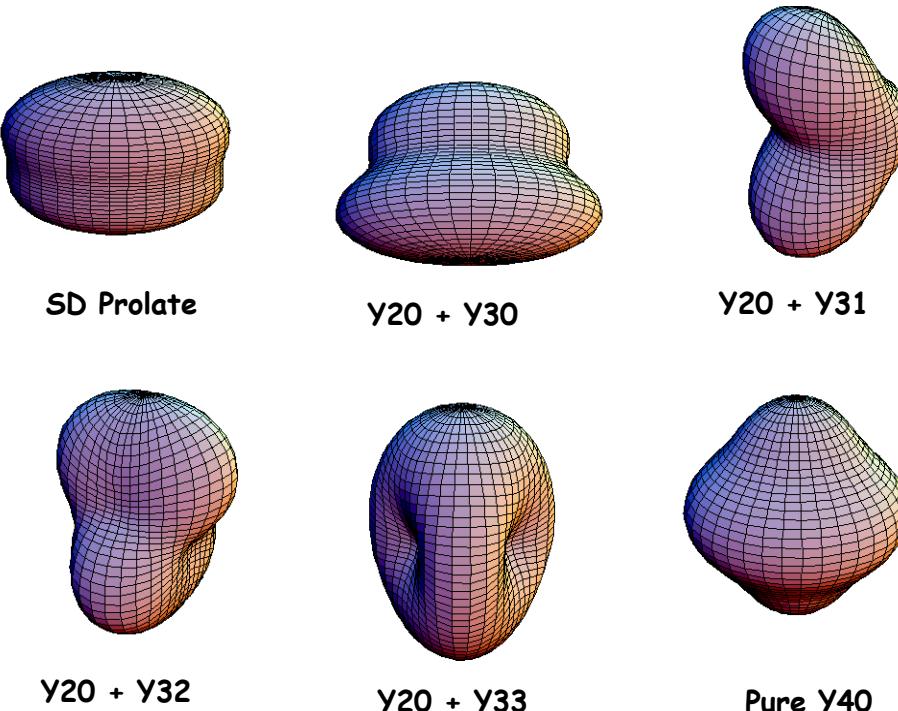


# SPES-LOI: Search for Exotic-Octupole deformation effects in n-rich Ce-Xe-Ba Nuclei



*Spokesperson: E. Sahin, D. Curien, J. Dudek, M. Zielinska, G. de Angelis*

*INFN, Laboratori Nazionali di Legnaro, Italy*

*IPHC Strasbourg, France*

*University of Warsaw, Poland*

*Marie-Curie-Skolodwska University, Lublin, Poland*

*Polish Academy of Science, Crakow, Poland*

*INFN, Sezione di Firenze, Italy*

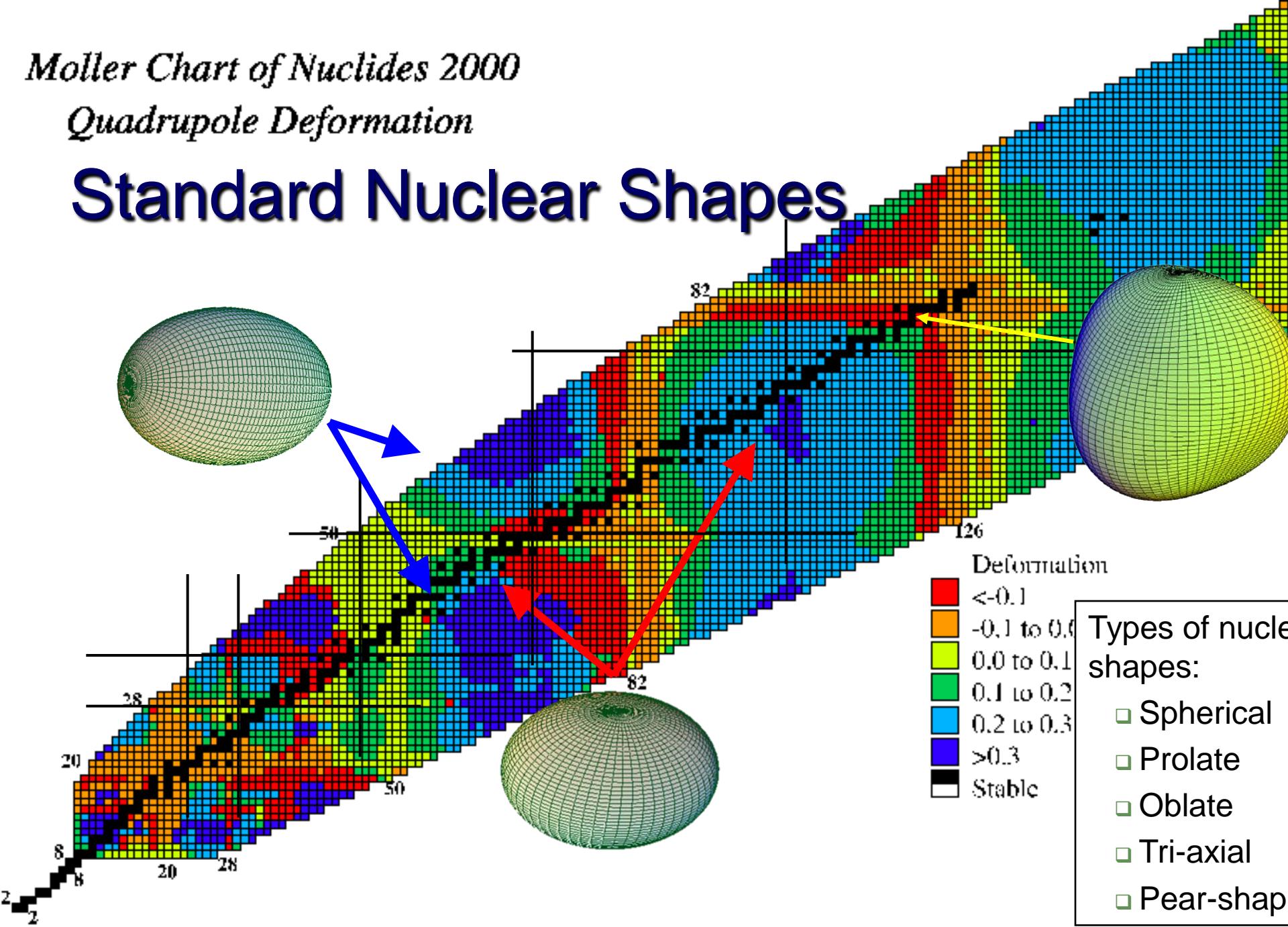
*Inter University Accelerator Center, Delhi, India*

*Bulgarian Academy of Science, Sofia, Bulgaria*

# Moller Chart of Nuclides 2000

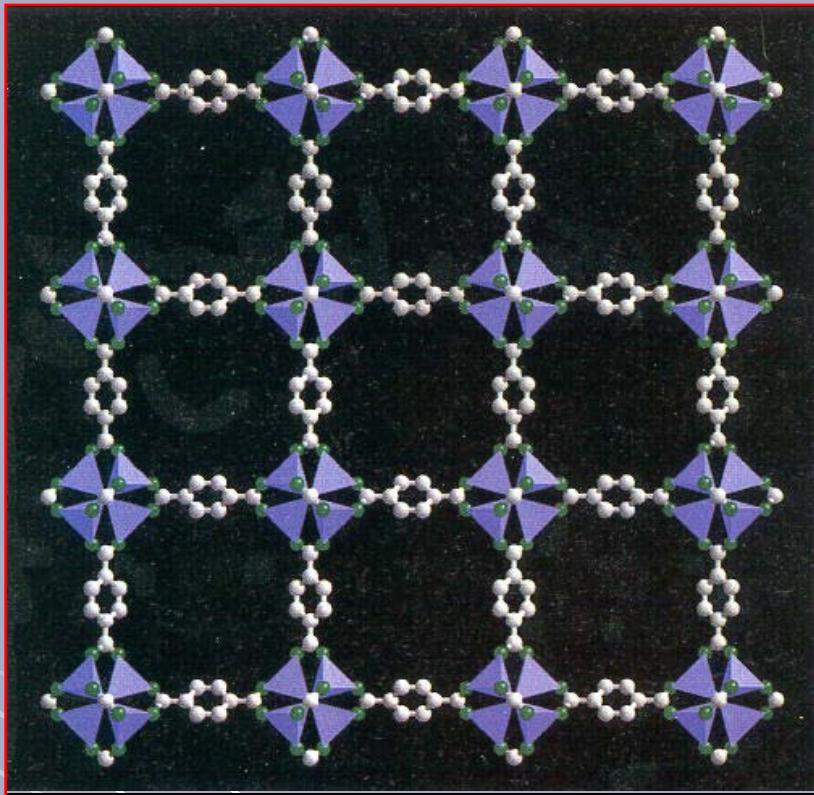
## Quadrupole Deformation

# Standard Nuclear Shapes

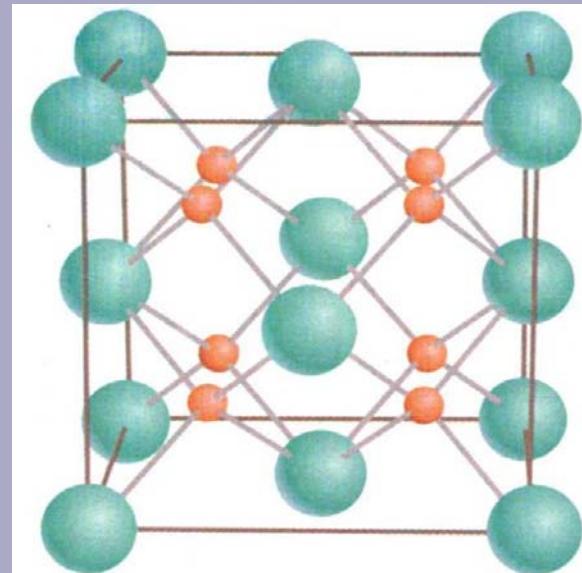
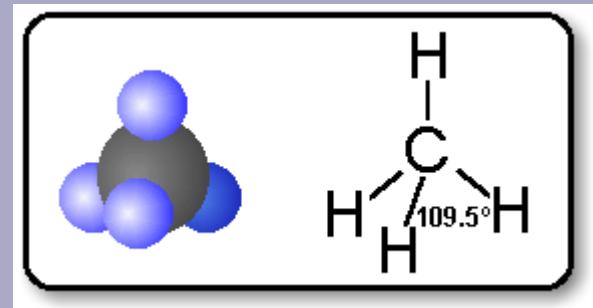


- Types of nuclear shapes:
- Spherical
  - Prolate
  - Oblate
  - Tri-axial
  - Pear-shape

# Point Symmetries in the Microscopic World



*Synthetic inorganic-organic compound with ZnO<sub>4</sub> tetrahedral clusters linked by C<sub>6</sub>H<sub>4</sub>-C-O<sub>2</sub> “struts” (Li, Nature, 1999). 1.29 nm spacing between centers of adjacent clusters.*



*Face-centered-cubic (fcc) crystal structure of PuO<sub>2</sub> (Pu atoms in green, O atoms in red).*

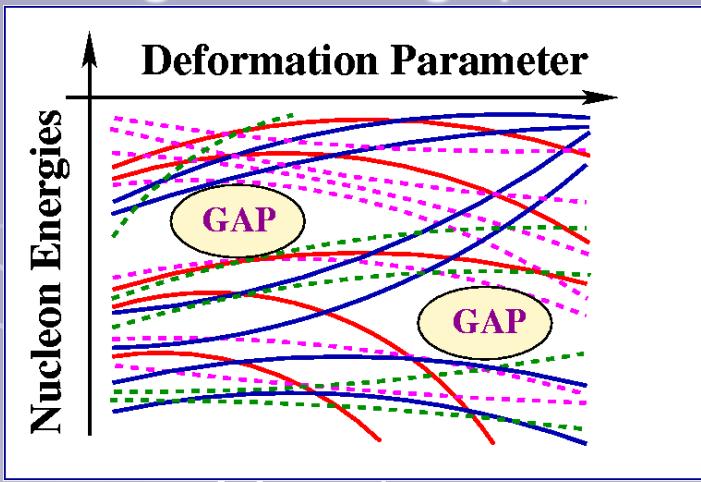
# Point Symmetries and Nuclear Stability

- **Shell Gaps**

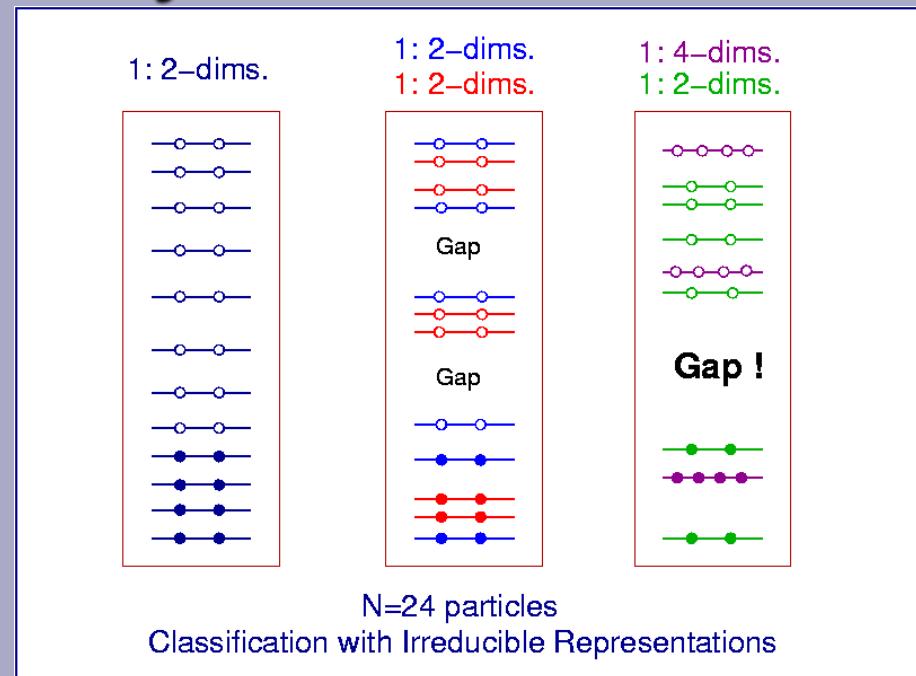
⇒ Stable configurations

- In nuclei:

Higher degeneracies ⇒  
Larger shell gaps



J. Dudek, A. Góźdź, N. Schunck and M. Miskiewicz  
Phys. Rev. Lett. **88** 252502 (2002)



Degeneracies are a direct consequence of the underlying point symmetry of the shape

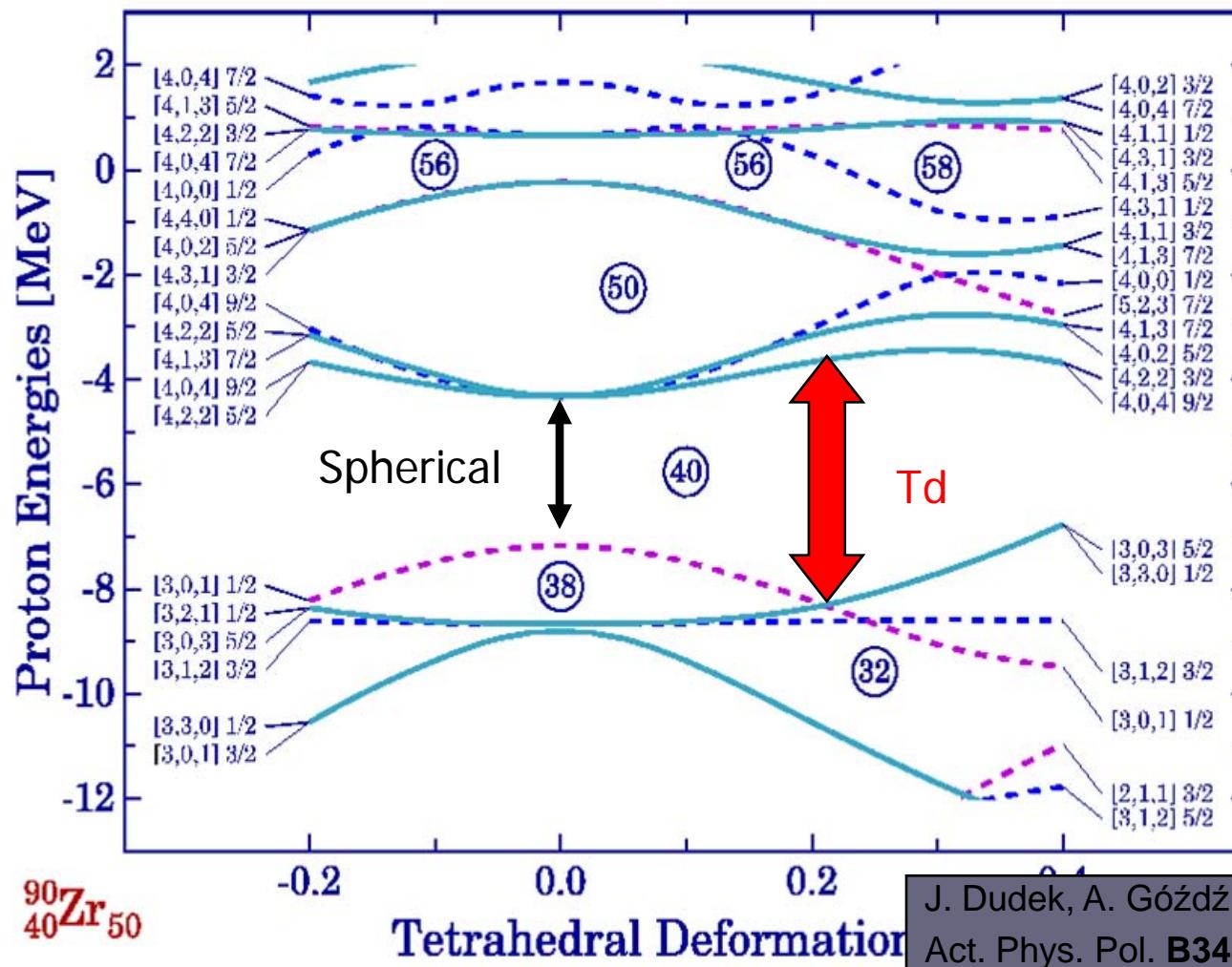
# Point Groups and Level Degeneracy

Properties	High symmetries			Low symmetries
Type	Spherical	Tetrahedral	Octahedral	Any other...
Number of Symmetry Elements	$\infty$	48	96	...
New Degeneracies	$2j + 1$	4, 2, 2	4, 2, 2 4, 2, 2	2, 2

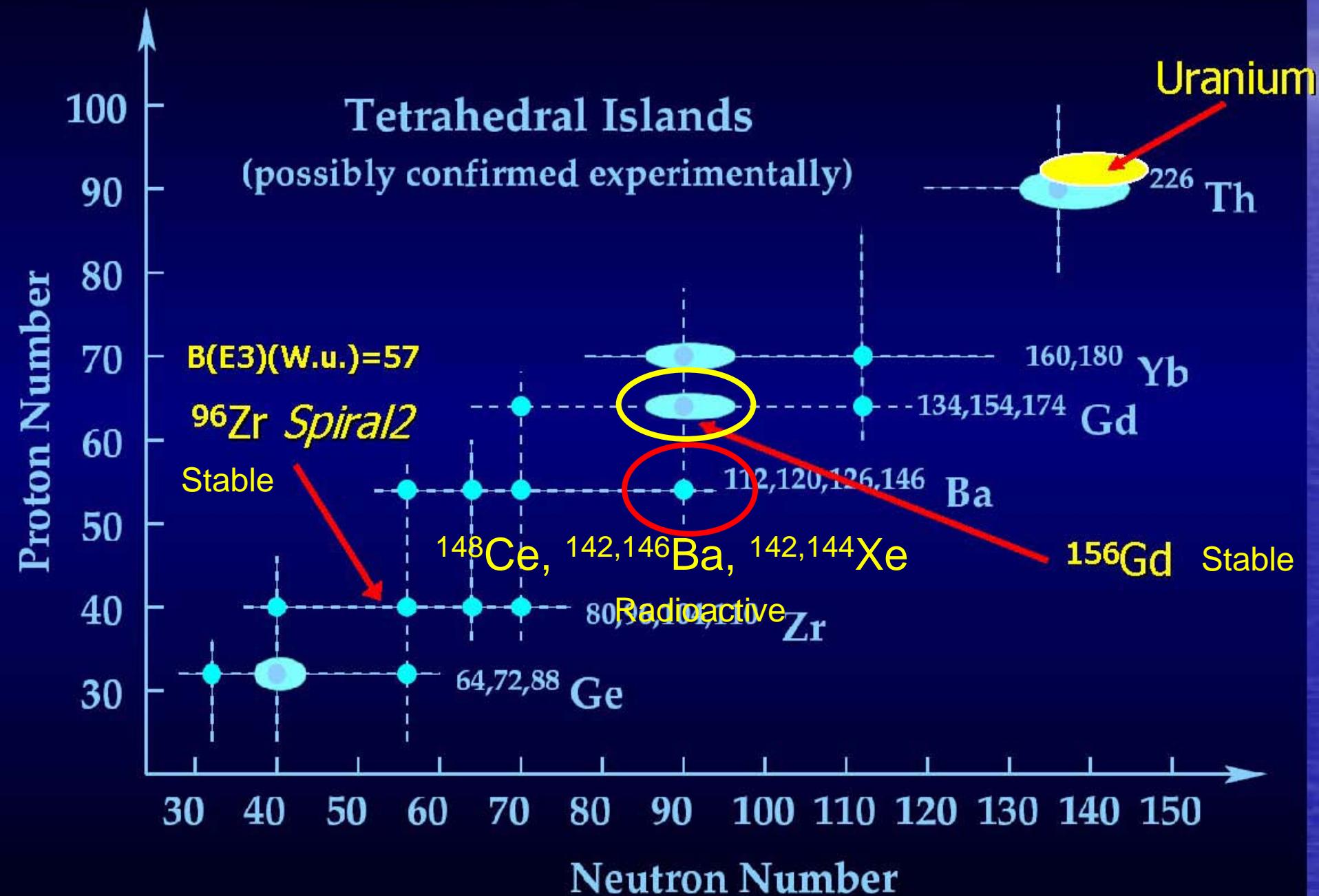
**Kramers Degeneracy (= time-reversal symmetry)**

*Survey of the properties of a few point groups*

# Tetrahedral Shell Gaps

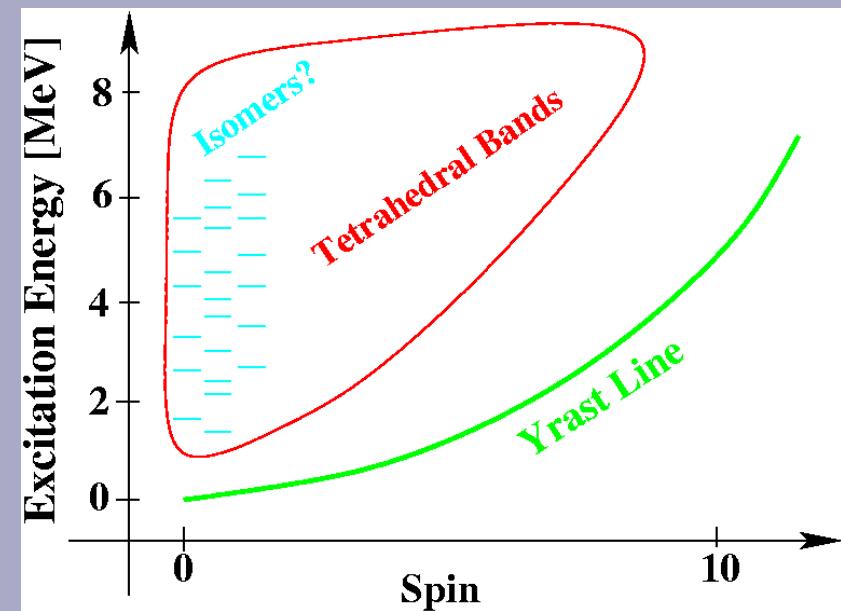
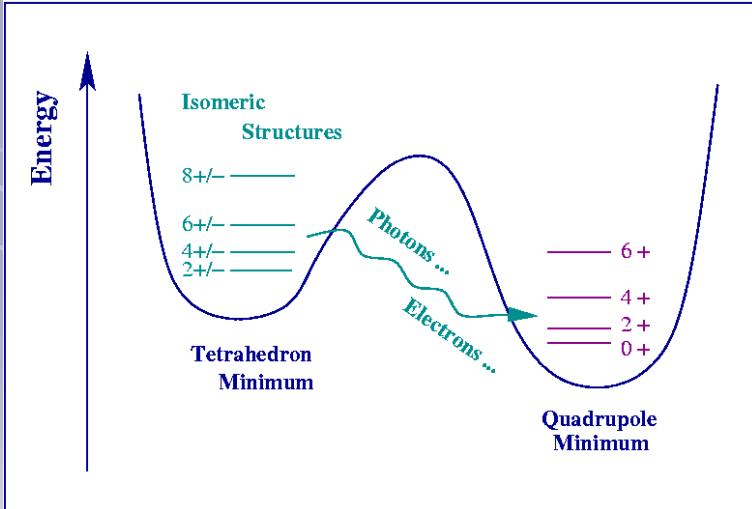


J. Dudek, A. Góźdź and N. Schunck  
Act. Phys. Pol. **B34** 2491 (2003)



# Experimental signatures (1/2)

- Stable tetrahedral minimum: **Shape isomer**
- **Low-spin physics**: don't expect  $I > 10 \hbar \dots$
- Vanishing **quadrupole moment  $Q_2$**
- Static **octupole moment  $Q_3$**
- No dipole moment



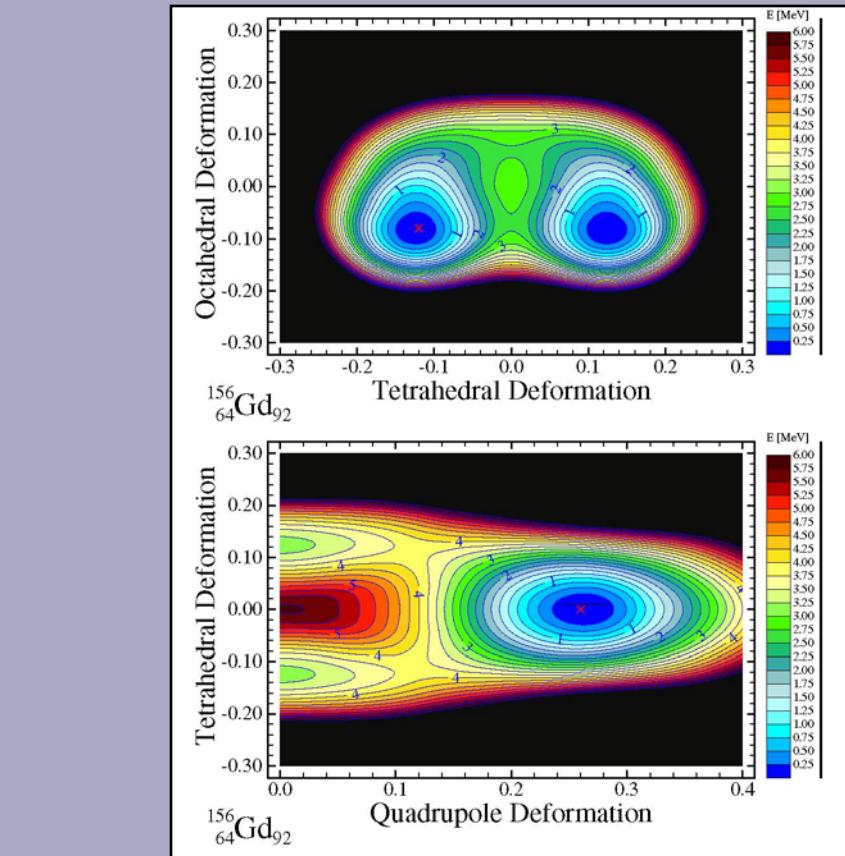
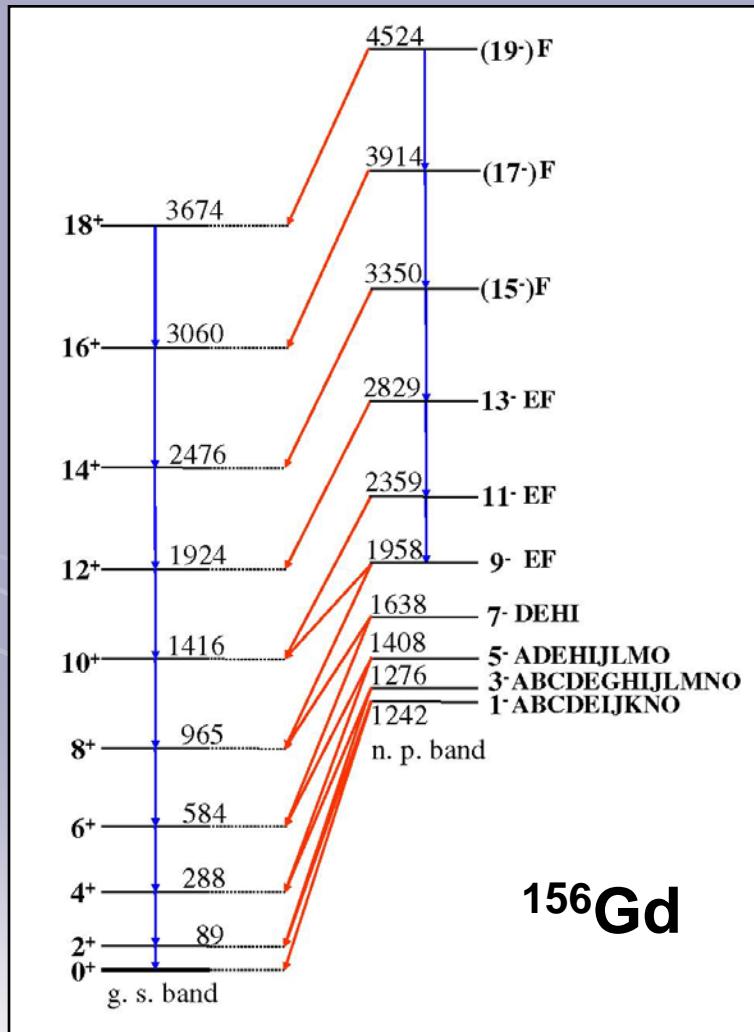
*Schematic illustrations of where to look for tetrahedral states*

# Experimental signatures (2/2)

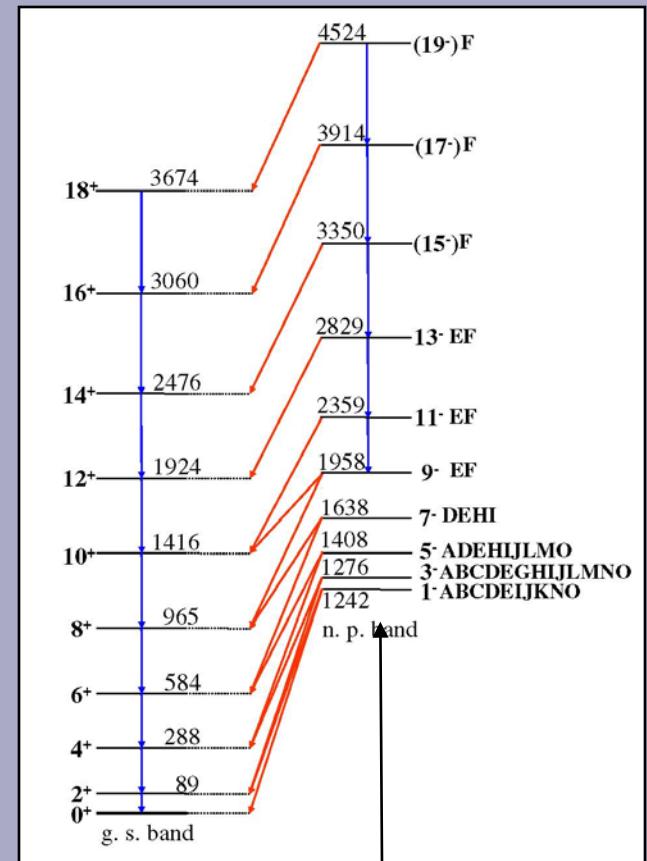
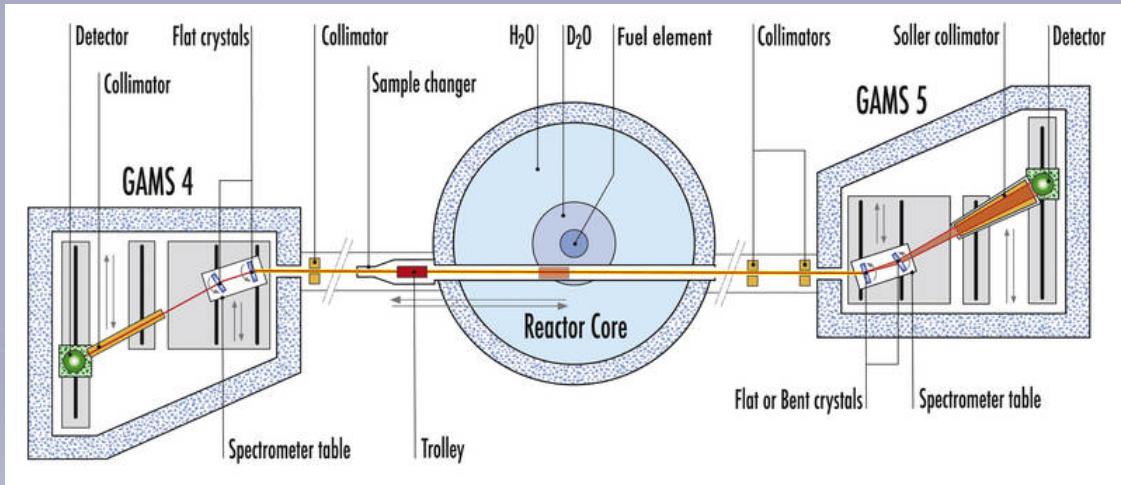
- The **quadrupole moment of a nucleus possessing a** **an exact  $T_d$  symmetry is equal to zero** and therefore also the corresponding **B(E2)** matrix elements have to vanish
- Large **B(E3)** matrix elements
- **B(E1)/B(E2)** ratios

## Island of Rare Earth Nuclei with Tetrahedral and Octahedral Symmetries: Possible Experimental Evidence

J. Dudek,<sup>1</sup> D. Curien,<sup>2</sup> N. Dubray,<sup>1</sup> J. Dobaczewski,<sup>3</sup> V. Pangon,<sup>1</sup> P. Olbratowski,<sup>3</sup> and N. Schunck<sup>4</sup>



**Vanishing E2 inband transitions  
Large E1 interband transitions**



$(n,\gamma)$  on  $^{155}\text{Gd} \rightarrow ^{156}\text{Gd}$

Ultrahigh resolution  $\gamma$ -ray spectroscopy at ILL

Intensity of the 132 keV  $5^- \rightarrow 3^- \gamma$  ray

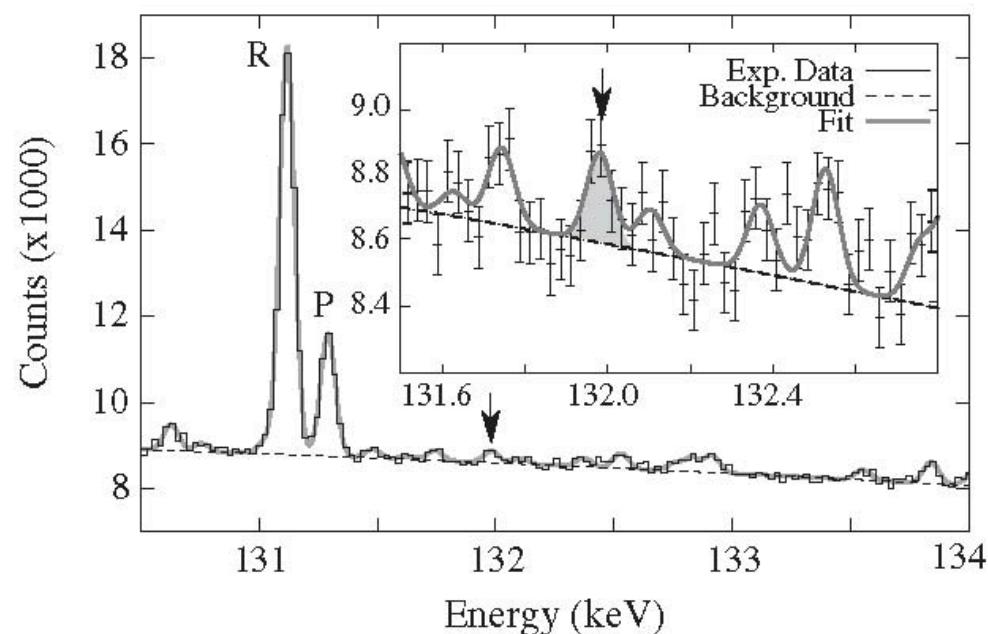
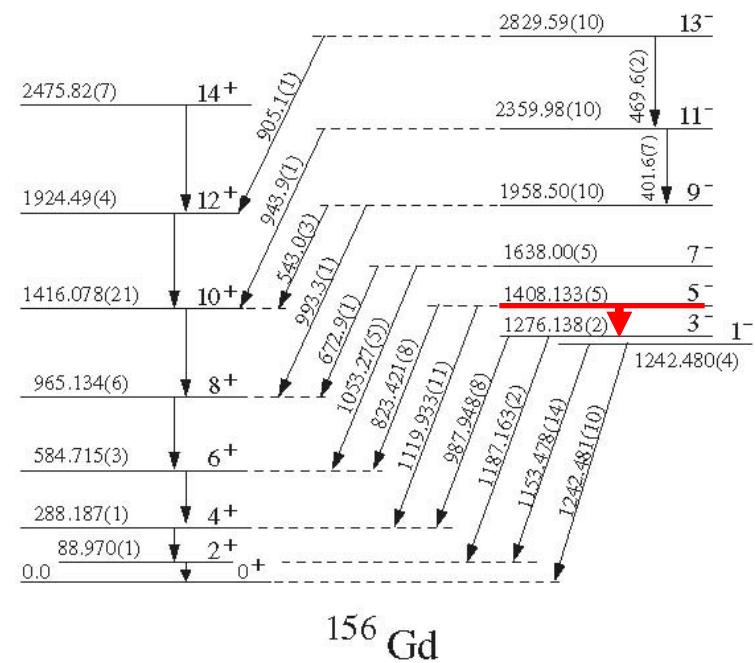
# Ultrahigh-Resolution $\gamma$ -Ray Spectroscopy of $^{156}\text{Gd}$ : A Test of Tetrahedral Symmetry

M. Jentschel,<sup>1</sup> W. Urban,<sup>1,2</sup> J. Krempel,<sup>1</sup> D. Tonev,<sup>3</sup> J. Dudek,<sup>4</sup> D. Curien,<sup>4</sup> B. Lauss,<sup>5</sup> G. de Angelis,<sup>6</sup> and P. Petkov<sup>3</sup>

PRL 104, 222502 (2010)

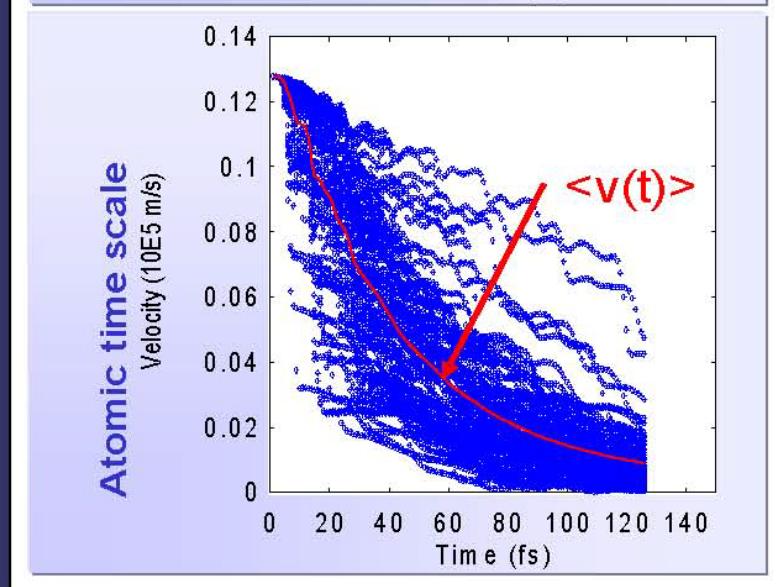
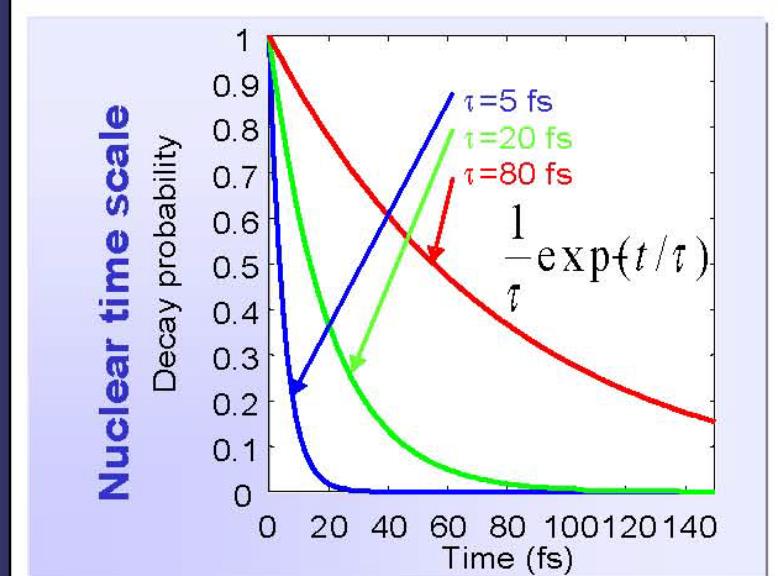
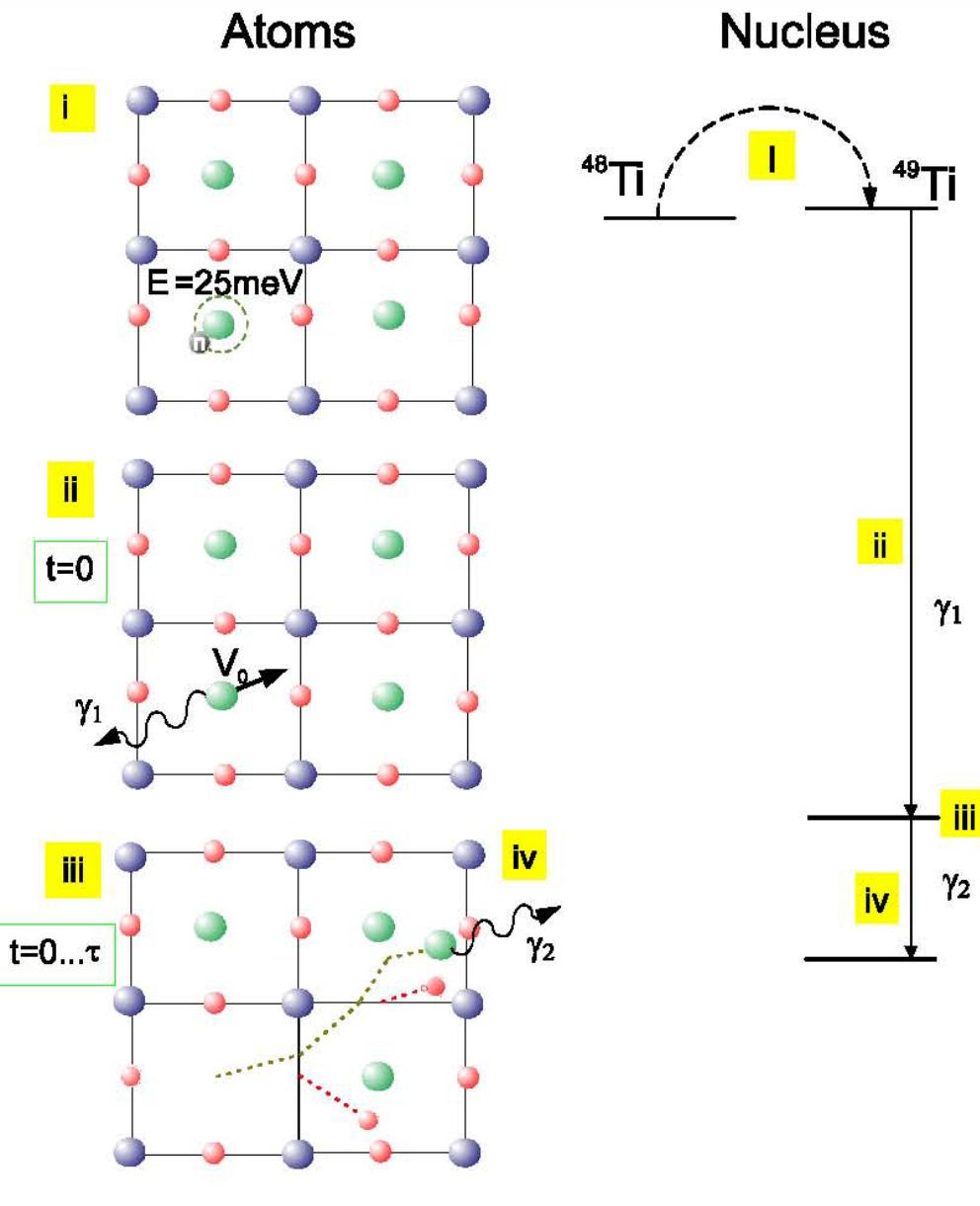
PHYSICAL PRL 104, 222502 (2010)

PHYSICAL R



Lifetime of the  $5^-$  level at 1.408 MeV  
Intensity of the 132 keV  $5^- \rightarrow 3^- \gamma$  ray

# Measuring a lifetime requires clocks



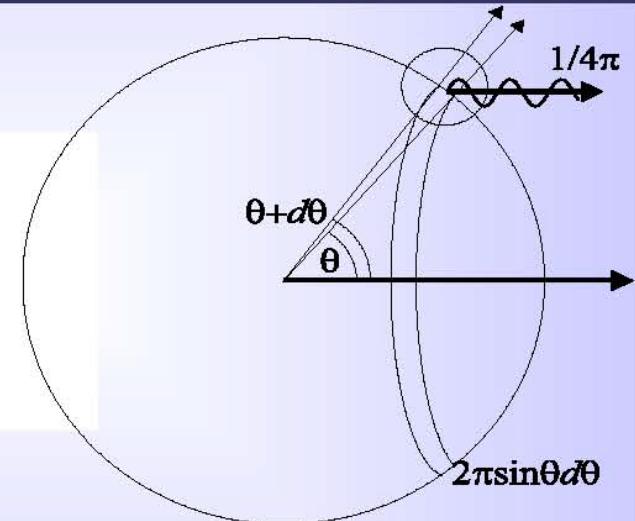
# Model of an isotropic slowing down

$$I(E)dE = C \sum_i \int_0^{\infty} dt \frac{\exp(-t/\tau) dE}{\left[ E - E_0 \left\{ 1 + \frac{v_i(t)}{c} \cos \theta_i(t) \right\} \right]^2 + [\Gamma/2]^2}$$

Doppler shift of one photon

Isotropic slowing down:

- $\theta(t) = \text{const}$
- $v(\theta_0, t) = v(t)$



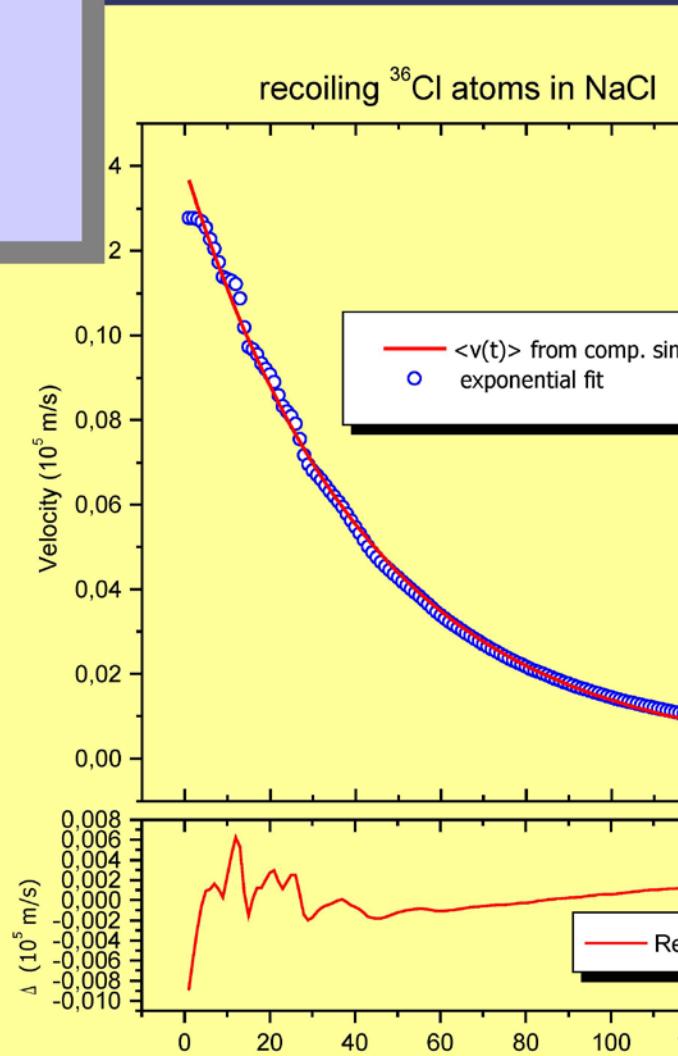
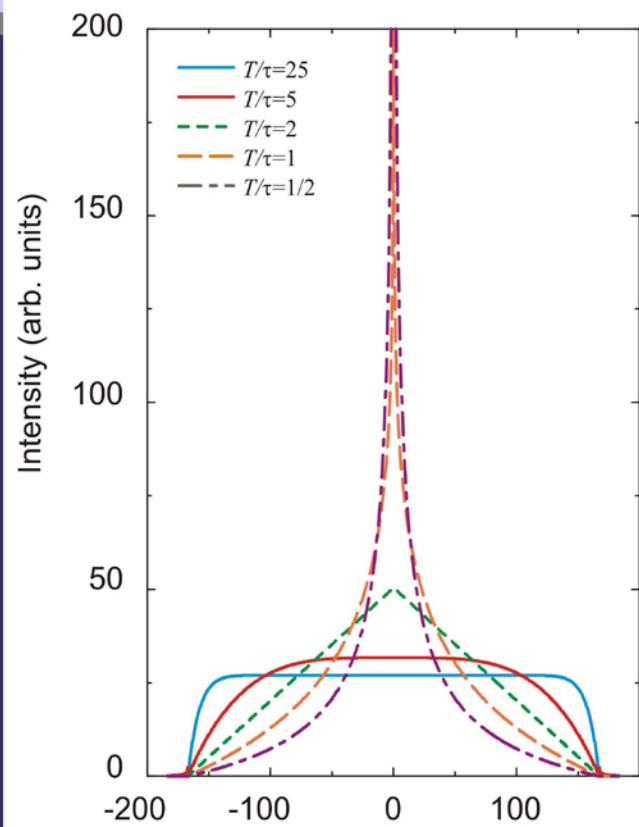
$$\begin{aligned} I(E)dE &= \tilde{C} \int_0^{\pi} d\theta \int_0^{\infty} dt \frac{\sin(\theta) \exp(-t/\tau) dE}{\left[ E - E_0 \left\{ 1 + \frac{v(t)}{c} \cos(\theta) \right\} \right]^2 + [\Gamma/2]^2} \\ &= \hat{C} \int_0^{\infty} \exp(-t/\tau) dt \left[ \arctan \frac{\Gamma}{2} \left\{ E - E_0 \left( 1 - \frac{v(t)}{c} \right) \right\} - \right. \\ &\quad \left. \arctan \frac{\Gamma}{2} \left\{ E - E_0 \left( 1 + \frac{v(t)}{c} \right) \right\} \right] \end{aligned}$$

Line profile of an isotropic moving particle

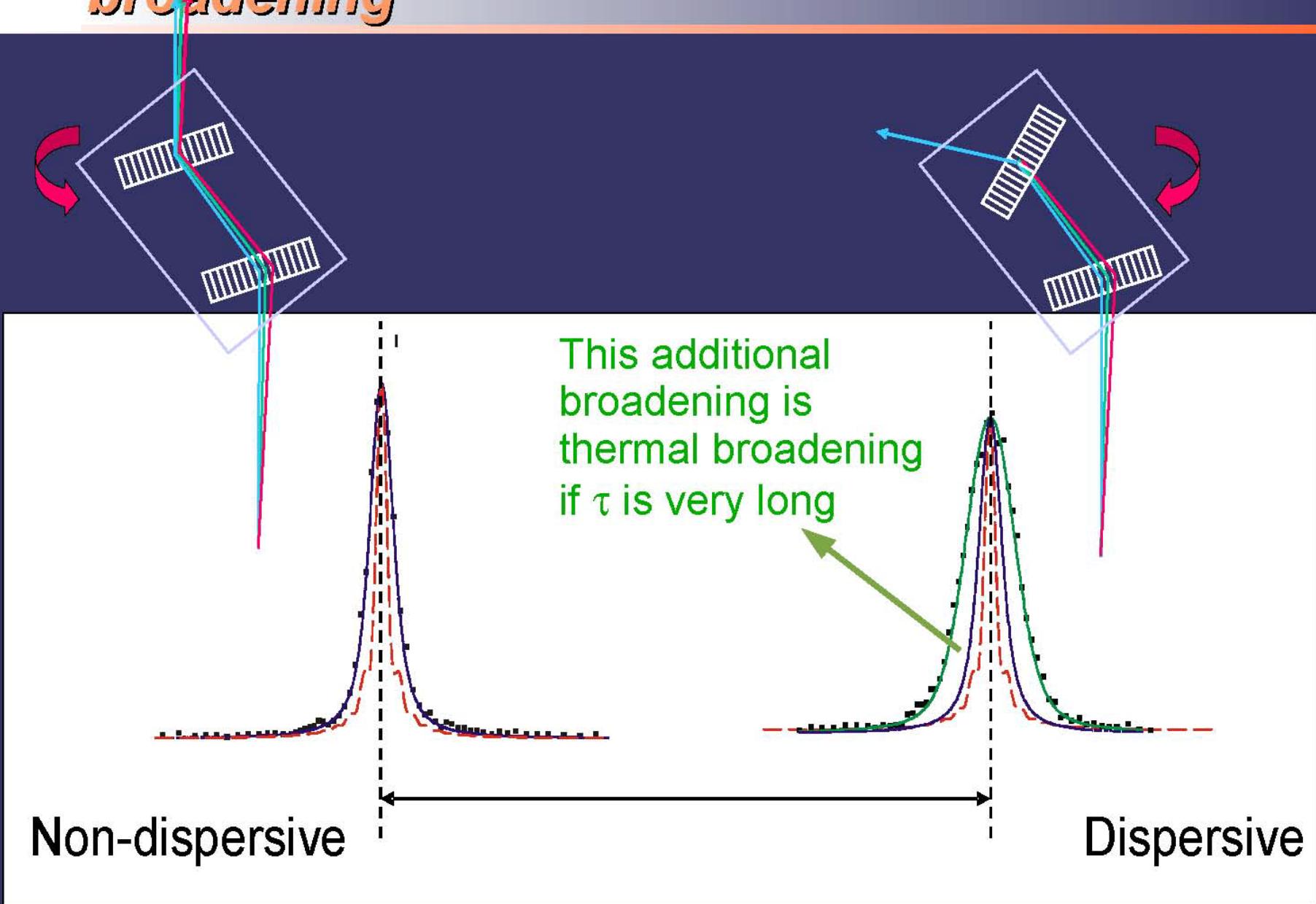
# Exponential slowing down model

Exponential slowing down:  $v(t) = v_0 \exp(-t/T)$

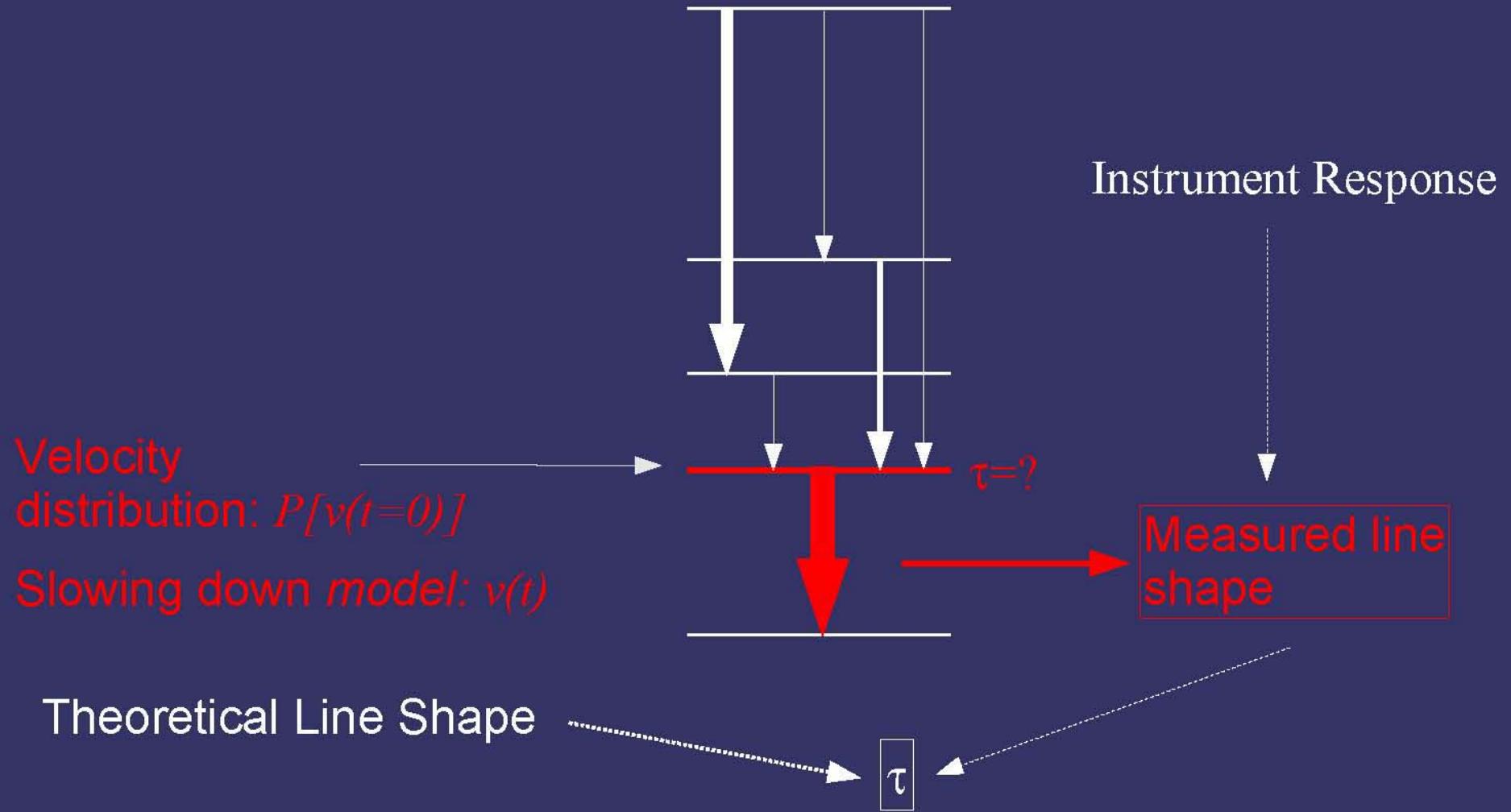
$$I(E)dE = \frac{C}{(T/\tau - 1)} \left( \frac{1}{v_0} \right)^{T/\tau - 1} \left[ v_0^{T/\tau - 1} - \left| c \left( 1 - \frac{E}{E_0} \right) \right|^{T/\tau - 1} \right] dE$$



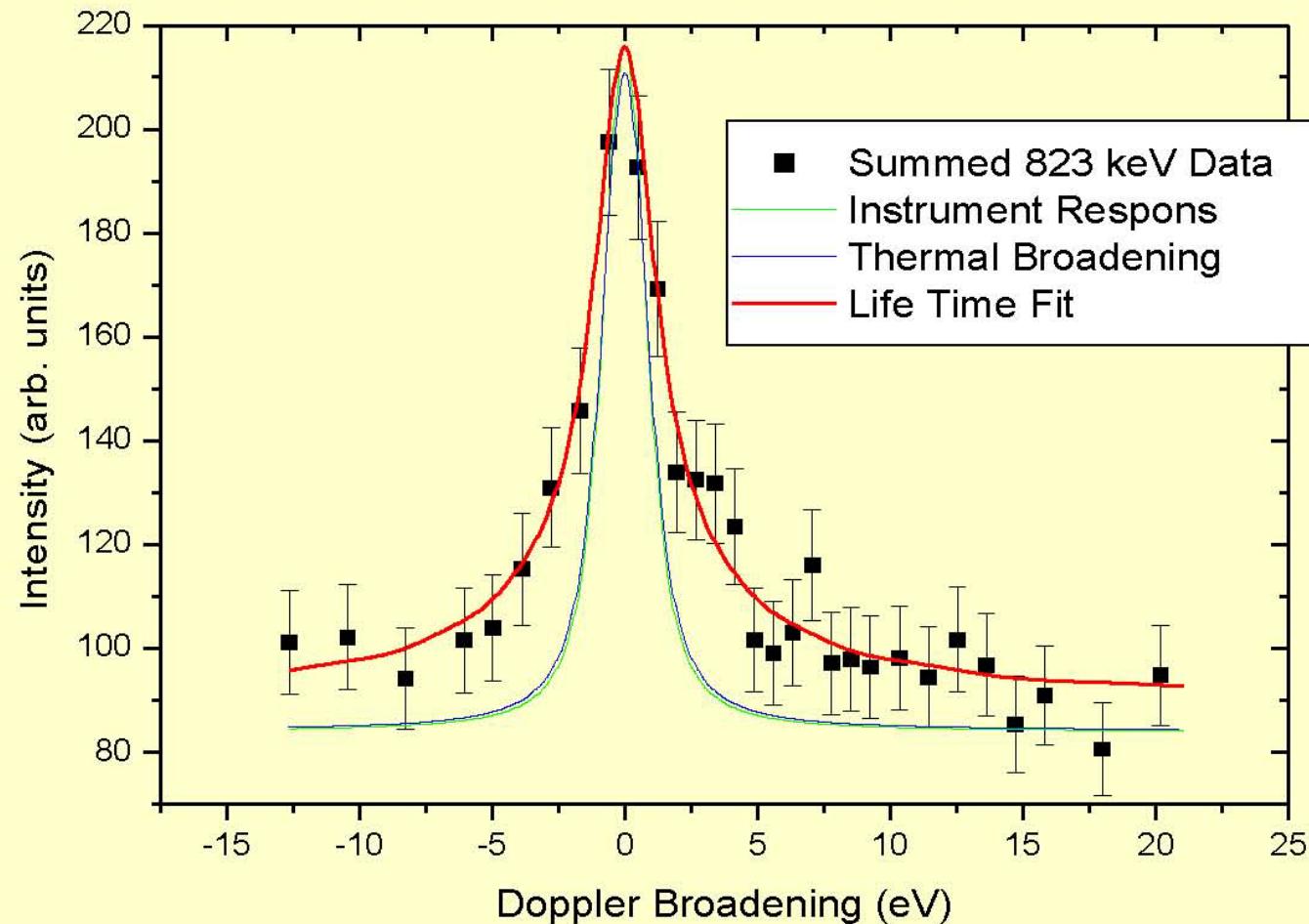
# *Measuring the temperature via Doppler broadening*



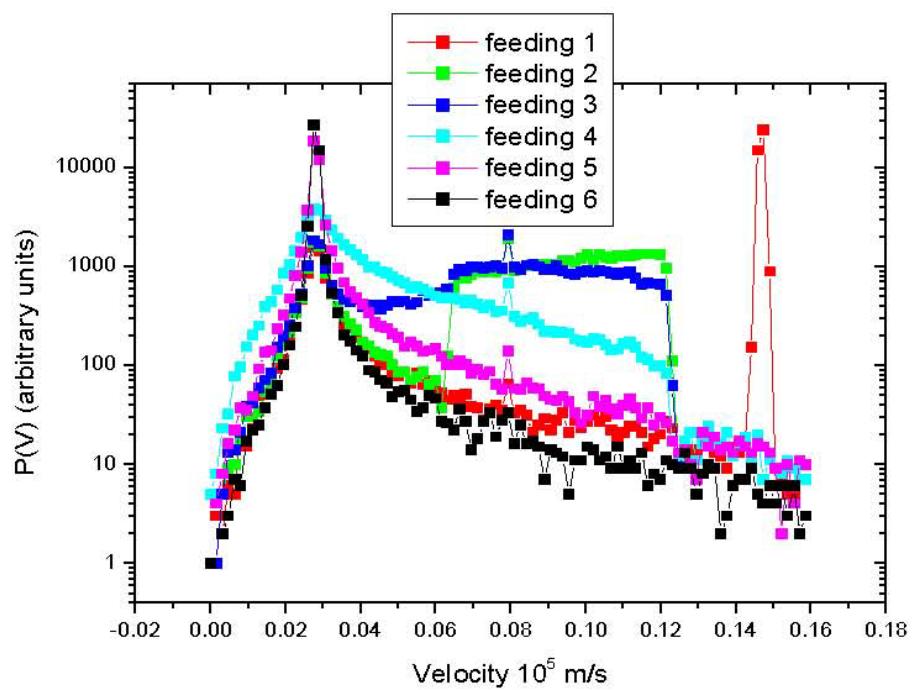
# *What do we really need to know?*



# (3,-3) Scan of the 823.421 keV Line



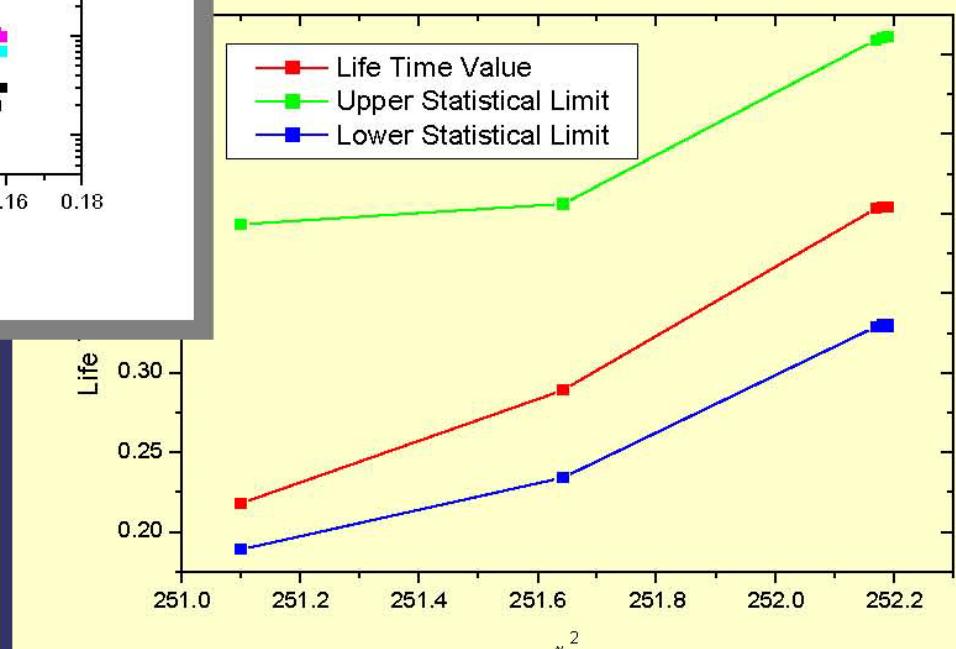
# *Life Time Results for different Scenarios*



Life Times for Different Scenarios

$$\tau = 220 (+180 -40)\text{fs}$$

Velocity Distribution for Different Scenarios



# Quadrupole moment of the $5^-$ state in $^{156}\text{Gd}$

$B(E2\ 5^- \rightarrow 3^-) = 293\ (+61-134)\ \text{W.U.}$

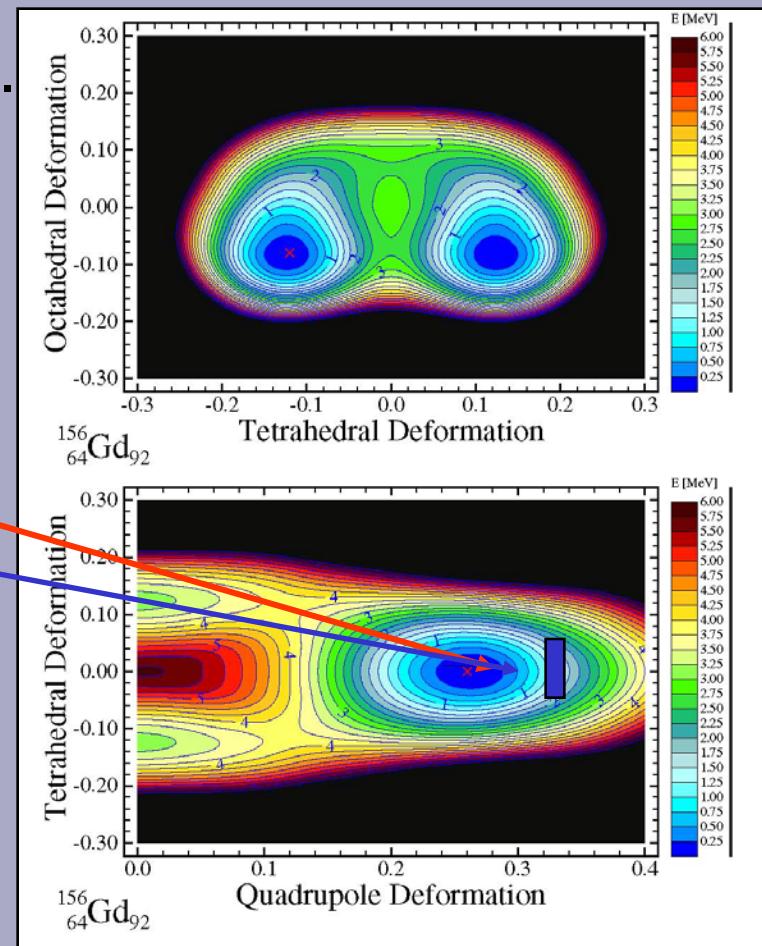
$B(E2\ 2^+ \rightarrow 0^+) = 186.1(20)\ \text{W.U.}$

$$\beta_{5^-} = 0.35(15)$$

$$\beta_{2^+} = 0.3378(18)$$

$$Q_{5^-} = 7.1\ (+0.7-1.6)\ \text{b}$$

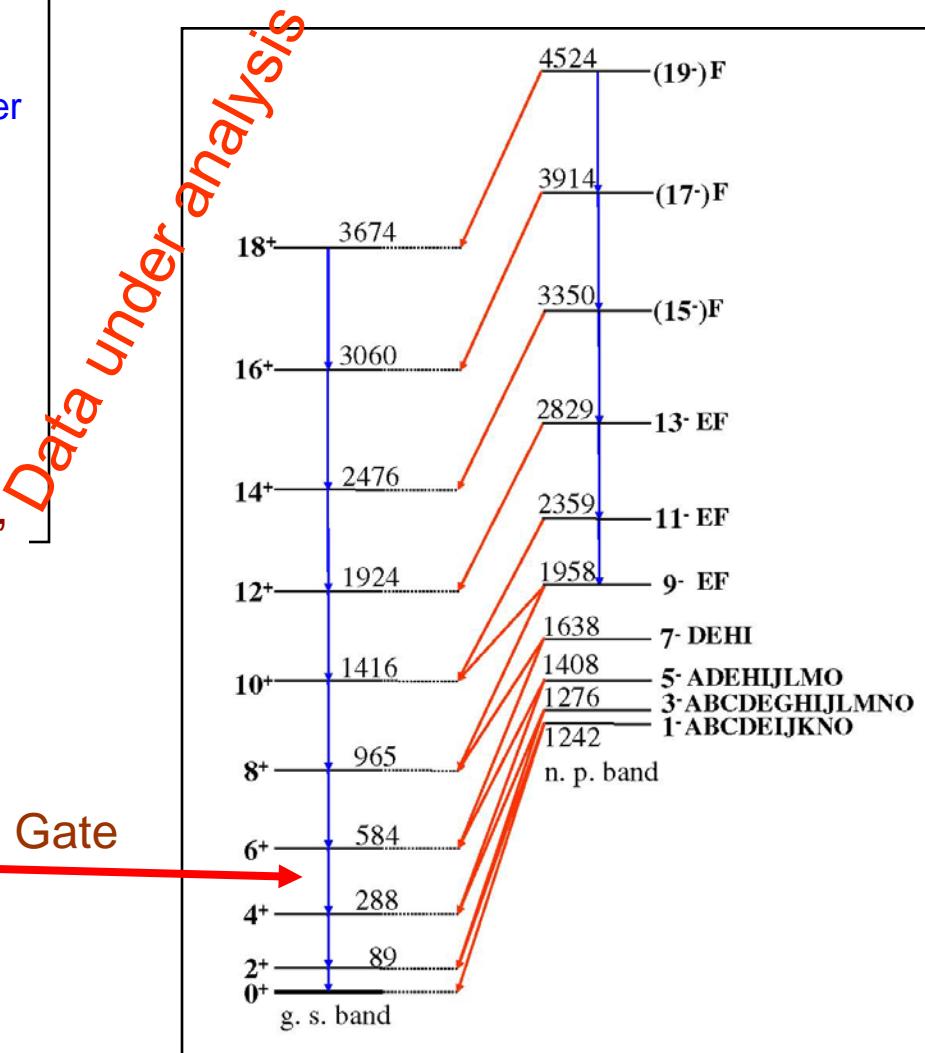
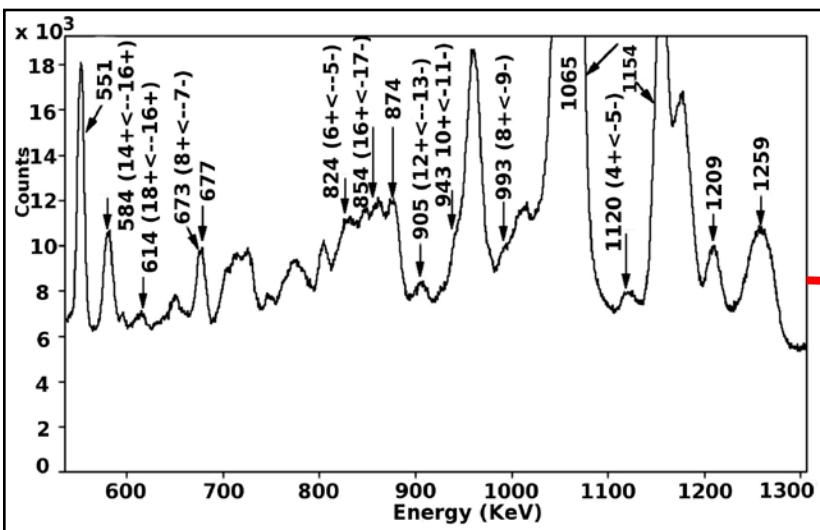
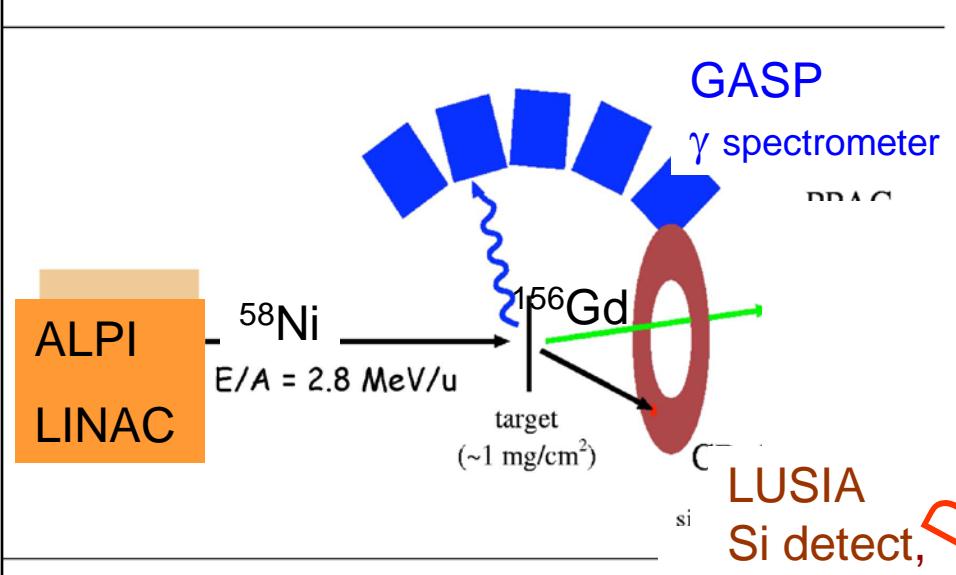
$$Q_{2^+} = 6.83\ (37)\ \text{b}$$



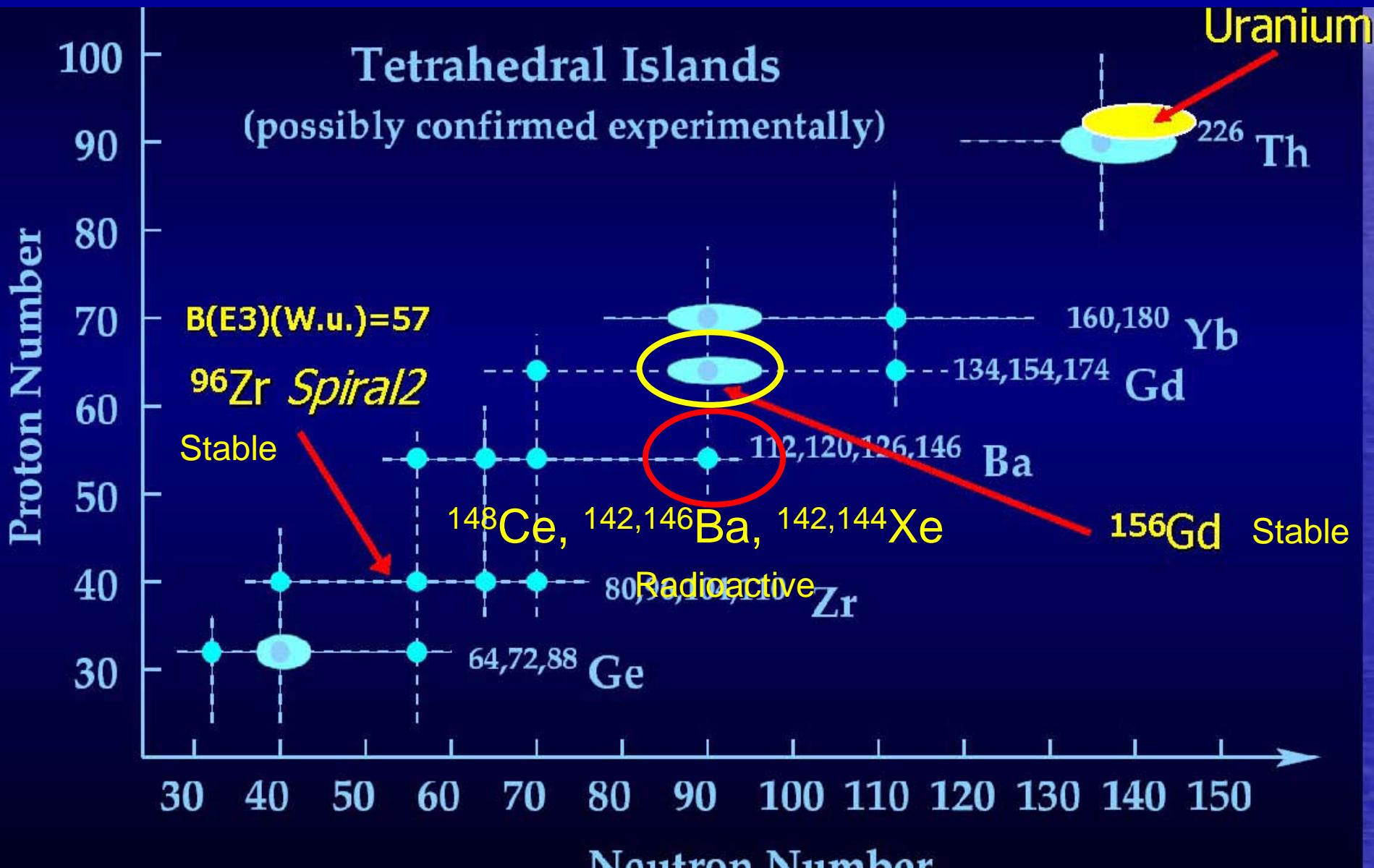
The negative parity band in  $^{156}\text{Gd}$  is incompatible with the description based on tetrahedral symmetry

# Electromagnetic transition matrix elements and quadrupole moment (with sign) accessible by low energy Coulomb excitation

Rajesh Pratap  
Singh et al.  
IUAC Delhi, India

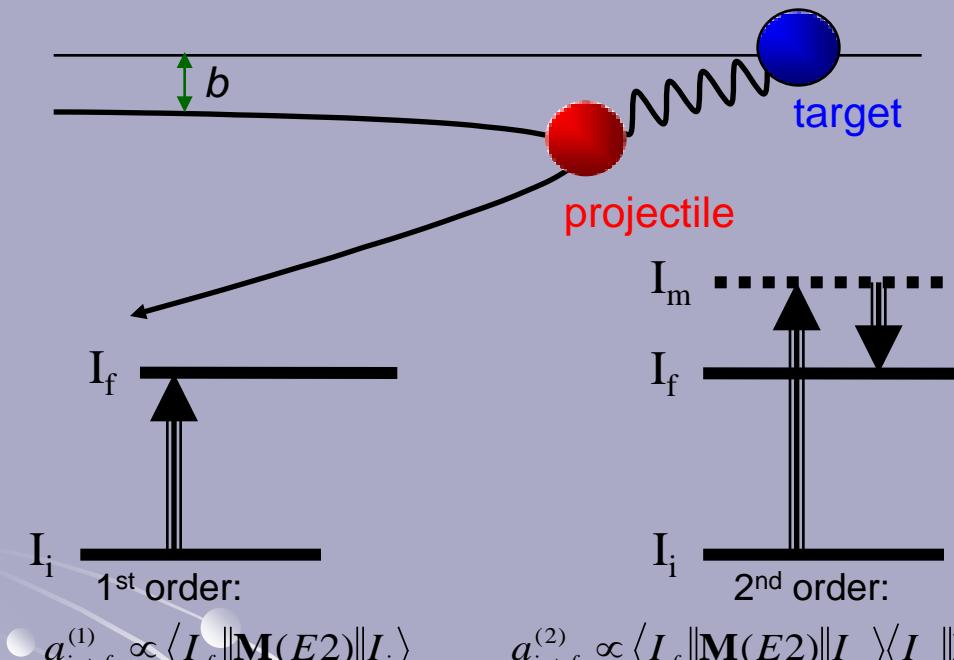


AIM of the LOI: Transition matrix elements and Q-moments of the exotic octupole bands from Coulex for the n-rich Ce, Ba, Xe nuclei.  
SPES intensities  $\sim$  105-107 pps

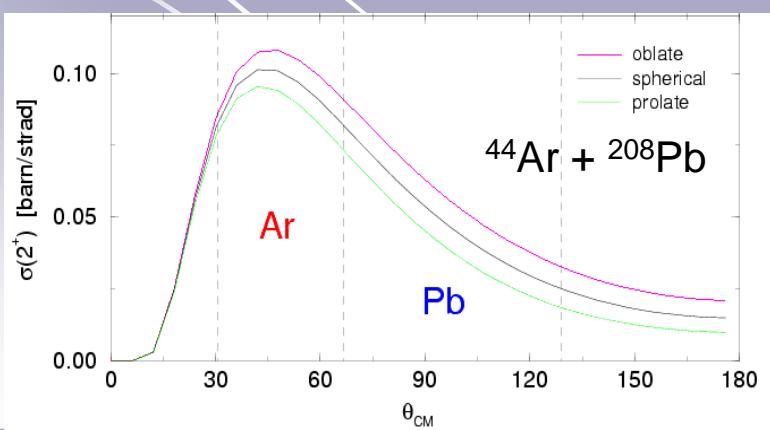
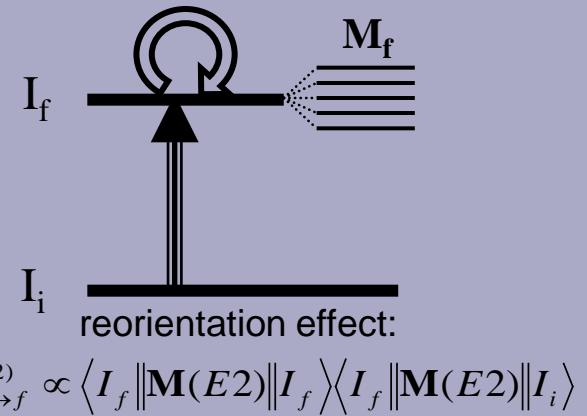


AIM of the LOI: Transition matrix elements and Q-moments (sign) of the exotic octupole bands from reorientation effects for the n-rich Ce, Ba, Xe nuclei.  
 SPES intensities  $\sim 10^5$ - $10^7$  pps

Nuclear excitation by electromagnetic field acting between nuclei.



The excitation cross section is a direct measure of the  $E\lambda$  matrix elements.



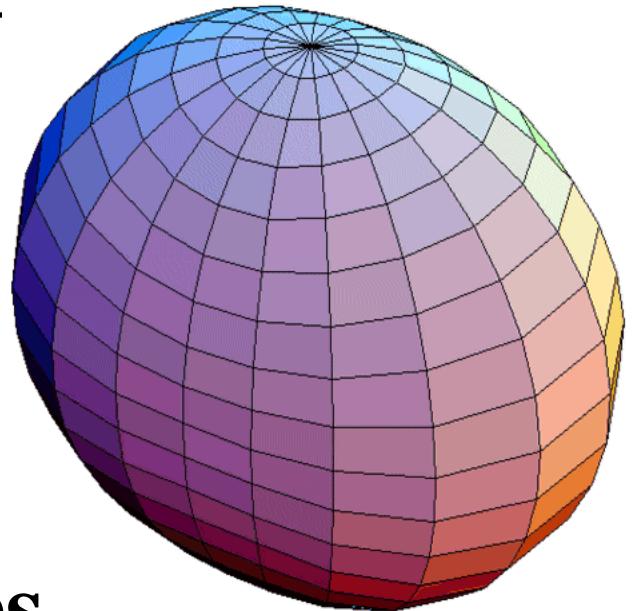
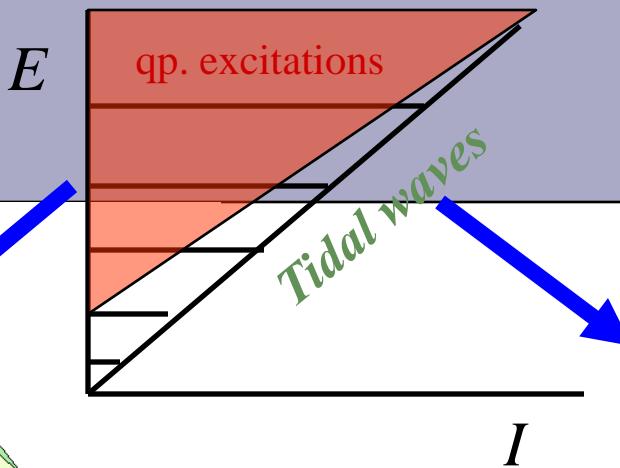
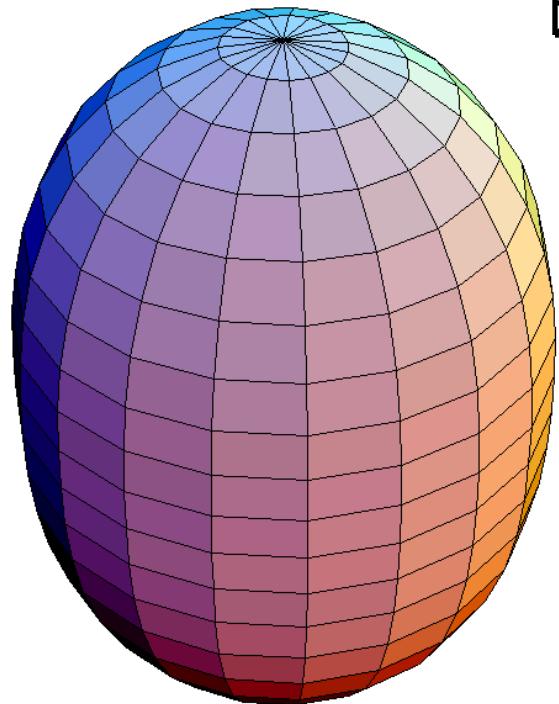
differential Coulomb excitation cross section  
 $\Rightarrow$  transition probability  $B(E2)$   
 $\Rightarrow$  quadrupole moment  $Q_s$

Set-up presented yesterday by  
 Barbara Mellon

# Summary

- Mean-field Theories predict tetrahedral configurations in islands of nuclei throughout the nuclear chart
- Signature: Vanishing quadrupole moment
- The best candidates will be found away from the valley of stability
- Aim of the LOI: Coulomb excitation of the quadrupole and octupole structures
- SPES intensities fine for the n-rich Ce, Ba, Xe

The nuclear tetrahedral symmetry reflects the quantal nature of the nucleus (always competing with the macroscopic, liquid-drop aspects)



## Tidal Waves

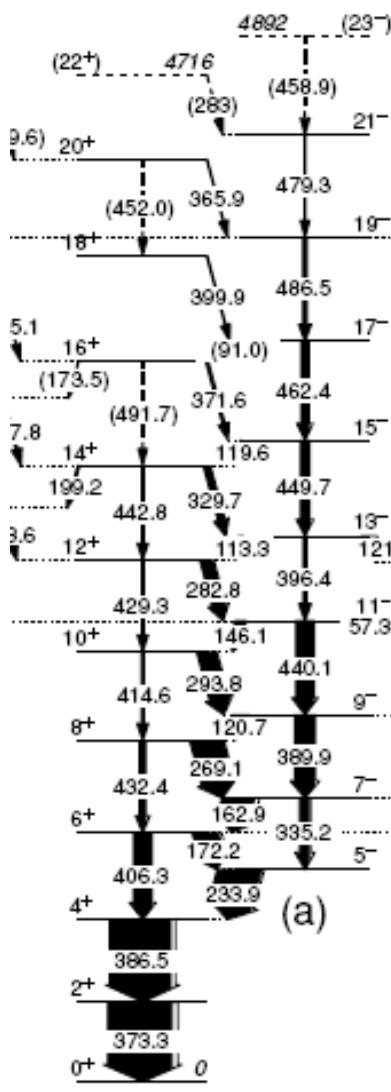
$$R(\vartheta, \varphi, t) =$$

$$R_0[1 + a_0 \cos(\Omega t) Y_{20}(\theta, \varphi = 0)]$$

$$R(\vartheta, \varphi, t) =$$

$$R_0[1 + 2a_2 \cos(2\varphi - \Omega t) Y_{22}(\vartheta, \varphi = 0)]$$

$$\omega = \frac{\Omega}{2} \quad E = \omega L_z$$



$^{220}_{\text{Th}} \text{Th}_{130}$

# Heart-shaped waves - good simplex

