Inclusive semileptonic D decays and the heavy quark expansion

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Motivation: CKM Unitarity Analysis

K.Trabelsi (CKMFitter) Beauty 2009

OUTA within the SM

 $\epsilon_K, \Delta m_d, \left| \frac{\Delta m_s}{\Delta m_d} \right|, \left| \frac{V_{ub}}{V_{cb}} \right|$

 relying on theoretical calculations of hadronic matrix elements



Motivation: CKM Unitarity Analysis

T. Browder et al. 0710.3799

OUTA within the SM



- relying on theoretical calculations of hadronic matrix elements
- Projected Super Flavour
 Factory sensitivity
 - V_{ub} (exclusive): 3-5%
 V_{ub} (inclusive): 2-6%



Status of $B \rightarrow X_u$

See talks by R. Kowalewski & T. Mannel

Lange, Neubert and Paz 🛛 👩 [hep-ph/0504071]

Andersen and Gardi [hep-ph/0509360]

Gambino, Giordano, Ossola, Uraltsev [arXiv:0707.2493]

Aglietti, Di Lodovico, Ferrera, Ricciardi [arXiv:0711.0860]

Bauer, Ligeti and Luke [hep-ph/0107074]

0907.5386

- Inclusive determination of Vub using OPE and HQE
 - Expansion in α_s and $1/m_b$ 0
- Present precision around 6-7%
 - however 15% tension with UTA 0
 - dominant source of theoretical 0 uncertainty due to shapefunction modeling (kinematical phase-space cuts)

A fully inclusive analysis would 0 Antonelli et al. carry a tiny 2-3% theoretical error



Status of $B \rightarrow X_u \mid v$

At 1/m_b³ leading spectator effects due to dimension 6 four quark operators (WA contributions)

Bigi & Uraltsev hep-ph/9310285

Dikeman & Uraltsev hep-ph/9703437

Bigi, Dikeman & Uraltsev hep-ph/9706520

Uraltsev hep-ph/9905520

Voloshin hep-ph/0106040

D. Becirevic hep-ph/0110124

D. Becirevic et al. 0804.1750
 16π² phase space enhanced compared to LO & NLO contributions
 Not present at dim=7*
 [Dassinger et al. hep-ph/0611168]

Affect both the total rate and spectra (expected to populate the q² / lepton energy endpoint region)

 \oslash Cannot be extracted from inclusive B->X_c IV analysis

Solution Nor completely from comparing B^+ and B^0 decay modes

Difficult to study non-perturbatively

Existing estimates spread between 3-10%

Inclusive Semileptonic Charm Decays

See talk by K. Ecklund

- $D_q \rightarrow X | v$
- Recently determined experimentally $D(D^+ + V_{ort}) = (16.12 \pm 0.20 \pm 0.00)$
 - $B(D^+ \to X e \nu) = (16.13 \pm 0.20 \pm 0.33)\%$ $B(D^0 \to X e \nu) = (6.46 \pm 0.17 \pm 0.13)\%$
 - Similar results for muons
- \odot Very recently results also for D_s decays

 $B(D_s \to Xe\nu) = (6.52\pm, 0.39\pm 0.15)\%$



Including spectra

N. E. Adam et al. [CLEO] hep-ex/0604044

M. Ablikim et al. [BES] arXiv:0804.1454

Asner et al. [CLEO] 0912.4232

Inclusive Semileptonic Charm Decays

See talk by K. Ecklund

Ratio of D_s and D^o rates shows significant [17(6)%] deviation from unity

 $\Gamma(D^+ \to X e^+ \nu) / \Gamma(D^0 \to X e^+ \nu) = 0.985(28) ,$ $\Gamma(D_s^+ \to X e^+ \nu) / \Gamma(D^0 \to X e^+ \nu) = 0.828(57)$ Asner et al. [CLEO] 0912.4232

Signs of WA in D_s decays?

How to disentangle from possible SU(3) violation?

SU(3) violation in Charm (Two examples) So Hyperfine mass splitting $\Delta_{D_q}^{hf} = 3(m_{D_q^*}^2 - m_{D_q}^2)/4$ $\Delta_{D^+}^{hf} = 0.409(1) \text{GeV}^2$, $\Delta_{D^0}^{hf} = 0.413(1) \text{GeV}^2$, $\Delta_{D_s}^{hf} = 0.440(2) \text{GeV}^2$. \odot SU(3) violation at 10% Decay constants Bazavov et al. In the set of the set [Fermilab & MILC] 0912.5221 \odot SU(3) violation at 20%

Inclusive Semileptonic Charm Decays in OPE

- Treating charm quark mass as heavy, one can attempt an expansion in $\alpha_s(m_c)$, Λ/m_c
 - Need to estimate local operator matrix elements between hadronic states
 - First appear at $1/m_c^2$ <- sources of SU(3) violation
 - Heavy quark symmetry relates these estimates between the charm and beauty sectors

I. I. Bigi & N. G. Uraltsev, Phys. Lett. B 280 (1992) Quantitative translation (renormalization) not straightforward

Gronau & Rosner 🧔 0903.2287

 Alternative approach involves an educated sum over known exclusive modes

OPE and heavy quark expansion

Bigi et al. [hep-ph/9207214] 0

Optical theorem

Manohar and Wise, [hep-ph/9308246] $\Gamma(H_{Q\bar{q}}) = \frac{1}{2m_H} \langle H_{Q\bar{q}} | \mathcal{T} | H_{Q\bar{q}} \rangle$ $\mathcal{T} = \operatorname{Im} i \int d^4x \, T \{ \mathcal{H}_{eff}(x) \mathcal{H}_{eff}(0) \}$

Global) quark-hadron duality, HQE & OPE

equations of motion

$$\bar{c}c = \bar{c}\not\!\!/c + \frac{1}{2m_c^2} \left(\bar{c}(iD_\perp)^2 c + \bar{c}\frac{g_s}{2}\sigma.Gc\right) + \mathcal{O}(1/m_c^3)$$

HQE parameters

$$\mu_{\pi}^{2} = -\frac{1}{2m_{D}} \langle D | \bar{c} (iD_{\perp})^{2} c | D \rangle$$

$$\mu_{G}^{2} = \frac{1}{2m_{D}} \langle D | \bar{c} \frac{g_{s}}{2} \sigma . B c | D \rangle$$

Only applicable for the total rate



OPE and heavy quark expansion

Bigi et al. [hep-ph/9207214]

0

Manohar and Wise, [hep-ph/9308246] Analogously define current correlator whose imaginary part gives the hadronic tensor contributing to inclusive semileptonic spectra

- Again use HQE & OPE
- Requires local quark-hadron duality to hold
 - Can be softened by instead computing spectral moments
 - Any spectral cuts will reintroduce sensitivity to contributions beyond OPE



OPE for the rate & leptonic moments

Rate & leptonic energy moments in HQE & OPE

a x=2E/m_c, r=(m_s/m_c)²

$$\Gamma^{(n)} \equiv \int_{0}^{(1-r)} \frac{d\Gamma}{dx} x^{n} dx = \frac{G_{F}^{2} m_{c}^{5}}{192\pi^{3}} |V_{cs}|^{2} \left[f_{0}^{(n)}(r) + \frac{\alpha_{s}}{\pi} f_{1}^{(n)}(r) + \frac{\alpha_{s}^{2}}{\pi^{2}} f_{2}^{(n)}(r) + \frac{\mu_{\pi}^{2}}{m_{c}^{2}} f_{\pi}^{(n)}(r) + \frac{\mu_{G}^{2}}{m_{c}^{2}} f_{G}^{(n)}(r) + \frac{\rho_{LS}^{3}}{m_{c}^{2}} f_{LS}^{(n)}(r) + \frac{\rho_{D}^{3}}{m_{c}^{2}} f_{D}^{(n)}(r) + \frac{32\pi^{2}}{m_{c}^{2}} B_{WA}^{(n)s} \right] ,$$

A. Pak & A. Czarnecki 🛛 🕢 0803.0960,

K. Melnikov 0803.0951

V. Aquila et al. hep-ph/0503083

Czarnecki & Jezabek hep-ph/9402326

0

Gremm and Kapustin hep-ph/9603448

Dassinger et al. hep-ph/0611168 α_s corrections known up to α_s^2 for the total rate $(\alpha_s^2\beta_0$ for the higher moments)

Cabibbo suppressed modes contribute to the total rate at the level of 5%, but their effect is highly suppressed in the normalized moments

WA in OPE

WA contributions to the rate can be related to matrix elements of dim=6 four quark operators

 $\langle H_{Q\bar{q}}|O_{V-A}^{q'}|H_{Q\bar{q}}\rangle \equiv \langle H_{Q\bar{q}}|\bar{Q}\gamma_{\mu}(1-\gamma_5)q'\bar{q}'\gamma^{\mu}(1-\gamma_5)Q|H_{Q\bar{q}}\rangle$

 $\langle H_{Q\bar{q}}|O_{S-P}^{q'}|H_{Q\bar{q}}\rangle \equiv \langle H_{Q\bar{q}}|\bar{Q}(1-\gamma_5)q'\bar{q}'(1-\gamma_5)Q|H_{Q\bar{q}}\rangle$

- In the SU(3) limit one distinguishes between isosinglet/triplet contributions
 only the later can be estimated from the rate differences of B⁺ and B⁰
- Conventionally one parametrizes deviations from VSA: bag parameters $\langle D|O_{V-A}|D\rangle = f_D^2 m_D^2 B_1$,

$$\langle D|O_{S-P}|D\rangle = f_D^2 m_D^2 B_2$$

P. Gambino et al. hep-ph/0505091, 0707.2493 Renormalization scale dependent, mix with the Darwin contributions at LO $\delta\Gamma \sim \left[C_{WA}B_{WA}(\mu_{WA}) - \left(8\ln\frac{m_c^2}{\mu_{WA}^2} - \frac{77}{6}\right)\frac{\rho_D^3}{m_c^3} + \mathcal{O}(\alpha_s)\right]$

I. I. Bigi et al. 0911.3322 can be used to estimate WA contributions to the rate

Modeling WA in leptonic moments

- WA contributions to the current correlators vanish in the OPE
 need to model
- Bigi & Uraltsev hep-ph/9310285
- Expected to populate the spectrum endpoint

A. K. Leibovich et al. 🛷 hep-ph/0205148]

- Develop a perturbative tail & nonperturbative smearing
- Possible phase-space suppression by hadronic thresholds

Gronau & Rosner 0902.1363 • Can be studied directly using exclusive channels ($D_s \rightarrow \omega \mid v$)



The WA interpretation of rate differences

Bigi et al. 0911.3322 Without resorting to quantitative OPE predictions, one can estimate WA from rate differences

 $\Gamma_{WA}(D^0) \propto \cos^2 \theta_c B^s_{WA}(D^0) + \sin^2 \theta_c B^d_{WA}(D^0),$ $\Gamma_{WA}(D^+) \propto \cos^2 \theta_c B^s_{WA}(D^+) + \sin^2 \theta_c B^d_{WA}(D^+),$ $\Gamma_{WA}(D_s) \propto \cos^2 \theta_c B^s_{WA}(D_s) + \sin^2 \theta_c B^d_{WA}(D_s),$

by equating the difference between D_s and D^o rates with the isotriplet component of WA

assumes SU(3) violating effects are sub-leading

isosinglet component unconstrained

Confronting OPE convergence in charm

Ligeti et al. 1003.1351

0

J.F.K. 0909.2755

Gambino & J.F.K 1004.0114 In order to constrain WA fully, need to explicitly compute semileptonic rates and/or distribution moments – compare with exp.

Perturbative corrections known in the pole scheme

$$\begin{split} \Gamma &= \Gamma_0 \left[1 - 0.72 \,\alpha_s - 0.29 \,\alpha_s^2 \beta_0 - 0.60 \,\mu_G^2 - 0.20 \,\mu_\pi^2 + 0.42 \,\rho_D^3 + 0.38 \,\rho_{LS} + 80 B_{WA}^{(0)} \right] \,, \\ < E > &= < E >_0 \left[1 - 0.03 \,\alpha_s - 0.03 \,\alpha_s^2 \beta_0 - 0.07 \,\mu_G^2 + 0.20 \,\mu_\pi^2 + 1.4 \,\rho_D^3 + 0.29 \,\rho_{LS} + 135 \bar{B}_{WA}^{(1)} \right] \,, \\ < E^2 > &= < E^2 >_0 \left[1 - 0.07 \,\alpha_s - 0.05 \,\alpha_s^2 \beta_0 - 0.14 \,\mu_G^2 + 0.52 \,\mu_\pi^2 + 3.5 \,\rho_D^3 + 0.66 \,\rho_{LS} + 204 \bar{B}_{WA}^{(2)} \right] \,, \\ \sigma_E^2 &= (\sigma_E^2)_0 \left[1 - 0.09 \,\alpha_s - 0.05 \,\alpha_s^2 \beta_0 - 0.14 \,\mu_G^2 + 1.7 \,\mu_\pi^2 + 9.4 \,\rho_D^3 + 1.4 \,\rho_{LS} + 641 \bar{B}_{WA}^{(\sigma)} \right] \,, \end{split}$$

c.f. Antonelli et al. 0907.5386 Renormalon (Λ/m_c) ambiguity of pole mass

all moments affected (n-th scales as m_c^n)

Better to use a short distance – threshold mass definition

Convergence of perturbative corrections

Ligeti et al. 1003.1351

Marginal in the pole scheme (α_s(m_c)≈0.35) 0 $\frac{1}{\Gamma_0[m_c^{\text{pole}}]} = 1 - 0.269 \epsilon - 0.360 \epsilon_{\text{BLM}}^2 + 0.069 \epsilon^2 + \dots,$ Improves in short distance m_c schemes $\frac{1}{\Gamma_0[m_c^{1S}]} = 1 - 0.133 \epsilon - 0.006 \epsilon_{\rm BLM}^2 - 0.017 \epsilon^2.$ One can try to soften the strong dependence on the charm quark mass using information from inclusive B decays $\frac{\Gamma}{\Gamma_0[m_b^{1S} - \Delta]} = 1 - 0.075\epsilon - 0.013\epsilon_{\rm BLM}^2 - 0.021\epsilon^2,$ $(\Delta = m_b - m_c)$

Convergence of perturbative corrections

Gambino & J.F.K 1004.0114

HFAG

In schemes with explicit IR cut-off, one needs to choose 0 proper (low) IR scale (0.5-0.8 GeV)

Need to translate OPE parameters as well (from global B fits) winter '09 update Perturbative and OPE corrections translated to kinetic scheme 0

 $\Gamma_{kin} = 1.2(3)10^{-13} \text{GeV} \left\{ 1 + 0.23 \,\alpha_s + 0.18 \,\alpha_s^2 \beta_0 - 0.79 \,\mu_G^2 - 0.26 \mu_\pi^2 + 1.45 \,\rho_D^3 + 0.56 \rho_{LS}^3 + 120 B_{WA}^{(0)} \right\}$ $< E_{\ell} >_{kin} = 0.415(21) \text{GeV} \left\{ 1 + 0.03 \,\alpha_s + 0.02 \,\alpha_s^2 \beta_0 - 0.09 \,\mu_G^2 + 0.26 \mu_\pi^2 + 2.7 \rho_D^3 + 0.44 \rho_{LS}^3 + 203 \bar{B}_{WA}^{(1)} \right\} \,,$ $< E_{\ell}^2 >_{kin} = 0.192(20) \text{GeV}^2 \left\{ 1 + 0.001 \,\alpha_s + 0.02 \,\alpha_s^2 \beta_0 - 0.18 \,\mu_G^2 + 0.68 \mu_{\pi}^2 + 6.6 \rho_D^3 + 0.99 \rho_{LS}^3 + 307 \bar{B}_{WA}^{(2)} \right\}$ $\sigma_{E,kin}^2 = 0.019(2) \text{GeV}^2 \left\{ 1 - 0.53 \,\alpha_s - 0.17 \,\alpha_s^2 \beta_0 - 0.18 \mu_G^2 + 2.2 \mu_\pi^2 + 17 \rho_D^3 + 2.1 \rho_{LS}^3 + 961 \bar{B}_{WA}^{(\sigma)} \right\} \,,$

- \odot Rate uncertainty dominated by $m_c \& \mu_G$
- \odot Higher leptonic moments by ρ_D

Extraction of WA contributions

Ligeti et al. 1003.1351

- Comparing theoretical expressions with experimental rates (in 1S scheme)
 - using OPE parameters and masses as extracted from global B decay fits
 - neglecting possible SU(3) violations
 - Indication of a non-zero isosinglet WA contribution

 $a_0 = 1.25 \pm 0.15$, $a_8 = -0.20 \pm 0.12$,



$$a_{0,8} = \frac{m_c^2 m_D f_D^2}{m_c^5} \, 16\pi^2 \left(B_2^{s,ns} - B_1^{s,ns} \right)$$

Translates into O(1−2%) effect in B->X_u l v rate

Extraction of WA contributions

Gambino & J.F.K 1004.0114 Including information on the leptonic energy moments

- Different dependence of moments on the OPE parameters allows to possibly disentangle SU(3) violating effects from WA contributions
- Introduces dependence due to the modeling of the WA shape in the spectra
- Correlated WA determination from the rate and the moments



Extraction of WA contributions

Gambino & J.F.K 1004.0114 Including information on the leptonic energy moments

- Different dependence of moments on the OPE parameters allows to possibly disentangle SU(3) violating effects from WA contributions
- Introduces dependence due to the modeling of the WA shape in the spectra
- Correlated WA determination from the rate and the moments
 - Allowing for O(20%) SU(3) violation in OPE parameters
 - Largest uncertainty due to ρ_D linear (scale dependent)
 combination of ρ_D and WA contributions determined precisely
 - For µ_{WA}≈1GeV no clear indication of non-zero WA contributions

 $B_{WA}^s = -0.0003(25) \text{GeV}^3$

Translates into O(2%) uncertainty in $B \rightarrow X_u \mid v$ decay rate

Conclusions

- Inclusive semileptonic charm decays can be used as a laboratory to test the OPE techniques used in the extraction of |V_{ub}| and |V_{cb}| from inclusive B decays
 - ø perturbative convergence seems to be surprisingly good
- Use several observables to over-constrain the OPE parameter uncertainties and test OPE convergence
- Indications that WA related uncertainties in inclusive |V_{ub}| extraction smaller than previously expected [O(1%)]
- More tests possible in the future with additional experimental inputs (experimentally determined leptonic energy and hadronic invariant mass moments) from Cleo and BESIII

Backup Slides

Status of $B \rightarrow X_u \mid v$

See talks by R. Kowalewski & T. Mannel

- Experimental cuts on the leptonic energy and hadronic invariant mass to suppress dominant charm final state contributions
 - Multivariate
 Introduce theoretical sensitivity to effects
 - beyond the OPE
 - Modeled by s.c. shapefunctions
- Antonelli et al. 6 0907.5386
- A fully inclusive analysis we carry a tiny 2-3% theoretic error



Events

Playing the experimentalist

One would want to compare completely inclusive leptonic energy moments in the rest-frame of the decaying hadron

This is not what Cleo presently provide:

ø do not compute the leptonic energy moments

- spectra given in the lab frame
- \odot involve a lower E_e=0.2 GeV cut
- o do subtract the $D_s \rightarrow \tau v$ leptonic background



Asner et al. [CLEO] 0912.4232

See talk by K. Ecklund

Playing the experimentalist

One would want to compare completely inclusive leptonic energy moments in the rest-frame of the decaying hadron

Gambino & J.F.K
We try to compensate: 1004.0114

- \circ extrapolate the spectra down to $E_e=0$ using inclusive model shapes
- compute the leptonic energy moments from extrapolated spectra (in the lab frame)
- boost the moments to the D frame by directional averaging $< E'_e > = \gamma < E_e > | < {E'_e}^2 > = \gamma^2 (1 + \beta^2/3) < E_e^2 >$
 - D's produced in pairs at E_{CM}=3774MeV
 - \circ D_s's produced associated with D_s*'s and through their decays