







nature

# La misura della violazione di fase oce nel settore leptonico: stato e prospettive

Lorenzo Magaletti (Politecnico di Bari & INFN Bari) per il gruppo T2K di Bari



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#### Mixing of three neutrinos



# Neutrino oscillations at T2K



## Near detector complex

at 280 m from the target



Intense high purity muon (anti)neutrino beam from J-PARC to Super-K to study:

- Muon (anti) neutrino disappearance ν<sub>µ</sub>→ν<sub>µ</sub> (ν̄<sub>µ</sub>→ν̄<sub>µ</sub>)
- $\Psi$  Electron (anti) neutrino appearance  $V_{\mu} \rightarrow V_{e}$  ( $\overline{V}_{\mu} \rightarrow \overline{V}_{e}$ )
- Rich program of:
  - neutrino cross sections studies with near detectors
  - "exotic" physics: sterile neutrinos, etc...

# T2K one of the biggest international collaboration of neutrino LBL



#### ~500 physicists, 69 institutions, 12 countries

Europe	261
France	38
Germany	5
Italy	28
Poland	28
Russia	19
Spain	14
Switzerland	30
UK	99

Americas	96
Canada	26
USA	70

Asla	117
Japan	114
Vietnam	3

![](_page_4_Picture_6.jpeg)

#### Very strong European contribution including CERN

#### Neutrino oscillations at T2K

$$P(\nu_{\mu} \to \nu_{\mu}) \simeq 1 - (\cos^4 \theta_{13} \sin^2 2\theta_{23} + \sin^2 2\theta_{13} \sin^2 \theta_{23}) \sin^2 \Delta m_{31}^2 \frac{L}{4E}$$

Precision measurement of  $\theta_{23}$  and  $\Delta m^{2}_{31}$ CPT test with anti-neutrino mode  $(\bar{\nu}_{\mu} \rightarrow \bar{\nu}_{\mu})$ 

$$\begin{split} P(\nu_{\mu} \rightarrow \nu_{e}) = & 4c_{13}^{2}s_{13}^{2}s_{23}^{2}\sin^{2}\frac{\Delta m_{13}^{2}L}{4E_{\nu}} \times \left[1 \pm \frac{2a}{\Delta m_{13}^{2}}(1 - s_{13}^{2})\right] & \theta_{13} \text{ driven} \\ & +8c_{13}^{2}s_{12}s_{13}s_{23}(c_{12}c_{23}\cos\delta_{CP} - s_{12}s_{13}s_{23})\cos\frac{\Delta m_{23}^{2}L}{4E_{\nu}}\sin\frac{\Delta m_{13}^{2}L}{4E_{\nu}}\sin\frac{\Delta m_{12}^{2}L}{4E_{\nu}} & CP \text{ even} \\ & \mp 8c_{13}^{2}c_{12}c_{23}s_{12}s_{13}s_{23}\sin\delta_{CP}\sin\frac{\Delta m_{23}^{2}L}{4E_{\nu}}\sin\frac{\Delta m_{13}^{2}L}{4E_{\nu}}\sin\frac{\Delta m_{12}^{2}L}{4E_{\nu}} & CP \text{ odd} \\ & +4s_{12}^{2}c_{13}^{2}(c_{13}^{2}c_{23}^{2} + s_{12}^{2}s_{23}^{2}s_{13}^{2} - 2c_{12}c_{23}s_{12}s_{23}s_{13}\cos\delta_{CP})\sin\frac{\Delta m_{12}^{2}L}{4E_{\nu}} & Solar \text{ driven} \\ & \mp 8c_{12}^{2}s_{13}^{2}s_{23}^{2}\cos\frac{\Delta m_{23}^{2}L}{4E_{\nu}}\sin\frac{\Delta m_{13}^{2}L}{4E_{\nu}}\frac{aL}{4E_{\nu}}(1 - 2s_{13}^{2}) & Matter \text{ effect (CP odd)} \\ & = 6c_{13}^{2}s_{13}^{2}s_{23}^{2}\cos\frac{\Delta m_{23}^{2}L}{4E_{\nu}}\sin\frac{\Delta m_{13}^{2}L}{4E_{\nu}}\frac{aL}{4E_{\nu}}(1 - 2s_{13}^{2}) & Matter \text{ effect (CP odd)} \\ & = 6c_{13}^{2}s_{13}^{2}s_{23}^{2}\cos\frac{\Delta m_{23}^{2}L}{4E_{\nu}}\sin\frac{\Delta m_{13}^{2}L}{4E_{\nu}}\frac{aL}{4E_{\nu}}(1 - 2s_{13}^{2}) & Matter \text{ effect (CP odd)} \\ & = 6c_{13}^{2}s_{13}^{2}s_{23}^{2}\cos\frac{\Delta m_{23}^{2}L}{4E_{\nu}}\sin\frac{\Delta m_{13}^{2}L}{4E_{\nu}}\frac{aL}{4E_{\nu}}(1 - 2s_{13}^{2}) & Matter \text{ effect (CP odd)} \\ & = 6c_{13}^{2}s_{13}^{2}s_{13}^{2}s_{23}^{2}\cos\frac{\Delta m_{23}^{2}L}{4E_{\nu}}\sin\frac{\Delta m_{13}^{2}L}{4E_{\nu}}\frac{aL}{4E_{\nu}}(1 - 2s_{13}^{2}) & Matter \text{ effect (CP odd)} \\ & = 6c_{13}^{2}s_{13}$$

#### $\mathbf{\hat{e}}$ $\mathbf{\theta}_{13}$ dependence of the leading term

 $\theta_{23}$  dependence of the leading term ( $\theta_{23}=45^{\circ}$  or  $\theta_{23} \ge 45^{\circ}$ ?)

 $\checkmark$  CP odd phase delta: asymmetry of probabilities  $P(v_{\mu} \rightarrow v_{e}) \neq P(\overline{v}_{\mu} \rightarrow \overline{v}_{e})$  if sin $\delta \neq 0$ 

 $\mathbf{V}$  Matter effect:  $V_e$  ( $\overline{V}_e$ ) appearance enhanced in normal (inverted) mass hierarchy

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## Learning from $V_e$ ( $\bar{V}_e$ ) appearance

![](_page_6_Figure_1.jpeg)

# **T2K experimental setup**

#### The off-axis neutrino beam

![](_page_8_Figure_1.jpeg)

Enhance CCQE-like interactions (signal at Super-Kamiokande)
 Reduces background from π<sup>0</sup> interactions
 Reduces V<sub>e</sub> contamination (less than 1%) at the peak

 $E_{v}$  (GeV)

![](_page_9_Figure_0.jpeg)

![](_page_9_Figure_1.jpeg)

![](_page_9_Figure_2.jpeg)

#### ND280 (off-axis)

- Magnet: B = 0.2 T
- **TPC:** p measurement + particle-ID with dE/dx
- **FGD:** Fine-grained detectors  $(2 \times 0.8 t) \rightarrow$  FGD1 (C), FGD2
- $(C+H_2O)$
- SMRD: magnetized muon range detector
- **POD:** pi-zero detector (Pb/brass-H<sub>2</sub>O-scintillator)
- **ECal:** electromagnetic calorimeter

#### **INGRID** (on-axis)

v<sub>µ</sub> CC rate → monitor beam profile and stability
 Fe/Scintillator tracking calorimeter (16 Fe/Scint modules + 1 central one made of scintillator only)

#### Neutrino cross sections at T2K energies

![](_page_10_Figure_1.jpeg)

Data

RHC CC-v,

- NEUT 5.4.0 ( $\chi^2$ =14.634)

----- NuWro 19.02 (χ²=32.077)

GENIE 2.12.10 ( $\chi^2$ =16.319)

RHC CC-V

24

22

20

18

16

14

12 10

T2K FHC 11.92 × 10<sup>20</sup> POT

T2K RHC 6.29 × 10<sup>20</sup> POT

FHC CC-v.

**0° <= θ <= 45°** 

- At T2K energies the main kind of interactions are **CCQE** Other neutrino interactions with production of **pions** in the final state are important as well
  - Discrepancies between different theoretical models
  - x-sec are not completely understood at T2K energies

#### Latest x-sec measurement at ND280:

- $v_{e}$  and  $\bar{v}_{e}$  measurement crucial for CPV
- $v_{\mu}/\bar{v}_{\mu}$  important for oscillation analysis
- Carbon/Oxigen Crucial for ND280 (CH, O) to SK (H<sub>2</sub>O) extrapolation

A dedicated experiment is needed in order to reduce these systematics  $\rightarrow$  AIDA-Innova project (HPTPC with hybrid readout) started in Bari since April 2021 Vessel design will be done by our CAD group here in Bari

![](_page_10_Figure_10.jpeg)

![](_page_10_Figure_11.jpeg)

## Far detector: Super-Kamiokande

#### Super-K (off-axis)

- Water Cherenkov (22.5 kt fiducial volume, > 11k PMT, ~40 m x 40 m)
- Excellent μ/e separation and π<sup>0</sup> detection (2 e-like rings)
- $\Delta E/E \sim 10\%$  for Quasi-Elastic (QE) events

#### $\nu_l + n \to l^- + p \qquad \bar{\nu}_l + p \to l^+ + n$

#### SIGNALS

SK MC

SK MC

SK MC

μ

 $e/\gamma$ 

multi-ring

Single μ/e like ring
Erec by energy/direction of lepton, 2-body kinematics

#### $\nu_e + p \to e^- + \pi^+ + p$

Single e like ring
 E<sub>rec</sub> by energy/direction of lepton, 2-body kinematics with a Δ<sup>++</sup> recoil
 One decay electron

#### BACKGROUNDS

 $\nu_l + (n/p) \to l^- + (n/p) + \pi$ 

 $\nu_l + (n/p) \to \nu_l + (n/p) + \pi^0$ 

- $\stackrel{\bullet}{=} \pi^0 \rightarrow \gamma \gamma$ : ring counting, 2-ring reconstruction
  - $\frac{1}{2}$   $\gamma$  misidentified as e from  $v_e$  CCQE
  - powerful rejection capabilities reduce this by O(10<sup>2</sup>)
- Ring counting, decay electron cut to reject non-CCQE interactions

![](_page_12_Picture_0.jpeg)

#### ND280

![](_page_13_Figure_1.jpeg)

![](_page_13_Figure_2.jpeg)

![](_page_13_Figure_3.jpeg)

Istituto Naziona

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## First large TPC with MPGD

![](_page_13_Picture_5.jpeg)

![](_page_13_Picture_6.jpeg)

TPC assembling

TPC design with advanced detectors (MPGD)

#### **INFN Bari activities in T2K**

- TPC design, assembling, calibration, maintenance and operation
- Leading role on TPCs (Emilio Radicioni)
- ${f \hat{s}}$  Leading in  $ar{
  u}_{\mu}$  analysis @ ND280
- Since 2012 our group is leading the T2K activities in Italy and in the executive committee of the T2K experiment (Gabriella Catanesi)

![](_page_13_Picture_14.jpeg)

![](_page_13_Picture_15.jpeg)

![](_page_14_Picture_0.jpeg)

#### The T2K Near Detector upgrade

- · Keep the electromagnetic calorimeter
- Horizontal active target detector: SuperFGD
- Two High-Angle TPCs

- Current
   Upgrade

   Target Mass (tons)
   2.2
   4.3
- Time-of-Flight detector around new tracker

![](_page_14_Figure_7.jpeg)

![](_page_14_Figure_8.jpeg)

## ND280-upgrade

Our group is heavily involved in the new Horizontal TPC fir the ND280 upgrade

#### COMSOL simulations:

- Good E filed uniformity up to 10-4
- Non uniformity <10 mm from the field strips</p>
- 2020-2021: CAD design and MOLD produced for the HTPC at the mechanical workshop here in Bari
- 2022-2023: final design and construction of HTPCs, assembling, integration and test at CERN and J-PARC
- Leading role in the ND280-upgrade global reconstruction

![](_page_14_Figure_17.jpeg)

## Super-Kamiokande and Hyper-Kamiokande

![](_page_15_Picture_1.jpeg)

![](_page_15_Picture_2.jpeg)

![](_page_15_Figure_3.jpeg)

![](_page_15_Picture_4.jpeg)

![](_page_15_Picture_5.jpeg)

Electronics at INFN

Participation to the SK refurbishment operations in Japan
 Proton decay channel analysis

$$\stackrel{\scriptstyle \odot}{=} \mathbf{p} \rightarrow \mathbf{v} \mathbf{K}^+ \rightarrow \mathbf{v} \mathbf{\pi}^+ \mathbf{\pi}$$

design Multi-PMTs for H-K (INFN+Poliba)

![](_page_15_Figure_10.jpeg)

# **F2K oscillation results**

#### Collected data analyzed

![](_page_17_Figure_1.jpeg)

### **Analysis Model**

T2K Run 1-10 Prelimi

![](_page_18_Figure_2.jpeg)

#### SK $v_e$ and $\bar{v}_e$ data and PMNS predictions

![](_page_19_Figure_1.jpeg)

#### Nature paper results (2019)

![](_page_20_Figure_1.jpeg)

#### New results: T2K vs T2K + Reactor

δ<sub>CP</sub> 3 T2K produces results with only T2K Reactor Constraint data and with the global reactor 2 constraint on  $\theta_{13}$ . T2K only 90% ----- T2K only 68% T2K only Best Fit **T2K ONLY result is consistent with** 0 reactor constraint to  $I\sigma$ . T2K+Reactor 90% -1 T2K+Reactor 68% -2 T2K+Reactor Best Fit **Results from here onward are** -3 with REACTOR CONSTRAINT 0.01 0.02 0.03 0.04 0.05 0.06 0.07 **APPLIED.**  $sin^2\theta_{13}$ 

PDG 2019 reactor constraint: https://pdg.lbl.gov/2019/reviews/rpp2019-rev-neutrino-mixing.pdf T2K Run 1-10

#### New results and comparison with other experiments

![](_page_22_Figure_1.jpeg)

![](_page_23_Picture_0.jpeg)

## T2K phase II with beam and ND280 upgrade (2022)

![](_page_24_Figure_1.jpeg)

![](_page_24_Figure_2.jpeg)

Solution Agreements signed with NOvA and T2K collaborations and work on joint fits have begun Solution Very different sensitivities, may break apart degeneracies.

- KEK now has budget for collecting **10<sup>22</sup> POT** with the second phase of T2K
- Continued rich physics program and improved oscillation sensitivity until Hyper-K and DUNE (expected 5σ sensitivity to δ<sub>cp</sub>)

#### Conclusions

- T2K has the world leading result for δ<sub>cp</sub> measurement (we exclude 35% of δ<sub>cp</sub> values at 3σ)
- $\frac{1}{2}$  Preference for upper octant  $\theta_{23}$  and Normal Ordering
- Slight preference for non maximal sin<sup>2</sup> $\theta_{23}$  mixing
- Next step T2K-II (ND280 and beam upgrade), long term Hyper-Kamiokande approved by MEXT and under construction
- Final INFN approval is expected by the end of this year
- Lots of exciting work and results to come in the next few years!

![](_page_25_Figure_7.jpeg)

![](_page_25_Picture_8.jpeg)

# Backup

#### The neutrino beam: flux predictions

Fluxes are predicted from a data-driven simulation → NA61/SHINE experiment measures hadron production cross sections using a thin carbon and a T2K replica target

![](_page_27_Figure_2.jpeg)

### SK-V with Gd

![](_page_28_Figure_1.jpeg)

#### Analysis strategy

![](_page_29_Figure_1.jpeg)

#### ND280 samples in v and $\bar{v}$ beam mode (post-ND280 fit)

![](_page_30_Figure_1.jpeg)

#### Samples collected at Super-Kamiokande

3000

![](_page_31_Figure_1.jpeg)

Reconstructed v energy (MeV)

	$\delta_{\rm CP} = -\pi/2$	$\delta_{\rm CP} = 0$	$\delta_{\rm CP} = \pi/2$	$\delta_{\rm CP} = \pi$	Data
FHC $1R\mu$	356.48	355.76	356.44	357.27	318
RHC $1R\mu$	138.34	137.98	138.34	138.73	137
FHC 1Re	97.62	82.44	67.56	82.74	94
RHC 1Re	16.69	18.96	20.90	18.63	16
FHC 1R $\nu_e \text{ CC1}\pi^+$	9.20	8.01	6.51	7.71	14
FHC 1R $\mu$ ( $E_{\rm rec} < 1.2 {\rm GeV}$ )	213.40	213.06	213.36	213.81	191
RHC 1R $\mu$ ( $E_{\rm rec} < 1.2 {\rm GeV}$ )	68.53	68.34	68.53	68.74	71

 $\mathbf{\tilde{\Psi}}$ Data prefer  $\delta_{CP}$  inducing the largest v- $\bar{v}$ asymmetry: -π/2 **Differences in µ-like events** are consistent with statistical and systematic errors

Oscillation and systematic parameters are shared between the 5 samples Fit simultaneously the 5 samples to maximize the sensitivity to the oscillation parameters

Error reduction with near detector fit on the number of expected events at SK

- $v_{\mu}$  event rate uncertainty from 11% to 3% Ŏ
- ve event rate uncertainty from 13% to 5%

#### What is new in the current analysis

![](_page_32_Figure_1.jpeg)

### $\delta_{cp}$ constraints

![](_page_33_Figure_1.jpeg)

CP conserving values (0,  $\pi$ ) excluded at 90% C.L. but  $\pi$  not quite at 2 $\sigma$ 

35% of all values excluded at  $3\sigma$  when marginalised over both hierarchies

#### Atmospheric parameters

![](_page_34_Figure_1.jpeg)

#### **Posterior Probabilities**

	$\sin^2 heta_{23} < 0.5$	$\sin^2 heta_{23} > 0.5$	Sum
NO $(\Delta m_{32}^2 > 0)$	0.195	0.613	0.808
IO $(\Delta m^2_{32} > 0)$	0.034	0.158	0.192
Sum	0.229	0.771	1.000

## Systematic uncertainties

Pre ND280 constraint

	$\ $ 1R $\mu$			$1\mathrm{R}e$		
Error source (units: $\%$ )	FHC	RHC	FHC	RHC	FHC CC1 $\pi^+$	FHC/RHC
Flux	5.1	4.7	4.8	4.7	4.9	2.7
Cross-section (all)	10.1	10.1	11.9	10.3	12.0	10.4
SK+SI+PN	2.9	2.5	3.3	4.4	13.4	1.4
Total	$\parallel 11.1$	11.3	13.0	12.1	18.7	10.7

#### Post ND280 fit

	1]	$\parallel 1 \mathrm{R} \mu \parallel$				
Error source (units: %)	$\parallel$ FHC	RHC	FHC	RHC	FHC CC1 $\pi^+$	FHC/RHC
Flux Xsec (ND constr)	$\begin{array}{ c c } 2.9\\ 3.1 \end{array}$	$\begin{array}{c} 2.8\\ 3.0 \end{array}$	$\begin{vmatrix} 2.8 \\ 3.2 \end{vmatrix}$	$2.9 \\ 3.1$	2.8 $4.2$	$\begin{array}{c} 1.4 \\ 1.5 \end{array}$
Flux+Xsec (ND constr) Xsec (ND unconstrained) SK+SI+PN	$ \begin{array}{ c c c } 2.1 \\ 0.6 \\ 2.1 \\ \end{array} $	$2.3 \\ 2.5 \\ 1.9$	$ \begin{array}{c c} 2.0 \\ 3.0 \\ 3.1 \end{array} $	$2.3 \\ 3.6 \\ 3.9$	$4.1 \\ 2.8 \\ 13.4$	$ \begin{array}{c c} 1.7 \\ 3.8 \\ 1.2 \end{array} $
Total	3.0	4.0	4.7	5.9	14.3	4.3

## T2K vs NOvA

![](_page_36_Figure_1.jpeg)

#### Comparison with other experiments

![](_page_37_Figure_1.jpeg)

 $\Delta m^2_{32} \ [eV^2/c^4]$ 

Theory may explain differences between T2K and NOvA on  $\delta_{cp}$ 

## NSI bring the estimates of $\delta_{CP}$ in agreement

![](_page_38_Figure_2.jpeg)

Contours obtained for the best fit of T2K + NOvA:  $[\varepsilon_{e\mu} = 0.15, \phi_{e\mu} = 1.38\pi]$ 

#### T2K region almost unaltered

NOvA region strongly modified

![](_page_38_Picture_6.jpeg)

#### Theory may explain differences between T2K and NOvA on $\delta_{cp}$

### **Biprobability plots in the presence of NSI**

![](_page_39_Figure_2.jpeg)

![](_page_39_Picture_3.jpeg)

#### Theory may explain differences between T2K and NOvA on $\delta_{cp}$

## Can the tension be resolved assuming IO?

![](_page_40_Figure_2.jpeg)

For IO the best fit of  $\delta_{CP}$  is the same in T2K and NOvA (left panel).

However, IO gains only  $\chi^2_{IO} - \chi^2_{NO} \sim -2$  in T2K + NOvA combination (middle panel). The reason is that T2K disfavors IO (dotted ellipses) (right panel). T2K and NO<sub>V</sub>A disappearance channel + Reactors prefer NO ( $\chi^2_{IO} - \chi^2_{NO} \sim 4$ ).

SK atmospheric data (v 2020) prefer NO ( $\chi^2_{IO}$  -  $\chi^2_{NO}$  ~ 3).

#### Therefore, IO seems not to be the favored solution

![](_page_40_Picture_7.jpeg)

## Hyper-Kamiokande Experiment

![](_page_41_Picture_1.jpeg)

OHyper-K detector will be built with 8.4 times larger fiducial mass (190 kiloton) than Super-K and will be instrumented with double-sensitivity PMTs

J-PARC neutrino beam will be upgraded from 0.5 to 1.3 Mega Watt x8 Natural Neutrino Rate and x20 Accelerator Neutrino Rate

New (IWCD) and upgraded (@280m) near detectors to control systematic errors

![](_page_41_Figure_5.jpeg)

## Hyper-Kamiokande

# Broad Science and Discovery Potential

Matter Antimatter asymmetry:

**Provide CP conservation exclusion versus**  $\delta_{CP}$ 

Large samples provide high statistics

Limited by systematics

<sup>O</sup>Pin down the  $\delta_{CP}$  size with a  $10^{\circ} - 20^{\circ}$  accuracy

Proton decay: Best capability to

address proton decays Only realistic approach beyond proton lifetime of  $10^{35}$  years

![](_page_42_Figure_9.jpeg)

![](_page_42_Figure_10.jpeg)

Unique astrophysical capabilities to address: Tension in solar neutrinos Supernova neutrino observation and capability to provide direction at 1°

T2K Collaboration Meeting

## Towards T2K phase II: ND280 upgrade

![](_page_43_Figure_1.jpeg)

- Goal of the upgrade project: replace the P0D with an **horizontal totally active target** (SuperFGD) and **2 horizontal TPCs** equipped with resistive MicroMegas by 2021
- Increase the current phase-space and reduce the cross-section systematics
- Currently working on R&D and prototypes + simulations

![](_page_43_Picture_5.jpeg)

![](_page_43_Figure_6.jpeg)

#### Neutrino cross sections at T2K energies

![](_page_44_Figure_1.jpeg)

NEUT 5.4.0

----- NuWro 19.02

GENIE 2.12.10 (x2=16.319)

(χ<sup>2</sup>=14.634)

 $(\chi^2 = 32.077)$ 

T2K FHC 11.92  $\times 10^{20}$  POT

T2K RHC 6.29 × 10<sup>20</sup> POT

**0° <= θ <= 45°** 

- At T2K energies the favoured interactions are CCQE Other neutrino interactions with production of **pions** in the final state are important as well
  - Discrepancies between different theoretical models
  - x-sec are not completely understood at T2K energies

#### Latest x-sec measurement at ND280:

- $v_{\rm e}$  and  $\bar{v}_{\rm e}$  measurement crucial for CPV
- $v_{\mu}/\bar{v}_{\mu}$  important for oscillation analysis
- Carbon/Oxigen Crucial for ND280 (CH, O) to SK (H<sub>2</sub>O) extrapolation

![](_page_44_Figure_9.jpeg)

![](_page_44_Figure_10.jpeg)

![](_page_44_Figure_11.jpeg)

#### $v_{\mu}$ and $\bar{v}_{\mu}$ disappearance results

Constraints on the atmospheric parameters:  $\theta_{23}$  and  $\Delta m_{31}^2$ 

![](_page_45_Figure_2.jpeg)

#### **Event selection at Super-Kamiokande**

v beam mode

![](_page_46_Figure_2.jpeg)

NC

A well understood selection/detector

# Two flavour V oscillation in vacuum

Considering two flavor  $v_{\alpha}$  and  $v_{\beta}$  the PMNS matrix become a 2 X 2 matrix:  $\mathbf{U} = \begin{pmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{pmatrix}$ 

Flavour eigenstate are superposition of mass eigenstates:

 $|\nu_{\alpha}\rangle = |\nu_{1}\rangle \cos{(\theta)} + |\nu_{2}\rangle \sin{(\theta)}, \quad \alpha = e, \mu, \tau$ 

The Schrödinger equation implies that massive neutrino eigenstate evolves in time as plane wave, so:

 $|\nu_{\alpha}(t)\rangle = |\nu_{1}\rangle e^{-iE_{1}t}\cos\left(\theta\right) + |\nu_{2}\rangle e^{-iE_{2}t}\sin\left(\theta\right)$ 

in the ultrarelativistic neutrinos ( $E = |\vec{p}|$ , t = L), it is possible to approximate:

 $E_k = \sqrt{\vec{p}^2 + m_k^2} \simeq E + \frac{m_k^2}{2E} \qquad E_k - E_j \simeq \frac{\Delta m_{kj}^2}{2E}, \ \Delta m_{kj}^2 \equiv m_k^2 - m_j^2$ 

Then the probability that a  $v_{\alpha}$  becomes a  $v_{\beta}$  is given by:

$$P(\nu_{\alpha} \to \nu_{\beta}) = |\langle \nu_{\beta} | \nu_{\alpha} \rangle|^2 = \sin^2(2\theta) \sin^2\left(\Delta m^2 \frac{L}{4E}\right)$$

Introducing the speed of light and the Plank costant:

$$P(\nu_{\alpha} \rightarrow \nu_{\beta}) = \sin^{2} 2\theta \times \sin^{2} \left(1.27 \frac{L[km]}{E[GeV]} \Delta m^{2}[eV^{2}]\right)$$

$$\int_{(I)}^{0} \int_{(I)}^{0} \int_{(I)}^$$

![](_page_47_Figure_12.jpeg)