

# Inspiral, merge, repeat: hierarchical black-hole mergers and their gravitational-wave signatures

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European Research Council



# Outline

1. How do two black holes get together?
2. Gravitational-wave observables
3. Repeated black-hole mergers for LIGO and Virgo

All in a new Nature Astronomy review: **DG** Fishbach 2021 ([arXiv:2105.03439](https://arxiv.org/abs/2105.03439))



# Can BHs really make it?

At lowest order, GW emission causes the orbit to shrink:

Peters and Mathews 1963

$$\text{separation} \quad \frac{da}{dt} = -\frac{64 G^3 M^3}{5 c^5 a^3} \frac{q}{(1+q)^2} (1-e^2)^{-7/2} \left( 1 + \frac{73}{24} e^2 + \frac{37}{96} e^4 \right)$$

$$\text{eccentricity} \quad \frac{de}{dt} = -\frac{304}{15} e \frac{G^3 M^3}{c^5 a^4} \frac{q}{(1+q)^2} (1-e^2)^{-5/2} \left( 1 + \frac{121}{304} e^2 \right)$$

## Inspiral timescale

$$t_{\text{GW}} \sim a \frac{dt}{da} \sim a^4$$

**Gravitational waves** are efficient below

$$a_{\text{GW}} = 1.2 \times 10^{11} \left( \frac{t_{\text{GW}}}{1.4 \times 10^{10} \text{yr}} \right)^{1/4} \left( \frac{M}{M_{\odot}} \right)^{3/4} \text{cm}$$

$$\sim 10 R_{\odot} \text{ for stellar-mass BHs}$$

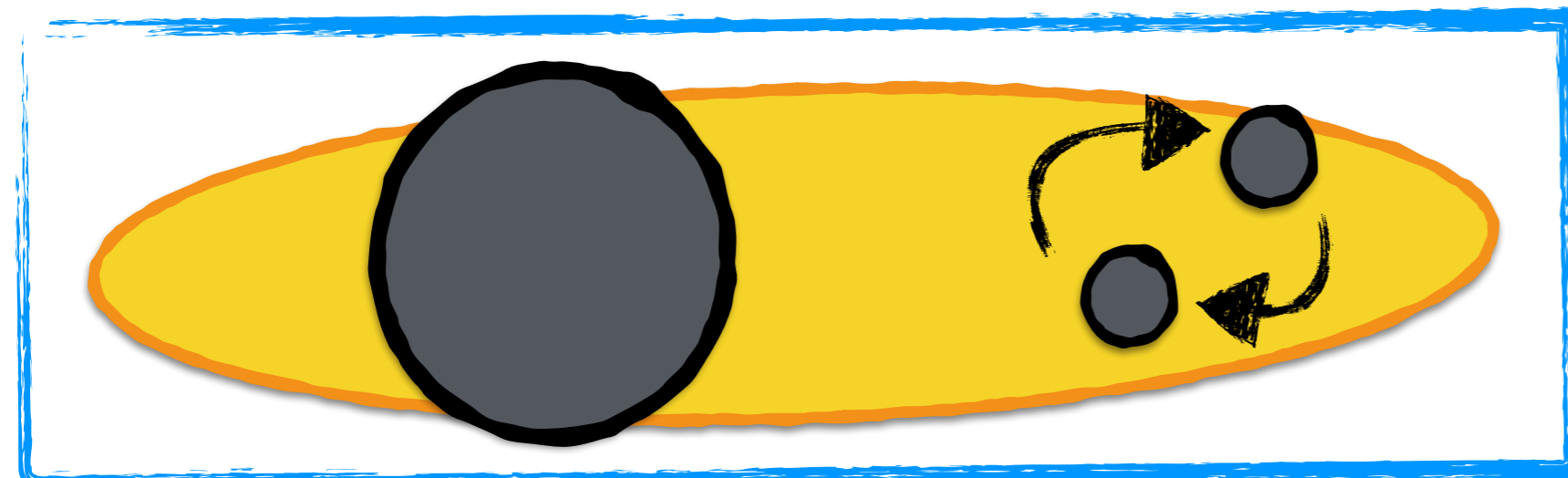
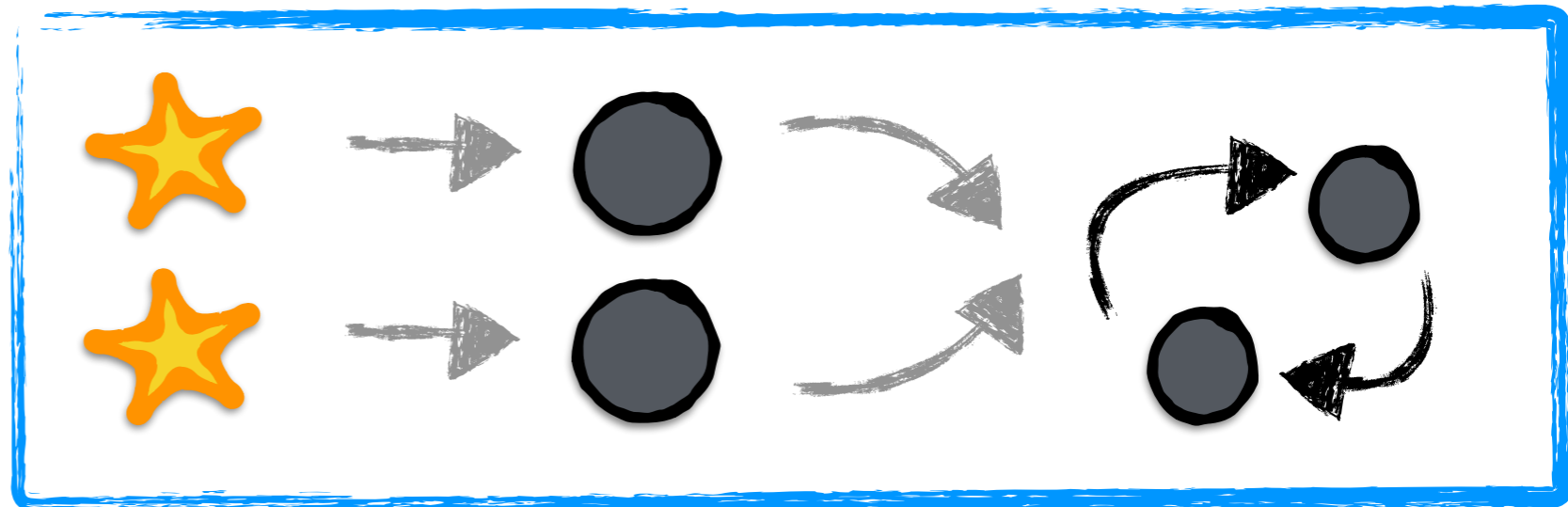
**Relativity** alone is great to model the LIGO signals...  
...but some **astrophysics** is needed to explain them

# Have we been together for so long?



Yes! I've known you since you were a star

Nah, we just met in cluster

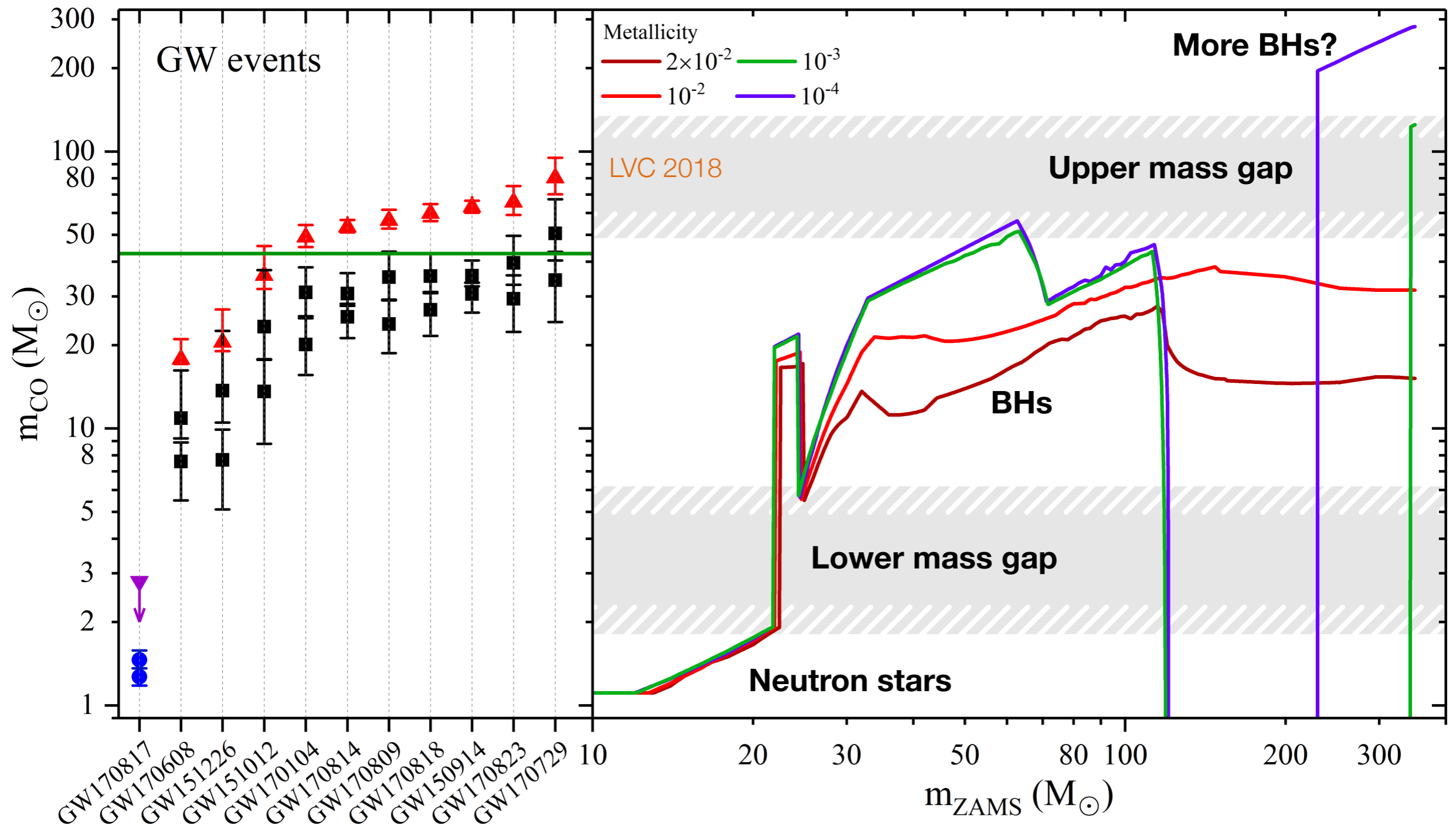


Our neighbour is so messy, we should move



# Mass predictions: the gaps

- **Lower mass gap:** between BHs and NSs
- **Upper mass gap:** supernova instabilities



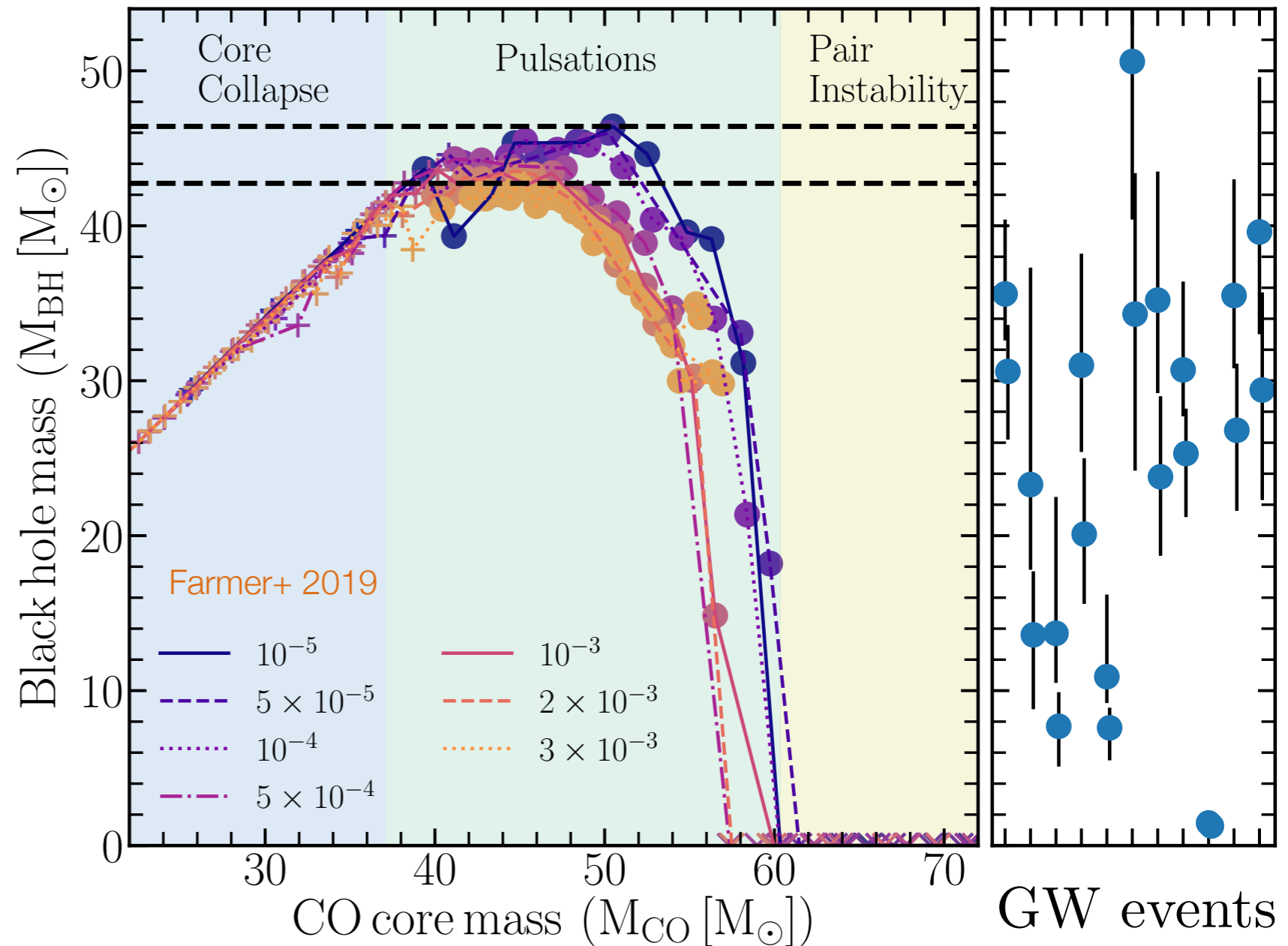
# Pair-instability supernovae

As the mass of the core increases:

1. Electron-positron production
2. Radiation pressure drops
3. Core contracts
4. Temperature goes up
5. Explosive oxygen burning
6. Entire star is gone (PISN)
7. Repeated pulsations (PPISN)

Heger Woosley 2002, Belczynski+ 2016,  
Woosley+ 2017, Spera Mapelli 2017,  
Marchant+ 2018, Stevenson+ 2019

BH forbidden for  
 $M \gtrsim 50M_{\odot}$



This limit is very solid...

Farmer+ 2019, Renzo+ 2020

...maybe

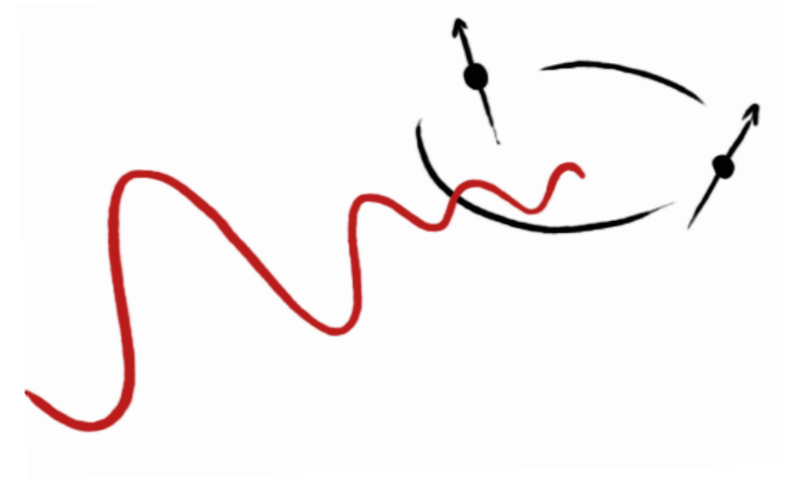
Belczynski+ 2019, 2020,  
Farmer+ 2020, Costa+ 2021

**Can we bypass stars and  
use black holes?**

# Spin predictions

Extremely sensitive to details

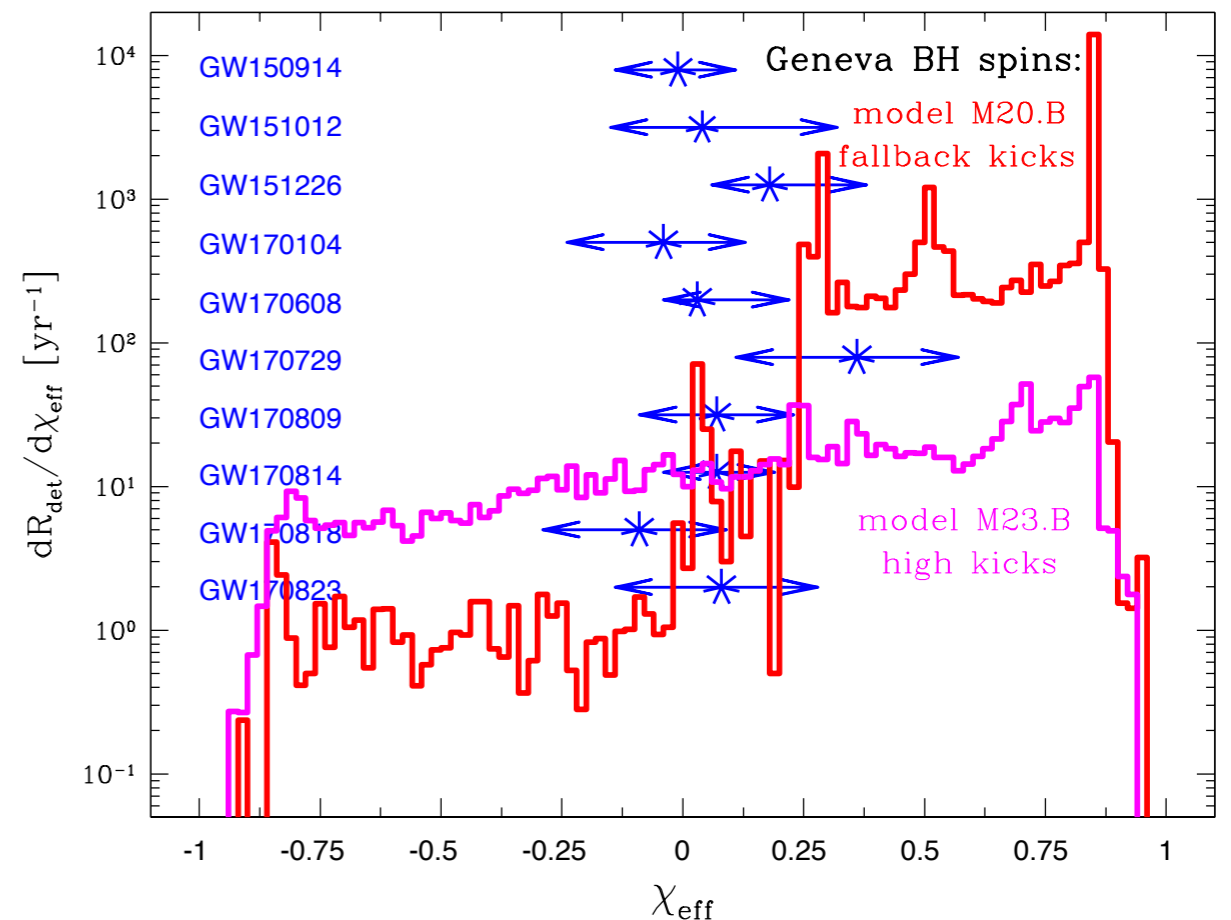
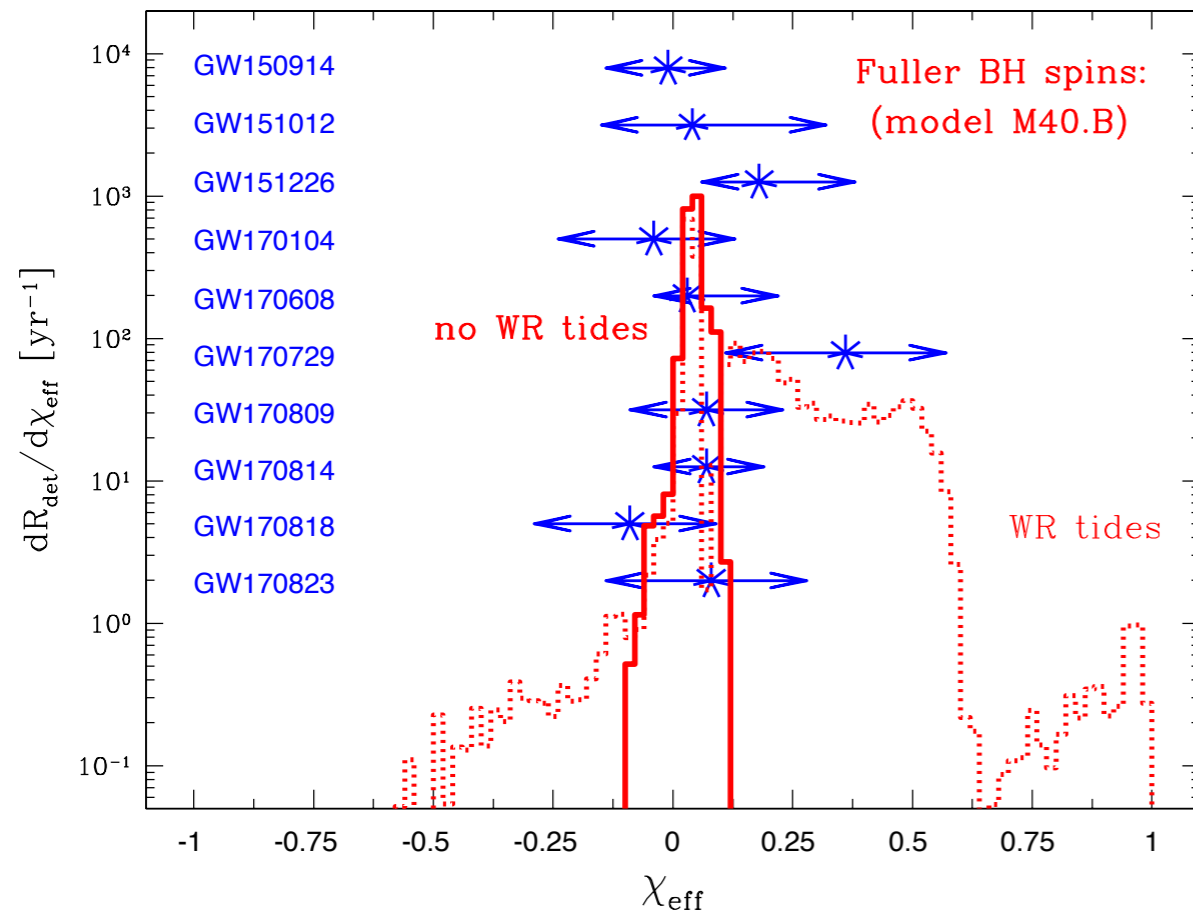
- Core-envelope interactions in massive stars [Fuller Ma 2019](#)
- Tidal realignment in the Wolf-Rayet phase [Zaldarriaga+ 2017](#)
- Supernova kicks [Kalogera 2000](#)
- Mass transfer [Stegmann+ 2020](#)
- Relativistic precession till merger [DG+ 2013, 2018](#)



$$\chi_{\text{eff}} = \left( \frac{\mathbf{S}_1/m_1 + \mathbf{S}_2/m_2}{m_1 + m_2} \right) \cdot \hat{\mathbf{L}}$$

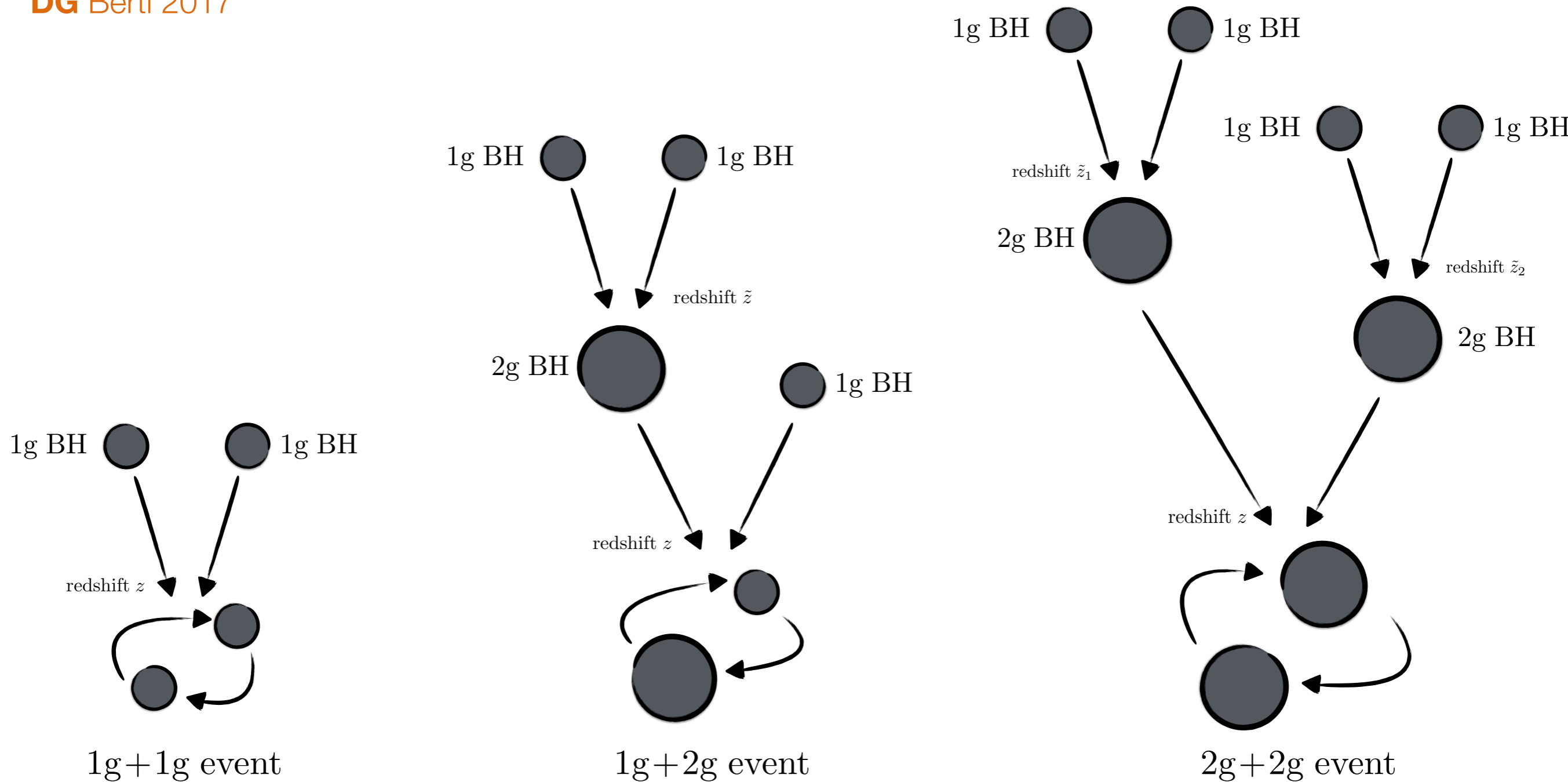
Sets the length of the waveform

[Belczynski, DG+ 2020](#)



# Black hole generations

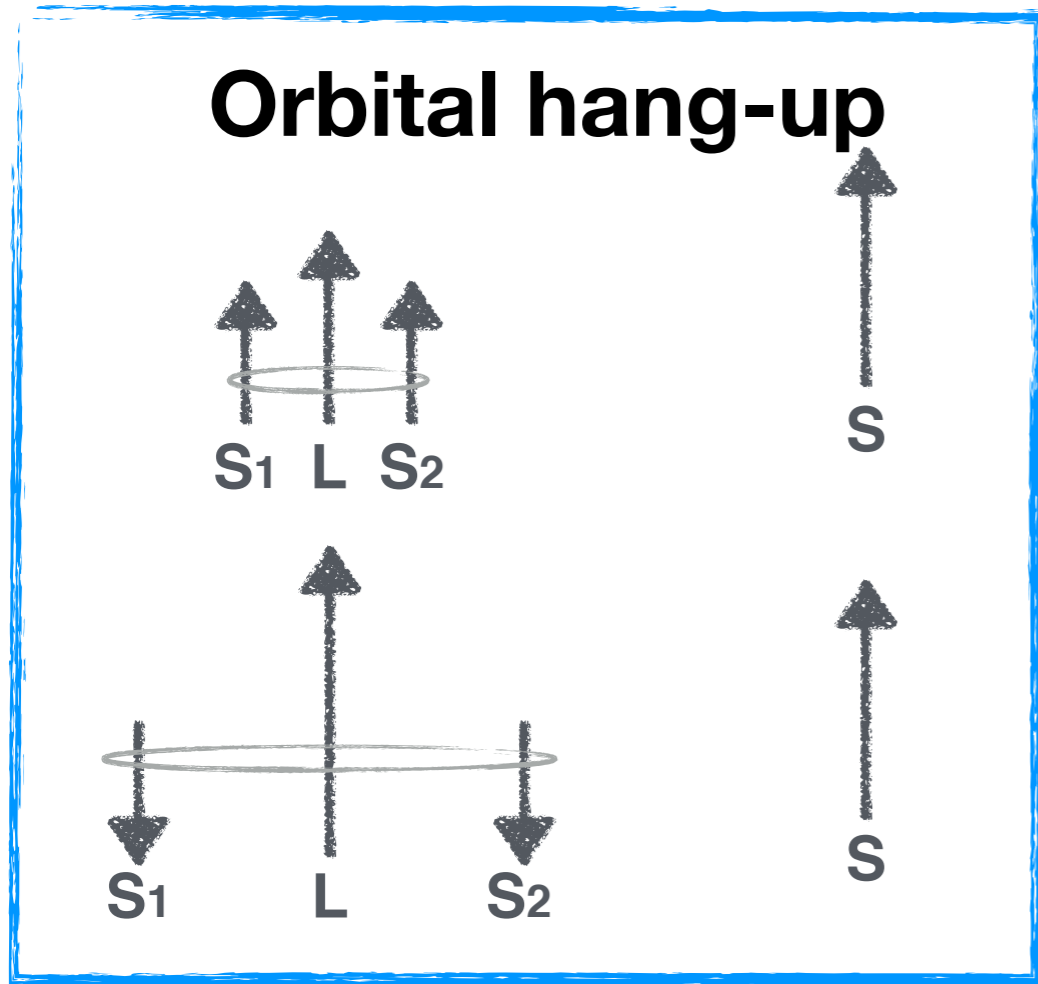
DG Berti 2017



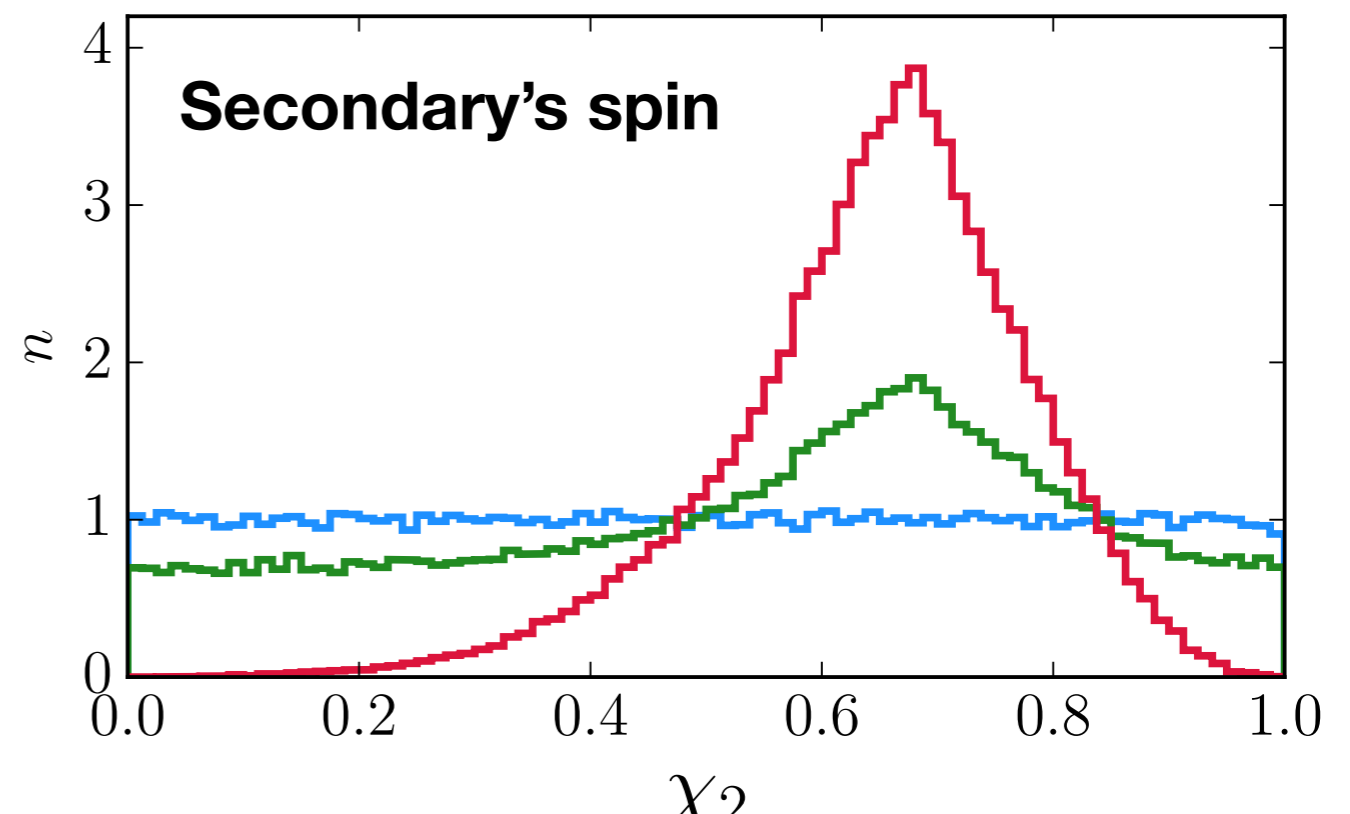
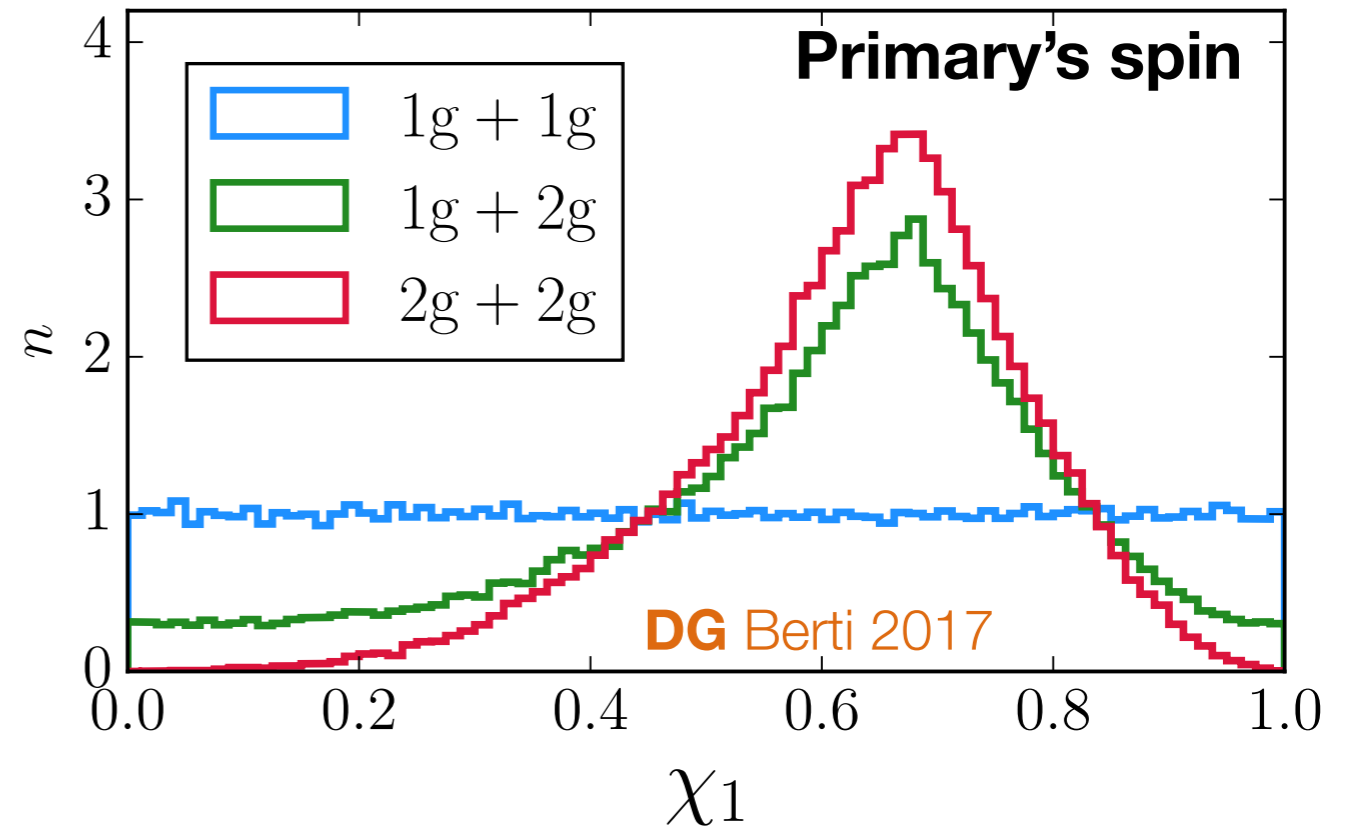
**Orthogonal**, but complementary, direction to the usual field vs. cluster debate

# Spins: the magic number

DG Berti 2017, Fishbach+ 2017, Berti Volonteri 2008

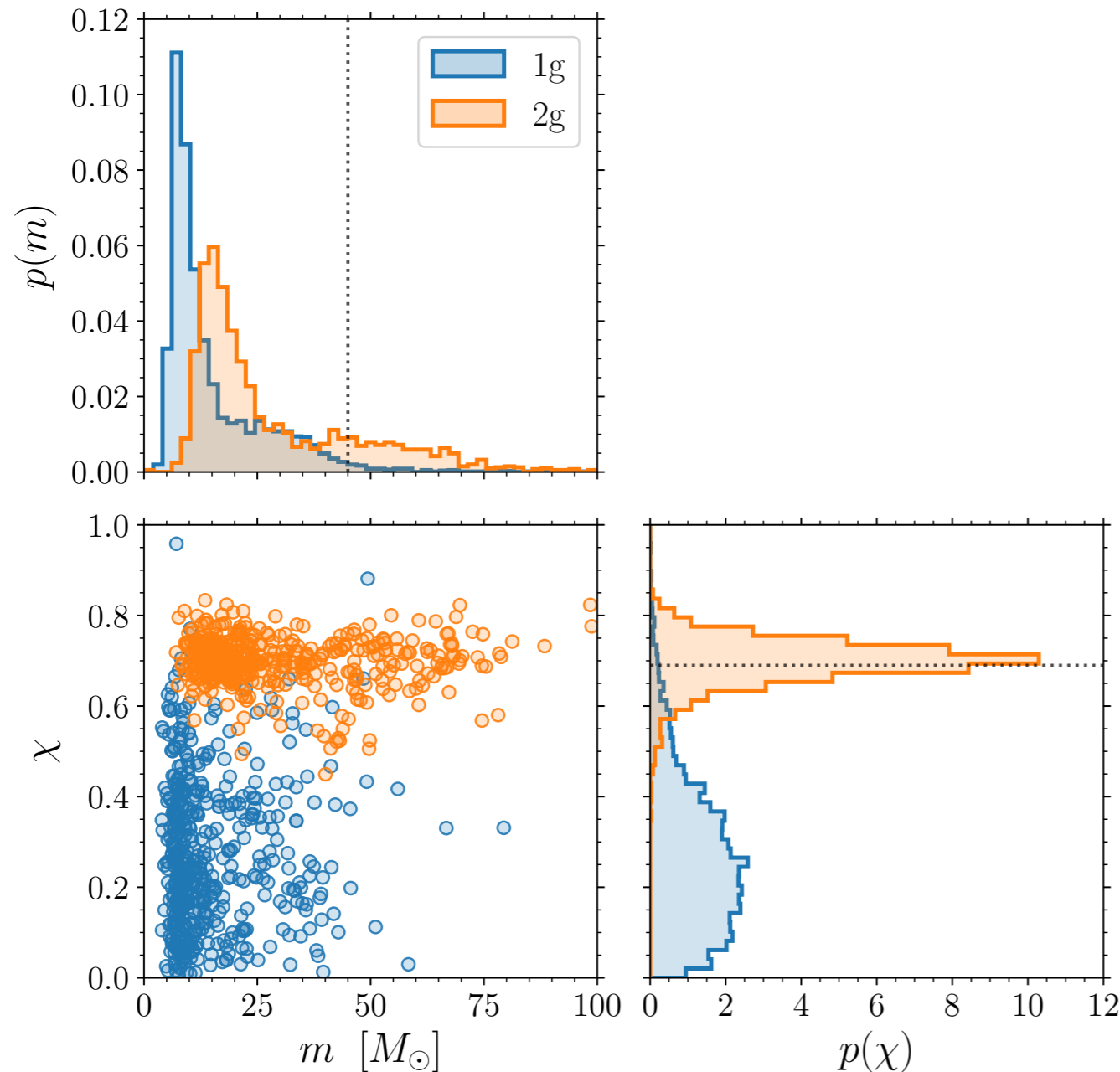


Peculiar spin distribution peaked at **0.7**





# An explosion of new predictions

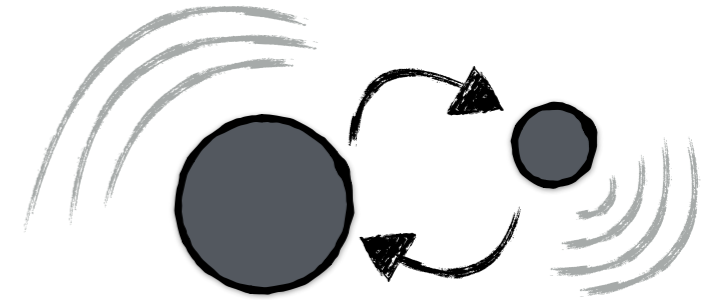


- Masses in the pair-instability mass gap  
Heger+ 2003, Woosley+ 2007
- Peculiar spin distribution peaked at 0.7  
**DG** Berti 2017, Fishbach+ 2017
- But GW kicks impose large escape speed  
**DG** Berti 2019
- Very frequent in AGNs  
Yang+ 2019, Tagawa+ 2020
- Promising for GW190412  
**DG** Vitale Berti 2020
- Leading explanation for GW190521  
LIGO/Virgo 2020
- Perhaps a several events in the new LIGO catalog?  
Kimball+ 2020
- Inferring the properties of the parents  
Baibhav, **DG**+ 2021
- A model that can be ruled out!  
**DG** Giacobbo Vecchio 2021
- Parametric inference with deep learning  
Mould, **DG**+ (soon!)

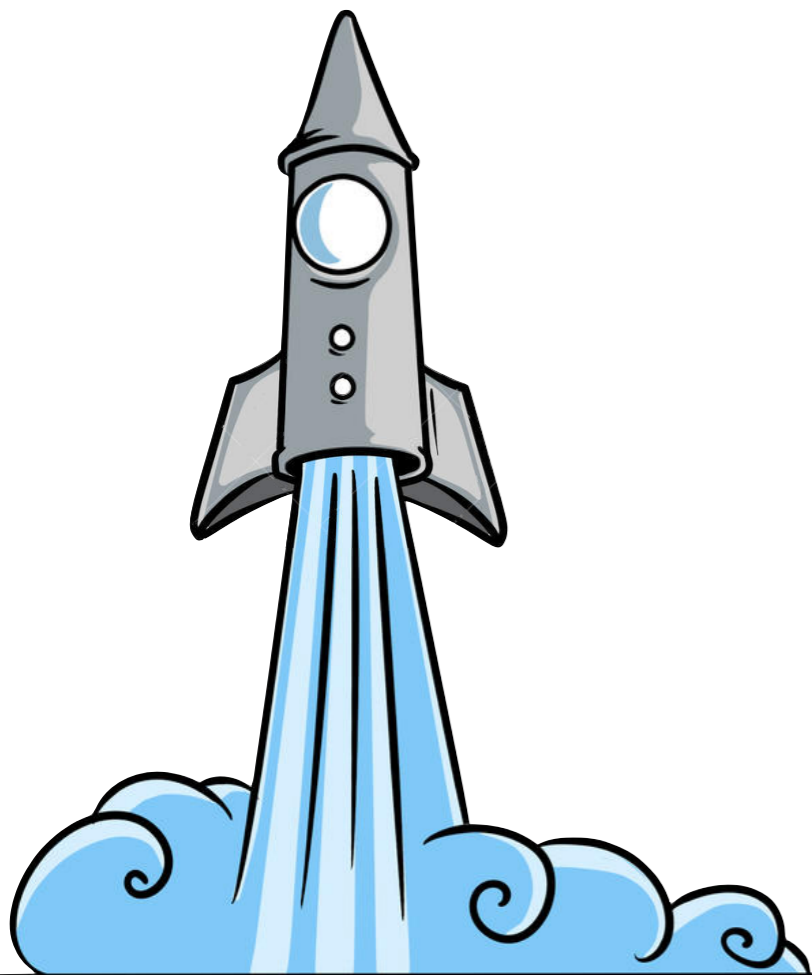
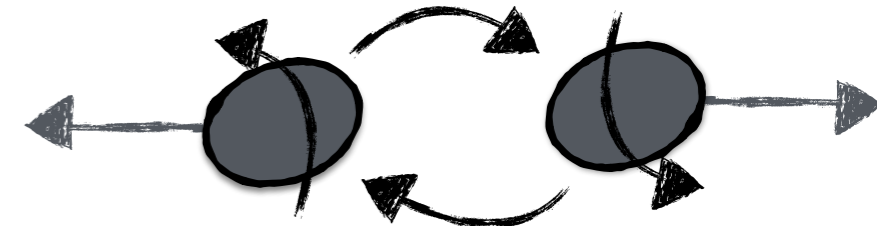
**New review** **DG** Fishbach 2021

# More spin means more kick

- **Non spinning BHs:** up to  $\sim 160$  Km/s  
Gonzales+ 2007



- **Misaligned spins:**  
“Superkick” up to  $\sim 5000$  Km/s  
Gonzales+ 2007; Campanelli+ 2007, Lousto Zlochower 2011,2013  
Enhanced by  $\sim 25\%$  for eccentric binaries  
Sopuerta+ 2007, Sperhake, **DG**+ 2020

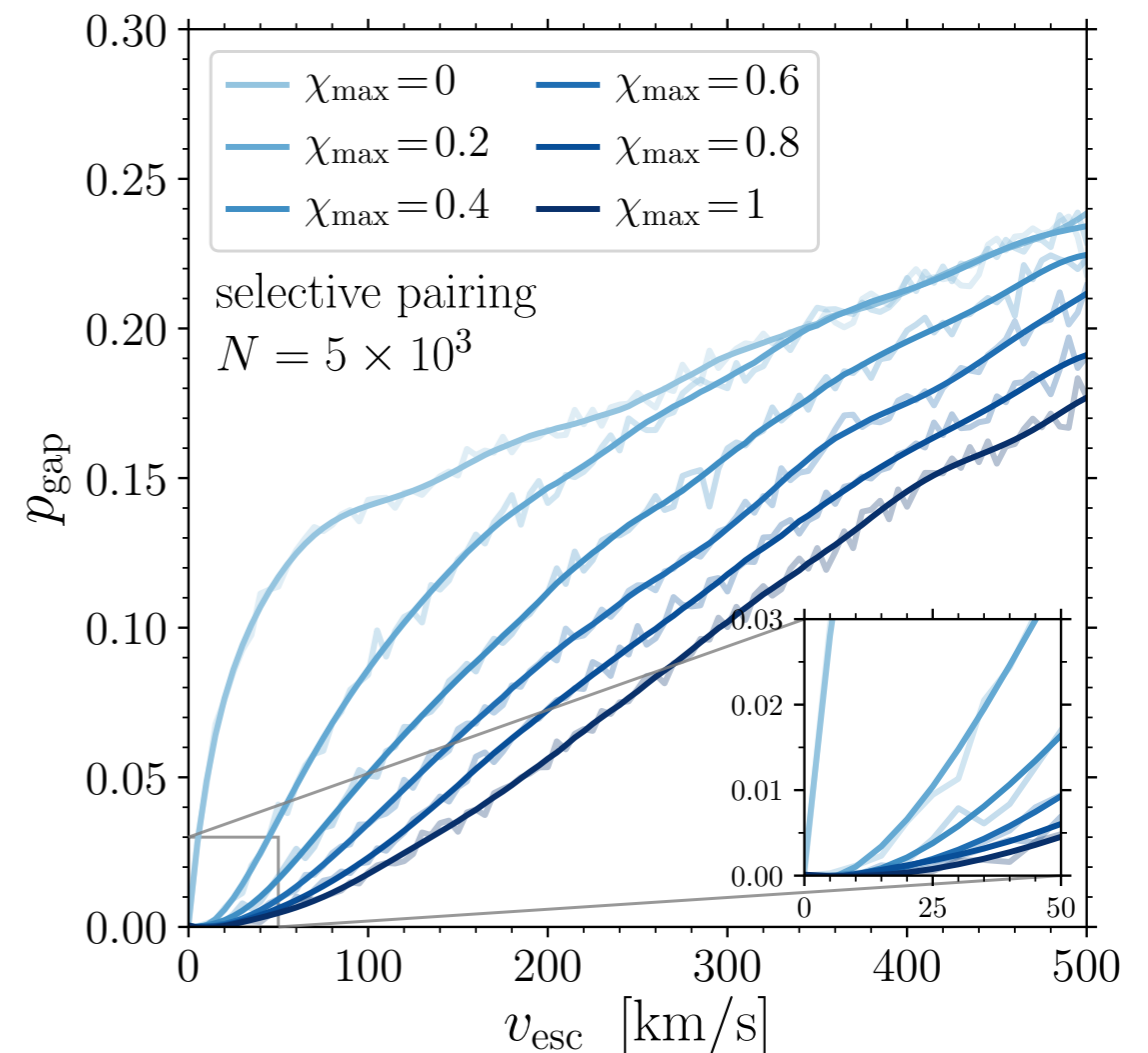
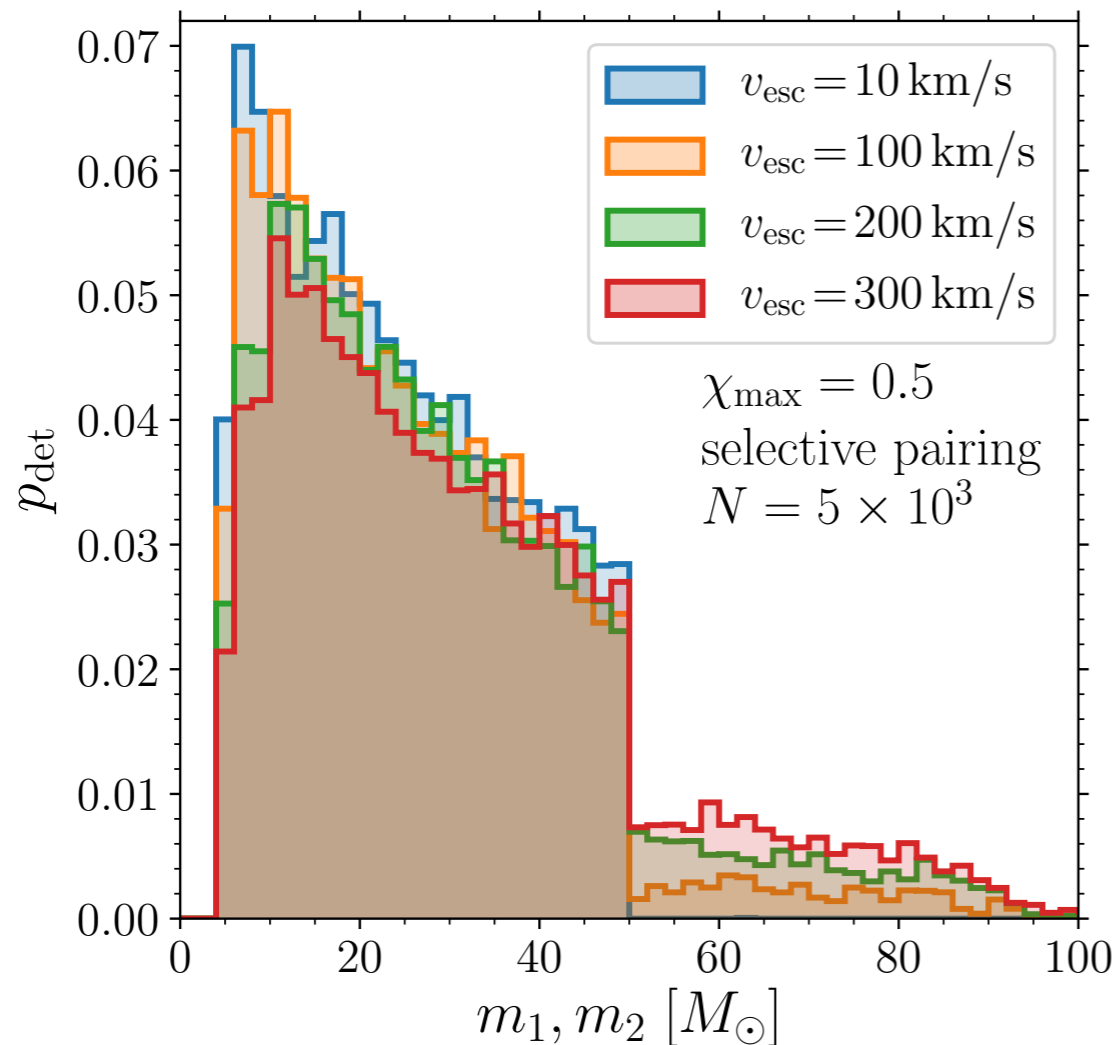


**Large spins have a critical impact on the kick: can black holes really merge again?**

# The role of the escape speed

An escape speed of  $\sim 50$  km/s is necessary to populate the mass gap

DG Berti 2019

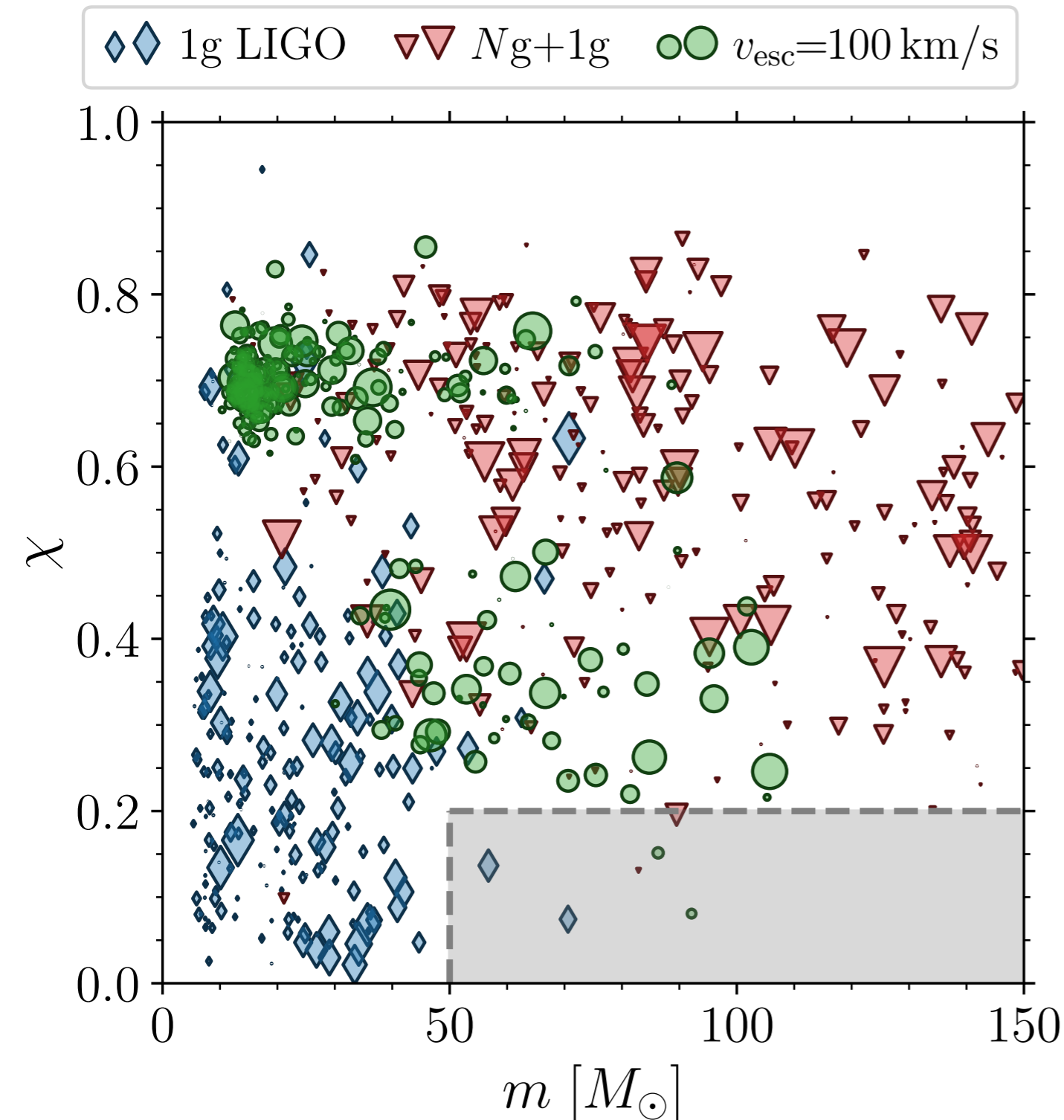


**$\sim 50$  km/s is more than most globular clusters.**

- Nuclear star cluster [Antonini+ 2016](#)
- Triples [Antonini+ 2017](#), [Bin+ 2019](#)
- Disc-assisted migration  
[Stone+ 2017](#), [Bartos+ 2017](#)

# High mass but low spin?

DG, Giacobbo, Vecchio 2021



## Hierarchical mergers cannot do it

(even if you try hard)

If a future event is there...  
we need something else!

- Lowered CO reaction rate  
e.g. Farmer+ 2020, Costa+ 2021
- Weaker stellar winds  
e.g. Leung+ 2019, Belczynski+ 2020
- Rotation  
e.g. Marchant Moriya 2020, Woosley Heger 2021
- Stellar collisions  
e.g. Di Carlo+ 2019, Renzo+ 2020
- Accretion  
e.g. van Son et al. 2020, Natarajan 2021
- Pop III stars  
e.g. Farrell et al. 2020, Kinugawa et al. 2021

# The gaps are precious

Baibhav, **DG+** 2020

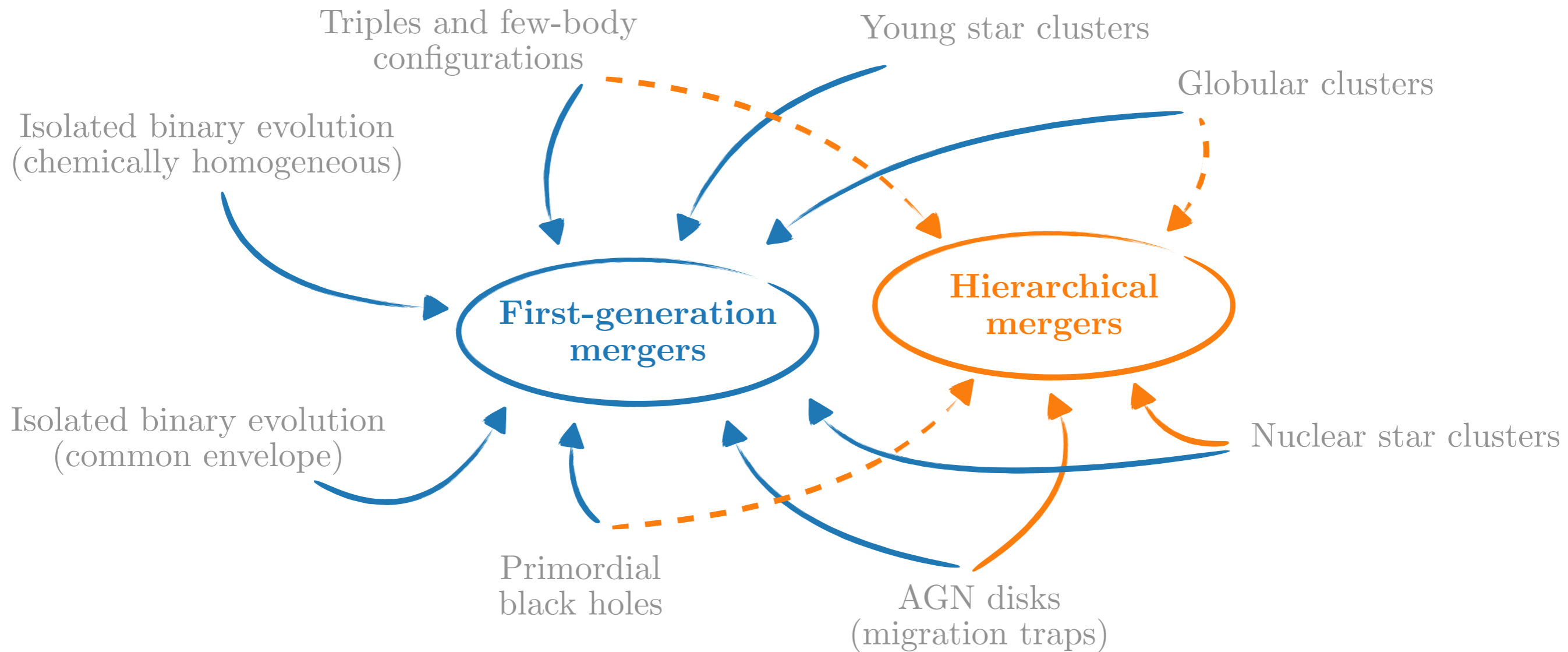
- Two channels “field” and “cluster”:  $N = N_{\text{field}} + N_{\text{cluster}}$
- Some are in the gap:  $N = N_{\text{no gap}} + N_{\text{gap}}$
- The gap is exclusive:  $N_{\text{field,gap}} = 0$        $N_{\text{cluster,gap}} = N_{\text{gap}}$
- A predicted efficiency:  $\lambda \equiv \frac{N_{\text{cluster,gap}}}{N_{\text{cluster}}}$
- Individual contributions:

$$N_{\text{cluster}} = \frac{N_{\text{gap}}}{\lambda} \qquad N_{\text{field}} = N - \frac{N_{\text{gap}}}{\lambda}$$



# Where do hierarchical BH mergers come from?

DG Fishbach (2021)



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