End benches scattered light modelling & substraction in Advanced Virgo

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LAPP/IN2P3 - Annecy









Outline

- Scattered light coupling model 4 different paths
- Using scattered light to measure intereferometer optical parameters
- Subtraction of scattered light noise from O3 Advanced Virgo h(t) data
- Checking h(t) calibration accuracy with scattered light



Advanced Virgo optical layout - end benches



Scattered light from suspended end benches



- Receiving beam transmitted by end mirrors
- 7 m behind end mirrors, suspended in separate vacuum chamber
- Tracking mirror position by pushing on the bench suspension point
- ⇒ No scattered light noise above 10 Hz in normal conditions

Scattered light noise coupling fully reconstructed



Scatter phase

$$\phi_{
m sc} = 4\pi rac{x_{
m SWEB} - x_{
m WE}}{\lambda}$$

• Photodiode on bench sees amplitude modulation: $\cos \phi_{\rm sc}$

$$P_{\rm B8} = \alpha T_{\rm WE} |E_0|^2 \left(1 + 2\sqrt{f_{\rm SC}} \cos \phi_{\rm SC}\right),$$

• Other quadrature of scatter phase can be reconstructed

$$\cos \phi_{\rm sc}(t) = \int_{-\infty}^{\infty} \hat{\phi}_{\rm sc}(\omega) e^{i\omega t} d\omega$$
$$\sin \phi_{\rm sc}(t) = i \operatorname{sign} \left[\frac{d\phi_{\rm sc}(t)}{dt} \right] \int_{0}^{\infty} \left[\hat{\phi}_{\rm sc}(-\omega) e^{-i\omega t} - \hat{\phi}_{\rm sc}(\omega) e^{i\omega t} \right] d\omega.$$

• Only requires adding direction of motion information from position sensors

Scattered light measured with large SNR



- Intentional 24 um bench motion at 0.1 Hz, single 3 minutes measurement
- Photodiode sensing noise >3 orders of magnitude below scattered light signal
- Dominated by light scattered by quadrant photodiode
- Shelf of scattered light from single and two round-trips can be seen

4 different coupling paths



- Derived analytically and confirmed with Optickle simulation
- Modulating phase of light in arms: $\sin \phi_{sc}(t)$
- Modulating amplitude of light in arms: $\cos \phi_{sc}(t)$
 - Coupled due to radiation pressure
 - Coupled due to contrast defect
 - Recycled in PR cavity and coupled due to radiation pressure

Powerful interferometer characterization tool



- Intentional 24 um bench motion at 0.1 Hz, single 3 minutes measurement
- Fitting parameters can remove scattered light by up to factor 40
- Measure precisely several interferometer parameters

		arm power	contrast	power
	T_{WE}	$ E_0 ^2$	defect	asymmetry
	(ppm)	(kW)	(μW)	(%)
SWEB injection	4.34 ± 0.04	92.1 ± 0.7	95 ± 8	1.41 ± 0.06
expected	4.3 ± 0.1	90 ± 5	120 ± 20	~ 1

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Subtracting scattered light noise from O3 data



- SWEB suspension under-performing during O3
- In bad weather scattered light arches up to 50 Hz visible in h(t)
- Online subtraction was able to remove radiation pressure coupling path
 - Using linear coupling of P_{B8} auxiliary channel, removes cos φ_{sc}(t) component
- Adding reconstruction of $\sin \phi_{sc}(t)$ allows to further reduce scattered light noise

A check of calibration accuracy



• Transmission of end mirrors measured after coating with 2% precision

$$h_{\rm sc, \, phase} = \frac{1}{L} T_{\rm WE} \sqrt{f_{\rm sc}} \frac{\lambda}{4\pi} \sin \phi_{\rm sc} = \frac{1}{L} T_{\rm WE} \frac{\lambda}{4\pi} \frac{\delta \tilde{P}_{\rm BB}}{2P_{\rm BB}}$$

Scattered light is an injection of calibrated light phase shift

A check of calibration accuracy

$$\frac{h_{\text{rec}}}{h_{\text{signal}}} = \frac{T_{\text{WE}}}{T_{\text{WE}}^{\text{LMA}}} = \frac{4.34 \pm 0.04 \times 10^{-6}}{4.3 \pm 0.2 \times 10^{-6}} = 1.009 \pm 0.05.$$
$$\frac{h_{\text{rec}}}{h_{\text{signal}}} = \frac{T_{\text{NE}}}{T_{\text{NE}}^{\text{LMA}}} = \frac{4.46 \pm 0.05 \times 10^{-6}}{4.4 \pm 0.1 \times 10^{-6}} = 1.014 \pm 0.025.$$

- Calibration checked with 2 5% accuracy
- Limited by mirror transmission metrology
 - 10 times lower error achieved for squeezing filter cavity mirrors
- Higher amplitude motion \rightarrow check h(t) accuracy as a function of frequency
- Completely independent from other calibration methods
- Other methods rely on mirror displacement
 - mirror actuators (magnets or electrostatic)
 - photon pressure (Pcal)
 - gravitational interaction (Ncal)

Conclusion



- · Scattered light is an inherent problem of interferometric GW detectors
- With good sensors and models scattered light noise can be removed from data in some cases
 - Has been done online during O3, but only for the cos \u03c6_{sc} component
- ⇒ Any installed photodiodes should have electronic noise below shot noise in the audio band
- ⇒ Quadrant photodiode can be a dominating source of scattered light
- Controlled scattered light injection is a tool to characterize the interferometer
- A new method to check the GW strain data calibration with potential < 0.5% precision
- ⇒ Requires good metrology of end mirrors transmission before installation
 - aLIGO, aVirgo changing mirrors for O5

https://arxiv.org/abs/2011.03539 - M Was et al 2021 Class. Quantum Grav. 38 075020

4 different coupling paths

• Photodiode on bench sees amplitude modulation: $\cos \phi_{sc}$

$$P_{\rm B8} = \alpha T_{\rm WE} |E_0|^2 \left(1 + 2\sqrt{f_{\rm sc}} \cos \phi_{\rm sc} \right),$$

• Modulating phase of light in arms: $\sin \phi_{sc}(t)$

$$h_{
m sc, \ phase} = rac{1}{L} T_{
m WE} \sqrt{f_{
m sc}} rac{\lambda}{4\pi} \sin \phi_{
m sc}$$

• Modulating amplitude of light in arms: $\cos \phi_{sc}(t)$

Coupled due to contrast defect

$$h_{
m sc,\ amplitude} = rac{\epsilon}{\psi}rac{1}{L}T_{
m WE}\sqrt{f_{
m sc}}rac{\lambda}{4\pi}\cos\phi_{
m sc}.$$

Coupled due to radiation pressure

$$h_{\rm sc, \, pressure} = \frac{G}{L} \frac{1}{M} \frac{1}{\Omega^2 - (2\pi f)^2} \frac{8|E_0|^2}{c} T_{\rm WE} \sqrt{f_{\rm sc}} \cos \phi_{\rm sc},$$

Recycled in PR cavity and coupled due to radiation pressure

$$h_{
m sc,\ pressure\ recycled} =
ho \sqrt{T_{
m WI}} rac{G_{
m combined}}{2} h_{
m sc,\ pressure}$$