



MAX-PLANCK-GESELLSCHAFT

Radio pulsars and relativistic gravity



Max-Planck-Institut
für Radioastronomie

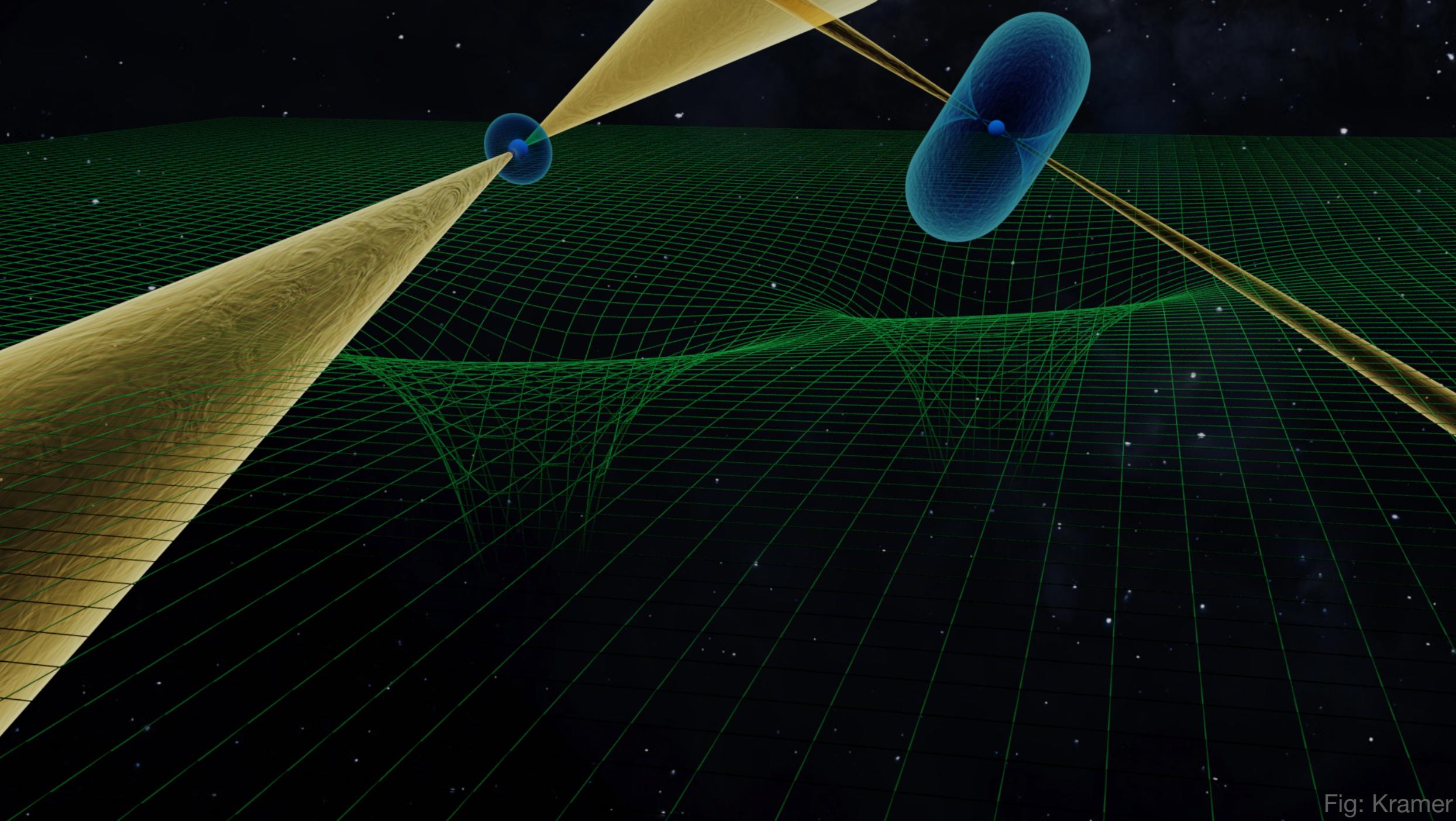
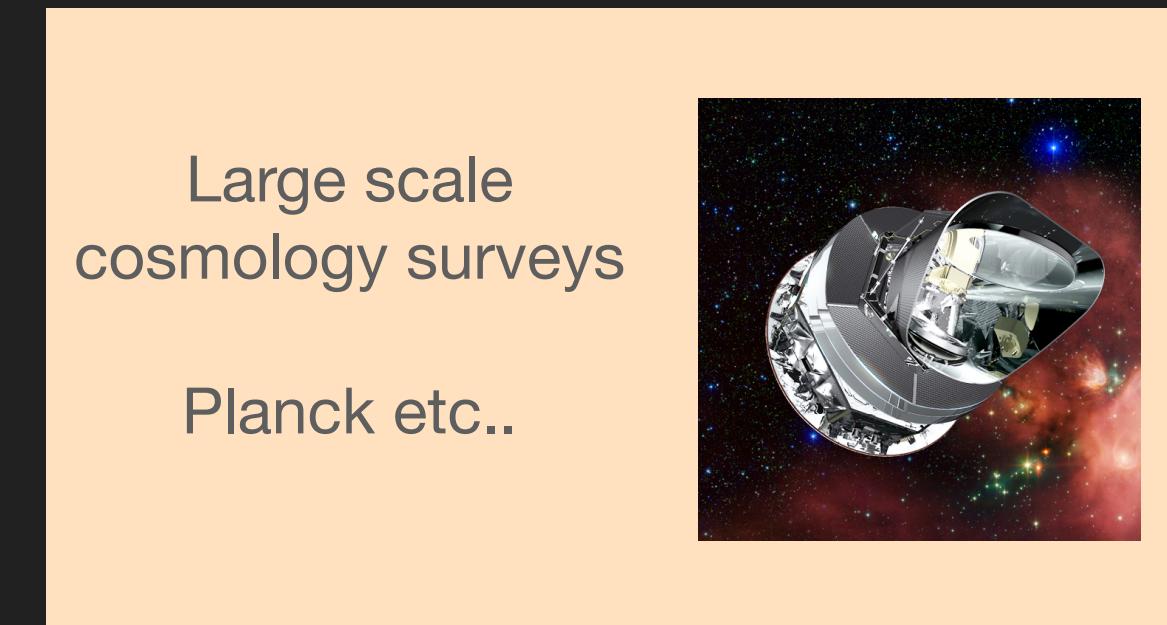
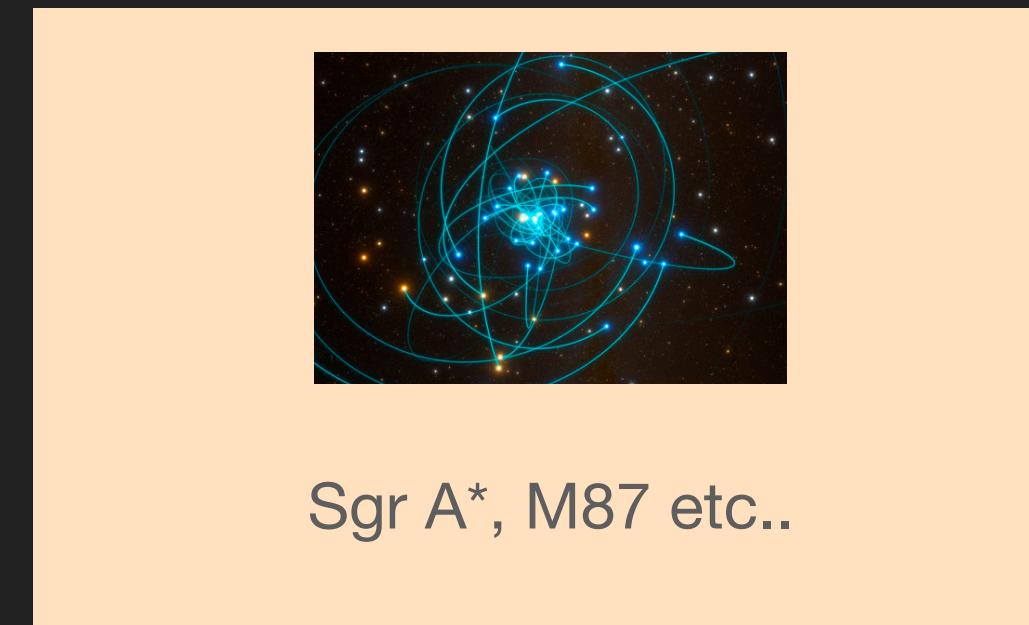
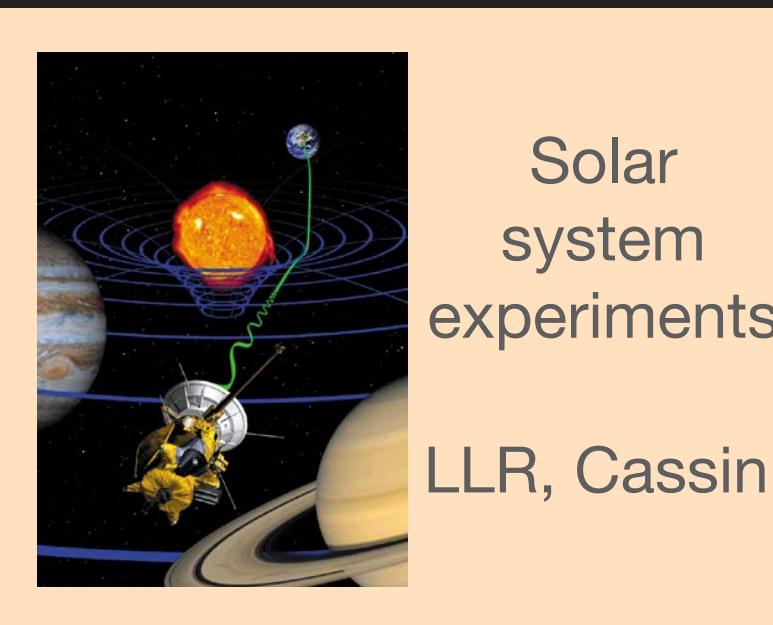


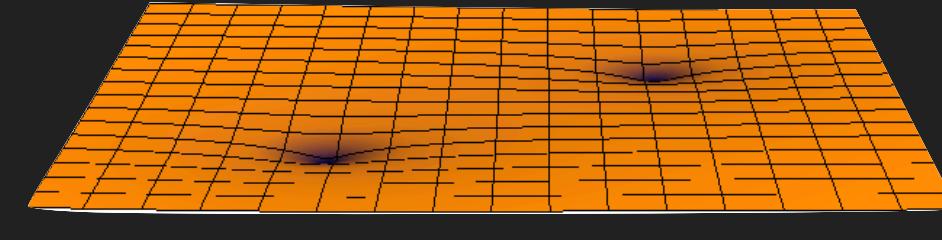
Fig: Kramer

Dr. Vivek Venkatraman Krishnan
Max-Planck-institut für Radioastronomie
Bonn, Germany

Gravity regimes and experiments

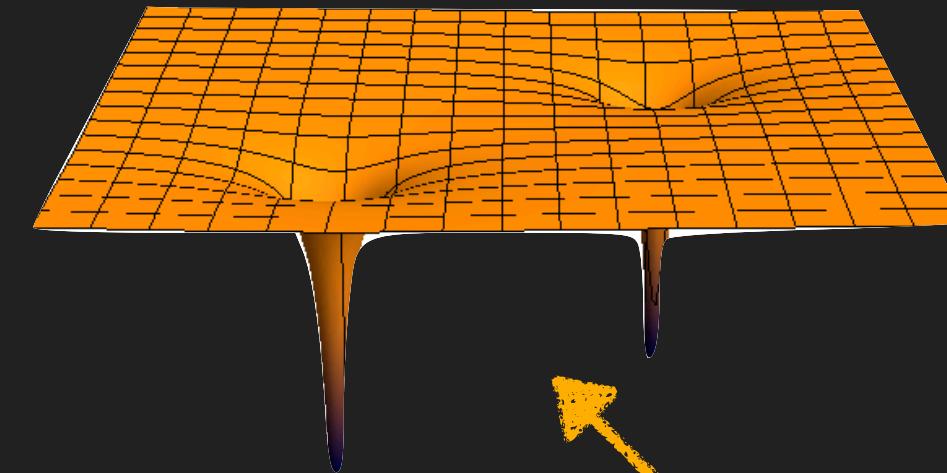


Quasi-stationary
Weak-field

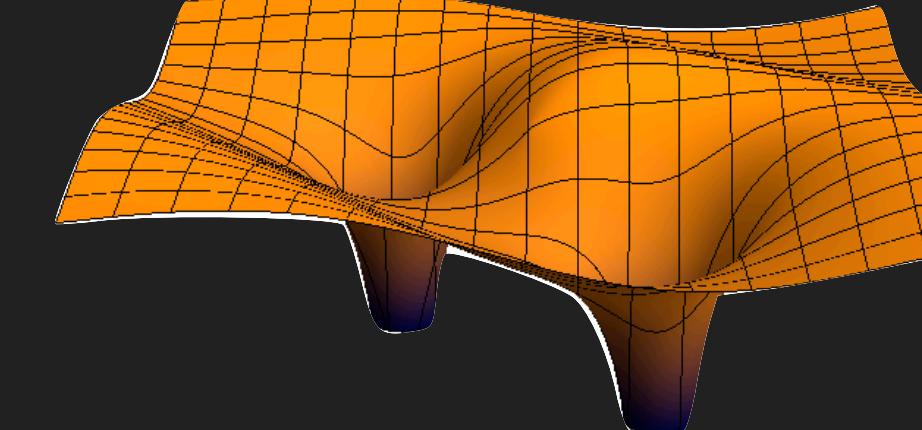


[Wex 2014]

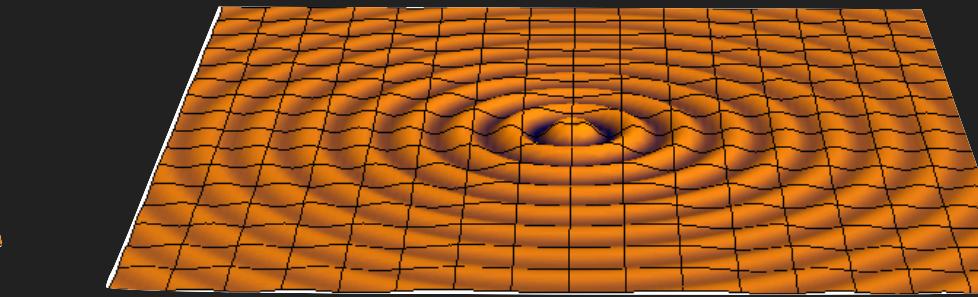
Quasi-stationary
Strong-field



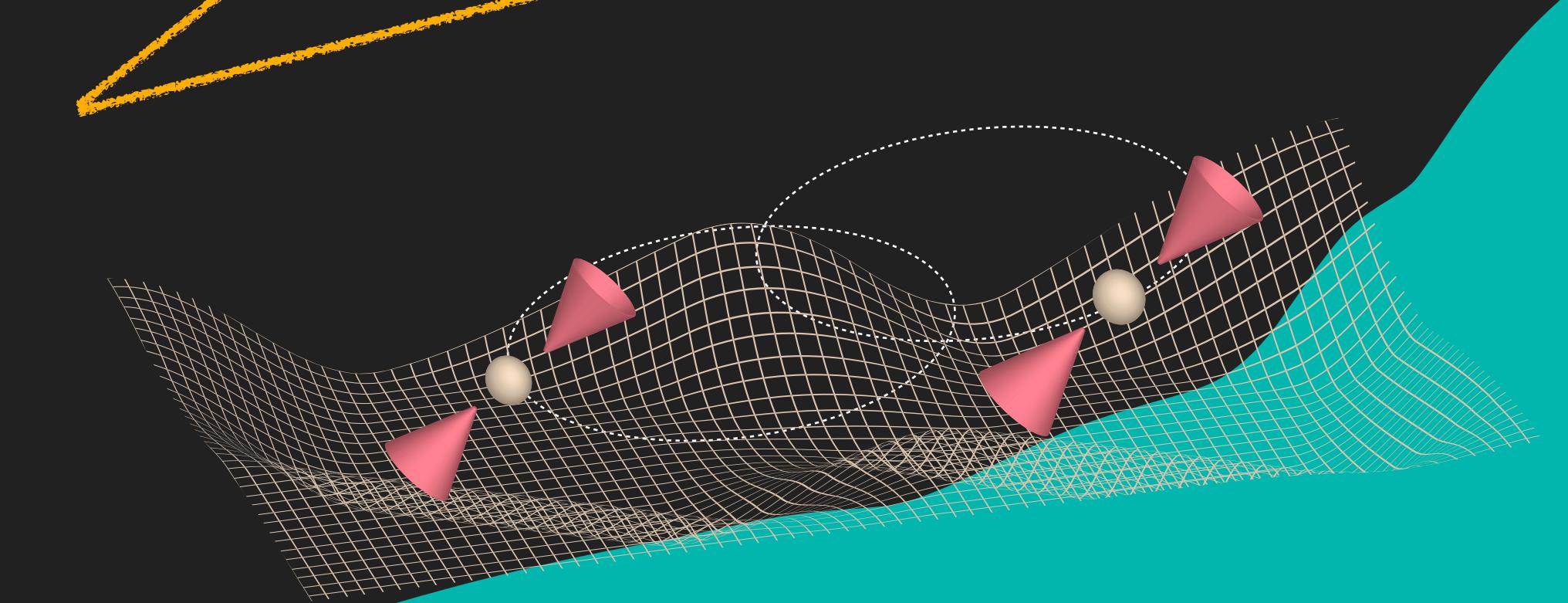
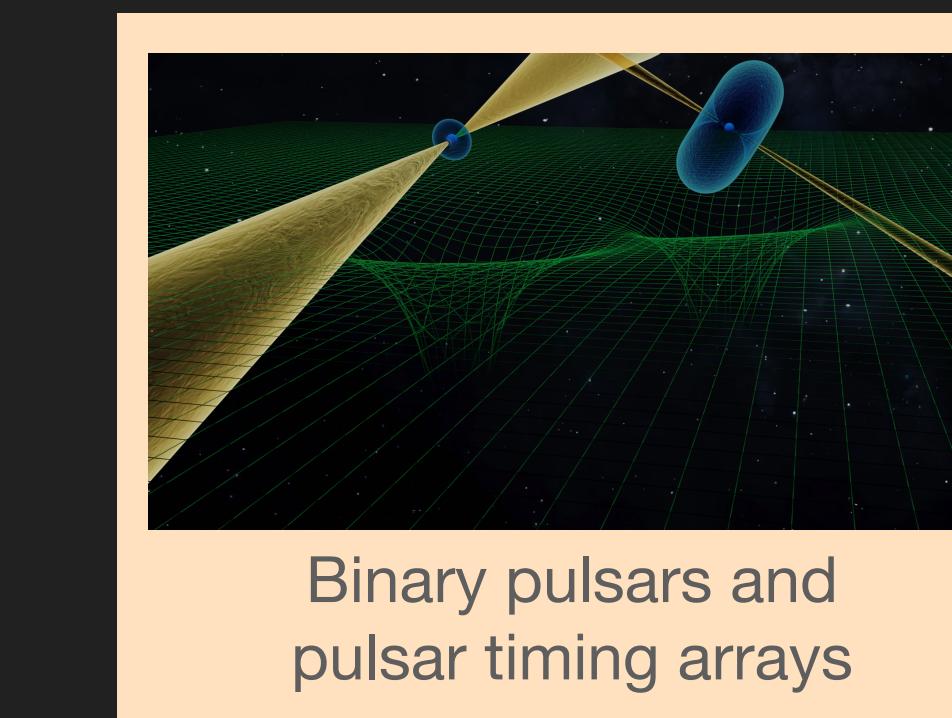
Dynamical
Strong-field



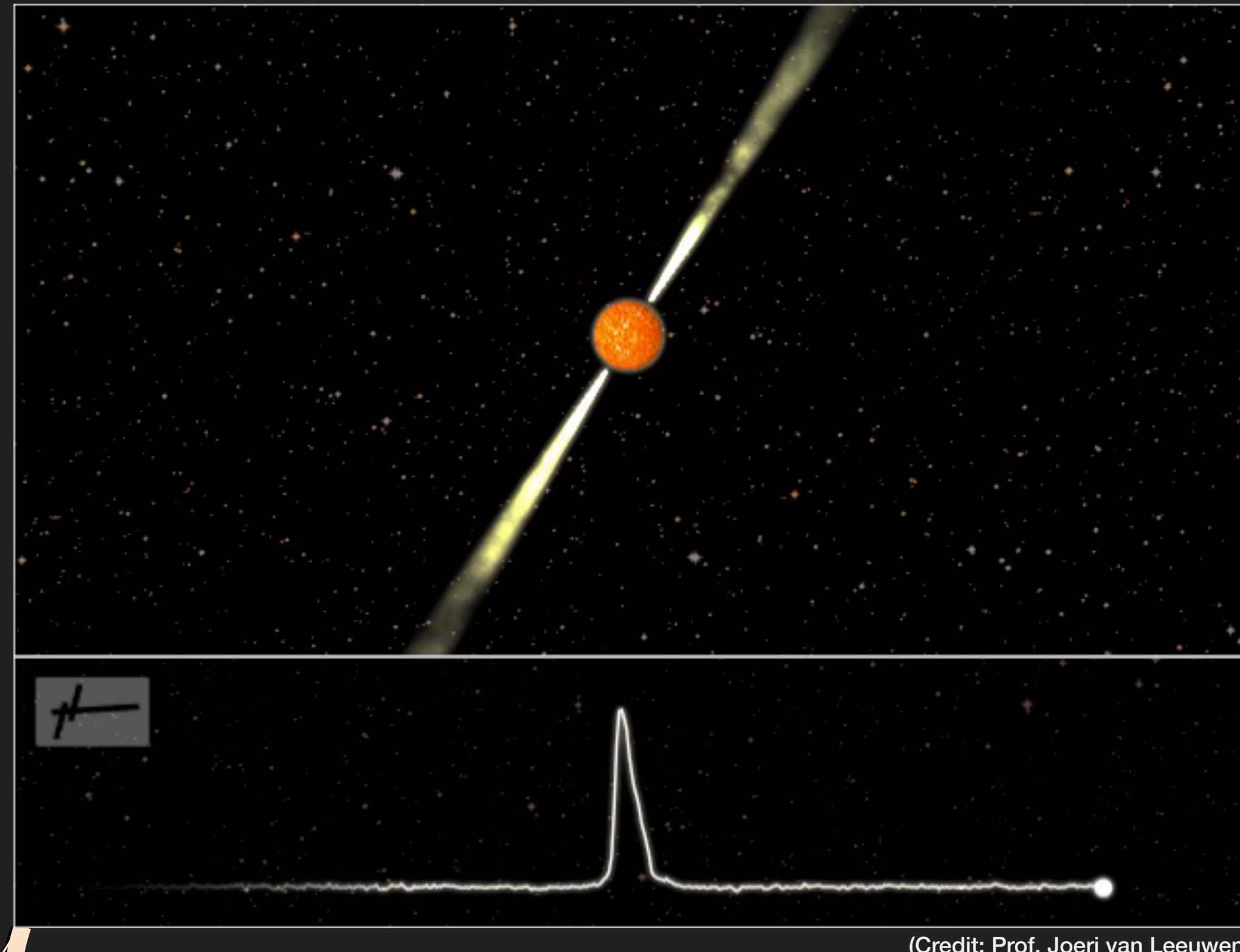
Radiative
Properties



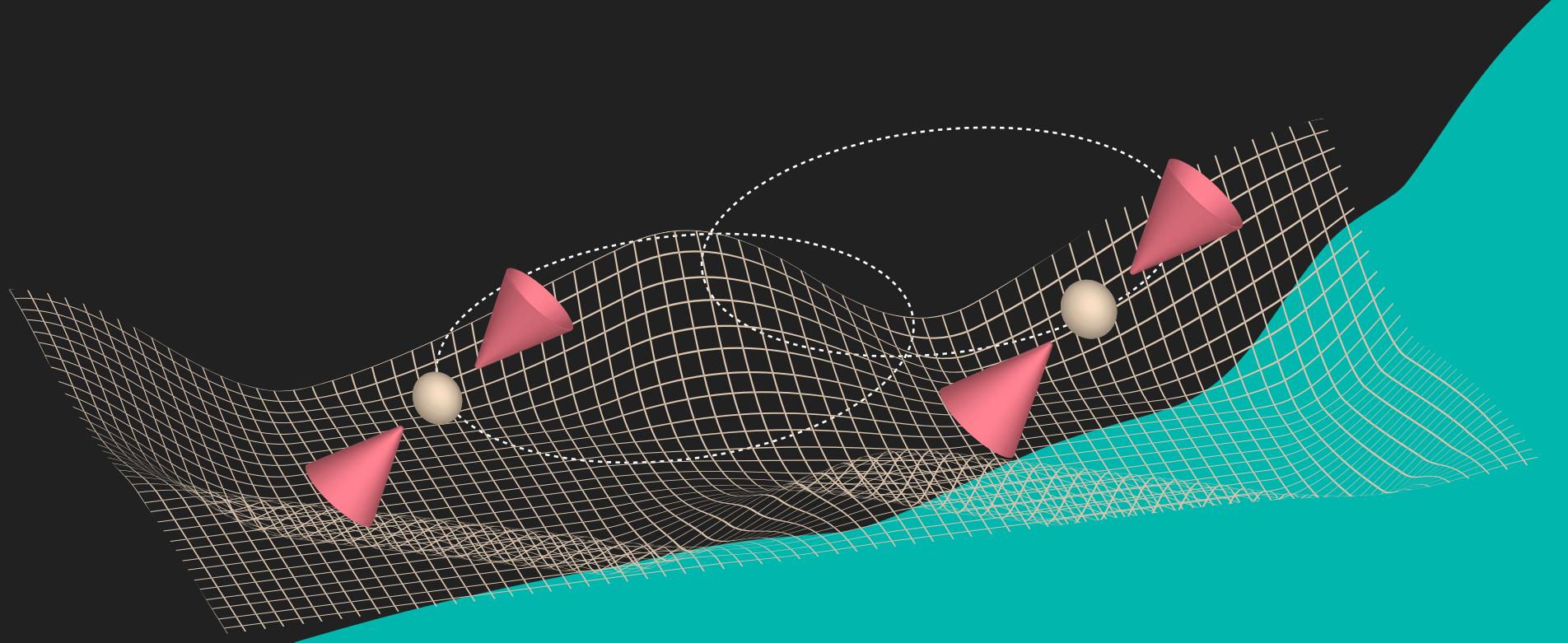
Cosmological
Scales



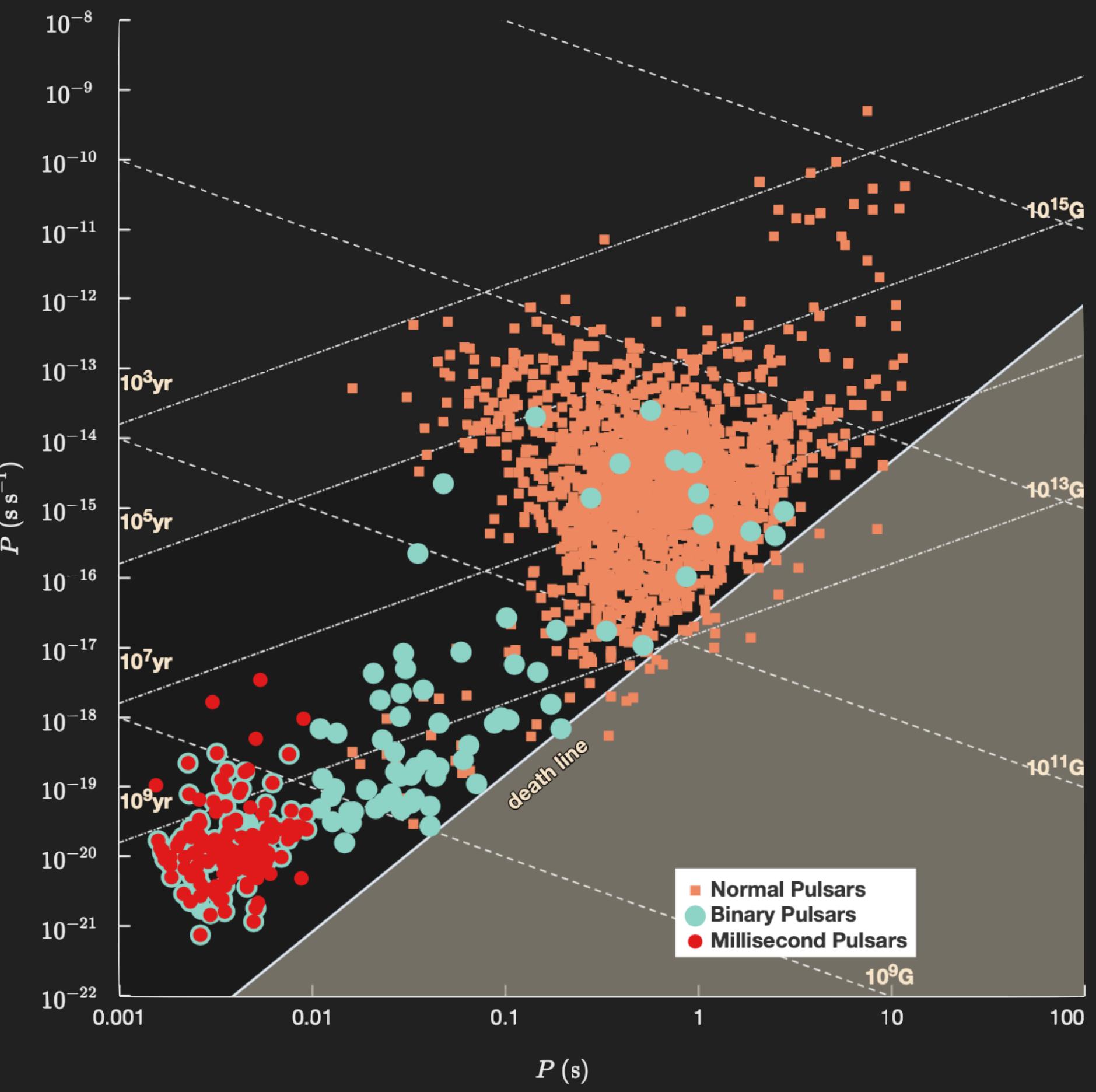
Pulsars



- Neutron stars that emit coherent magnetic dipole radiation
- High rotational stability
- arrival times of "pulses" are highly regular and can be "timed" to unparalleled precision*



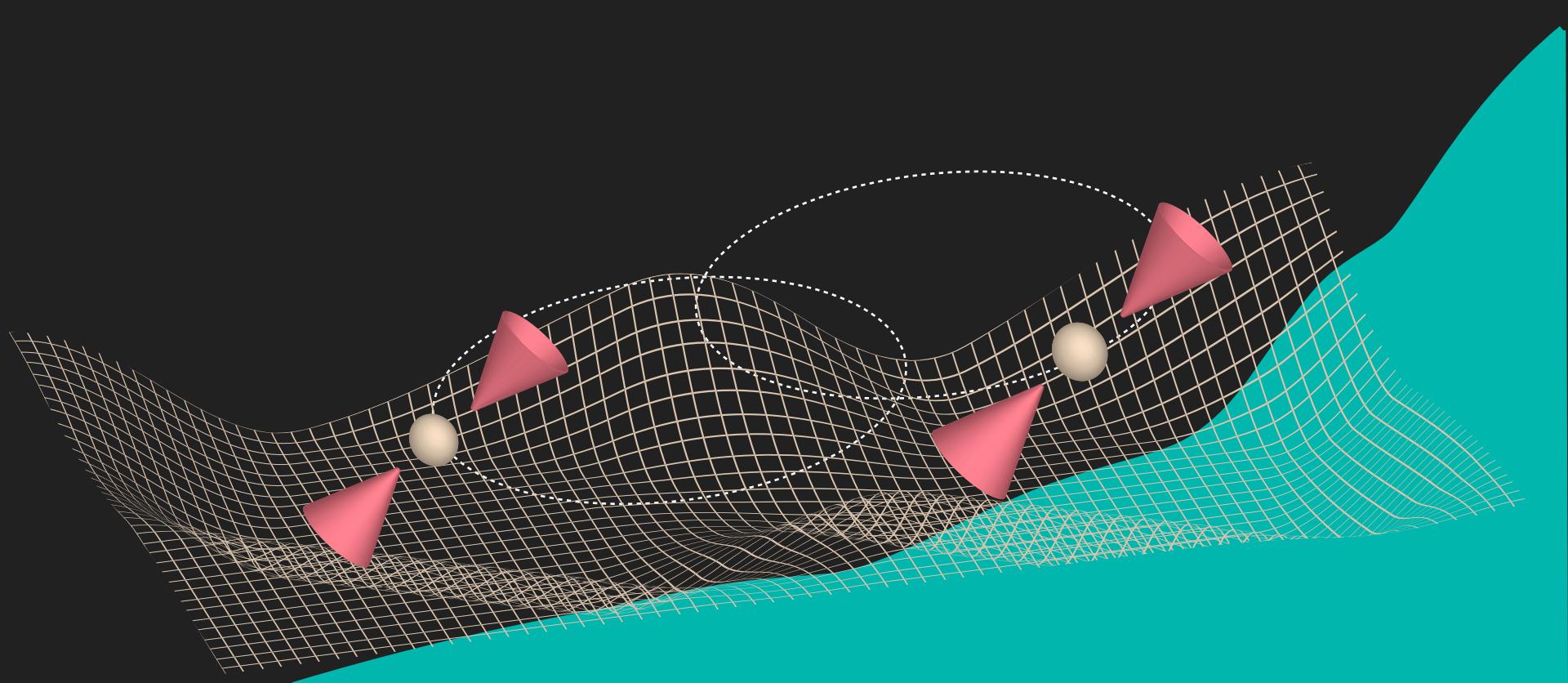
The $P - \dot{P}$ diagram



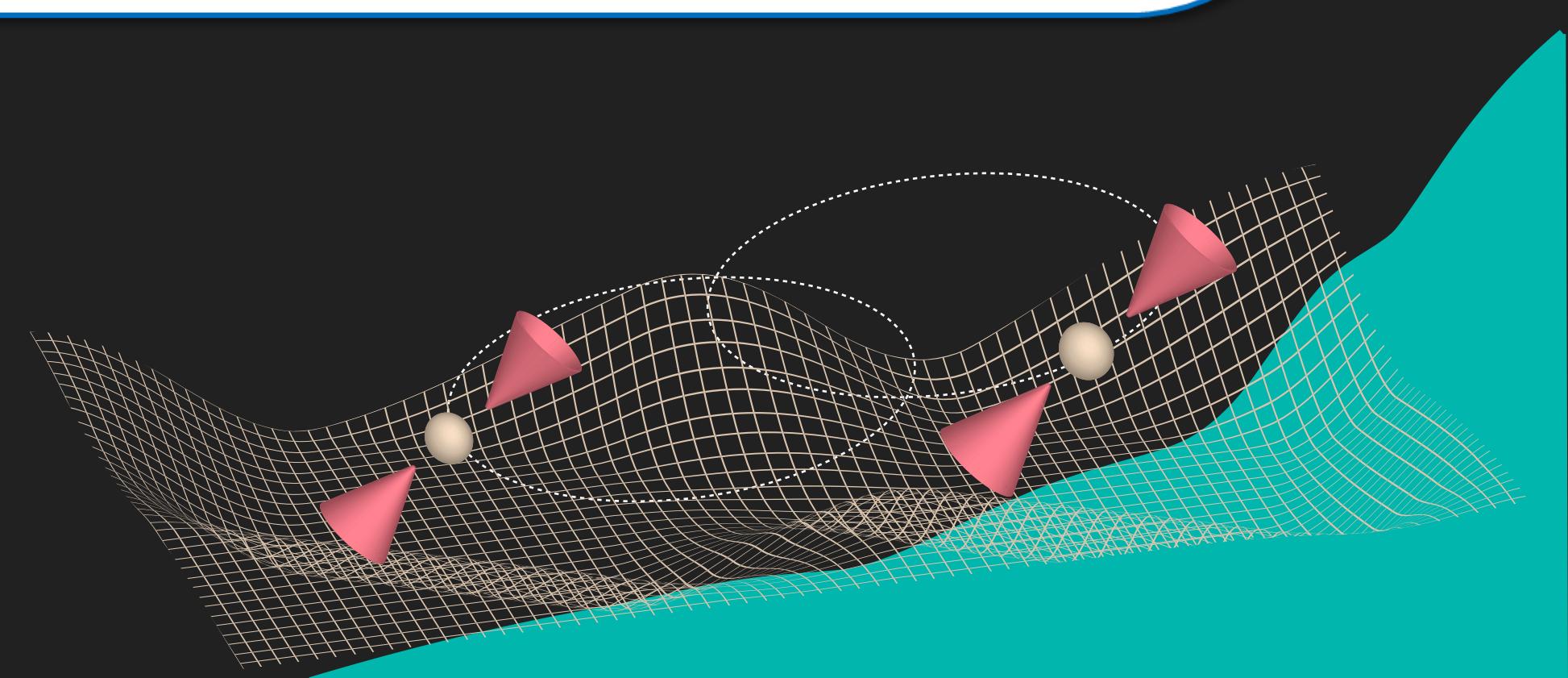
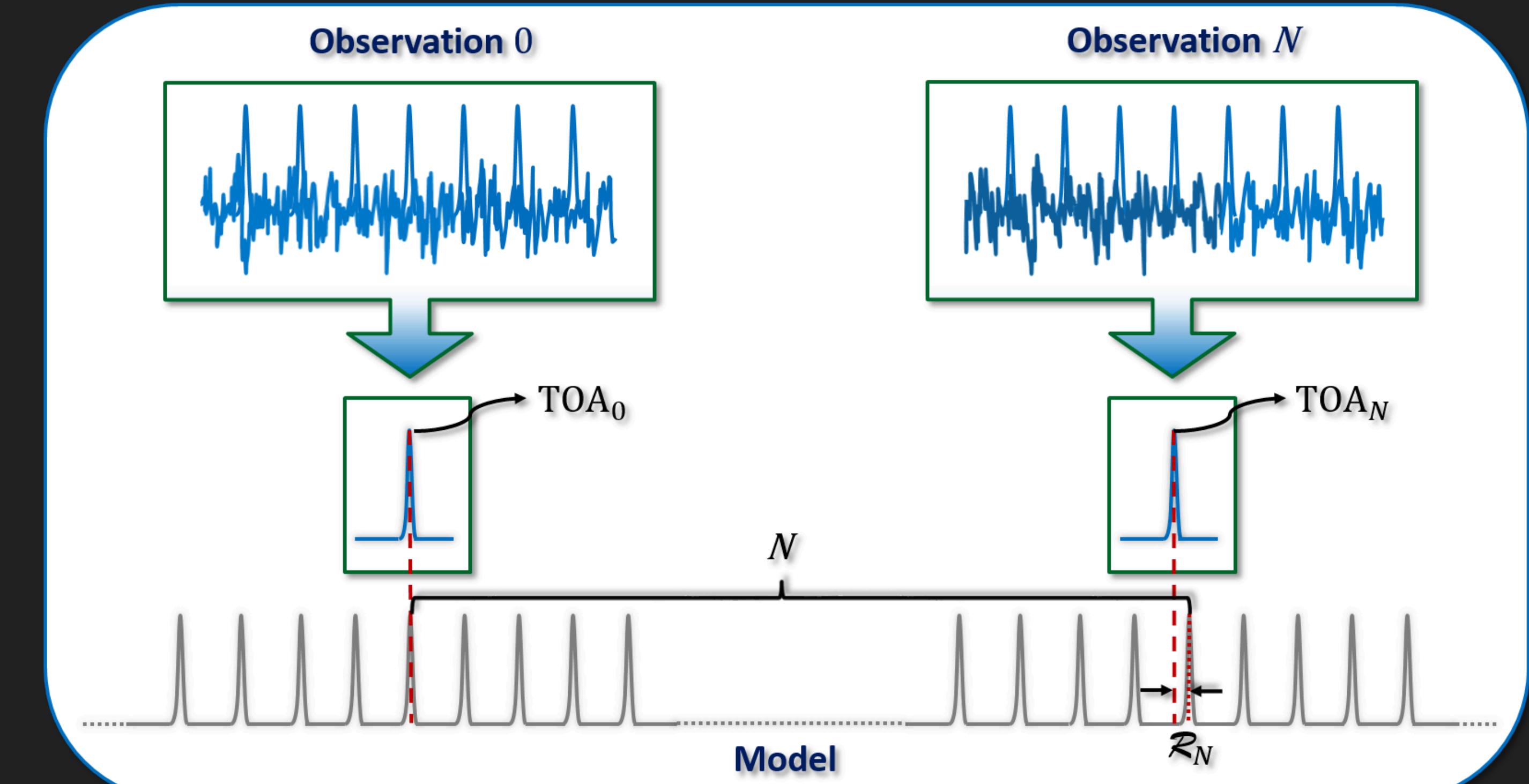
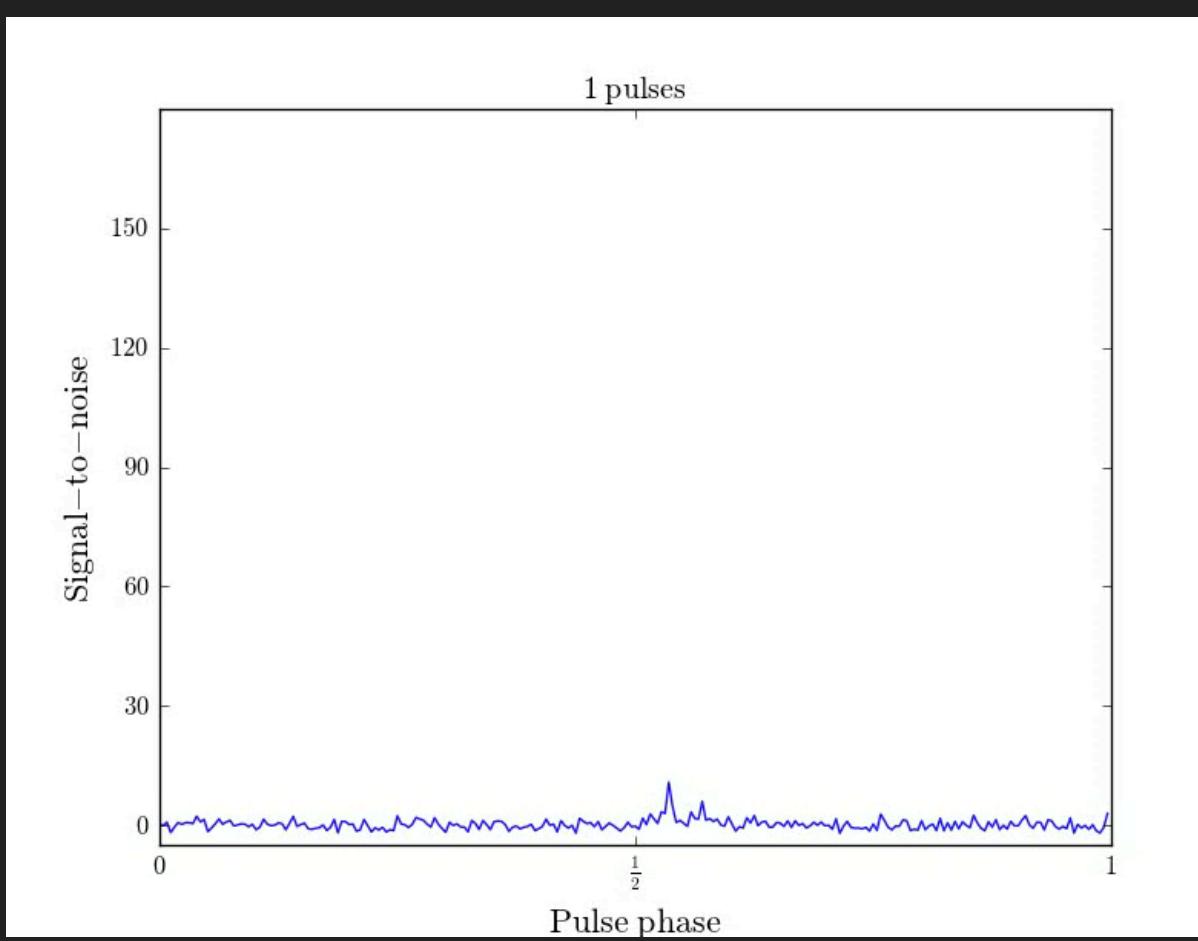
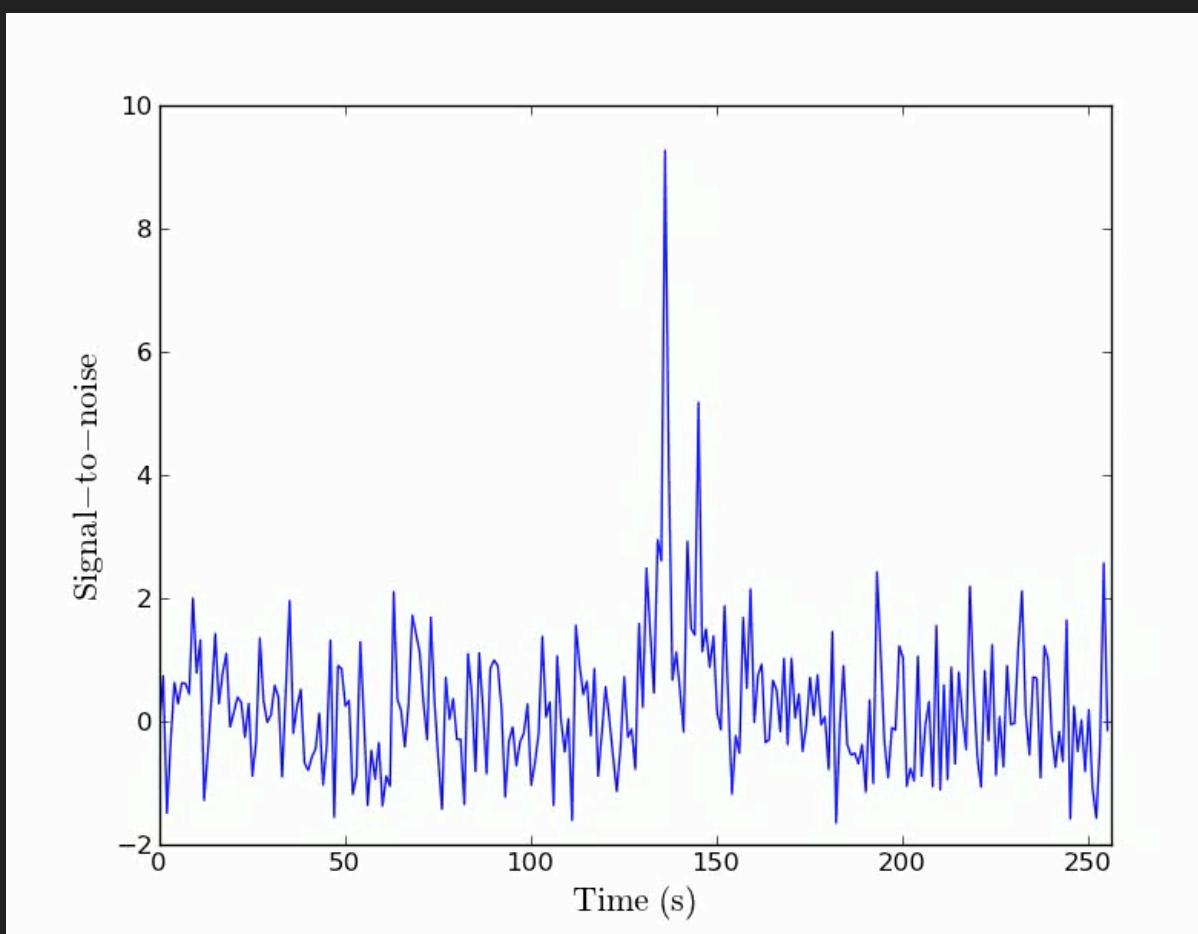
- 10% of known pulsars in binary systems
- 10% of binaries exhibits relativistic effects

How do we measure it?

The art of pulsar timing!

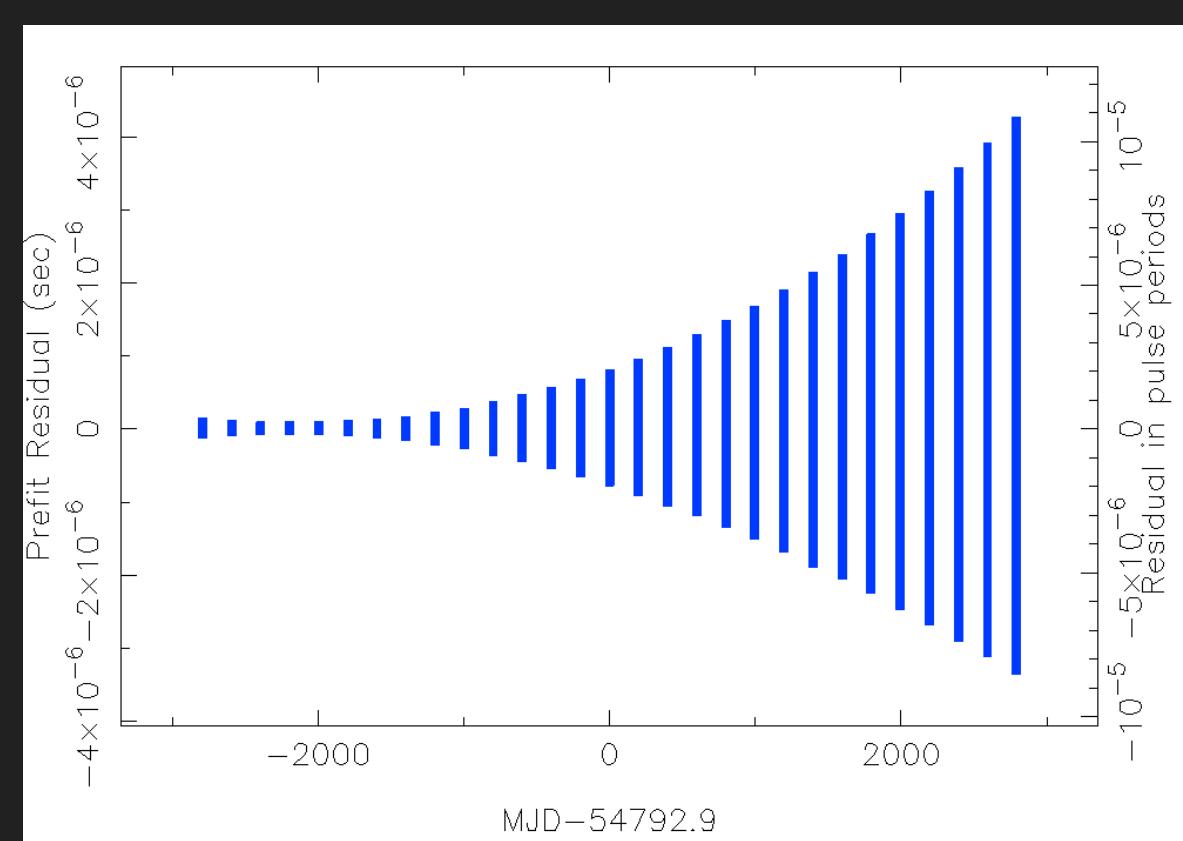
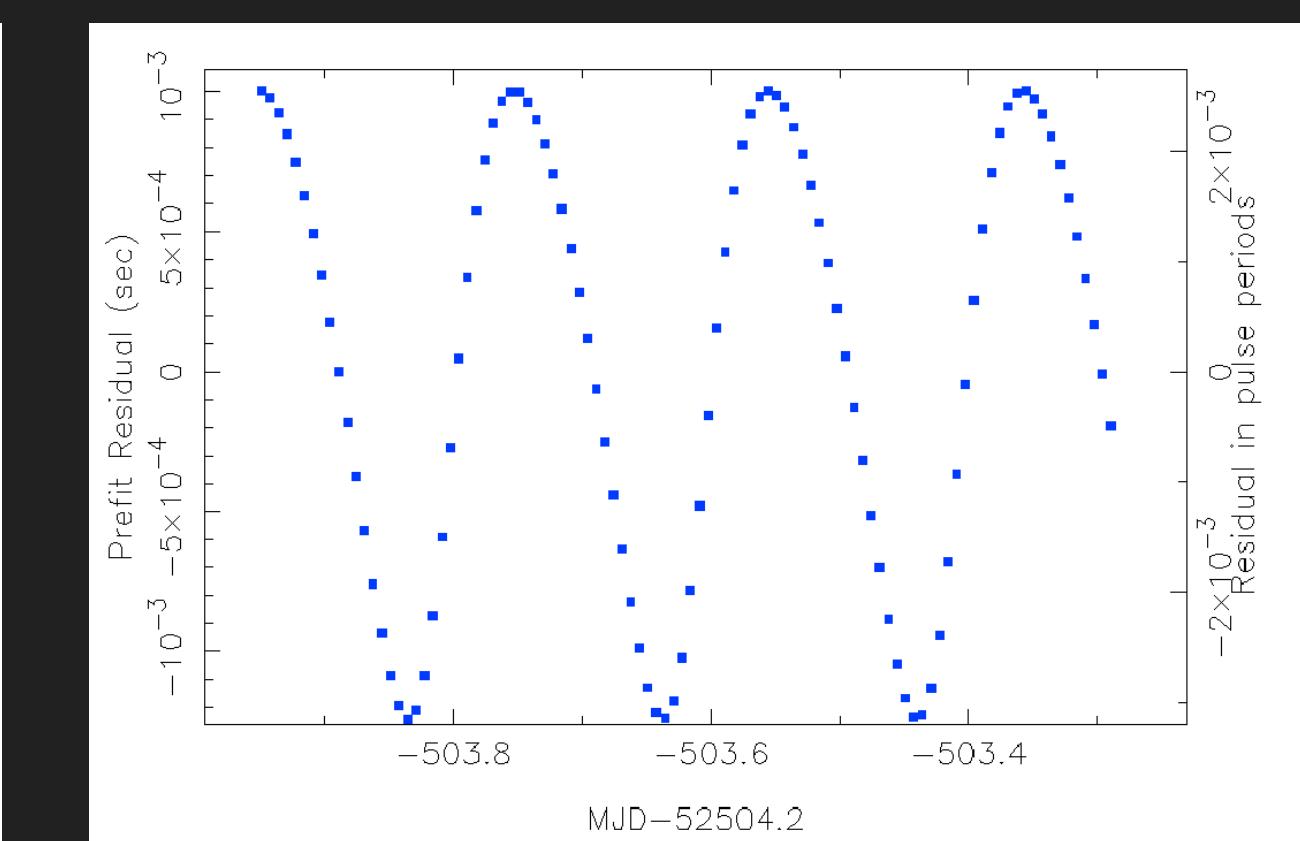
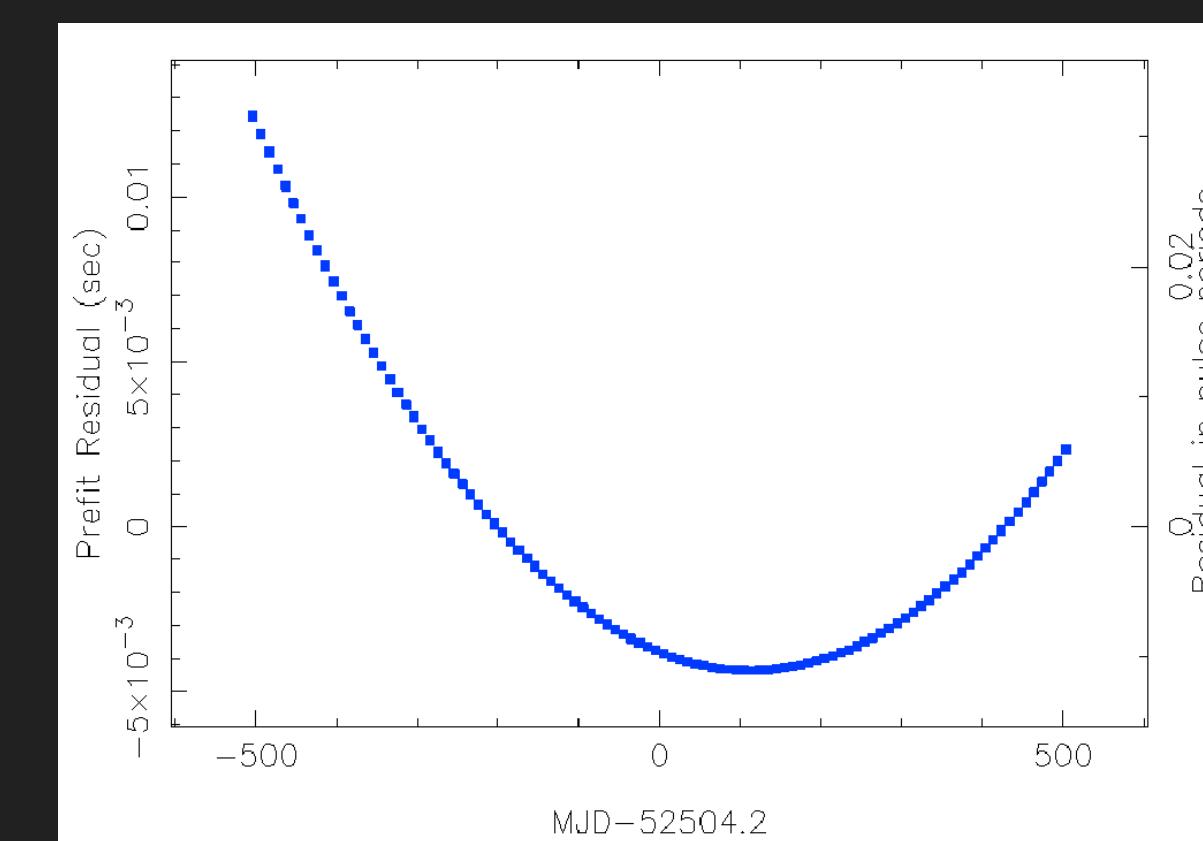
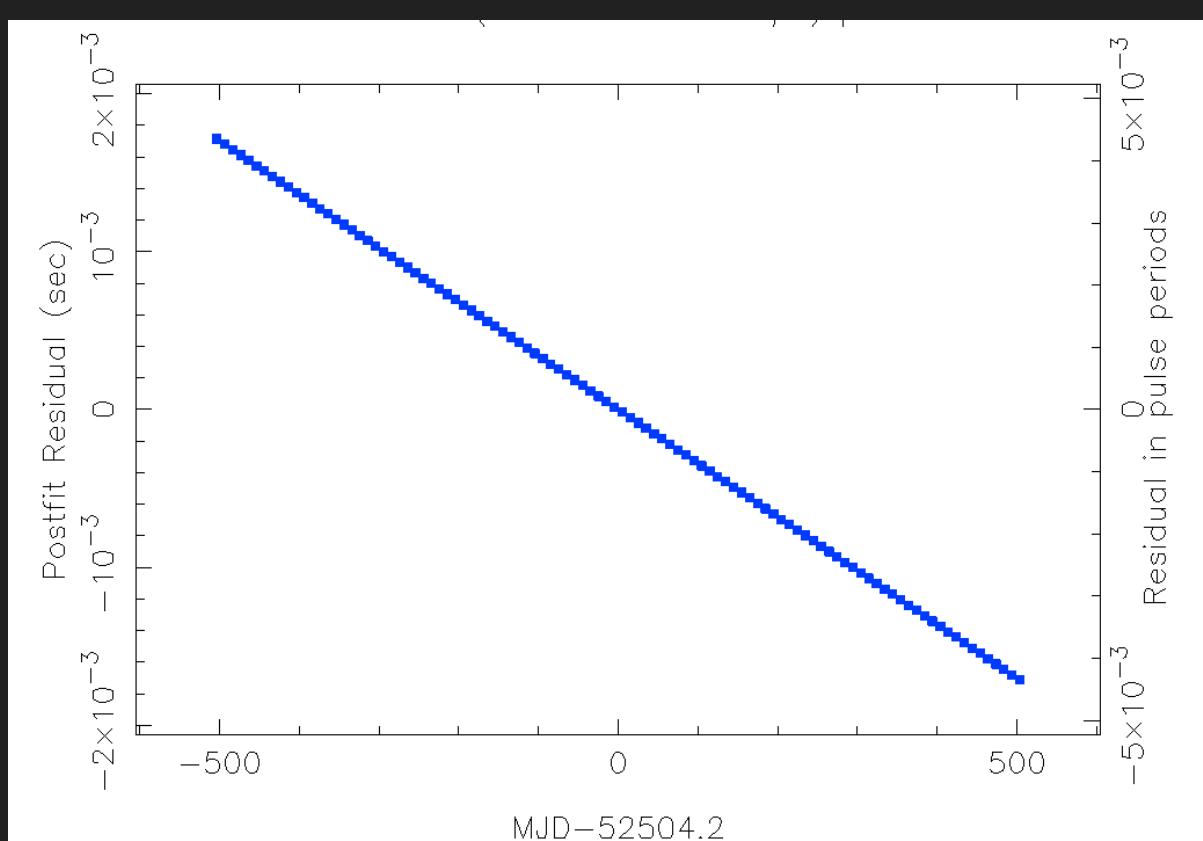


Pulsar timing, ToA and the residual

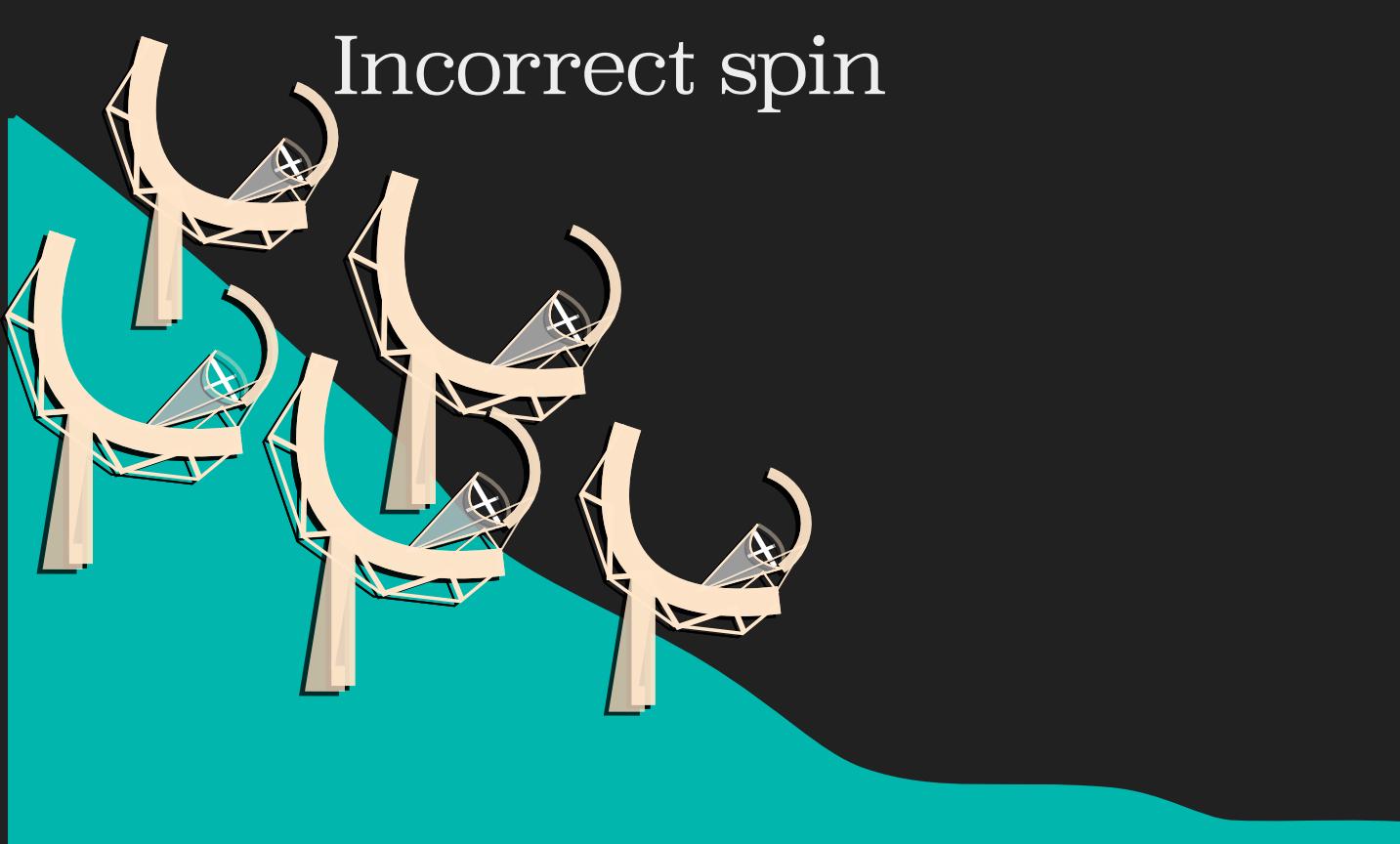


But how do you know what is wrong?

- Un-modelled/ inaccurate models of spin, orbital, astrometric & relativistic dynamics in the system create short to long term drifts in the timing residuals.
- One can fit for such offsets and develop a better pulsar “model”



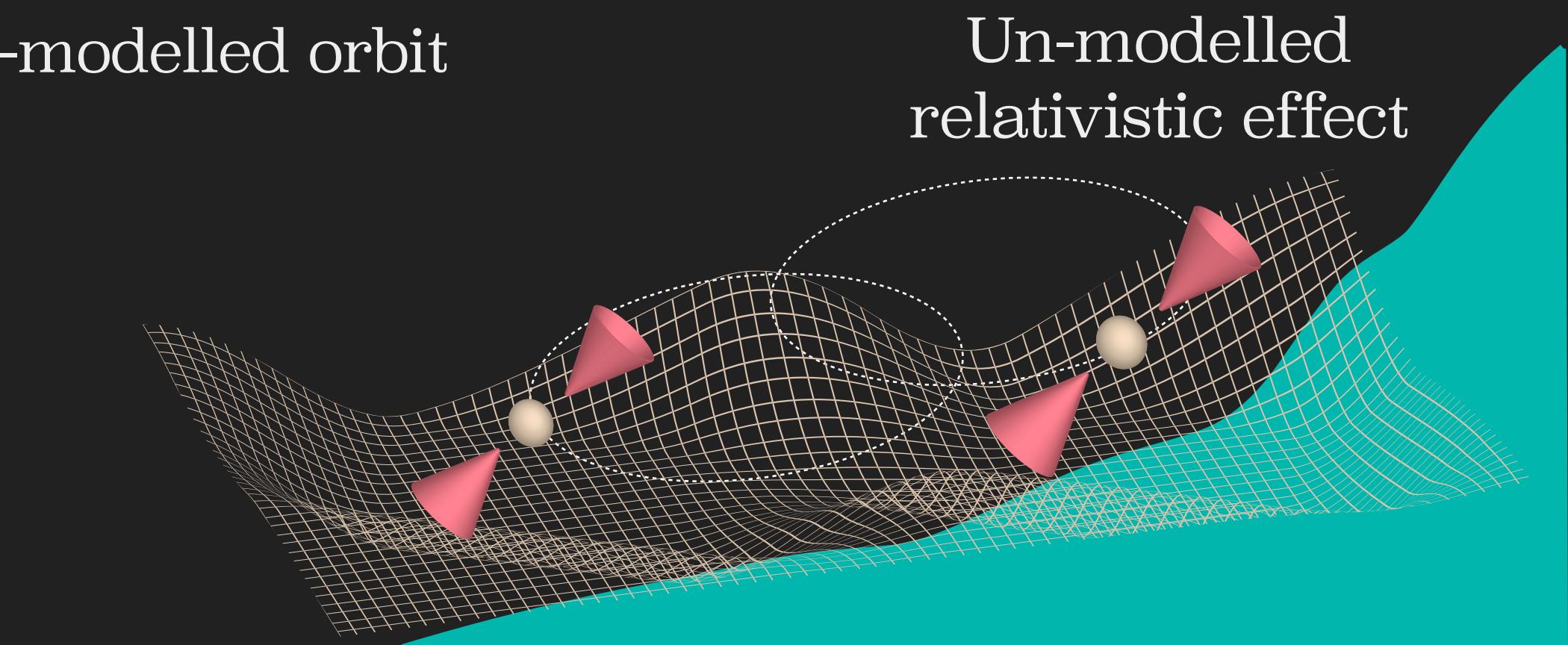
Incorrect spin



Incorrect spin-down

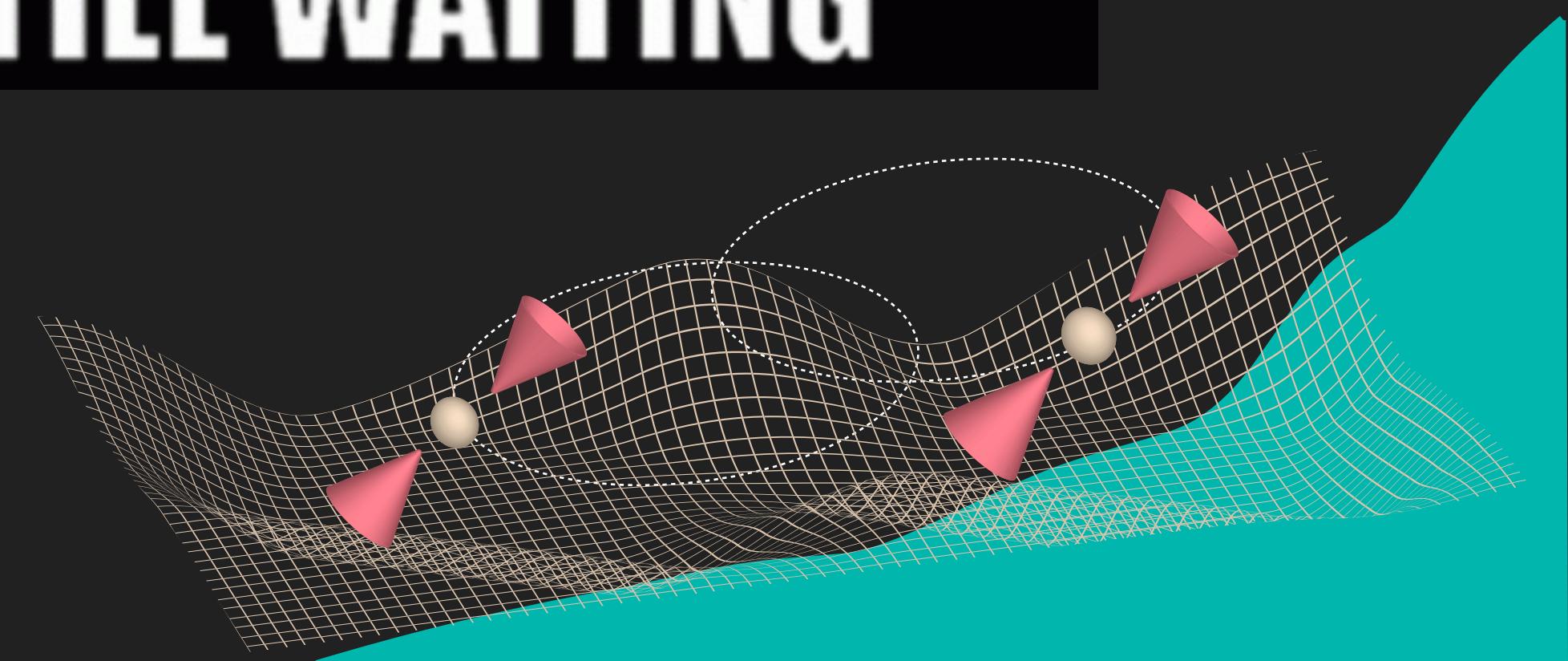
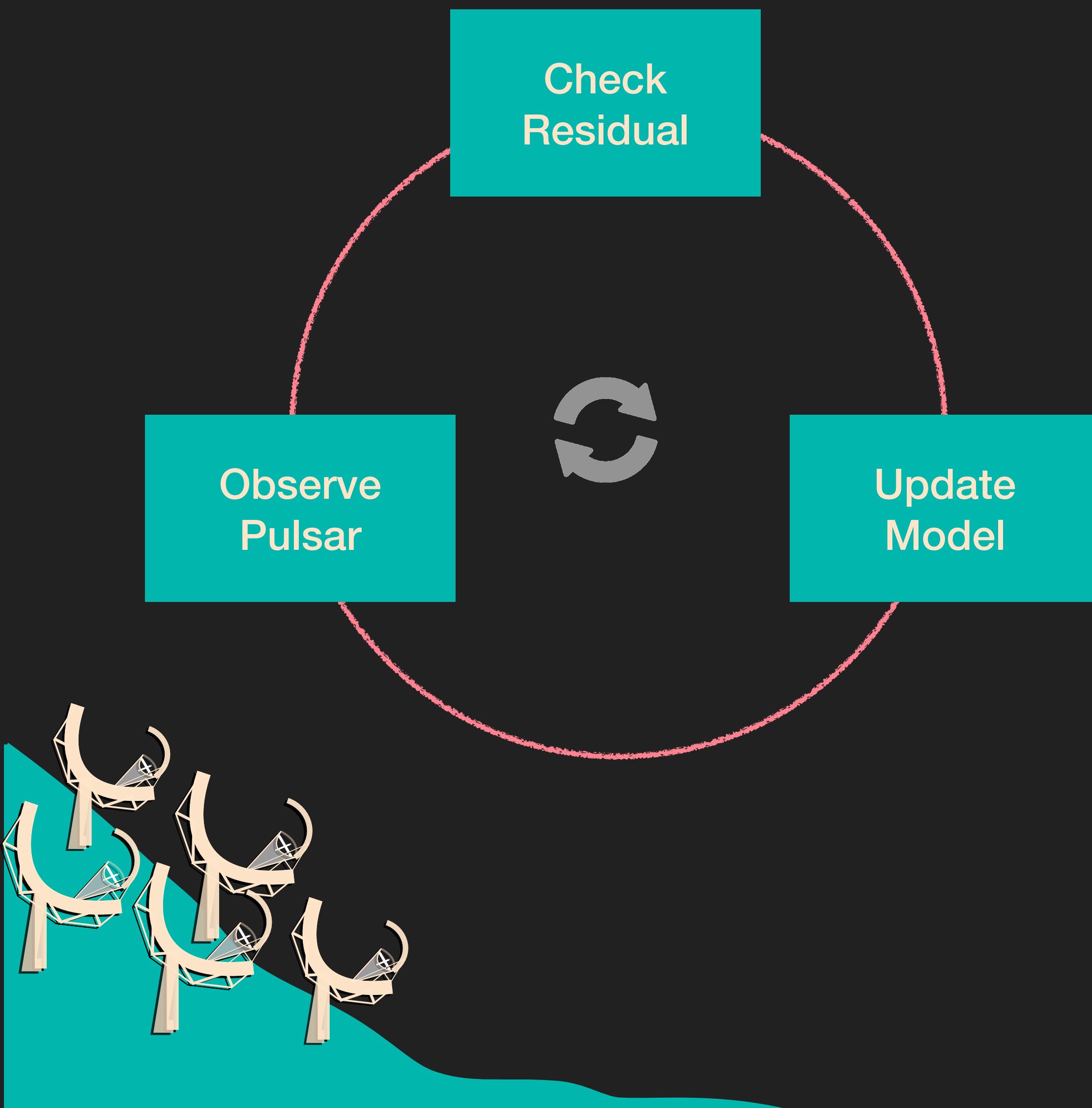


Un-modelled orbit

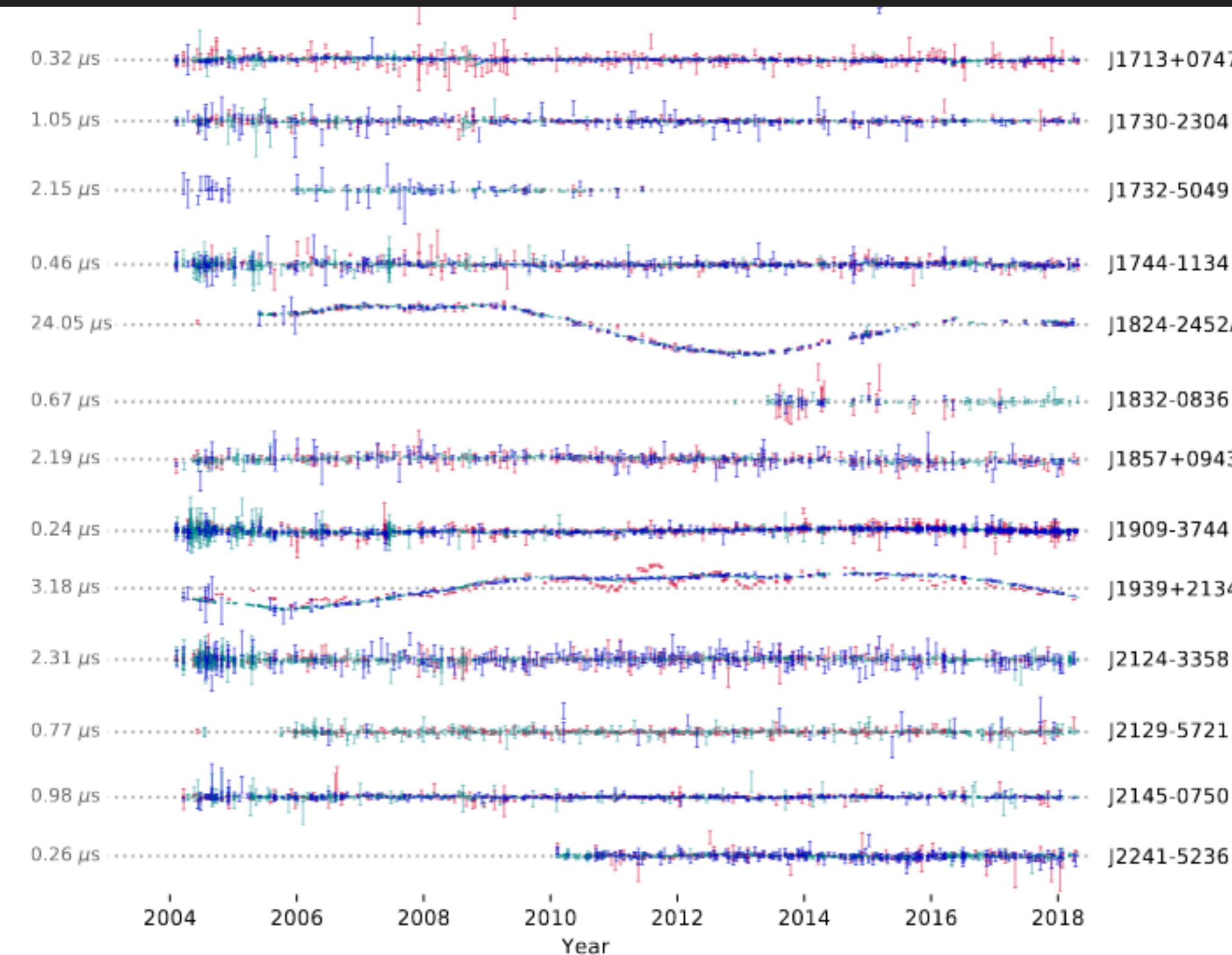


Un-modelled relativistic effect

For the next few years.....



The power of pulsar timing



Spin parameters:

Period:

2.947108069160717(3) ms (Reardon et al. 2015)

3 atto seconds uncertainty!

Astrometry:

Position in the sky:

0.6 μas (Reardon et al. 2015)

Proper motion:

140.911(3) mas/yr (Reardon et al. 2015)

Distance:

156.79 ± 0.25 pc (Reardon et al. 2015)

Orbital parameters:

Orbital period:

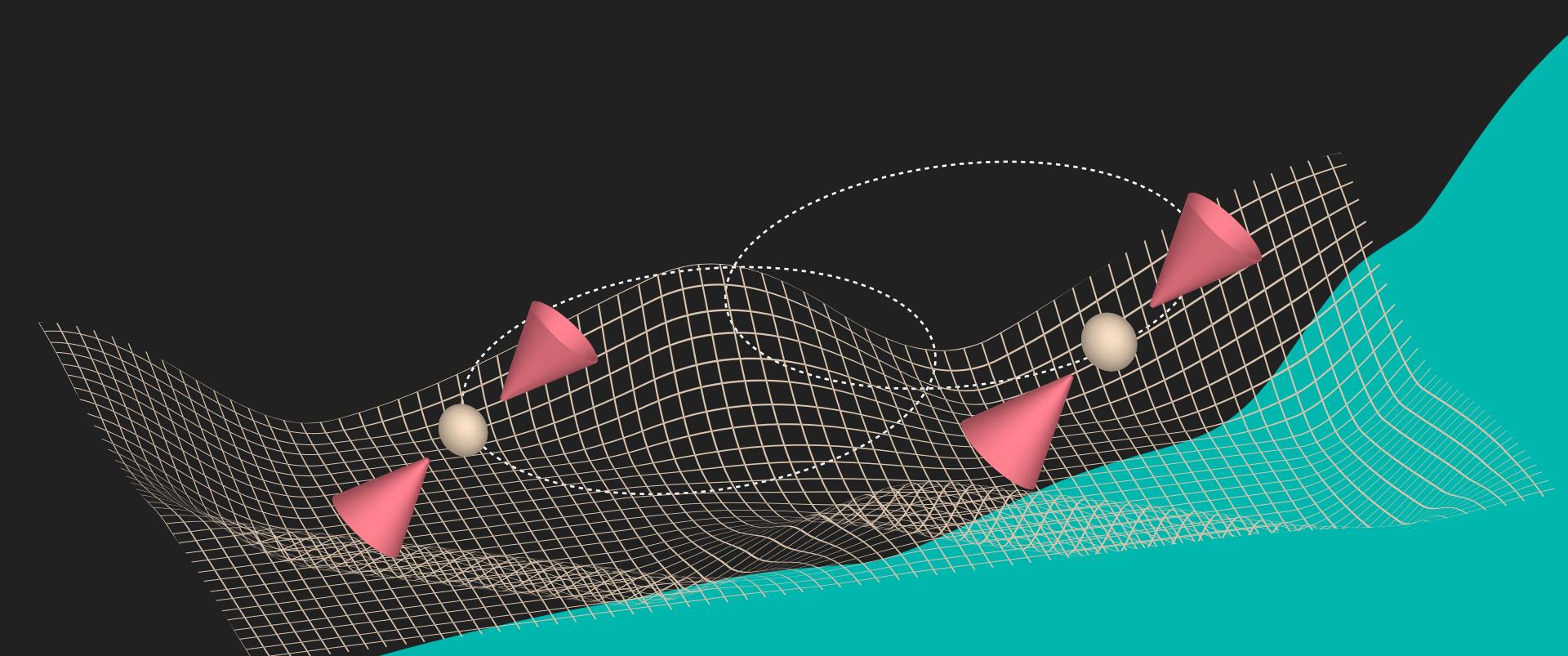
0.102251559297(1) days (Kramer et al., submitted)

Projected semi-major axis

31 659 820.5(2) km (Heusgen et al., in prep.)

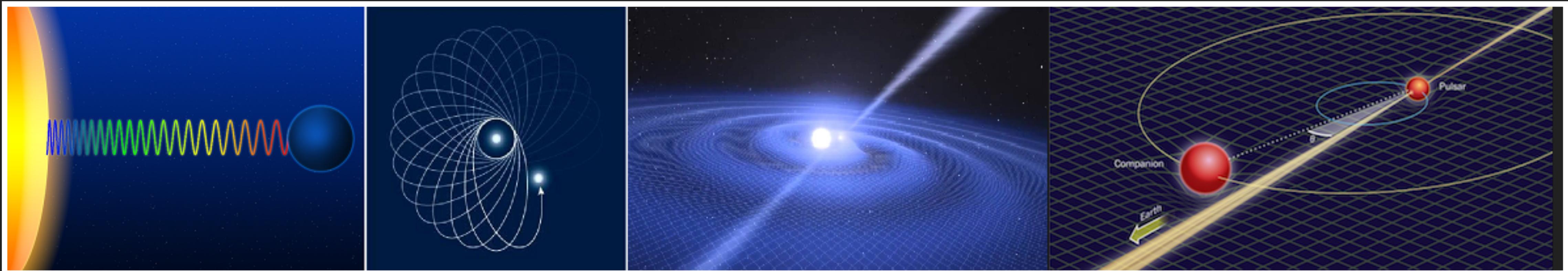
Eccentricity:

0.436678414(5) (Heusgen et al., in prep.)



Relativistic effects: The PK formalism

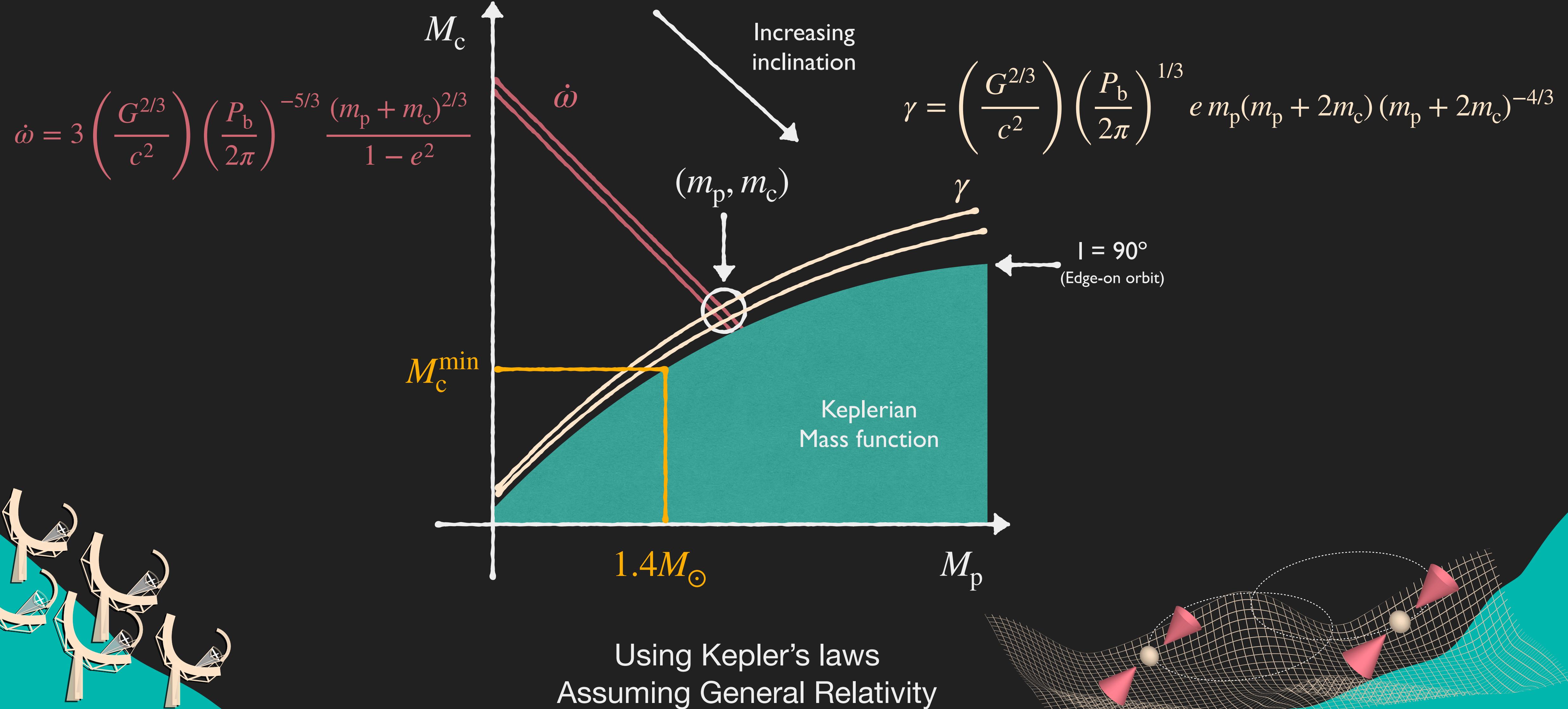
- Periastron advance ($\dot{\omega}$)
- Gravitational wave damping (\dot{P}_b)
- Shapiro delay (r, s)
- Gravitational redshift and transverse Doppler effect (γ)



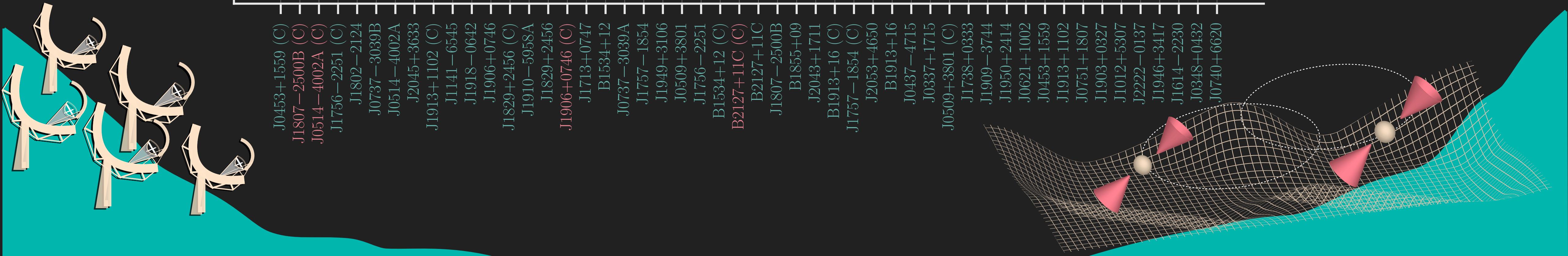
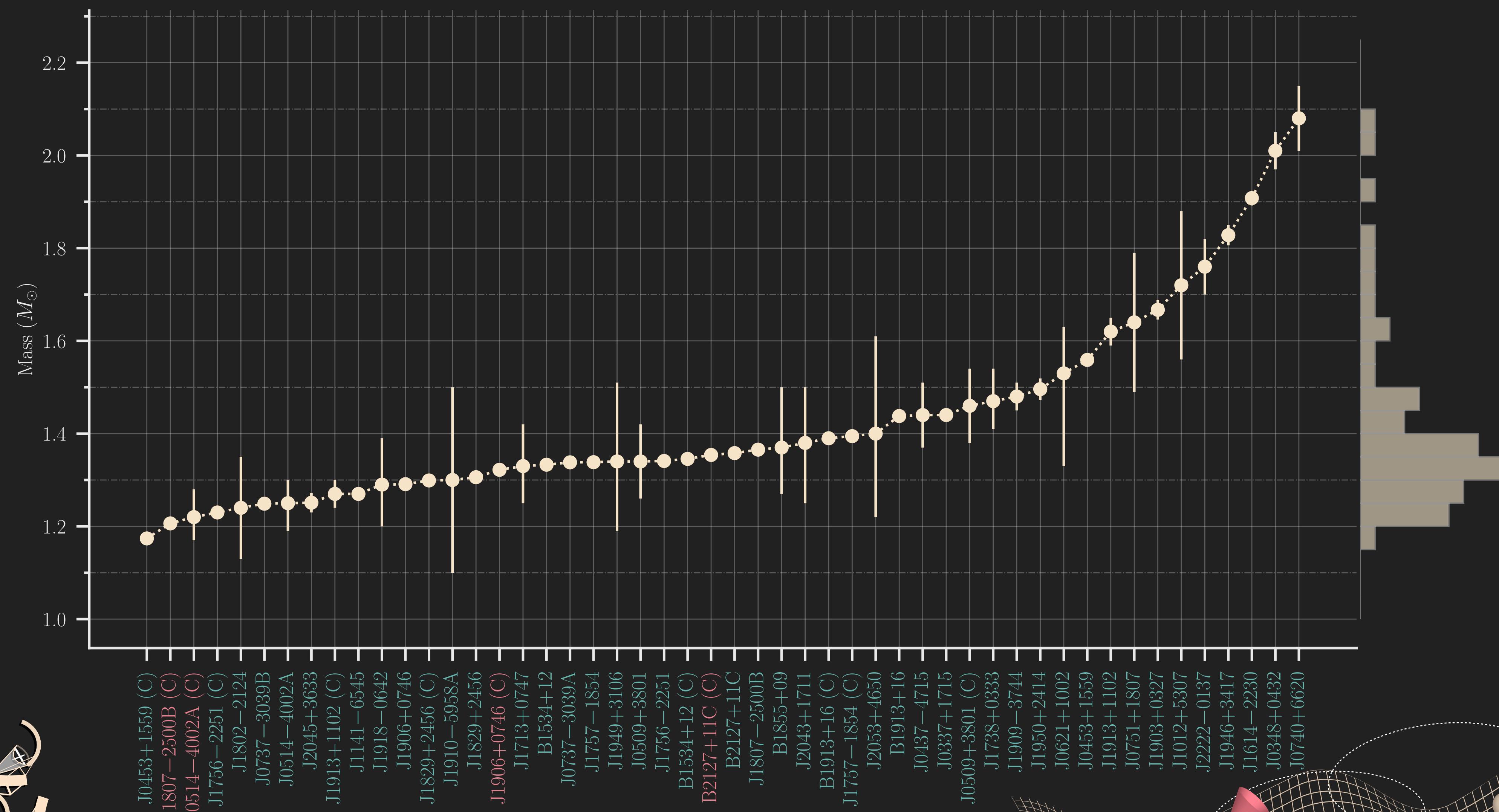
Measurements from Geometry & Algebra. Hence theory independent!

Theories of gravity relate PK parameters to masses

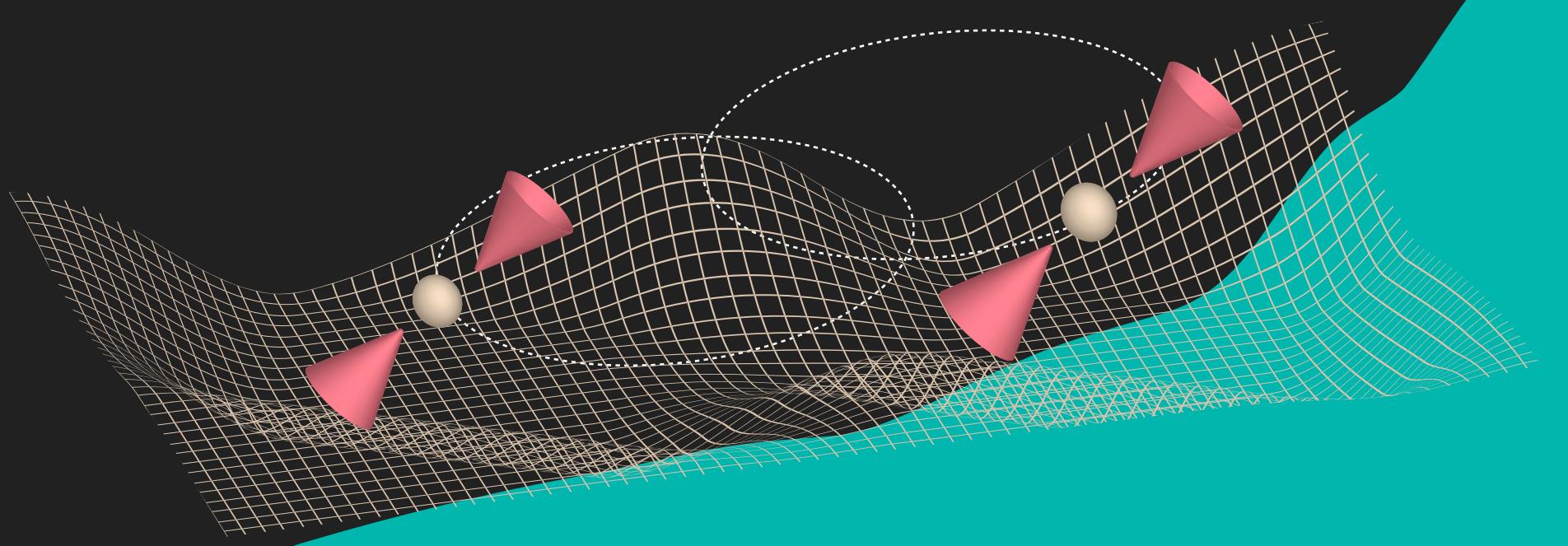
The mass-mass diagram



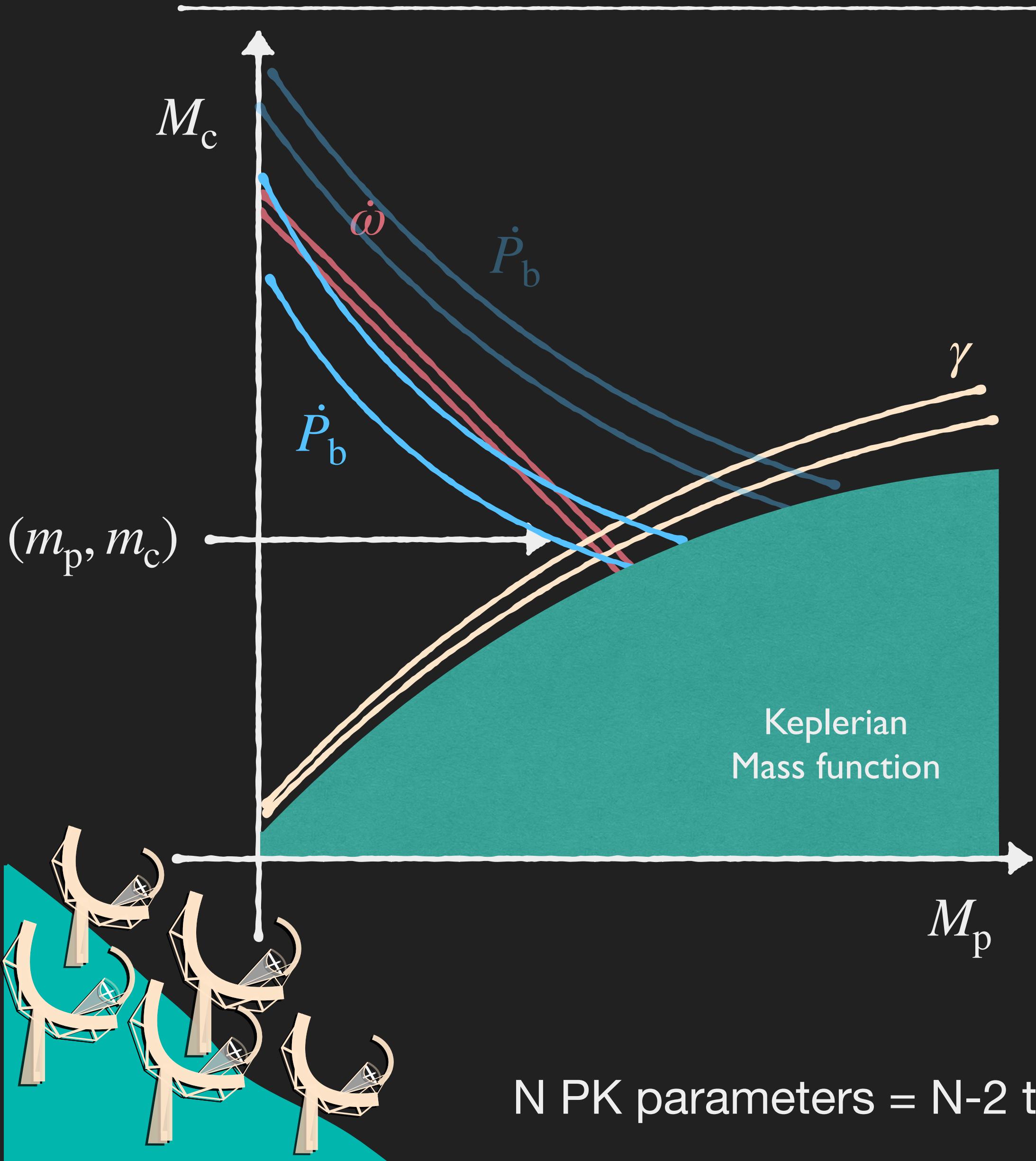
Mass measurements of binary pulsar systems



What if you can measure more?



Testing gravity

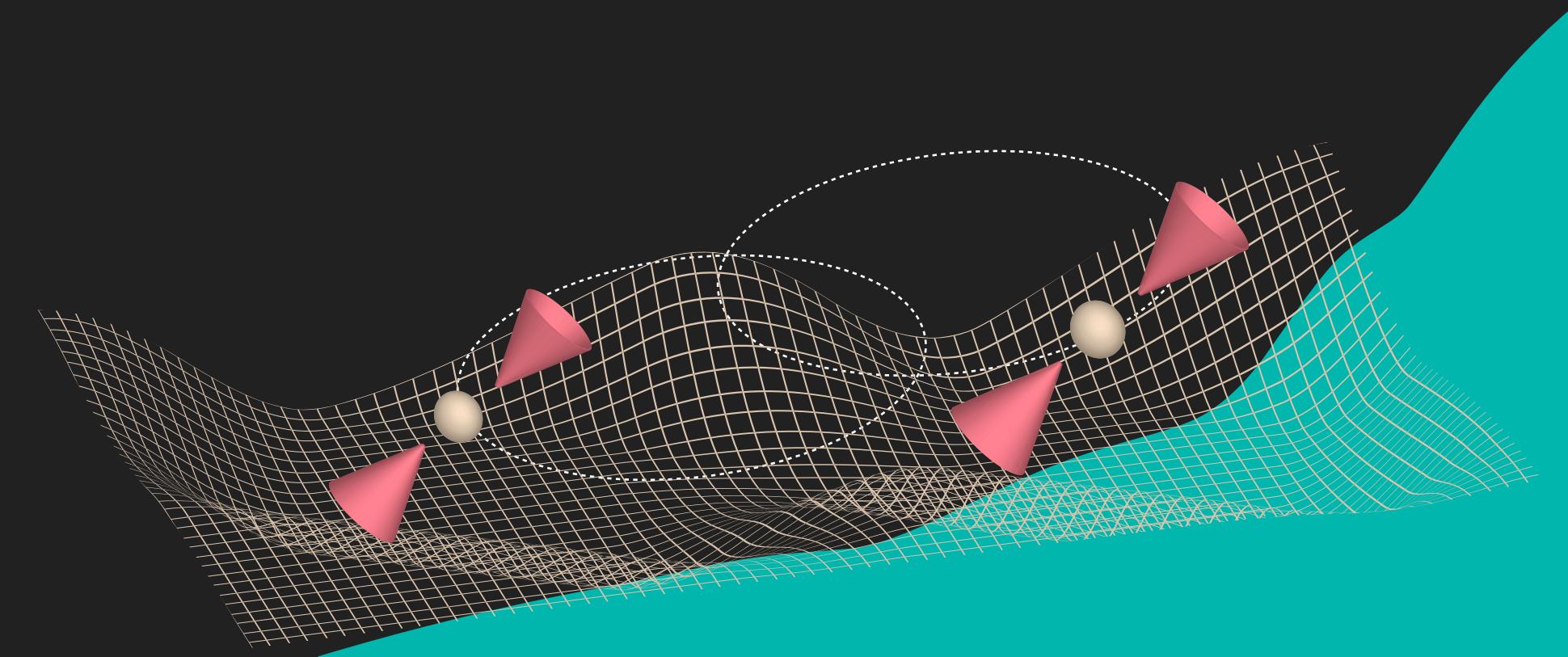


N PK parameters = N-2 tests of the theory

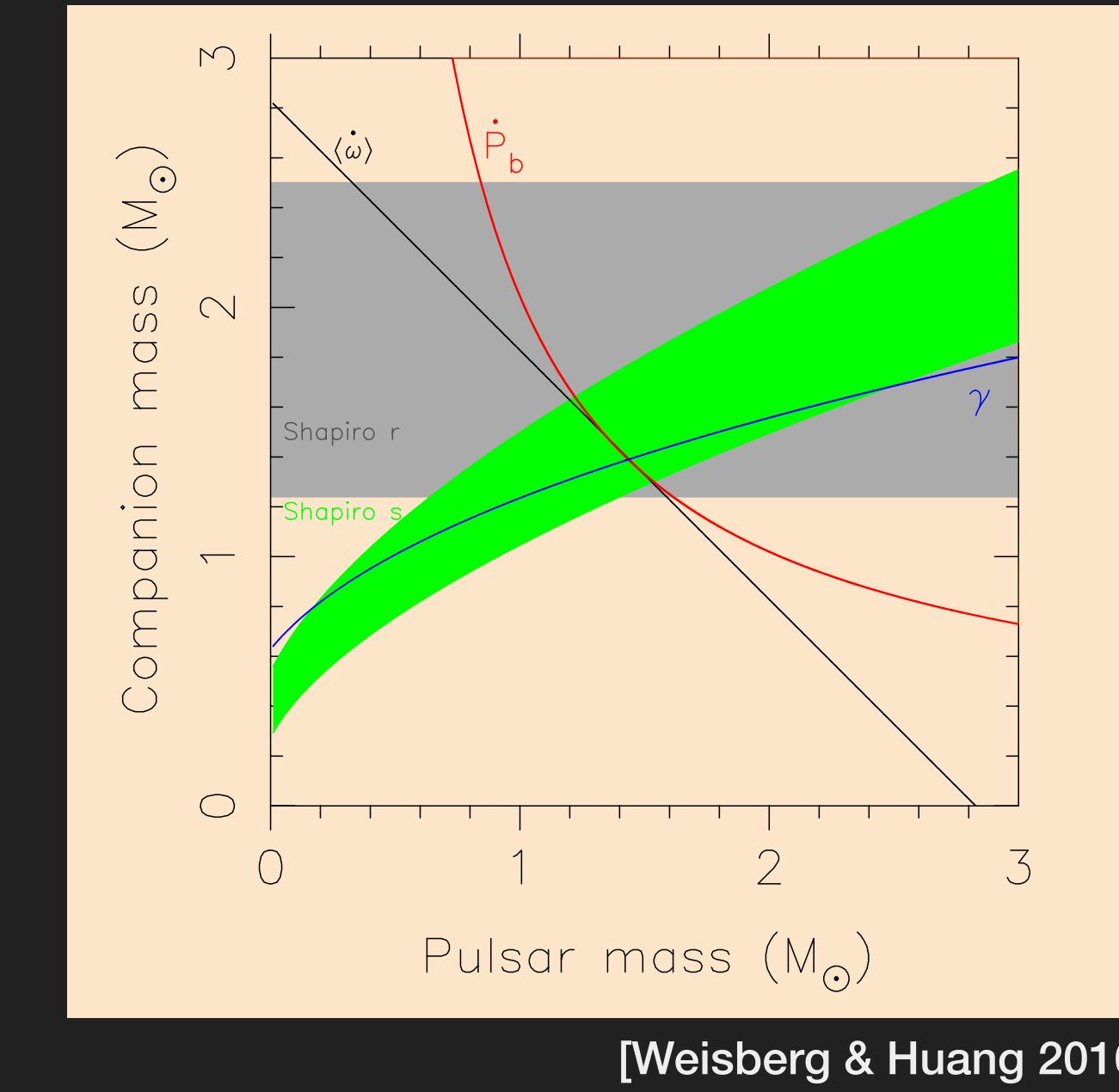
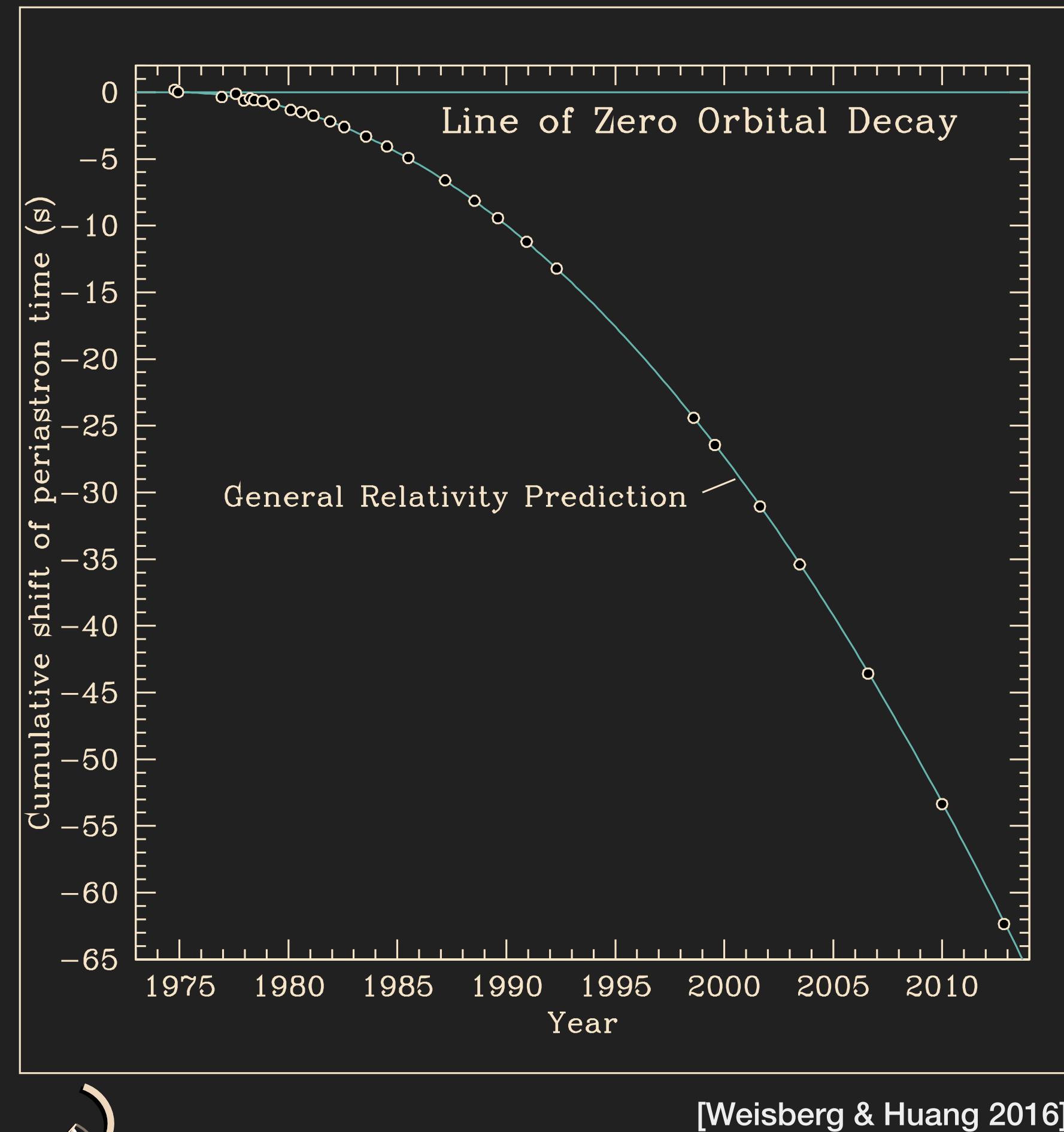
$$\dot{\omega} = 3 \left(\frac{G^{2/3}}{c^2} \right) \left(\frac{P_b}{2\pi} \right)^{-5/3} \frac{(m_p + m_c)^{2/3}}{1 - e^2}$$

$$\gamma = \left(\frac{G^{2/3}}{c^2} \right) \left(\frac{P_b}{2\pi} \right)^{1/3} e m_p (m_p + 2m_c) (m_p + 2m_c)^{-4/3}$$

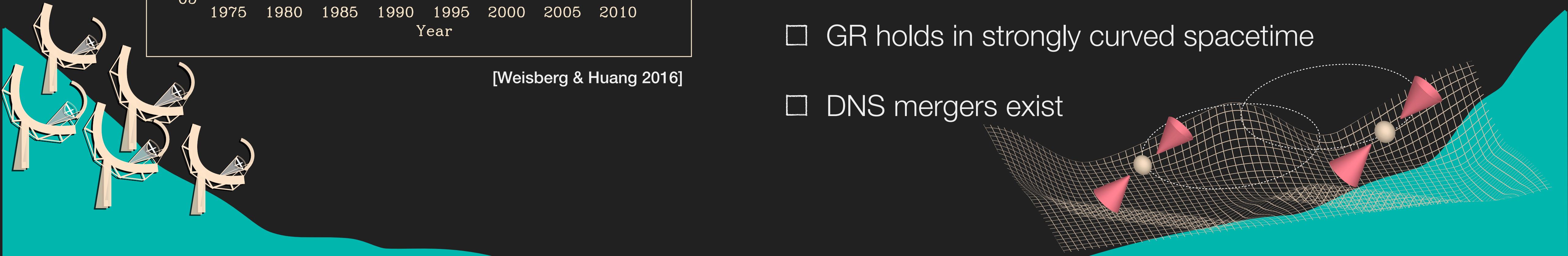
$$\dot{P}_b = - \frac{192\pi G^{5/3}}{5c^5} \left(\frac{P_b}{2\pi} \right)^{5/3} \frac{(1 + 73e^2/24 + 37e^4/96)}{(1 - e^2)^{7/2}} m_p m_c (m_p + m_c)^{-1/3}$$



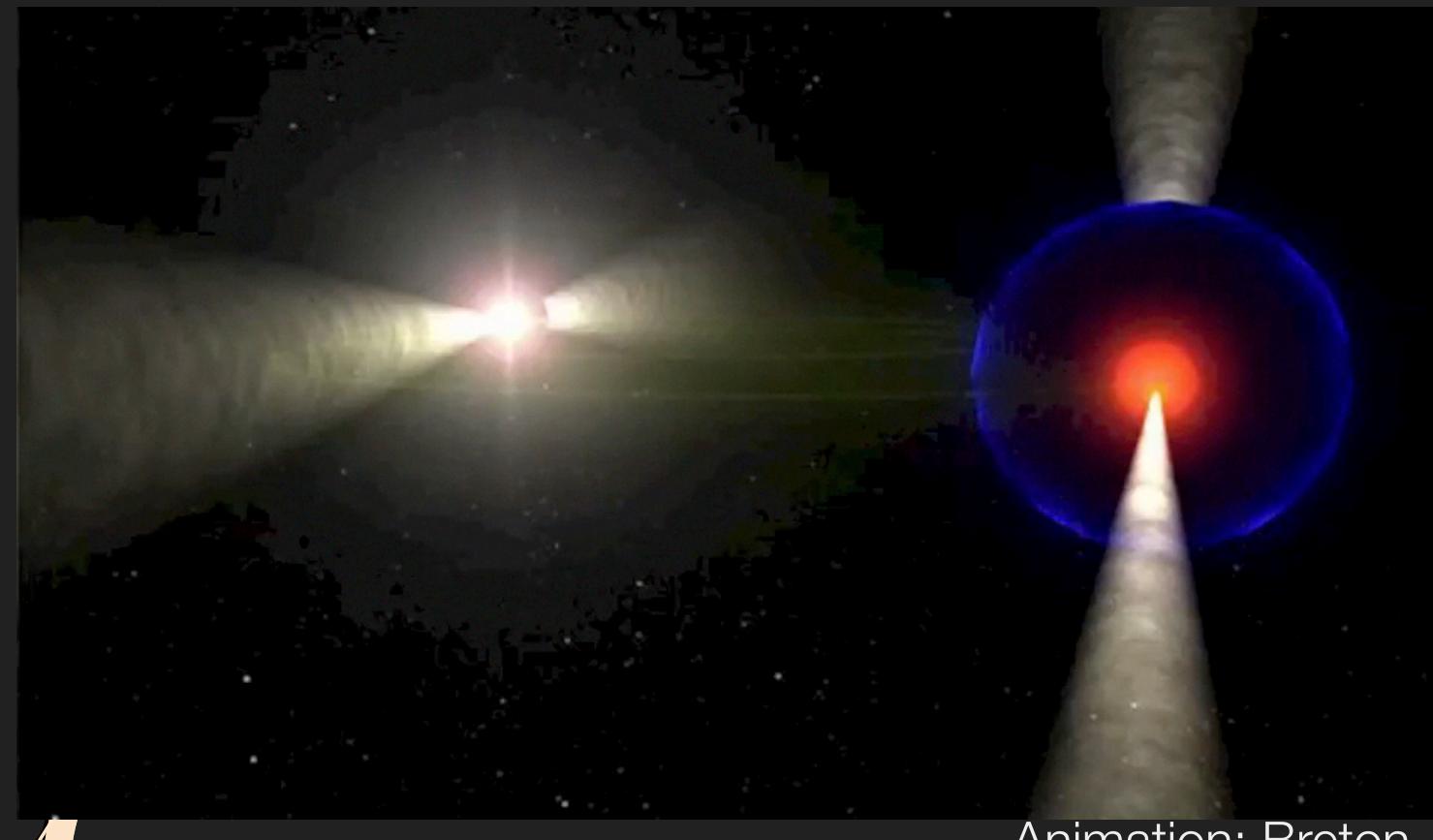
The Hulse-Taylor pulsar: PSR B1913+16



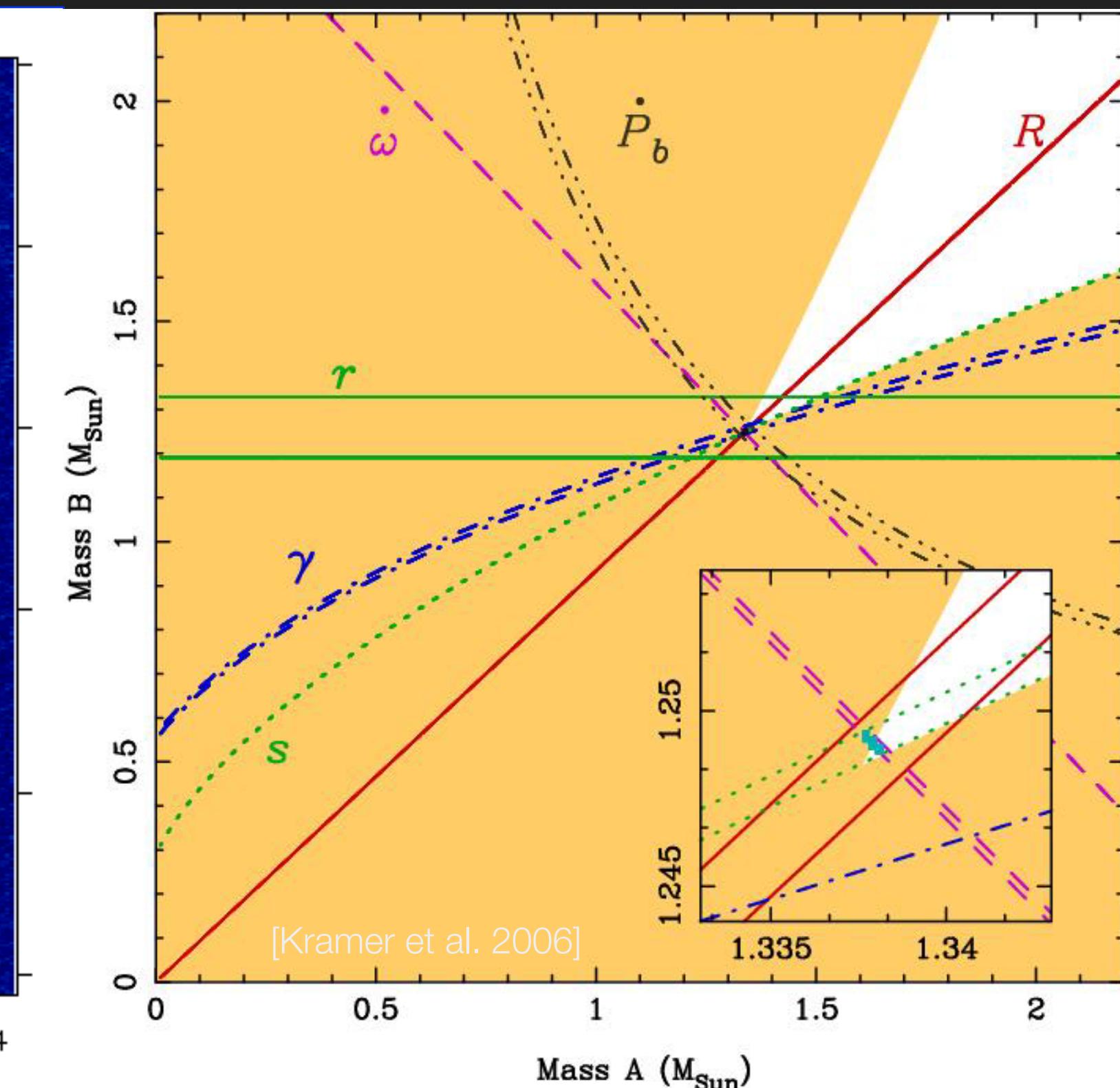
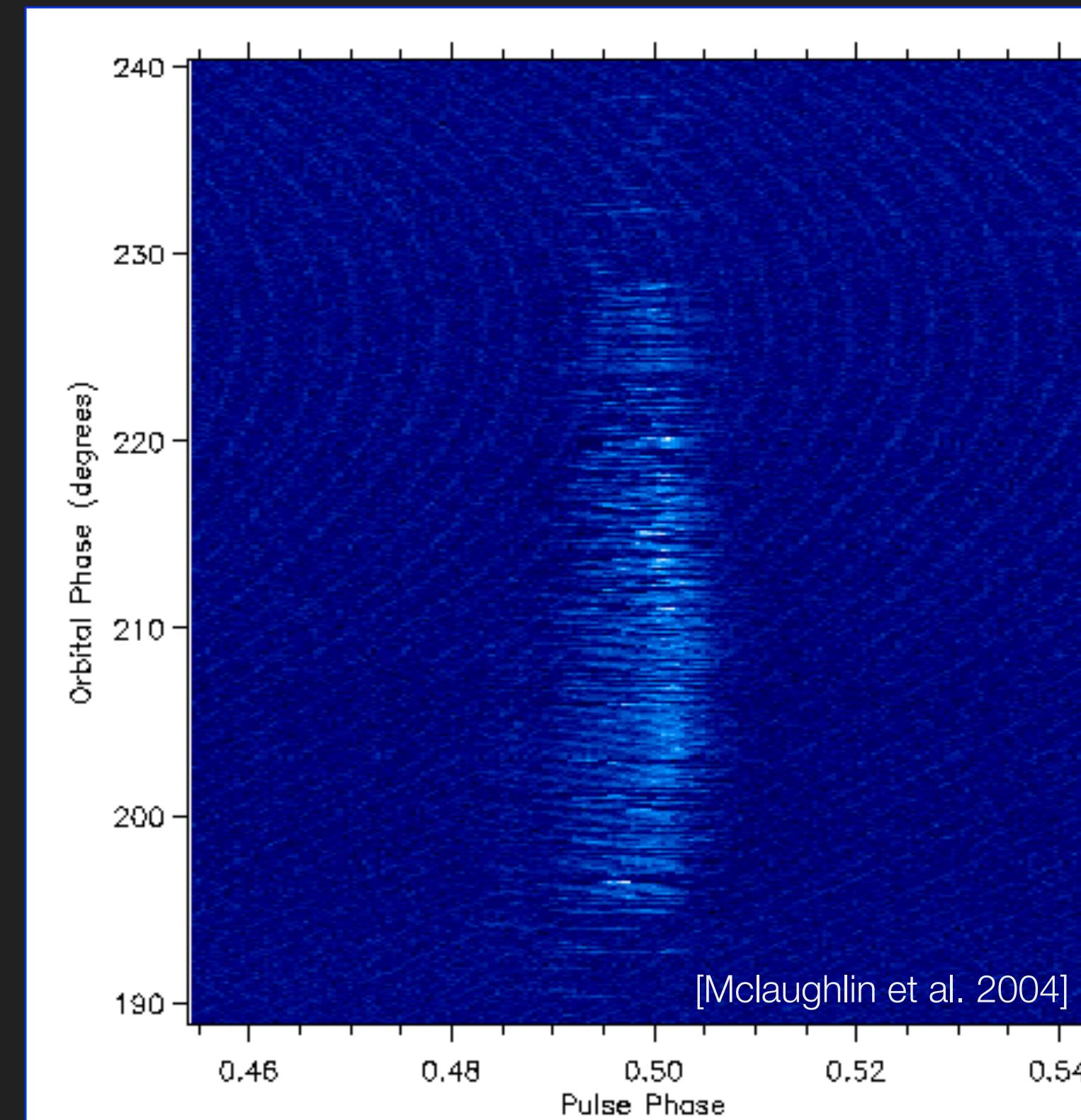
- Gravitational waves exist with energy loss predicted by GR
- GR holds in strongly curved spacetime
- DNS mergers exist



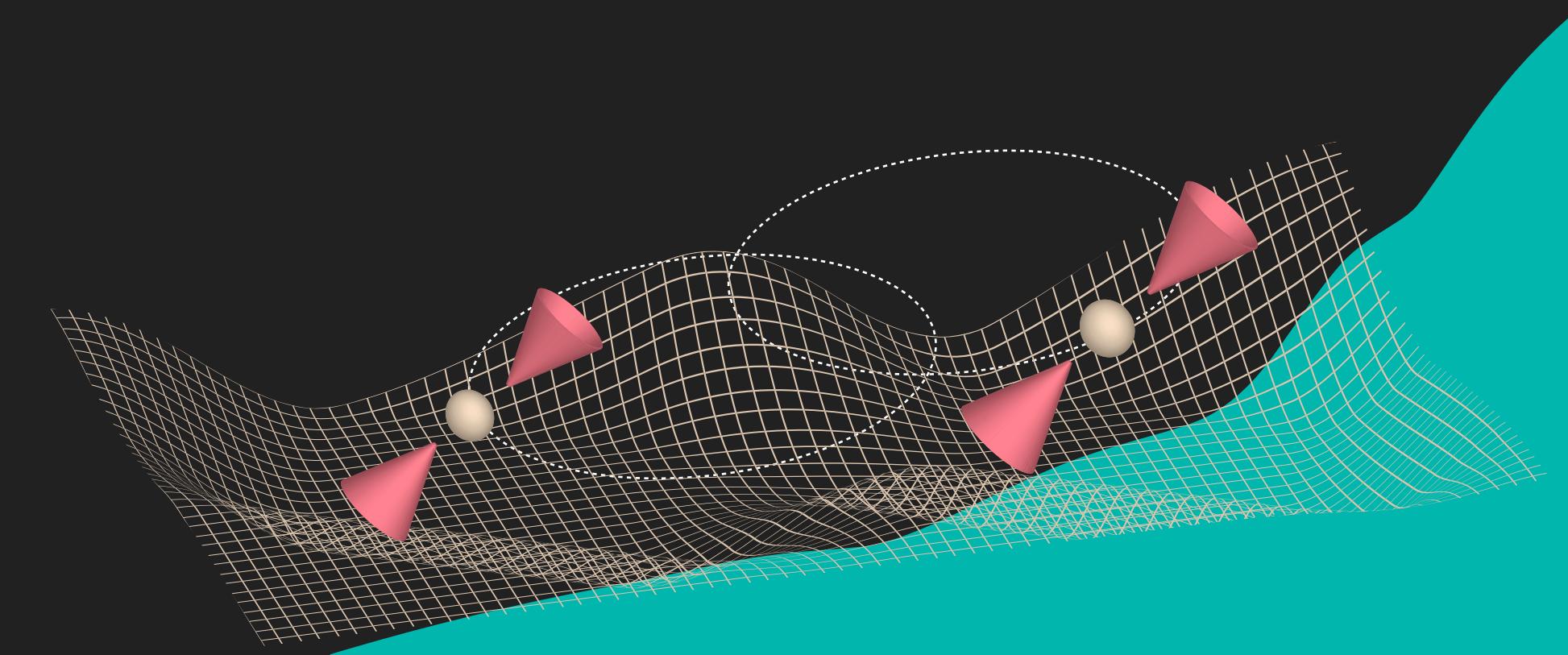
The double pulsar



Animation: Breton



Spin periods: 23 ms / 2.8 s
Orbital period: 2.45 h
Eccentricity: 0.088



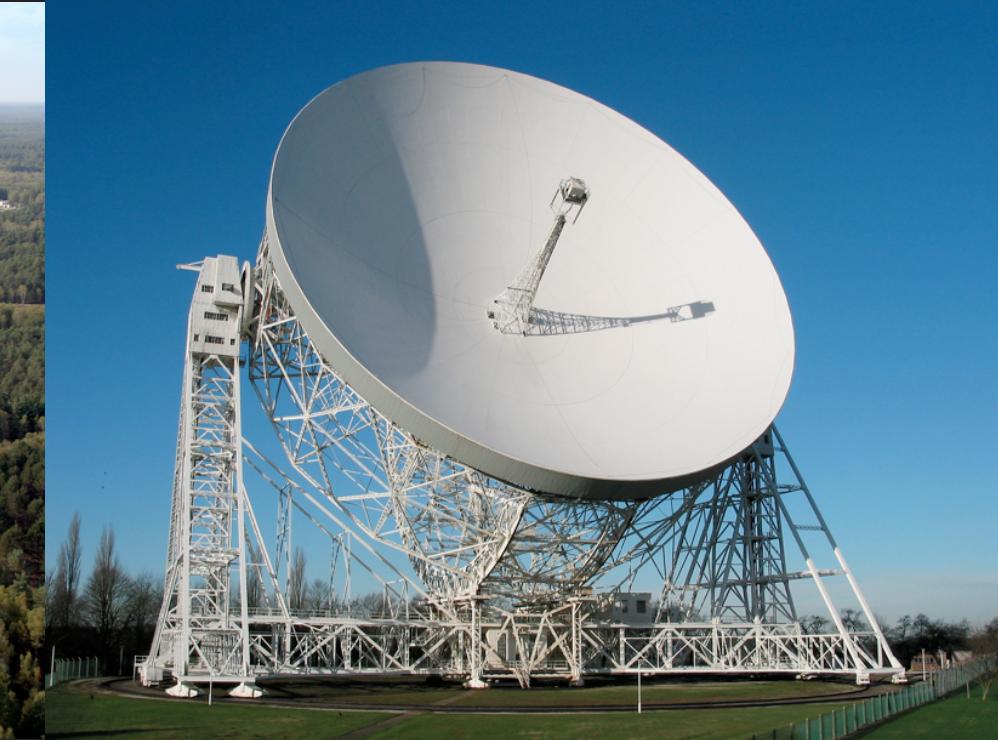
The double pulsar: until now



Green Bank
Telescope, USA



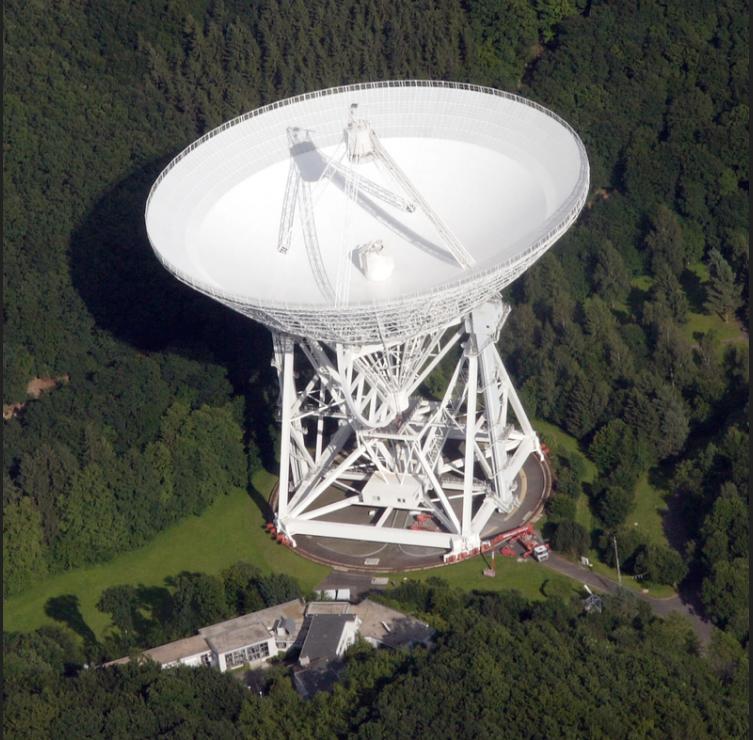
Nançay Radio
Telescope, France



Lovell telescope, UK

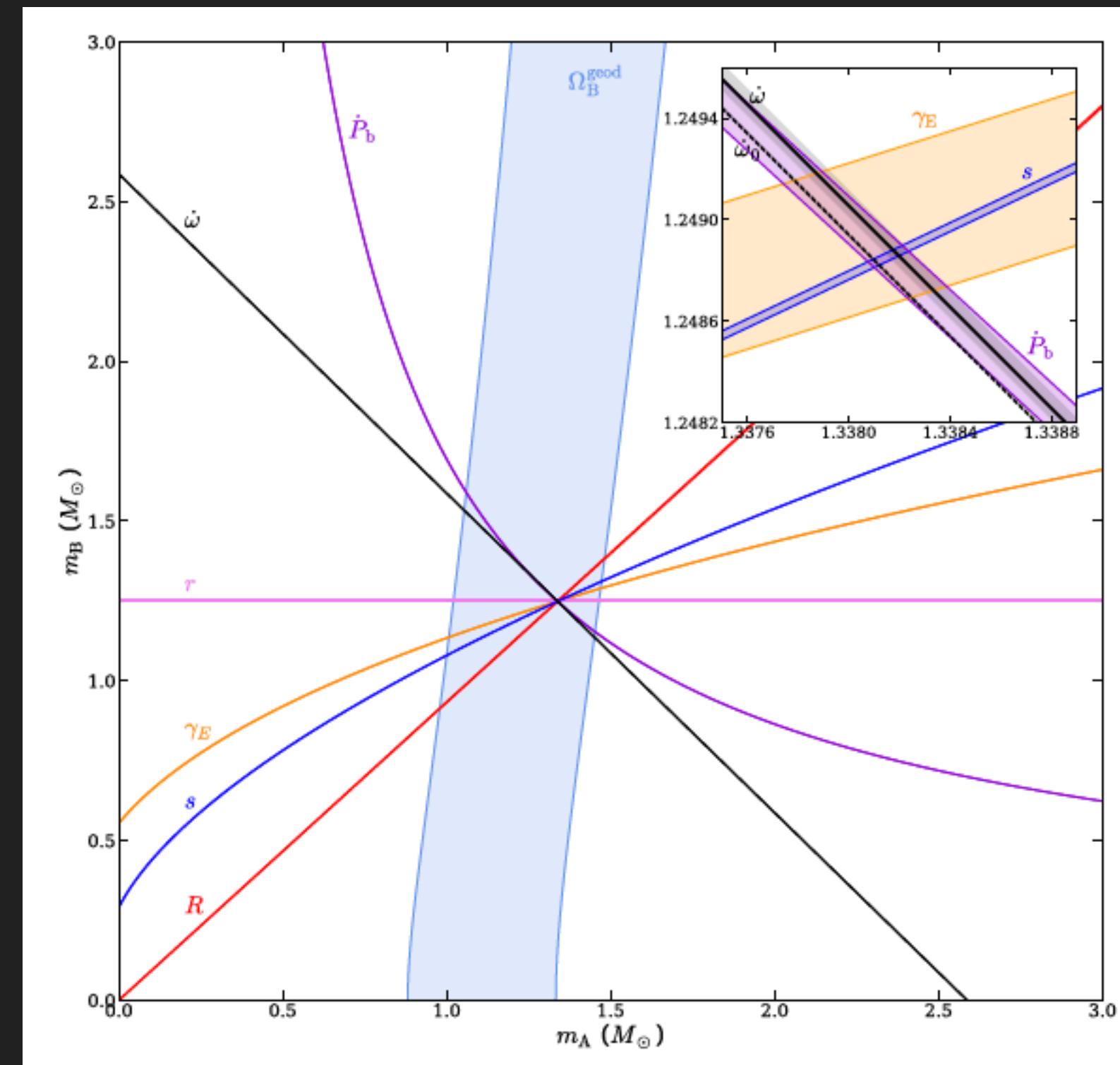


Parkes Radio Telescope,
Australia



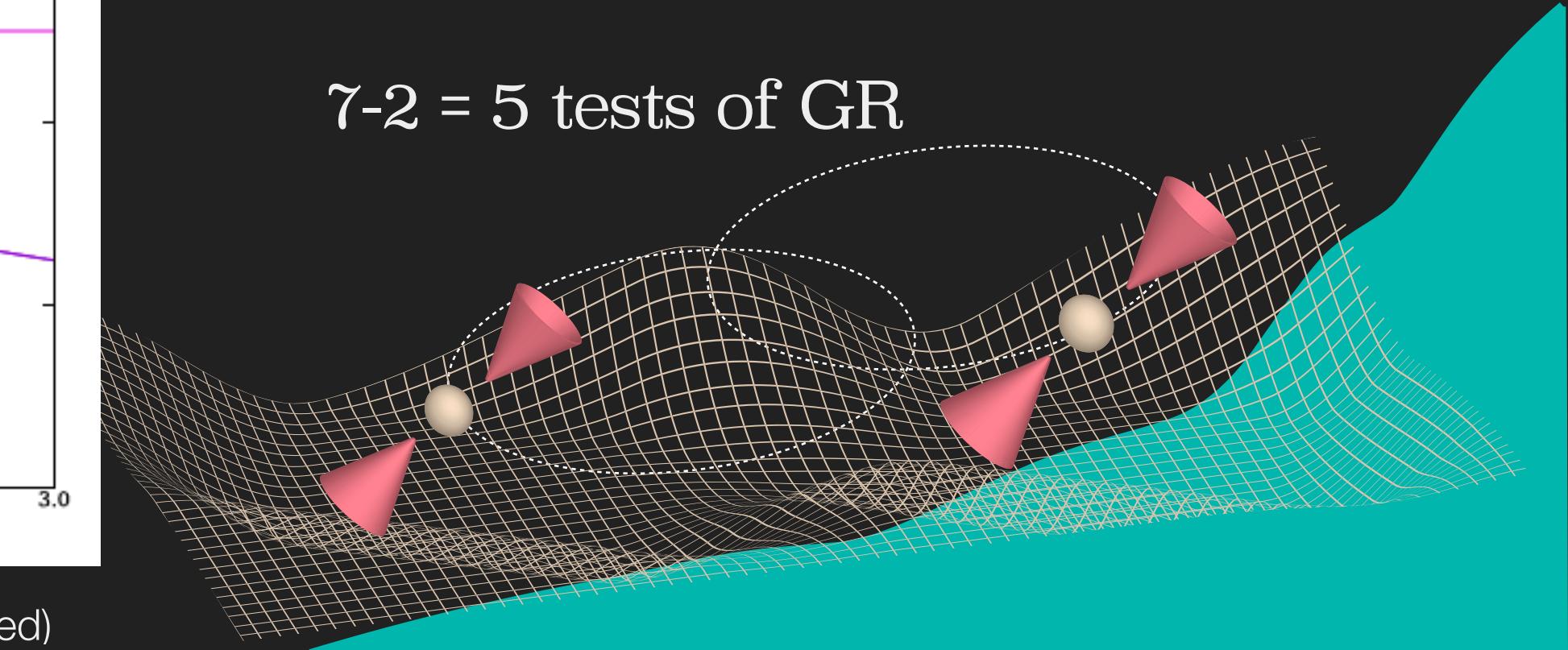
100-m Effelsberg telescope,
Germany

1 million arrival time
estimates over 16 years

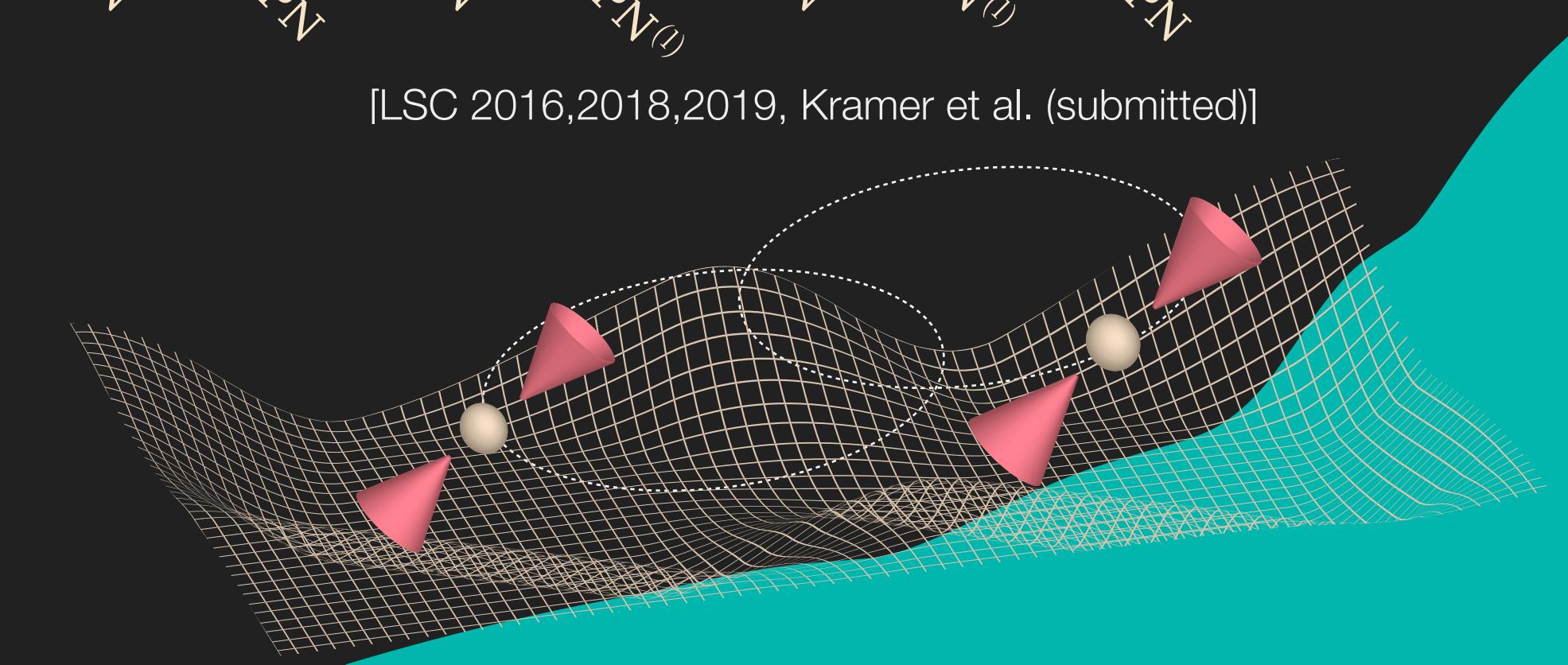
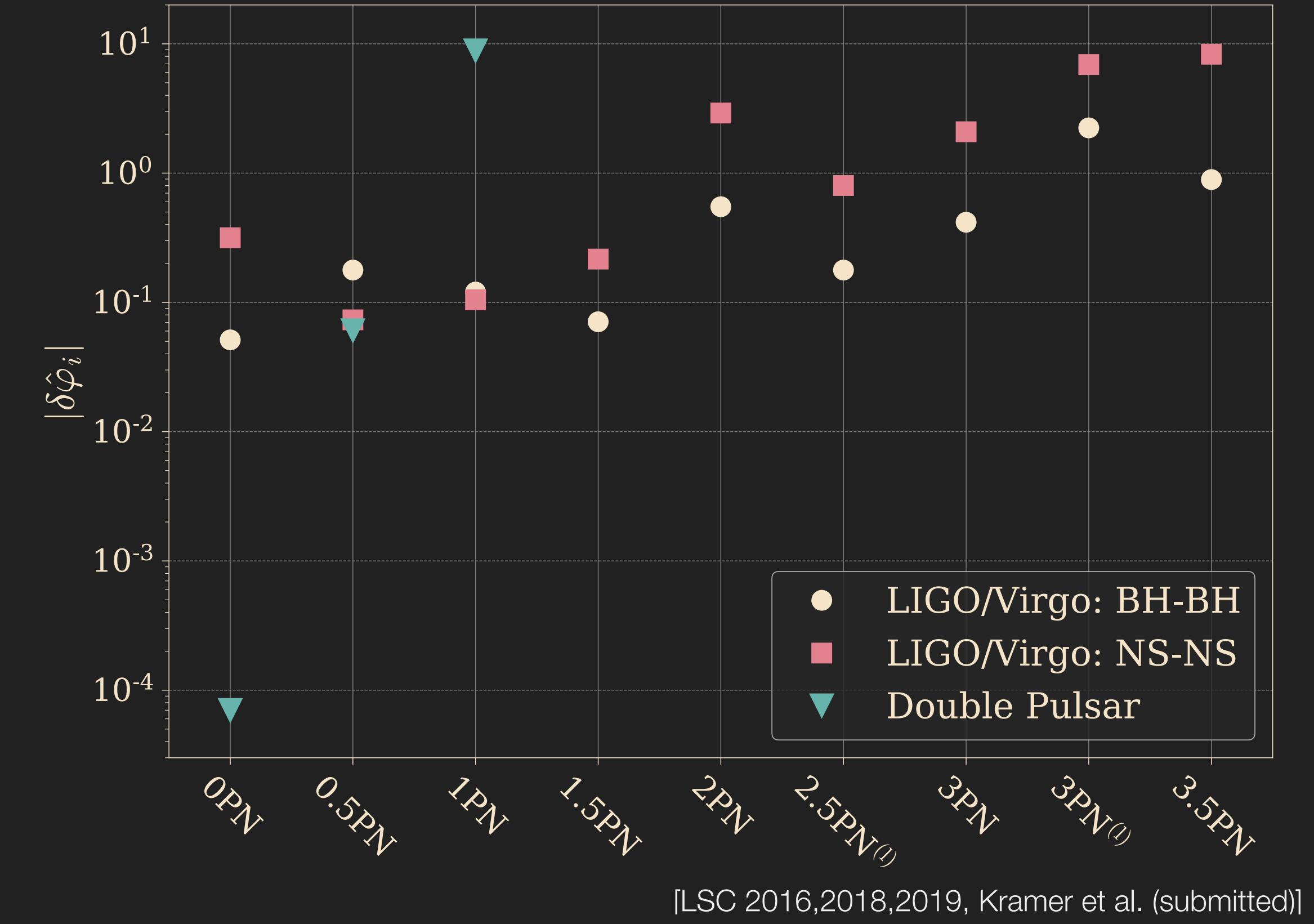
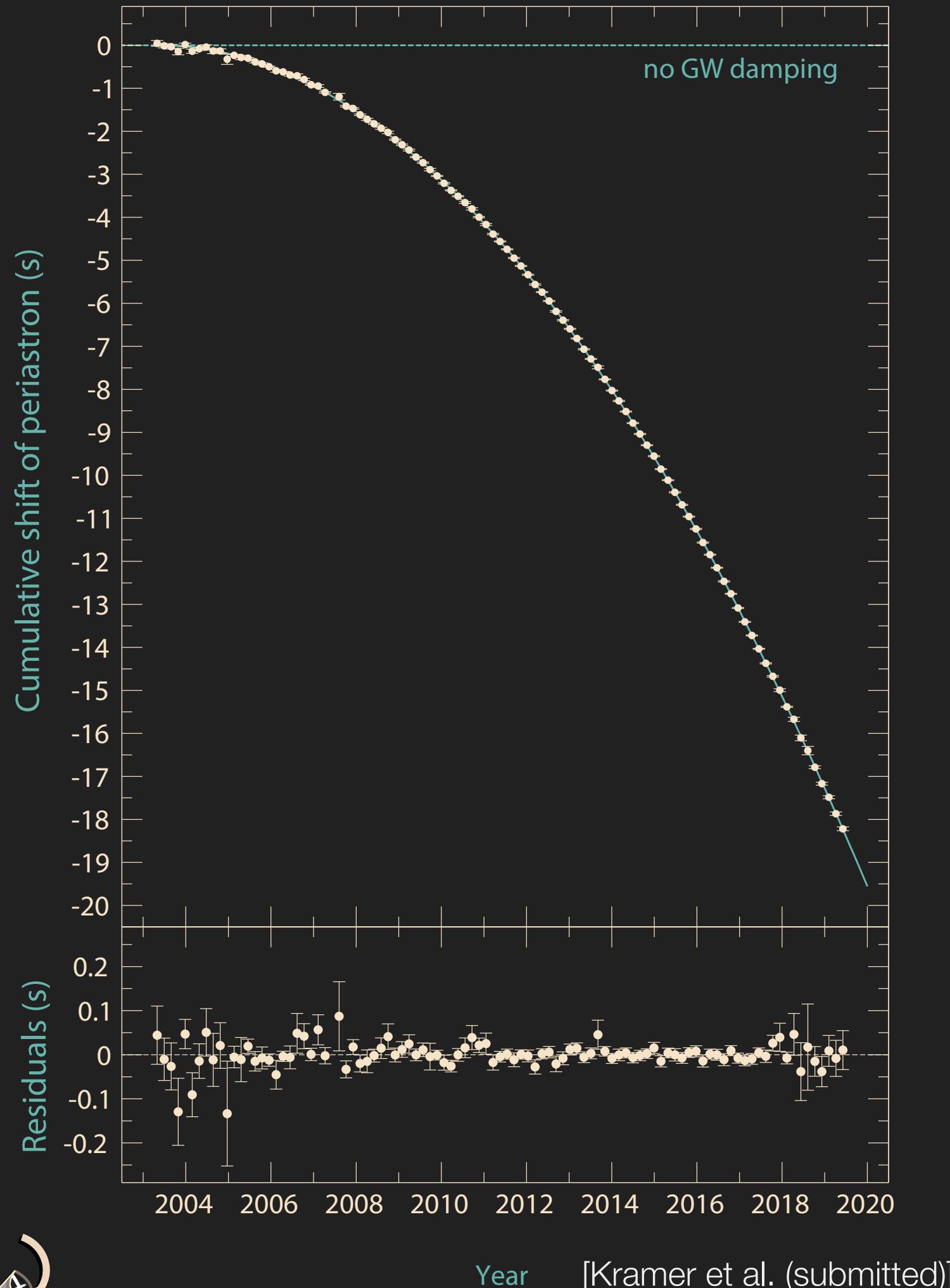


$$m_p = 1.33818(1)M_\odot$$
$$m_c = 1.24886(1)M_\odot$$

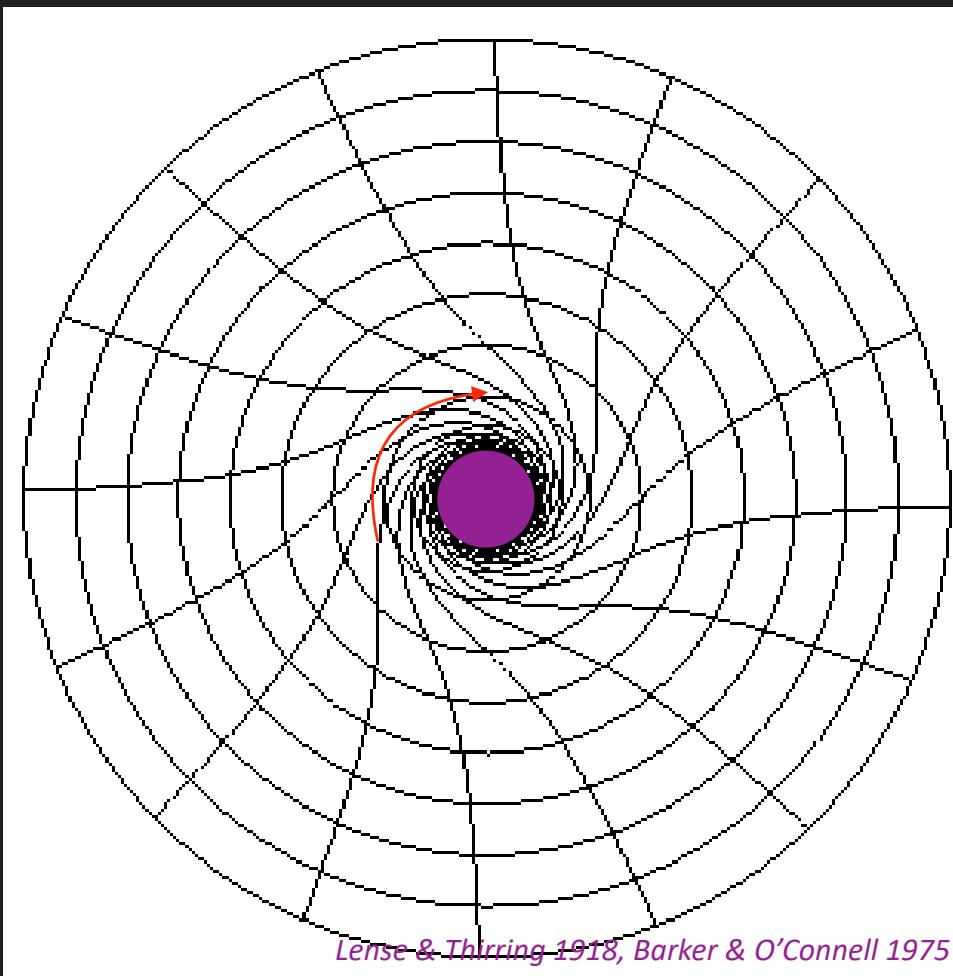
7-2 = 5 tests of GR



The double pulsar: gravitational wave damping

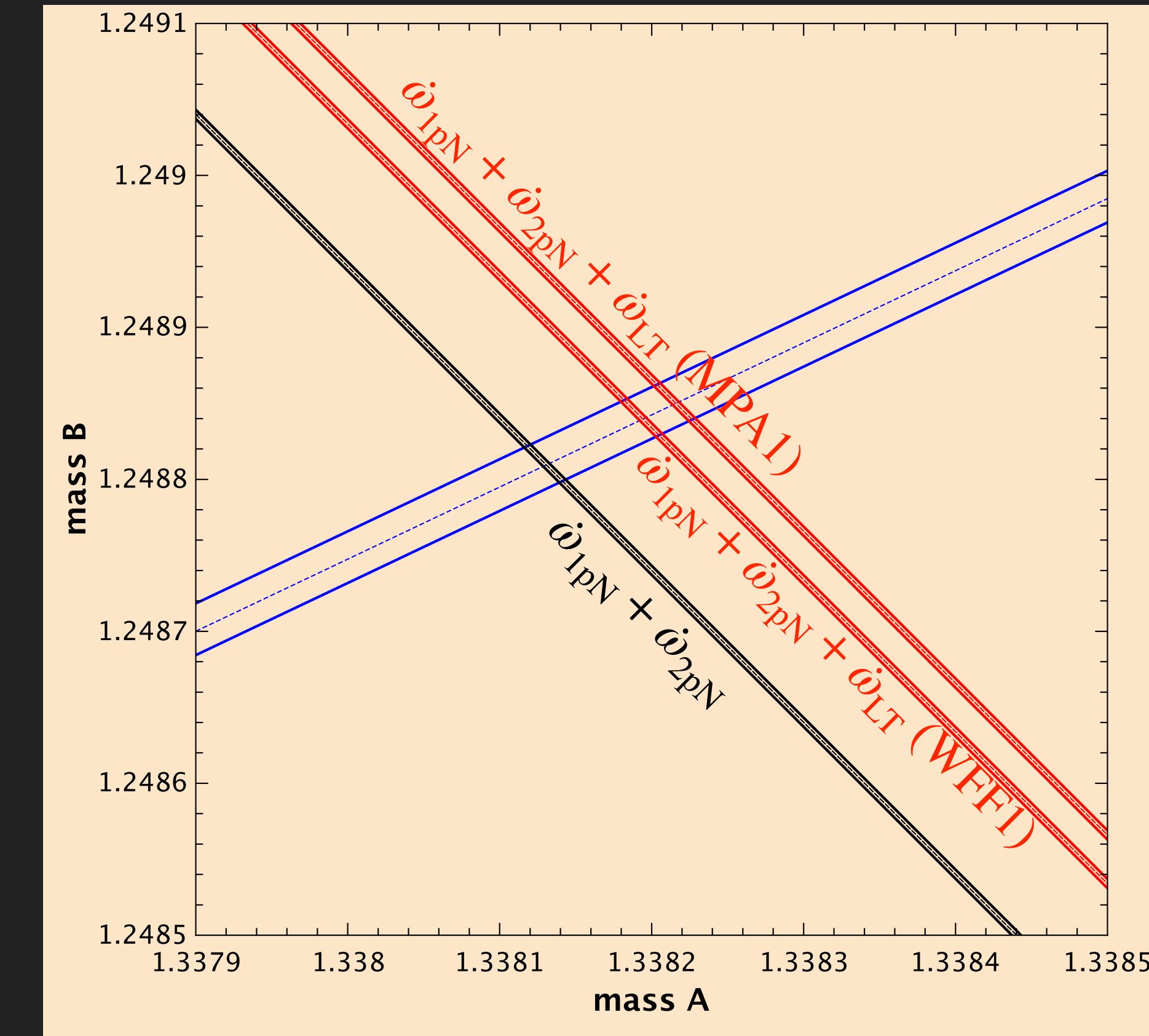


The double pulsar: LT precession?



$$\dot{\omega}_{\text{obs}} = \dot{\omega}_{1\text{PN}} + \dot{\omega}_{2\text{PN}} + \dot{\omega}_{\text{LT}}$$

$$\dot{\omega}_{\text{LT}} = - T_{\odot} \left(\frac{P_b}{2\pi} \right)^{-2} \frac{1}{(1-e^2)^{3/2}} \frac{4m_p + 3m_c}{m_p + m_c} \frac{c}{G} S^p$$

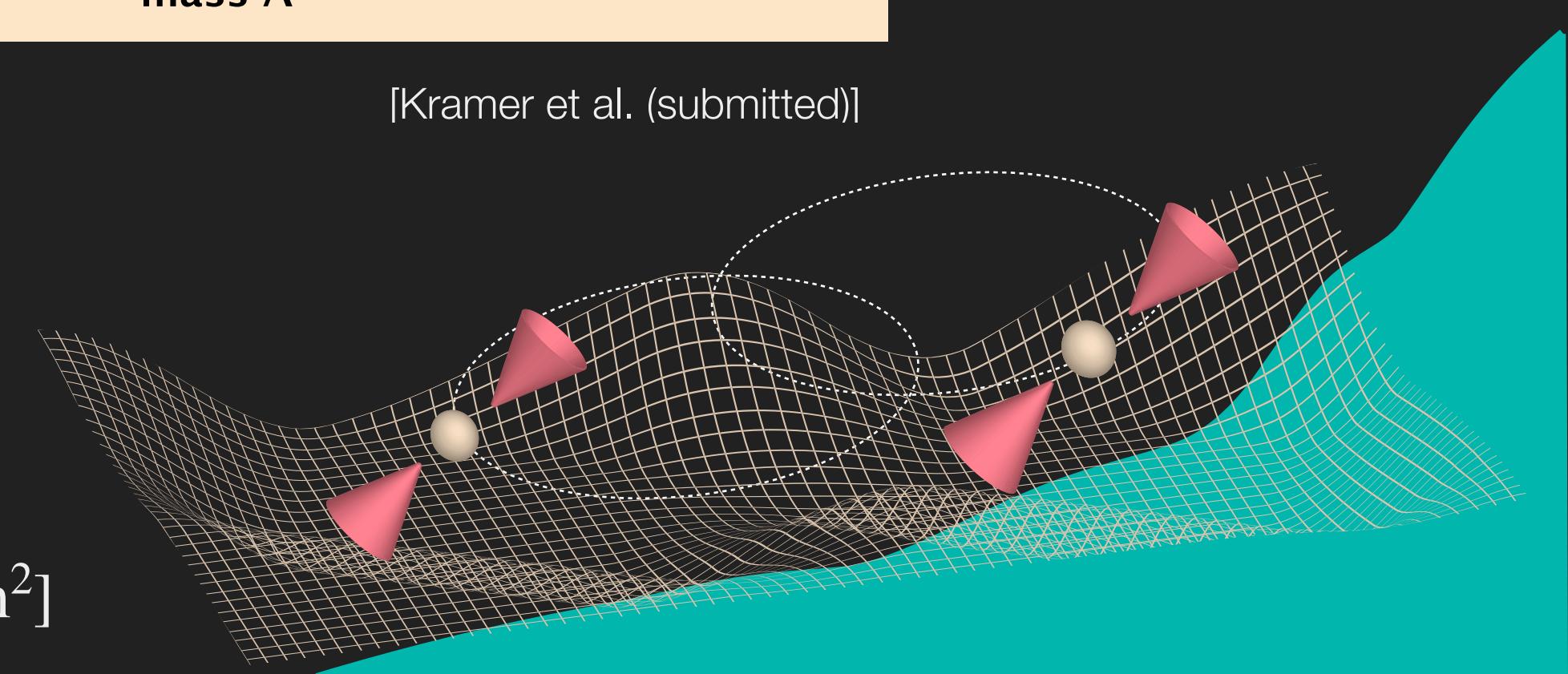


[Kramer et al. (submitted)]

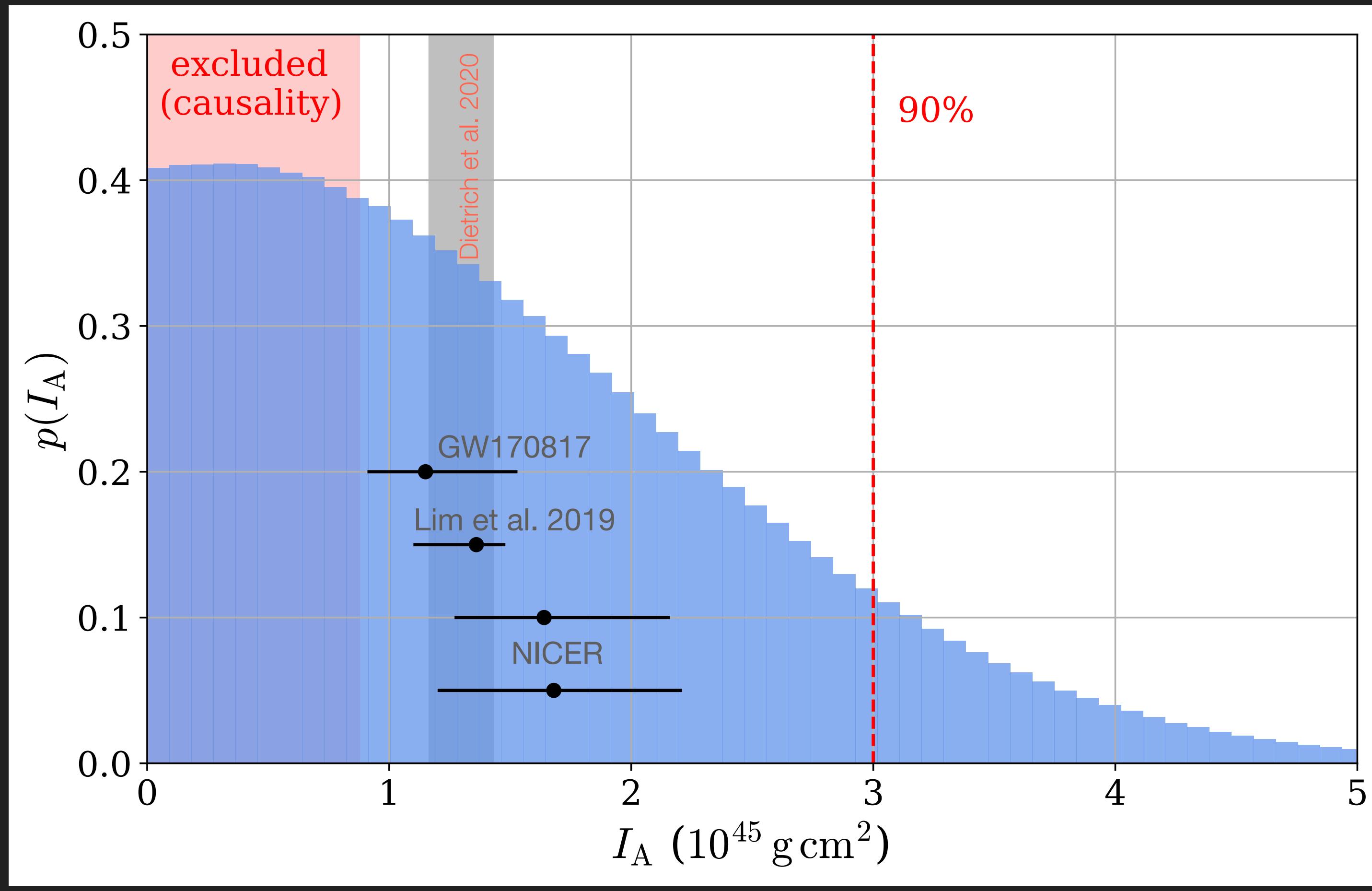
$$\dot{\omega}_{\text{obs}}[\text{deg/yr}] = 16.899317(13)$$

$$\dot{\omega}_{2\text{PN}}[\text{deg/yr}] = 0.000439$$

$$\dot{\omega}_{\text{LT}}[\text{deg/yr}] = - 0.000377 \times I_A [10^{45} \text{ g cm}^2]$$

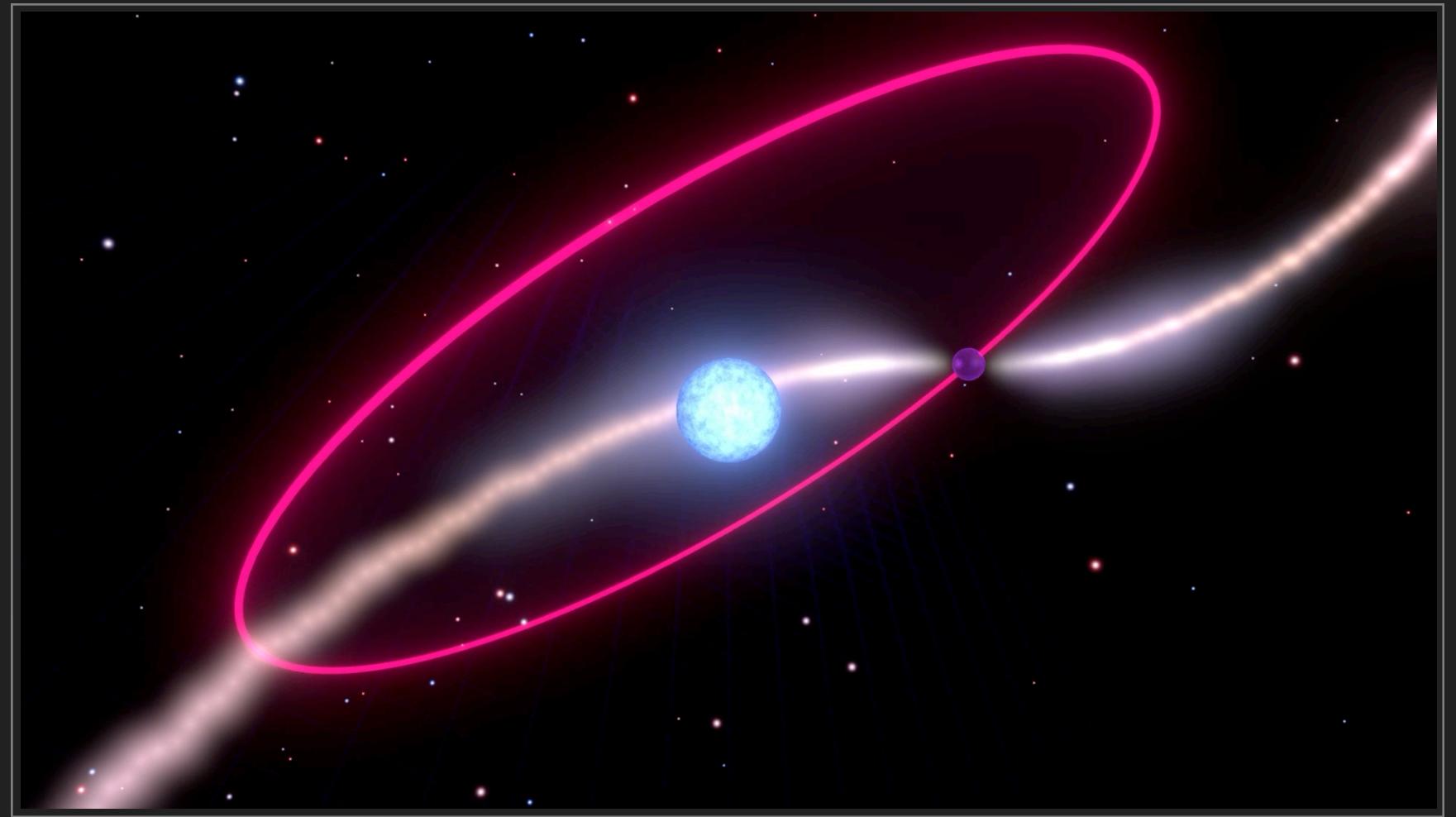


Constraints on MoI

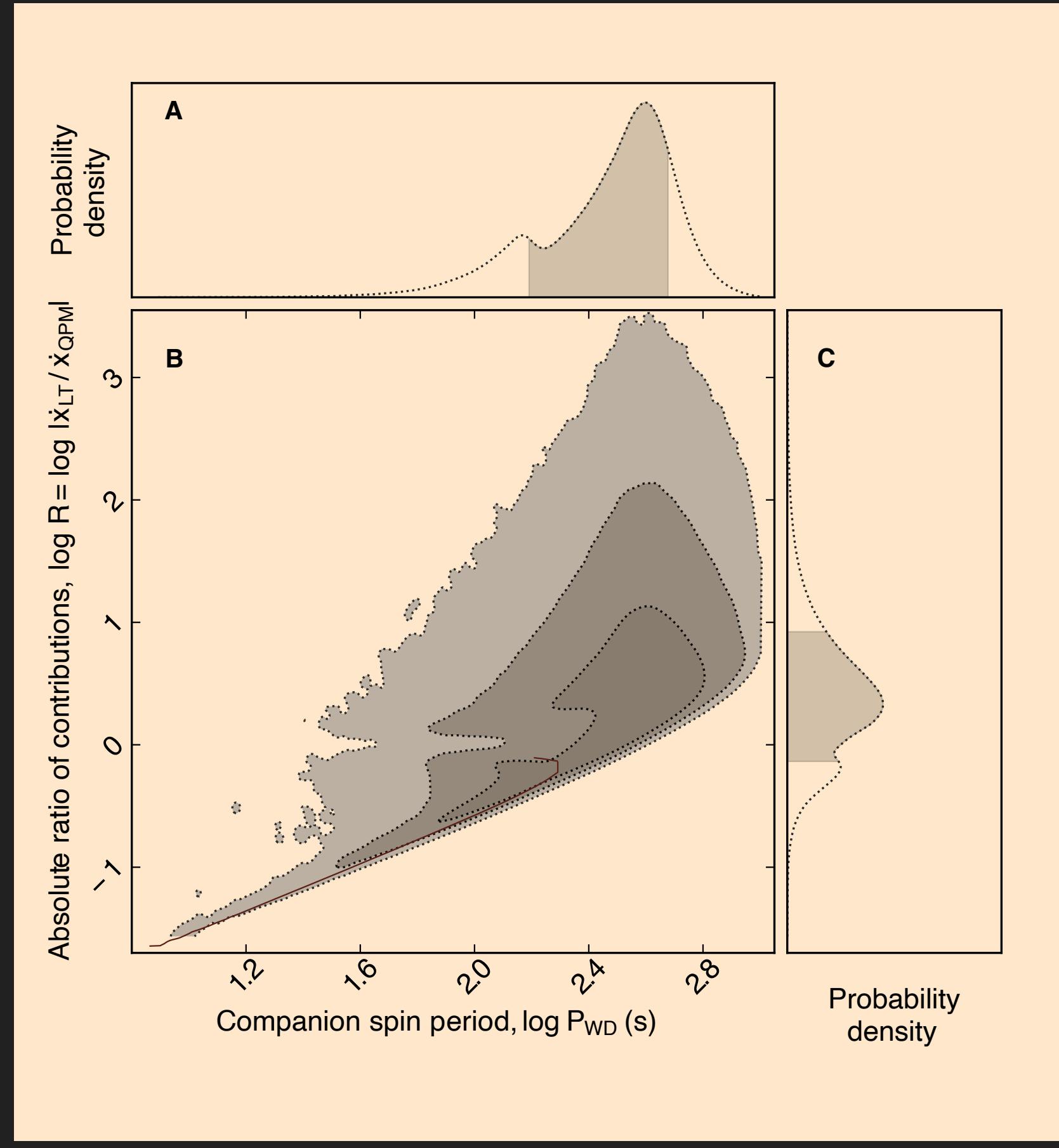


Check Hu et al. 2020 for predictions

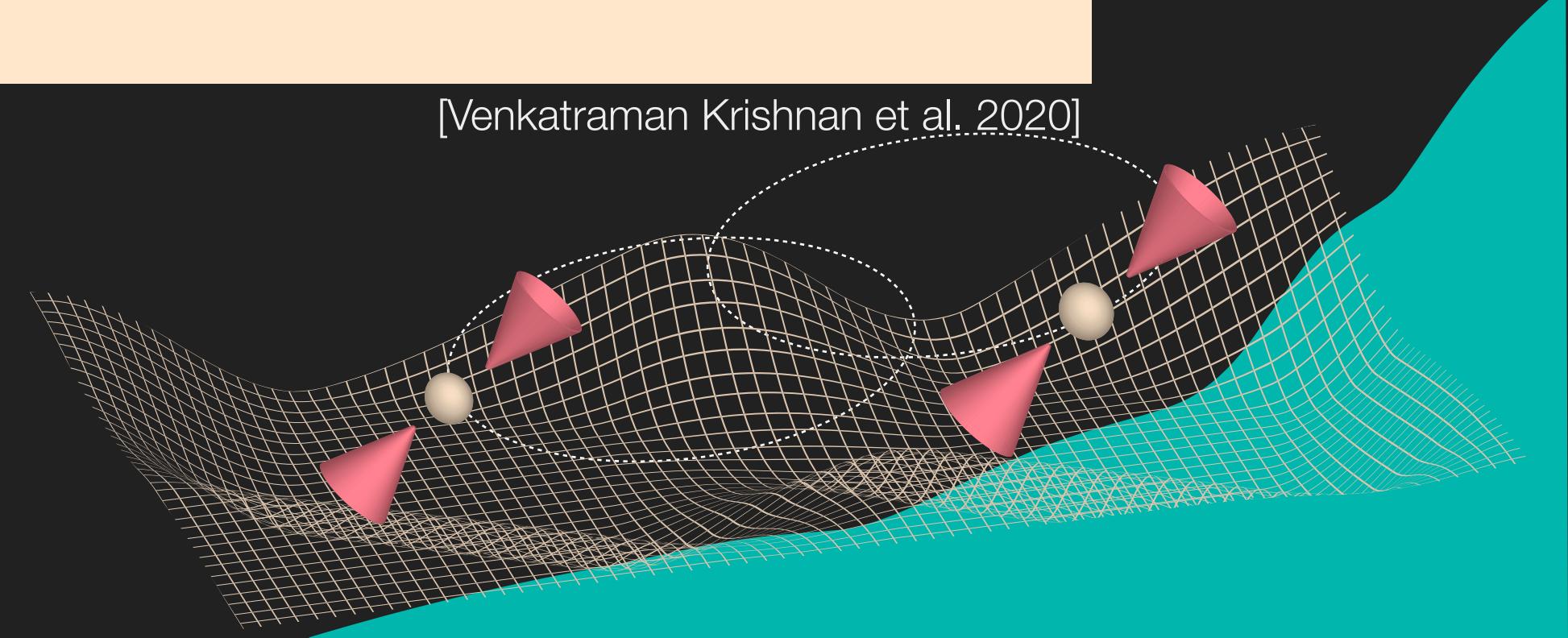
J1141-6545



- Pulsar-WD system with a young pulsar - 394ms spin period in a 4.74-hr orbit
- Peculiar binary evolution
- LT precession makes the orbit tumble: 1.7" per year
- Use LT precession as a tool to infer the spin-period of the WD



[Venkatraman Krishnan et al. 2020]



Tests of alternative theories of gravity: DEF gravity

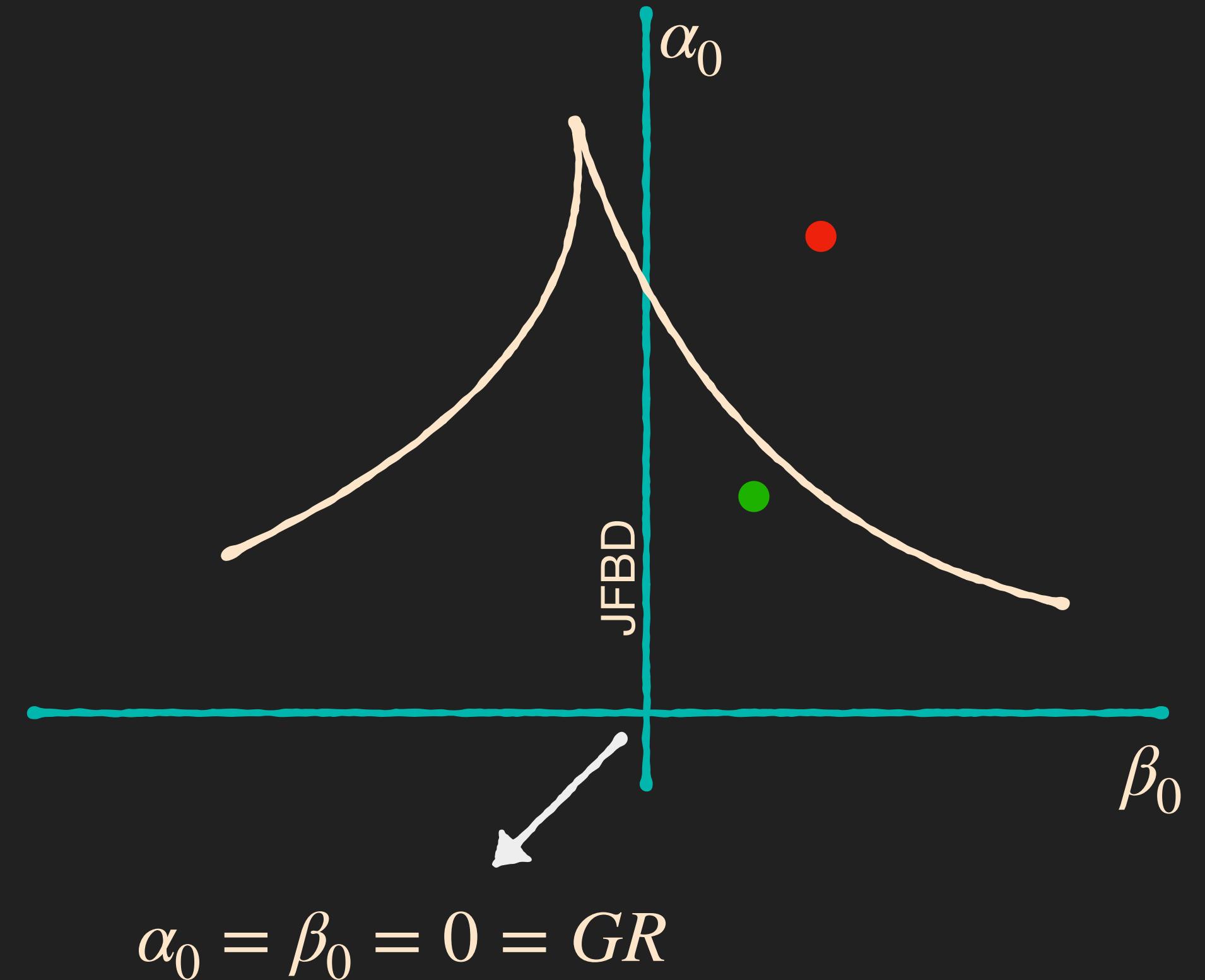
[Damour & Esposito Farésé 1992,1993,1996,1998]

- DEF gravity:
- Scalar-tensor theory of gravity
- Gravity is mediated by a scalar φ in addition to the Einstein metric $g_{\mu\nu}$
- Natural extension of GR, generalisation of JFBD theory

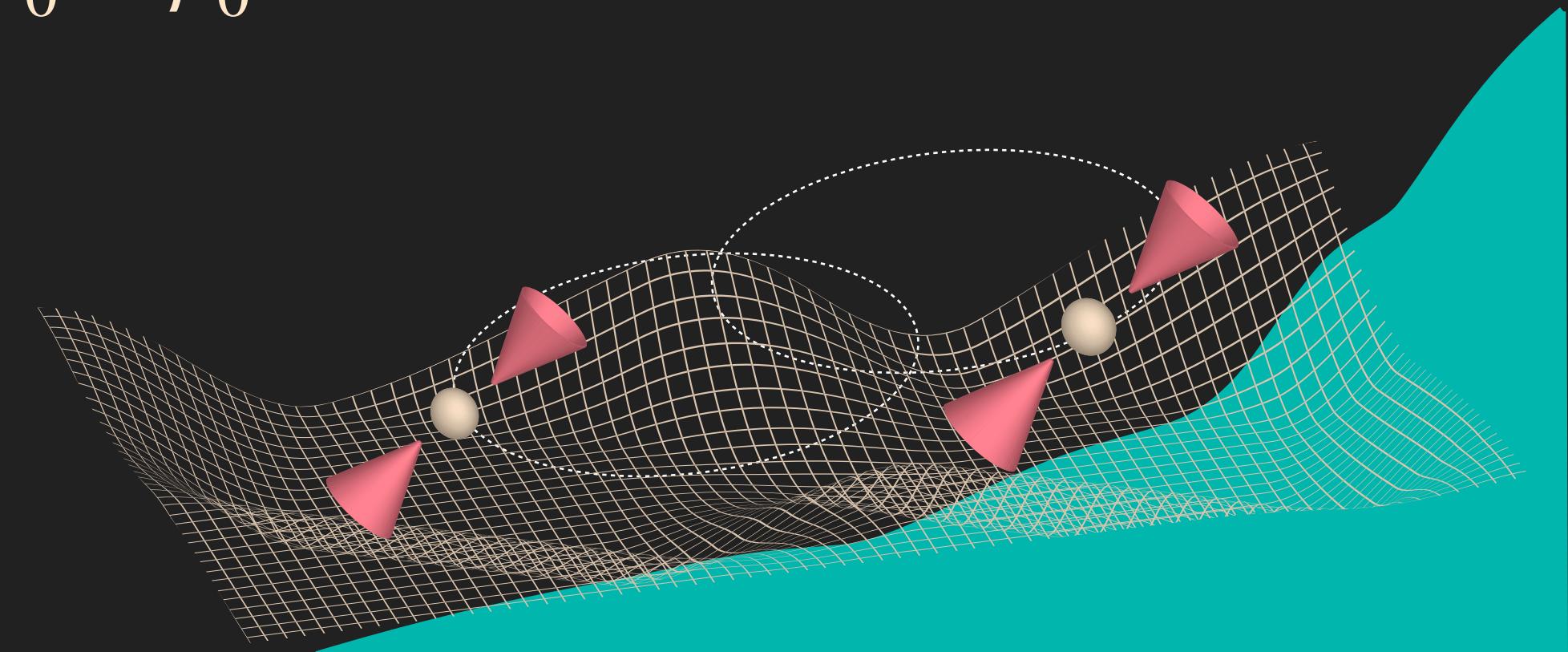
$$\tilde{g}_{\mu\nu} \equiv A(\varphi)^2 g_{\mu\nu}; \quad A(\varphi) \equiv \exp\left(\frac{1}{2}\beta\varphi^2\right)$$

$$\alpha(\varphi) \equiv \frac{\partial \ln(A(\varphi))}{\partial \varphi} = \beta\varphi; \quad \beta(\varphi) \equiv \frac{\partial^2 \ln(A(\varphi))}{\partial \varphi^2} = \frac{\partial \alpha(\varphi)}{\partial \varphi}.$$

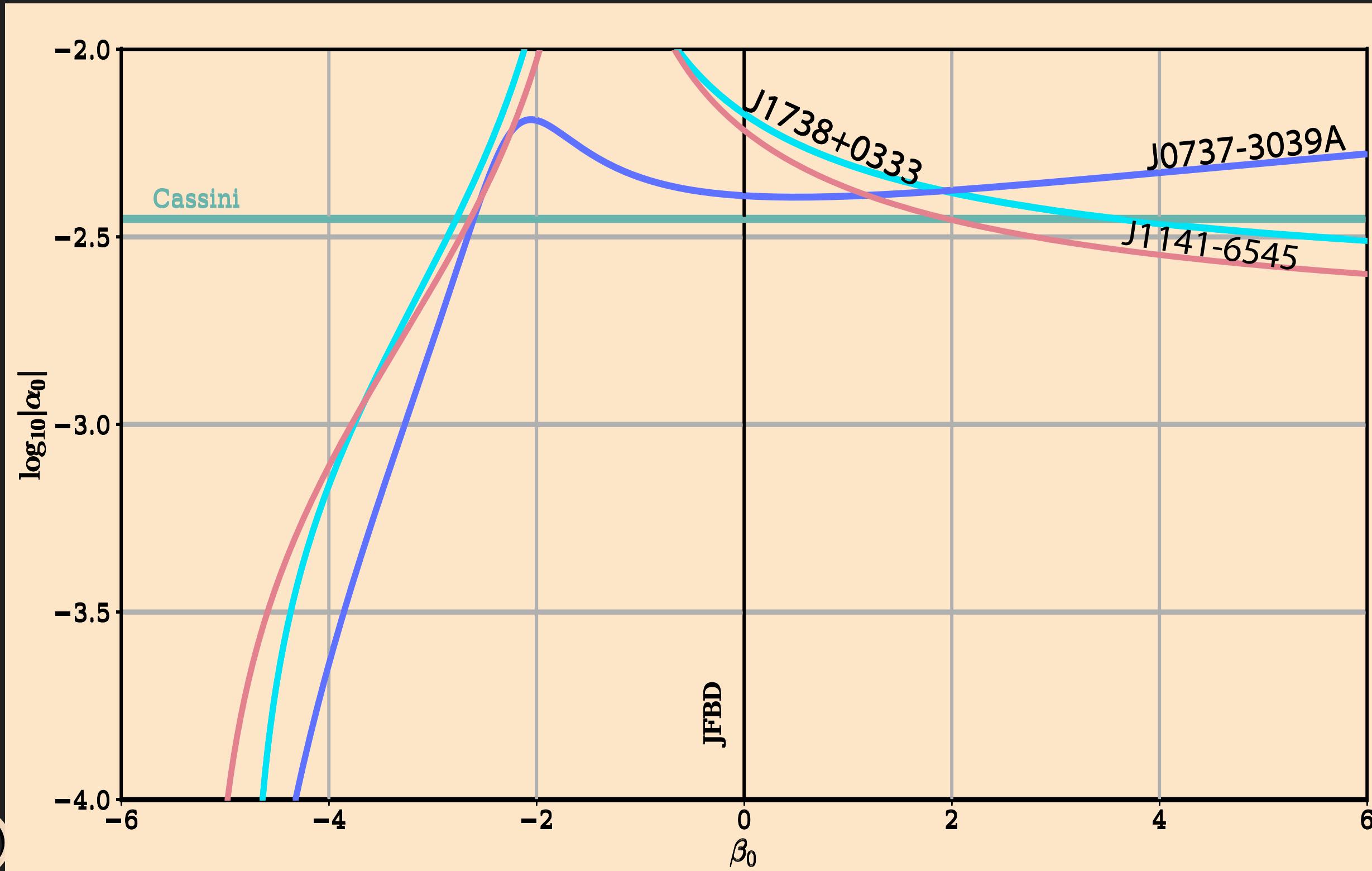
At infinity, $\varphi = \varphi_0$; $\Rightarrow \alpha = \alpha_0; \beta = \beta_0$.



$$\alpha_0 = \beta_0 = 0 = GR$$



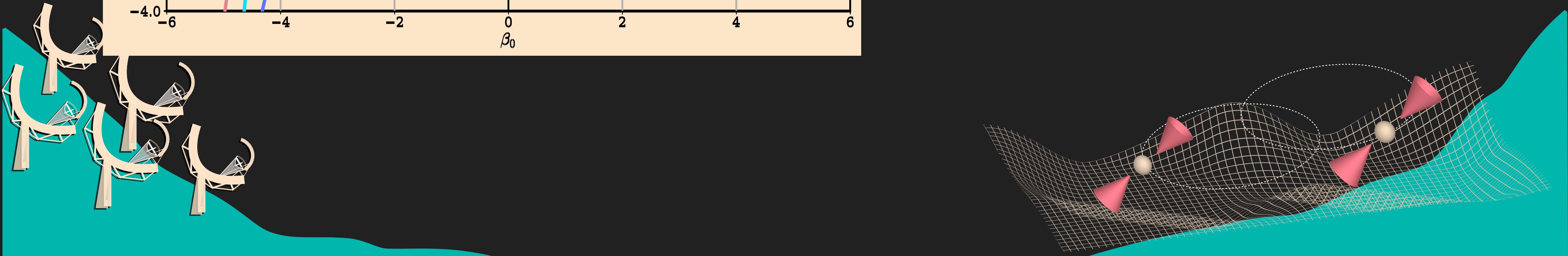
DEF gravity vs Pulsars



J1738+0333 - Freire et al. (2012)

J0737-3039A - Kramer et al. (submitted)

J1141-6545 - Batrakov et al. (in prep.)



Tests of universality of free fall

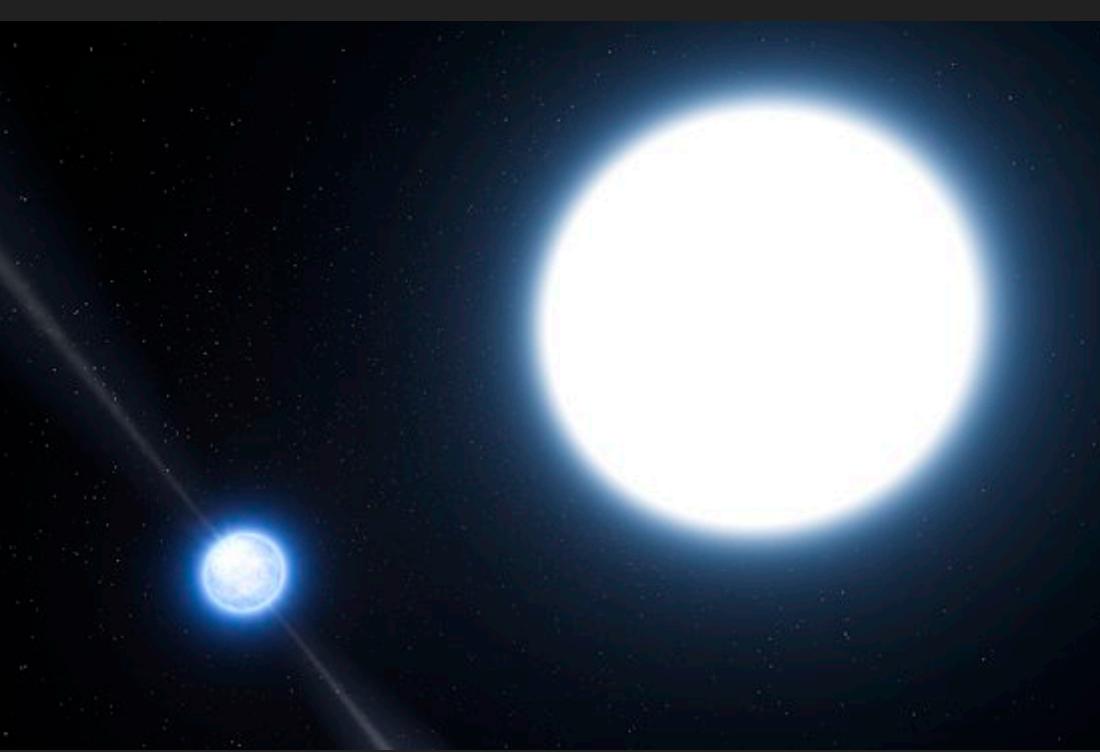
Weak equivalence
principle



Strong equivalence
principle



Weak field



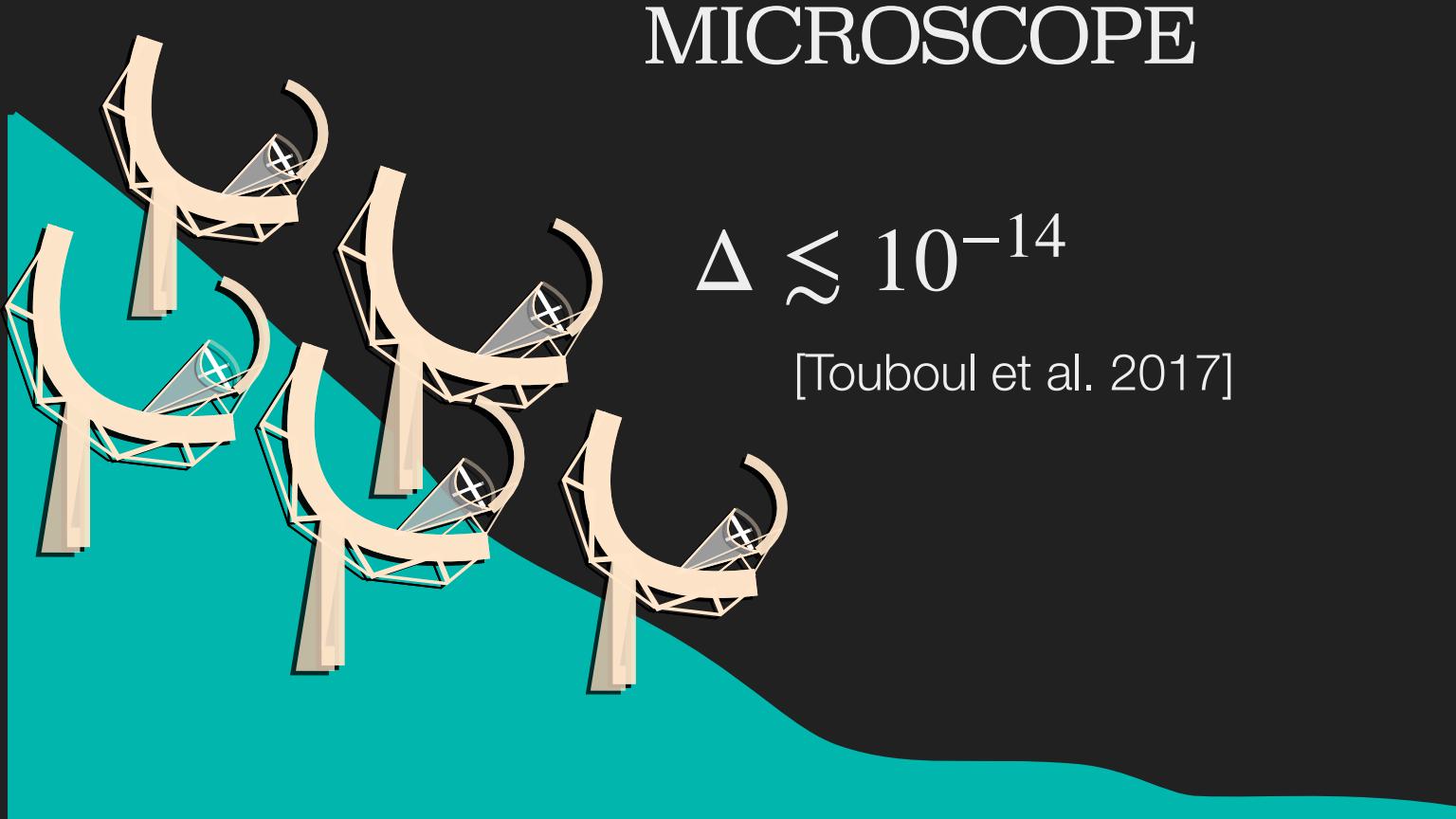
Strong field

$$E_{grav} = 0$$

MICROSCOPE

$$\Delta \lesssim 10^{-14}$$

[Touboul et al. 2017]



$$\epsilon \equiv \frac{E_{grav}}{mc^2} \simeq -5 \times 10^{-10}$$

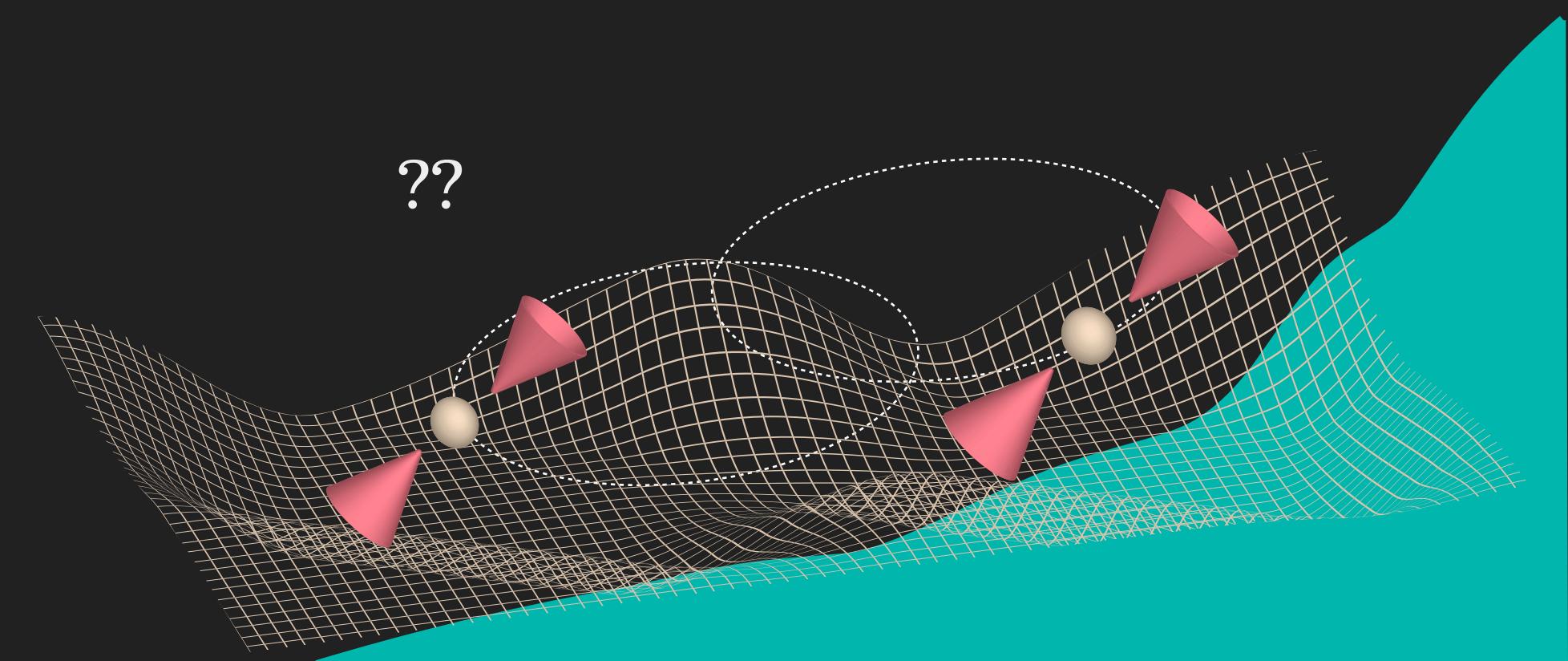
Lunar Laser Ranging

$$\Delta \lesssim 4 \times 10^{-4} |\epsilon|$$

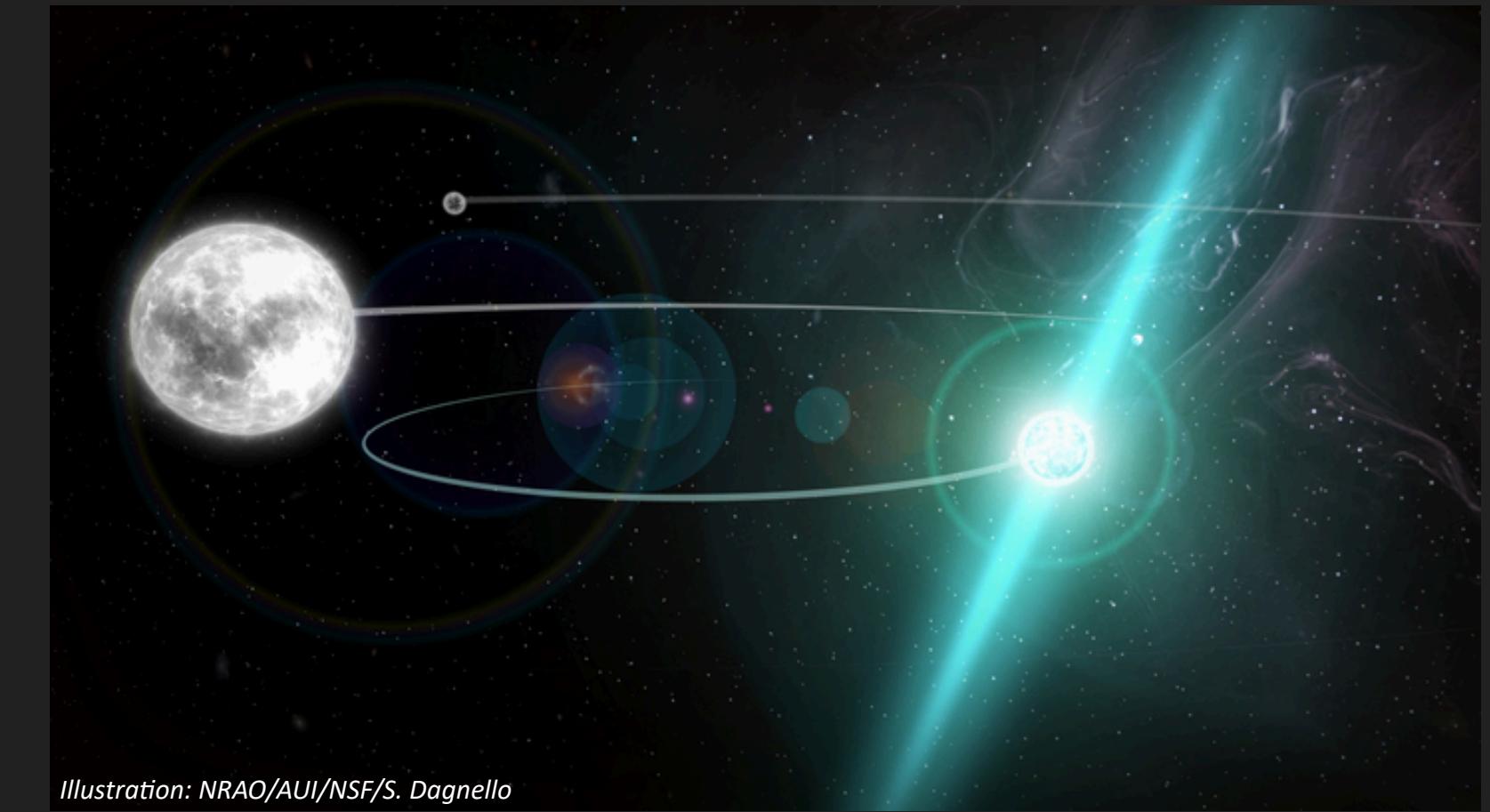
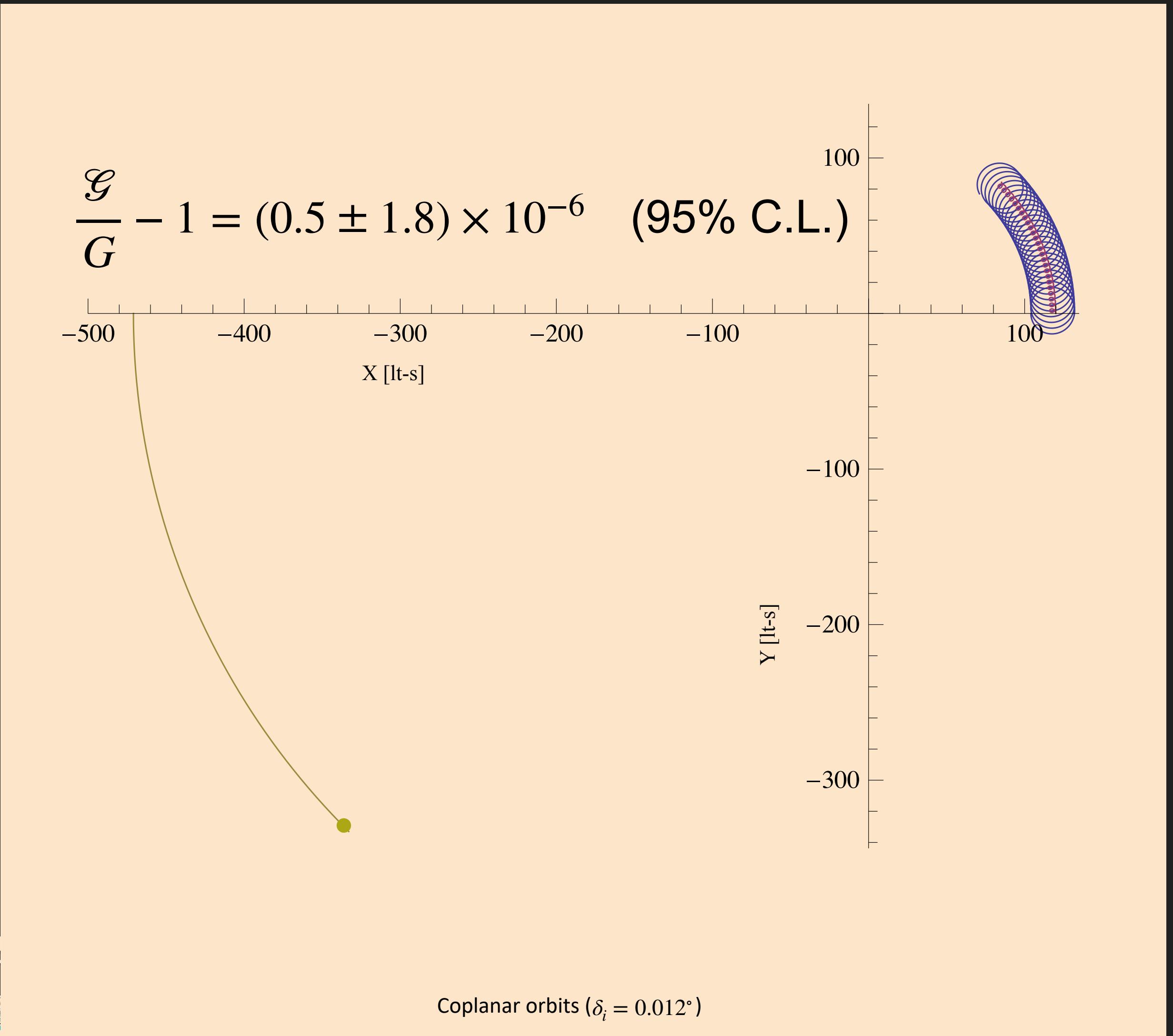
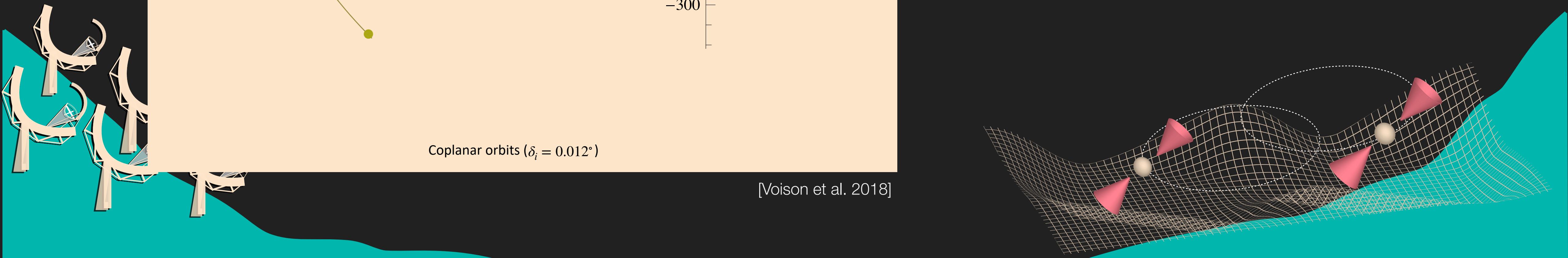
[Hofmann & Müller 2018]

$$\epsilon \equiv \frac{E_{grav}}{mc^2} \simeq -0.2$$

??

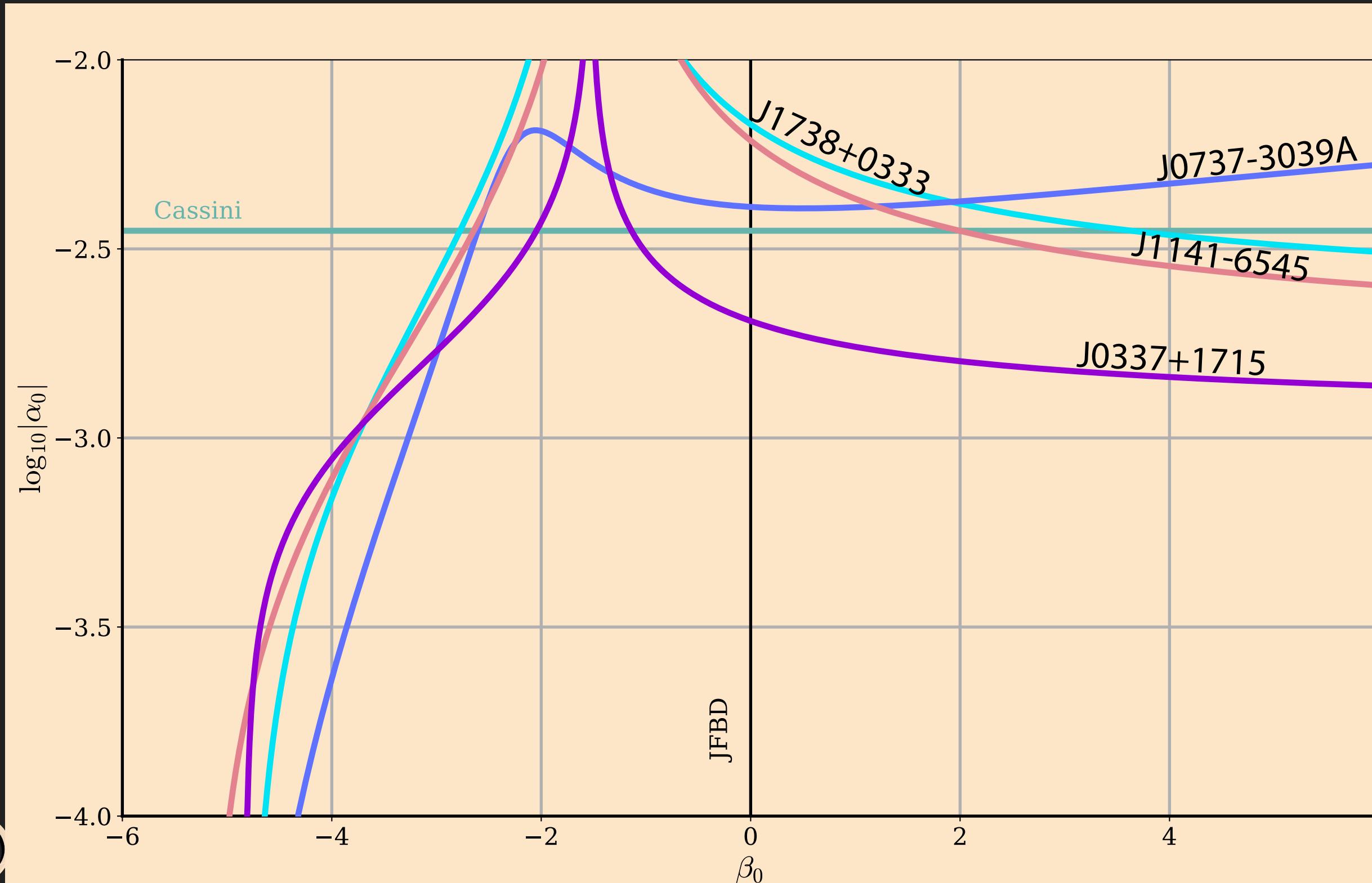


A stellar triple system



PSR J0337+1715: $P = 2.7$ ms, $M_{\text{PSR}} = 1.436 M_\odot$
Inner orbit: 1.63 d, $M_{\text{WD}} = 0.197 M_\odot$
Outer orbit: 327 d, $M_{\text{WD}} = 0.410 M_\odot$

Tests of scalar-tensor gravity: triple system

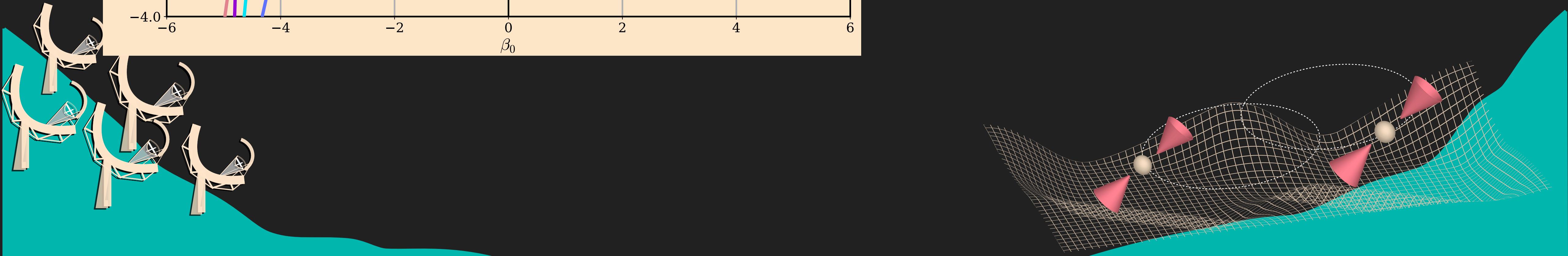


J1738+0333 - Freire et al. (2012)

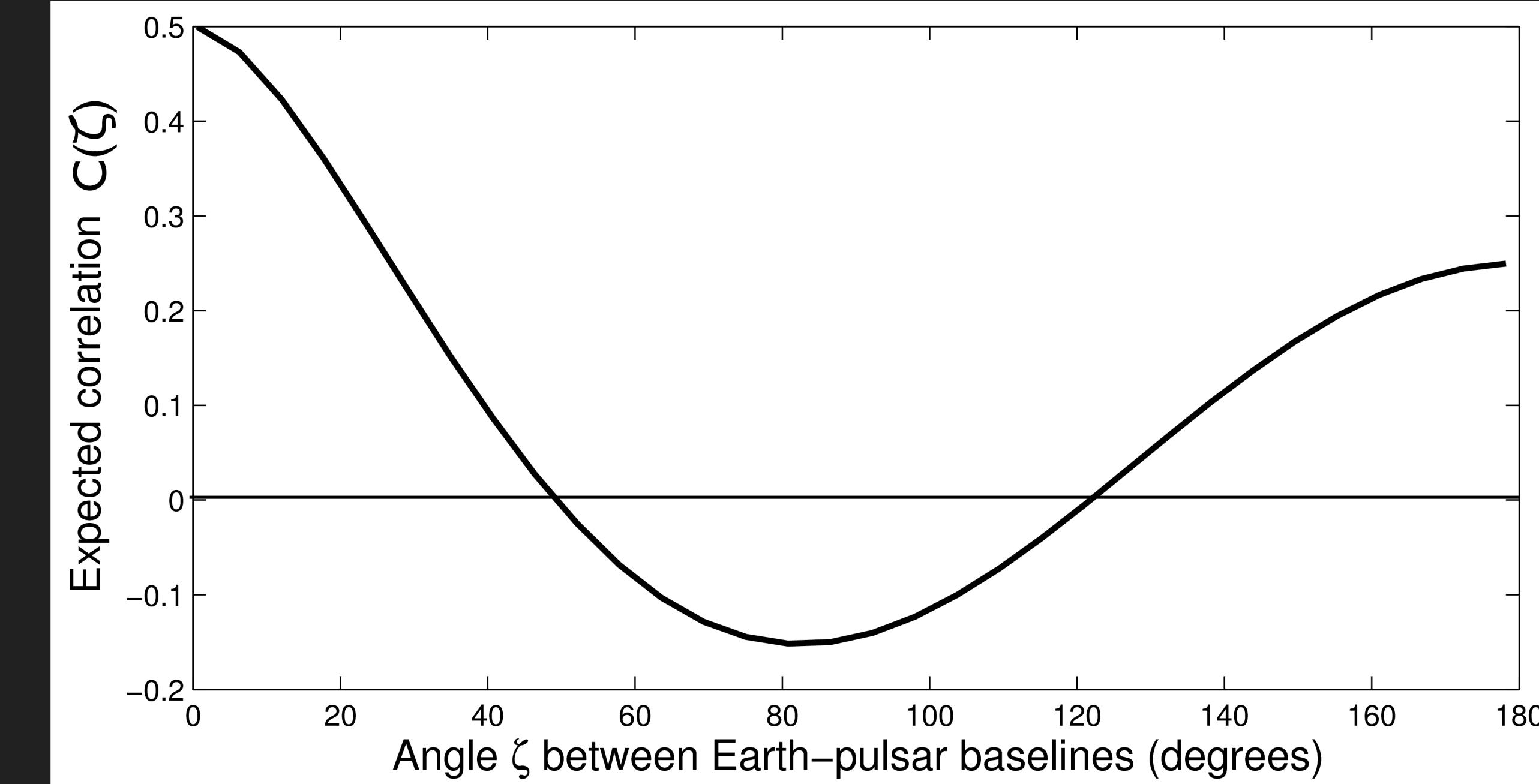
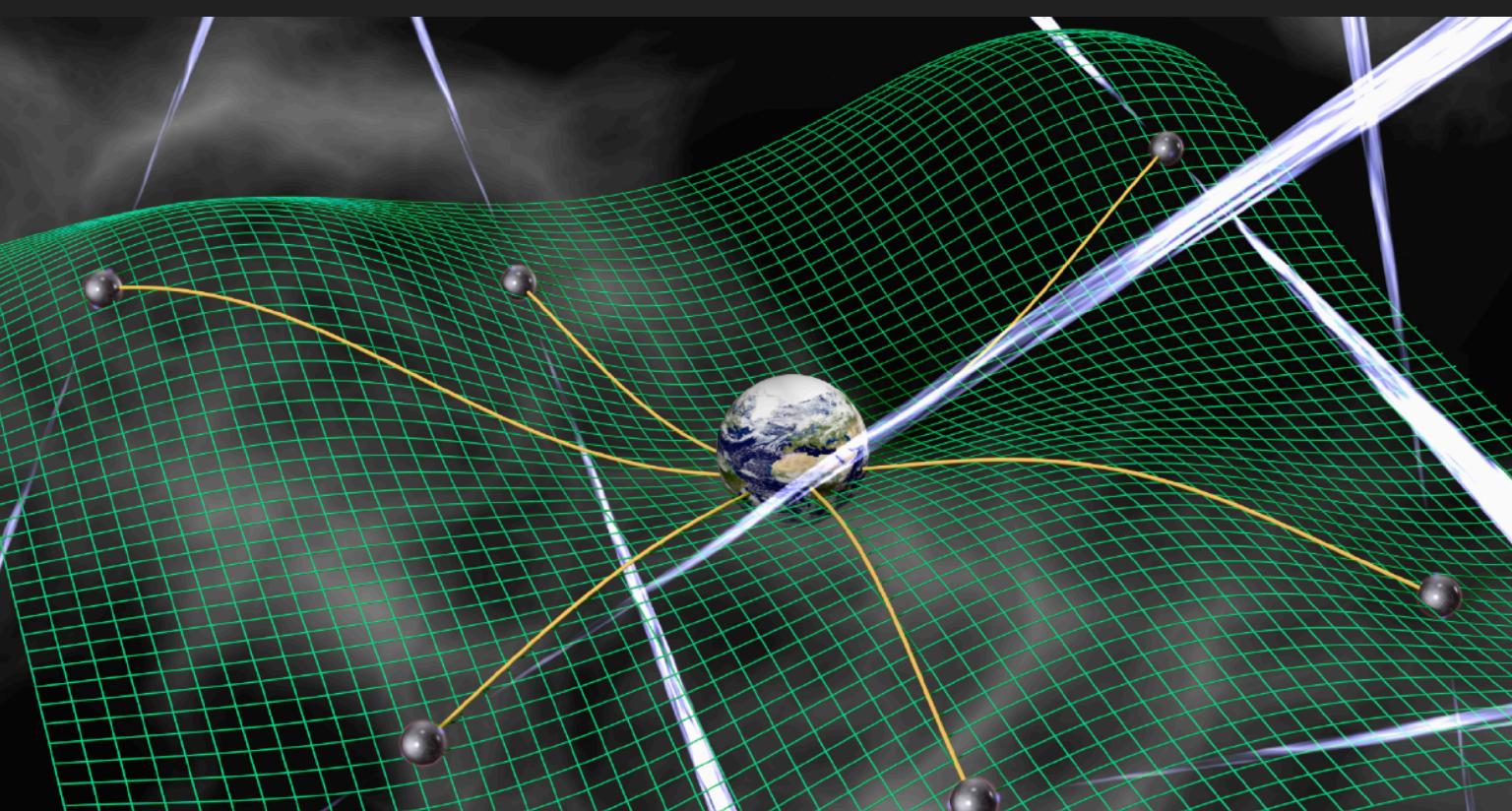
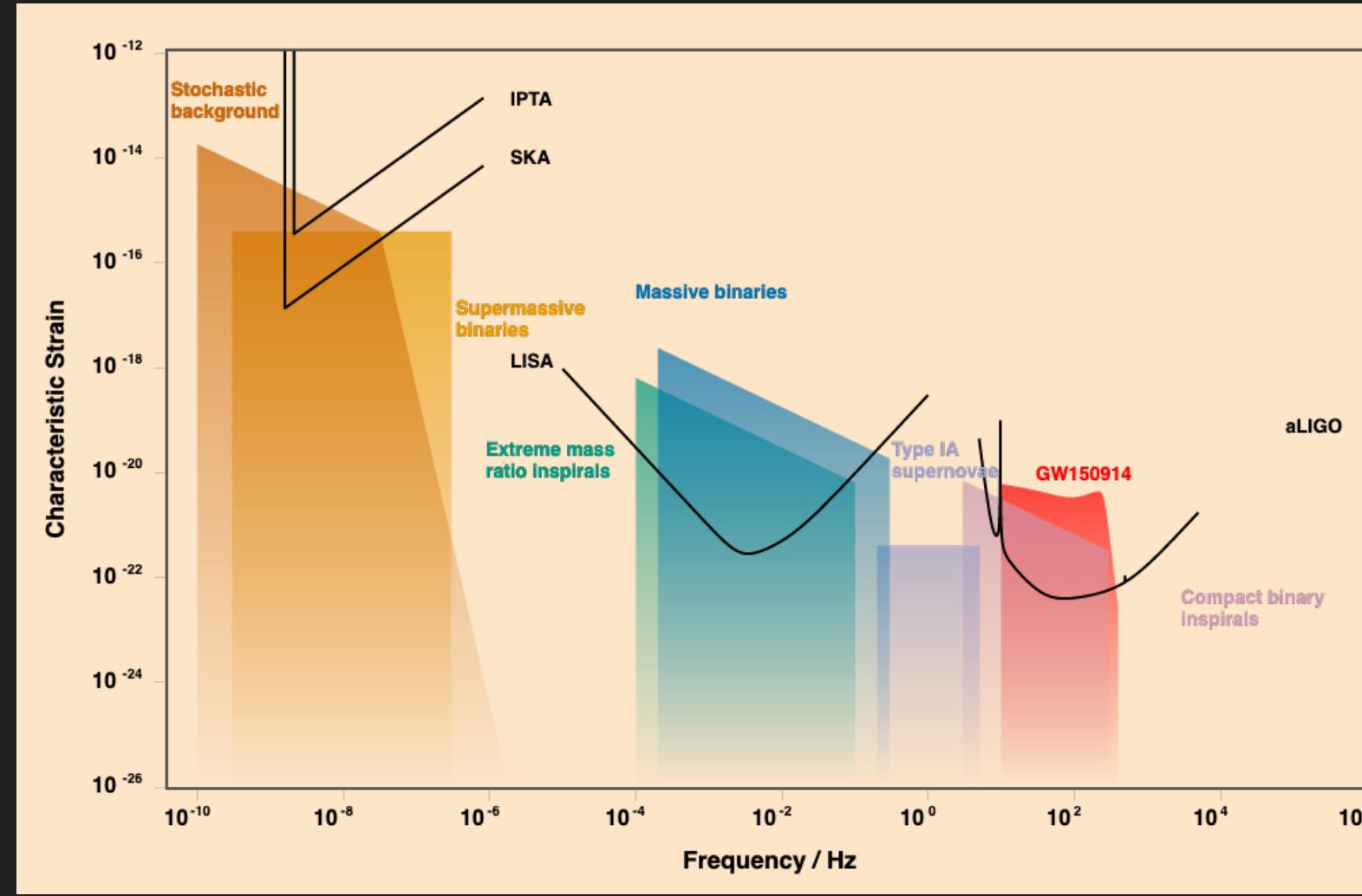
J0737-3039A - Kramer et al. (submitted)

J1141-6545 - Batrakov et al. (in prep.)

J0337+1715 - Voison et al. (2018)

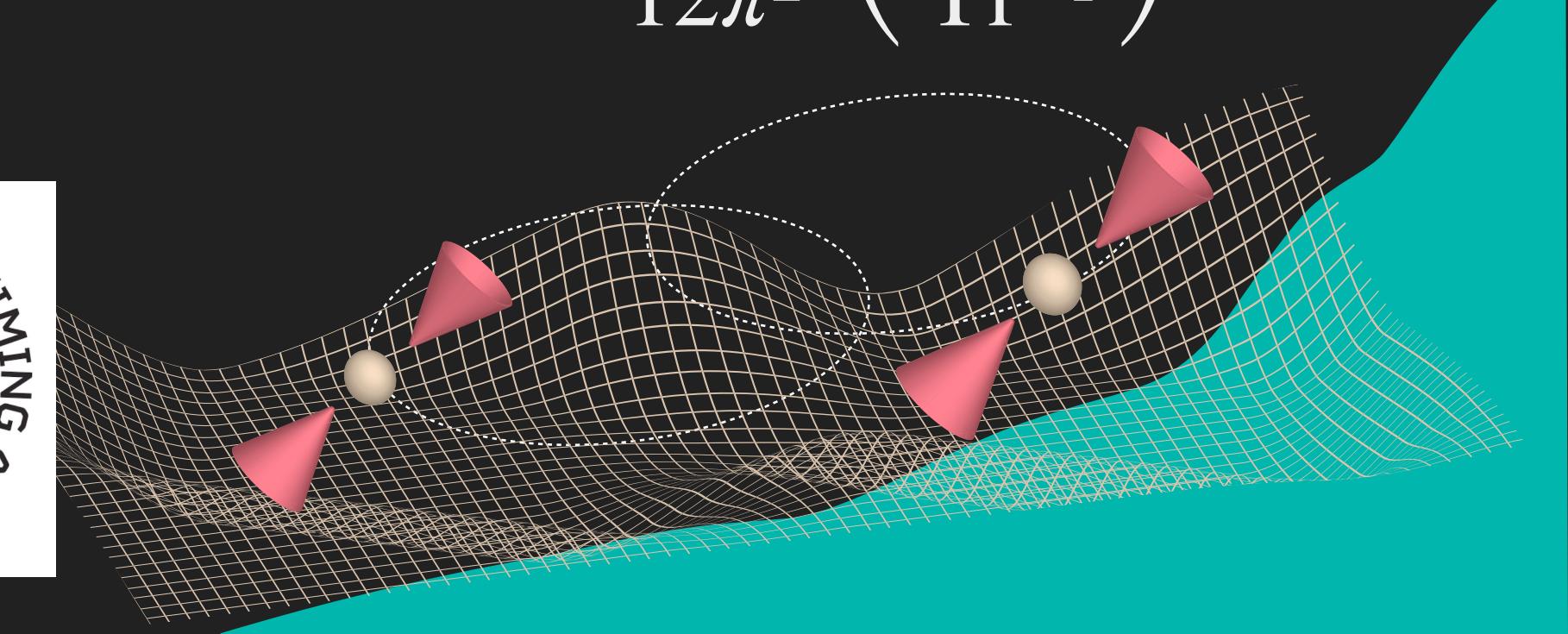


Pulsars as gravitational wave detectors

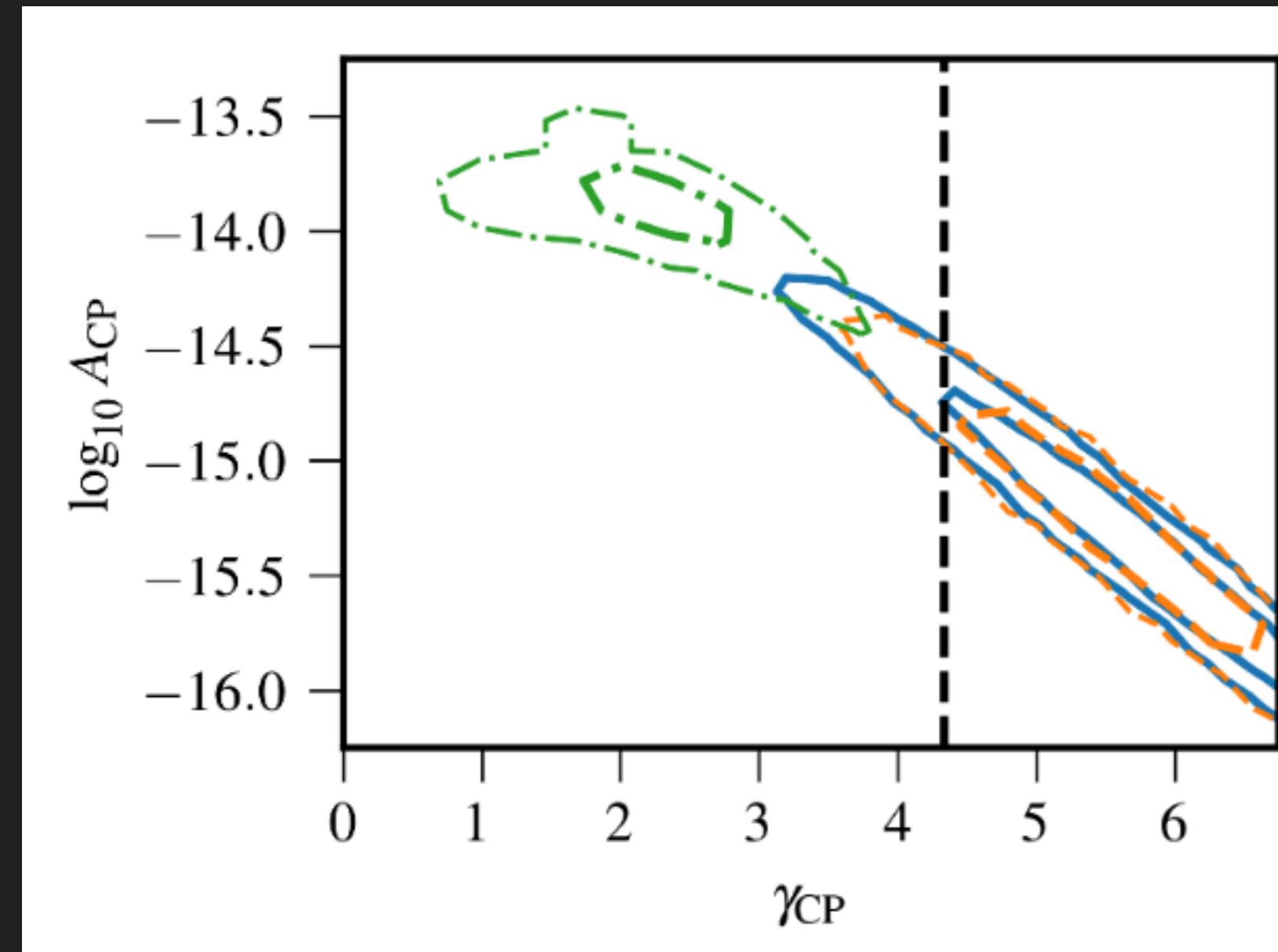


[Hellings & Downs 1983]

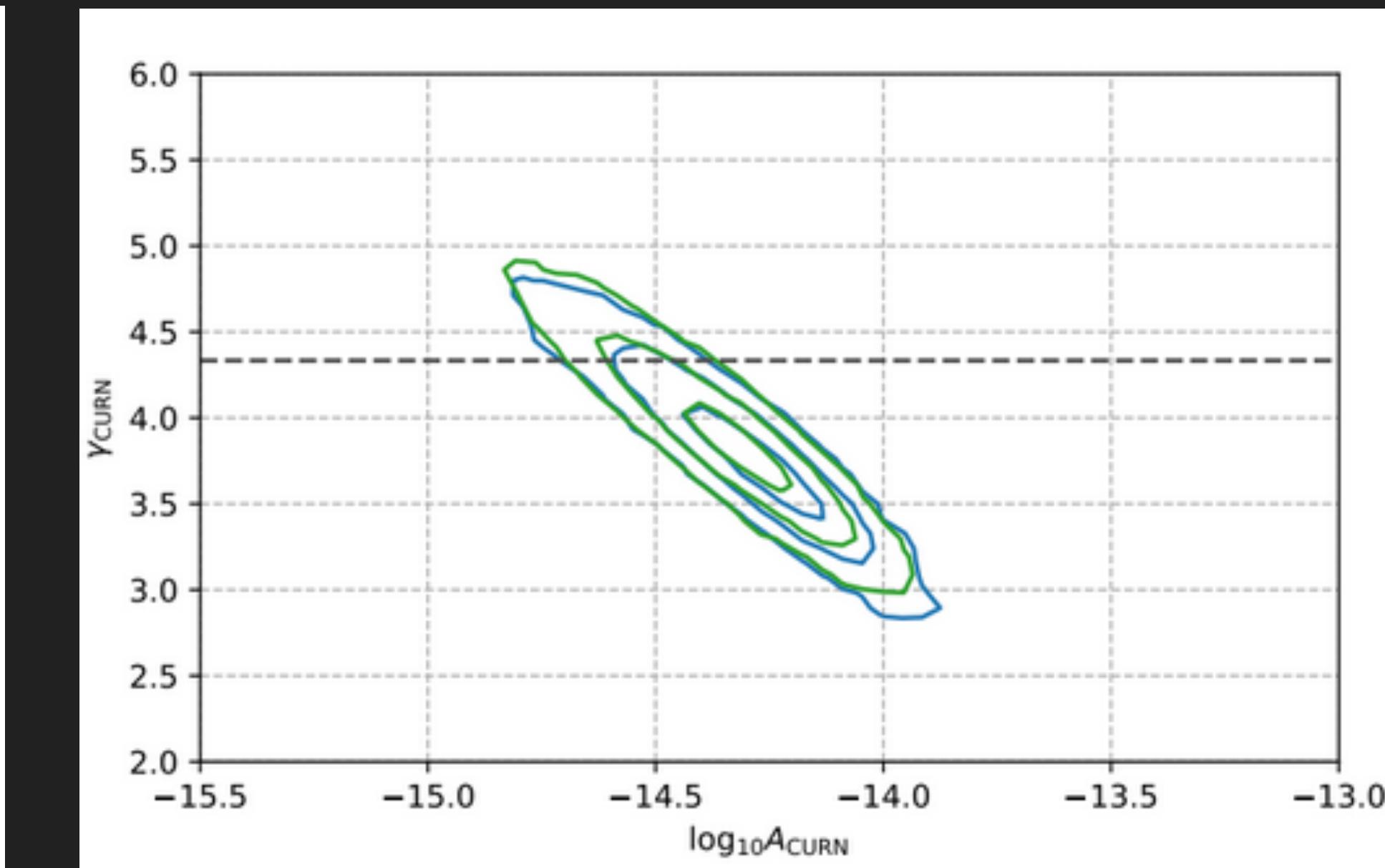
$$h(f) = A_{\text{gwb}} \left(\frac{f}{\text{Yr}^{-1}} \right)^{\alpha=-2/3} \implies P(f) = \frac{A_{\text{gwb}}^2}{12\pi^2} \left(\frac{f}{\text{Yr}^{-1}} \right)^{\alpha^2-3=-13/3}$$



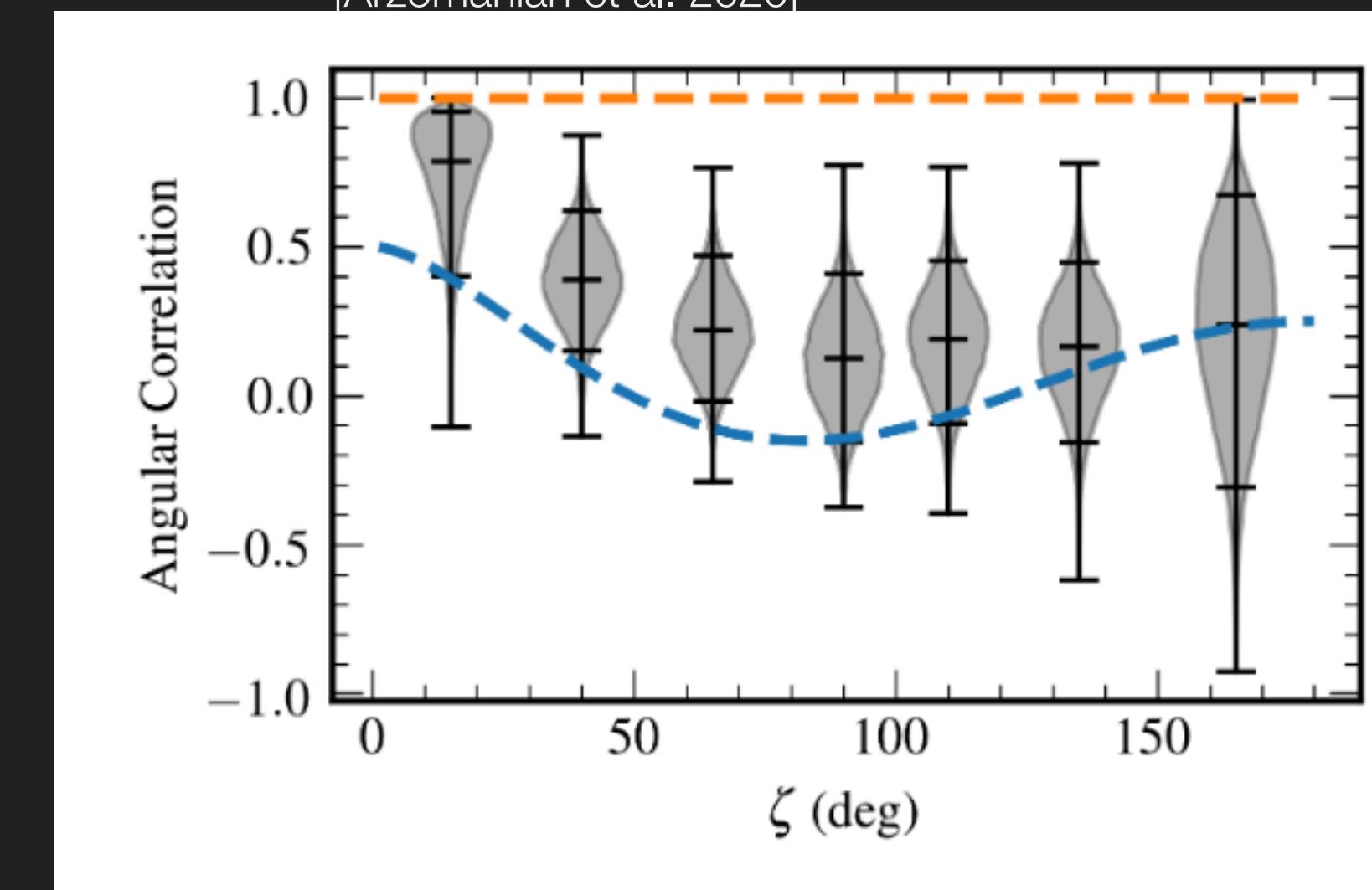
There is something, is this gravitational waves?



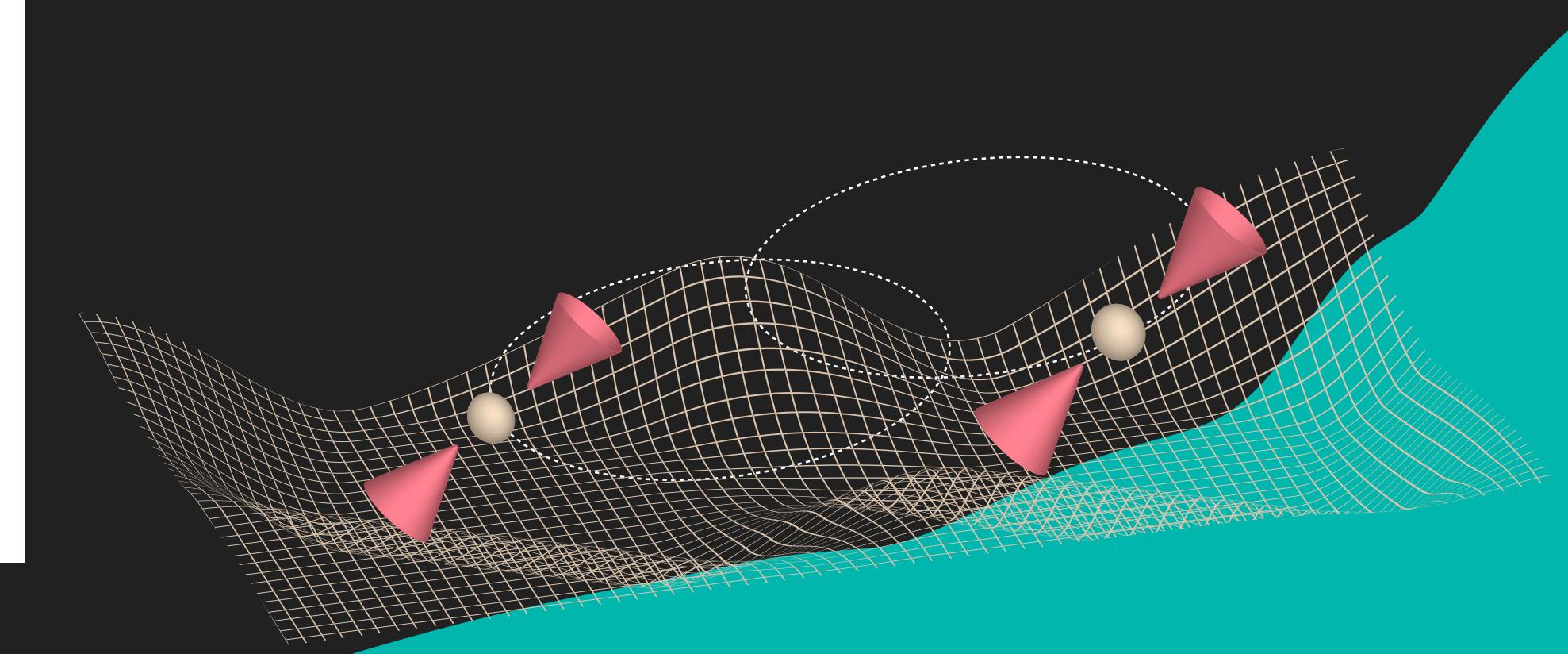
[Arzomanian et al. 2020]



[EPTA collaboration, in prep.; PRELIMINARY RESULT]



[Arzomanian et al. 2020]

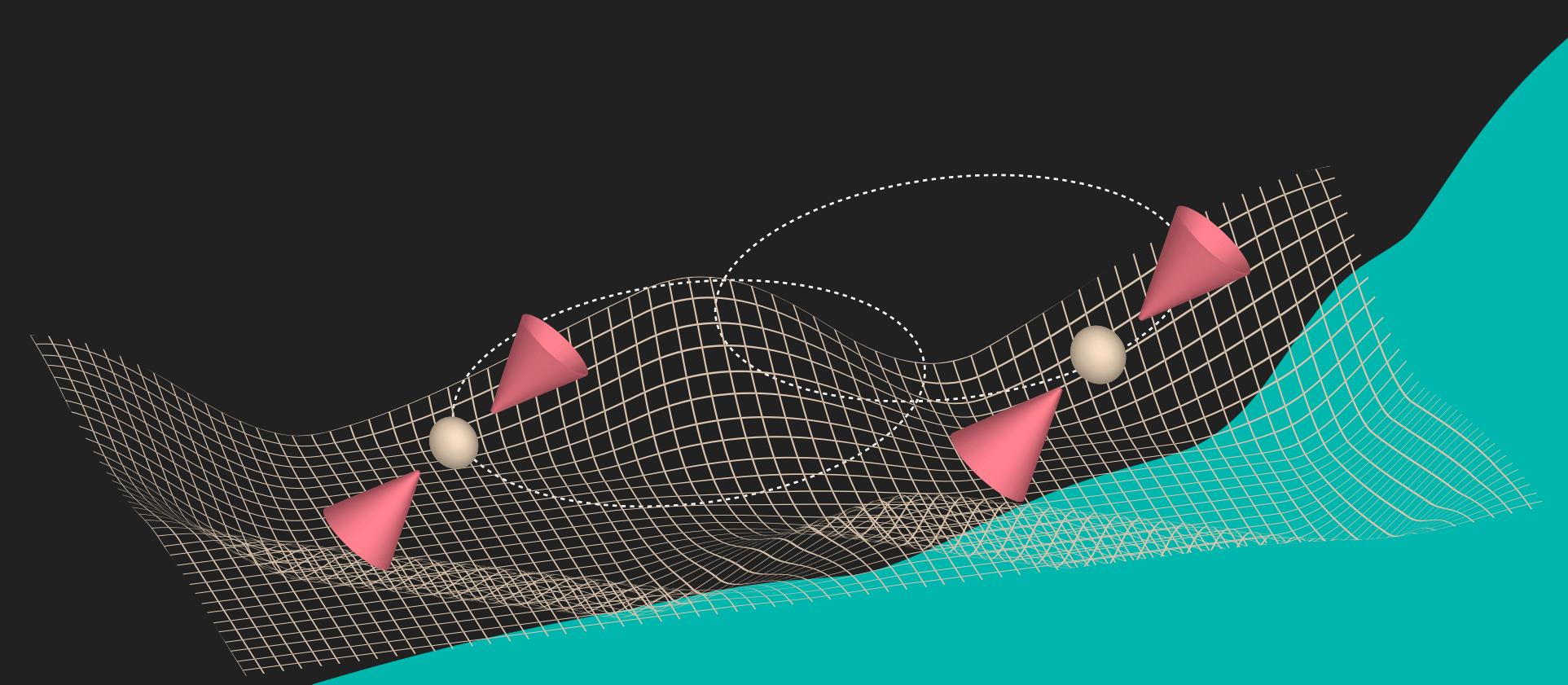


Pulsar timing: Near future

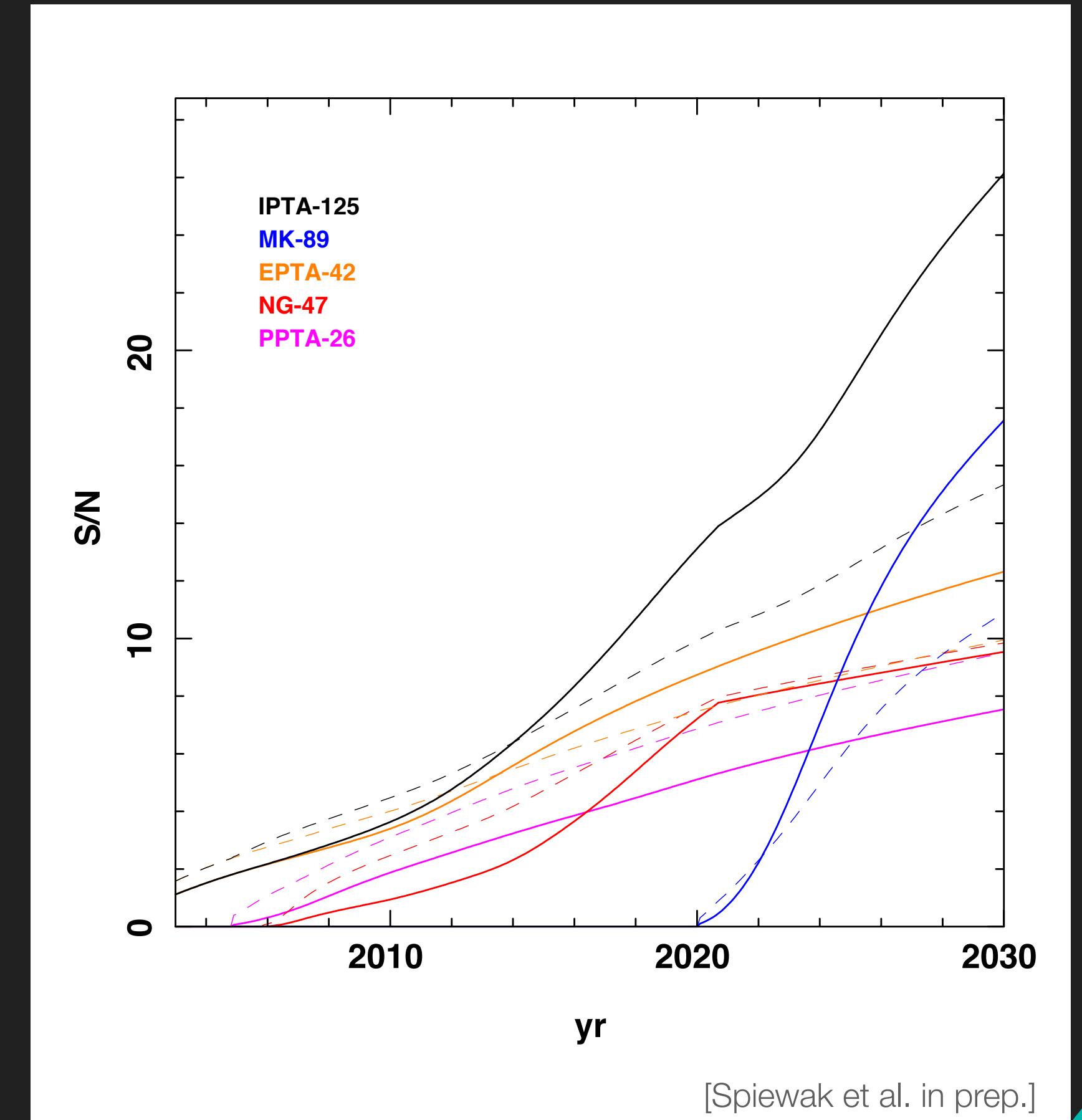
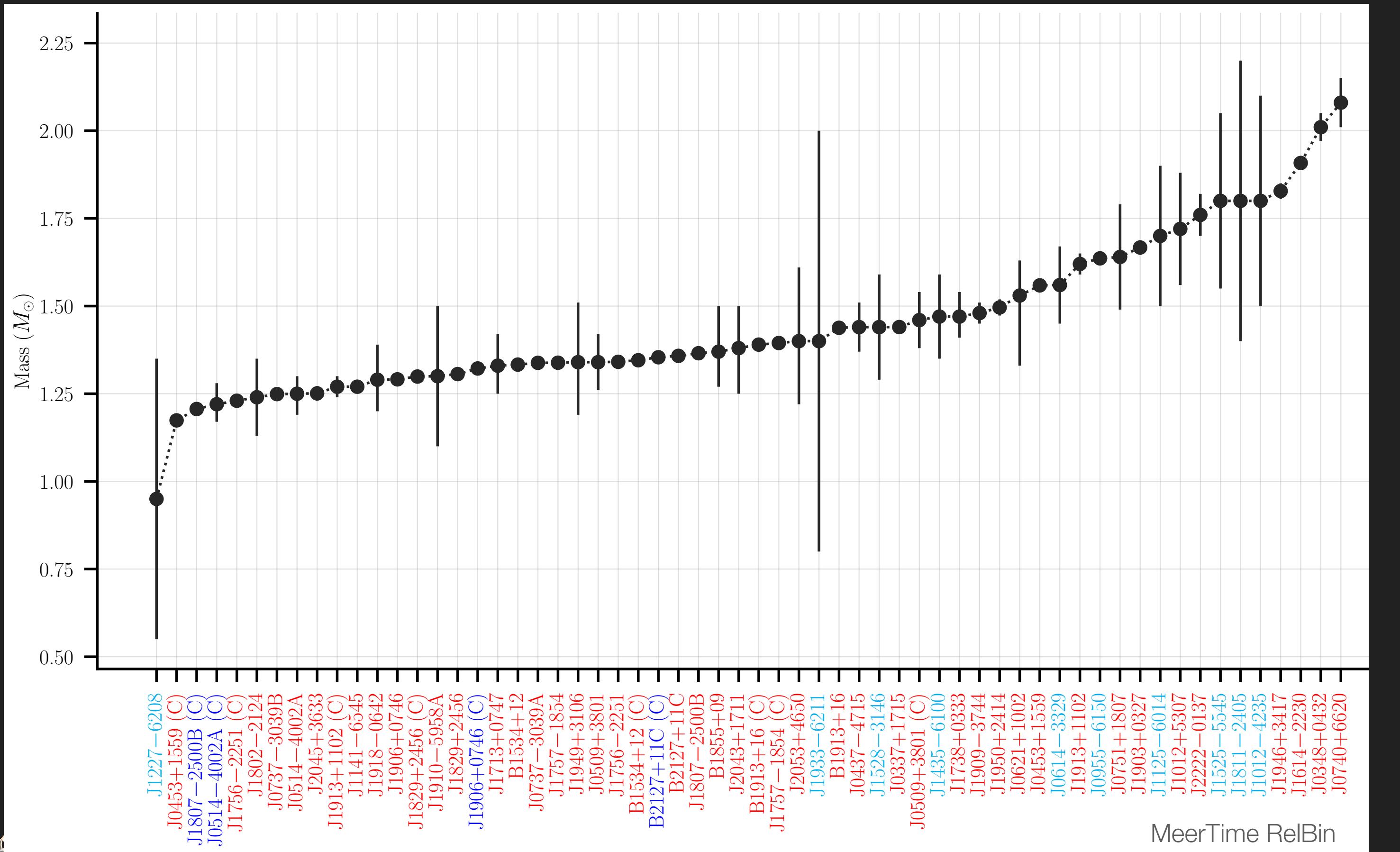
FAST Telescope, China



MeerKAT telescope, SA



MeerKAT as a pulsar timing instrument



Thank you for listening!

[Spiewak et al. in prep.]