

# Fellini project QE-TherMa Quantum Equilibrium Thermal Machines

Ugo Marzolino

INFN, Trieste Unit



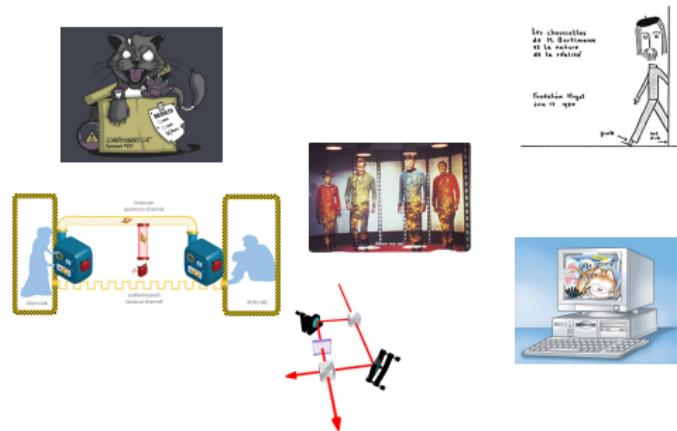
Supervisor: Prof. Fabio Benatti, University of Trieste & INFN Trieste

# Background and motivation

## Quantum technologies

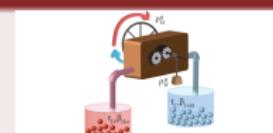
### Quantum effects and enhancements in information technologies

- EPR paradox
- Schrödinger's cat
- Bell's tests
- quantum teleportation
- quantum cryptography
- quantum computing
- quantum metrology



## Quantum thermodynamics

### Heat engines using quantum systems



# Quantum metrology and phase transitions

## Cramér-Rao bound and the Fisher information

$$\text{Var } X \geq \frac{1}{F_X}, \quad F_X[\rho_X] = \lim_{\epsilon \rightarrow 0} \frac{8}{\epsilon^2} \left( 1 - \text{Tr} \sqrt{\sqrt{\rho_X} \rho_{X+\epsilon} \sqrt{\rho_X}} \right)$$

## Quantum criticality as a resource for enhanced metrological devices

✓ D. Braun, G. Adesso, F. Benatti, R. Floreanini, U. Marzolino, M. Mitchell, S. Pirandola, *Rev. Mod. Phys.* **90**, 35006 (2018)

## Phase separation at critical points

$$\frac{F_X}{N} \xrightarrow[N \rightarrow \infty]{} \infty \quad \text{or superextensive finite size scaling} \quad F_X = O(N^\alpha), \quad \alpha > 1$$

- thermal phase transitions
- quantum phase transitions
- topological phase transitions
- quantum non-equilibrium phase transitions
- excited state quantum phase transitions

# Precision magnetometry

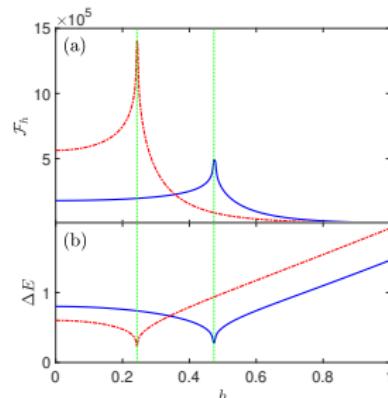
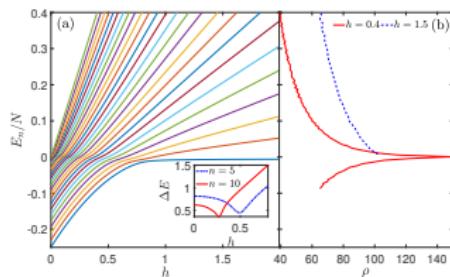
## Excited state phase transitions

Phase transitions at each excited state formin a continuous set of critical points

- ✓ Q. Wang, U. Marzolini, *Precision magnetometry exploiting excited-state quantum phase transitions*, under review

Lipkin-Meshkov-Glick model in nuclear systems and superconductors

$$H = h S_z - \frac{S_x^2}{N}, \quad S_\alpha = \sum_{i=1}^N \sigma_i^\alpha, \quad |h| < 1$$

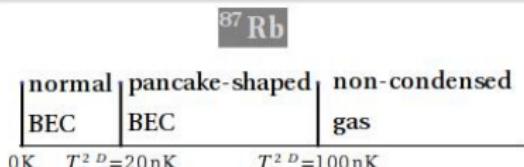
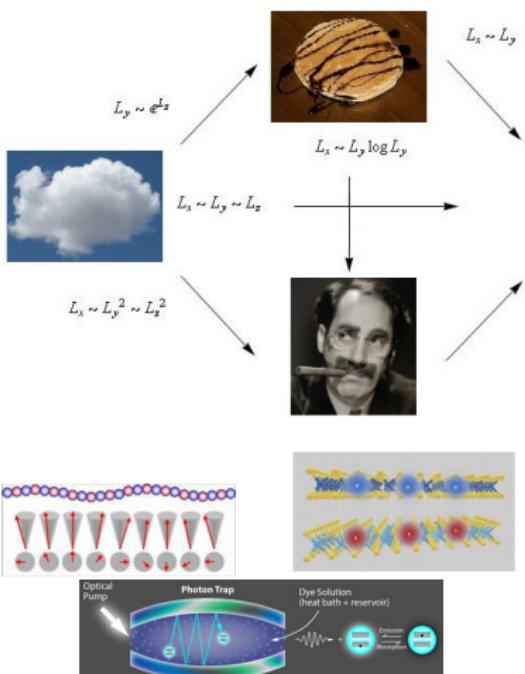


- Best accuracy for measuring the magnetic field:  $\delta^2 h \sim \frac{1}{F_h} \sim \frac{1}{N^{2.07}}$
- Excited state quantum phase transitions overcome the shot-noise benchmark (central limit theorem)  $\delta^2 h \sim \frac{1}{N}$

# Bose-Einstein condensates

BECs depending on the spatial dimensions

Macroscopic occupation of a set of modes with zero measure



- Atom species:
  - Lithium, Sodium, Potassium, Rubidium, Caesium, Chromium, Calcium, Strontium, Ytterbium, Dysprosium, Erbium

- Quasi-particles (room temp.):
  - Magnons, Polaritons, Exitons
- Photons in cavity with dye molecules (room temp.)

# Quantum chemical engines

## Conversion of chemical into mechanical energy

### Role of quantum statistics

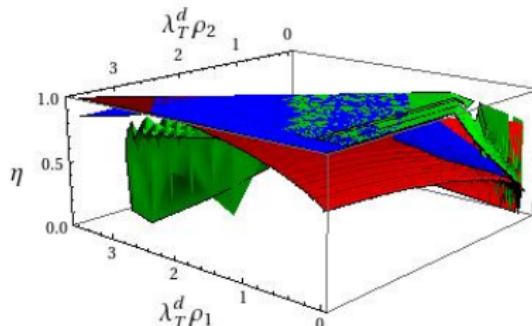
Realisable with quantum simulators  
 Potential applications in biological systems

- ✓ U. Marzolini,  *$\mu$ PT statistical ensemble*, under review
- ✓ U. Marzolini, F. Benatti, *Quantum chemical engines*, work in progress

- Chemical Carnot engine:    iso- $\mu T$  → iso- $NT$  → iso- $\mu T$  → iso- $NT$

$$\eta = \frac{\text{mech. work}}{\text{abs. chem. work}} = 1 - \frac{\mu_1}{\mu_2}, \quad \text{BEC chemical source} \implies \mu_1 \approx 0, \quad \eta \approx 1$$

- Chemical Otto engine:    iso- $VT$  → iso- $NT$  → iso- $VT$  → iso- $NT$



Quantum degenerate working fluid  
(fermionic or bosonic)

$$\implies \eta \approx 1$$

# Perspectives

## Complex models

- Strong interactions
- Mean field models

## Irreversible effects

- Dissipation
- Endoreversible engines

## Applications

- Realisability with atoms, quasi-particles, and photons
- Connection with biological phenomena