#### SUSY Renormalization Group Effects in Ultra High Energy Neutrinos

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## Outline

- Review of Neutrino RGEs
- How to probe Neutrino RGEs
- Theoretical Predictions for Ultra High Energy Neutrinos
- Experimental Prospects

### **Neutrino RGEs**

#### **Neutrino Mass Operator**

**Dimension-5 Mass Operator:** 

$$\mathcal{L}_{\nu} = \frac{1}{4} (\overline{L}_{i}^{c} H) \frac{m_{ij}^{\nu}}{\Lambda_{\nu}} (L_{j} H)$$

#### **Neutrino Mass Operator**

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Neutrino Mass Matrix:

$$\begin{split} M^{\nu}_{ij} &= \frac{1}{4} \frac{m^{\nu}_{ij}}{\Lambda_{\nu}} v^2 \qquad \qquad M^{\nu}_{ij} = \frac{1}{4} \frac{m^{\nu}_{ij}}{\Lambda_{\nu}} v^2 \sin^2 \beta \\ & \text{SM} \qquad \qquad \text{SUSY} \end{split}$$

At one loop, we have:

# $16\pi^2 \frac{dm_{ij}^{\nu}}{dx} = C\left( (Y_e^{\dagger} Y_e)_{ik}^T m_{kj}^{\nu} + m_{ik}^{\nu} (Y_e^{\dagger} Y_e)_{kj} \right) + \alpha \, m_{ij}^{\nu}$

Babu, Leung, Pantaleone (hep-ph/9309223) Antusch, Drees, Kersten, Lindner, Ratz (hep-ph/0108005) Antusch, Drees, Kersten, Lindner, Ratz (hep-ph/0110366)

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$$C = \begin{cases} -\frac{3}{2} \\ 1 \end{cases}$$
  

$$\alpha = \begin{cases} -3g_2^2 + 2\operatorname{Tr}(Y_e^{\dagger}Y_e) + 6\operatorname{Tr}(Y_u^{\dagger}Y_u) + 6\operatorname{Tr}(Y_d^{\dagger}Y_d) + \lambda \\ -\frac{6}{5}g_1^2 - 6g_2^2 + 6\operatorname{Tr}(Y_u^{\dagger}Y_u) \end{cases}$$

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$$\dot{\theta}_{12} = -C \frac{y_{\tau}^2}{32\pi^2} \sin 2\theta_{12} \sin^2 \theta_{23} \frac{\left|m_1 e^{i\phi_1} + m_2 e^{i\phi_2}\right|^2}{\Delta m_{21}^2} + O(\theta_{13})$$

# Mixing Angle RGEs

#### Still at one loop:

$$\dot{\theta}_{12} = -C \frac{(y_{\tau}^2)}{32\pi^2} \sin 2\theta_{12} \sin^2 \theta_{23} \frac{\left|m_1 e^{i\phi_1} + m_2 e^{i\phi_2}\right|^2}{\Delta m_{21}^2} + O(\theta_{13})$$

$$y_{\tau}^{SM} = \sqrt{2} \frac{m_{\tau}}{v}$$
$$y_{\tau}^{SUSY} = \sqrt{2} \frac{m_{\tau}}{v \cos \beta}$$

A large  $tan\beta$  can enhance running

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Large neutrino masses can enhance running

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Large neutrino masses can enhance running

WMAP (7 yr)  $\Sigma m_i < 1.3 \ {
m eV}$  Komatsu *et al* (1001.4538 [hep-ph])

**Full Bounds** 

#### $\Sigma m_i < 0.2 \,\,{ m eV}$ Fogli *et al* (0805.2517 [hep-ph])

$$\dot{\theta}_{12} = -C \frac{y_{\tau}^2}{32\pi^2} \sin 2\theta_{12} \sin^2 \theta_{23} \frac{\left|m_1 e^{\phi_1} + m_2 e^{\phi_2}\right|^2}{\Delta m_{21}^2} + O(\theta_{13})$$

$$m_1^2 + m_2^2 + 2m_1m_2\cos(\phi_1 - \phi_2)$$

Majorana phases can enhance running

$$\dot{\theta}_{12} = -C \frac{y_{\tau}^2}{32\pi^2} \sin 2\theta_{12} \sin^2 \theta_{23} \frac{\left|m_1 e^{i\phi_1} + m_2 e^{i\phi_2}\right|^2}{\Delta m_{21}^2} + O(\theta_{13})$$
  
$$\dot{\theta}_{23} = -C \frac{y_{\tau}^2}{32\pi^2} \sin 2\theta_{23} \left(\cos^2 \theta_{12} \frac{m_2 e^{i\phi_2} + m_3^2}{\Delta m_{32}^2} + \sin^2 \theta_{12} \frac{m_1 e^{i\phi_1} + m_3^2}{\Delta m_{31}^2} + O(\theta_{13})\right)$$
  
$$+O(\theta_{13})$$

$$\begin{aligned} \dot{\theta}_{12} &= -C \frac{y_{\tau}^2}{32\pi^2} \sin 2\theta_{12} \sin^2 \theta_{23} \frac{\left|m_1 e^{i\phi_1} + m_2 e^{i\phi_2}\right|^2}{\Delta m_{21}^2} + O(\theta_{13}) \\ \dot{\theta}_{23} &= -C \frac{y_{\tau}^2}{32\pi^2} \sin 2\theta_{23} \left(\cos^2 \theta_{12} \frac{\left|m_2 e^{i\phi_2} + m_3\right|^2}{\Delta m_{32}^2} + \sin^2 \theta_{12} \frac{\left|m_1 e^{i\phi_1} + m_3\right|^2}{\Delta m_{31}^2}\right) \\ &+ O(\theta_{13}) \\ \dot{\theta}_{13} &= C \frac{y_{\tau}^2}{32\pi^2} \sin 2\theta_{12} \sin 2\theta_{23} \times \\ &\times \left(\frac{m_3 m_1}{\Delta m_{31}^2} \cos \phi_1 - \delta\right) \frac{m_3 m_2}{\Delta m_{32}^2} \cos \phi_2 - \delta \right) \frac{\Delta m_{21}^2}{\Delta m_{32}^2} m_3^2 \sin \delta \right) \\ &+ O(\theta_{13}) \end{aligned}$$

# **Probing Neutrino RGEs**

#### How can we probe RGEs?

- If you talk about RGEs, you are talking about a scale μ.
- To avoid large logarithmic corrections, it is customary to set  $\mu^2 = Q^2$ .

#### How can we probe RGEs?

- If you talk about RGEs, you are talking about a scale μ.
- To avoid large logarithmic corrections, it is customary to set  $\mu^2 = Q^2$ .
- Thus, we need to look for experiments with large Q<sup>2</sup>.
- To get large Q<sup>2</sup>, we need very high energy neutrinos.



#### Credit: ESA/NASA/AVO/Paolo Padovani

#### Active Galactic Nuclei

#### From NASA Webpage:

"AGN - extraordinarily energetic cores of galaxies powered by accreting supermassive black holes. AGN such as quasars, blazars, and Seyfert galaxies are among the most luminous objects in our Universe, often pouring out the energy of billions of stars from a region no larger than our solar system."

#### Stecker *et al*:

(Phys. Rev. Lett. 66, 2697-2700 (1991))

"Collectively, AGN produce the dominant isotropic v background between  $10^4$  and  $10^{10}$  GeV, detectable with current instruments."



#### Credit: Aurore Simonnet, Sonoma State University

















 $\mu = m_{\pi}$  $U_{\nu} = U_{\rm PMNS}$ 

 $\mu \sim 10^4 \text{ GeV}?$  $U_{\nu} \neq U_{\rm PMNS}$ 

$$P_{\alpha\beta}(Q) = \sum_{i=1}^{3} \left| (U_{\nu})_{\alpha i} \right|^{2} \left| (U_{\nu}'(Q))_{\beta i} \right|^{2}$$





### **Transition Probability**



### **Theoretical Predictions**

 $(\nu_e:\nu_\mu:\nu_\tau)$ 







 $(\nu_e:\nu_\mu:\nu_ au)$ 

(1:2:0) Pion + Muon Decay (0:1:0) Pion Decay



 $(\nu_e:\nu_\mu:\nu_\tau)$ 



(1:2:0) Pion + Muon Decay (0:1:0) Pion Decay

(1:0:0) Neutron Decay (1:1:0) Charm Decay





 $T = \frac{\Phi_{\nu_{\mu}+\bar{\nu}_{\mu}}}{\Phi_{\nu_{e}+\bar{\nu}_{e}} + \Phi_{\nu_{\mu}+\bar{\nu}_{\mu}} + \Phi_{\nu_{\tau}+\bar{\nu}_{\tau}}}$ 



$$T = \frac{\Phi_{\nu_{\mu} + \bar{\nu}_{\mu}}}{\Phi_{\nu_{e} + \bar{\nu}_{e}} + \Phi_{\nu_{\mu} + \bar{\nu}_{\mu}} + \Phi_{\nu_{\tau} + \bar{\nu}_{\tau}}}$$

$$(1:2:0) \quad (0:1:0) \quad (1:0:0) \quad (1:1:0)$$

$$0.32 \qquad 0.37 \qquad 0.28 \qquad 0.32$$

$$R = \frac{\Phi_{\nu_e + \bar{\nu}_e}}{\Phi_{\nu_\tau + \bar{\nu}_\tau}}.$$

 $\begin{array}{cccc} (1:2:0) & (0:1:0) & (1:0:0) & (1:1:0) \\ 1.1 & 0.71 & 3.3 & 1.4 \end{array}$ 

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 $\begin{array}{cccc} (1:2:0) & (0:1:0) & (1:0:0) & (1:1:0) \\ 1.1 & 0.71 & 3.3 & 1.4 \end{array}$ 

What happens when one includes RGE effects?

#### Neutron Decay Production (1:0:0)



SMSUSY

#### Pion Decay Production (0:1:0)



SM SUSY



SMSUSY





#### Unknown Production (1:n:0)



# Experimental Prospects (Preliminary)

Neutrino-nucleon interactions are through Deep Inelastic Scattering:

$$\left\langle P_{\alpha\beta}\left(E_{\nu}\right)\right\rangle^{\overleftarrow{\nu}} = \frac{1}{\sigma_{\mathrm{CC}}^{\overleftarrow{\nu}}\left(E_{\nu}\right)} \int_{0}^{1} dx \int_{0}^{1} dy \frac{d^{2}\sigma_{\mathrm{CC}}^{\overleftarrow{\nu}}}{dxdy}\left(E_{\nu}, x, y\right) P_{\alpha\beta}\left(Q^{2}\right)$$

Neutrino-nucleon interactions are through Deep Inelastic Scattering:

$$\langle P_{\alpha\beta} \left( E_{\nu} \right) \rangle^{\widetilde{\nu}} = \frac{1}{\sigma_{\rm CC}^{\widetilde{\nu}} \left( E_{\nu} \right)} \int_{0}^{1} dx \int_{0}^{1} dy \frac{d^{2} \sigma_{\rm CC}^{\widetilde{\nu}}}{dx dy} \left( E_{\nu}, x, y \right) P_{\alpha\beta} \left( Q^{2} \right)$$

$$\text{Bjorken variables}$$

$$\text{Diferential cross-section}$$

Neutrino-nucleon interactions are through Deep Inelastic Scattering:



Transition Probability

Neutrino-nucleon interactions are through Deep Inelastic Scattering:



pdfs prefer low values of Q<sup>2</sup>!

### Step 1: Average Probability Cutoff Q<sub>th</sub>:



**Probability-Averaged Ratios:** 



# Step 2: Number of Events Need to add fluxes:

$$N_{\widetilde{\nu}_{\alpha}}^{\text{CC}} = t n_T V_{\text{eff}} \Omega \int_{E_{\nu}^{\min}}^{E_{\nu}^{\max}} dE_{\nu} \int_{0}^{1} dx \int_{0}^{1} dy \frac{d^2 \sigma_{\text{CC}}^{\widetilde{\nu}}}{dx dy} (E_{\nu}, x, y) \times \left[ \sum_{\beta = e, \mu, \tau} P_{\beta \alpha} \left( Q^2 \right) \tilde{\Phi}_{\widetilde{\nu}_{\beta}}^{0} \right] \Phi_{\nu_{\text{all}}} (E_{\nu})$$

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$$\begin{split} N_{\widetilde{\nu}_{\alpha}}^{\mathrm{CC}} &= t \, n_T V_{\mathrm{eff}} \Omega \int_{E_{\nu}^{\mathrm{min}}}^{E_{\nu}^{\mathrm{max}}} dE_{\nu} \int_{0}^{1} dx \int_{0}^{1} dy \frac{d^2 \sigma_{\mathrm{CC}}^{\widetilde{\nu}}}{dx dy} \left( E_{\nu}, x, y \right) \times \\ & \times \left[ \sum_{\beta = e, \mu, \tau} P_{\beta \alpha} \left( Q^2 \right) \tilde{\Phi}_{\widetilde{\nu}_{\beta}}^{0} \right] \Phi_{\nu_{\mathrm{all}}} \left( E_{\nu} \right) \\ & \text{Transition Probability} \end{split}$$

**Diferential Cross-Section** 

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#### Need to add fluxes:



#### Fluxes are too low!



Waxman, Bahcall (hep-ph/9807282) Becker, Bierman (0805.1498 [astro-ph])

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### Experimentally Unobservable?

Experiment requires:

- Sensitivity to high energy
- Neutrino flavour distinction
- Transferred momentum reconstruction
- 10<sup>8</sup> times number of targets of IceCube.

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- Sensitivity to high energy
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- 10<sup>8</sup> times number of targets of IceCube.
  - > Academic exercise?
  - > Breakthrough in neutrino detection techniques????

### Conclusions

- SUSY RGEs can modify transition probability in neutrino experiments.
- Effects depend on neutrino mass, tanβ and Majorana phases.
- Theoretically, R and T ratios for AGNs can distinguish a SUSY from a SM scenario.
- Low neutrino fluxes and cross-section pdfs seem to make observation currently unfeasible.



# Probability

$$\begin{split} P_{\alpha e} &= g_{\alpha 3} + c_{\zeta_{13}}^{2} \left[ \left( g_{\alpha 1} - g_{\alpha 3} \right) - s_{\zeta_{12}}^{2} \left( g_{\alpha 1} - g_{\alpha 2} \right) \right] \\ P_{\alpha \mu} &= g_{\alpha 2} + s_{\zeta_{12}}^{2} \left( g_{\alpha 1} - g_{\alpha 2} \right) \\ &+ s_{\zeta_{23}}^{2} \left[ \left( g_{\alpha 3} - g_{\alpha 2} \right) - s_{\zeta_{12}}^{2} \left( 1 + s_{\zeta_{13}}^{2} \right) \left( g_{\alpha 1} - g_{\alpha 2} \right) + s_{\zeta_{13}}^{2} \left( g_{\alpha 1} - g_{\alpha 3} \right) \right] \\ &+ \left( \frac{g_{\alpha 1} - g_{\alpha 2}}{2} \right) c_{\delta_{1}} s_{2\zeta_{12}} s_{2\zeta_{23}} s_{\zeta_{13}} \\ P_{\alpha \tau} &= g_{\alpha 2} + s_{\zeta_{12}}^{2} \left( g_{\alpha 1} - g_{\alpha 2} \right) \\ &+ c_{\zeta_{23}}^{2} \left[ \left( g_{\alpha 3} - g_{\alpha 2} \right) - s_{\zeta_{12}}^{2} \left( 1 + s_{\zeta_{13}}^{2} \right) \left( g_{\alpha 1} - g_{\alpha 2} \right) + s_{\zeta_{13}}^{2} \left( g_{\alpha 1} - g_{\alpha 3} \right) \right] \\ &- \left( \frac{g_{\alpha 1} - g_{\alpha 2}}{2} \right) c_{\delta_{1}} s_{2\zeta_{12}} s_{2\zeta_{23}} s_{\zeta_{13}} \end{split}$$

#### **Transition Probability**



#### Majorana Phase Dependence



#### **Non-Enhanced Scenarios**



#### **Particle Distribution Functions**

