

# Theoretical interpretations of the B-physics anomalies

Gino Isidori

[ *University of Zürich* ]

- ▶ *A closer look to the data*
- ▶ *EFT interpretations*
- ▶ *From EFT to simplified models*
- ▶ *Speculations on UV completions*
- ▶ *Conclusions*

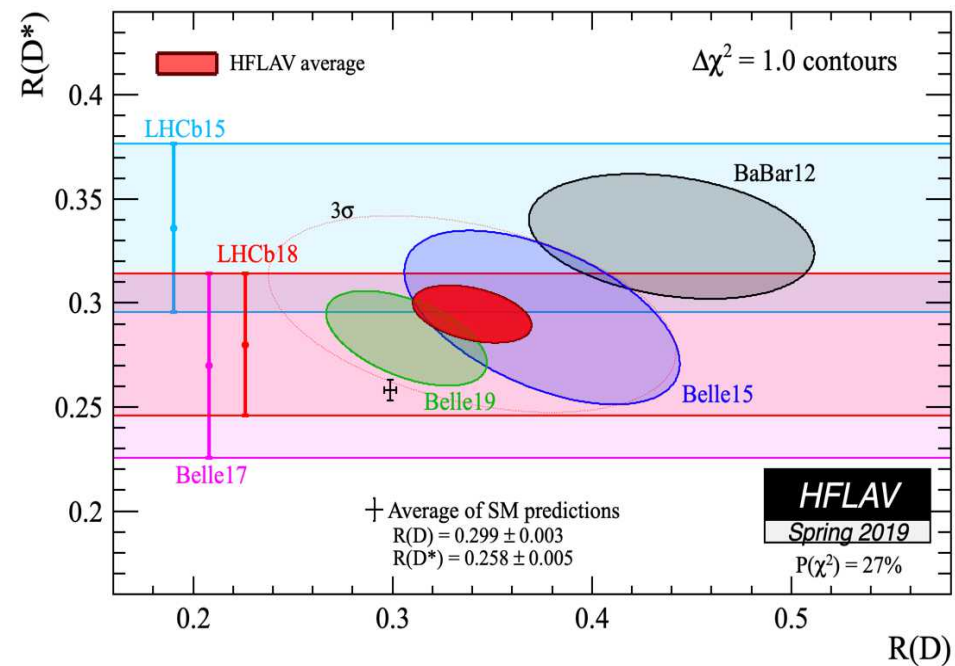
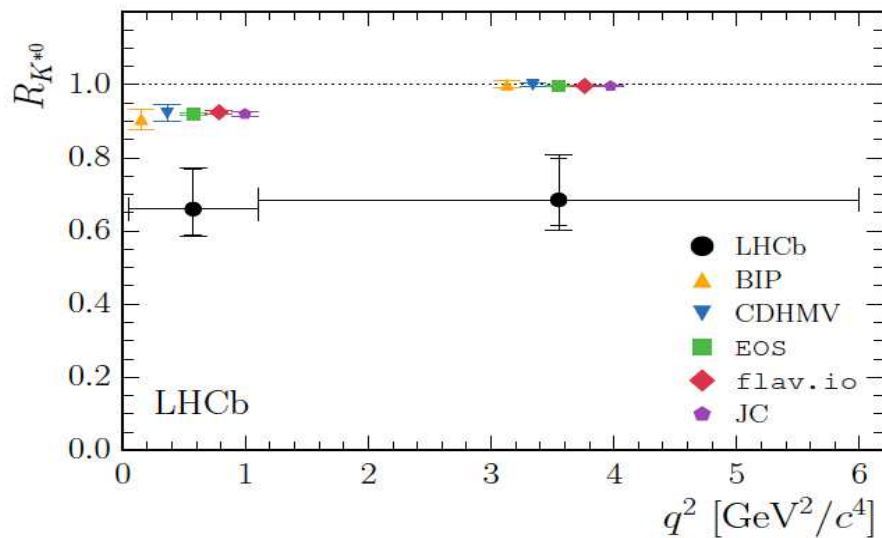
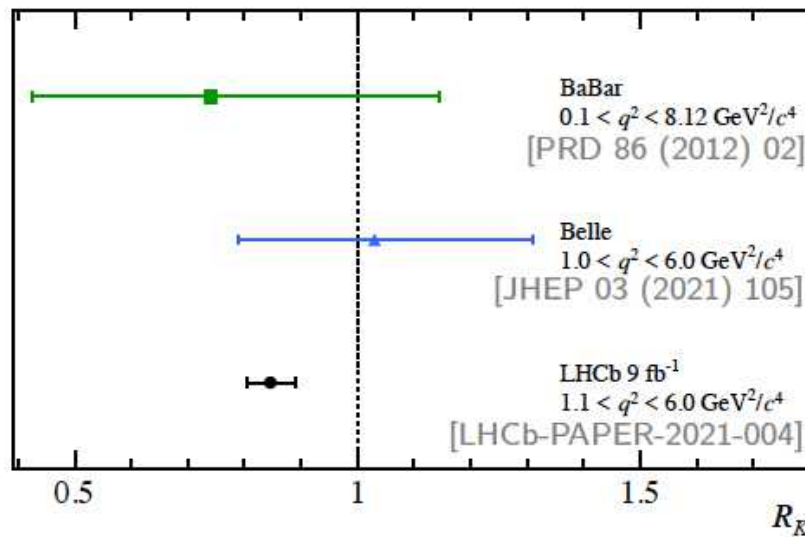


University of  
Zurich <sup>UZH</sup>



European Research Council  
Established by the European Commission

A closer look to the data



► *A closer look to the data*

Since 2013 results in semi-leptonic B decays started to exhibit tensions with the SM predictions connected to a possible violation of **L**epton **F**lavor **U**niversality

More precisely, we seem to observe a different behavior (*beside pure kinematical effects*) of different lepton species in the following processes:

- $b \rightarrow s \, l^+ l^-$  (neutral currents):  $\mu$  vs.  $e$
- $b \rightarrow c \, l \nu$  (charged currents):  $\tau$  vs. light leptons ( $\mu, e$ )

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**N.B:** **LFU** is an accidental symmetry of the SM Lagrangian in the limit where we neglect the lepton Yukawa couplings.

LFU is badly broken in the Yukawa sector, but all the lepton Yukawa couplings are small within the SM ( $y_\tau \sim 0.01$ ), giving rise to the (*approximate*) universality of decay amplitudes which differ only by the different lepton species involved.

*As for all accidental symmetries* → ideal “tool” to look for BSM effects...

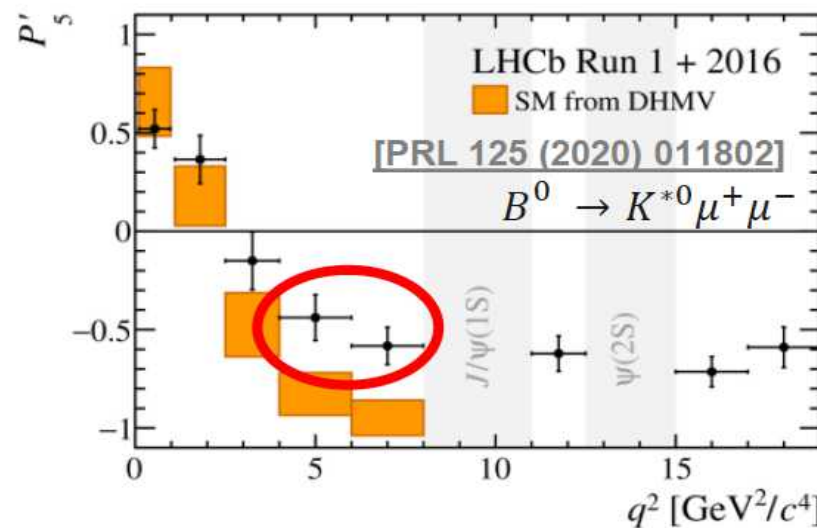
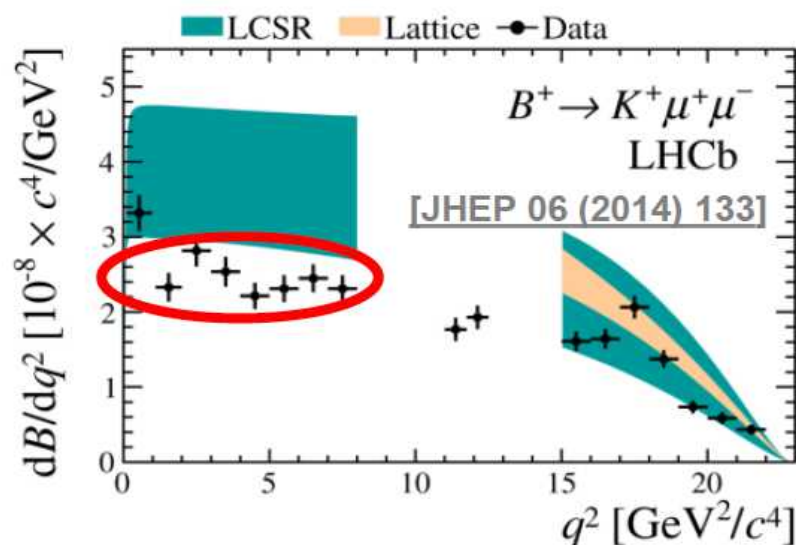
► A closer look to the data

•  $b \rightarrow s l^+ l^-$  (neutral currents)

List of the observables:

- $P'_5$  anomaly [ $B \rightarrow K^* \mu\mu$  angular distribution]
- Smallness of all  $B \rightarrow H_s \mu\mu$  rates [ $H_s=K, K^*, \phi$  (from  $B_s$ )]
- LFU ratios ( $\mu$  vs.  $e$ ) in  $B \rightarrow K^* \ell\ell$  &  $B \rightarrow K \ell\ell$
- Smallness of  $\text{BR}(B_s \rightarrow \mu\mu)$

↓  
chronological  
order



## ► A closer look to the data

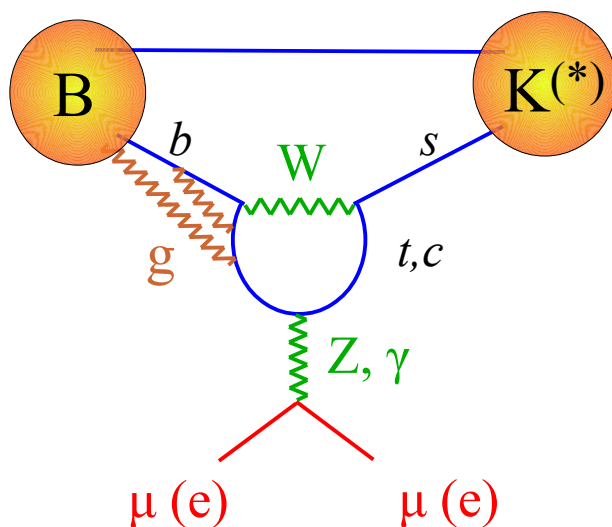
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😊 th. error <1%

😊 th. error few %



Some of these observables are affected by irreducible theory errors (*form factors + long-distance contributions*)

The new result strengthens the overall consistency of the picture: all data coherently point to well-defined non-SM contributions of short-distance origin.

## ► A closer look to the data

To describe  $b \rightarrow sll$  decays we

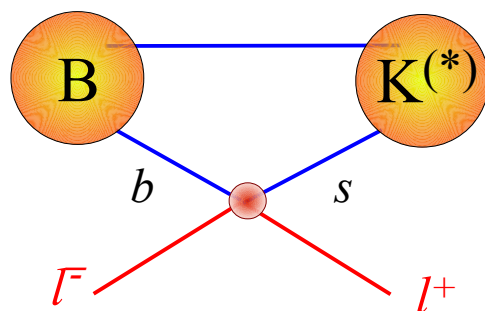
- build an EFT Lagrangian
- evolve it down to  $\mu \sim m_b$
- evaluate hadronic matrix elements

$$\mathcal{L}_{\text{eff}} = \frac{4G_F}{\sqrt{2}} V_{tb}^* V_{ts} \sum_i c_i \mathcal{O}_i$$

*FCNC operators:*

$$\mathcal{O}_{10}^l = (\bar{s}_L \gamma_\mu b_L)(\bar{l} \gamma^\mu \gamma_5 l)$$

$$\mathcal{O}_9^l = (\bar{s}_L \gamma_\mu b_L)(\bar{l} \gamma^\mu l)$$

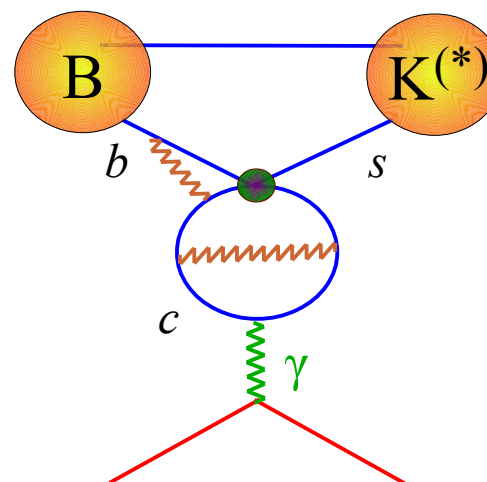


“easy” & “clean”

*Four-quark operators:*

$$\mathcal{O}_2 = (\bar{s}_L \gamma_\mu b_L)(\bar{c}_L \gamma_\mu c_L)$$

⋮



“difficult”



induces  $\Delta C_9^{\text{Univ}}$

**N.B.:** long-distance effect cannot induce LFU breaking terms ( $\rightarrow$  LFU ratios “clean”) and cannot induce axial-current contributions ( $\rightarrow B_s \rightarrow \mu\mu$  “clean”)

► A closer look to the data

The LFU ratios:

$$R_H = \frac{\int d\Gamma(B \rightarrow H \mu\mu)}{\int d\Gamma(B \rightarrow H ee)} \quad (H=K, K^*)$$

SM prediction very robust:  $(R_H)=1$

[*up tiny QED and lepton mass effects*]

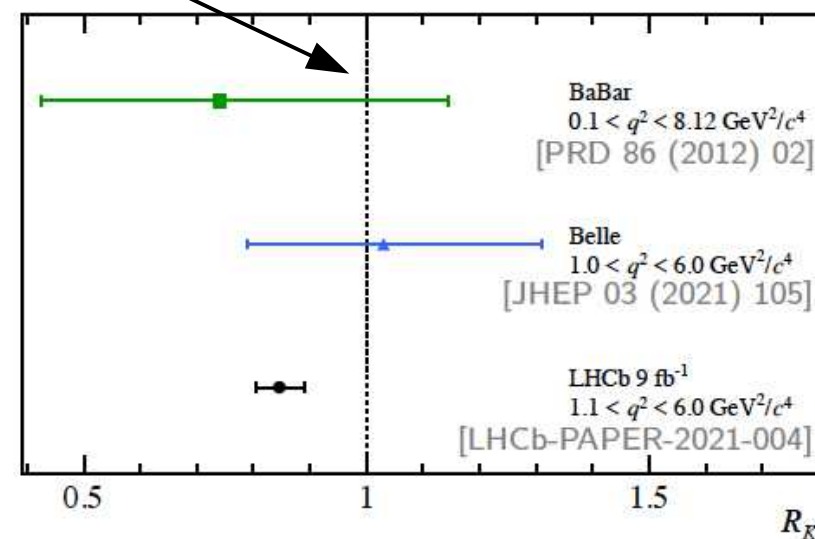
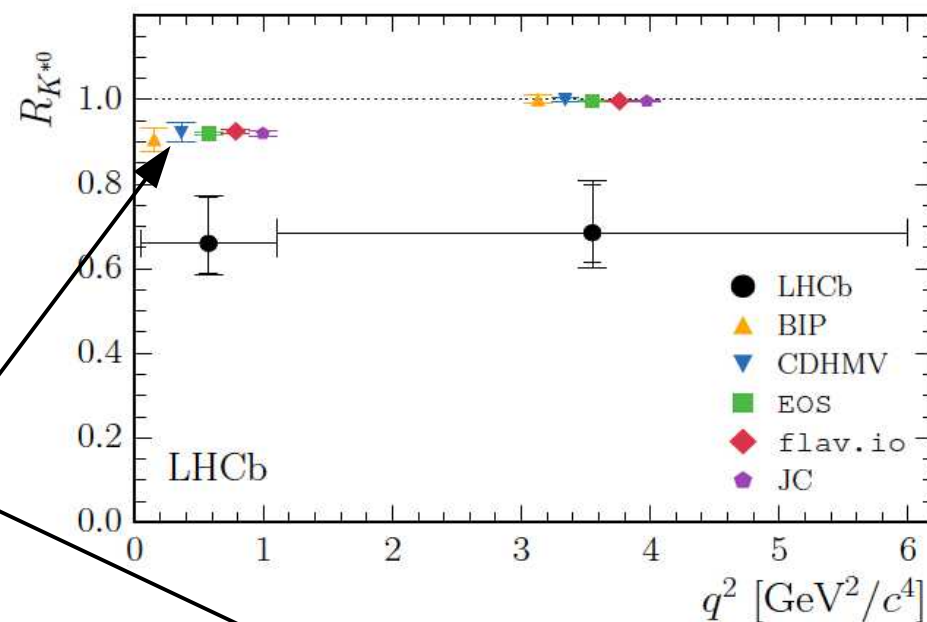
Bordone, GI, Patteri '16

GI, Nabeebascus, Zwicky '20

Deviations from the SM predictions

ranging from  $2.2\sigma$  to  $3.1\sigma$

in each of the 3 bins measured by LHCb





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$B_s \rightarrow \mu\mu$ :

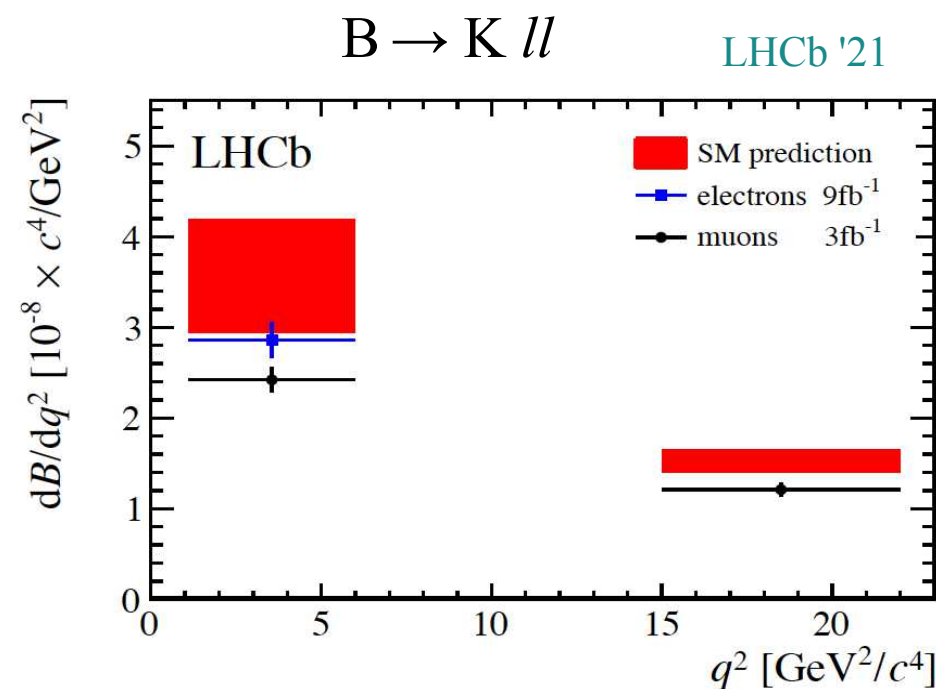
$$BR(B_s \rightarrow \mu\mu)_{SM} = (3.66 \pm 0.14) \times 10^{-9}$$

Beneke *et al.* '19

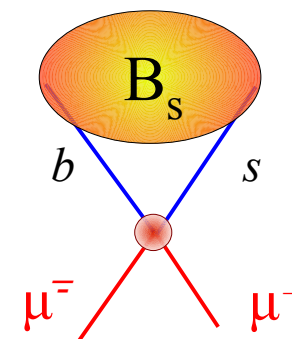
$$BR(B_s \rightarrow \mu\mu)_{exp} = (2.85 \pm 0.32) \times 10^{-9}$$

$2.3\sigma$

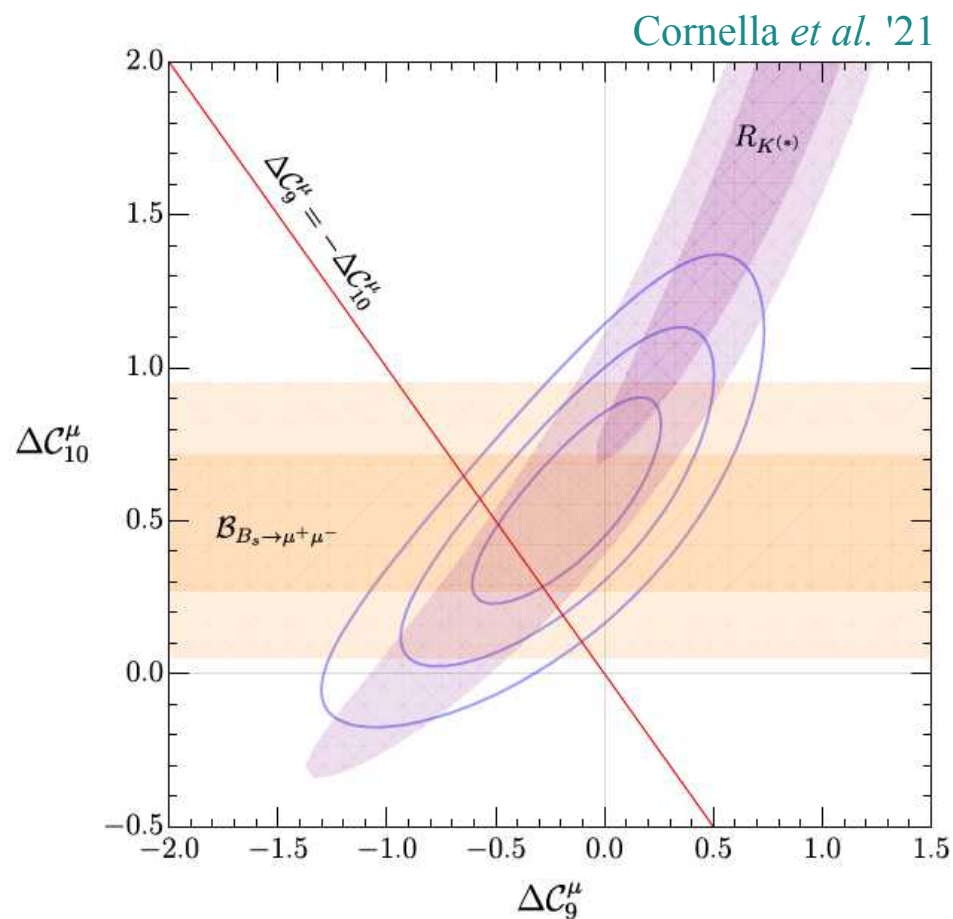
ATLAS+CMS+LHCb '21



According to our best estimates of the SM rates, what is observed is a (15-20)% deficit of the muon modes



► A closer look to the data



Conservative fit using “clean obs.”

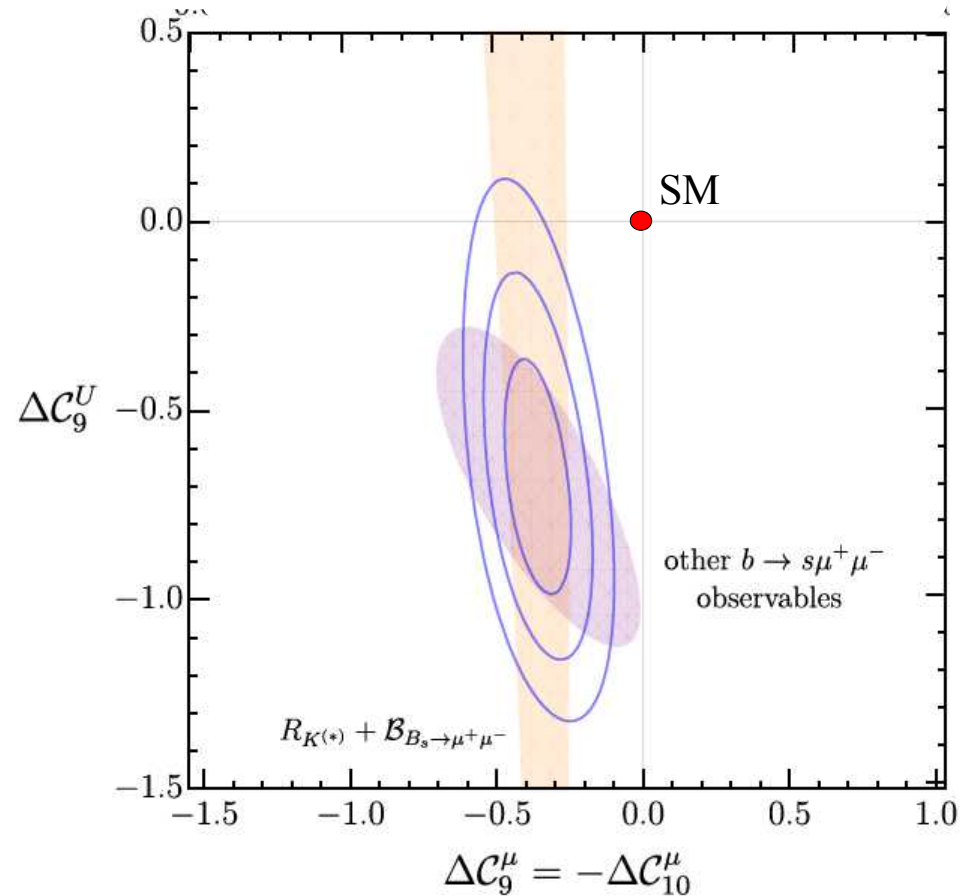
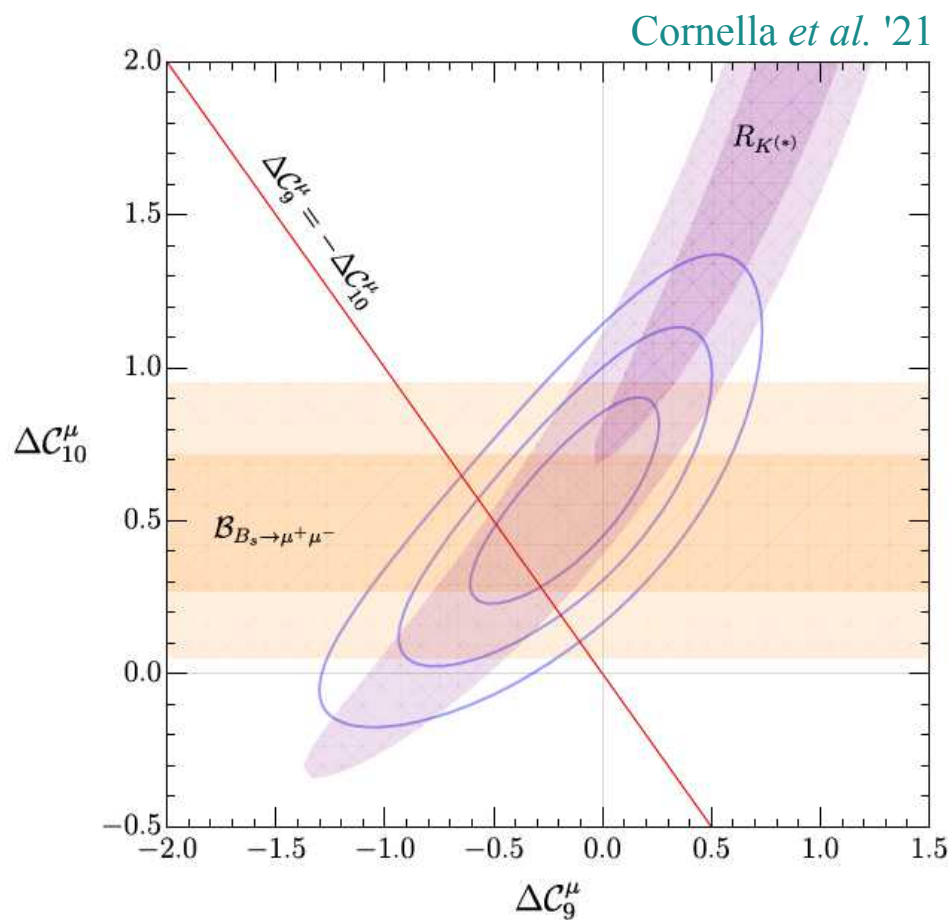
only [  $\Delta C_i^{\mu} = C_i^{\mu} - C_i^e$  ]:

4.6 $\sigma$

significance of NP hypothesis

$$\Delta C_9^{\mu} = -\Delta C_{10}^{\mu} \text{ vs. SM}$$

► A closer look to the data



Conservative fit using “clean obs.”  
only [  $\Delta C_i^\mu = C_i^\mu - C_i^e$  ]:

**4.6σ** significance of NP hypothesis  
 $\Delta C_9^\mu = -\Delta C_{10}^\mu$  vs. SM

**>> 5σ** with current best estimate  
of charm contrib

Alguero et al. '19  
Ciuchini et al. '20  
Li-Sheng Geng et al. '21  
Altmanshofer & Stangl '21

► A closer look to the data

**N.B.:** the “ $n\sigma$ ” quoted by various theory groups holds for specific NP hypotheses, motivated, but made *a posteriori* (after looking at the data) → *local significance*

The *global significance* of observing any form of **heavy new physics in  $b \rightarrow sll$**  can be estimated via the following procedure

- Employ the most general eff. Lagrangian for  $b \rightarrow sll$  [full basis with 9  $C_i^{\text{NP}}$ ]
- Consider all the observables  $O_i$  with good sensitivity to (at least some of) the  $C_i^{\text{NP}}$  [taking into account conservative th. errors → no charm loops]
- Generate pseudo-data to evaluate the  $O_i$  [assuming SM theory & exp. errors]
- Fit the simulated  $O_i$  with generic  $C_i^{\text{NP}}$  →  $\Delta\chi^2$  distribution of the pseudo-data
- Evaluate probability  $P(\Delta\chi^2 > \Delta\chi^2_{\text{obs}})$

Lancierini, GI,  
Owen, Serra, '21

↑  
*probability that data  
randomly align to one of the  
possible NP directions*

## ► A closer look to the data

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**3.9 $\sigma$**

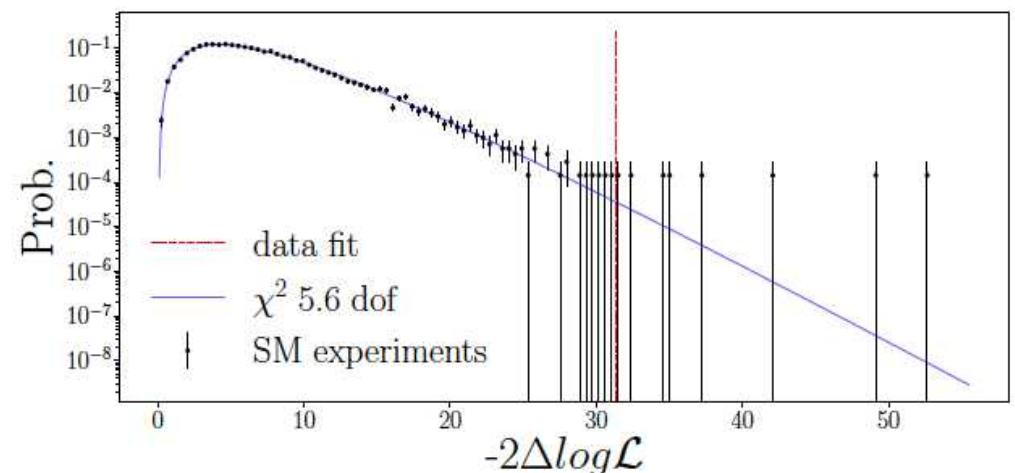
*global significance*

with respect to any form of heavy NP

Lancierini, GI,  
Owen, Serra, '21

Remarkably high !

[despite being very conservative]

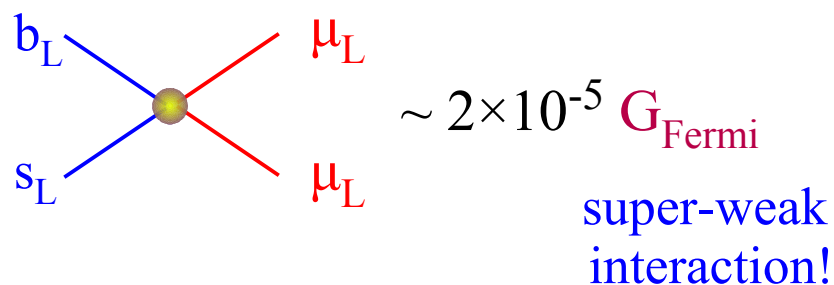


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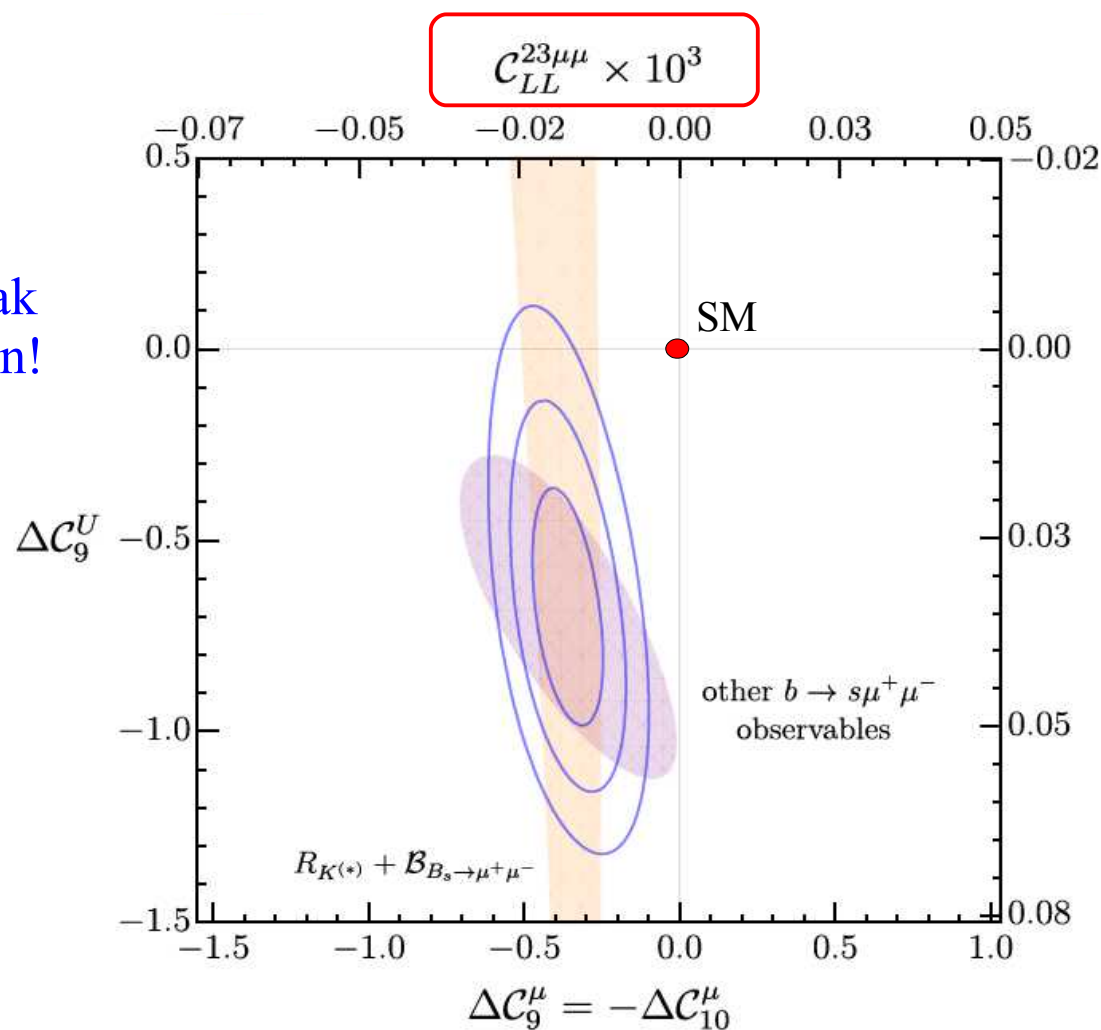
Coming back to the theory interpretation ( $\rightarrow$  *th. motivated fits are essential!*)

Data point to (short-distance) NP effects in operators of the type

$$\mathcal{O}_{LL}^{ij\alpha\beta} = (\bar{q}_L^i \gamma_\mu \ell_L^\alpha) (\bar{\ell}_L^\beta \gamma_\mu q_L^j)$$



$$C_{LL}^{23\mu\mu} \rightarrow \Delta C_9^\mu = -\Delta C_{10}^\mu$$

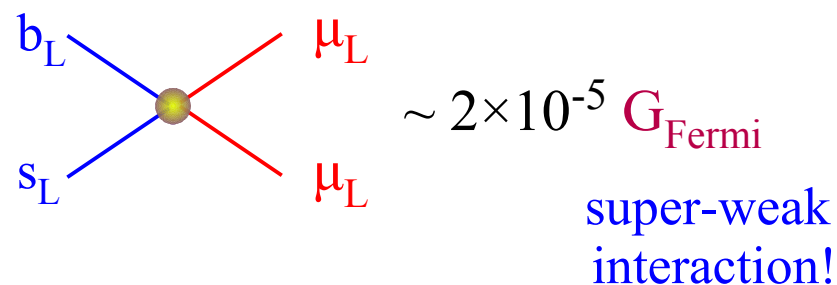


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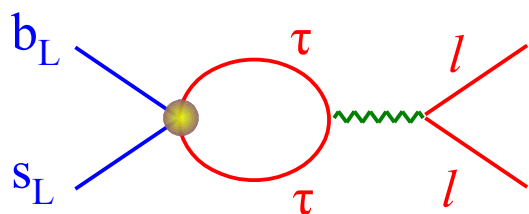
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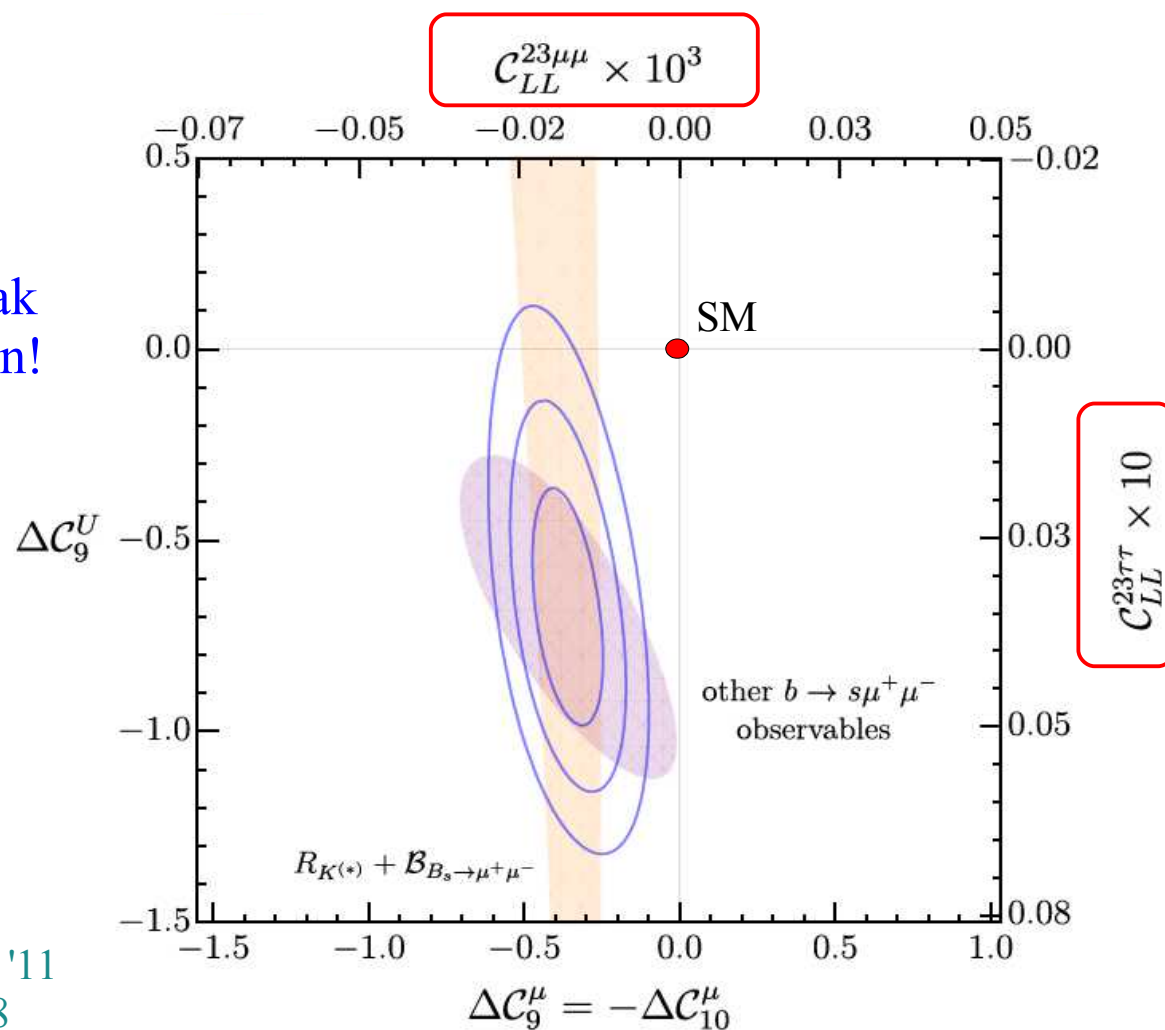


$$C_{LL}^{23\mu\mu} \rightarrow \Delta C_9^\mu = -\Delta C_{10}^\mu$$



$$C_{LL}^{23\tau\tau} \rightarrow \Delta C_9^{\text{Univ}}$$

Bobeth & Haisch '11  
Crivellin *et al.* '18



## ► A closer look to the data

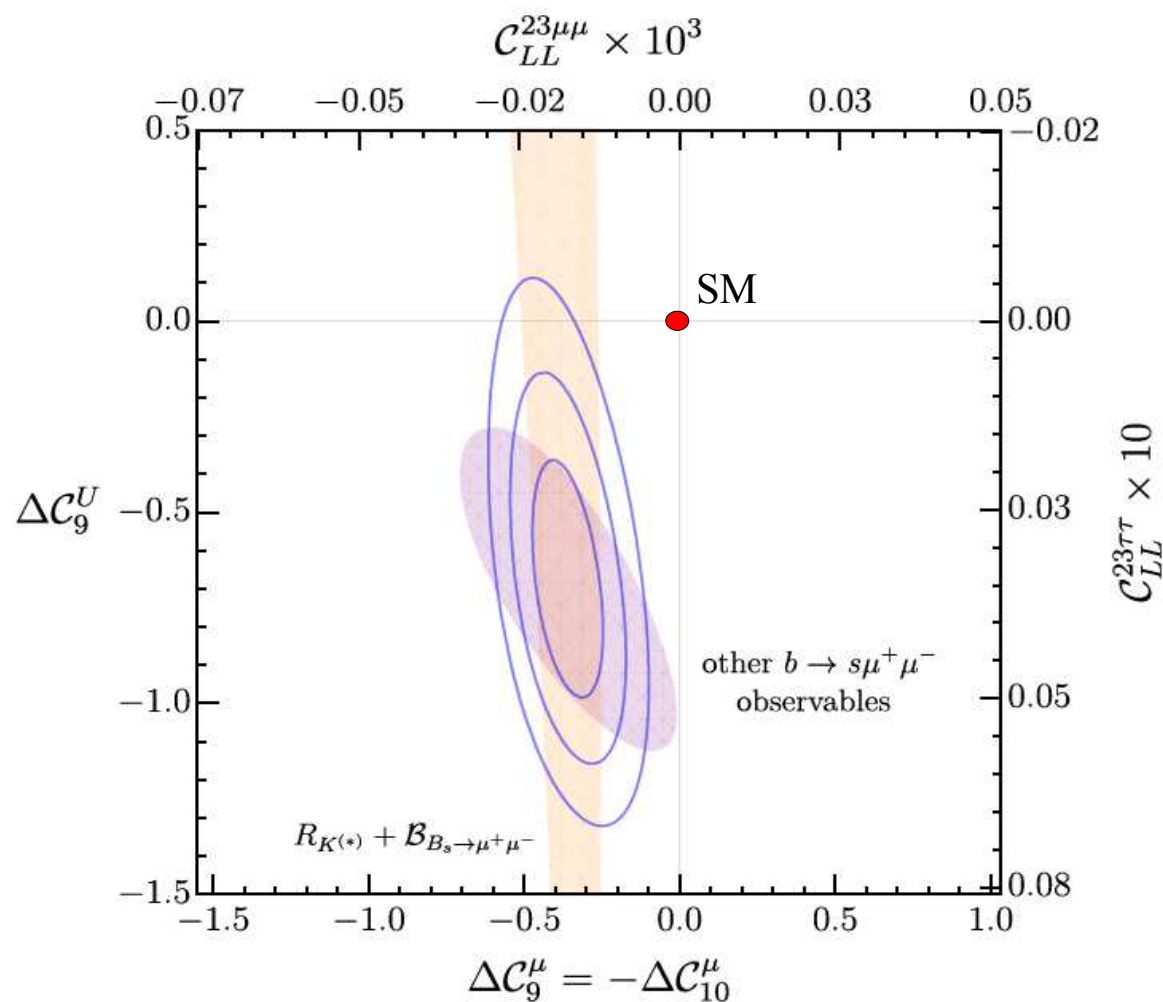
Some *historical* remarks,  
on how we arrived here:

2013  $P_5'$  [ $B \rightarrow K^* \mu\mu$ ]  $\rightarrow C_9 \neq C_9^{\text{SM}}$  Descotes-Genon,  
Matias, Virto '13

2014 hypothesis  $\Delta C_9^\mu = -\Delta C_{10}^\mu$   
 $\Rightarrow R_{K^*} \sim R_K$  &  $B(B_s \rightarrow \mu\mu) < B_{\text{SM}}$

Hiller & Schmaltz '14

$$\mathcal{O}_{LL}^{ij\alpha\beta} = (\bar{q}_L^i \gamma_\mu \ell_L^\alpha) (\bar{\ell}_L^\beta \gamma_\mu q_L^j)$$





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 $\implies R_{K^*} \sim R_K$  &  $B(B_s \rightarrow \mu\mu) < B_{\text{SM}}$  2017-19

Hiller & Schmaltz '14

2015 U(2) hypothesis for  $b \rightarrow s$  &  $b \rightarrow c$   
combined  $\implies C^{23\tau\tau} \sim O(10^2) \times C^{23\mu\mu}$

Barbieri, GI, Patteri, Senia '15  
 [+ others...]

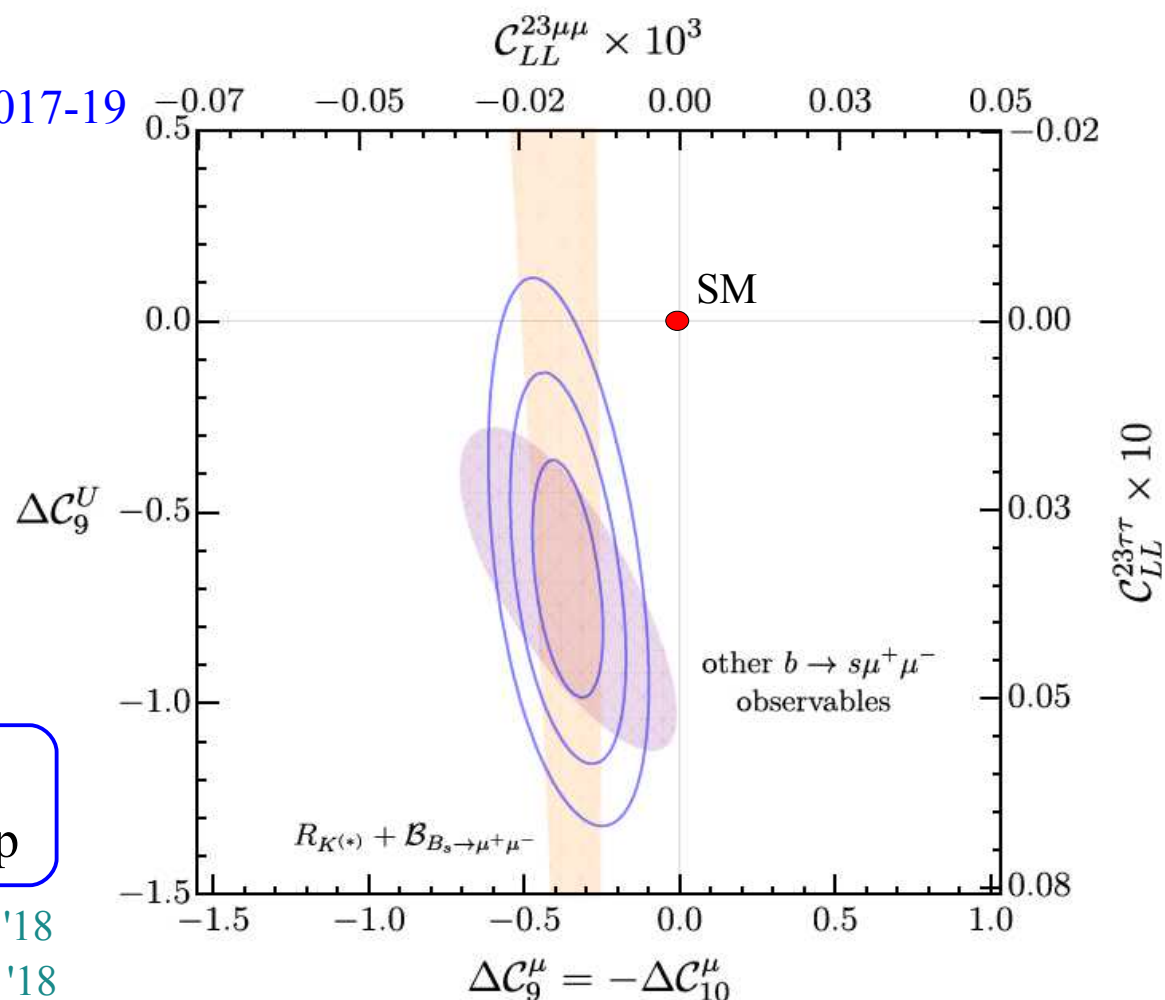
2017 High-pT and EWPO

$\implies C^{23\tau\tau}$  needed to explain  $b \rightarrow c$   
 Buttazzo, Greljo, GI, Marzocca '17

2018 - 2021 evidence of  $\Delta C_9^U$  from global fits  
 of correct size from  $C^{23\tau\tau}$  @ 1-loop

Crivellin, Greub, Muller, Saturnino '18

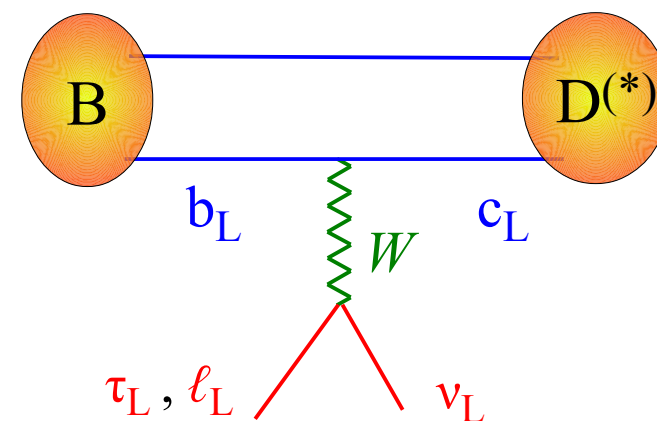
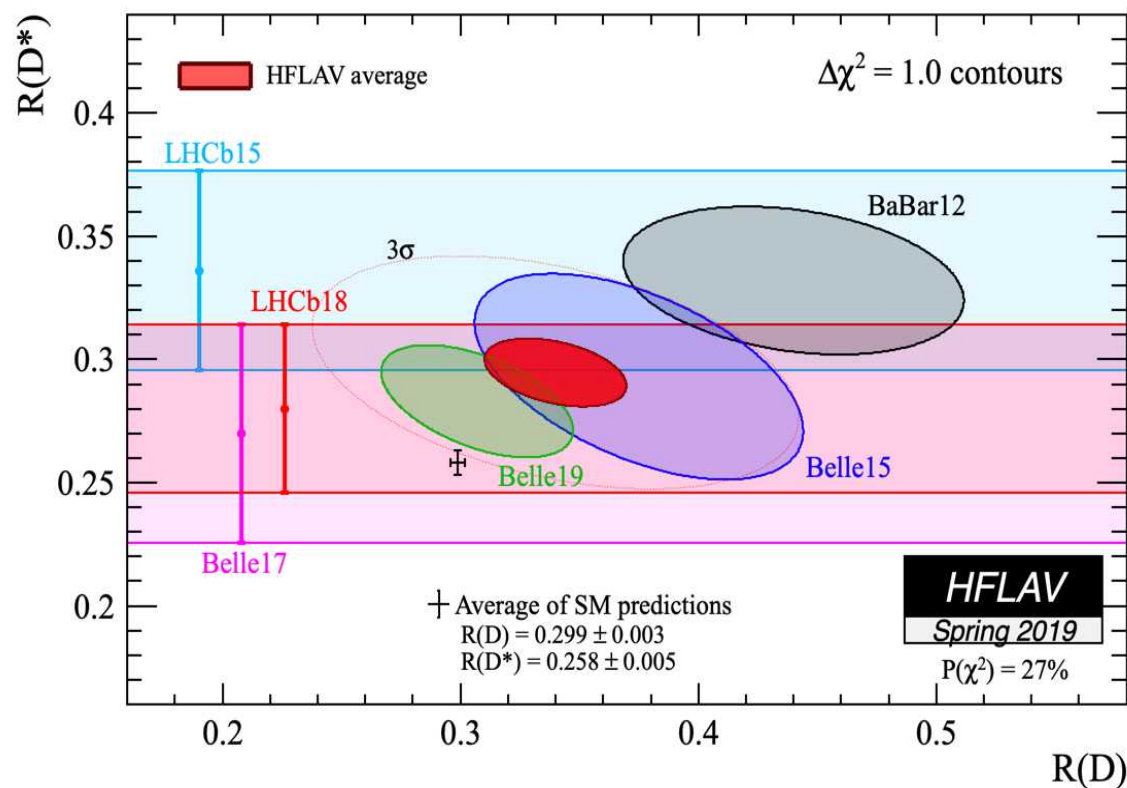
Alguero et al. '18



► A closer look to the data

- $b \rightarrow c \ell \bar{\nu}$  (charged currents):  $\tau$  vs. light leptons ( $\mu, e$ )

$$R(X) = \frac{\Gamma(B \rightarrow X \tau \bar{\nu})}{\Gamma(B \rightarrow X \ell \bar{\nu})} \quad X = D \text{ or } D^*$$

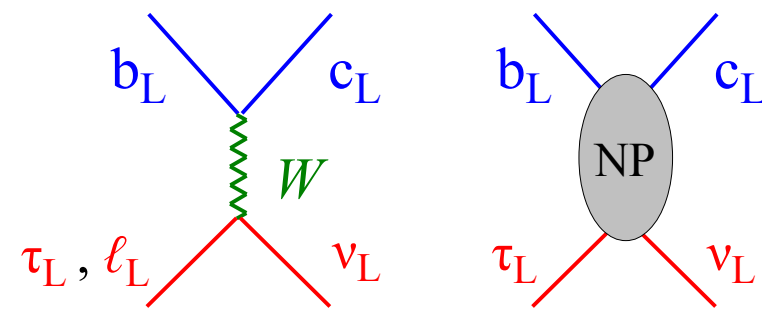
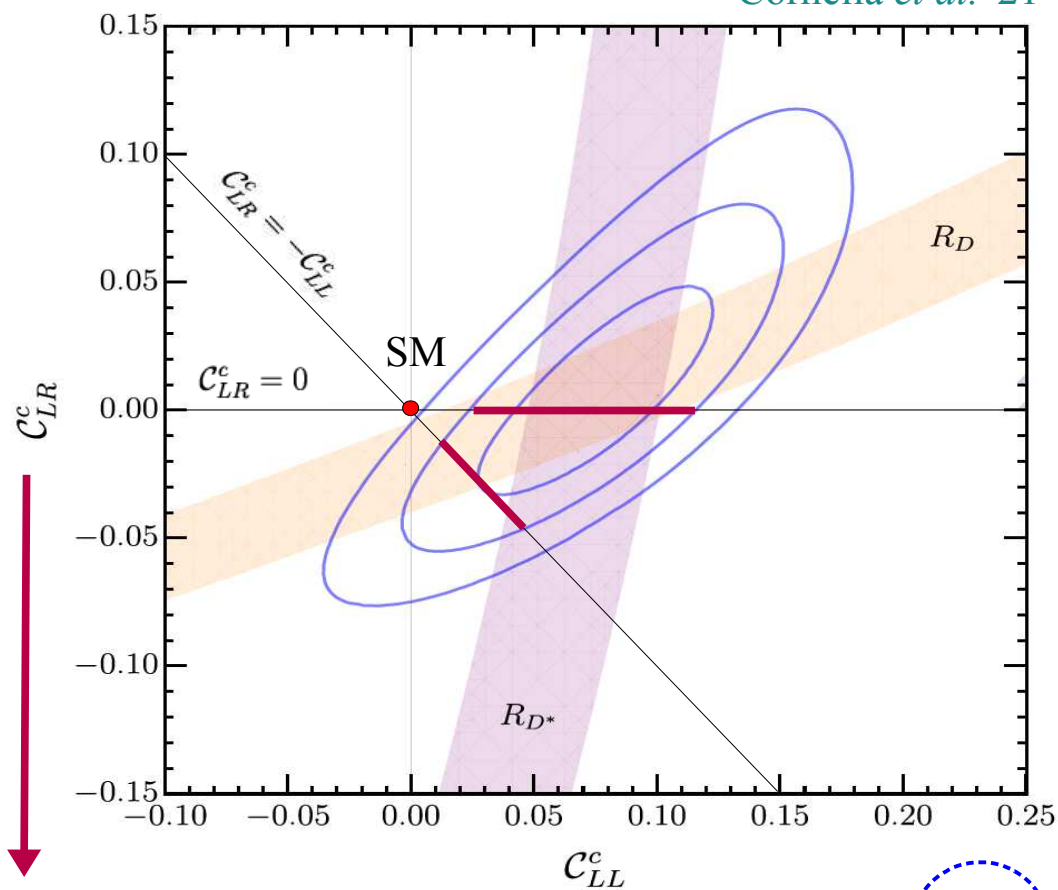


- Consistent results by three different exps.  $\sim 3.1\sigma$  excess over SM ( $D$  and  $D^*$  combined)
- SM predictions quite “clean”: hadronic uncertainties cancel (to large extent) in the ratios

► A closer look to the data

- $b \rightarrow c \ell \nu$  (charged currents):  $\tau$  vs. light leptons ( $\mu, e$ )

Cornella et al. '21



Data consistent with a universal enhancement (10-20%) of  $\tau$  modes  
 But other options (*RH currents*) possible

$$(\bar{q}_L^i \gamma_\mu \tau_L)(\bar{\tau}_R \gamma_\mu b_R)$$

CKM “weighted mix” as for  $C_{LL}^c$

$$\frac{V_{cb} C_{LL}^{33\tau\tau} + V_{cs} C_{LL}^{23\tau\tau}}{V_{cb}}$$

Same operator contributing to  $b \rightarrow s \ell \ell$

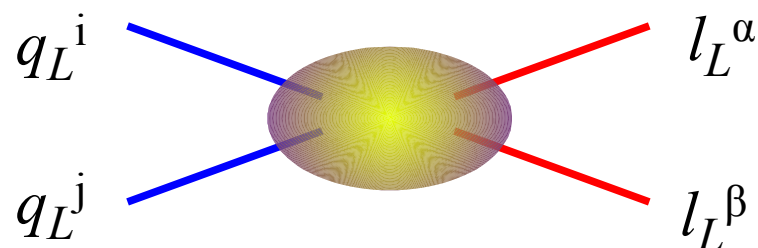
all 3<sup>rd</sup> gen. (contribute via CKM rotation)

## EFT considerations



## ► EFT considerations

- Anomalies are seen only in semi-leptonic (**quark**×**lepton**) operators
- We definitely need non-vanishing **left-handed** current-current operators although other contributions are also possible



Bhattacharya *et al.* '14  
 Alonso, Grinstein, Camalich '15  
 Greljo, GI, Marzocca '15  
 (+many others...)

- Large coupling [*competing with SM tree-level*] in **bc** →  $l_3 \nu_3$  [ $\mathbf{R}_D, \mathbf{R}_{D^*}$ ]
- Small coupling [*competing with SM loop-level*] in **bs** →  $l_2 l_2$  [ $\mathbf{R}_K, \mathbf{R}_{K^*}, \dots$ ]



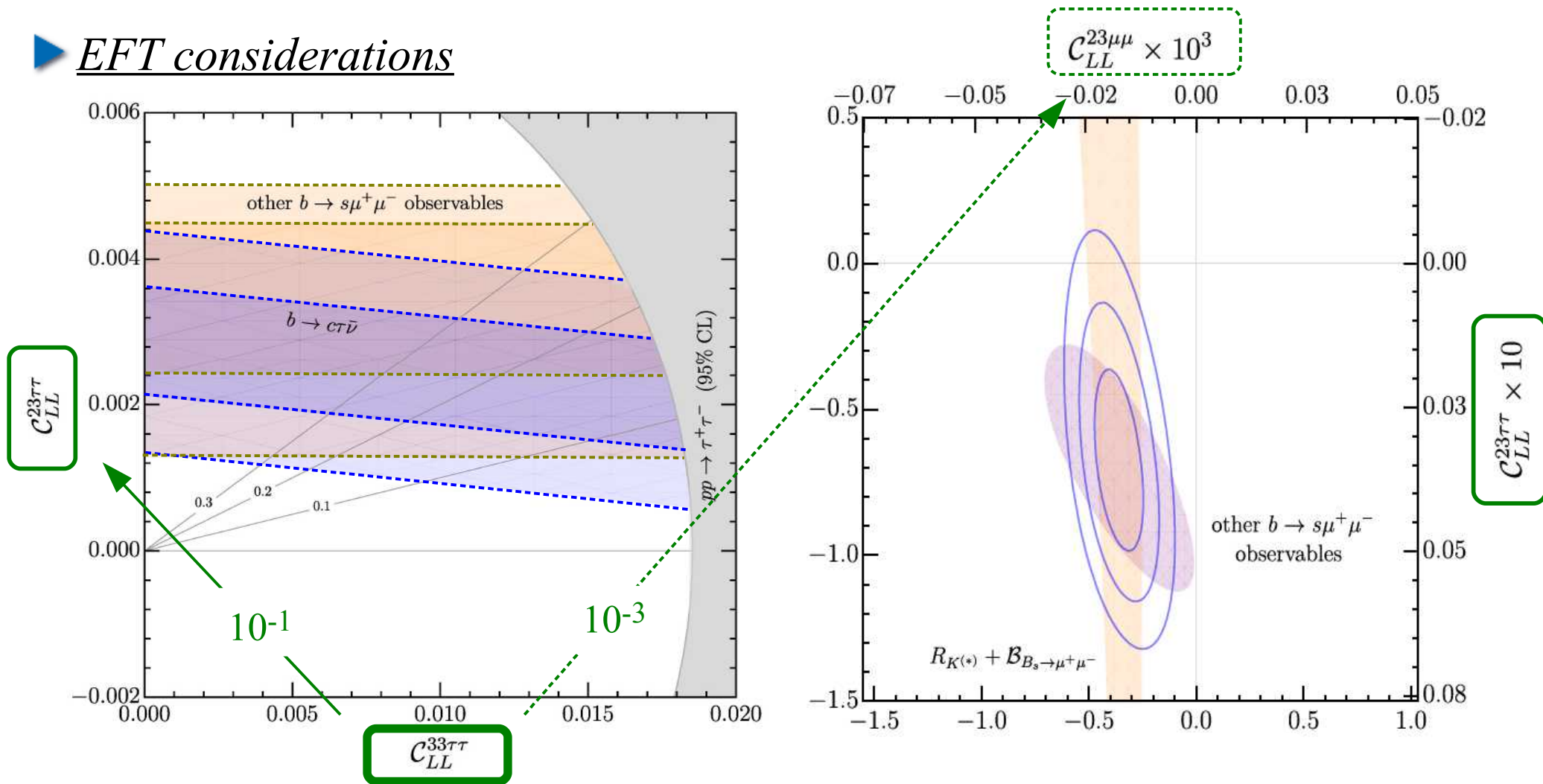
$$T_{ij\alpha\beta} = (\delta_{i3} \times \delta_{3j}) \times (\delta_{\alpha 3} \times \delta_{3\beta}) +$$

small terms  
 for 2<sup>nd</sup> (& 1<sup>st</sup>)  
 generations



*Link to pattern  
 of the Yukawa  
 couplings !*

► EFT considerations



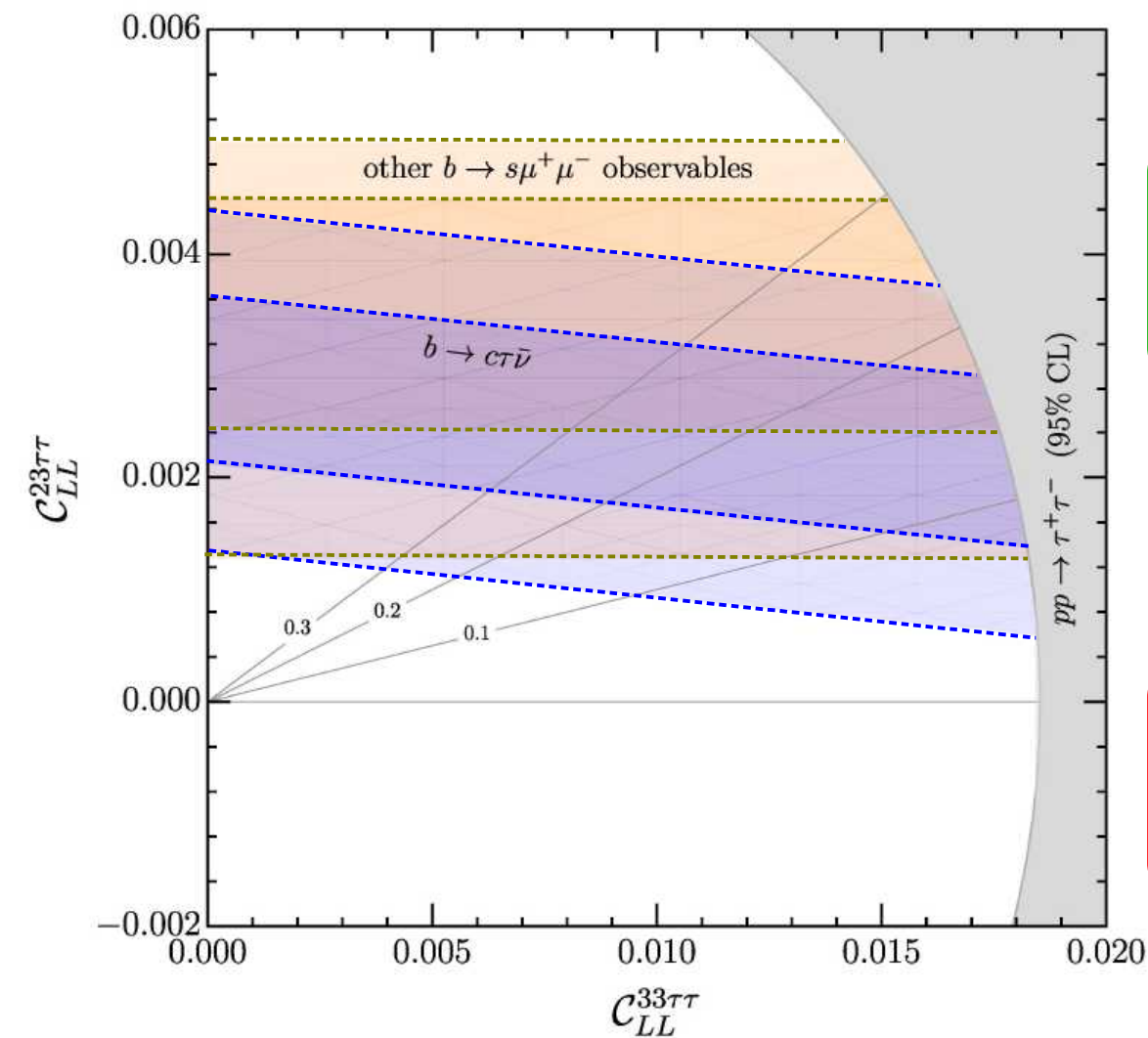
Pattern emerging from data:

$$\mathcal{O}_{LL}^{ij\alpha\beta} = (\bar{q}_L^i \gamma_\mu \ell_L^\alpha) (\bar{\ell}_L^\beta \gamma_\mu q_L^j)$$

- ✓  $O(10^{-1})$  suppress. for each 2<sup>nd</sup> gen.  $q_L$  or  $l_L$  [ recall  $|V_{ts}| \sim 0.4 \times 10^{-1}$  ]
- ✓ Nice consistency among the 2 sets of anomalies

## ► EFT considerations

$$\mathcal{O}_{LL}^{ij\alpha\beta} = (\bar{q}_L^i \gamma_\mu \ell_L^\alpha) (\bar{\ell}_L^\beta \gamma_\mu q_L^j) = \frac{1}{2} \left[ \mathcal{O}_{lq}^{(1)} + \mathcal{O}_{lq}^{(3)} \right]^{ij\alpha\beta}$$



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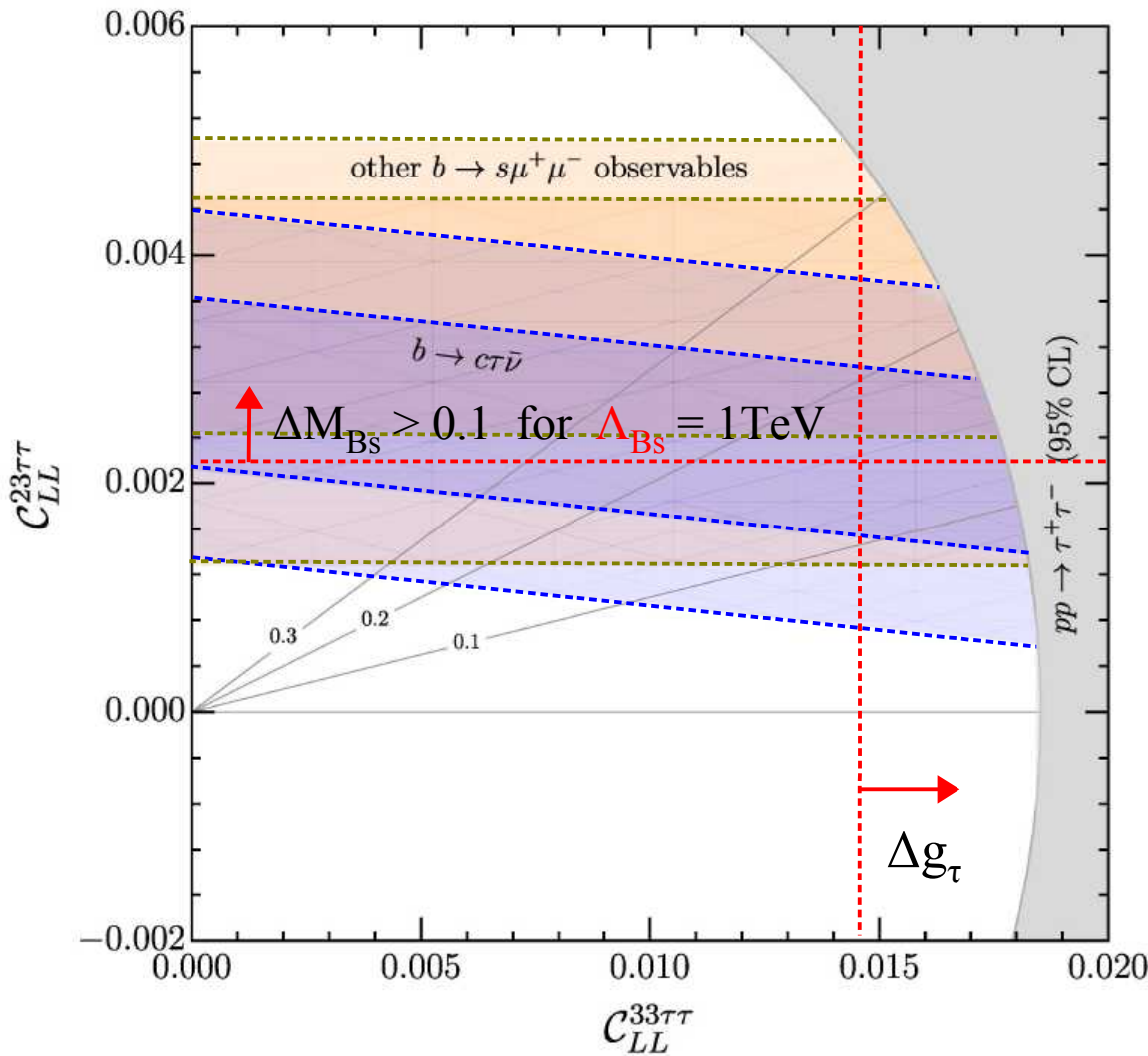
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What we do not see (*seem to call for an additional  $\sim$  loop suppression*):

- ✗ Four-quarks ( $\Delta F=2$ )
- ✗ Four-leptons ( $\tau \rightarrow \mu\nu\nu$ )
- ✗ Semi-leptonic  $O^{(1-3)}$  ( $b \rightarrow s\nu\nu$ )

► EFT considerations

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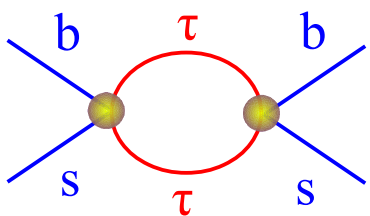


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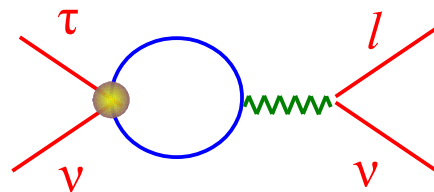
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$$\Delta M_{B_s} \sim (C^{23\tau\tau})^2 \Lambda_{B_s}^2$$



$$\Delta g_\tau \sim (C^{33\tau\tau}) \log(\Lambda/m_t)$$

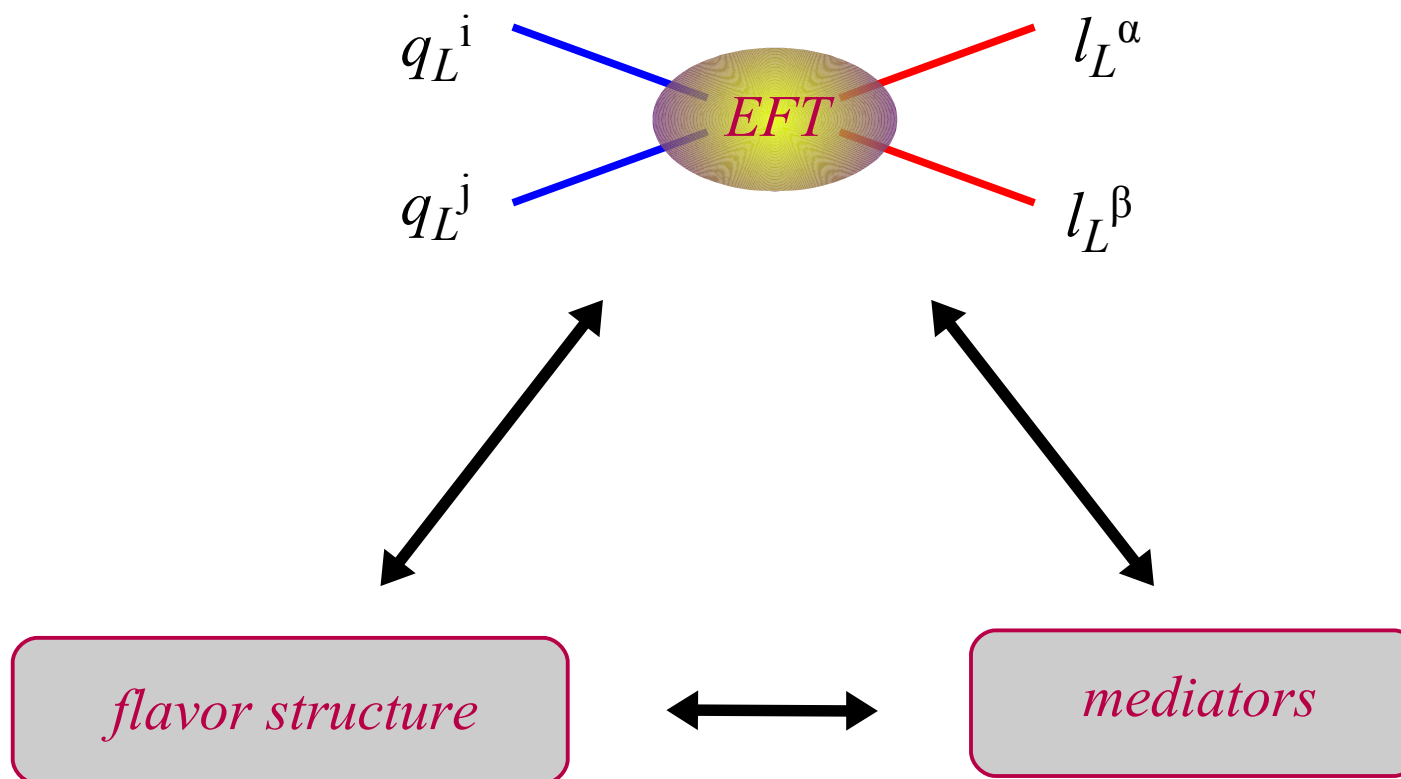


## From EFT to simplified models



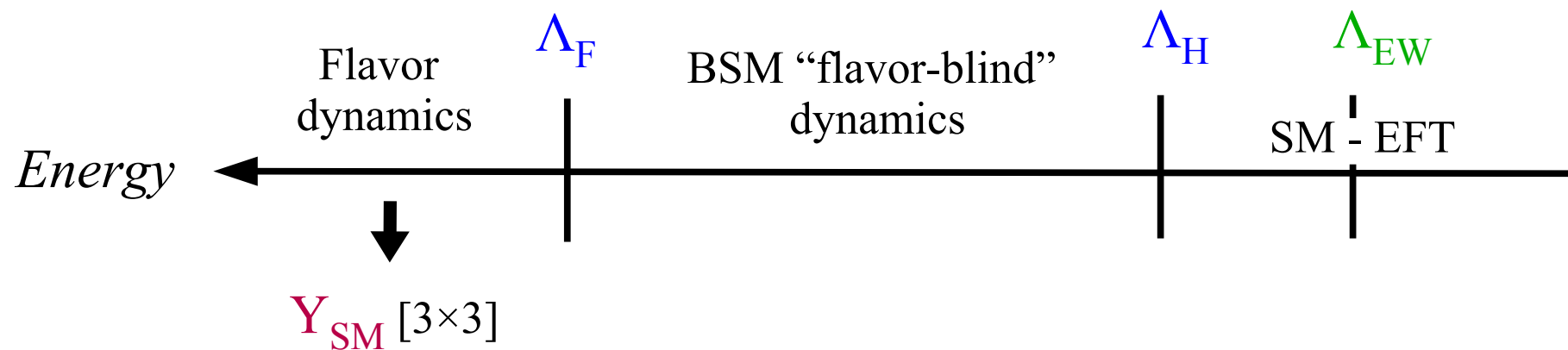
► From EFT to simplified models

To move from the EFT toward more complete/ambitious models, we need to address two general aspects: the *flavor structure* of the underlying theory, and the nature of the possible *mediators*



► From EFT to simplified models [the flavor structure]

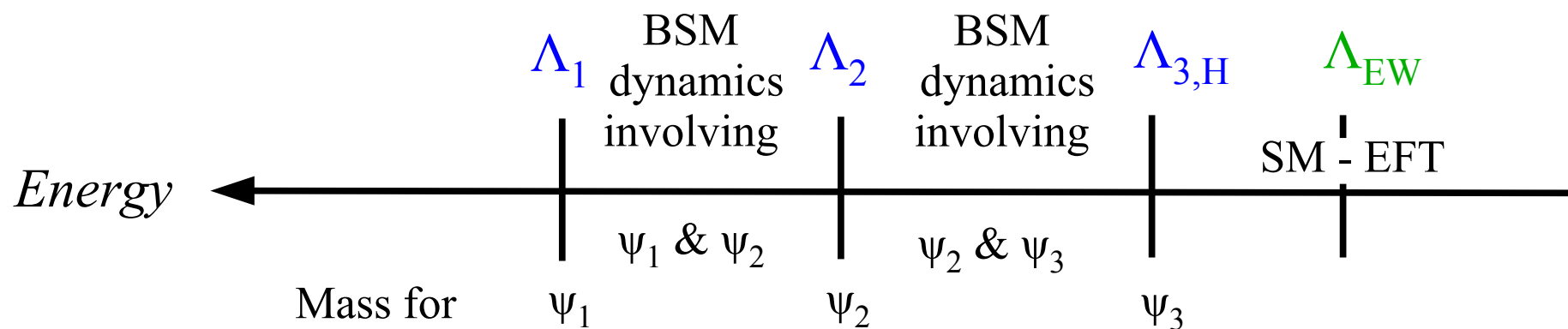
*The MFV paradigm:*



► From EFT to simplified models [the flavor structure]

~~The MFV paradigm~~

Multi-scale picture @ origin of flavor:



Light families have small masses because they are coupled to heavier states

- Barbieri '21
- Allwicher, GI, Thomsen '20
- ⋮
- Bordone *et al.* '17
- Panico & Pomarol '16
- ⋮
- Dvali & Shifman '00

$$\mathcal{L}_{\text{SM-EFT}} = \mathcal{L}_{\text{gauge}} + \mathcal{L}_{\text{Higgs}} + \mathcal{L}_Y + \sum_i \frac{1}{\Lambda_i^{d-4}} \mathcal{O}_i^{d \geq 5}$$

Non-trivial UV imprints

► From EFT to simplified models [the flavor structure]

From the EFT point of view, the generic consequence of a construction of this type is that the nearby dynamics ( $E \sim \Lambda_3$ ) is characterized by an approximate  $U(2)^n$  flavor symmetry:

$$\begin{array}{c} \Psi \\ \uparrow \\ \text{SM fermion (e.g. } q_L) \end{array} = \begin{array}{c} \left[ \begin{array}{c} \Psi_1 \\ \Psi_2 \\ \dots \\ \Psi_3 \end{array} \right] \end{array} \begin{array}{l} \leftarrow \text{light generations (flavor doublet)} \\ \leftarrow \text{3}^{\text{rd}} \text{ generation (flavor singlet)} \end{array}$$

with suitable (small) symmetry-breaking terms, related to the SM Yukawa couplings  
[ *largest breaking*:  $3_L \rightarrow 2_L$  controlled by  $|V_{ts}| \sim 0.04$  ]

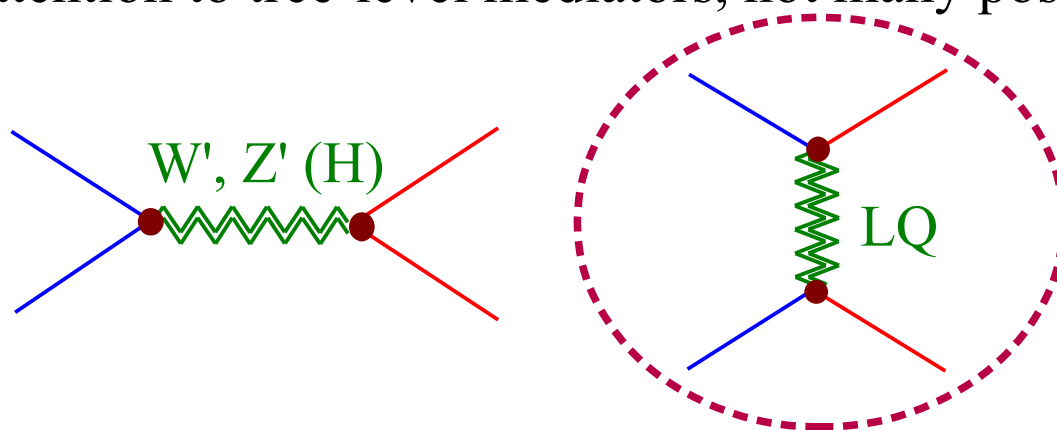
Barbieri, G.I., Jones-Perez,  
Lodone, Straub, '11

**NB:** In the 3-scale picture this flavor symmetry is an “accidental” symmetry, resulting from the (flavor) non-universal structure of BSM interactions

**N.B.:** this symmetry (& symmetry-breaking pattern) was proposed well-before the anomalies appeared...

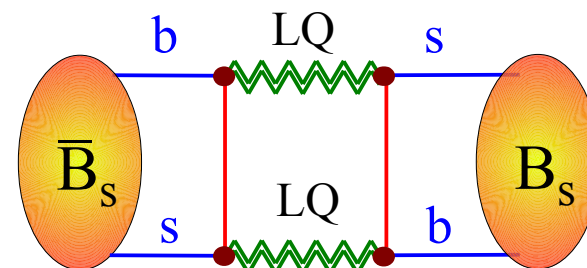
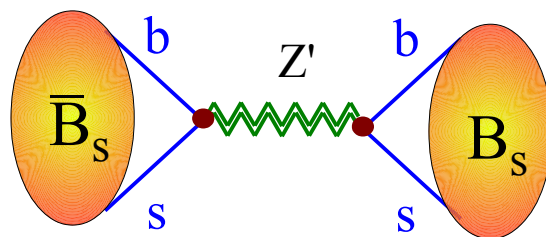
► From EFT to simplified models [the possible mediators]

Which mediators can generate the effective operators required for by the EFT fit?  
If we restrict the attention to tree-level mediators, not many possibilities...



LQ (both scalar and vectors) have two general strong advantages with respect to the other mediators:

I.  $\Delta F=2$  &  
 $\tau \rightarrow l\nu\nu$



II. Direct searches:

3<sup>rd</sup> gen. LQ are also in better shape as far as direct searches are concerned (*contrary to Z'...*).

► From EFT to simplified models [the possible mediators]

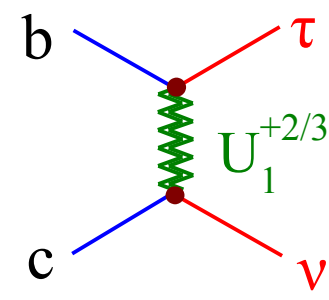
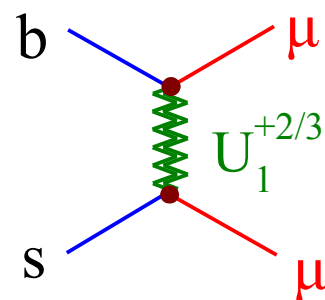
“Renaissance” of LQ models (*to explain the anomalies, but not only...*):

- Scalar LQ as PNG  
Gripaios, '10  
Gripaios, Nardecchia, Renner, '14  
Marzocca '18
- Scalar LQ from GUTs & ~~R~~ SUSY  
Hiller & Schmaltz, '14; Becirevic *et al.* '16,  
Fajfer *et al.* '15-'17; Dorsner *et al.* '17;  
Crivellin *et al.* '17; Altmannshofer *et al.* '17  
Trifinopoulos '18, Becirevic *et al.* '18 + ...
- Vector LQ in GUT gauge models  
Assad *et al.* '17  
Di Luzio *et al.* '17  
Bordone *et al.* '17  
Heeck & Teresi '18  
+ ...
- Vector LQ as techni-fermion resonances  
Barbieri *et al.* '15; Buttazzo *et al.* '16,  
Barbieri, Murphy, Senia, '17 + ...
- LQ as Kaluza-Klein excit.  
Megias, Quiros, Salas '17  
Megias, Panico, Pujolas, Quiros '17  
Blanke, Crivellin, '18 + ...

Which LQ explains which anomaly?

	Model	$R_{K(*)}$	$R_{D(*)}$	$R_{K(*)}$ & $R_{D(*)}$
Scalars	$S_1 = (\mathbf{3}, \mathbf{1})_{-1/3}$	✗	✓	✗
	$R_2 = (\mathbf{3}, \mathbf{2})_{7/6}$	✗	✓	✗
	$\tilde{R}_2 = (\mathbf{3}, \mathbf{2})_{1/6}$	✗	✗	✗
	$S_3 = (\mathbf{3}, \mathbf{3})_{-1/3}$	✓	✗	✗
Vector	$U_1 = (\mathbf{3}, \mathbf{1})_{2/3}$	✓	✓	✓
	$U_3 = (\mathbf{3}, \mathbf{3})_{2/3}$	✓	✗	✗

Angelescu, Becirevic, DAF, Sumensari [1808.08179]



► From EFT to simplified models [the possible mediators]

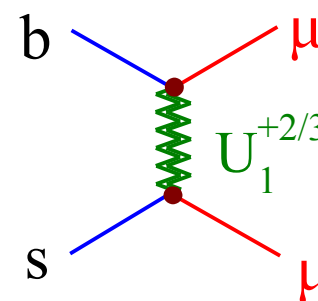
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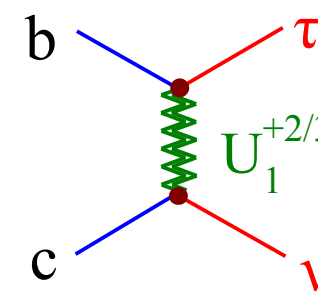
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Scalars	$S_1 = (\mathbf{3}, \mathbf{1})_{-1/3}$	✗	✓	✗
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	$S_3 = (\mathbf{3}, \mathbf{3})_{-1/3}$	✓	✗	✗
Vector	$U_1 = (\mathbf{3}, \mathbf{1})_{2/3}$	✓	✓	✓
	$U_3 = (\mathbf{3}, \mathbf{3})_{2/3}$	✓	✗	✗

Angelescu, Becirevic, DAF, Sumensari [1808.08179]



Barbieri, GI,  
Pattori, Senia '15

- mediator:  $U_1$
- flavor structure:  $U(2)^n$



LQ of the Pati-Salam gauge group:

$SU(4) \times SU(2)_L \times SU(2)_R$

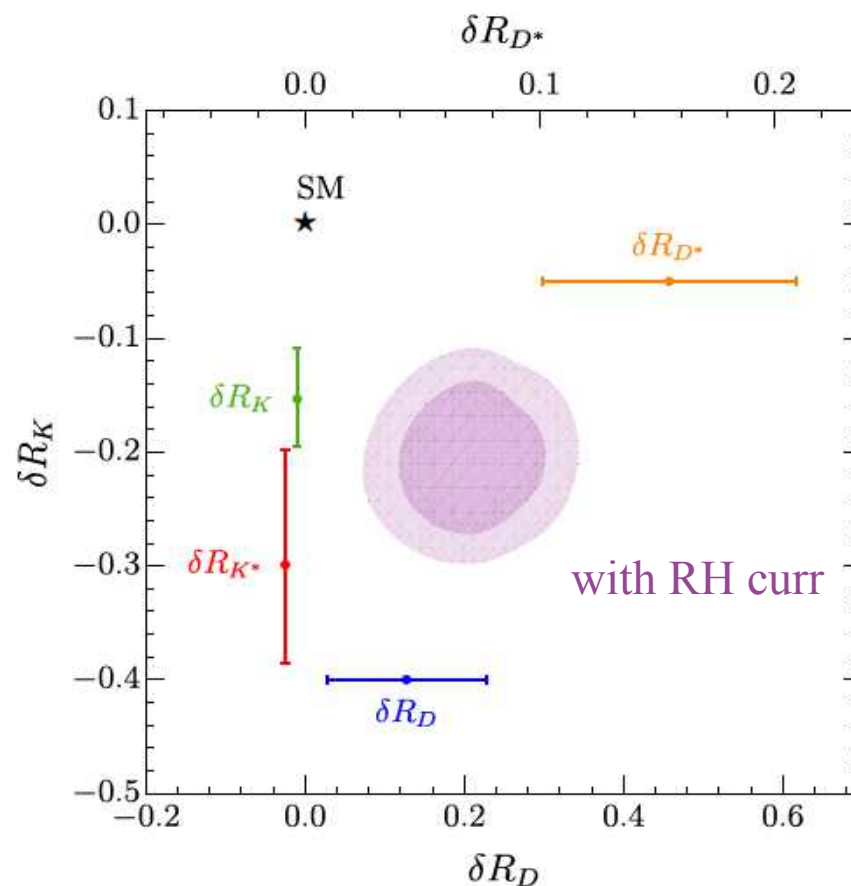
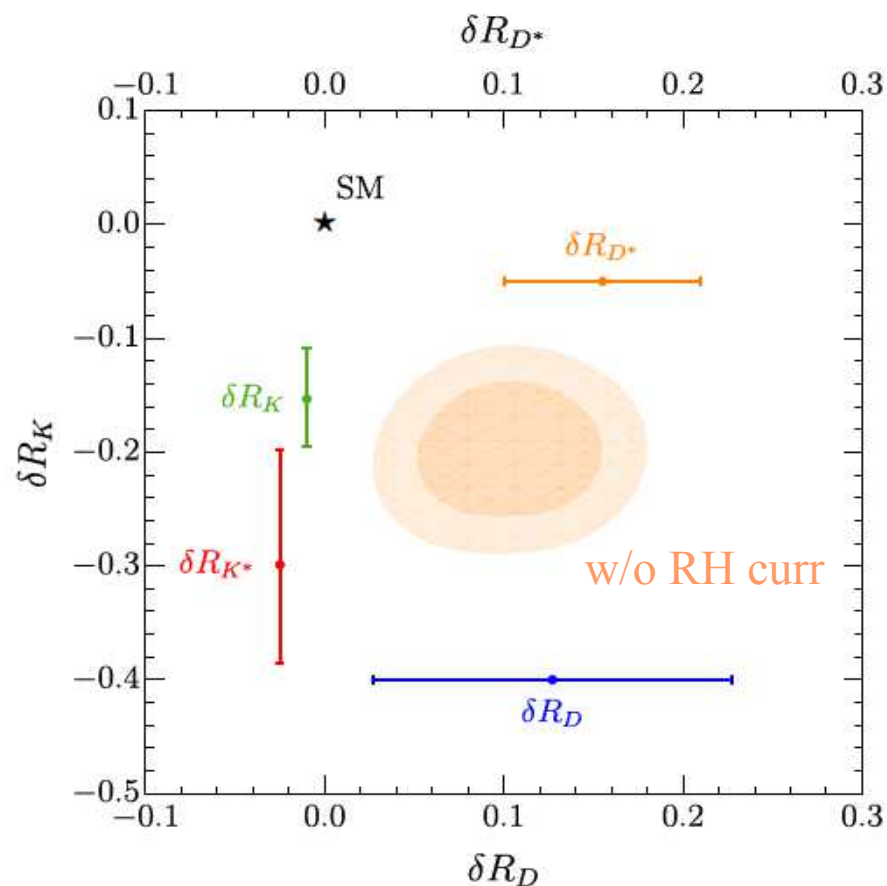


► From EFT to simplified models [the possible mediators]

Considering the  $U_1$  only

$$\mathcal{L} \supset \frac{g_U}{\sqrt{2}} U_1^\mu \left[ \beta_{i\alpha}^L (\bar{q}_L^i \gamma_\mu \ell_L^\alpha) - \beta_{i\alpha}^R (\bar{d}_R^i \gamma_\mu e_R^\alpha) \right] + \text{h.c.}$$

and fitting all low-energy data leads to an excellent description of present data:



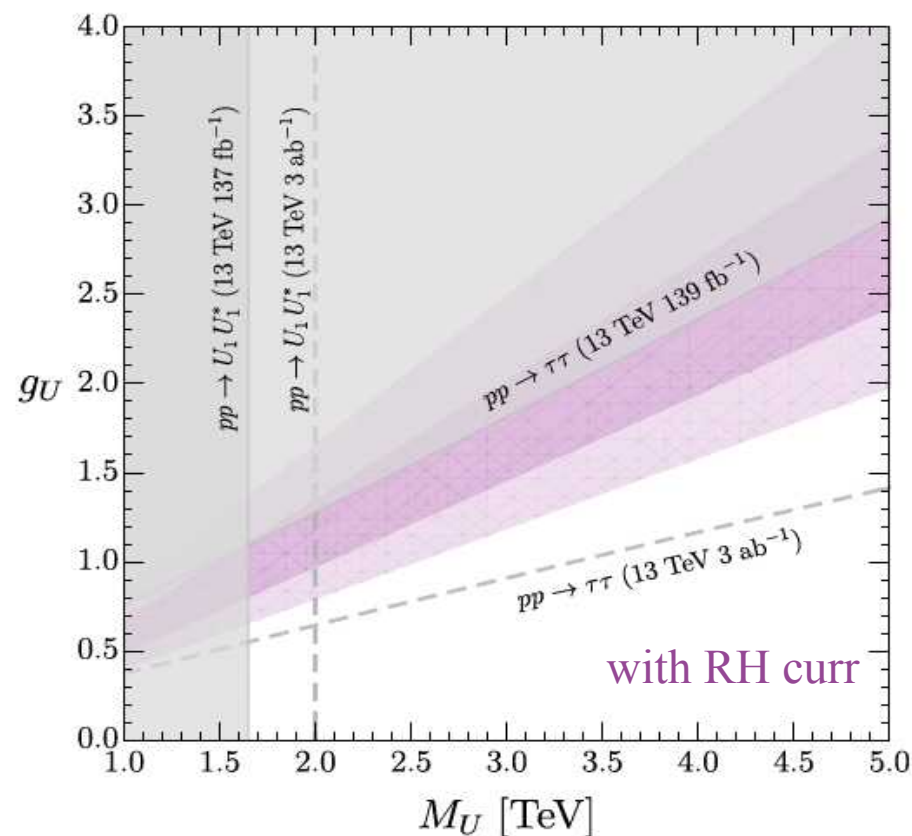
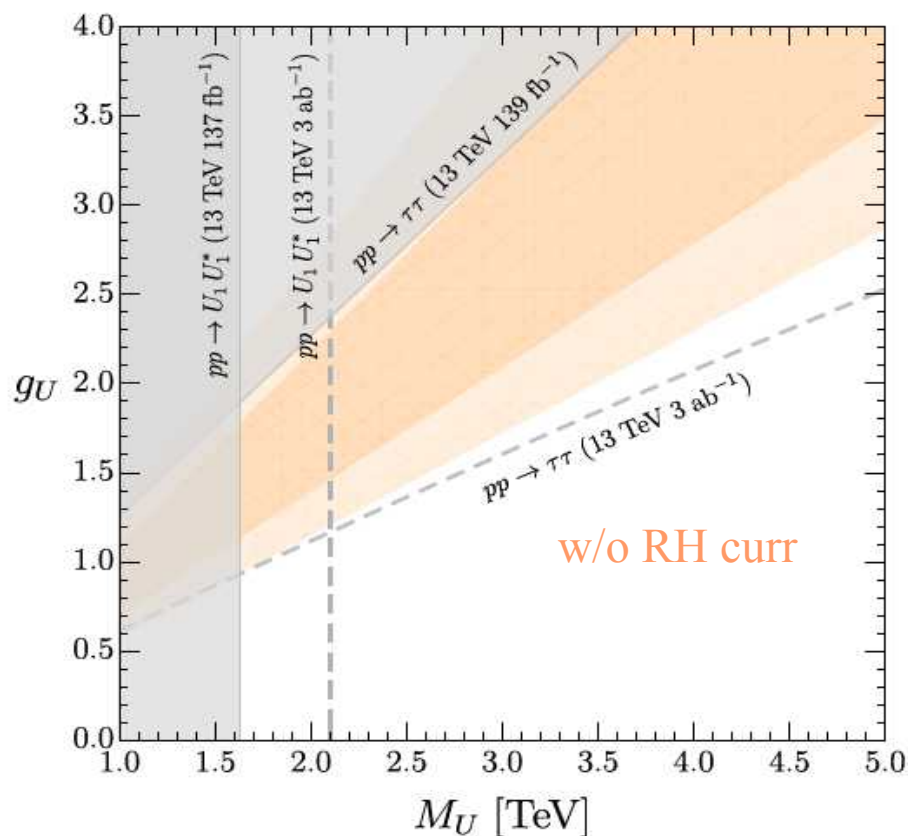
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and fitting all low-energy data leads to an excellent description of present data which is fully consistent with high-pT searches [*within the reach of HL-LHC*]:

Cornella, Fuentes-Martin, Faroughi, GI, Neubert, '21



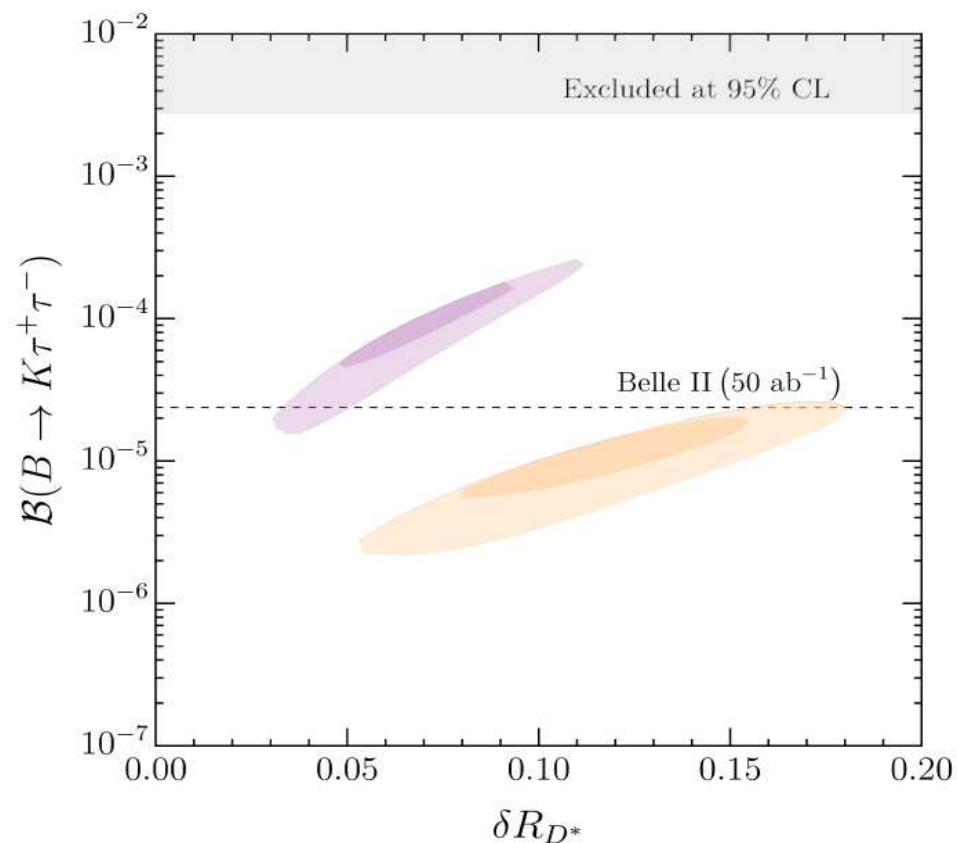
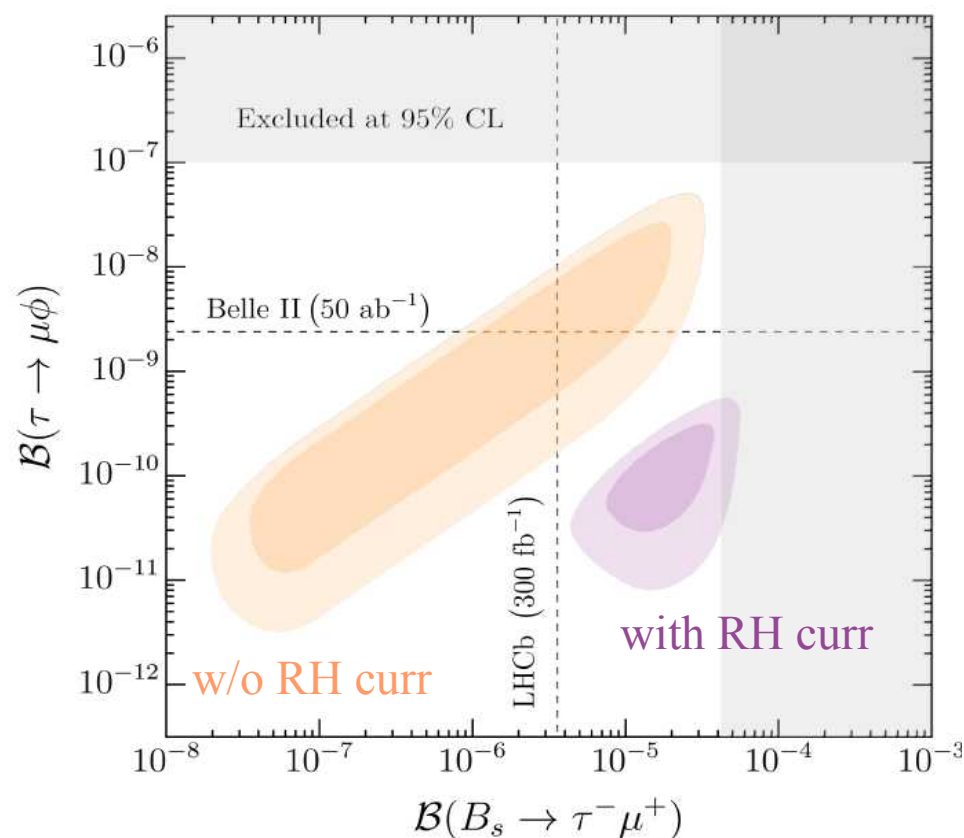
► From EFT to simplified models [the possible mediators]

Considering the  $U_1$  only

$$\mathcal{L} \supset \frac{g_U}{\sqrt{2}} U_1^\mu \left[ \beta_{i\alpha}^L (\bar{q}_L^i \gamma_\mu \ell_L^\alpha) - \beta_{i\alpha}^R (\bar{d}_R^i \gamma_\mu e_R^\alpha) \right] + \text{h.c.}$$

and fitting all low-energy data leads to an excellent description of present data which is fully consistent with high-pT searches & has interesting implications for future low-energy searches:

Cornella, Fuentes-Martin, Faroughi, GI, Neubert, '21



## Speculations on UV completions



## ► Speculations on UV completions

**First observation:** the Pati & Salam group, proposed in the 70's to unify quarks & leptons predicts the only massive LQ that is a good mediator for both anomalies:

Pati-Salam group:  $SU(4) \times SU(2)_L \times SU(2)_R$

Fermions in SU(4):

$$\begin{bmatrix} Q_L^\alpha \\ Q_L^\beta \\ Q_L^\gamma \\ L_L \end{bmatrix} \quad \begin{bmatrix} Q_R^\alpha \\ Q_R^\beta \\ Q_R^\gamma \\ L_R \end{bmatrix}$$

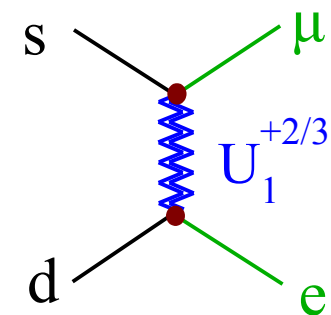
Main Pati-Salam idea:  
Lepton number as “the 4<sup>th</sup> color”

The massive LQ [ $U_1$ ] arise from the breaking  $SU(4) \rightarrow SU(3)_C \times U(1)_{B-L}$

The problem of the “original PS model” are the strong bounds on the LQ couplings to 1<sup>st</sup> & 2<sup>nd</sup> generations [e.g.  $M > 200 \text{ TeV}$  from  $K_L \rightarrow \mu e$ ]

*Attempts to solve this problem simply adding extra fermions or scalars*

Calibbi, Crivellin, Li, '17;  
Fornal, Gadam, Grinstein, '18  
Heeck, Teresi, '18

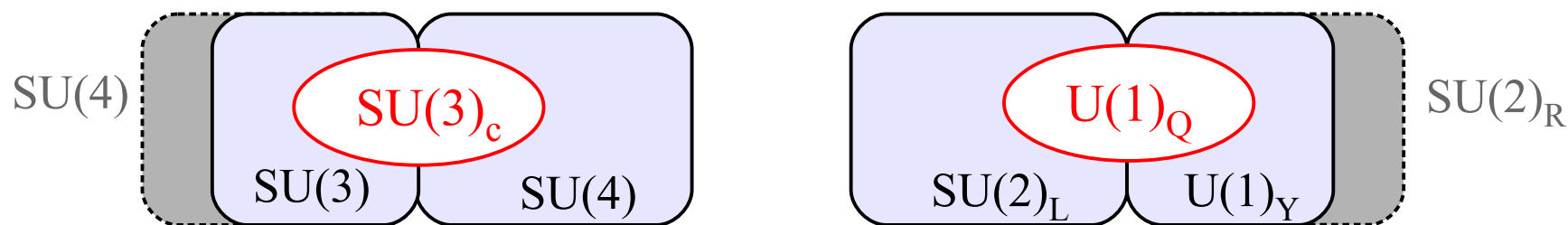


► Speculations on UV completions

**Second observation:** we can “protect” the light families charging under SU(4) only the 3rd gen. or, more generally, “separating” the universal SU(3) component

PS group:  $SU(4) \times SU(2)_L \times SU(2)_R$  • *flavor universality*

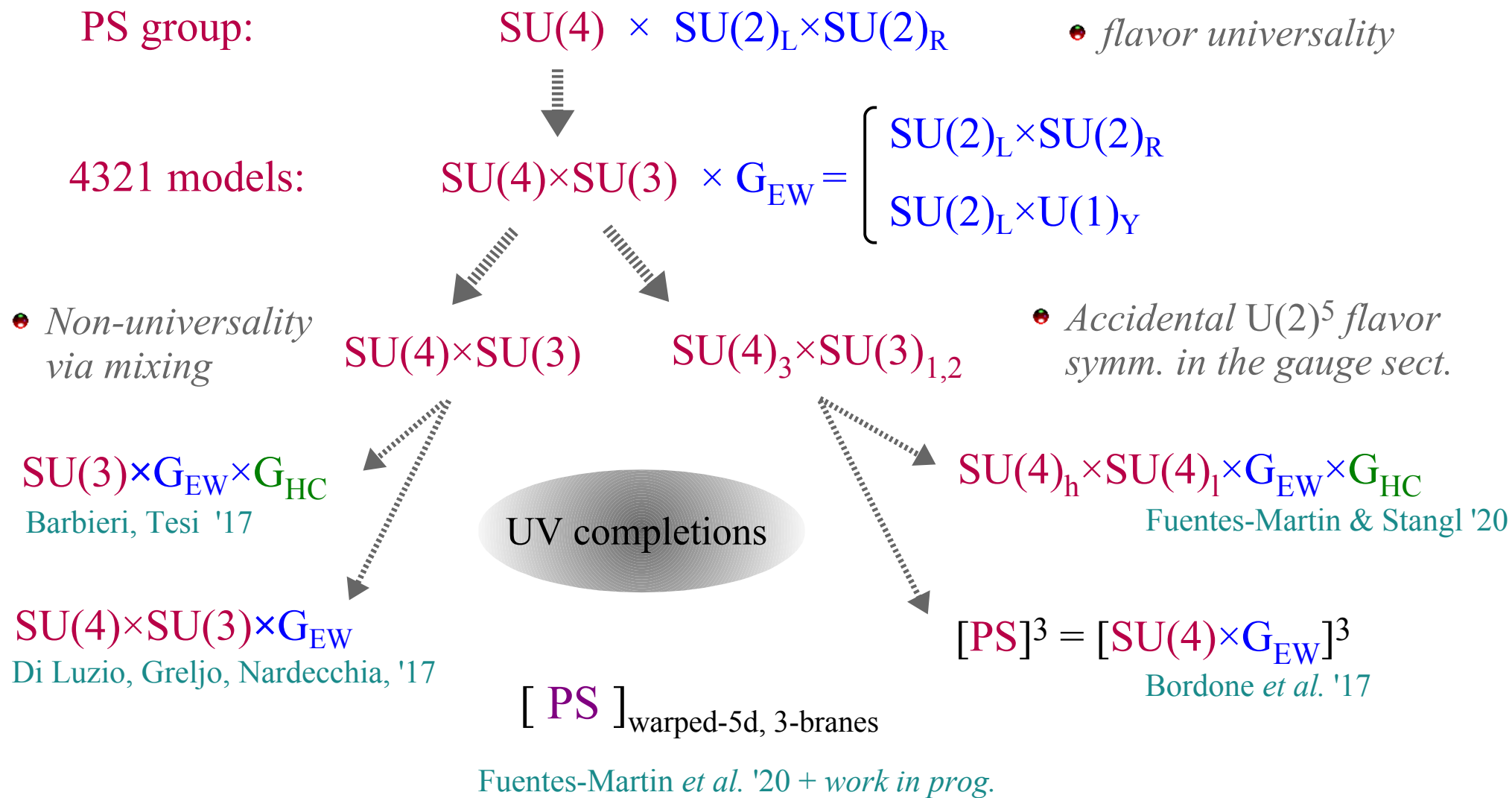
4321 models:  $SU(4) \times SU(3) \times G_{EW} = \begin{cases} SU(2)_L \times SU(2)_R \\ SU(2)_L \times U(1)_Y \end{cases}$



*This separation is not  
flavor blind*

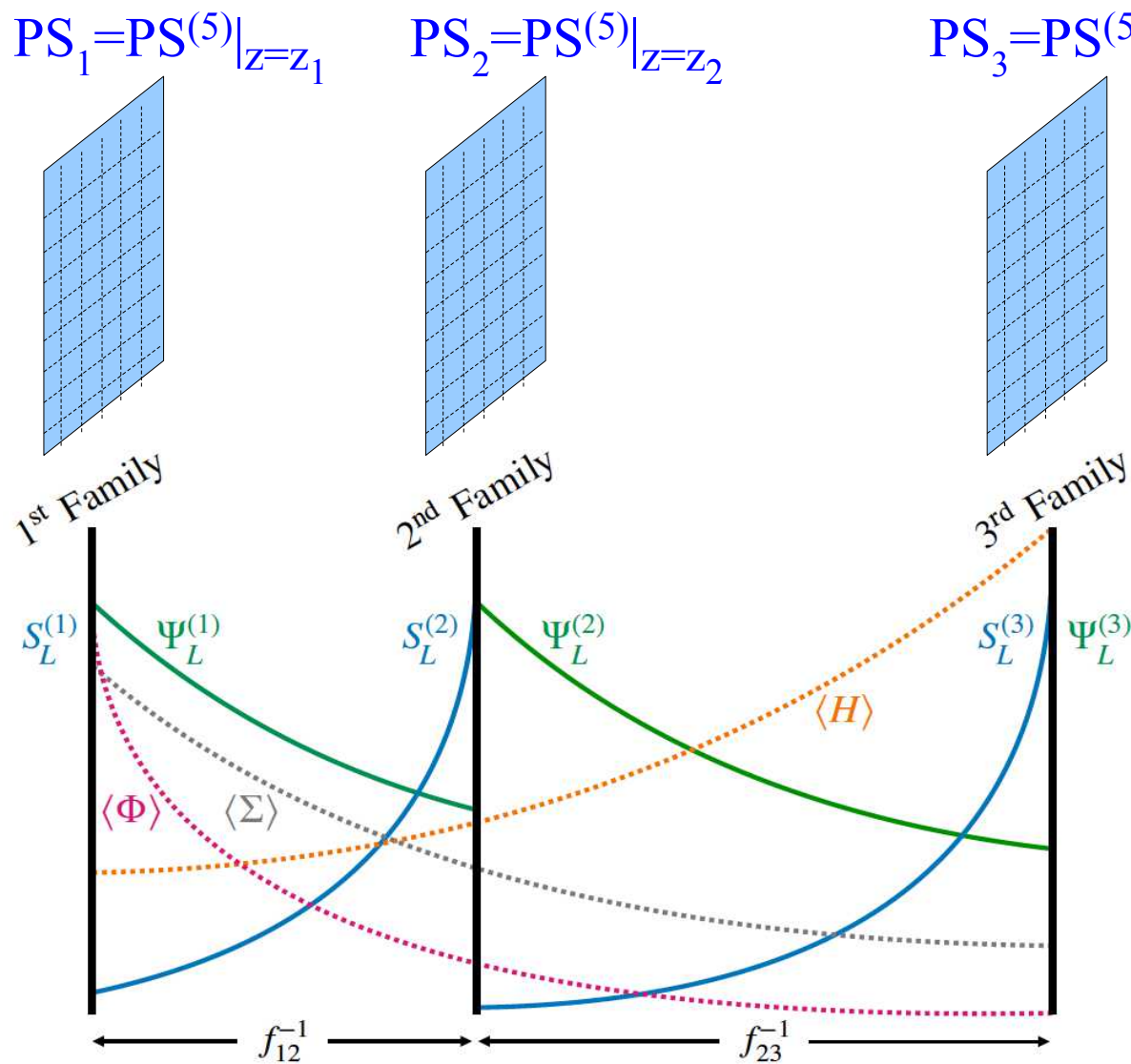
► Speculations on UV completions

**Second observation:** we can “protect” the light families charging under SU(4) only the 3rd gen. or, more generally, “separating” the universal SU(3) component



► Speculations on UV completions

An ambitious attempt to construct a *full theory of flavor* has been obtained embedding the Pati-Salam gauge group into an extra-dimensional construction:



Flavor  $\leftrightarrow$  special position  
(*topological defect*) in an  
extra (compact) space-like  
dimension

Dvali & Shifman, '00

Higgs and SU(4)-breaking fields  
with oppositely-peaked profiles,  
leading to the desired flavor  
pattern for masses & anomalies

Bordone, Cornella, Fuentes-Martin, GI '17  
Fuentes-Martin, GI, Pages, Stefaneck '20

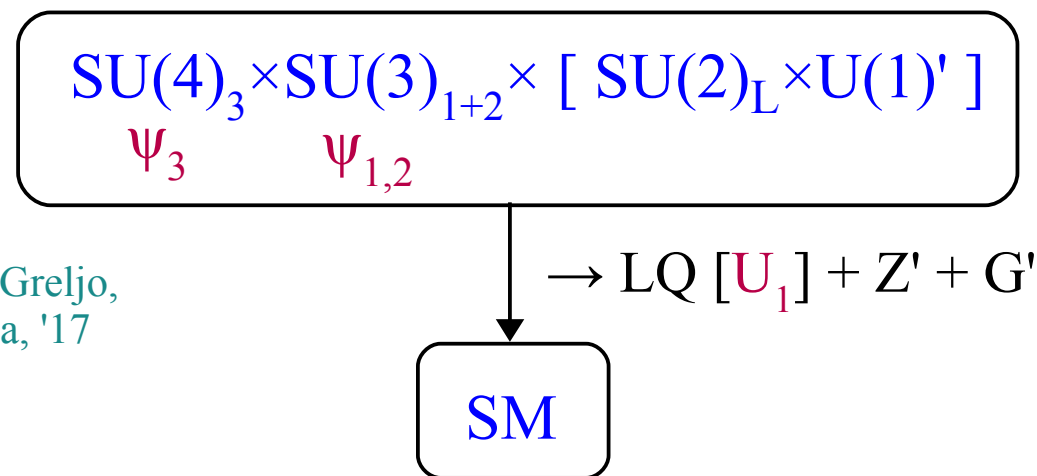
Possible to implement anarchic  
neutrino masses via an inverse  
see-saw mechanism



► Speculations on UV completions

In most *PS-extended models* collider and low-energy pheno are controlled by the effective 4321 gauge group that rules TeV-scale dynamics

Di Luzio, Greljo, Nardecchia, '17

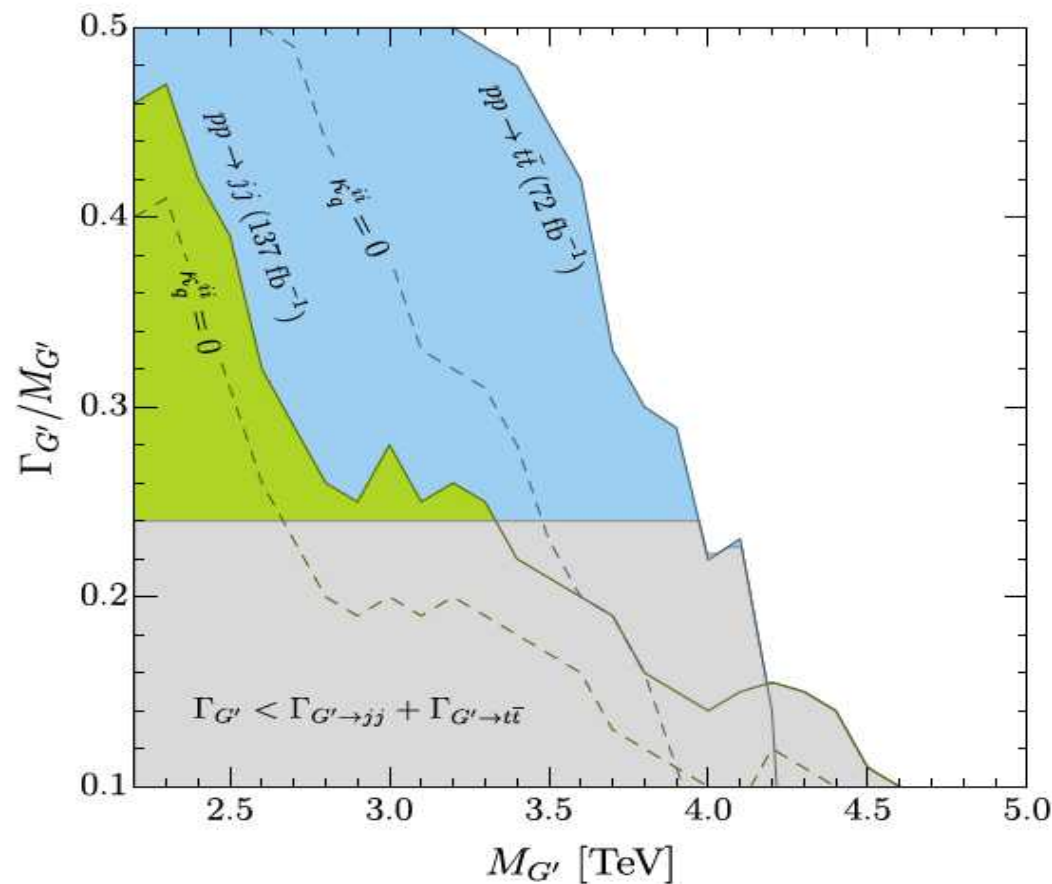


Despite the apparent complexity, the construction is highly constrained

- Positive features the EFT reproduced
  - Calculability of  $\Delta F=2$  processes
  - Precise predictions for **high-pT data**
- consistent with present data !

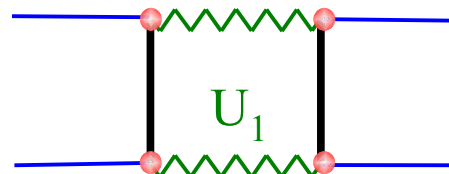
New striking collider signature:  $G'$  (“coloron” = heavy color octet)

→ strongest constraint on the scale of the model from  $pp \rightarrow t \bar{t}$

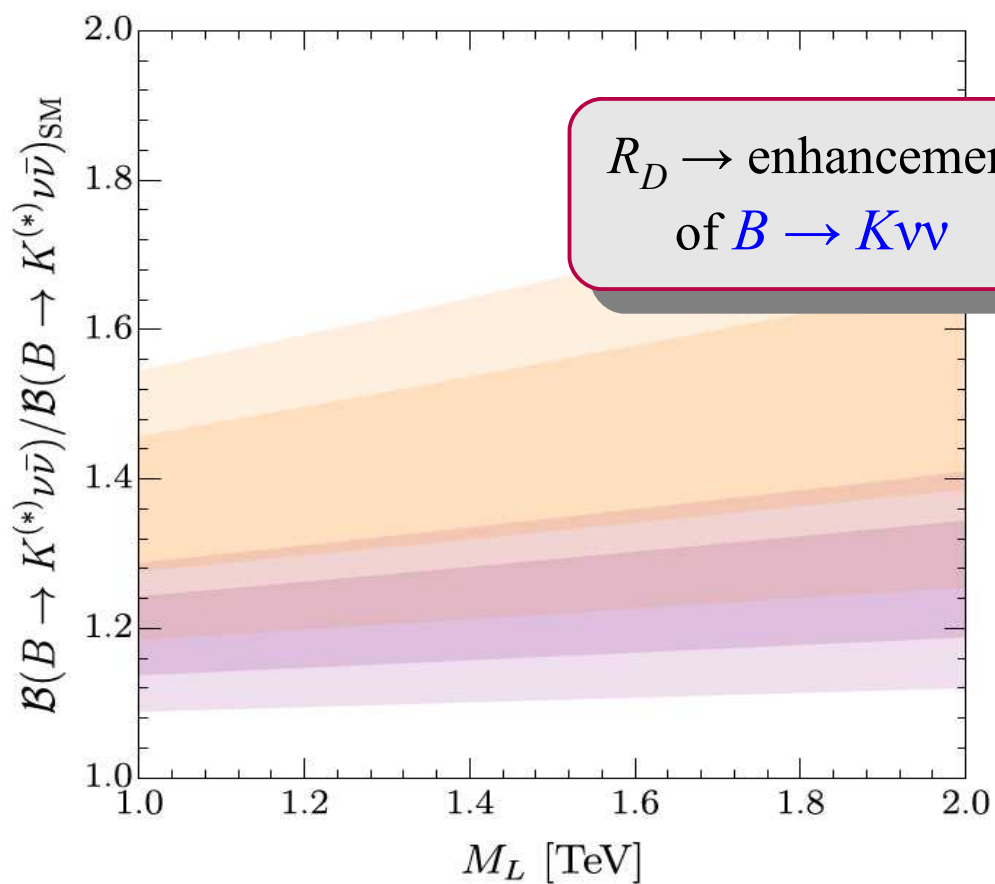


► Speculations on UV completions

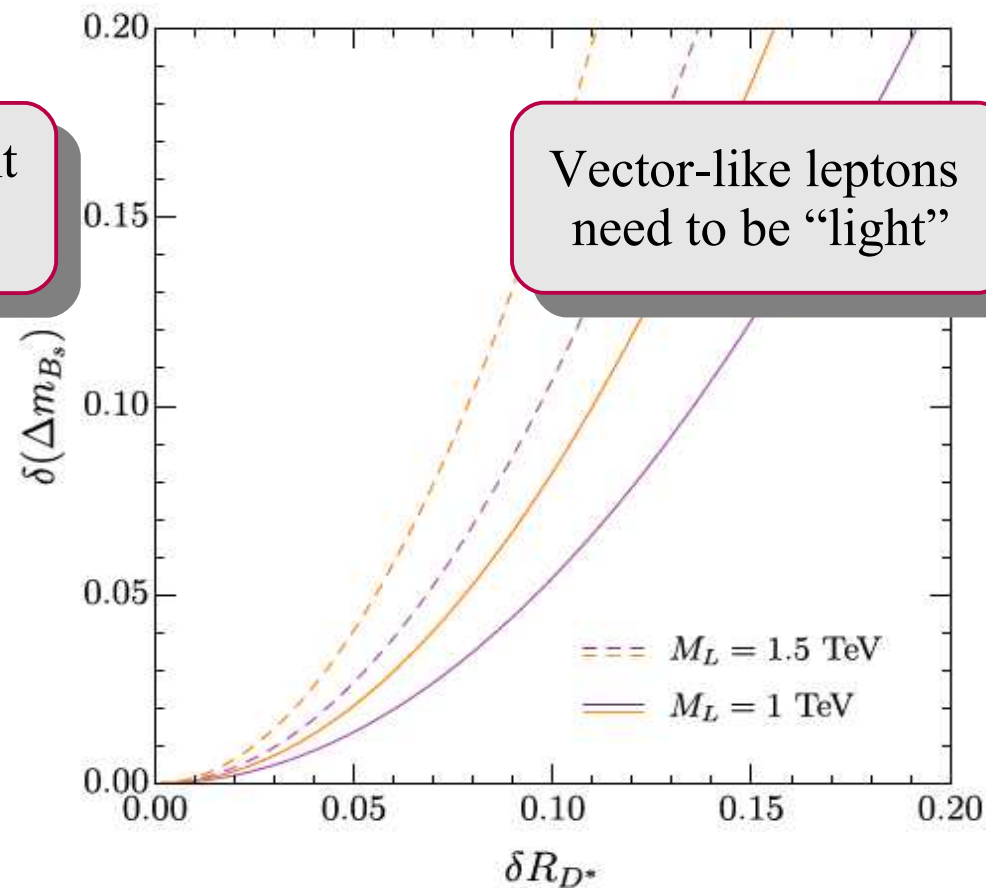
UV-sensitive observables in 4321 models



A)  $B \rightarrow K\nu\nu$



B)  $B_s$  mixing [ $\Delta F=2$ ]



## Conclusions

- The statistical significance of the **LFU anomalies is growing**: in the  $b \rightarrow sll$  system the chance this is a pure statistical fluctuation is marginal...
- If combined, the two sets of anomalies point to non-trivial flavor dynamics around the TeV scale, involving mainly the 3<sup>rd</sup> family  $\rightarrow$  **connection to the origin of flavor** [multi-scale picture at the origin of flavor hierarchies ]
- No contradiction with existing low- & high-energy data, but new non-standard effects should emerge soon in both these areas

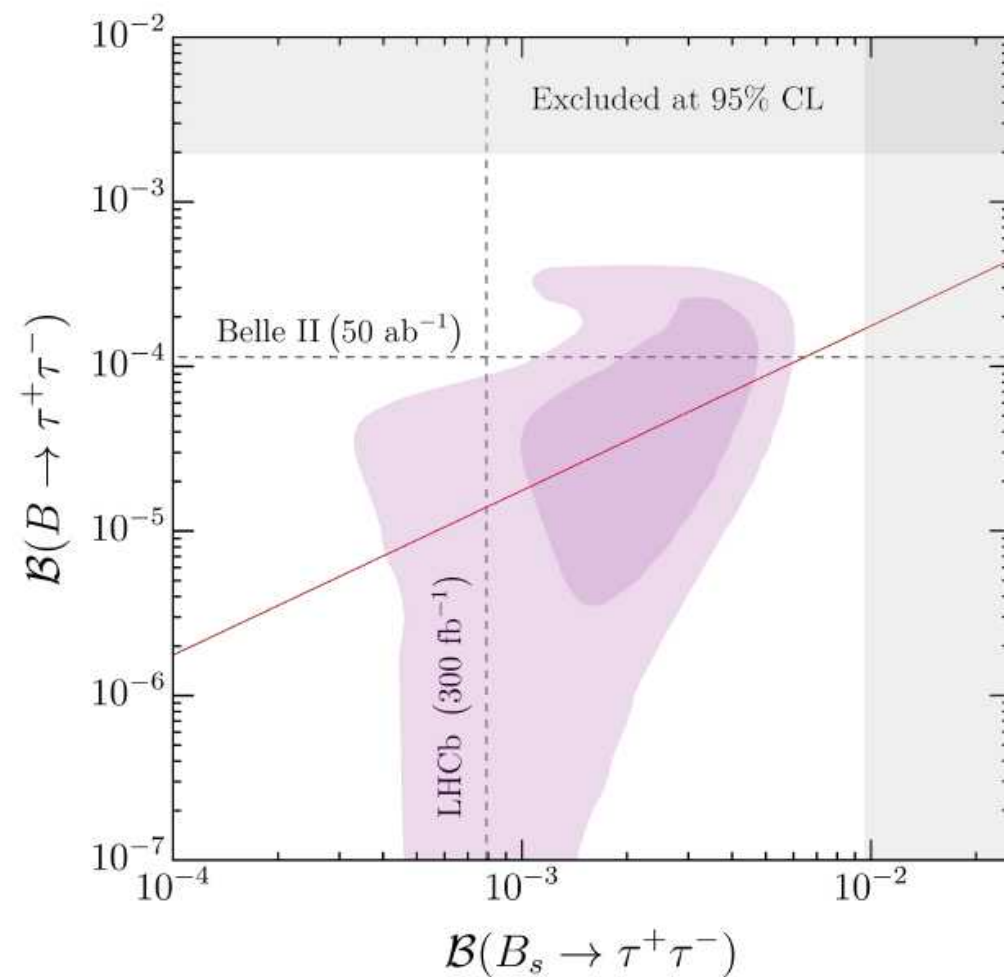
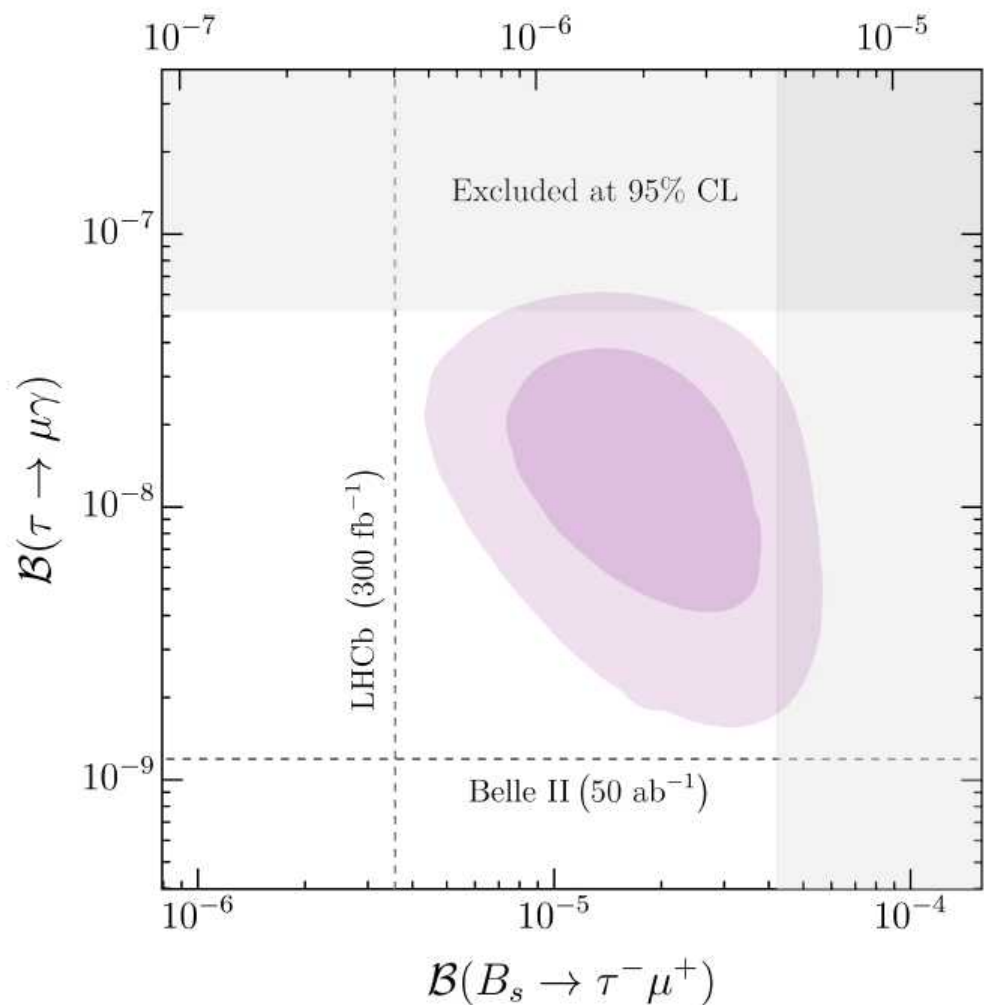


*A lot of fun ahead of us...*

(both on the exp., the pheno,  
and the model-building point of view)



► Other low-energy observables



► Other low-energy observables

Correlations among  $b \rightarrow s(d)ll$  within the U(2)-based EFT

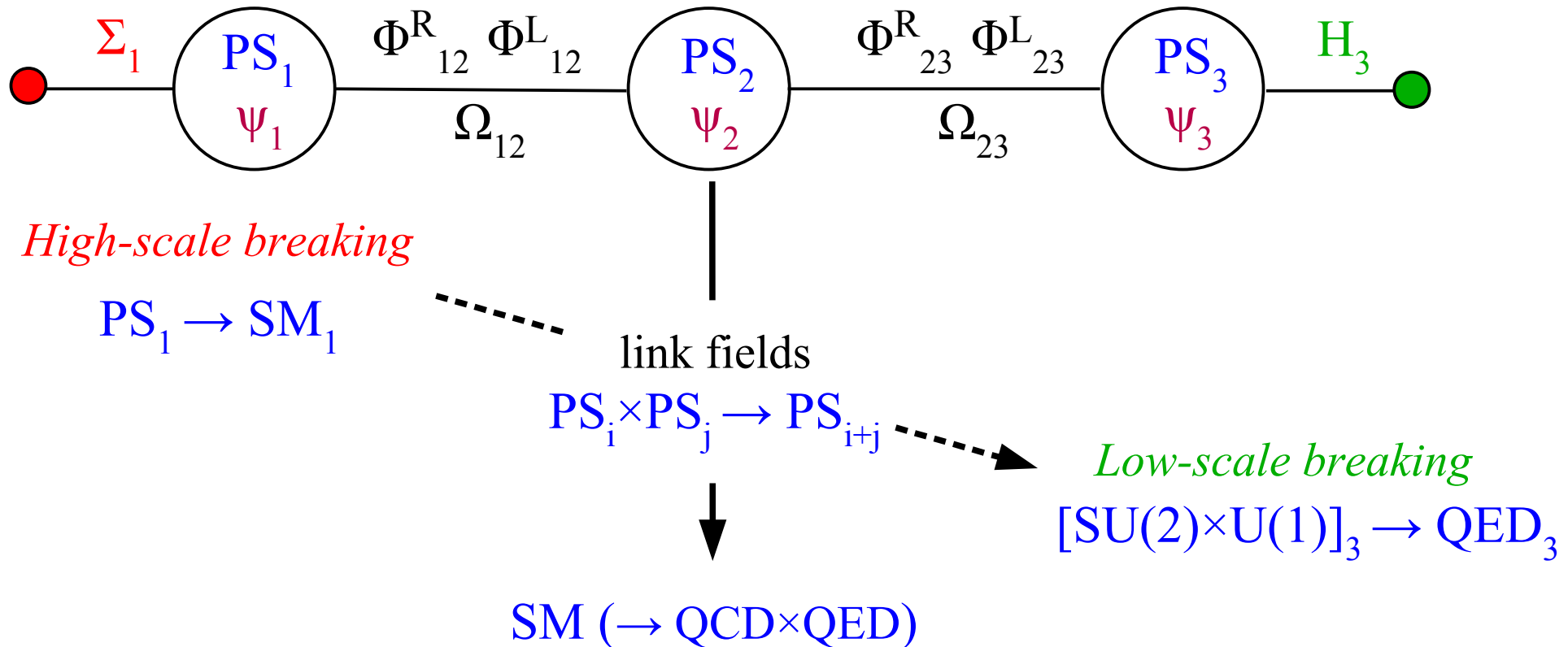
	$\mu\mu$ ( $ee$ )	$\tau\tau$	$\nu\nu$
$b \rightarrow s$	$R_K, R_{K^*}$ $O(20\%)$	$B \rightarrow K^{(*)} \tau\tau$ $\rightarrow 100 \times SM$	$B \rightarrow K^{(*)} \nu\nu$ $O(1)$
$b \rightarrow d$	$B_d \rightarrow \mu\mu$ $B \rightarrow \pi \mu\mu$ $B_s \rightarrow K^{(*)} \mu\mu$ $O(20\%) [R_K = R_\pi]$	$B \rightarrow \pi \tau\tau$ $\rightarrow 100 \times SM$	$B \rightarrow \pi \nu\nu$
$s \rightarrow d$	long-distance pollution	NA	$K \rightarrow \pi \nu\nu$ $O(1)$

$$\frac{A(b \rightarrow d ll)_{SM+NP}}{A(b \rightarrow s ll)_{SM+NP}} = \frac{A(b \rightarrow d ll)_{SM}}{A(b \rightarrow s ll)_{SM}}$$

## ► Speculations on UV completions

The  $PS^3$  set-up:

Bordone, Cornella, Fuentes-Martin, GI, '17

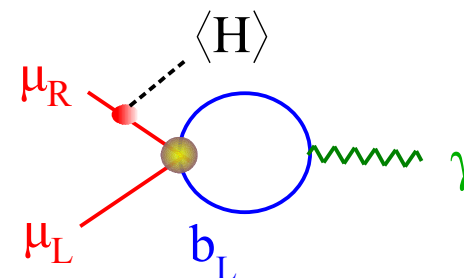


- ★ **Unification** of quarks and leptons [*natural explanation for  $U(1)_Y$  charges*]
- ★ **De-unification** (= *flavor deconstruction*) of the gauge symmetry
- ★ Breaking to the diagonal SM group occurs via appropriate “**link**” fields, responsible also for the **generation of the hierarchies in the Yukawa couplings**.

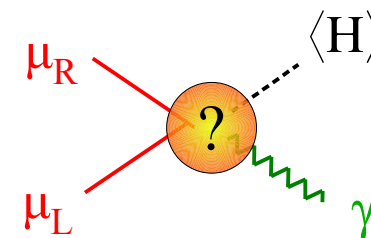
## ► About $g-2$

It is **not easy** to reconcile the  $(g-2)_\mu$  anomaly with both flavor anomalies and, more generally, with models with a “natural” flavor structure ( $\leftrightarrow Y_{SM}$ ).

We do find a non-standard contribution to  $(g-2)_\mu$  in the set up I described, but is very small



Is  $(g-2)_\mu$  suggesting something a different way?



*Maybe....* examples of recent “attempts”:

→  $a_\mu \oplus R_K$  with special role of muons [ $U(1)_{B-3L_\mu} \subset G$ ] Greljo, Stangl, Thomsen '21

→  $a_\mu \oplus R_K \oplus R_D$  with 2 scalars [ $S_1 + \phi^+$ ] and peculiar flavor struct. Marzocca, Trifinopoulos '21

*But...*  $(g-2)_\mu$  is more “flexible” (no generation change, necessary loop-level)  
 → could come from light NP: no obvious connection to the flavor anomalies