

## T and CPT SYMMETRIES in ENTANGLED NEUTRAL MESON SYSTEMS



# OUTLINE

- Symmetries in the Laws of Physics
- Universe t-Asymmetry, the “Arrow of Time”
- Can TRV be searched in unstable system?
- EPR-Entanglement: CP-Tag
- Genuine Observables in B-factories: not needing  $\Delta\Gamma$
- CPV, TRV, CPTV Asymmetries
- Monte Carlo Study for TRV: Significance of Asymmetries
- Genuine Asymmetries in  $\Phi$ -factory
- The  $\omega$ -effect:  $K^0 \rightarrow \bar{K}^0$  Identity?
- Observables and Measurements of  $\omega$ -effect
- Conclusions, Outlook

# SYMMETRIES IN THE LAWS OF PHYSICS

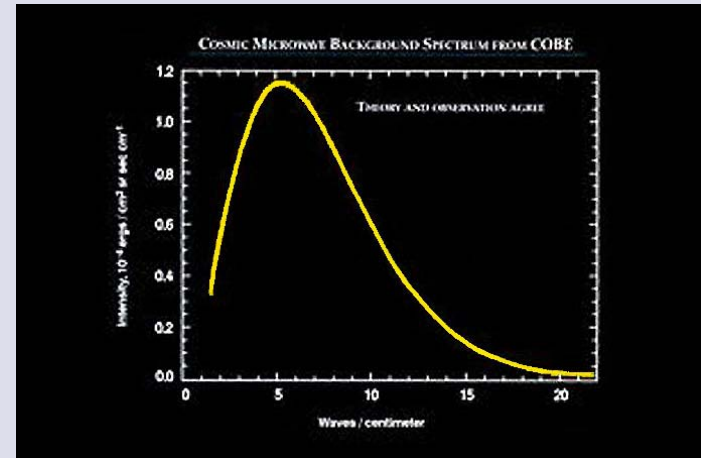
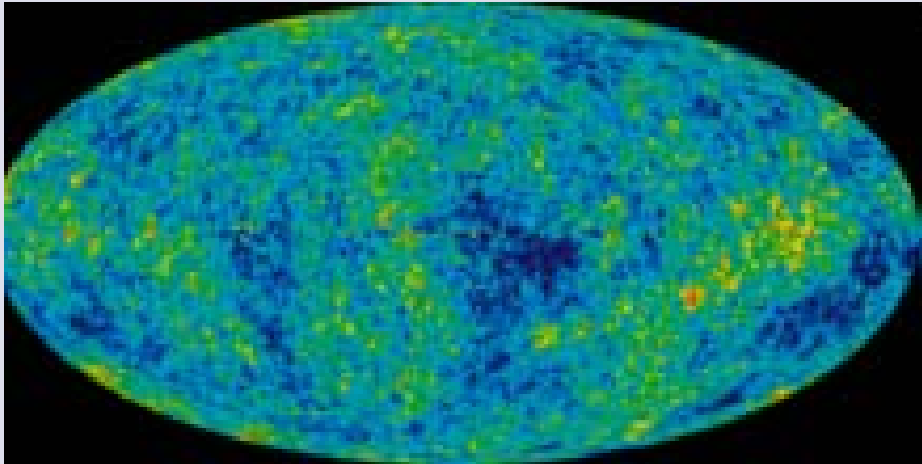
- "Microscopic" Symmetry Violations.
- T-Violation exists in the Standard Model or any field theoretic extension.
- All field theories with Lorentz invariance have CPT symmetry
- ➔ Automatic connection between CP-violation  $\leftrightarrow$  related T-violation
- T and CPT described by ANTIUNITARY rather than unitary operators, introducing many intriguing subtleties.
- ➔ Observed CP-Violation  $\Rightarrow$  T should be violated as well: Is it observed?

**T - Violation means Asymmetry under  
Interchange in  $\leftrightarrow$  out states**

- Effects in particle physics odd under  $t \leftrightarrow -t$  are not necessarily T-violating.
- $t$ - asymmetries can occur in theories with exact T- symmetry.

# UNIVERSE $t$ - ASYMMETRY

- No doubt Universe is expanding, even accelerating  $\Rightarrow$  asymmetry  $t \leftrightarrow -t$
- BUT this is perfectly compatible with laws of physics that are TR symmetric
- This  $t$ -asymmetry is due to the initial condition of our Universe  $\rightarrow$  Inflation?
- Similar to the fact that in our Universe we have a privileged reference frame  
 $\leftrightarrow$  CMB radiation with same temperature



- BUT this is not a violation of Lorentz invariance of the laws of physics



# THE “ARROW OF TIME”

- Macroscopic t-asymmetry
- Nature of Thermodynamics  $\Rightarrow$  (Eddington)  
Time's Arrow is a property of ENTROPY alone



Time is asymmetric with respect to the amount of order in an isolated system.

- Unsolved problem?  
Is quantum wave function collapse related to the thermodynamic arrow of time?
- In particle physics,  
Particle Decay is an example of a time-asymmetric process:

The mismatch between the preparation of  $P \rightarrow 1 + \dots + n$  and  $1 + \dots + n \rightarrow P$  is no related to T-violation. In fact, it looks like it prevents a true test of T-symmetry in unstable systems [Wolfenstein]

- Any connection between the Universe t-asymmetry and the “arrow of time”?  
Probably YES, saying that the initial condition was improbable: more ordered.
- But none of these t-asymmetries is a test of TRV

# CAN TR BE TESTED IN UNSTABLE SYSTEMS?

➤ A direct evidence for TRV would mean an experiment that, considered by itself, clearly shows TRV INDEPENDENT and unconnected to the results for CPV

➤ No existing result up to now clearly demonstrates TRV in this sense.

Two types of experiments:

1) A non-zero expectation value of a T-odd operator for a non-degenerate stationary state → Electric Dipole Moment: P-odd, C-even, T-odd [Semertzidis]

It can be generated by either

- Strong T-violation →  $\theta$ -term  $\epsilon_{\mu\nu\zeta\sigma} F^{\mu\nu} F^{\zeta\sigma}$  [Peccei & Quinn], or
- Weak T-violation

2) in  $\leftrightarrow$  out:  $S_{f,i} \rightarrow S_{-i,-f}$  transition.

[Sozzi] The Kabir asymmetry  $K^0 \rightarrow \bar{K}^0_{\text{ys}}$ .  $\bar{K}^0 \rightarrow K^0$  has been measured in CP-LEAR with non-vanishing value. But  $K^0 \rightarrow \bar{K}^0$  is a CPT-even transition, so  $CP \equiv T$  here!

This is apparent in that the effect is t-independent and proportional to  $\Delta\Gamma$

Is it possible to search for TRV in Mixing x Decay transitions?

**NEUTRAL MESON FACTORIES**

# CAN TR BE TESTED IN UNSTABLE SYSTEMS? CP-TAG

➤ The opportunity arises [M.C. Bañuls, J.B.] from the quantum mechanical entanglement imposed by the EPR correlation: one can have SEPARATE tests of CP, T and CPT!

➤ This coherence between the orthogonal  $B^0, \bar{B}^0$  states has been used for flavour tag:

$$|i\rangle = \frac{1}{\sqrt{2}} \left[ B^0(t_1)\bar{B}^0(t_2) - \bar{B}^0(t_1)B^0(t_2) \right]$$

where the states 1 and 2 are defined by the time of their decay with  $t_1 < t_2$ . The observation of  $B^0 \rightarrow l^+$ , for example, at time  $t_1$ , tells us that the complementary (still living) state is  $\bar{B}^0$  at  $t_1$  and, since  $t_1$ , single state evolution.

➤ BUT the INDIVIDUAL STATE of each neutral meson is NOT DEFINED BEFORE its collapse as a filter imposed by the observation of the decay of its companion!

➤ One can rewrite  $|i\rangle$  in terms of any other pair of orthogonal states of the individual neutral B-mesons:

Consider  $B_+$  and  $B_-$ , where  $B_-$  is filtered by the decay  $J/\psi K_+$ ,  $K_+$  being the neutral K-meson decaying  $K_+ \rightarrow \pi\pi$ , and  $B_+$  is the orthogonal to  $B_-$ , not connected to  $J/\psi K_+$ .

We may call the filter imposed by a first observation of one of these decays a “CP-tag”, although  $B_{\pm}$  are not CP-eigenstates of B’s necessarily.

# GENUINE OBSERVABLES NOT NEEDING $\Delta\Gamma$

- The same entangled state of the system can be rewritten

$$|i\rangle = \frac{1}{\sqrt{2}} [B_+(t_1)B_-(t_2) - B_-(t_1)B_+(t_2)]$$

- We may proceed to a partition of the complete set of events into four categories, defined by the tag in the first decay at  $t_1$ :  $B_+, B_-, B^0$  or  $\bar{B}^0$  so we have 8 different Decay-Intensities at our disposal as functions of  $\Delta t = t_2 - t_1 > 0$

- Each of these 8 processes

$$I_i(\Delta t) \sim e^{-\Gamma\Delta t} \{ C_i \cos(\Delta m\Delta t) + S_i \sin(\Delta m\Delta t) + C'_i \cosh(\Delta\Gamma\Delta t) + S'_i \sinh(\Delta\Gamma\Delta t) \}$$

- Careful: Up to now, for CPV analyses in B-factories, BABAR & BELLE have assumed CPT-invariance and  $\Delta\Gamma = 0$ :

➡ A “theorem”: Then  $\Delta t \leftrightarrow -\Delta t$  exchange, which is NOT TR-operation, becomes equivalent to TR  $\rightarrow$  CP-odd  $\sim$  T-odd  $\sim$   $\Delta t$ -odd.

➡ Only 2 independent Intensities to be compared, if CP  $\sim$  T  $\sim$   $\Delta t$  are connected.



# GENUINE OBSERVABLES NOT NEEDING $\Delta\Gamma$

- 1) Take  $B_0 \rightarrow B_+$  as the Reference transition and call (X,Y) the observed decays at times  $t_1$  and  $t_2$ . The CP, T and CPT transformed transitions are

Transition	$B^0 \rightarrow B_+$	$\bar{B}^0 \rightarrow B_+$	$B_+ \rightarrow B^0$	$B_+ \rightarrow \bar{B}^0$
(X,Y)	( $l^-, J/\psi K_L$ )	( $l^+, J/\psi K_L$ )	( $J/\psi K_S, l^+$ )	( $J/\psi K_S, l^-$ )
Transformation	Reference	CP	T	CPT

Exercise: Check that the 4 processes are experimentally independent and that  $\Delta t$ -exchange (in the same experimental “sample”)  $X \leftrightarrow Y$  is NOT in the Table

- 2) Take  $B^0 \rightarrow B_-$  as the Reference transition. The CP, T and CPT transformed transitions are

Transition	$B^0 \rightarrow B_-$	$\bar{B}^0 \rightarrow B_-$	$B_- \rightarrow B^0$	$B_- \rightarrow \bar{B}^0$
(X,Y)	( $l^-, J/\psi K_S$ )	( $l^+, J/\psi K_S$ )	( $J/\psi K_L, l^+$ )	( $J/\psi K_L, l^-$ )
Transformation	Reference	CP	T	CPT

➔ A second Asymmetry for each of the 3 transformations can be built!

- 3) Select (Y,X) from 1) as Reference.

- 4) Select (Y,X) from 2) as Reference.

- Only QM EPR-Entanglement assumed.

4 Model-Independent Asymmetries for CP



4 Model-Independent Asymmetries for T

# GENUINE CPV-ASYMMETRIES

$$\begin{aligned}
 A_{CP,1} &= \frac{\Gamma(l^-, J / \Psi K_L) - \Gamma(l^+, J / \Psi K_L)}{\Gamma(l^-, J / \Psi K_S) - \Gamma(l^+, J / \Psi K_S)} \\
 A_{CP,2} &= \frac{\Gamma(l^-, J / \Psi K_S) - \Gamma(l^+, J / \Psi K_S)}{\Gamma(J / \Psi K_L, l^-) - \Gamma(J / \Psi K_L, l^+)} \\
 A_{CP,3} &= \frac{\Gamma(J / \Psi K_L, l^-) - \Gamma(J / \Psi K_L, l^+)}{\Gamma(J / \Psi K_S, l^-) - \Gamma(J / \Psi K_S, l^+)} \\
 A_{CP,4} &= \frac{\Gamma(J / \Psi K_S, l^-) - \Gamma(J / \Psi K_S, l^+)}{\Gamma(J / \Psi K_S, l^-) - \Gamma(J / \Psi K_S, l^+)}
 \end{aligned}$$

$\Delta t$

# GENUINE TRV-ASYMMETRIES

$$\begin{aligned}
 A_{T,1} &= \frac{\Gamma(l^-, J / \Psi K_L) - \Gamma(J / \Psi K_S, l^+)}{+} \\
 A_{T,2} &= \frac{\Gamma(l^-, J / \Psi K_S) - \Gamma(J / \Psi K_L, l^+)}{+} \\
 A_{T,3} &= \frac{\Gamma(J / \Psi K_L, l^-) - \Gamma(l^+, J / \Psi K_S)}{+} \\
 A_{T,4} &= \frac{\Gamma(J / \Psi K_S, l^-) - \Gamma(l^+, J / \Psi K_L)}{+}
 \end{aligned}$$

$\Delta t$

$\Delta t$

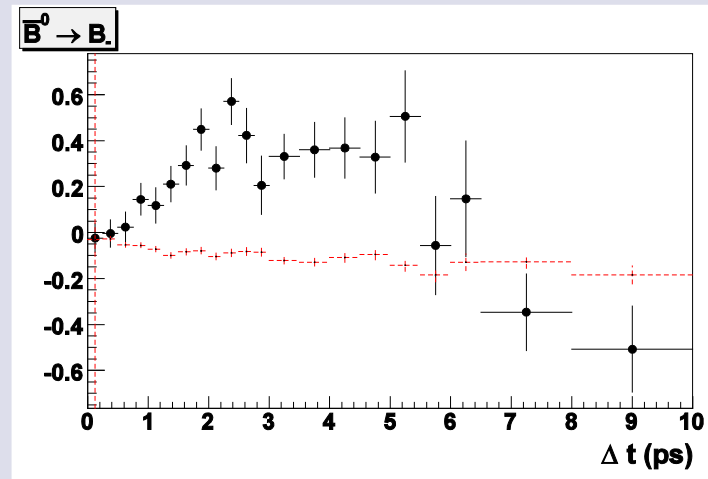
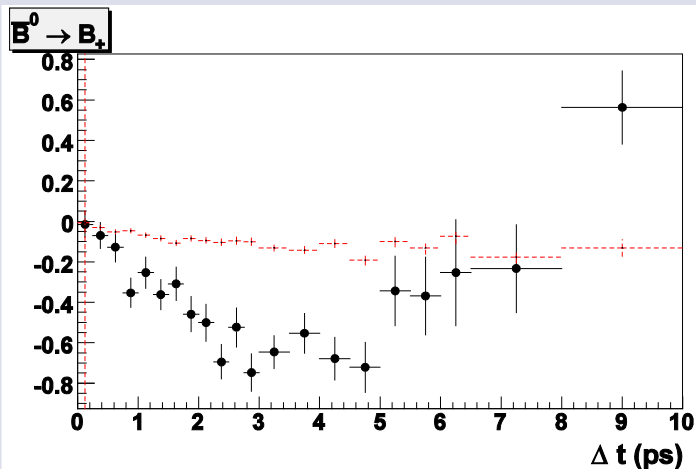
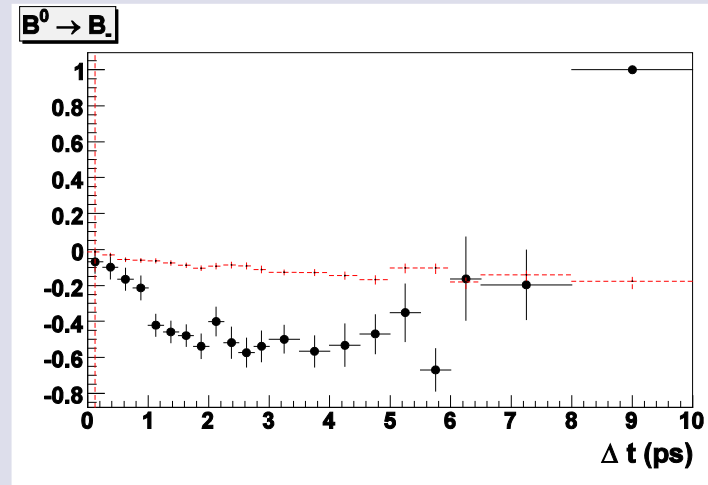
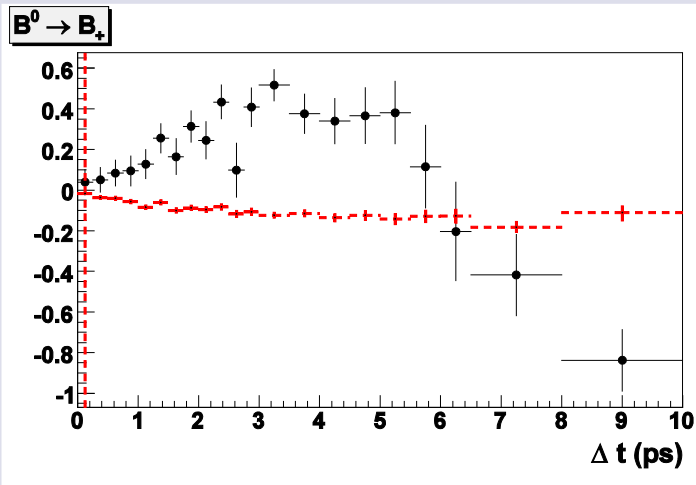
# GENUINE CPTV-ASYMMETRIES

$$\begin{aligned}
 \Delta t \left. \begin{array}{l} \rightarrow \\ \rightarrow \end{array} \right\} & A_{CPT,1} = \frac{\Gamma(l^-, J / \Psi K_L) - \Gamma(J / \Psi K_S, l^-)}{\Gamma(l^-, J / \Psi K_S) + \Gamma(J / \Psi K_L, l^-)} \\
 & A_{CPT,2} = \frac{\Gamma(l^-, J / \Psi K_S) - \Gamma(J / \Psi K_L, l^-)}{\Gamma(l^+, J / \Psi K_L) - \Gamma(J / \Psi K_S, l^+)} \\
 & A_{CPT,3} = \frac{\Gamma(l^+, J / \Psi K_L) - \Gamma(J / \Psi K_S, l^+)}{\Gamma(l^+, J / \Psi K_S) - \Gamma(J / \Psi K_L, l^+)} \\
 & A_{CPT,4} = \frac{\Gamma(l^+, J / \Psi K_S) - \Gamma(J / \Psi K_L, l^+)}{\Gamma(l^+, J / \Psi K_S) - \Gamma(J / \Psi K_L, l^+)}
 \end{aligned}$$

$\left. \begin{array}{l} \leftarrow \\ \leftarrow \end{array} \right\} \Delta t$

# MONTE CARLO STUDY FOR TRV

➤ Pablo Villanueva [see parallel session talk] has generated events with a PDF allowing CP, T & CPT violation parameters. The true value taken from Standard Model: CPT-symmetry,  $\Delta\Gamma = 0$ ,  $C_i = 0$ ,  $S_i = \pm 0.672 (\sin 2\beta)$ . For  $A_T$  asymmetries, including proper-time resolution, mistags and efficiency effects (from BABAR published papers),





# SIGNIFICANCE OF TRV ASYMMETRIES

- Each one of the 4 TRV-Asymmetries has an experimental significance obtained from a  $\chi^2$  test. One gets much more than 5  $\sigma$ - effect !

TRV test	$B^0 \rightarrow B_+$	$B^0 \rightarrow B_-$	$\bar{B}^0 \rightarrow B_+$	$\bar{B}^0 \rightarrow B_-$
Standard Deviations	6.70	9.84	9.42	7.34

- The global significance could be obtained in the  $\chi^2$ -test because, to first order, the four results are statistically independent.

**Expected “guarantee” of a significant discovery for TRV ↔**

**a fundamental result:**

**A first observation of true, direct evidence for genuine TRV by many  $\sigma$ 's from zero, without any reference to, and independent of, CPV.**

- Similar significances are expected for the Asymmetries testing genuine CPV independently

# GENUINE ASYMMETRIES IN DAPHNE

- For  $K^0 \rightarrow \bar{K}^0$ , contrary to  $B^0 \rightarrow \bar{B}^0$ , the “physical” states of definite mass have  $\Delta\Gamma \neq 0$ , essentially  $\Delta\Gamma \sim \Gamma_S \sim 2\Delta m$ , so that the “theorem” is not valid: CP-odd is NOT  $\Delta t$ -odd.
- If  $K_+$  is the neutral K-state filtered by the decay to  $2\pi$  and  $K_-$  is its orthogonal state, the Master Table for the  $\Phi$ -factory becomes

	<b>Reference</b>	<b>CP</b>	<b>T</b>	<b>CPT</b>
$\Delta t$	$K^0 \rightarrow K_+$ ( $l^-, 2\pi$ )	$\bar{K}^0 \rightarrow K_+$ ( $l^+, 2\pi$ )	$K_+ \rightarrow K_0$ ( $3\pi, l^+$ )	$K_+ \rightarrow \bar{K}^0$ ( $3\pi, l^-$ )
	$K^0 \rightarrow K_-$ ( $l^-, 3\pi$ )	$\bar{K}^0 \rightarrow K_-$ ( $l^+, 3\pi$ )	$K_- \rightarrow K_0$ ( $2\pi, l^+$ )	$K_- \rightarrow \bar{K}^0$ ( $2\pi, l^-$ )
	$K_- \rightarrow \bar{K}^0$ ( $2\pi, l^-$ )	$K_- \rightarrow K^0$ ( $2\pi, l^+$ )	$\bar{K}^0 \rightarrow K_-$ ( $l^+, 3\pi$ )	$K^0 \rightarrow K_-$ ( $l^-, 3\pi$ )
	$K_+ \rightarrow \bar{K}^0$ ( $3\pi, l^-$ )	$K_+ \rightarrow K^0$ ( $3\pi, l^+$ )	$\bar{K}^0 \rightarrow K_+$ ( $l^+, 2\pi$ )	$K^0 \rightarrow K_+$ ( $l^-, 2\pi$ )

- Experimental analyses of CP, T, CPT Asymmetries with DAΦNE data are going on [A.Di Domenico, P.Villanueva]

# IS EPR-ENTANGLEMENT APPLICABLE?

- Proposed tests of separate CP, T, CPT symmetries based on EPR-Entanglement imposed by Particle Identity:  
 $K^0, \bar{K}^0$  are two states of identical particles.
- The two states connected by C, so that  $C\mathcal{P} = +$  [ $\mathcal{P}$ : permutation operation].
- In neutral meson factories,  $K^0 \rightarrow \bar{K}^0$  produced by  $\Phi$ -decay:  $J=1, S=0 \Rightarrow L=1 \Rightarrow C = - \Rightarrow \mathcal{P} = -, \text{ antisymmetric wave function} \leftrightarrow$   
 Time evolution (including the Mixing  $K^0 \rightarrow \bar{K}^0$ ) preserves  $K^0 \bar{K}^0$  terms only.  
 ➡ Perfect for tagging: Flavour-Tag, CP-Tag,...
- What if the  $K^0, \bar{K}^0$  Identity is lost ? [J.B. , Mavromatos, Papavassiliou]

The two particle system would not satisfy the requirement  $C\mathcal{P} = +$ .  
 In perturbation theory, if still  $J=1, C=-$ ,

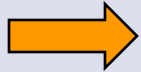
$$|i\rangle = |\text{antisymmetric}\rangle + \omega |\text{symmetric}\rangle \implies \text{the } \omega\text{-effect}$$

➡ Time evolution:  $\omega K^0 \bar{K}^0$  terms  $\leftrightarrow$  Demise of tagging

# THE $\omega$ -EFFECT

- Loosing the  $K^0, \bar{K}^0$  Identity...
- In some Quantum Gravity models, matter propagation in topologically non-trivial space-time vacua suffers a possible loss of quantum coherence or “decoherence”.
- Originated by space-time foam backgrounds? [Wheeler, Ellis et al.]

The matter quantum system is an open system, interacting with the “environment” of quantum gravitational d. o. f.  $\Rightarrow$  Apparent loss of unitarity for low-energy observers



Not a well-defined S-matrix between asymptotic states  $\Rightarrow$   
The CPT-operator is NOT well-defined [Wald]

- It should be disentangled from the case of effective theories for Lorentz violation [Altschul], in which CPT breaking means  $[H_{\text{eff}}, \text{CPT}] \neq 0$ .
- The CPT “Violation” discussed here would be an “intrinsic” microscopic time irreversibility, so that  $\bar{K}^0$  is not “well-defined” from  $K^0$ . It implies:
  - 1) a modified single  $K^0 \rightarrow \bar{K}^0$  evolution:  $\alpha, \beta, \gamma$  parameterization [Lindblad].
  - 2) for entangled Kaon states in a  $\Phi$ -factory, **the  $\omega$ -effect**

# $\omega$ -EFFECT OBSERVABLES

[J.B., Mavromatos, Papavassiliou]

- Consider the  $\Phi$ -decay amplitude

$$A(X, Y) = \langle X | K_S \rangle \langle Y | K_S \rangle N(A_1 + A_2)$$

$$A_1 = e^{-i(\lambda_L + \lambda_S)t/2} \left[ \eta_X e^{-i\Delta\lambda\Delta t/2} - \eta_Y e^{i\Delta\lambda\Delta t/2} \right]$$

$$A_2 = \omega \left[ e^{-i\lambda_S t} - \eta_X \eta_Y e^{-i\lambda_L t} \right]$$



- Strategy: Choose a channel suppressed by  $\eta$ 's:  $X = Y = \bar{u}^+ \bar{u}^-$ , CP “forbidden”

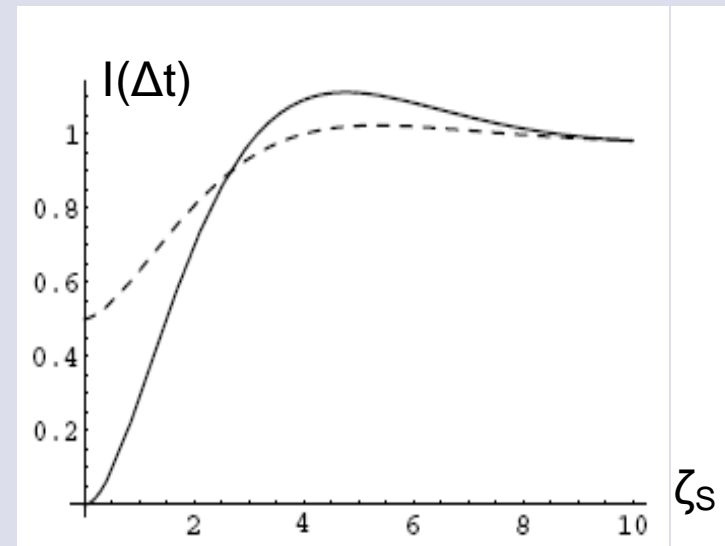
➡ Enhanced effects  $\omega/|\eta_{+-}|$

- Intensity

$$I(\Delta t) \equiv \frac{1}{2} \int_{\Delta t}^{\infty} dt |A(X, Y)|^2$$

for  $|\omega| = |\eta_{+-}|$

$$\Omega = \phi_{+-} - 0.16\pi$$





# MEASUREMENT OF $\omega$ -EFFECT

- KLOE [Di Domenico et al.] obtained the first measurement of the  $\omega$ -parameter

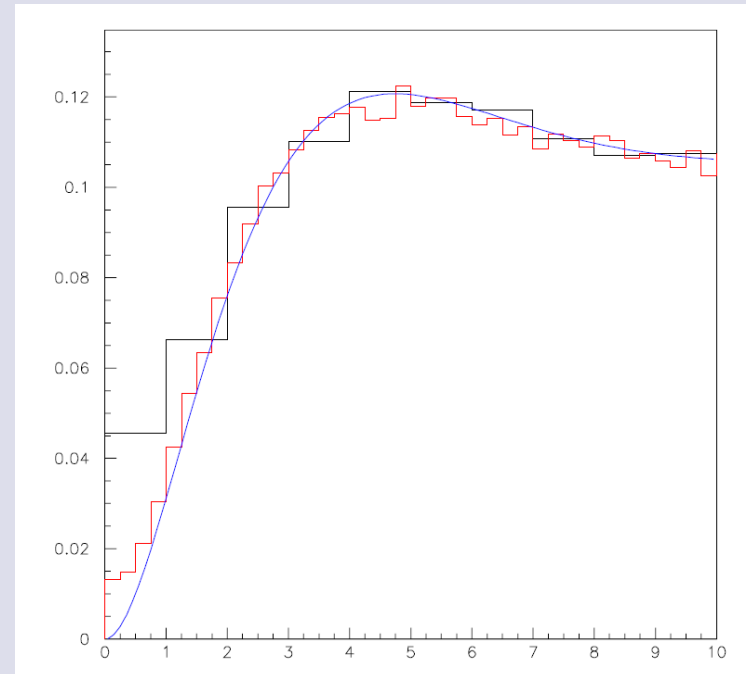
$$\left. \begin{aligned} \text{Re}(\omega) &= (-1.6^{+3.0}_{-2.1_{stat}} \pm 0.4_{syst}) \times 10^{-4} \\ \text{Im}(\omega) &= (-1.7^{+3.3}_{-3.0_{stat}} \pm 1.2_{syst}) \times 10^{-4} \end{aligned} \right\} |\omega| < 1.0 \times 10^{-3} \text{ at 95\% CL}$$

- At least one order of magnitude improvement is expected with KLOE-2 at the upgraded DAΦNE.

- All decoherence effects, including the  $\omega$ -effect, manifest as a DEVIATION from the QM prediction of the correlation  $I(\pi^+\pi^-, \pi^+\pi^-; \Delta t=0)=0$ . Hence the reconstruction of events in the region near  $\Delta t \approx 0$  is crucial  $\longleftrightarrow$  vertex resolution.


- **In B-factories, there is no such a privileged channel.**

- With currently available data from BABAR and BELLE, the CPV semileptonic charge asymmetry, in equal sign dilepton channel  $I(l^\pm l^\pm; \Delta t)$ , gives the bounds [Alvarez, J.B., Nebot]
 
$$-0.0084 \leq \text{Re}(\omega) \leq 0.0100 \text{ at 95\%CL}$$



[de Santis] Monte Carlo simulation of  $I(\pi^+\pi^-, \pi^+\pi^-; \Delta t)$ , with the KLOE resolution  $\sigma_{\Delta t} \approx \zeta s$  and with the expected KLOE-2  $\sigma_{\Delta t} \approx 0.3 \zeta s$

# $\omega$ -EFFECT FROM SPACE-TIME FOAM MODEL

- $\omega$ -effect: as the result of local distortions of space-time in the neighborhood of defects, interacting with matter [J.B., Mavromatos, Sarkar].
- Recoil of Planck-mass defect  $\Rightarrow$  metric deformation  $g_{0i} \sim \Delta k^i / M_P = \zeta k^i / M_P$
- Lorentz invariance still holds macroscopically  $\langle \zeta k^i \rangle = 0$ , but
- One has non-trivial quantum fluctuations  $\langle \zeta^2 k_i k_j \rangle \propto \delta_{ij} \zeta^2 |\vec{k}|^2$
- Stochastic effects of the space-time foam   $|\omega|^2 \sim \frac{\zeta^2 |\vec{k}|^4}{M_P^2 \Delta m^2}$   
enhanced by quasi-degeneracy of mass eigenstates.
- At the DAΦNE energy,  $|\omega| \sim 10^{-4} \zeta$ , which lies within the sensitivity of KLOE-2 for not much small values of the momentum transfer fraction  $\zeta$ .
- In some concrete string-theory-inspired models examined by [Mavromatos, Sarkar],  $\zeta \sim \sum m^2 / |\vec{k}|^2$

# CONCLUSION

- Observed t-Asymmetries are not T-violating:  
TRV means Asymmetry under in  $\leftrightarrow$  out
- Unique opportunity for unstable systems: EPR-Entanglement between the two neutral mesons in B-, and  $\Phi$ -, factories.
- Golden Channels  $\rightarrow$  8 different Decay-Intensities.  
In appropriate combinations,  
4 Genuine independent Asymmetries for each: CP, T, CPT
- Monte Carlo study for TRV in B-factories  $\rightarrow$  more than 5  $\sigma$ 's in each of the 4 asymmetries  $\Rightarrow$

Expectation of a first observation of true TRV

- In QG models, S-matrix not well defined, CPT-operator not well defined

The  $\omega$ -effect: Preferred channel in  $\Phi$ -factory  $\rightarrow$  I ( $\pi^+\pi^-$ ,  $\pi^+\pi^-$ ;  $\Delta t$ )

- A sensitivity to  $|\omega| \sim 10^{-4}$  at KLOE-2 not far from expectations in certain models of space-time foam.