

Search for a muon EDM with the frozen-spin technique



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Overview

- Physics motivation
- Experimental techniques for muon EDM searches
 - the frozen-spin technique
- A muon EDM search at PSI
 - Possible experimental concepts
 - Ongoing activities
 - Tentative schedule

Physics Motivation

Evidences of New Physics

- Despite its impressive experimental success, the Standard Model (SM) is clearly not a complete theory — New Physics does exist
- Beside cosmological and astrophysical evidences (dark matter, matter-antimatter asymmetry of the Universe), there is at least one purely particle-physics evidence:

Where the neutrino mass comes from?

• This is indeed the most striking aspect of a more general problem:

Where the flavour structure of the SM comes from? (namely, the hierarchy of masses and mixings)

The quest for New Physics

Exploring the intensity frontier appears crucial

٠

- direct look at the flavour problem from many different points of view
- great sensitivity in a scenario where NP could be right above the energy of the next generation of accelerators





Recent news from the intensity frontier (I)



• Hint of Lepton-flavour universality violation (LFUV) in the theoretically and experimentally clean $B^+ \rightarrow K^+ \ell^+ \ell^-$ decays at LHCb

arXiv:2103.11769 [LHCb]

$$R_{K} = \frac{\mathcal{B}(B^{+} \to K^{+} \mu^{+} \mu^{-})}{\mathcal{B}(B^{+} \to J/\psi \, (\to \mu^{+} \mu^{-}) K^{+})} \Big/ \frac{\mathcal{B}(B^{+} \to K^{+} e^{+} e^{-})}{\mathcal{B}(B^{+} \to J/\psi \, (\to e^{+} e^{-}) K^{+})}$$



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Recent news from the intensity frontier (II)

• The long-standing deviation of the anomalous magnetic moment of the muon ($a_{\mu} = g_{\mu} - 2$) from SM predictions have been confirmed by the new FNAL experiment



Phys. Rev. Lett. 126 (2021) 14, 141801





Recent news from the intensity frontier (III)

- Controversial measurements of $\alpha_{\rm em}$ in ¹³³Cs (Berkeley, LBNL) and ⁸⁷Rb (Paris, LKB)
- If the LBNL measurement is taken as good and included in the $(g 2)_e$ SM calculation (at 10th order in QED!!!), there is a 2.4σ discrepancy with respect to the (0.1 ppb!!!) electron EDM measurement



... x 12672

 $\Delta a_e^{\text{LKB}} = a_e^{\text{exp}} - a_e^{\text{LKB}} = (4.8 \pm 3.0) \times 10^{-13}$ $\Delta a_e^{\text{B}} = a_e^{\text{exp}} - a_e^{\text{B}} = (-8.8 \pm 3.6) \times 10^{-13}.$



Muon g-2, electron g-2 and LFUV

Taking the LBNL α_{em} as good:

$$\Delta a_e = a_e^{\text{exp}} - a_e^{\text{SM}} = (-87 \pm 36) \times 10^{-14}$$
$$\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (25.1 \pm 5.9) \times 10^{-10}$$

• The **opposite sign** in the experimental deviations of $(g - 2)_{\mu,e}$ from the SM predictions could indicate an even worse tension and point toward **NP with LFUV**

A. Crivellin, HiMB Physics Case Workshop, PSI, Apr. 2021 A. Crivellin *et al., Phys.Rev.D* 103 (2021) 7, 073002



e.g. Leptoquarks, gauged L_{μ} - L_{τ} symmetry...

Dipole interactions in effective field theories



Dipole interactions in effective field theories



Electric dipole moments



 $\overrightarrow{\mu} = \frac{ge}{2mc}\vec{s}$



Magnetic dipole moment

$$U = -\overrightarrow{\mu} \cdot \overrightarrow{B}$$

P- and T-even

Electric dipole moment

 $U = - \overrightarrow{d} \cdot \overrightarrow{E}$

- EDMs of fundamental particles imply CP violation (CPV)
 - leptons EDM in the SM from CKM phases in loops involving quarks —> very small, not accessible



Muon EDM

Electron and muon EDM

- The need of non-standard CPV sources to explain the matter-antimatter asymmetry of the Universe motivates many searches for EDMs
- Strong constraints exist on the electron EDM (spin precession in molecular systems excited by lasers):



- the muon EDM was somehow experimentally overlooked, due to the indirect constraint coming from the electron EDM under minimal flavour violation (MFV) assumptions

$$|d_e|_{\exp} \le 8 \times 10^{-30} e \,\mathrm{cm}$$

MFV
 $|d_\mu|_{\inf} \le 1.6 \times 10^{-27} e \,\mathrm{cm}$
 $|d_\mu|_{\exp} \le 1.5 \times 10^{-19} e \,\mathrm{cm}$

- Current muon EDM limits produced as by-product of g-2 experiments
- Indeed the existing tensions, pointing toward LFUV, challenge the MFV scenario and make a dedicated experiment to search for a muon EDM of great interest

Experimental techniques for muon EDM searches



Magnetic spin precession in the particle rest frame

$$\overrightarrow{\omega}_L = 2 \overrightarrow{\mu} \cdot \overrightarrow{B^*} / \hbar$$



Electric spin precession in the particle rest frame

$$\overrightarrow{\omega}_{d} = 2 \overrightarrow{d} \cdot \overrightarrow{E^{*}} / \hbar$$
$$\overrightarrow{d} = \frac{\eta e}{2mc} \overrightarrow{s}$$

Electromagnetic spin precession in the laboratory rest frame

$$\begin{split} \vec{\Omega} &= \vec{\Omega}_0 - \vec{\Omega}_c = \frac{q}{m} \left[a\vec{B} - \frac{a\gamma}{(\gamma+1)} \left(\vec{\beta} \cdot \vec{B} \right) \vec{\beta} - \left(a + \frac{1}{1-\gamma^2} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right] \\ &+ \frac{\eta q}{2m} \left[\vec{\beta} \times \vec{B} + \frac{\vec{E}}{c} - \frac{\gamma}{(\gamma+1)c} \left(\vec{\beta} \cdot \vec{E} \right) \vec{\beta} \right]. \end{split}$$



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$$\begin{split} & \overset{\text{Cyclotron}}{\vec{n}} \\ & \vec{\Omega} = \vec{\Omega}_0 - \left(\vec{\Omega}_c \right) = \frac{q}{m} \left[a \vec{B} - \frac{a \gamma}{(\gamma + 1)} \left(\vec{\beta} \cdot \vec{B} \right) \vec{\beta} - \left(a + \frac{1}{1 - \gamma^2} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right] \\ & \quad + \frac{\eta q}{2m} \left[\vec{\beta} \times \vec{B} + \frac{\vec{E}}{c} - \frac{\gamma}{(\gamma + 1)c} \left(\vec{\beta} \cdot \vec{E} \right) \vec{\beta} \right]. \end{split}$$



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Electromagnetic spin precession in the laboratory rest frame

Cyclotron frequency

Thomas-Bargmann-Michel-Telegdi Equation (T-BMT)

$$\begin{split} \vec{\Omega} &= \vec{\Omega}_0 - \left(\vec{\Omega}_c \right) = \frac{q}{m} \left[a\vec{B} - \frac{a\gamma}{(\gamma+1)} \left(\vec{\beta} \cdot \vec{B} \right) \vec{\beta} - \left(a + \frac{1}{1-\gamma^2} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right] \\ &+ \frac{\eta q}{2m} \left[\vec{\beta} \times \vec{B} + \frac{\vec{E}}{c} - \frac{\gamma}{(\gamma+1)c} \left(\vec{\beta} \cdot \vec{E} \right) \vec{\beta} \right]. \end{split}$$



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EDM contribution

Muon g-2 measurements in storage rings

- Thanks to parity violation, the *horizontally precessing* spin is reflected into the angular distribution of electrons produced in muon decays
- Counts on detectors at a given angle oscillate with frequency Ω



e'V.V.

Muon EDM from g-2 experiments

- Search for vertical precession due to the "relativistic" electric field observed by the muon in its rest frame, $\overrightarrow{E^*} = \gamma c \overrightarrow{\beta} \times \overrightarrow{B} \sim 13.5 \text{ GV/m}$
- Although the experiments are not optimised for this measurement, the vertical granularity of the detectors combined with such a huge field still allows a precise measurement of the muon EDM

$$\begin{split} |d_{\mu}|_{\exp} &\leq 1.5 \times 10^{-19} \, e \, \mathrm{cm} \\ \hline Phys.Rev.D \ 80 \ (2009) \ 052008 \ [BNL \ Muon \ g-2]} & \gamma &\simeq 1/\sqrt{a} \\ \vec{\beta} \perp \vec{B} & \vec{p} \simeq 3.09 \ GeV/c \\ (\text{``magic'' momentum}) \\ \vec{\Omega} &= \vec{\Omega}_{0} - \vec{\Omega}_{c} = \frac{q}{m} \left[a\vec{B} - \frac{a\gamma}{(\gamma+1)} (\vec{\beta} \cdot \vec{B}) \vec{\beta} - \left(a + \frac{1}{1 - \gamma^{2}}\right) \vec{\beta} \times \vec{E} \\ + \frac{\eta q}{2m} \left[\vec{\beta} \times \vec{B} \right] + \frac{\vec{E}}{c} - \frac{\gamma}{(\gamma+1)c} \left(\vec{\beta} \cdot \vec{E} \right) \vec{\beta} \right]. \quad \text{Small} \end{split}$$

Farley at al., Phys. Rev. Lett. 93 (2004) 052001 Adelmann et al., J. Phys. G 37 (2010), 085001

The frozen spin technique

- An electric field is applied to cancel the horizontal precession
- For $\eta = 0$, the spin is locked parallel to the momentum (as it has been produced in π decays)
- Search for a vertical precession due to a nonnull EDM in the relativistic electric field



$$\vec{\beta} \perp \vec{B} + \text{apply an electric field } E_f \simeq aBc\beta\gamma^2 \text{ so that}$$

$$a\vec{B} = \left(a - \frac{1}{\gamma^2 - 1} \frac{\vec{\beta} \times \vec{E}}{c}\right)$$

$$\vec{\Omega} = \vec{\Omega}_0 - \vec{\Omega}_c = \frac{q}{m} \left[a\vec{B} - \frac{a\gamma}{(\gamma+1)} \left(\vec{\beta} \cdot \vec{B}\right) \vec{\beta} - \left(a + \frac{1}{1 - \gamma^2}\right) \frac{\vec{\beta} \times \vec{E}}{c}\right]$$
"Relativistic" $\left(\frac{\eta q}{2m} \left[\vec{\beta} \times \vec{B}\right] + \frac{\vec{E}}{c} - \frac{\gamma}{(\gamma+1)c} \left(\vec{\beta} \cdot \vec{E}\right) \vec{\beta}\right]$. Small

Experimental signal: up/down asymmetry



Sensitivity from the asymmetry averaged over

a couple of muon lifetimes γau_{μ}

$$\sigma(|d_{\mu}|) = \frac{d|d_{\mu}|}{d\overline{A}} \sigma(\overline{A}) \sim \frac{a\hbar\gamma}{2P_{0}E_{f}\sqrt{N}\tau_{\mu}\alpha}$$

The "PENTA" formula

 P_0 = initial polarisation degree E = electric field in the lab frame N = number of observed decays τ_{μ} = muon lifetime α = mean decay asymmetry (~ 0.3)

A muon EDM search at PSI

The Paul Scherrer Institute (PSI)



• The largest Swiss research institute for fundamental and applied science, with a strong multidisciplinary mission and operating large, world-leading user facilities



Swiss Spallation Neutron Source (SINQ)

Swiss Light Source (SLS)

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The proton accelerator complex at PSI



- One of the most intense proton beams in the world (2.2 mA, 1.3 MW, 50 MHz RF)
- Producing the most intense continuous muon beams in the world (up to 10⁸ μ/s)
 - μ from π decays (highly polarised & time distribution flattened by the π lifetime)
 - 15-500 MeV/c
- Several beam lines with different specs and applications (particle physics, muonic atoms, material science)

Muon beams at PSI (a few examples)

- The muonEDM sensitivity improves with increasing muon intensity and $E_f/\gamma \propto \gamma$
- **πE5**:
 - pions and muons, high intensity, **low energy**, e.g. surface muons (28.4 MeV/c muons produced by pions decaying at rest on the surface of the proton target) up to $10^8 \,\mu/s$
 - ideal for muon decay studies (e.g. LFV)
- π**E1**:
 - medium intensity pions, muons and electrons from 10 to 500 MeV/c
 - very good momentum resolution (down to 0.26%)
 - often used as a beam test facility
- µE1:
 - high intensity muon beam with very low pion and electron contamination
 - provides the **highest muon rates at high momentum** (typically 125 MeV/c)
 - mainly used for µSR experiments

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- π**E1**:
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The muonEDM Lol

• A Lol for a Muon EDM experiment was presented in January 2021 to the PSI Research Committee for Particle Physics



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Experimental approach



The μ E1 beam line

- Up to $10^8 \,\mu/s @ 125 \,MeV/c$
- Emittance (1σ) :
 - 945 mm·mrad horizontal

Vertical Phase Space @SciFi

0

-5

5

10

15

y [mm]

α = 1.93749

β = 0.379402 [m]

∈ = 716.426 [mm⋅mrad]

- 716 mm·mrad vertical
- > 93% polarization

y' [mrad]

60

40

20

0

-20-

-40

-60

-80

-15

-10



Experimental concepts — Storage ring

- Compact storage ring with lateral injection through a magnetic channel
- Need a kick within 1 revolution

 (10 ns) to avoid hitting the injection
 channel after 1 turn
- In principle, 0.14% injection efficiency is possible



Experimental concepts — Storage ring

- Compact storage ring with lateral injection through a magnetic channel
- Need a kick within 1 revolution

 (10 ns) to avoid hitting the injection channel after 1 turn
- In principle, 0.14% injection efficiency is possible
- In practice, before the orbit stabilises, muons are lost due to MS through the E-field electrodes
 - efficiency ~ 10⁻⁴
 - positron detection rate ~ 10 kHz



Experimental concepts — Helix muonEDM

- Vertical injection into a 3T solenoid
- Also need a kick to stabilise the orbit in the central region, but within > 50 ns
- No material along the muon trajectories



Injection channel







Magnetic field kicker



Magnetic field along the nominal trajectory



N.B. due to the necessity of a kick and the continuous structure of the beam, **only one muon at a time can be stored**



















200

400

600

0

-0.02

-0.04

-0.06

-600

-400

-200

0

vertical position /mm

Generated initial phase space points Initial phase space points of muons decaying in the central region

Efficiency ~ 5 x 10⁻⁴

- Detection rate ~ 50 kHz
- Looks promising, but still a lot of room for improvements.
- Contributions and new ideas are welcome!

100

80

60

The Detector — Entrance trigger

- A muon detector with reasonable timing performances (~ ns) is needed at the entrance to:
 - set the T₀ for the precession measurement
 - trigger the magnetic kick
 - start the measurement cycle
- O(10 MHz) muons pass the injection channel, only O(60 kHz) are in a phase space region that allows the capture:
 - to avoid a large dead time, need to trigger only muons that can be captured





To the solenoid

Anti-coincidence between entrance and lateral scintillators

Only muons on a trajectory close to the nominal one will be triggered

The Detector — Muon tagger

- Among triggered muons, there will be still some with a relatively large vertical angle in the measurement region
 - the measurement of the decay angle can be biased
- A muon tracker/tagger can identify such events for a proper treatment
 - needs σ(θ) ~ 1 mrad —> very precise and very light





- Design derived from Mu3e $(\mu^+ \rightarrow e^+ e^+ e^- @ PSI)$

The Detector — End signals

- The measurement has to be stopped as early as possible to allow a new entrance trigger and avoid dead time
- Stop signal should arrive when:
 - a positron from the muon decay is detected
 - the muon exits the measurement region
- Fast scintillators to:
 - measure the decay time
 - lift the veto for a subsequent entrance trigger
 - identify muons exiting the measurement region before decaying



Systematic uncertainties

- The main sources of systematic uncertainties were discussed in the paper by Farley *et al.*
 - 1. $B_r \neq 0$
 - 2. Misalignment of B and E planes
 - 3. Electric field not on a plane —> magnetic precession in the rest frame —> vertical precession in the lab frame
 - 4. Residual (g-2) precession + locally nonhorizontal orbit = vertical precession
 - 5. $B_{\theta} \neq 0$
 - 6. Early-to-late detector effects

Vertical orbit oscillations! Average to 0, but can deteriorate the quality of the asymmetry fit

Can be canceled by comparing clockwise (CW) and counter-clockwise (CCW) injection

CW vs. CCW

+ Single muon storage avoids high detector rates changing with time + injection effects measured without muons

Sensitivity and Physics reach (1 year run)

- a = 1.12 x 10⁻³
- $\gamma = 1.55$
- $P_0 = 0.93$
- E = 2 MV/m
- $N = 50 \text{ MHz} \times 200 \text{ days} = 7 \times 10^{11}$
- $\tau = 2.2 \times 10^{-6} \text{ s}$
- $\alpha = 0.3$

$$\sigma(|d_{\mu}|) \le 6 \times 10^{-23} e \cdot \mathrm{cm}$$

$$\sigma(|d_{\mu}|) = \sim \frac{a\hbar\gamma}{2P_{0}E_{f}\sqrt{N}\tau_{\mu}\alpha}$$



Challenges

- Fast injection & injection trigger
- Field uniformity and characterisation
- Detectors in high E & B fields
- Minimal material budget

Tentative Schedule

	2021	2022	2023	2024	2025	2026	2027	2028	2029	2030
Conceptional design		0	•							
Technical design			1							
R&D			•							
Construction					2					
Commissioning					•					
Data taking						3				
Analysis						•			4	•
Preparation phase II									•	
Phase II at HIMB/muCool								beyond 20)30	ļ

- An intermediate phase with a demonstrator to be installed on a mediumintensity beam line is being considered
 - the present limit could be challenged in a very short time scale
- PSI is considering an upgrade of the muon beam lines (HiMB, $10^{10} \,\mu/s$)
 - combined with innovative beam-cooling approaches (muCool), a much higher injection probability could be reached

Conclusions

- In a scenario where several hints of NP with LFUV are arising, a dedicated experiment to search for a muon EDM is highly desirable
- Excellent prospects for a ground-breaking muon EDM experiment at PSI within this decade
 - improving the present limit by 3 orders of magnitudes, down to
 6 x 10⁻²³ e ⋅ cm per year
 - improving the expected limit from FNAL g-2/EDM by a factor 20
- Excellent long term prospects with the upgrade of the PSI beam lines
- Still in a conceptual design phase, many challenges to face, a lot of room for new ideas and new contributions

Backup

muCool



The HiMB Project @ PSI

- PSI is designing a high intensity muon beam line (HiMB) with a goal of ٠ ~ $10^{10} \,\mu$ /sec (x100 the MEG-II beam)
- Optimization of the beam optics: •
 - improved muon capture efficiency at the production target
 - improved transport efficiency to the experimental area -

x4 μ capture eff. $x6 \mu$ transport eff.

1.3 x 10¹⁰ µ/s

in the experimental area with 1400 kW beam power

