

Channeling radiation on single crystals

S. Dabagov, W. Wagner, and B. Azadegan

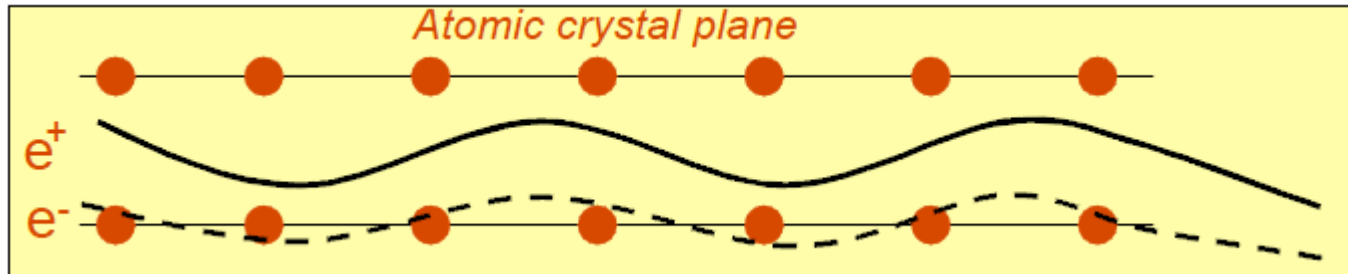
Cooperation from Italy-Russia, Germany, and Iran

Publications

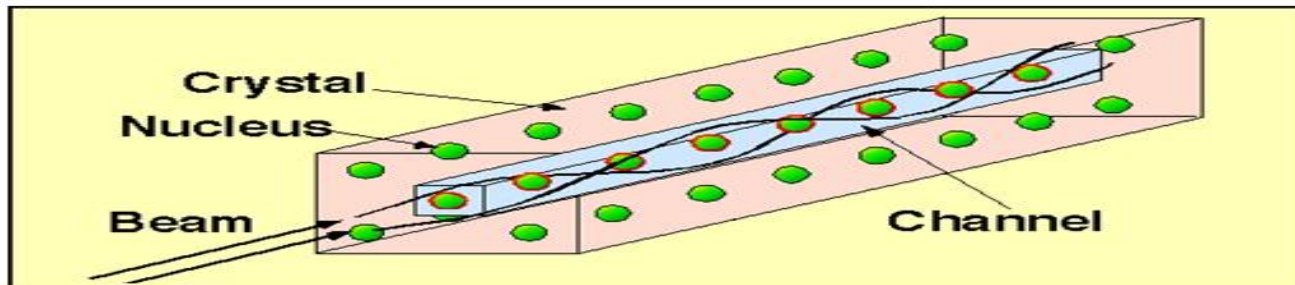
1. Azadegan, B., S. B. Dabagov, and W. Wagner. "Simulation of axial channeling radiation on a thin Ge single crystal. *Nuovo Cimento-C* 34, no. 4 (2011): 149.
2. Azadegan, B., and S. B. Dabagov. "Planar channeling radiation by 20-800 MeV electrons in a thin silicon carbide." *The European Physical Journal Plus* 126, no. 6 (2011): 58.
3. Azadegan, B., S. B. Dabagov, and W. Wagner. "Computer simulation of the radiation of electrons axially channeled in a thin Ge single crystal." *Nuclear Instruments and Methods in Physics Research Section B: Beam Interactions with Materials and Atoms* 269, no. 19 (2011): 2098-2106.
4. Azadegan, B., S. B. Dabagov, and W. Wagner. "Planar channeling radiation by relativistic electrons in different structures of silicon carbide." *Journal of Physics: Conference Series*, vol. 357, no. 1, p. 012027. IOP Publishing, 2012.
5. Azadegan, B., A. Mahdipour, S. B. Dabagov, and W. Wagner. "Positron energy distributions from a hybrid positron source based on channeling radiation." *Nuclear Instruments and Methods in Physics Research Section B: Beam Interactions with Materials and Atoms* 309 (2013): 56-58.

1. Introduction

Planar channeling: One dimensional problem



Axial channeling: two dimensional problem



2. Theory of planar channeling radiation

Planar channeling

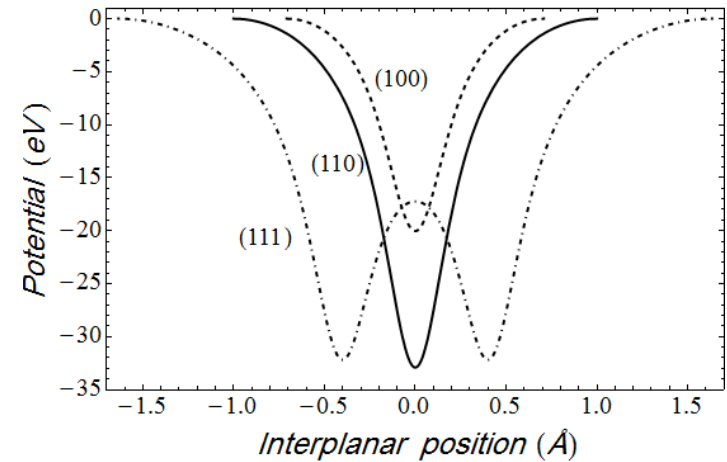
$$V(x) = \sum_n v_n e^{ingx}$$

$$v_n = -\frac{2\pi}{V_c} a_0^2 (e^2 / a_0) \sum_j e^{-M_j(\vec{g})} e^{-i\vec{g} \cdot \vec{r}_j} \sum_{i=1}^4 a_i e^{\left(-\frac{1}{4} \left(\frac{b_i}{4\pi^2}\right) (ng)^2\right)}$$

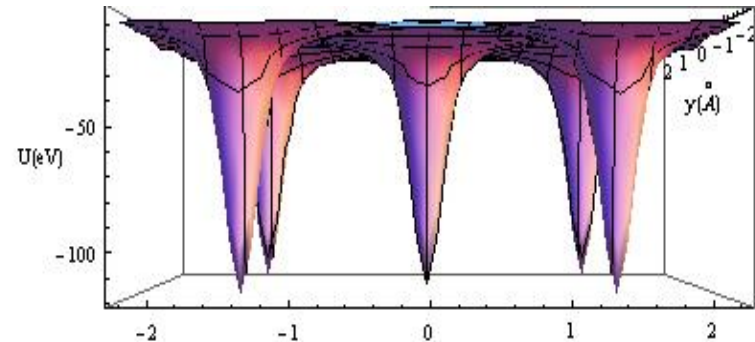
Axial channeling

$$V(x, y) = \sum_{\vec{g}_m} v_{\vec{g}_m} e^{i\vec{g}_m \cdot \vec{r}_\perp}$$

$$v_{\vec{g}_m} = -\frac{2\pi}{V_c} a_0^2 (e^2 / a_0) \sum_j e^{-i\vec{g} \cdot \vec{r}_j} \sum_{i=1}^4 a_i e^{\left(-\frac{1}{4} \left(\frac{b_i}{4\pi^2} + 2\langle u_j^2 \rangle\right) |\vec{g}_m|^2\right)}$$



The planar continuum potentials of diamond for electrons



The <100> axial continuum potential of germanium for electrons

3. Theory of planar channeling radiation (Quantum)

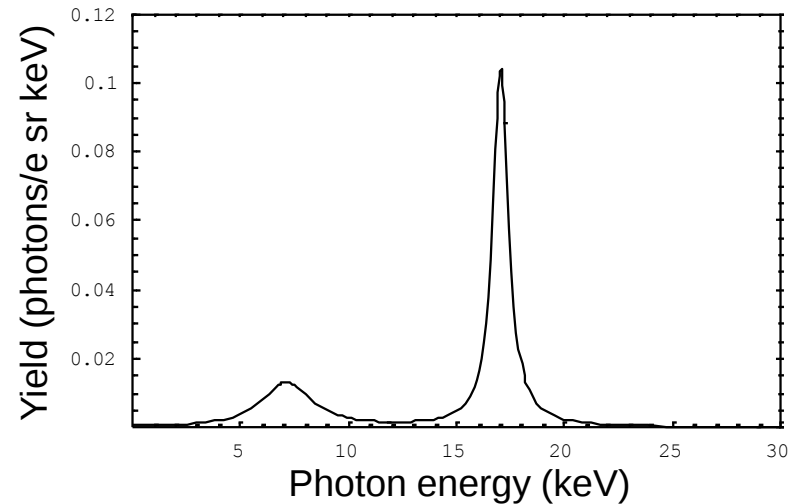
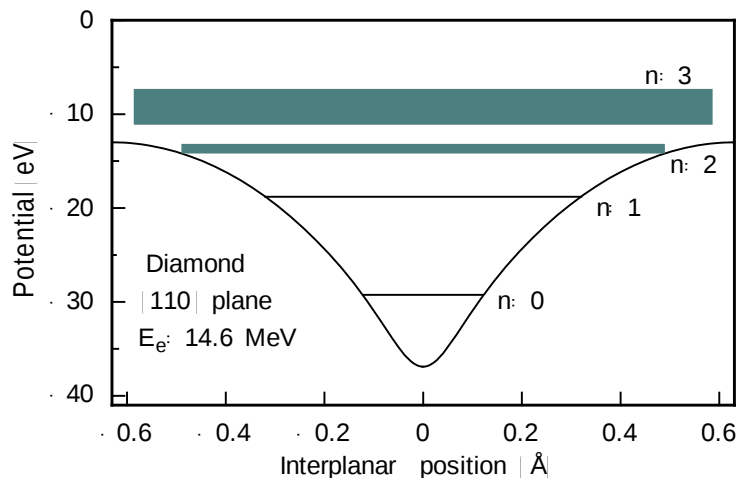
Quantum mechanical model

$$E_e < 100 \text{ MeV}$$

$$-\frac{\hbar^2}{2m_e\gamma} \frac{d^2\psi(x)}{dx^2} + V(x)\psi(x) = E\psi(x) \longrightarrow \text{Wave functions } \psi_i(x) \text{ and eigenvalues } E_i$$

$$E_0 = 2\gamma^2(E_i - E_f)$$

$$\frac{d^2 N_{CR}(i \rightarrow f)}{d\Omega_\gamma dE_\gamma} = \frac{\alpha \lambda_c^2}{\pi \hbar c} 2\gamma^2(E_i - E_f) \left| \left\langle \psi_f(x) \left| \frac{d}{dx} \right| \psi_i(x) \right\rangle \right|^2 \int_0^z dz P_i(z) \times \frac{\Gamma_{\text{tot}}/2}{(E_\gamma - E_0)^2 + 0.25\Gamma_{\text{tot}}^2}$$



A Mathematica package for calculation of planar channeling radiation spectra of relativistic electrons channeled in a diamond-structure single crystal (quantum approach)

4. Theory of planar channeling radiation (classical)

Classical model

$$E_e > 100 \text{ MeV}$$

Planar :

$$\gamma m \ddot{x}(t) = F = -\frac{\partial V(x)}{\partial x}$$

$$\gamma m \ddot{x} = -\frac{\partial V(x, y)}{\partial x}$$

Axial :

$$\gamma m \ddot{y} = -\frac{\partial V(x, y)}{\partial y}$$

$$\gamma m \ddot{z} = 0$$

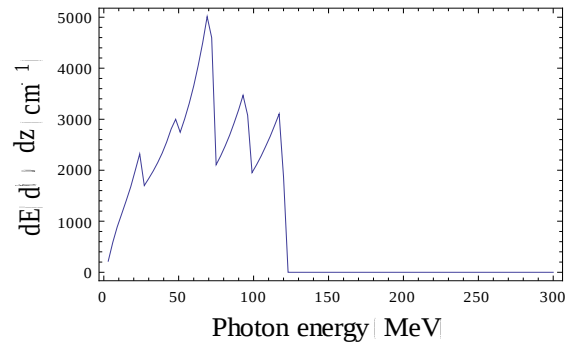
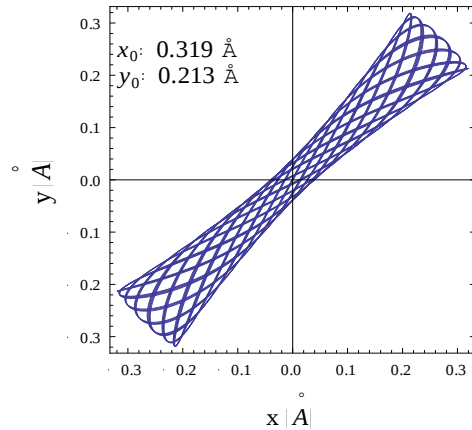
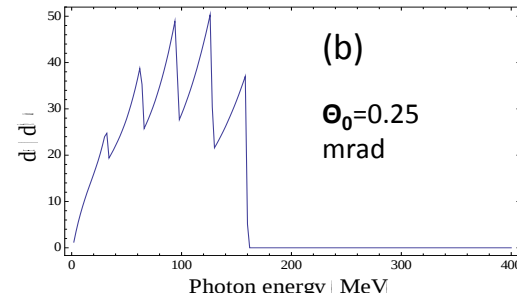
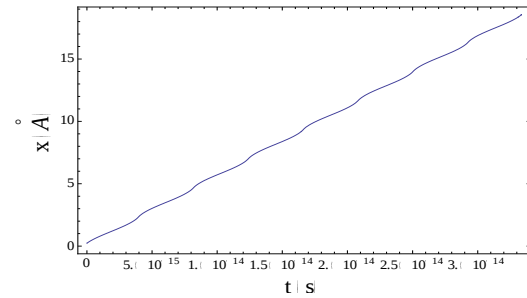
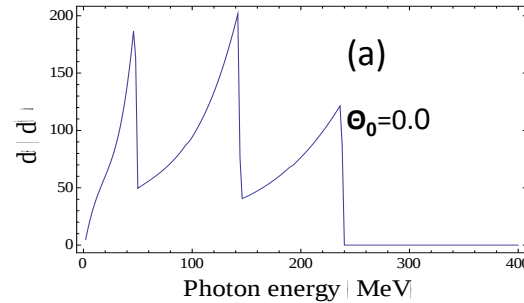
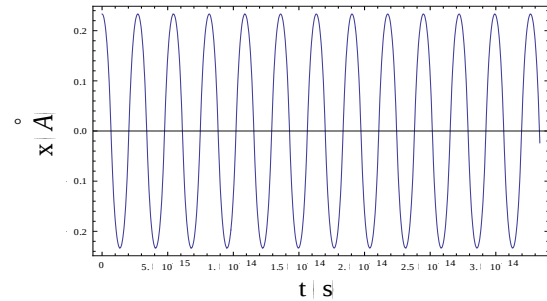
Angular energy distribution:

$$\frac{d^2 E}{d\omega d\Omega} = \frac{e^2}{4\pi^2 c} \left| \int_0^\tau e^{i(\omega t - \vec{k} \cdot \vec{r})} \frac{\vec{n} \times ((\vec{n} - \vec{\beta}) \times \dot{\vec{\beta}})}{(1 - \vec{\beta} \cdot \vec{n})^2} dt \right|^2$$

Total radiated energy in thick crystal:

$$\frac{dE}{d\omega \Delta z} = \frac{e^2}{c^4 T^2} \sum_{n=1}^{\infty} \Theta[1 - \eta_n] (\eta_n^2 - \eta_n + \frac{1}{2}) \cdot |\dot{x}_{\tilde{\omega}}|^2$$

$$\eta_n = \frac{T\omega}{4\pi\gamma^2 n}; \quad \tilde{\omega} = \frac{2\pi n}{T}; \quad \dot{x}_{\tilde{\omega}} = \int_0^T \dot{x} e^{i\tilde{\omega}t}$$



Trajectories and CR spectra for one incident point with a) zero b) 0.25 mrad incidence angles for 2 GeV electron channeled along the (110) plane of a tungsten single crystal.

Trajectory (rosette motion) and CR spectra for one incident point for 1 GeV electron channeled along the <100> axis of W single crystal.

Simulation of axial channeling radiation on a thin Ge single crystal

Azadegan, B. and Dabagov, S. B. and Wagner, W. (2011) nuovo cemento C, 34 (4). pp. 149-156. ISSN 1826-9885

Official URL: <https://www.sif.it/riviste/sif/ncc/econtents/2011/...>

Abstract

Based on classical electrodynamics the radiation emitted by axially channeled electrons has been investigated by means of computer simulations. Using the Doyle-Turner approximation for the atomic scattering factor and taking thermal vibrations of atoms into account, we calculated the two-dimensional continuum potential of the 110 crystallographic axis of a thin Ge single crystal. The trajectories, velocities and accelerations of electrons are obtained by solving the equations of motion in three dimensions, and the spectral-angular distribution of radiation has been calculated within classical approach.

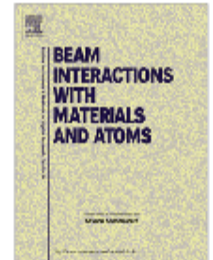


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Positron energy distributions from a hybrid positron source based on channeling radiation



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Regular Article

Planar channeling radiation by 20–800 MeV electrons in a thin silicon carbide

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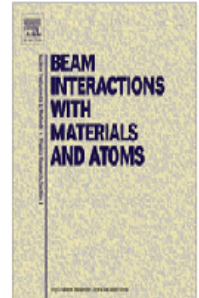


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Computer simulation of the radiation of electrons axially channeled in a thin Ge single crystal

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Thank you