

# Gluon TMDs in Quarkonium Production in SIDIS

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# TMDs

Mulders and Rodrigues PRD 63 094021(2001)

## Quark correlator

$$\Phi_{ij}(x, k) = \int \frac{d^4\xi}{(2\pi)^4} e^{ik \cdot \xi} \langle P | \bar{\Psi}_j(0) W[0, \xi] \Psi_i(\xi) | P \rangle$$

Quark field

## Gluon correlator

$$\Phi_g^{\mu\nu;\rho\sigma}(x, k) = \int \frac{d^4\xi}{(2\pi)^4} e^{ik \cdot \xi} \langle P | \text{Tr}[F^{\mu\nu}(\xi) W[\xi, 0] F^{\rho\sigma}(0) W[0, \xi]] | P \rangle$$

Gluon field

Wilson line

quark pol.

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

nucleon pol.

gluon pol.

	U	Circularly	Linearly
U	$f_1^g$		$h_{1L}^{\perp g}$
L		$g_{1L}^g$	$h_{1L}^{\perp g}$
T	$f_{1T}^{\perp g}$	$g_{1T}^g$	$h_1^g, h_{1T}^{\perp g}$

nucleon pol.

**U**: Unpolarized, **L**: Longitudinally, **T**: Transverse

# Quark Sivers TMDs

- **GPM** : Quark Sivers function (QSF) extracted using latest SIDIS data from HERMES, COMPASS and JLab experiments in pion and kaon production

M. Anselmino, M. Boglione, U. D'Alesio, F. Murgia and A. Prokudin, JHEP 04 (2017) 046

M. Boglione, U. D'Alesio, C. Flore and G. Hernandez, JHEP 2018

M. Boglione, U. D'Alesio, C. Flore, G. Hernandez, F. Murgia and A. Prokudin, PLB 815(2021)

see talk by Carlo. F

- **TMD Evolution**: QSF has been extracted by using SIDIS, DY and  $W^\pm$  /Z-boson data

Global fit @ NNLL:

M.G. Echevarria, Z.B. Kang and J.Terry JHEP01(2021)126

Global fit @ NNNLO:

M. Bury, A. Prokudin, A. Vladimirov JHEP 05 (2021) 151, PRL 126, 112002 (2021)

Global fit @ NLL:

A. Bacchetta, F.Delcarro, C.Pisano, M.Radici and A. Signori JHEP06 (2017) 081

A.Bacchetta, F.Delcarro, C.Pisano and M.Radici arXiv:2004.14278

QSF is established very well but not the gluon Sivers function

# What about Gluon Sivers TMD?

- Gluon Sivers function (GSF) is not known fully

U. D'Alesio, F. Murgia, and C. Pisano, JHEP 09 (2015) 119

- GSF has been extracted from mid rapidity  $pp^\uparrow \rightarrow \pi^0 + X$
- First moment of the GSF has been extracted using mid rapidity  $pp^\uparrow \rightarrow \pi^0 + X$  and  $pp^\uparrow \rightarrow D^0 + X$  data at RHIC

U. D'Alesio, C. Flore, F. Murgia, C. Pisano and P. Tael, PRD 99 (2019) 036013

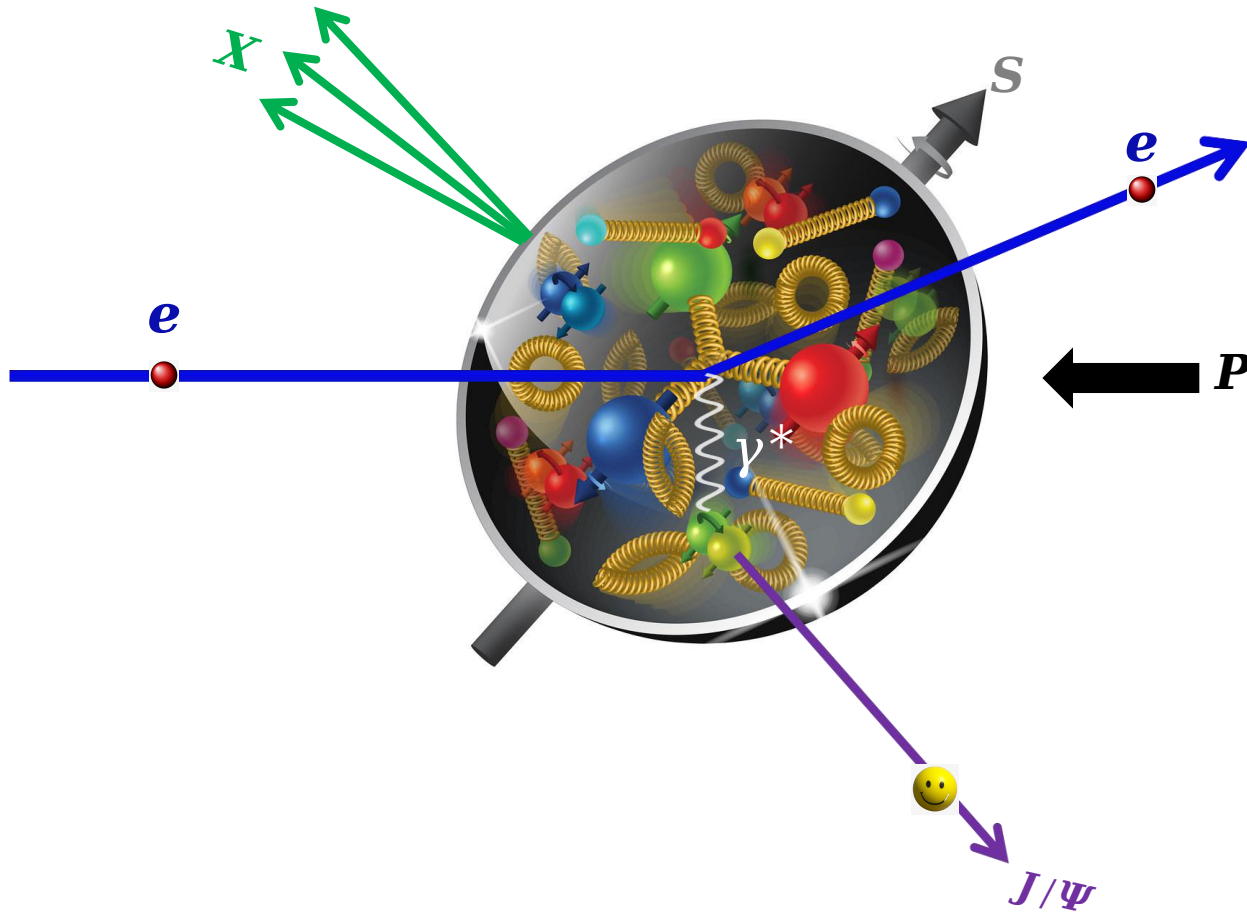
- Due to the limited data, GSF could not be constrained over the wide range in  $x$  and  $K_\perp$
- EIC could play vital role in shaping the GSF
- The  $ep^\uparrow \rightarrow e + J/\psi + X$  process has been studied at  $z = 1$

A. Mukherjee and SR EPJC 77 (2017) 12, 854

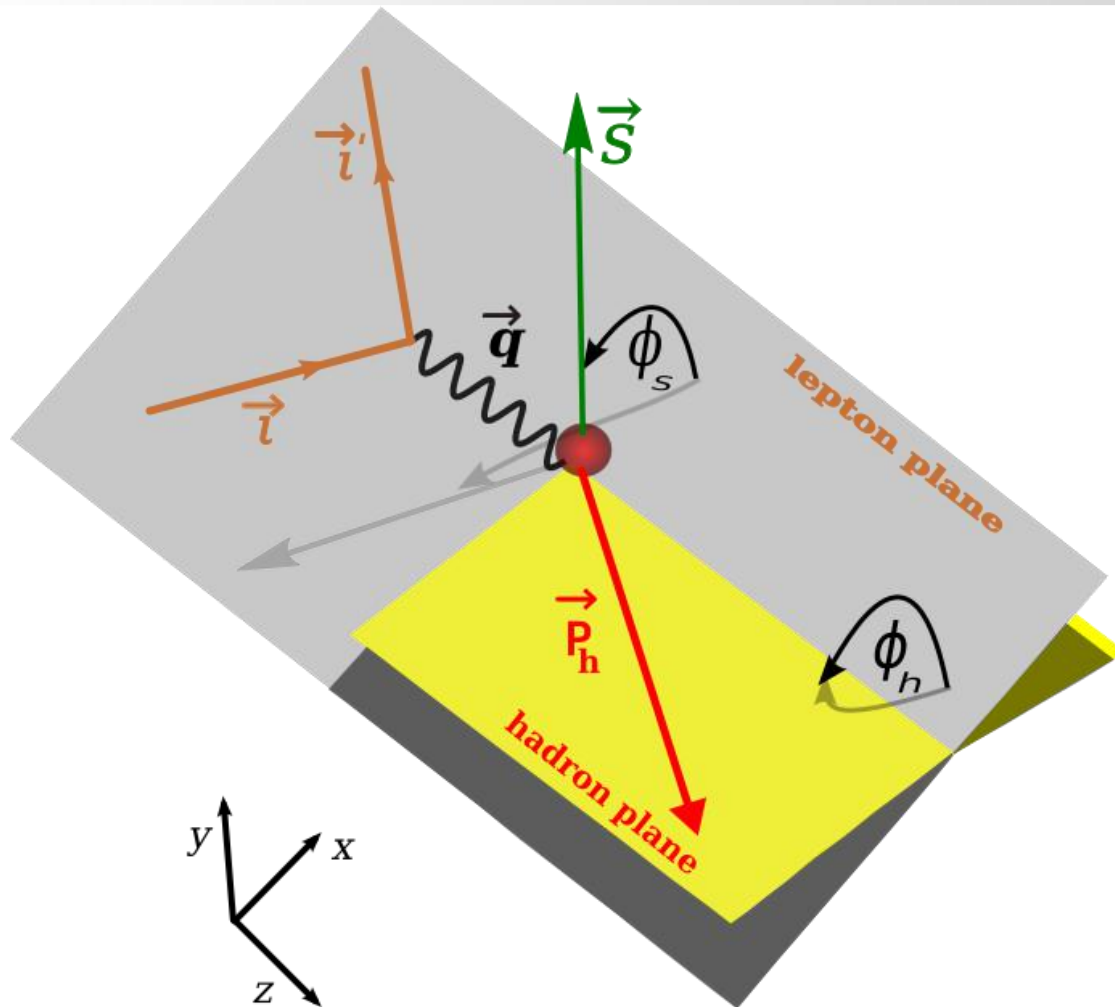
A. Bacchetta, D. Boer, C. Pisano and P. Tael EPJC 80 (2020) 1, 72

- We propose the inelastic leptonproduction of  $J/\psi$  at EIC for probing the poorly known GSF in the region  $z < 1$

$$e + P^\uparrow \rightarrow e + J/\psi + X \text{ at EIC}$$



$$e + P^\uparrow \rightarrow e + J/\psi + X$$



$$s = (P + l)^2 = 2P.l$$

$$-q^2 = Q^2$$

$$x_B = \frac{Q^2}{2P.q}$$

$$y = \frac{P.q}{P.l}$$

$$z = P.P_h/P.q$$

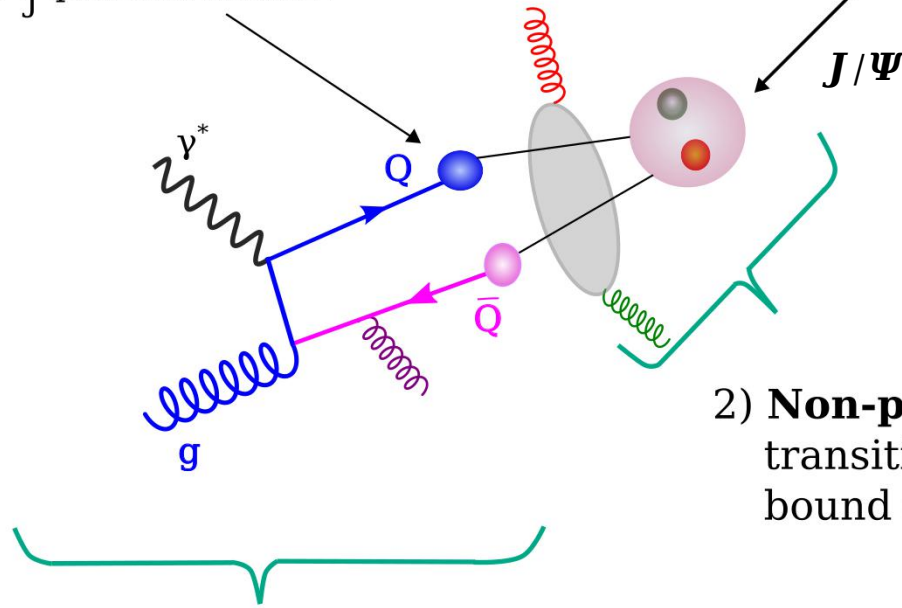
- We consider a frame in which the proton and virtual photon are moving along -z and +z axes respectively

# J/ψ as a probe for Gluon TMDs

- **Color Singlet Model (CSM)**

Baier and R. Ruckl, Z.Phys.C 19 (1983) 251

$Q\bar{Q}$  pair with possible  
 $2S+1L_J$  quantum number



1) **Perturbative** part

- **Color Evaporation Model (CEM)**

H. Fritzsche, PL 67B (1977) 217-221

Quarkonium

$J/\psi$

see talk by Jean-Philippe. L

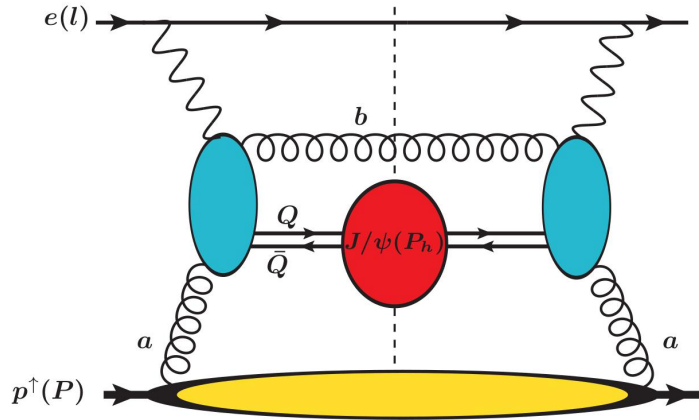
2) **Non-perturbative**  
transition to the  
bound state

- **Non-Relativistic QCD (NRQCD)**

$$d\sigma^{ab \rightarrow J/\psi} = \sum_n d\hat{\sigma}_n [ab \rightarrow c\bar{c}(n)] \langle 0 | \mathcal{O}_n^{J/\psi} | 0 \rangle$$

G. T. Bodwin et al, PRD51 (1995)

# Generalized Parton Model (GPM)



- Inclusion of intrinsic transverse momentum and spin effects in a natural way
- Assumed TMD factorization
- Gaussian ansatz for TMD parametrization

Unpolarized cross section:  $ep \rightarrow e + J/\Psi + X$  in GPM

$$\frac{d\sigma}{dQ^2 dy d^2\mathbf{P}_T dz} = \frac{1}{2S} \frac{2}{(4\pi)^4 z} \sum_a \int \frac{dx_a}{x_a} d^2\mathbf{k}_{\perp a} \delta(\hat{s} + \hat{t} + \hat{u} - M^2 + Q^2) \times \sum_n \frac{1}{Q^4} f_{a/p}(x_a, k_{\perp a}) L^{\mu\nu} H_{\mu\nu}^{a,U}[n] \langle 0 | \mathcal{O}^{J/\psi}(n) | 0 \rangle,$$

Leptonic tensor

$$L^{\mu\nu} = 8\pi\alpha Q^2 \left( -g^{\mu\nu} + \frac{2}{Q^2} (l^\mu l'^\nu + l'^\mu l^\nu) \right) \\ = 8\pi\alpha Q^2 \left( -g^{\mu\nu} + \frac{(2-y)^2}{y^2} \frac{4x_B^2}{Q^2} P^\mu P^\nu + \frac{(2-y)\sqrt{1-y}}{y^2} \frac{8x_B}{Q} \frac{P^\mu \hat{l}_\perp^\nu + P^\nu \hat{l}_\perp^\mu}{2} + 4 \frac{1-y}{y^2} \hat{l}_\perp^\mu \hat{l}_\perp^\nu \right)$$

Hard part  
 $q^\mu H_{\mu\nu}^{a,U}[n] = 0$

NRQCD 8



# unpolarized dsigma

- Two sets of **LDMEs** are considered

M. Butenschoen and B. Kniehl, PRD84 (2008) 051501 (BK11)

P. Sun, C. Yuan and F. Yuan PRD88 (2013) 054008 (SYY13)

Partonic channels @  $\alpha\alpha_s^2$

$$\gamma^* + g \rightarrow J/\Psi + g$$

$$\gamma^* + q(\bar{q}) \rightarrow J/\Psi + q(\bar{q})$$

- Intrinsic charm-quark  $\gamma^* + c(\bar{c}) \rightarrow J/\Psi + c(\bar{c})$  is also considered
- QED diagrams contribution is also included @  $\alpha^3$
- Feed-down contribution:  $\psi(2S)$  included,  $\chi_c$  and b-quark are very small
- $\psi(2S)$  LDMEs are taken from R. Sharma and I. Vitev, PRC 87, 044905 (2013)

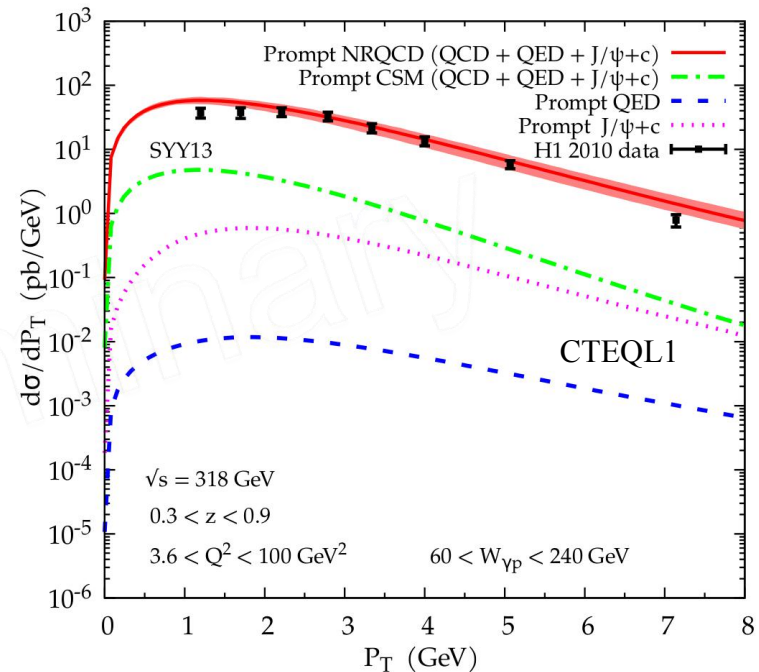
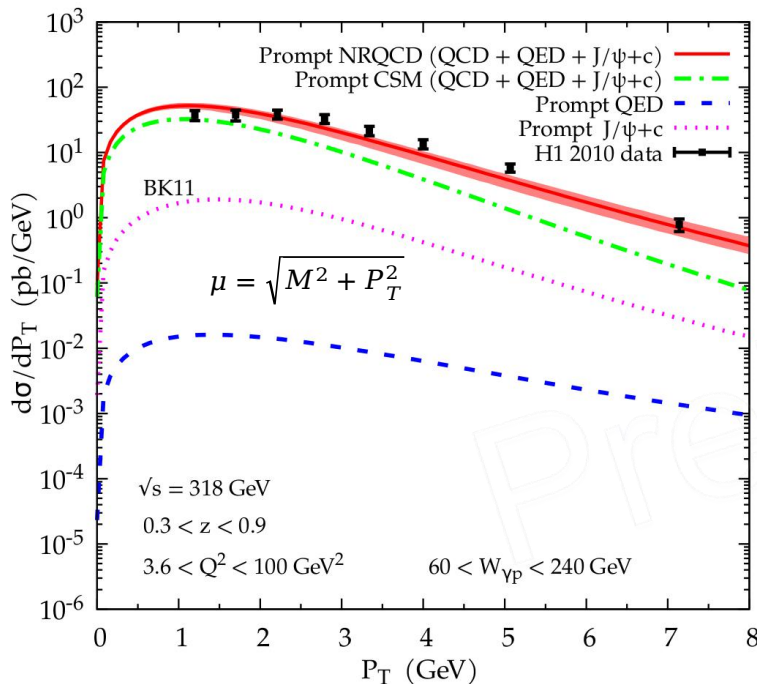
# H1 Unp. dsigma

- Free parameters in our calculation are: Gaussian width and LDMEs

For Quarks:  $\langle k_{\perp}^2 \rangle = 0.25 \text{ GeV}^2$       Gluons:  $\langle k_{\perp}^2 \rangle = 1 \text{ GeV}^2$

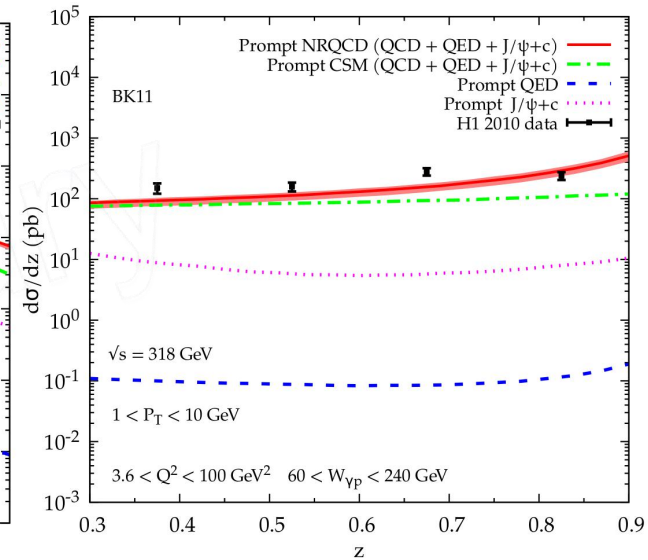
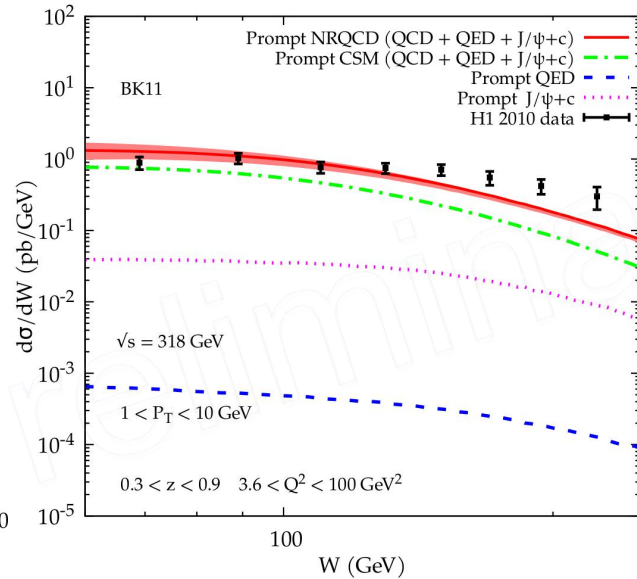
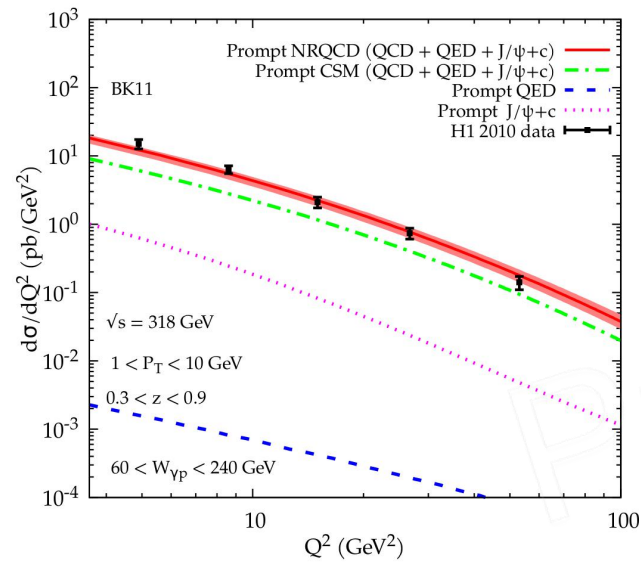
M. Anselmino, M. Boglione, U. D'Alesio, A. Kotzinian, F. Murgia and A. Prokudin PRD 71 (2005) 074006

U. D'Alesio, F. Murgia, C. Pisano and SR, EPJC 79 (2019) 12, 1029



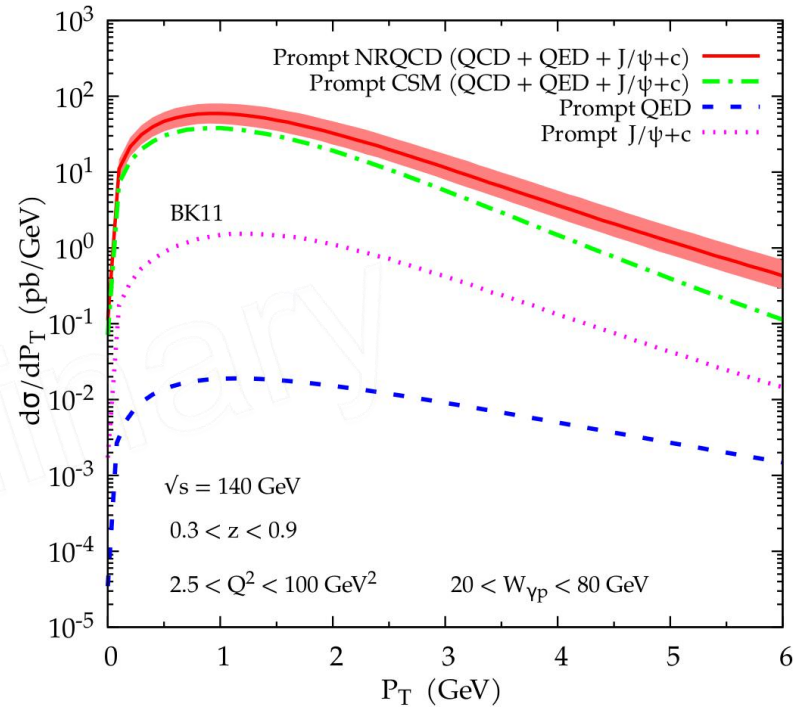
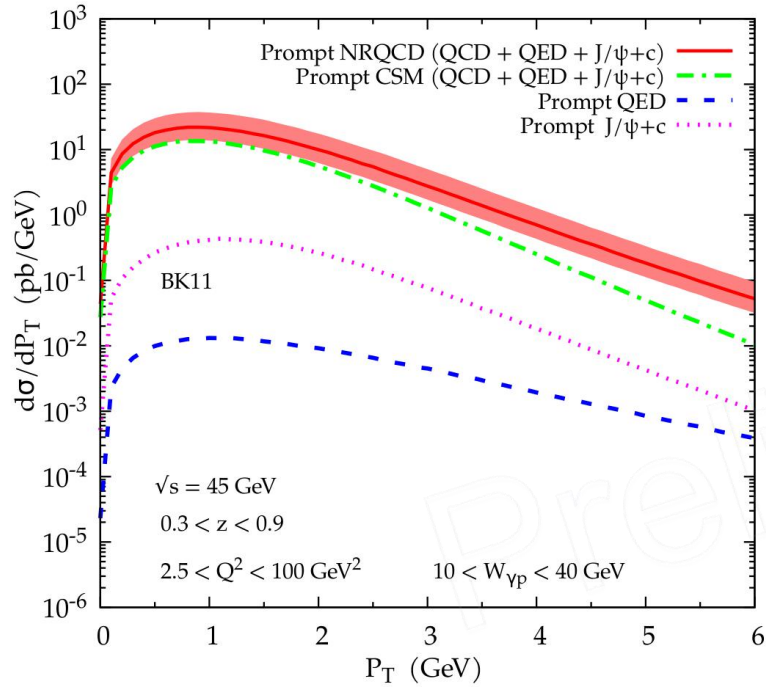
- Data from F.D. Aaron et al (H1), EPJC 68 (2010) 401

# H1 Unp. dsigma



- Data from F.D. Aaron et al (H1), EPJC 68 (2010) 401

# EIC Unp. dsigma



# Sivers Asymmetry

$$A_N^{\sin(\phi_h - \phi_s)} \equiv 2 \frac{\int d\phi_s d\phi_h \sin(\phi_h - \phi_s) (d\sigma^\uparrow - d\sigma^\downarrow)}{\int d\phi_s d\phi_h (d\sigma^\uparrow + d\sigma^\downarrow)} \equiv 2 \frac{\int d\phi_s d\phi_h \sin(\phi_h - \phi_s) d\Delta\sigma(\phi_s, \phi_h)}{\int d\phi_s d\phi_h 2d\sigma}$$

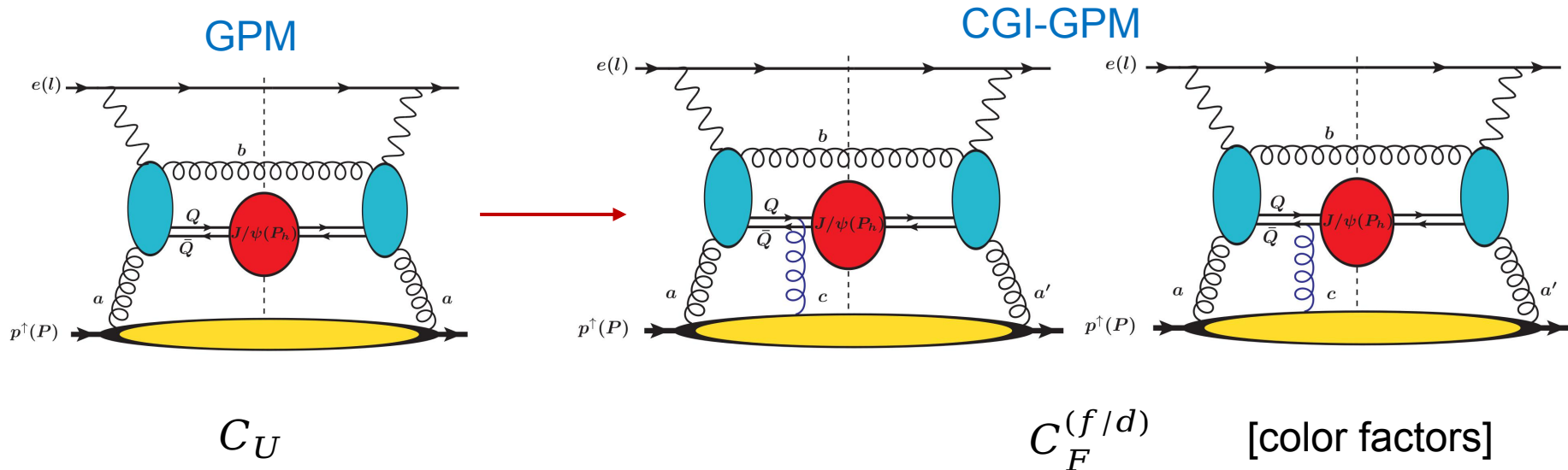
- The denominator is twice the unpolarized differential cross section
- The numerator of the asymmetry is sensitive to the Sivers function

$$d\Delta\sigma^{\text{GPM}} = \frac{1}{2S} \frac{2}{(4\pi)^4 z} \sum_a \int \frac{dx_a}{x_a} d^2\mathbf{k}_{\perp a} \delta(\hat{s} + \hat{t} + \hat{u} - M^2 + Q^2) \left(-2 \frac{k_{\perp a}}{M_p}\right) \sin(\phi_s - \phi_a) \\ \times \sum_n \frac{1}{Q^4} f_{1T}^{\perp a}(x_a, k_{\perp a}) L^{\mu\nu} H_{\mu\nu}^{a,U}[n] \langle 0 | \mathcal{O}^{J/\psi}(n) | 0 \rangle.$$

- In **GPM**: 1 QSF and 1 GSF (universal, process independent)
- In **CGI-GPM**: 1 QSF and 2 GSFs (universal but process dependent)

$$d\Delta\sigma^{\text{CGI-GPM}} = \frac{1}{2S} \frac{2}{(4\pi)^4 z} \int \frac{dx_a}{x_a} d^2\mathbf{k}_{\perp a} \delta(\hat{s} + \hat{t} + \hat{u} - M^2 + Q^2) \left(-2 \frac{k_{\perp a}}{M_p}\right) \sin(\phi_s - \phi_a) \\ \times \sum_n \frac{1}{Q^4} L^{\mu\nu} \left\{ \sum_q f_{1T}^{\perp q}(x_a, k_{\perp a}) H_{\mu\nu}^{q,\text{Inc}}[n] + \sum_{m=f,d} f_{1T}^{\perp g}(x_a, k_{\perp a}) H_{\mu\nu}^{g,\text{Inc}(m)}[n] \right\} \langle 0 | \mathcal{O}^{J/\psi}(n) | 0 \rangle$$

# CGI-GPM



- The new color factors are shifted to hard part

$$H^{Inc(f/d)} \equiv \frac{C_I^{(f/d)} + C_F^{(f/d)}}{C_U} H^U$$

- Two independent  $f_{1T}^\perp(f/d)$  which are process dependent

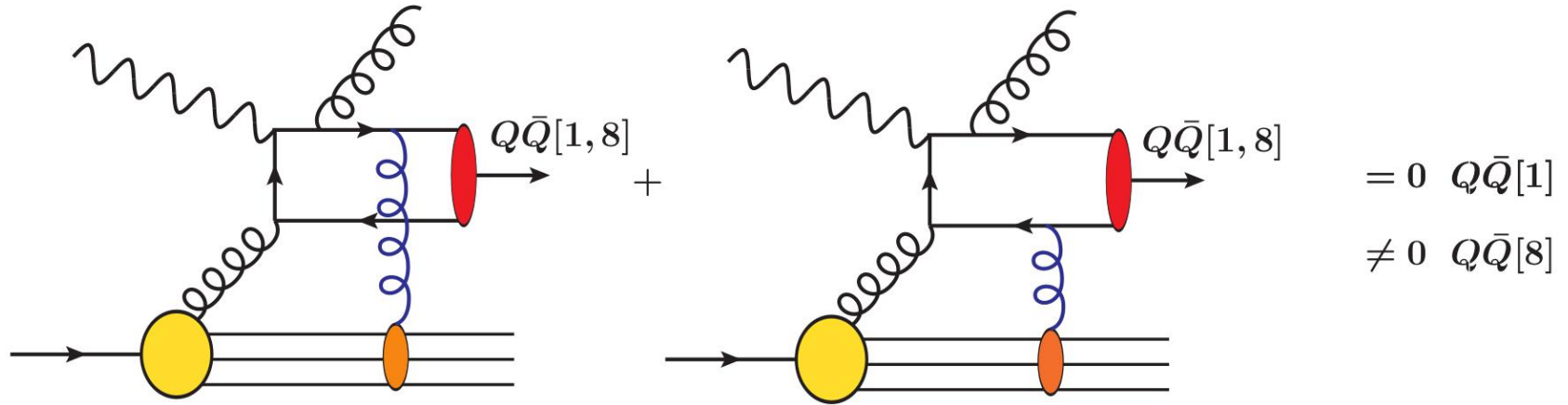
$$[\text{GPM}] f_{1T}^\perp H^U \longrightarrow f_{1T}^\perp{}^f H^{Inc(f)} + f_{1T}^\perp{}^d H^{Inc(d)} \quad [\text{CGI-GPM}]$$

L. Gamberg and Z. B. Kang, PLB 696 (2011)

U. D'Alesio, L. Maxia, F. Murgia, C. Pisano and SR, PRD 102 (2020)

- No initial state interactions due to colorless photon  $C_I^{(f/d)} = 0$

# CGI-GPM



- CS state does not contribute to asymmetry
- Only CO states contribute to asymmetry

$$\gamma^* q(\bar{q}) \rightarrow Q\bar{Q} \left[ {}^{2S+1}L_J^{(1,8)} \right] + q(\bar{q})$$

$$\gamma^* g \rightarrow Q\bar{Q} \left[ {}^{2S+1}L_J^{(1,8)} \right] + g$$

State	$C_U$	$C_F$	$\frac{C_F}{C_U}$
${}^3S_1^{(8)}, {}^1S_0^{(8)} \& {}^3P_J^{(8)}$	$\frac{N_c^2-1}{4N_c}$	$\frac{N_c}{4}$	$\frac{N_c^2}{N_c^2-1}$

State	$C_U$	$C_F^{(f)}$	$C_F^{(d)}$	$\frac{C_F^{(f)}}{C_U}$	$\frac{C_F^{(d)}}{C_U}$
${}^1S_0^{(8)} \& {}^3P_J^{(8)}$	$\frac{N_c}{2}$	$\frac{N_c}{4}$	0	$\frac{1}{2}$	0
${}^3S_1^{(8)}$	$\frac{N_c^2-4}{2N_c}$	$\frac{N_c^2-4}{4N_c}$	0	$\frac{1}{2}$	0
${}^3S_1^{(1)}$	$\frac{1}{4N_c}$	0	0	0	0

- $d$ -type GSF is zero due to  $C_F^{(d)} = 0$

# TMDs Parametrization

- Parametrization of TMDs within GPM: Gaussian ansatz

- Unp. TMD 
$$f(x_a, \mathbf{k}_{\perp a}^2, \mu) = f(x_a, \mu) \frac{1}{\pi \langle k_{\perp a}^2 \rangle} e^{-\mathbf{k}_{\perp a}^2 / \langle k_{\perp a}^2 \rangle}$$

- Sivers TMD 
$$\Delta^N f_{a/p\uparrow}(x_a, k_{\perp a}, \mu) = 2\mathcal{N}_a(x_a) f_{a/p}(x_a, \mu) \frac{\sqrt{2}e}{\pi} \sqrt{\frac{1-\rho}{\rho}} k_{\perp g} \frac{e^{-k_{\perp a}^2 / \rho \langle k_{\perp a}^2 \rangle}}{\langle k_{\perp a}^2 \rangle^{3/2}}$$

$$\mathcal{N}_a(x_a) = N_a x_a^\alpha (1 - x_a)^\beta \frac{(\alpha + \beta)^{(\alpha + \beta)}}{\alpha^\alpha \beta^\beta}$$

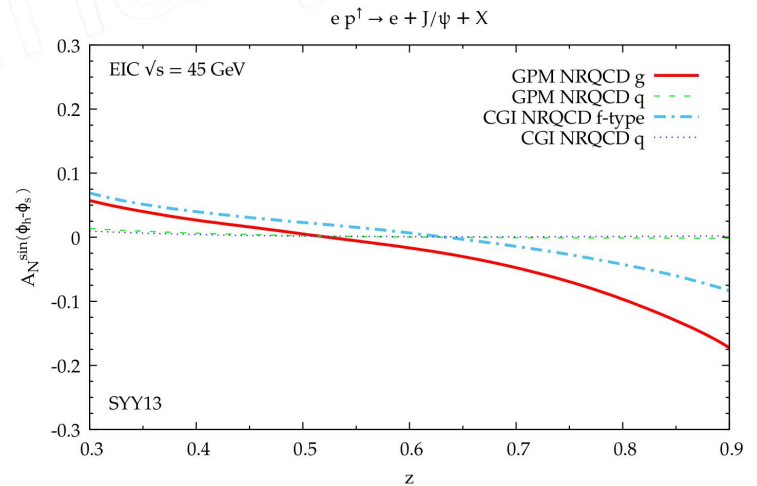
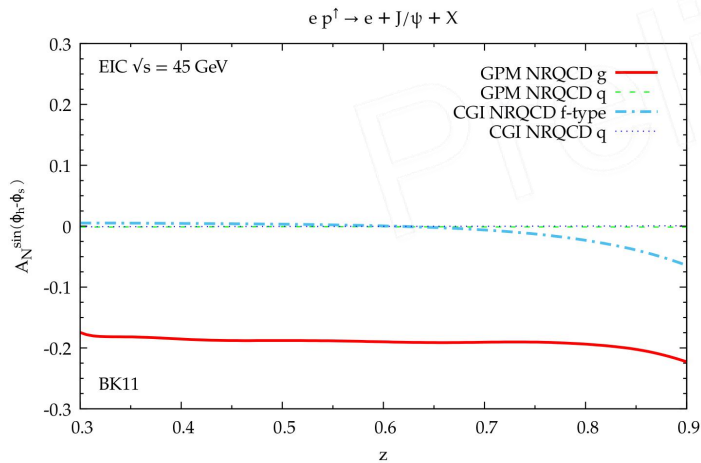
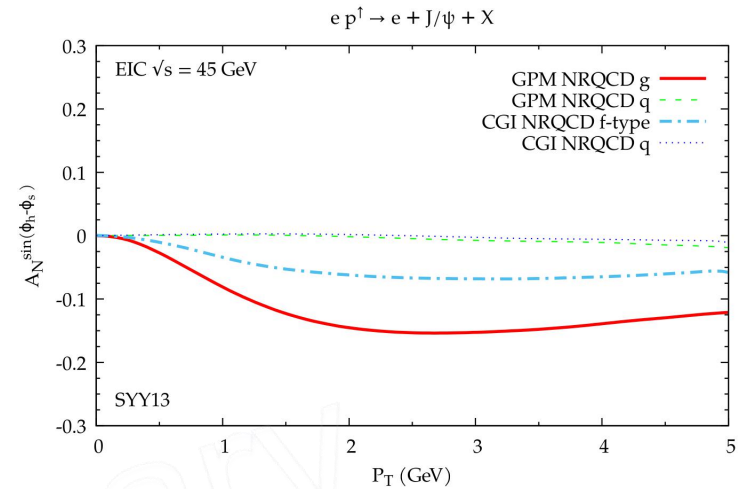
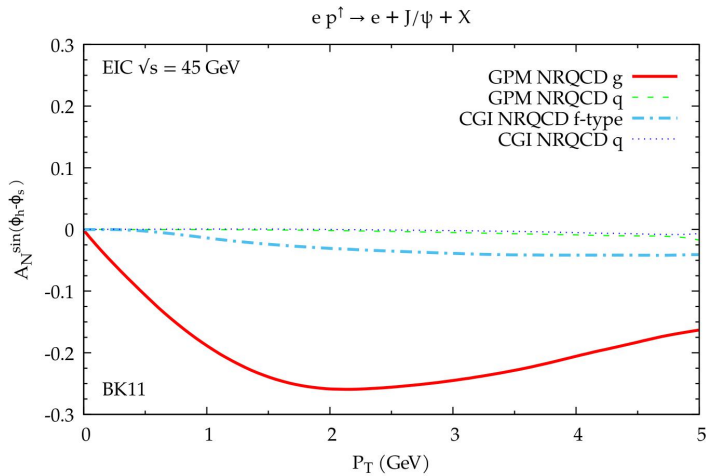
U. D'Alesio, C. Flore, F. Murgia, C. Pisano and P. Tael, PRD 99 (2019) 036013

- For maximized asymmetry: Saturate the Sivers function

$$\rho = 2/3, \mathcal{N}_a(x_a) = +1 \ \& \ \mathcal{N}_g^{(f,d)}(x_g) = +1$$

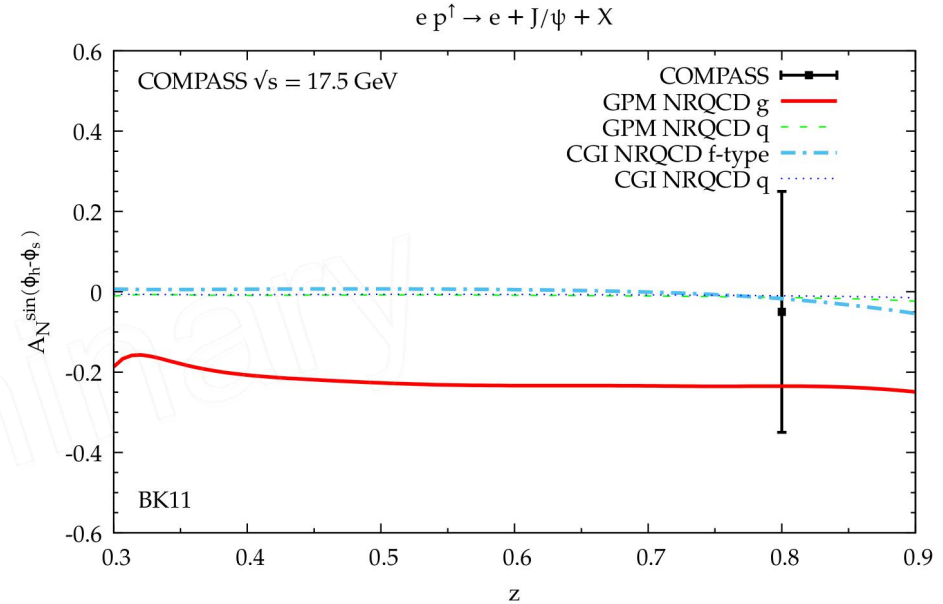
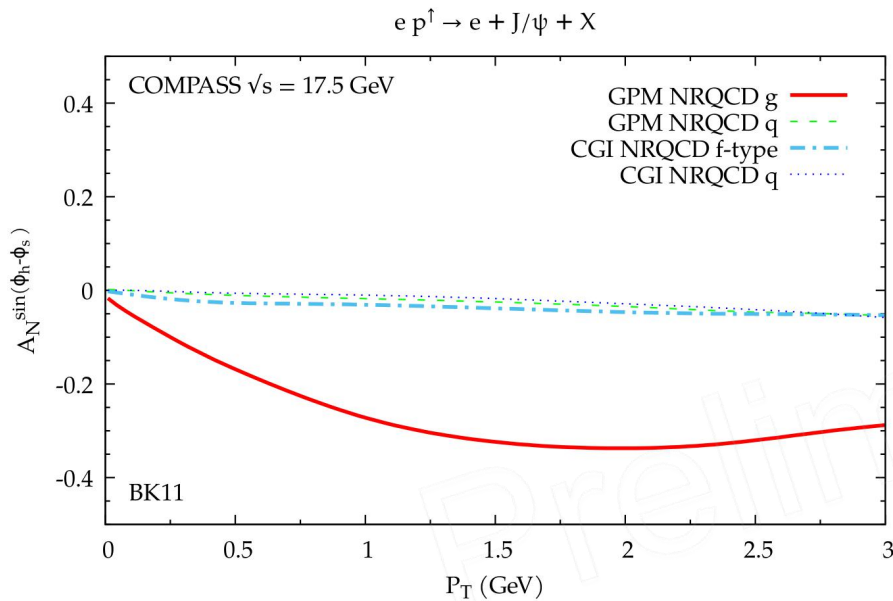


# Sivers Asymmetry at EIC



$\sqrt{s} = 45 \text{ GeV}$    
  $0.3 < z < 0.9$    
  $2.5 < Q^2 < 100 \text{ GeV}^2$    
  $10 < W_{\gamma p} < 40 \text{ GeV}$    
 17

# Sivers Asymmetry at COMPASS



$$\sqrt{s} = 17.5 \text{ GeV} \quad 0.3 < z < 0.9 \quad 0.03 < Q^2 < 20 \text{ GeV}^2 \quad 0.003 < X_B < 0.1$$

- Data from J. Matoušek (COMPASS), J. Phys. Conf. Ser. 678, 012050 (2016)
- Negative GSF has been reported by COMPASS using Monte Carlo simulation

# Summary

- Siverts asymmetry in inelastic lepton production of  $J/\psi$  in  $ep$  collision is studied at EIC
- GPM predicts the sizable Siverts asymmetry, while it is drastically reduced in CGI-GPM
- Hence, quarkonium production in  $ep$  collision is a promising channel to probe the unknown GSF
- Process dependence of GSF:  $ep^\uparrow \rightarrow e + J/\psi + X$  at EIC could be used to probe the  $f$ -type GSF
- Unpolarized cross-section estimation is in good agreement with HERA data in the low  $P_T$  region

Thank you for the attention