dominant fraction of inclusive pions come from VM decays

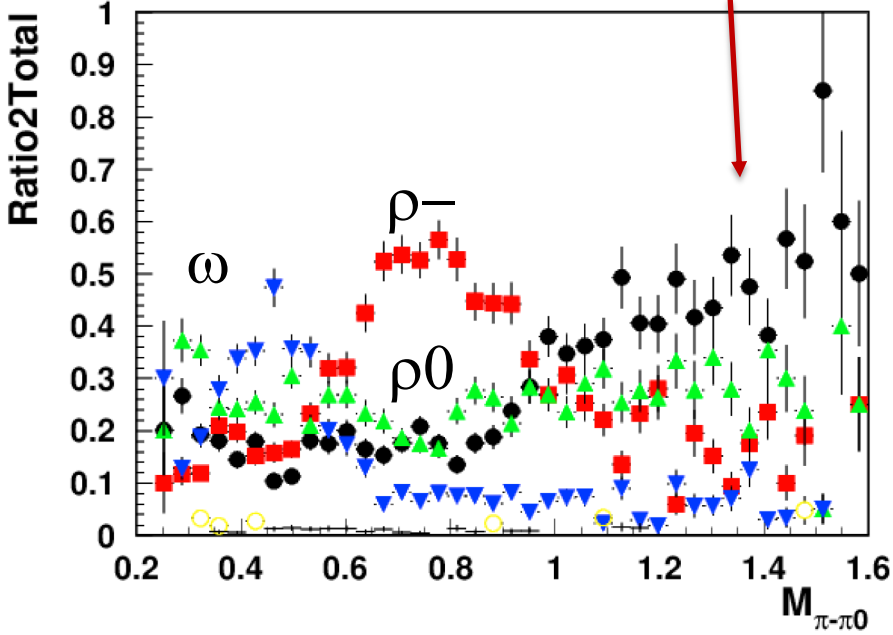
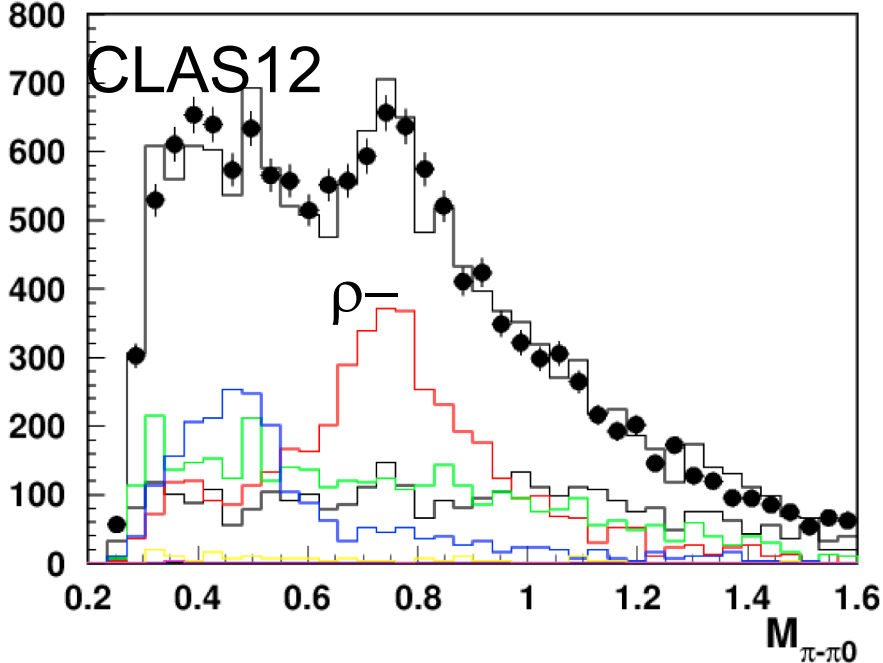
CLAS12 due to unique capability for precision measurements of neutral pions, will provide measurements of multiplicities of variety of semi-inclusive and exclusive hadron pairs (could be also VMs).

# Sources of inclusive pions: CLAS12 vs MC

$$\rho^\pm \rightarrow \pi^0 + \pi^\pm$$

Detection of  $\pi^0$ s allows studies of  $\rho^\pm$

High  $P_T$  pions at large  $M_{\pi\pi}$



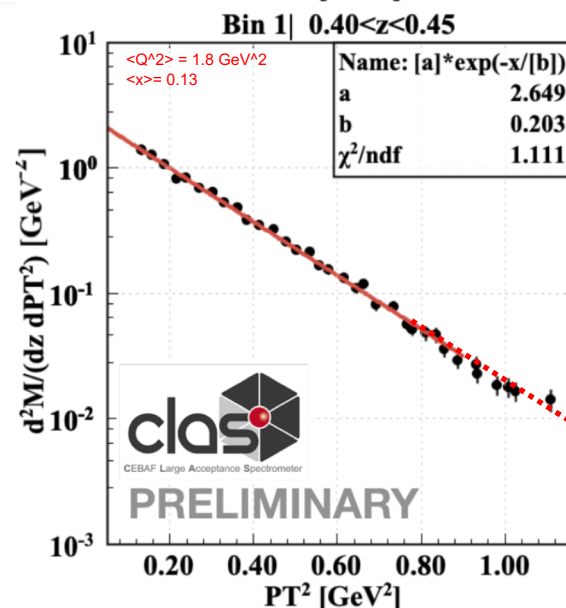
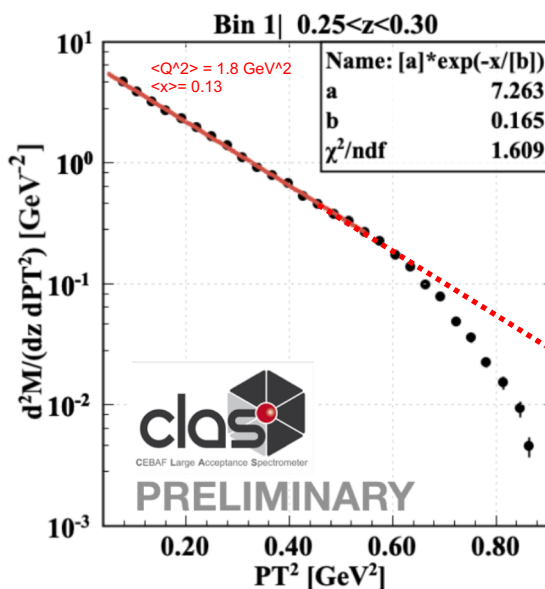
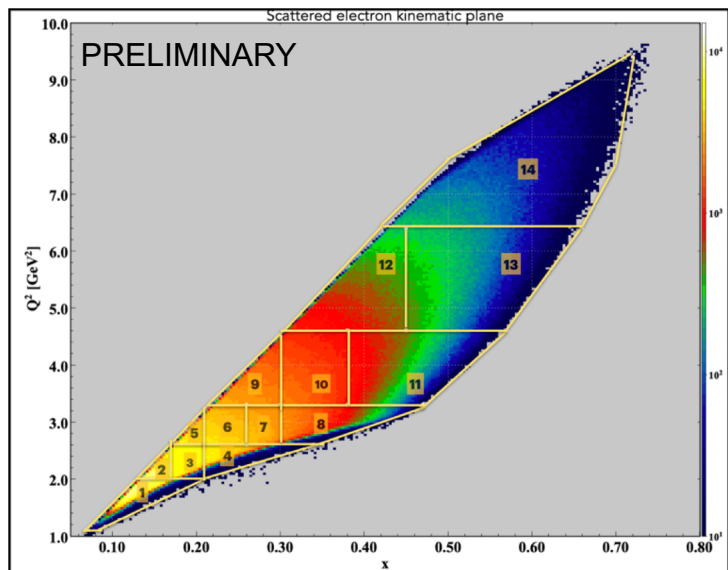
$\pi^-$  from:

- $\rho^-$
- string
- $\rho^0$
- $\omega$

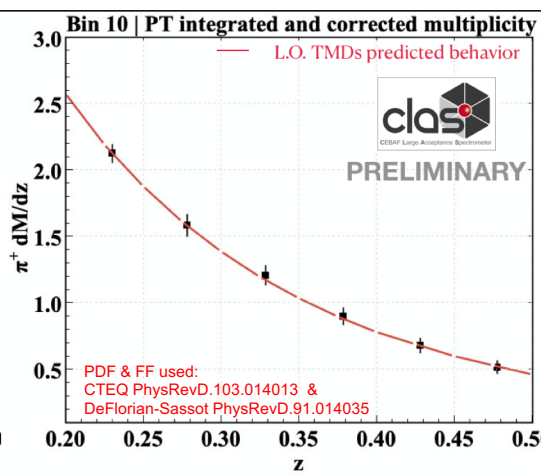
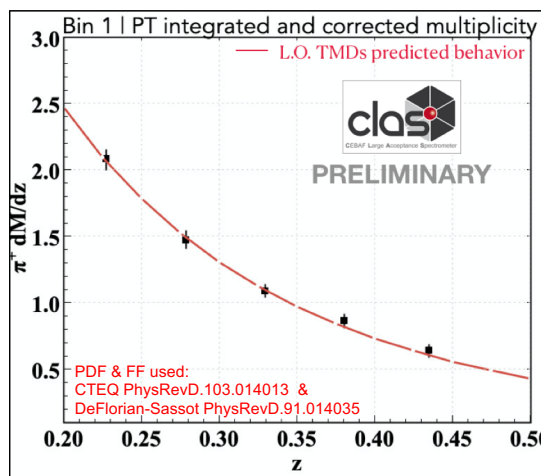
Dominant fraction of inclusive pions come from VM decays

Precision measurements of all combination of pion pairs is crucial for separation of multiplicities of different vector mesons

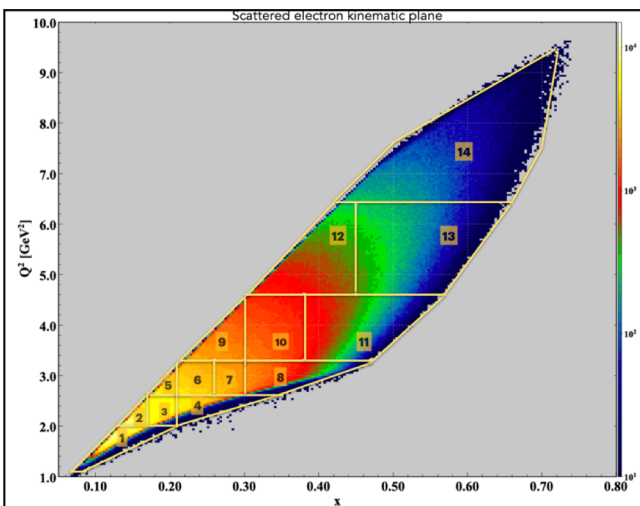
# CLAS12 1h Multiplicities: high $P_T$ & phase space



For some kinematic regions, at low  $z$ , the high  $P_T$  distribution appear suppressed: there is not enough energy in the system to produce hadron with high transverse momentum (phase space effect). If the effect is accounted, the CLAS data follows global fits.

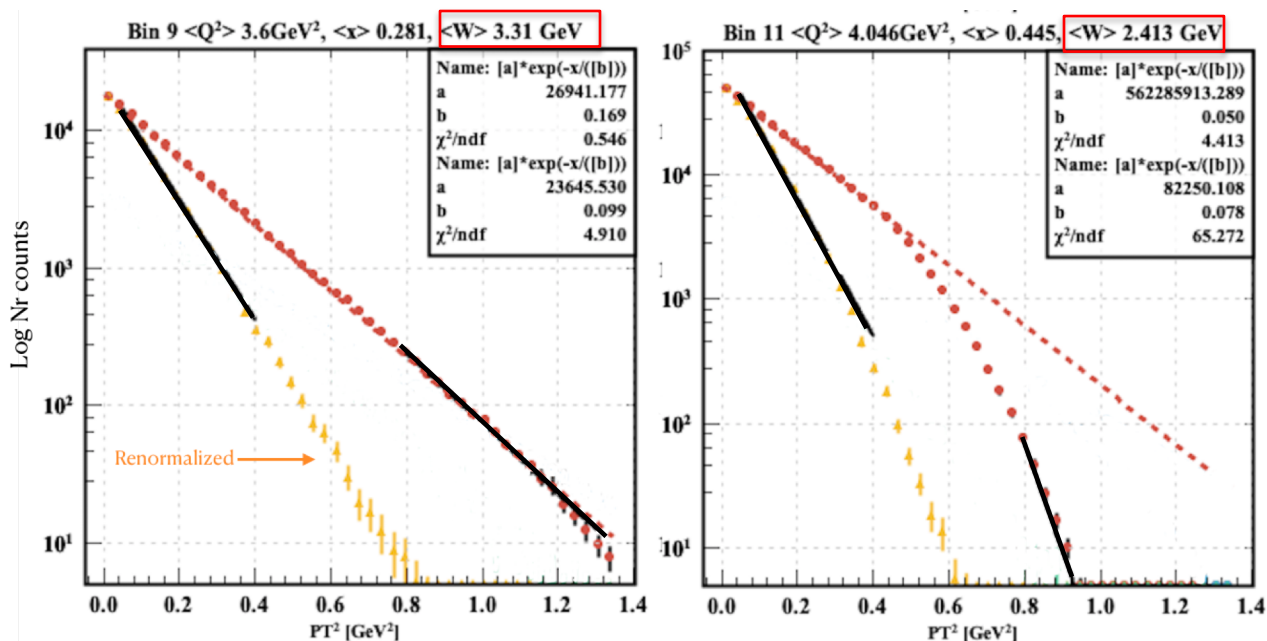


# CLAS12 1h Multiplicities: high $P_T$ & phase space



We binned the MC Phase space as for the CLAS12 multiplicity analysis, we used a single hadron generator with PDFs, FFs, and Gaussian Ansatz for transverse momentum and looked at the produced distribution.

- Coded PT distribution in generator ( $0.2 < z < 0.25$ )
- Directly Generated  $\pi^+$  ( $0.2 < z < 0.25$ )
- ▲  $\pi^+$  decayed from  $\omega$  ( $0.2 < z < 0.25$ )
- Gaussian Fit

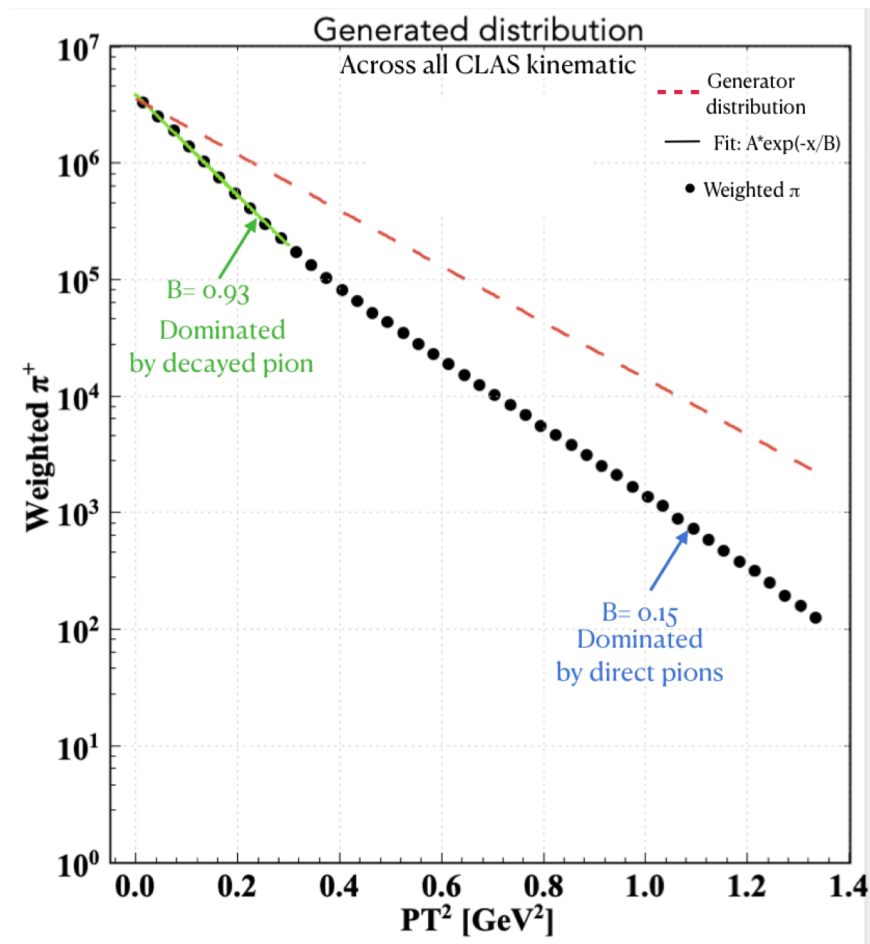
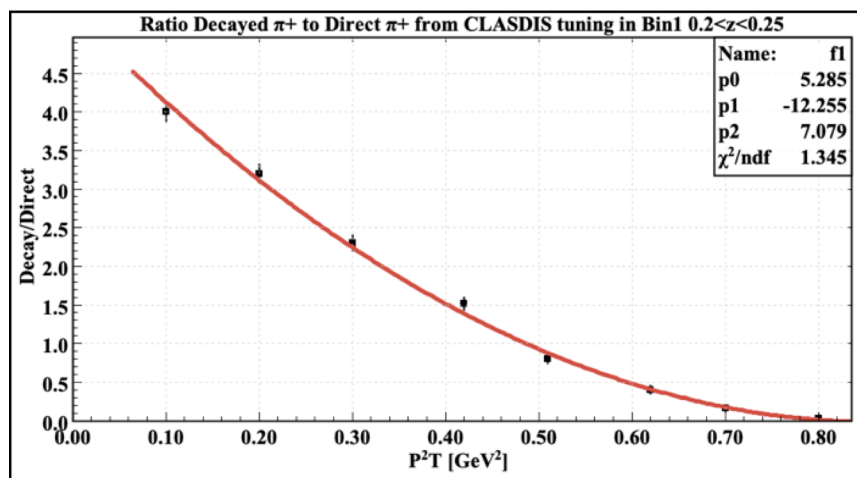


- Phase space limitations for direct pion production more significant at low  $W$ , and low  $z$
- Decayed pions have a much steeper  $P_T$  distribution at the same  $z$



# CLAS12 high $P_T$ : impact of vector mesons

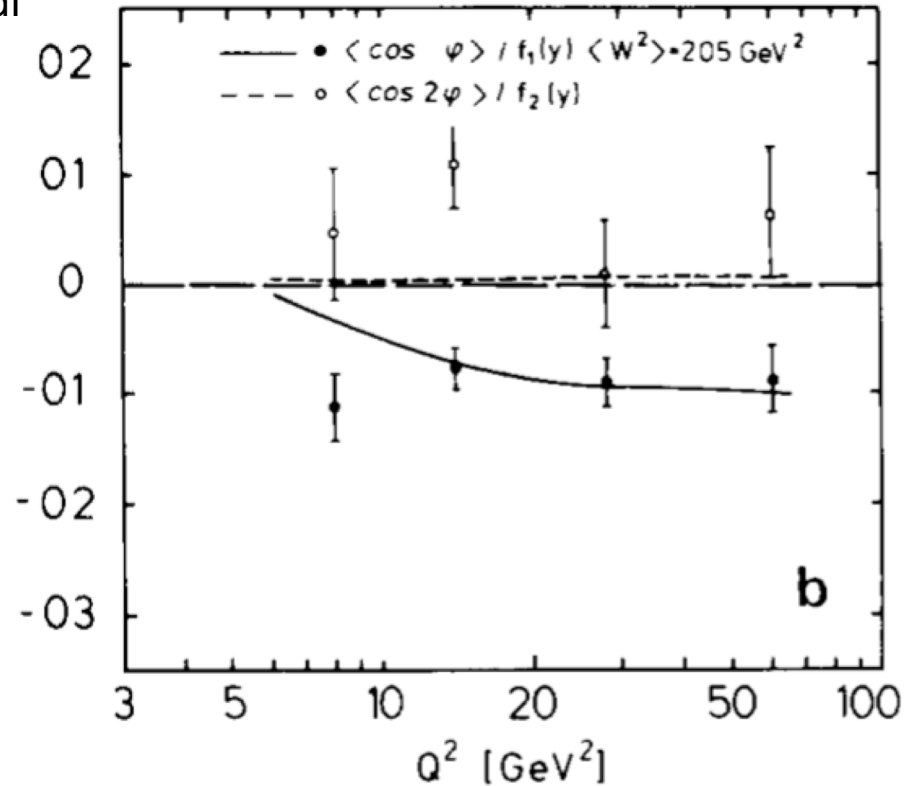
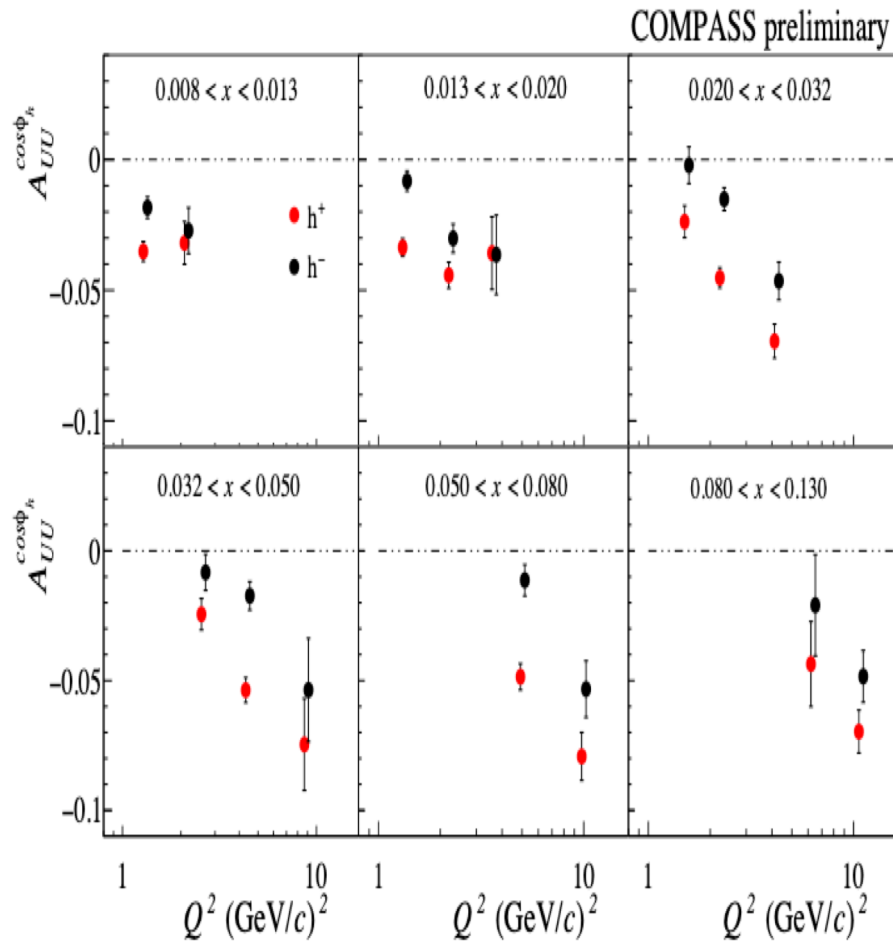
We consider the ratio of Decayed to Direct pions from the LEPTO MC (that well describes our data) and reweighted the distribution of pions accordingly.



By combining the directly produced pions and the decayed pions, two Gaussian slopes are effectively generated even if we started with one single gaussian

# Large cosines from EMC to COMPASS

A. Moretti: <https://arxiv.org/pdf/2107.10740.pdf>



J. Aubert *et al.*, "Measurement of Hadronic Azimuthal Distributions in Deep Inelastic Muon Proton Scattering," *Phys. Lett. B*, vol. 130, pp. 118–122, 1983.

A. König and P. Kroll, "A Realistic Calculation of the Azimuthal Asymmetry in Semi-inclusive Deep Inelastic Scattering," *Z. Phys. C*, vol. 16, p. 89, 1982.

Cosine moments do not really follow the expected Q-behaviour

# Unpolarized x-section: $F_{UU}^{\text{Cahn}}$

Anselmino et al arXiv:hep-ph/0412316

assume, both for the parton densities and the fragmentation functions, a factorized Gaussian dependence

$$\langle P_T^2 \rangle = \langle p_\perp^2 \rangle + z_h^2 \langle k_\perp^2 \rangle$$

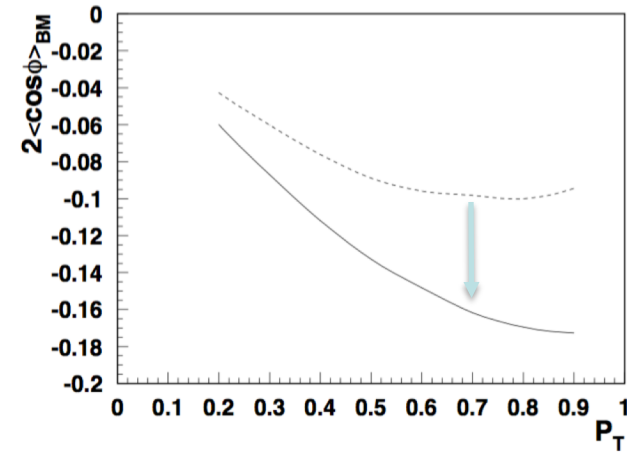
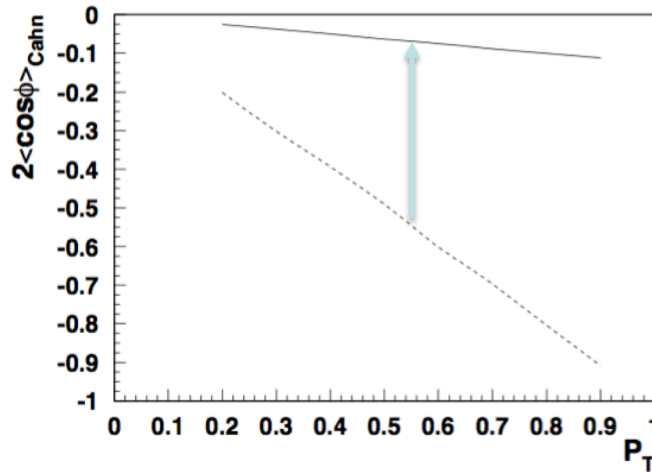
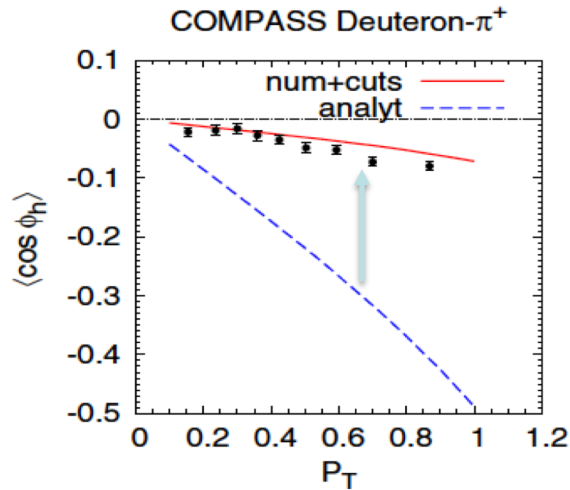
$$\frac{d^5 \sigma^{\ell p \rightarrow \ell h X}}{dx_B dQ^2 dz_h d^2 \mathbf{P}_T} \simeq \sum_q \frac{2\pi\alpha^2 e_q^2}{Q^4} f_q(x_B) D_q^h(z_h) \left[ (1 + (1-y)^2) - 4 \frac{(2-y)\sqrt{1-y} \langle k_\perp^2 \rangle z_h P_T}{\langle P_T^2 \rangle Q} \cos \phi_h \right] \frac{1}{\pi \langle P_T^2 \rangle} e^{-P_T^2 / \langle P_T^2 \rangle},$$

Cahn effect, within assumptions can be the most sensitive observable for intrinsic  $k_T$

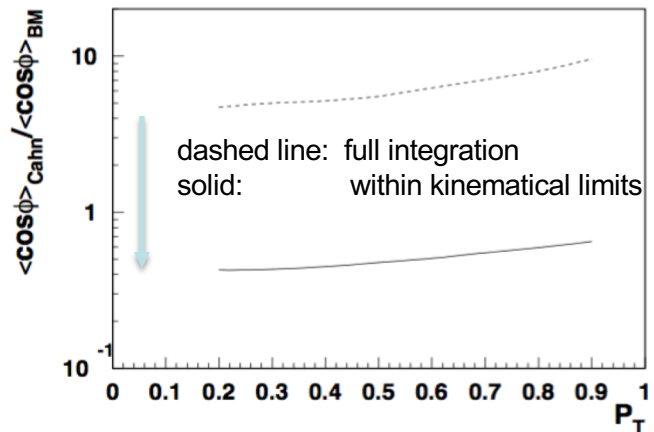
# $k_T$ -max: Effect on BM vs Cahn

M. Boglione, S. Melis & A. Prokudin  
 Phys. Rev. D 84, 034033 2011

## EVA tests from JLAB: Cahn & BM



$$C[w, fD] = x \sum_a e_a^2 \int d^2 p_{\perp} d^2 k_{\perp} \delta^{(2)}(z k_{\perp} + p_{\perp} - P_{h\perp}) w(k_{\perp}, p_{\perp}) f^a(x, k_{\perp}^2) D^a(z, p_{\perp}^2)$$



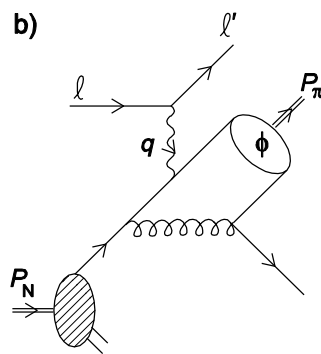
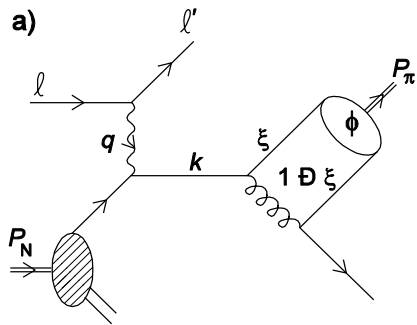
$$F_{UU}^{\cos \phi_h} = \frac{2M}{Q} C \left[ \frac{\hat{h} \cdot p_{\perp}}{zM_h} \frac{k_{\perp}^2}{M^2} h_1^{\perp} H_1^{\perp} - \frac{\hat{h} \cdot k_{\perp}}{M} z f_1 D_1 \right]$$

BM contribution seem to be less sensitive to phase space limitations  
 PRELIMINARY: Need cross checks.

# Azimuthal Asymmetries in semi-exclusive limit

• *Phys.Lett.B* 347 (1995) 413-418

- Higher twists (Berger 1980, Brandenburg et al 1995)  $z \rightarrow 1$   
dominant contribution  $u + e^- \rightarrow e^- \pi^+ d$



$$H_1 = \mathcal{N} \frac{1}{2x_B} \left( [I_2(z, p_T/Q)]^2 + \frac{p_T^4}{Q^4} [I_1(z, p_T/Q)]^2 \right),$$

$$H_2 = \mathcal{N} \left( [I_2(z, p_T/Q)]^2 + 4 \frac{p_T^2}{Q^2} z^2 [I_1(z, p_T/Q)]^2 + \frac{p_T^4}{Q^4} [I_1(z, p_T/Q)]^2 \right)$$

$$I_1(z, p_T/Q) = z \int_0^1 d\xi \frac{\phi(\xi)}{z - \xi(z^2 - p_T^2/Q^2)},$$

$$I_2(z, p_T/Q) = \int_0^1 d\xi \frac{\phi(\xi)}{1 - \xi} - z^2 I_1(z, p_T/Q)$$

$$\frac{Q^2 d\sigma}{dx_B dy dz dp_T^2 d\varphi} = \frac{4\pi\alpha^2 ME}{Q^2} \left( x_B y^2 H_1 + (1 - y) H_2 \right.$$

$$\left. + \frac{p_T}{Q} (2 - y) \sqrt{1 - y} H_3 \cos \varphi + \frac{p_T^2}{Q^2} (1 - y) H_4 \cos 2\varphi \right)$$

Significant contributions at large  $z$  and  $P_T$  also for  $H_1/F_{UU}$

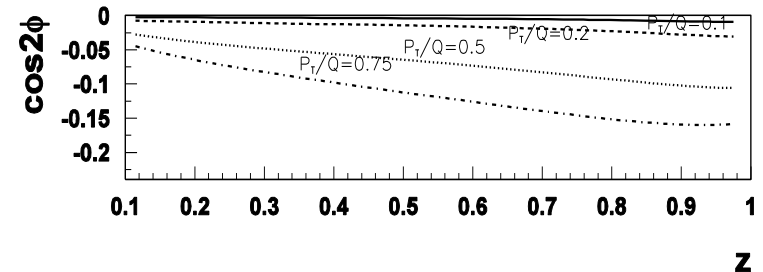
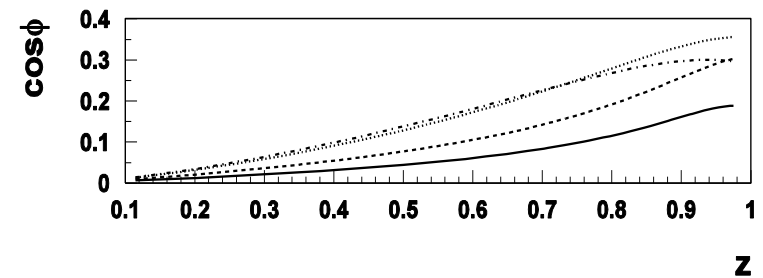
$$F_{UU,T} = 2xH_1$$

# Azimuthal Asymmetries in semi-exclusive limit

- Higher twists (Berger 1980, Brandenburg et al 1995)
- $z \rightarrow 1$  dominant contribution  $u + e^- \rightarrow e^- \pi^+ / \rho^0 d/u$

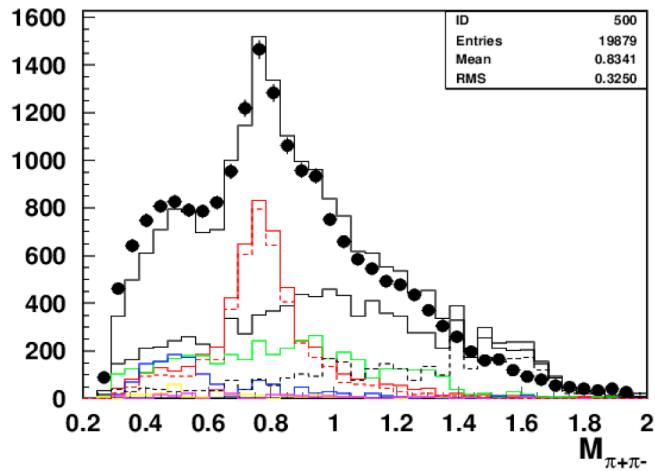
$$\langle \cos \varphi \rangle = \frac{1}{2} \frac{p_T}{Q} \frac{(2-y)\sqrt{1-y} H_3}{x_B y^2 H_1 + (1-y) H_2},$$

$$\langle \cos 2\varphi \rangle = \frac{1}{2} \frac{p_T^2}{Q^2} \frac{(1-y) H_4}{x_B y^2 H_1 + (1-y) H_2}$$



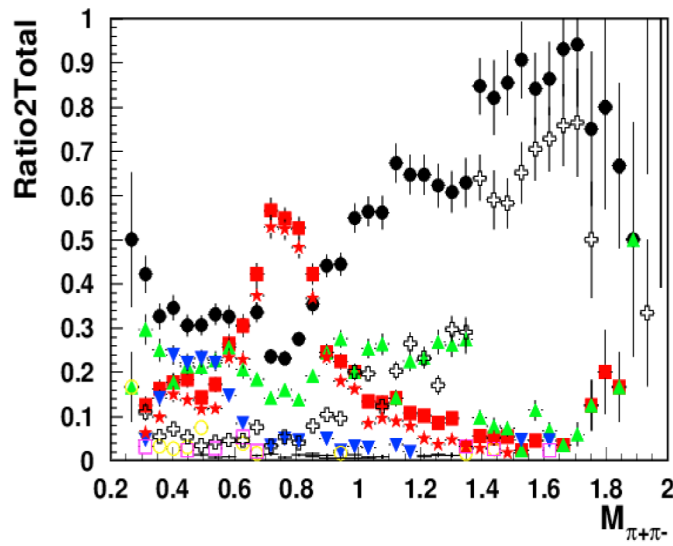
- Semi-exclusive production of pions and even more for VMs will be crucial to understand**
- Dominant contribution to meson wave function is the perturbative one gluon exchange and approach is valid at factor  $\sim 3$  lower  $Q^2$  than in case of hard exclusive scattering (Afanasev & Carlson 1997)

# Azimuthal modulations in SIDIS: decay pions



Significant fraction of pions are from VM decays.

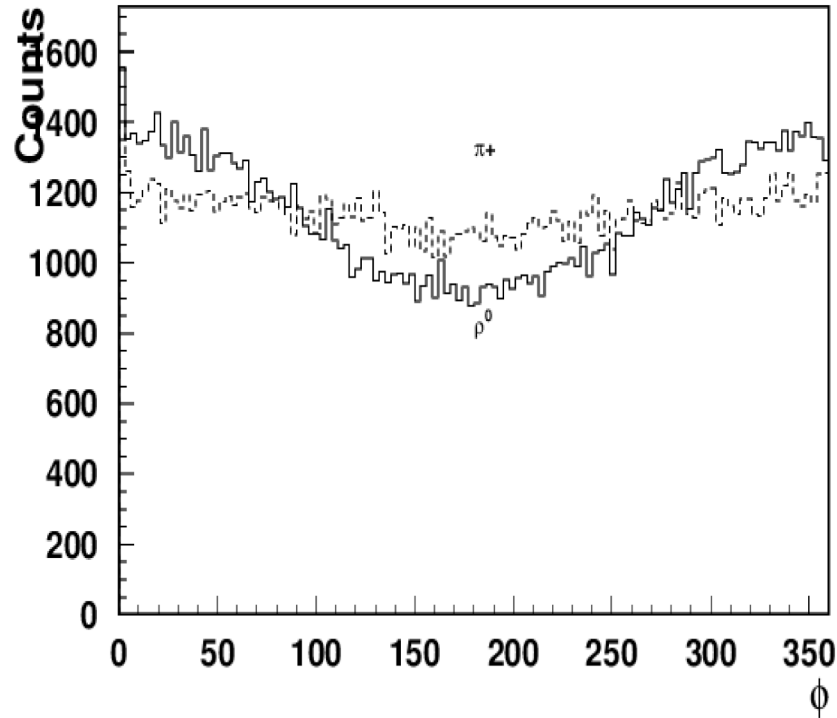
VM decays dominates the low PT region and shows steeper PT distributions.



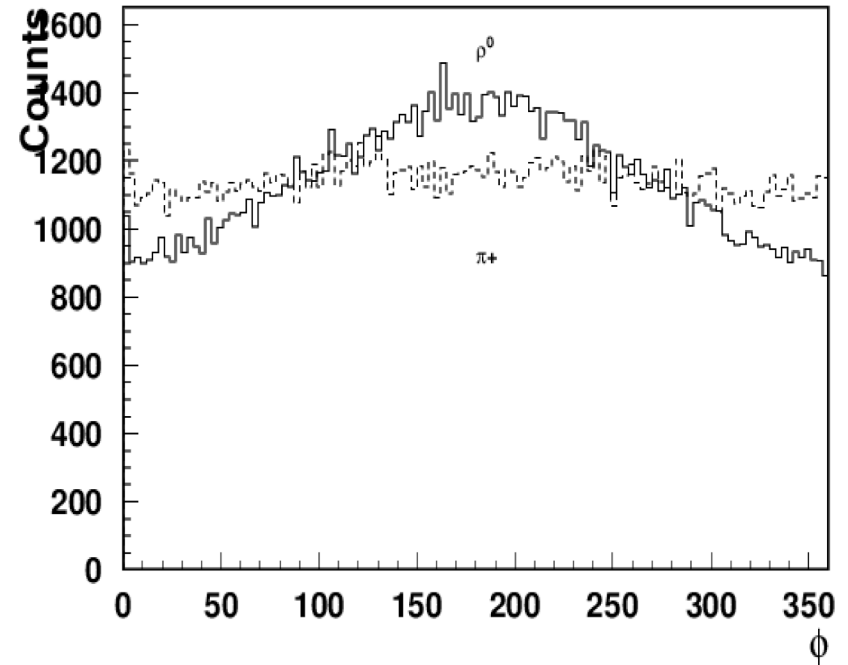
What is the impact on azimuthal distributions?

# Azimuthal Asymmetries: impact of rho

## Berger HT for rho



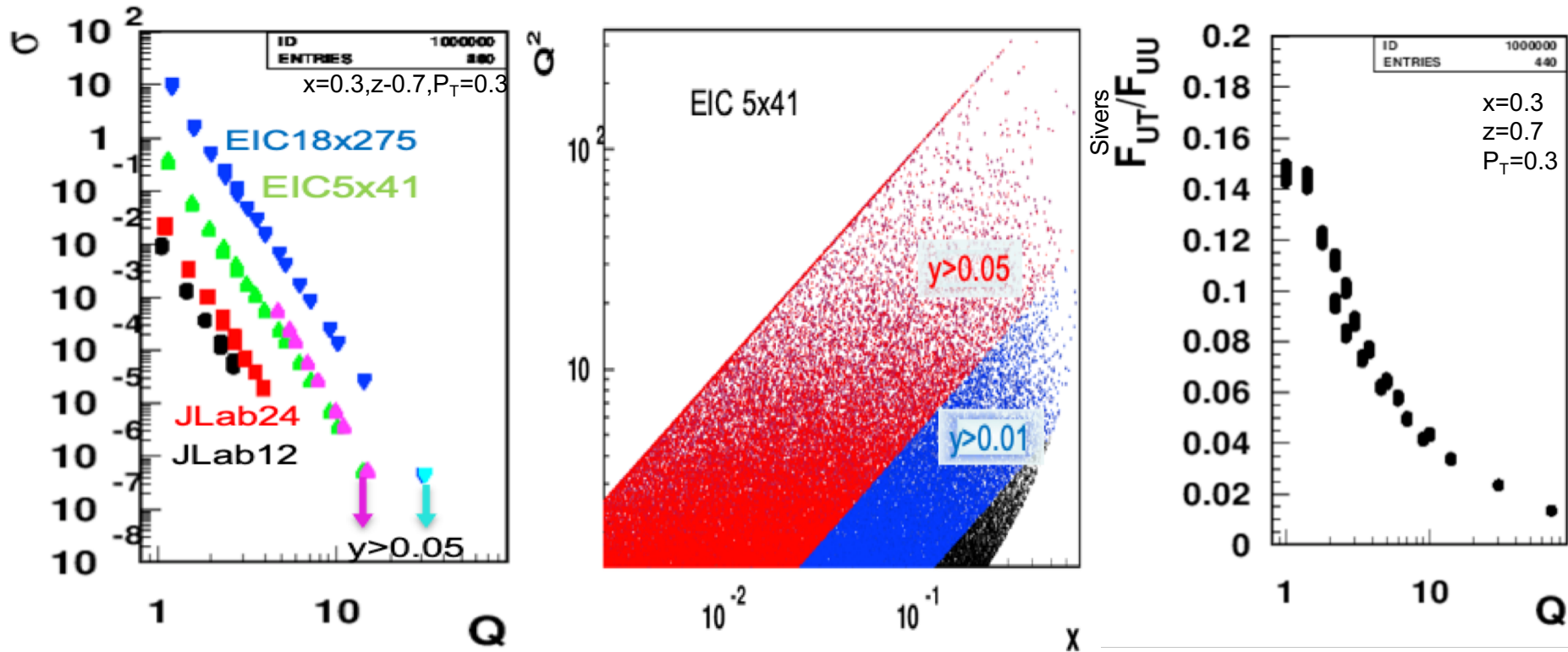
## Cahn HT for rho



- For the  $0.2 < z < 0.4$ ,  $P_T < 0.5$  there will be a significant dilution in azimuthal modulations for decay pions.



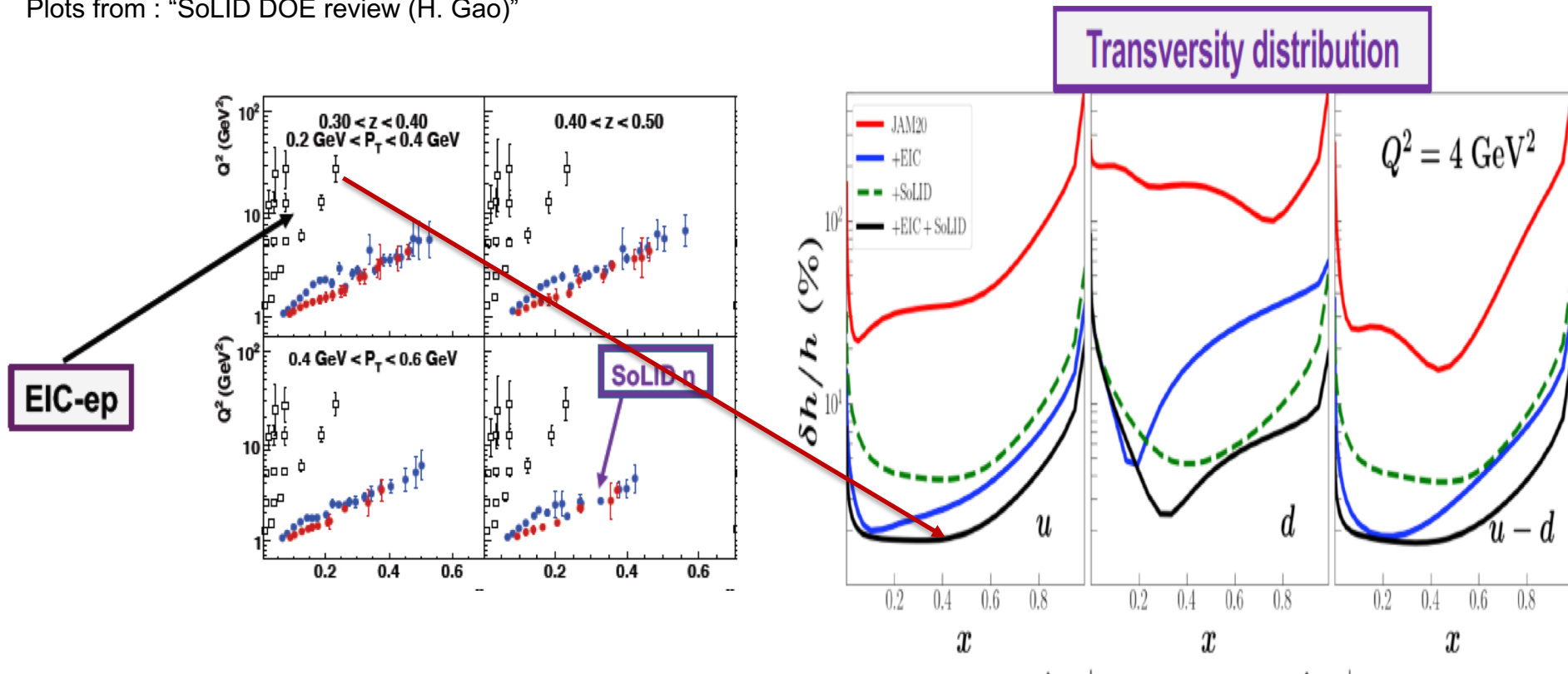
# From JLab to EIC: complementarity



- Understanding of  $Q^2$ -dependence of multiplicities crucial for interpretation
- Proper evaluation of systematics, will require definition of fiducial kinematics
- JLab at 24 GeV will provide critical input in evolution studies of TMDs
- Higher  $Q^2$ -coverage of “Low  $s$ ” EIC running will provide validation of evolution studies at JLab at large  $x$

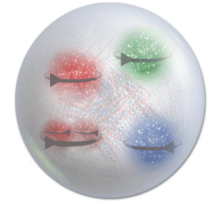
# TMDs sensitivity to transversity: large x

Plots from : “SoLID DOE review (H. Gao)”



- SOLID measurements with transversely polarized targets will provide crucial input at large x
- Complementarity of JLab and EIC at large x should be carefully examined for better coordination

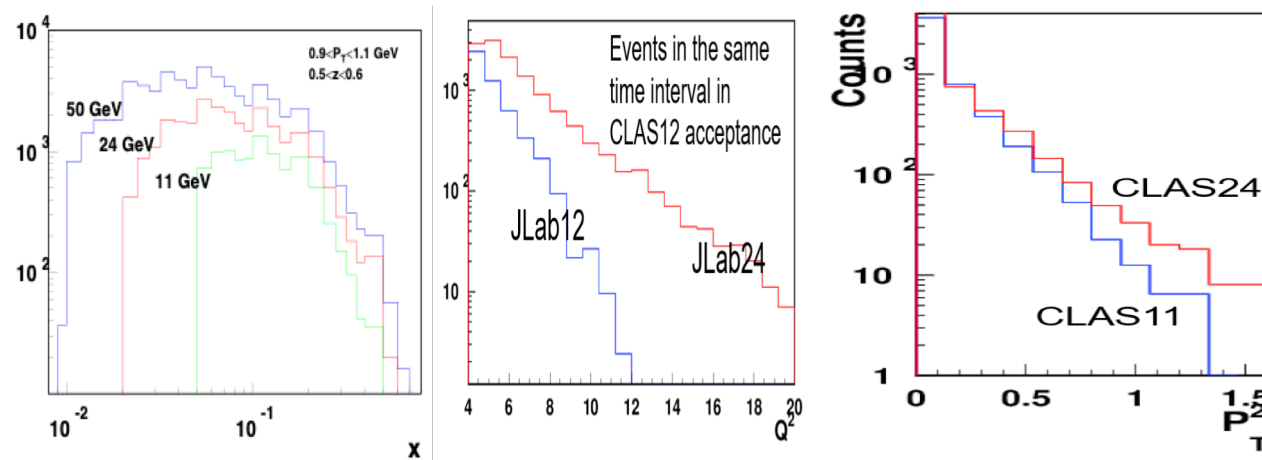
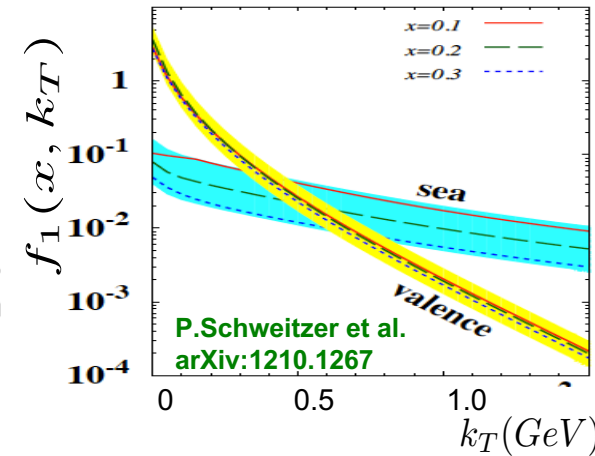
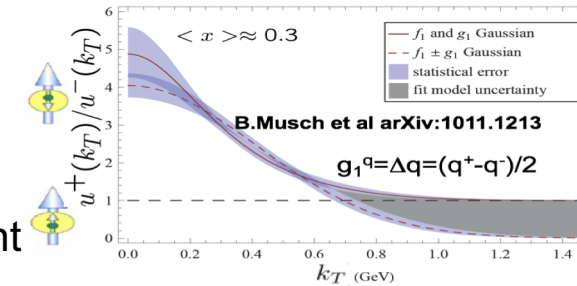
# Extending to small x, large Q2 and large P<sub>T</sub>



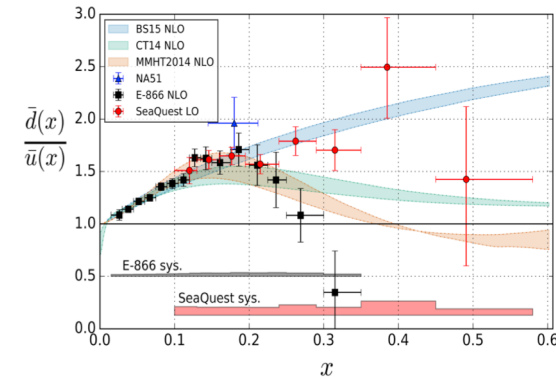
Non-perturbative sea (“tornado”) in nucleon is a key to understand the nucleon structure

$$\bar{d} > \bar{u}$$

- Spin and momentum of struck quarks are correlated with remnant
- Correlations of spins of q-q-bar with valence quark spin and transverse momentum will lead to observable effects
- Spin-Orbit correlations so far were shown (measurements and model calculations) to be significant in the region where non-perturbative effects dominate



Upgrade to 24 GeV will qualitatively increase the JLab phase space, opening access to large P<sub>T</sub>, high Q<sup>2</sup> and low x (sea) region



# Summary

Measurements of dihadron multiplicities and asymmetries provide qualitatively new possibilities for understanding the structure of the nucleon and the process of hadronization, allowing experimental studies of the fractions and distributions of pions coming from vector meson decays. CLAS12 provides high statistical multidimensional measurements.

Extraction of multiplicities and spin-azimuthal asymmetries in multidimensional space is critical for interpretation of results and understanding of the systematics of TMD extractions

The extraction of universal 3D PDFs requires a clear understanding of the impact of the phase space in polarized electroproduction experiments, especially at JLab.

Understanding contributions from VM (with stronger phase space dependence) will be important to understand the systematics of TMD extraction and maybe provide a possible explanation for the single hadron  $P_T$  distribution.

Upgrade to 24 GeV will qualitatively increase the JLab phase space, opening access to large  $P_T$ , high  $Q^2$  and low  $x$  (sea) region