

Kaon-nucleon/nuclei interaction studies at DAΦNE present and future perspectives

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On the behalf of the AMADEUS collaboration

AMADEUS at LNF



Istituto Nazionale di Fisica Nucleare
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The AMADEUS collaboration

Anti-kaonic **M**atter **A**t **D**_{AΦNE}: an **E**xperiment with **U**nravelling **S**pectroscopy

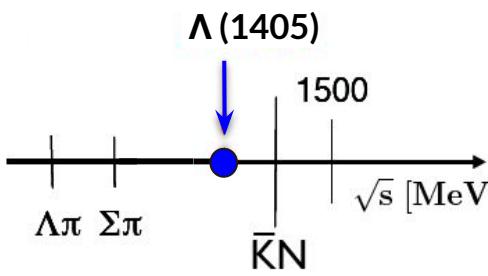


Motivation

AMADEUS (Antikaonic Matter At DAΦNE: an Experiment with Unravelling Spectroscopy)
investigates **low-energy K^- absorption in nuclei** with the aim to extract information on:

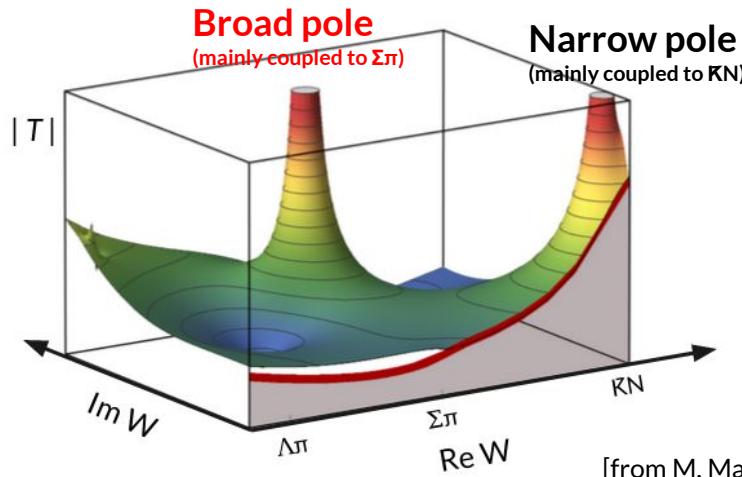
- K^-N interaction above and below threshold
 - $\Lambda(1405)$ nature
 - kaonic bound states
 - K^-N scattering amplitudes and cross sections
- K^-NN , K^-NNN , K^-NNNN (multi-nucleon) interactions
 - essential for the determination of K^- -nuclei optical potential
- In medium modification of the KbarN interaction
 - partial restoration of chiral symmetry → hadrons mass origin
 - Equation of State of Neutron Stars
 - modification of $\Lambda(1405)$ and $\Sigma(1385)$ properties in nuclear medium

$\Lambda(1405)$ nature

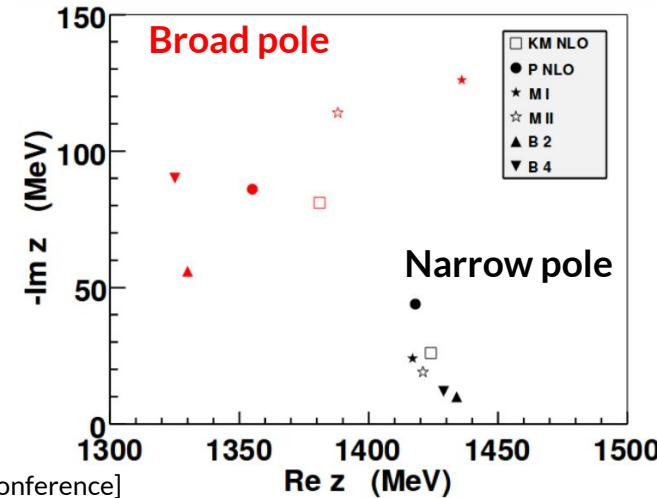


The $\Lambda(1405)$ state does not fit with the simple three quarks model (uds) and it is commonly accepted to be **partially a $\bar{K}N$ bound state**. Decay channels: $\Sigma^+\pi^-$, $\Sigma^-\pi^+$, $\Sigma^0\pi^0$

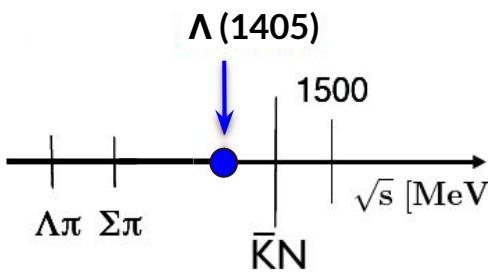
Chiral models: dynamical origin. Two poles of the scattering amplitude \rightarrow pole positions is model dependent (relative contributions not measured experimentally)



[from M. Mai talk at NSTAR19 conference]

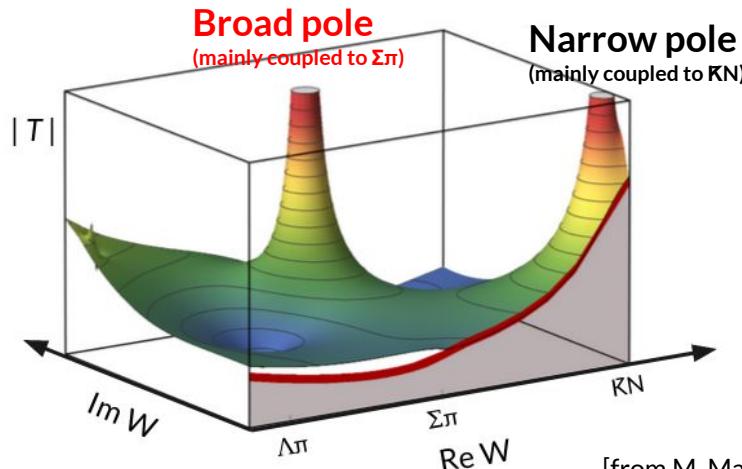


Impact on $\Lambda(1405)$ nature

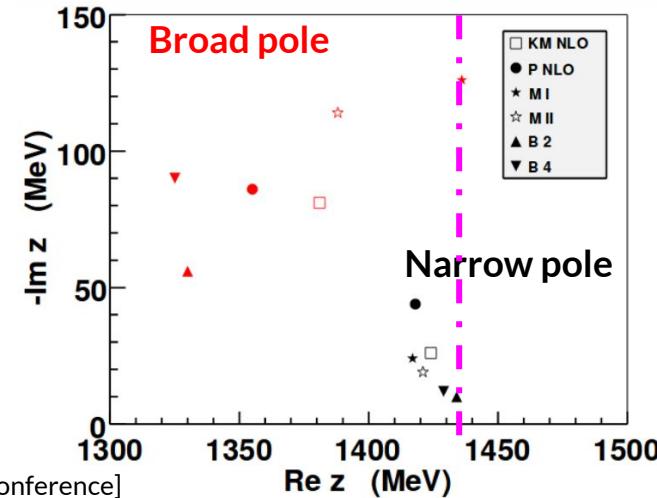


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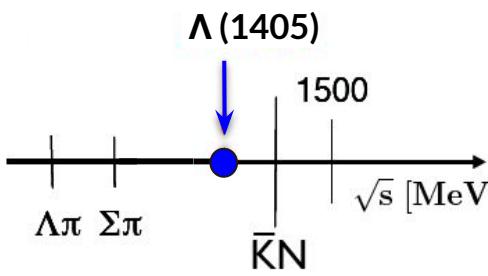
Chiral models: dynamical origin. Two poles of the scattering amplitude \rightarrow pole positions is model dependent (relative contributions not measured experimentally)



[from M. Mai talk at NSTAR19 conference]
see also Ulf-G. Meißner, Symmetry 12 (2020) 6, 981

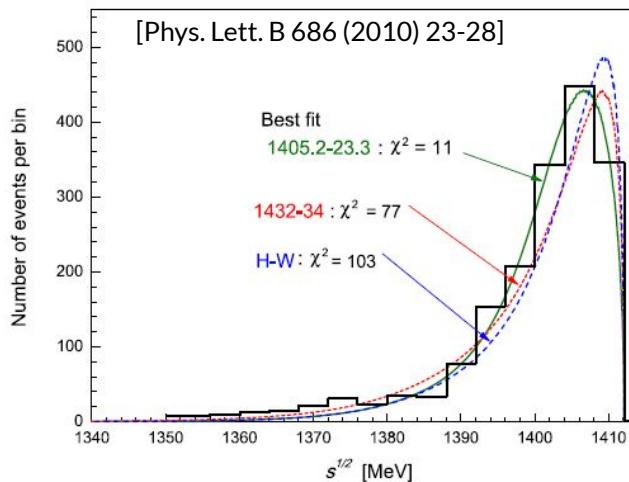


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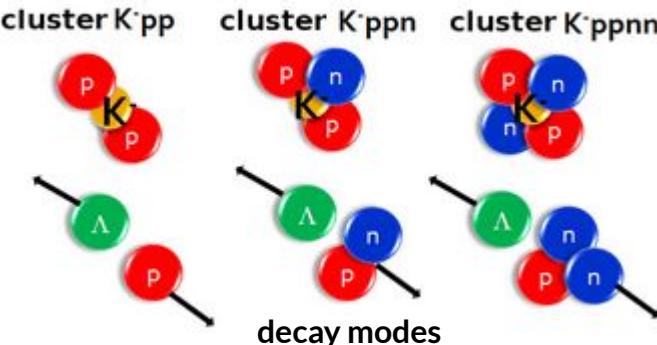


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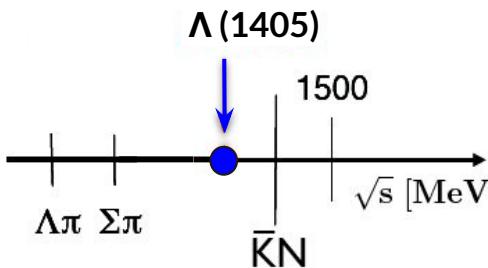
Single pole ansatz (Esmaili-Akaishi-Yamazaki phenomenological potential model): Very strongly attractive $\bar{K}N$ interaction in the $I = 0$ channel → existence of deeply bound kaonic states



Kaonic Bound States

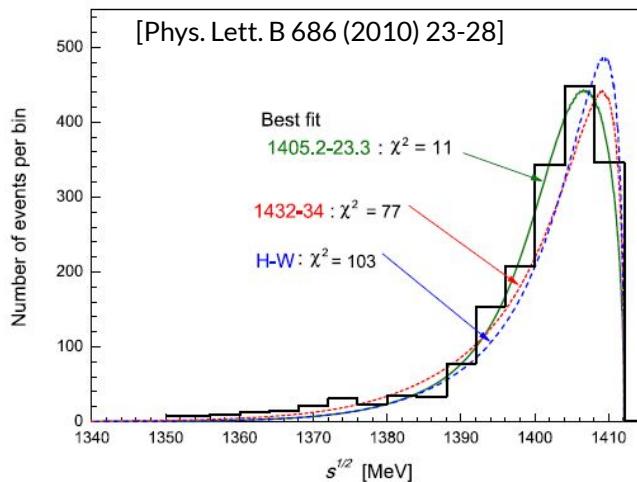


Impact on $\Lambda(1405)$ nature

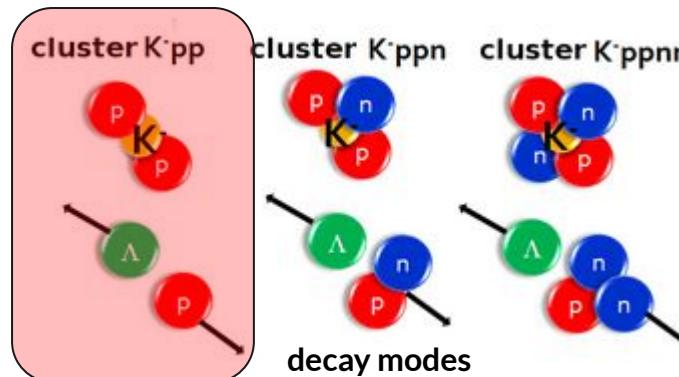


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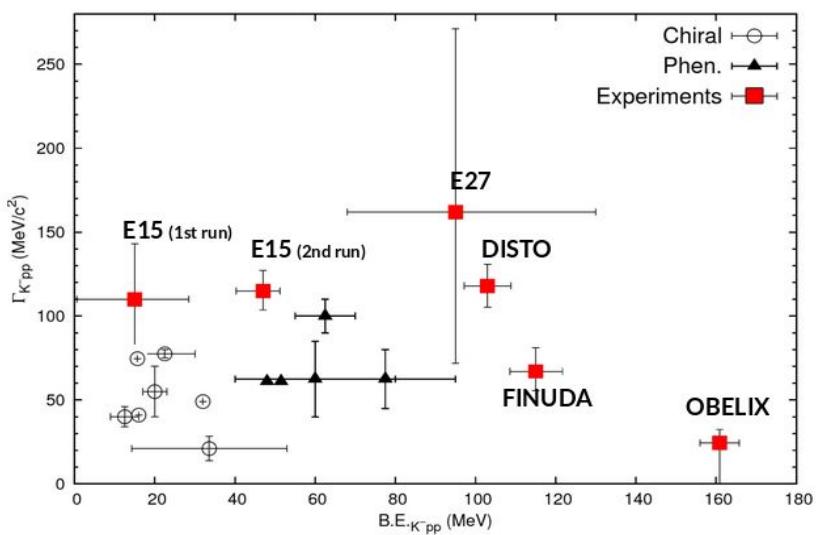


Kaonic Bound States



K^-pp bound state

- KN input model is critical for the theoretical interpretation
- different bound state production mechanisms give different predictions
- **E15 gives positive evidence in K^- induced reactions in flight (theoretical interpretation by Sekihara, Oset, Ramos)**



Experiments

Theory

	BE (MeV)	Γ (MeV)	Reference
Dote, Hyodo, Weise	17-23	40-70	Phys.Rev.C79 (2009) 014003
Akaishi, Yamazaki	48	61	Phys.Rev.C65 (2002) 044005
Barnea, Gal, Liverts	16	41	Phys.Lett.B712 (2012) 132-137
Ikeda, Sato	60-95	45-80	Phys.Rev.C76 (2007) 035203
Ikeda, Kamano, Sato	9-16	34-46	Prog.Theor.Phys. (2010) 124(3): 533
Shevchenko, Gal, Mares	55-70	90-110	Phys.Rev.Lett.98 (2007) 082301
Revai, Shevchenko	32	49	Phys.Rev.C90 (2014) no.3, 034004
Maeda, Akaishi, Yamazaki	51.5	61	Proc.Jpn.Acad.B 89, (2013) 418
Bicudo	14.2-53	13.8-28.3	Phys.Rev.D76 (2007) 031502
Bayar, Oset	15-30	75-80	Nucl.Phys.A914 (2013) 349
Wycech, Green	40-80	40-85	Phys.Rev.C79 (2009) 014001
Sekihara, Oset, Ramos	16	72	Prog.Theor.Phys. (2016) no.12, 123D03
Sekihara, Oset, Ramos	20	80	E. Oset talk at UJ Symposium 2019

Experiment	BE (MeV)	Γ (MeV)	Reference
FINUDA	115^{+6}_{-5} (stat.) $^{+3}_{-4}$ (syst.)	67^{+14}_{-11} (stat.) $^{+2}_{-3}$ (syst.)	PRL 94 (2005), 212303
OBELIX	160.9 ± 4.9	$< 24.4 \pm 8.0$	NPA 789 (2007), 222
E549	-	-	MPLA 23 (2008), 2520
DISTO	103 ± 3 (stat.) ± 5 (syst.)	118 ± 8 (stat.) ± 10 (syst.)	PRL 104 (2010), 132502
LEPS/SPring-8	Upper Limit		PLB 728 (2014), 616
HADES	Upper Limit		PLB 742 (2015), 242
E27	95^{+18}_{-17} (stat.) $^{+30}_{-21}$ (syst.)	162^{+87}_{-45} (stat.) $^{+66}_{-78}$ (syst.)	PTEP (2015), 021D01
AMADEUS	Upper Limit		PLB 758 (2016), 134
E15	15^{+6}_{-8} (stat.) ± 12 (syst.)	110^{+19}_{-17} (stat.) ± 27 (syst.)	PTEP (2016), 051D01
E15 (2 nd run)	47 ± 3 (stat.) $^{+3}_{-4}$ (syst.)	115 ± 7 (stat.) $^{+10}_{-20}$ (syst.)	PLB 789 (2019), 620

Goals of AMADEUS

Unprecedented studies of the **low-energy charged kaons interactions in nuclear matter**: solid and gaseous targets (H , ${}^4\text{He}$, ${}^9\text{Be}$, ${}^{12}\text{C}$...) in order to obtain unique quality information about:

1. Controversial nature of the $\Lambda(1405)$ and $\text{K}N$ amplitude below threshold



Y π CORRELATION STUDIES

(i.e. $\Lambda\pi$ and $\Sigma\pi$ and final states)

2. Low-energy charged kaon **cross sections** for momenta of 100 MeV/c



3. a) Interaction of K^- with more nucleons
(multi-nucleon K^- absorptions)



YN CORRELATION STUDIES

(i.e. Λp , $\Sigma^0 p$, and Λt final states)

3. b) possible existence of **kaonic bound states**

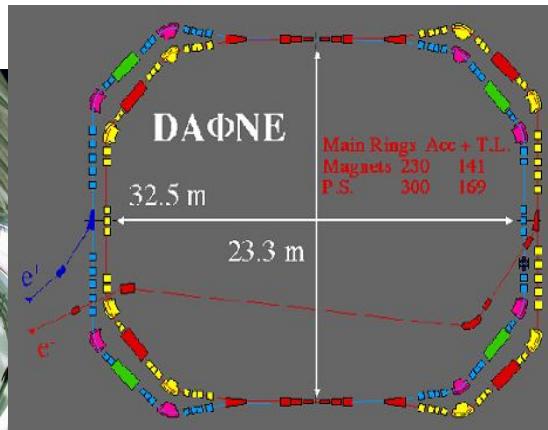
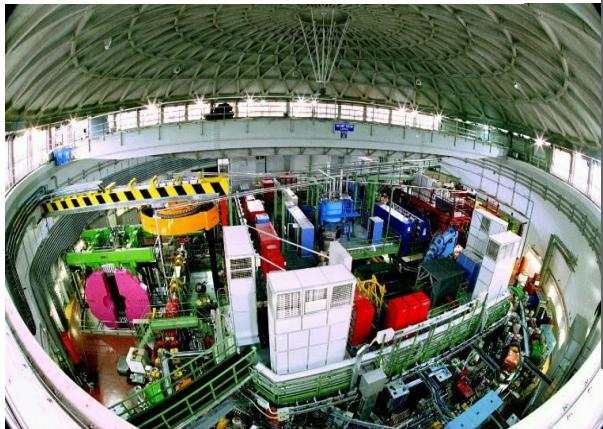


4. **future: YN scattering** → extremely poor experimental information from scattering data
(important for the EoS of Neutron Stars)

DAΦNE the Φ factory



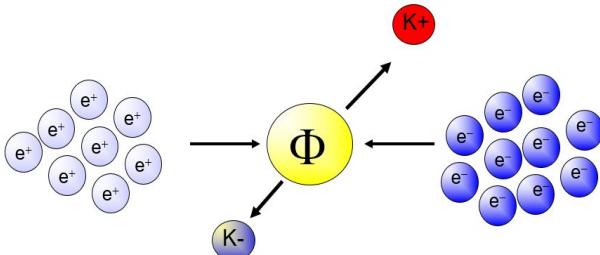
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- $e^+ e^-$ at 510 MeV
- Φ resonance decays at 49.2 % in K^+
- K^- back to back pair
- Very low momentum (≈ 127 MeV) K^- beam
- Flux of produced kaons: about 1000/second

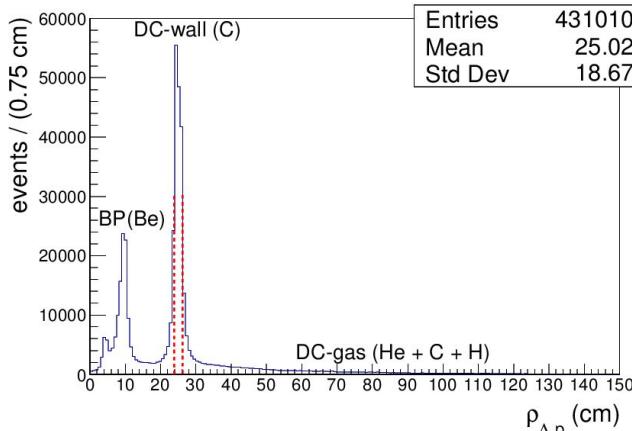
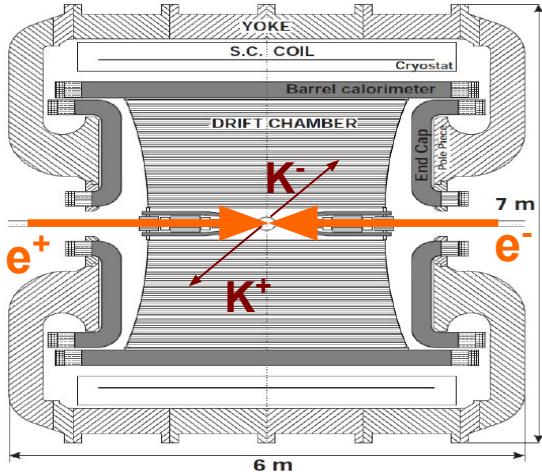


Best low momentum K^- factory in the world



Suitable for low-energy kaon physics:
→ **Kaonic atoms (SIDDHARTA-2)**
→ **Kaon-nucleons/nuclei interaction studies (AMADEUS)**

AMADEUS step 0



The KLOE detector

- Cylindrical drift chamber with a **4π geometry** and electromagnetic calorimeter
- **96% acceptance**
- optimized in the energy range of all **charged particles** involved
- **good performance** in detecting **photons and neutrons** checked by kloNe group

[M. Anelli et al., Nucl Inst. Meth. A 581, 368 (2007)]

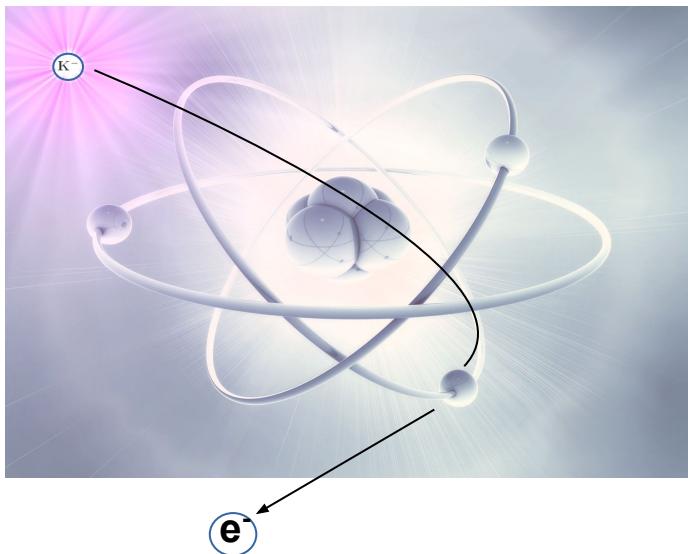
Presently we use **KLOE** as an **active target**

- DC wall ($750 \mu\text{m}$ C foil, $150 \mu\text{m}$ Al foil);
- DC gas (90% He, 10% C_4H_{10}).

K^- absorptions at-rest and in-flight

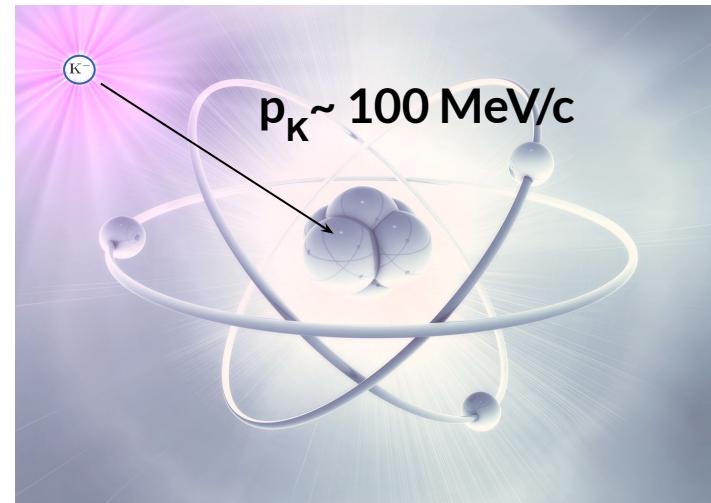
AT-REST

K^- absorbed from atomic orbitals
($p_K \sim 0 \text{ MeV}/c$)



IN-FLIGHT

($p_K \sim 100 \text{ MeV}/c$)



K^- multi-nucleon absorptions

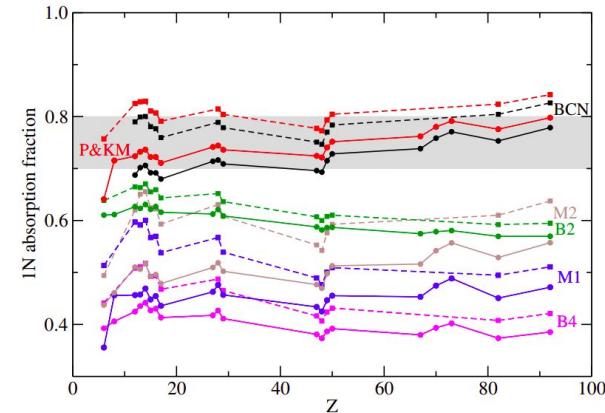
In order to fit the kaonic atoms data a K^- multi-nucleon absorption term is necessary in the K^- -nuclei optical potential:

$$V_{K^-}(\rho) = V_{K^-}^{(1)}(\rho) + V_{K^-}^{(2)}(\rho) \rightarrow \text{phen. multi-nucleon term}$$

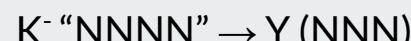
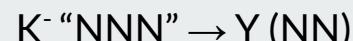
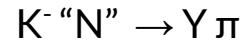
[E. Friedman, A. Gal, Nucl. Phys. A 959, 66 (2017)]

[Hrtáková, J. & Mareš, J. Phys. Rev. C96, 015205 (2017)]

single nucleon term from chiral models



- Single nucleon absorption (**1NA**):
- Two nucleon absorption (**2NA**):
- Three nucleon absorption (**3NA**):
- Four nucleon absorption (**4NA**):



→ multi-N processes

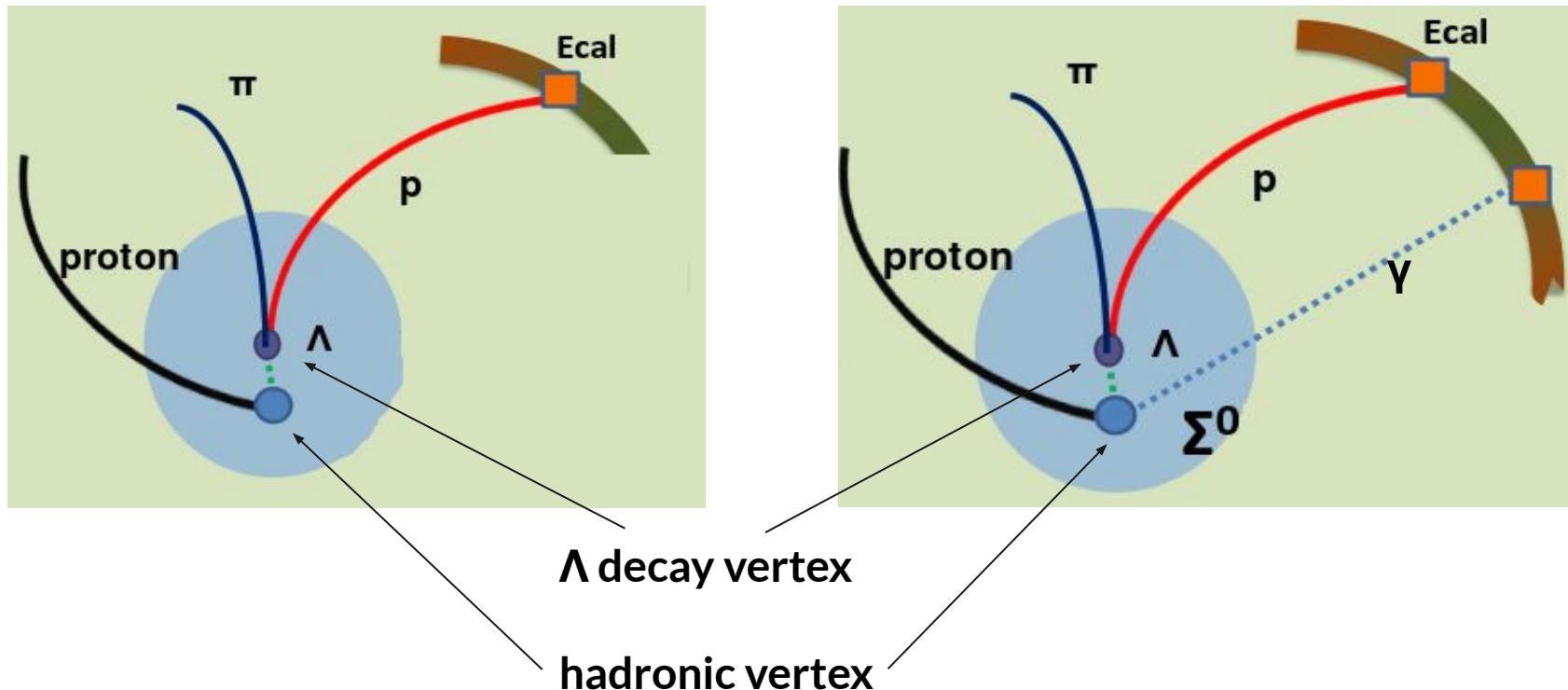
bound nucleons = “N”, “NN”, “NNN”, “NNNN”

bound or unbound nucleons = (NN), (NNN)

$Y = \Lambda, \Sigma$

YN correlation studies

K⁻ multi-nucleon absorptions are investigated by reconstructing the **hyperon-nucleon/nuclei** emitted in the final state of the process (i.e. Λp , $\Sigma^0 p$, and Λt final states)

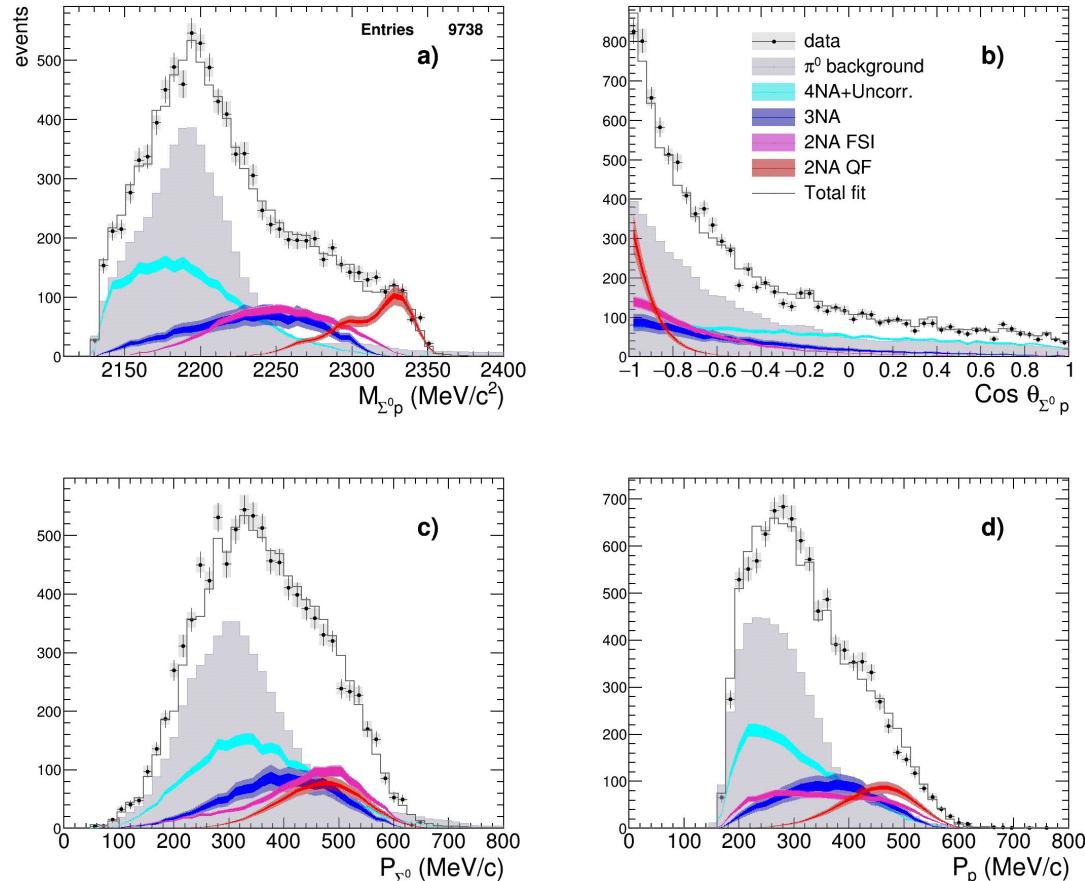


$\Sigma^0 p$ analysis: $K^- + ^{12}C \rightarrow \Sigma^0 + p + R$

Simultaneous fit of:

- $\Sigma^0 p$ invariant mass;
- angular correlation;
- proton momentum;
- Σ^0 momentum.

Total reduced χ^2 : $\chi^2/dof = 0.85$



[O. Vazquez Doce, L. Fabbietti et al.,
Phys.Lett. B 758, 134-139 (2016)]

$\Sigma^0 p$ analysis: $K^- + ^{12}C \rightarrow \Sigma^0 + p + R$

Simultaneous fit of:

- $\Sigma^0 p$ invariant mass;
- angular correlation;
- proton momentum;
- Σ^0 momentum.

Total reduced χ^2 : $\chi^2/dof = 0.807$

Best solution:

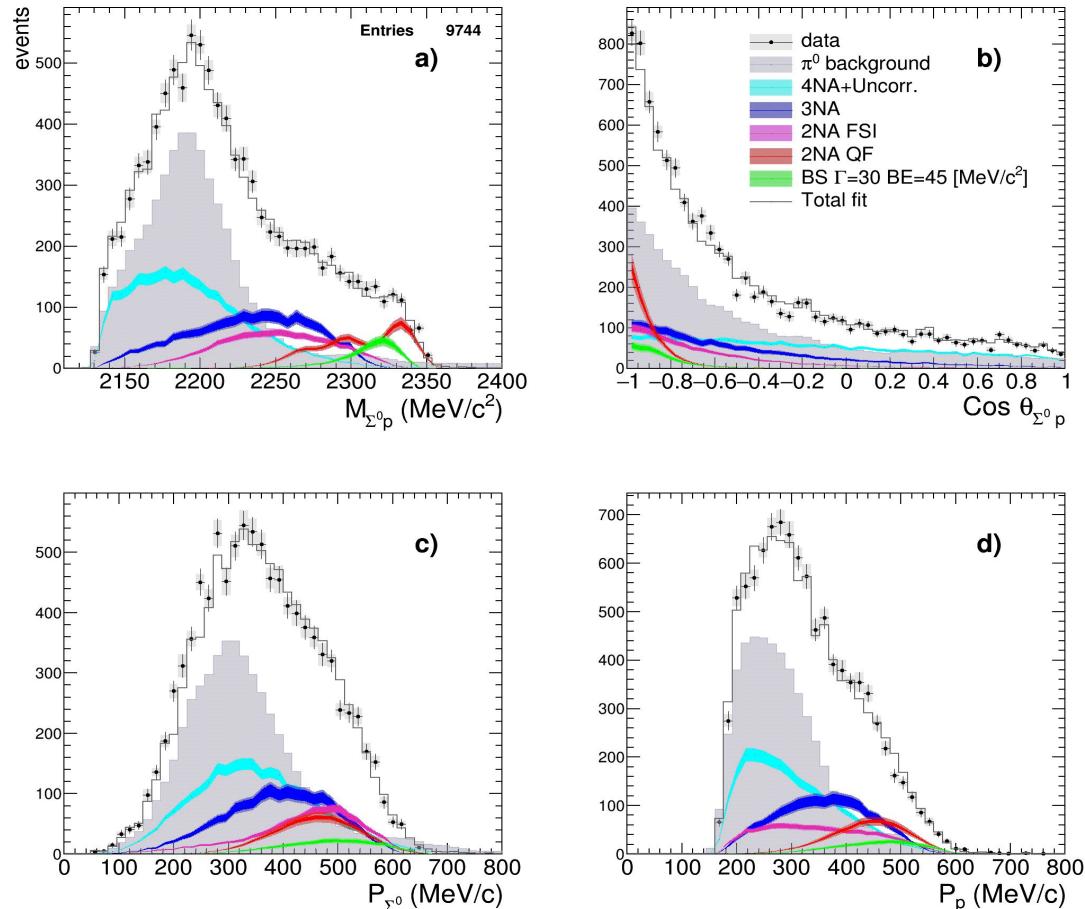
(best χ^2 and higher yield)

- $B = 45 \text{ MeV}/c^2$
- $\Gamma = 30 \text{ MeV}/c^2$

Statistical significance of 1σ

(evaluated by means of F-test method)

[O. Vazquez Doce, L. Fabbietti et al.,
Phys.Lett. B 758, 134-139 (2016)]

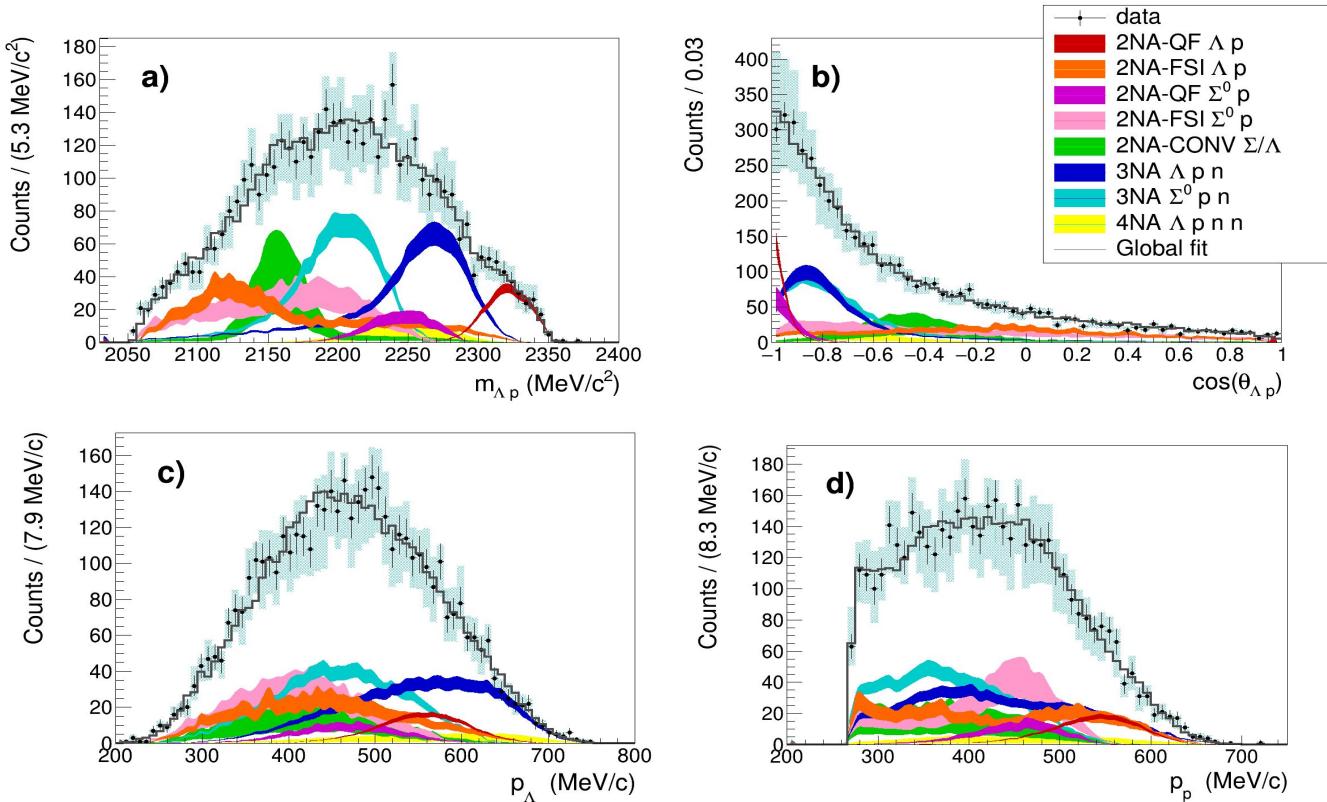


Λp analysis: $K^- + {}^{12}C \rightarrow \Lambda + p + R$

Simultaneous fit of:

- Λp invariant mass;
- angular correlation;
- proton momentum;
- Λ momentum.

Total reduced χ^2 : $\chi^2/dof = 0.94$



[R. Del Grande, K. Piscicchia, O. Vazquez Doce et al., Eur.Phys.J. C79 (2019) no.3, 190]
[R. Del Grande, K. Piscicchia, S. Wycech, Acta Phys. Pol. B 48 (2017) 1881]

Λp analysis: K^- multi-nucleon absorption BRs and σ

[R. Del Grande, K. Piscicchia, O. Vazquez Doce et al., Eur.Phys.J.C79 (2019) no.3, 190]

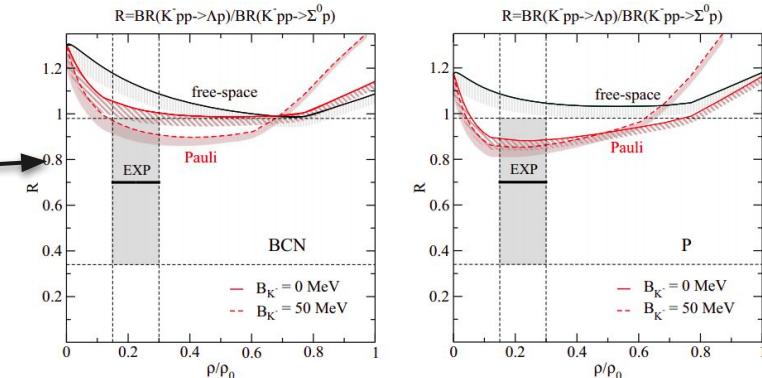
Process	Branching Ratio (%)	σ (mb)	@	p_K^- (MeV/c)
2NA-QF Λp	0.25 ± 0.02 (stat.) $^{+0.01}_{-0.02}$ (syst.)	2.8 ± 0.3 (stat.) $^{+0.1}_{-0.2}$ (syst.)	@	128 ± 29
2NA-FSI Λp	6.2 ± 1.4 (stat.) $^{+0.5}_{-0.6}$ (syst.)	69 ± 15 (stat.) ± 6 (syst.)	@	128 ± 29
2NA-QF $\Sigma^0 p$	0.35 ± 0.09 (stat.) $^{+0.13}_{-0.06}$ (syst.)	3.9 ± 1.0 (stat.) $^{+1.4}_{-0.7}$ (syst.)	@	128 ± 29
2NA-FSI $\Sigma^0 p$	7.2 ± 2.2 (stat.) $^{+4.2}_{-5.4}$ (syst.)	80 ± 25 (stat.) $^{+46}_{-60}$ (syst.)	@	128 ± 29
2NA-CONV Σ/Λ	2.1 ± 1.2 (stat.) $^{+0.9}_{-0.5}$ (syst.)	-		
3NA $\Lambda p n$	1.4 ± 0.2 (stat.) $^{+0.1}_{-0.2}$ (syst.)	15 ± 2 (stat.) ± 2 (syst.)	@	117 ± 23
3NA $\Sigma^0 p n$	3.7 ± 0.4 (stat.) $^{+0.2}_{-0.4}$ (syst.)	41 ± 4 (stat.) $^{+2}_{-5}$ (syst.)	@	117 ± 23
4NA $\Lambda p n n$	0.13 ± 0.09 (stat.) $^{+0.08}_{-0.07}$ (syst.)	-		
Global $\Lambda(\Sigma^0)p$	21 ± 3 (stat.) $^{+5}_{-6}$ (syst.)	-		

The ratio between the branching ratios of the 2NA-QF in the Λp channel and in the $\Sigma^0 p$ is measured to be:

$$\mathcal{R} = \frac{BR(K^- pp \rightarrow \Lambda p)}{BR(K^- pp \rightarrow \Sigma^0 p)} = 0.7 \pm 0.2 \text{ (stat.)}^{+0.2}_{-0.3} \text{ (syst.)}$$

and the ratio between the corresponding phase spaces is $\mathcal{R}' \simeq 1.22$.

Information on the in-medium dynamics



[J. Hrtáková and A. Ramos. Phys. Rev. C, 101(3):035204, 2020]

Total BR of the K⁻ 2NA process in ¹²C

Hyperon-nucleon pairs produced in K⁻2NA process:

Λp Λn $\Sigma^0 p$ $\Sigma^0 n$ $\Sigma^+ n$ $\Sigma^- p$ $\Sigma^- n$

BCN calculation at $0.3 \rho_0$ (baryon density in ¹²C) → BR(K⁻2NA → YN) = (15.4 ± 2.2) %
[J. Hrtánková and A. Ramos. Phys. Rev. C, 101(3):035204, 2020]

Process	Branching Ratio (%)
2NA-QF Λp	0.25 ± 0.02 (stat.) $^{+0.01}_{-0.02}$ (syst.)
2NA-FSI Λp	6.2 ± 1.4 (stat.) $^{+0.5}_{-0.6}$ (syst.)
2NA-QF $\Sigma^0 p$	0.35 ± 0.09 (stat.) $^{+0.13}_{-0.06}$ (syst.)
2NA-FSI $\Sigma^0 p$	7.2 ± 2.2 (stat.) $^{+4.2}_{-5.4}$ (syst.)
2NA-CONV Σ/Λ	2.1 ± 1.2 (stat.) $^{+0.9}_{-0.5}$ (syst.)
3NA $\Lambda p n$	1.4 ± 0.2 (stat.) $^{+0.1}_{-0.2}$ (syst.)
3NA $\Sigma^0 p n$	3.7 ± 0.4 (stat.) $^{+0.2}_{-0.4}$ (syst.)
4NA $\Lambda p n n$	0.13 ± 0.09 (stat.) $^{+0.08}_{-0.07}$ (syst.)
Global $\Lambda(\Sigma^0)p$	21 ± 3 (stat.) $^{+5}_{-6}$ (syst.)

We measure a total K⁻2NA BR in ¹²C

$\rightarrow (16.1 \pm 2.9 \text{ (stat.)} ^{+4.3}_{-5.5} \text{ (syst.)})\%$,

Λp and $\Sigma^0 p$ pairs in the final state....

....information on the remaining YN
pairs provided by FSI e Conversion
reactions

[R. Del Grande, K. Piscicchia et al., 2020 Phys. Scr. 95 084012]

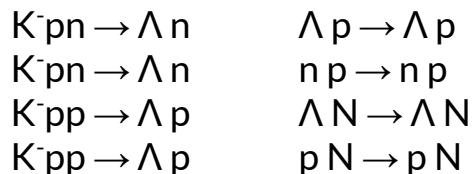
Total BR of the K^- 2NA process in ^{12}C

FSI and Conversion reactions contributing to the measured BRs

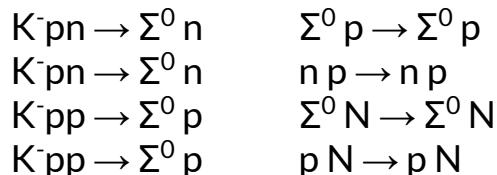
primary interaction

secondary interaction

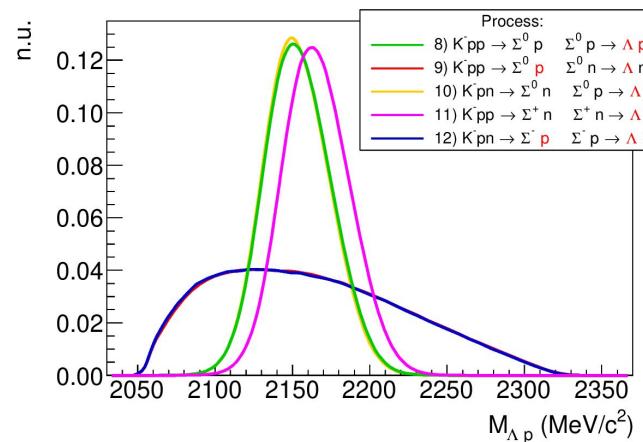
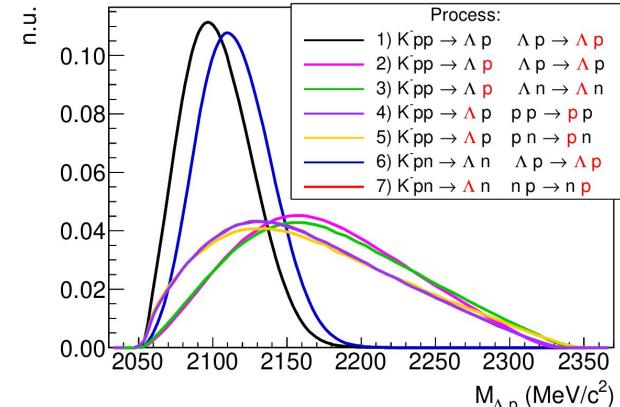
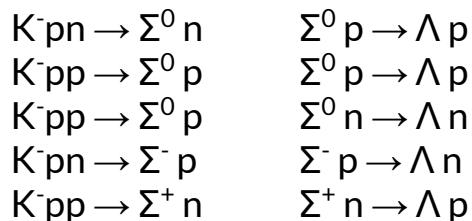
2NA-FSI Λp



2NA-FSI $\Sigma^0 p$



2NA-Conv.



red = detected
 Λp pair

Total BR of the K⁻ 2NA process in ¹²C

the only missing components are:

- $\text{BR}(\Sigma^-\text{n}) = (0.12 \pm 0.01\text{(syst.)})\%$
- $\text{BR}(\text{QF-}\Lambda\text{n} + \text{QF-}\Sigma^0\text{n}) = (0.76 \pm 0.09\text{(stat.)}^{+0.13}_{-0.06}\text{(syst.)})\%$
- $\text{BR}(\text{FSI-}\Lambda\text{n} + \text{FSI-}\Sigma^0\text{n}) = (1.62 \pm 0.04\text{(stat.)}^{+0.22}_{-0.21}\text{(syst.)})\%$
- $\text{BR}(\text{no conv } \Sigma^+ \text{ and } \Sigma^-) = (3.04 \pm 0.03\text{(stat.)} \pm 0.92\text{(syst.)})\%$

$$\rightarrow (5.5 \pm 0.1\text{(stat.)}^{+1.0}_{-0.9}\text{(syst.)})\%$$

[R. Del Grande, K. Piscicchia et al., 2020 Phys. Scr. 95 084012]

[R. Del Grande, K. Piscicchia et al., Few Body Syst. 62 (2021) 1, 7]

Including the missing components the total BR of the K⁻2NA is:

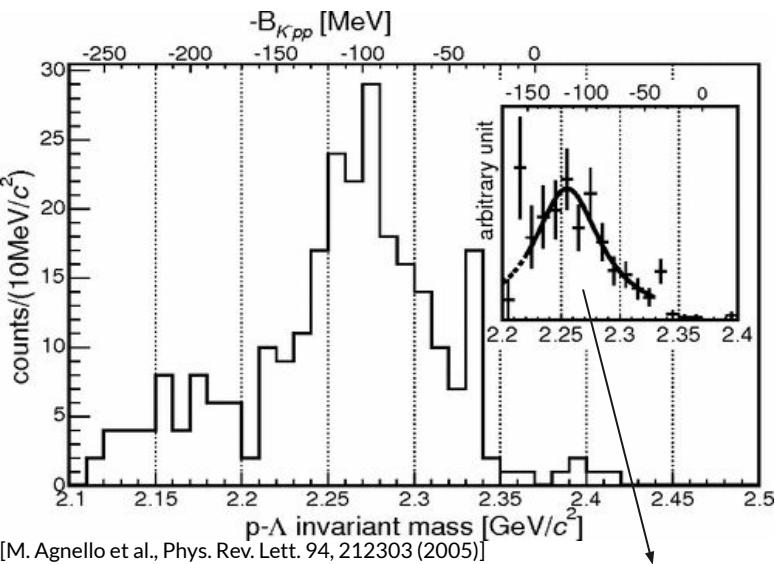
$$\text{BR}(K^-\text{2NA} \rightarrow YN) = (21.6 \pm 2.9\text{(stat.)}^{+4.4}_{-5.6}\text{(syst.)})\%$$

Experimental search in K^- induced reactions

FINUDA at DAΦNE: $K^-_{\text{stop}} + X \rightarrow \Lambda + p + X'$

only back-to-back Λp pairs ($\cos\theta_{\Lambda p} < -0.8$)

detected particles



[M. Agnello et al., Phys. Rev. Lett. 94, 212303 (2005)]

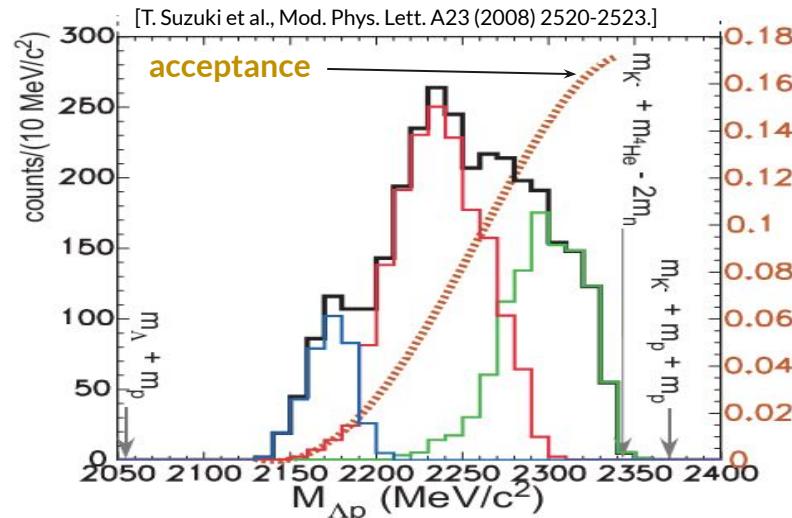
Interpreted as the signal of:
extracted parameters: $K^- pp \rightarrow \Lambda + p$

$$BE = (115^{+6}_{-5} \text{ (stat.)}^{+3}_{-4} \text{ (syst.)}) \text{ MeV}$$

$$\Gamma = (67^{+14}_{-11} \text{ (stat.)}^{+2}_{-3} \text{ (syst.)}) \text{ MeV}/c^2$$

E549 at KEK: $K^-_{\text{stop}} + {}^4\text{He} \rightarrow \Lambda + p + X'$

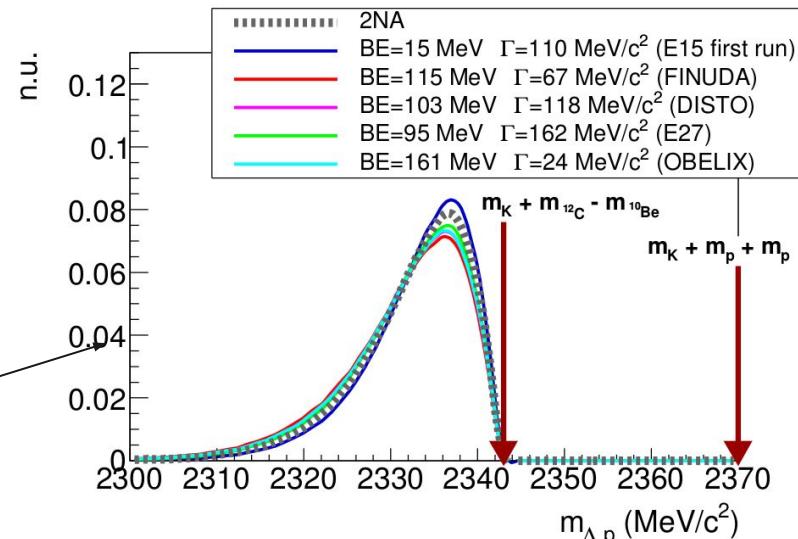
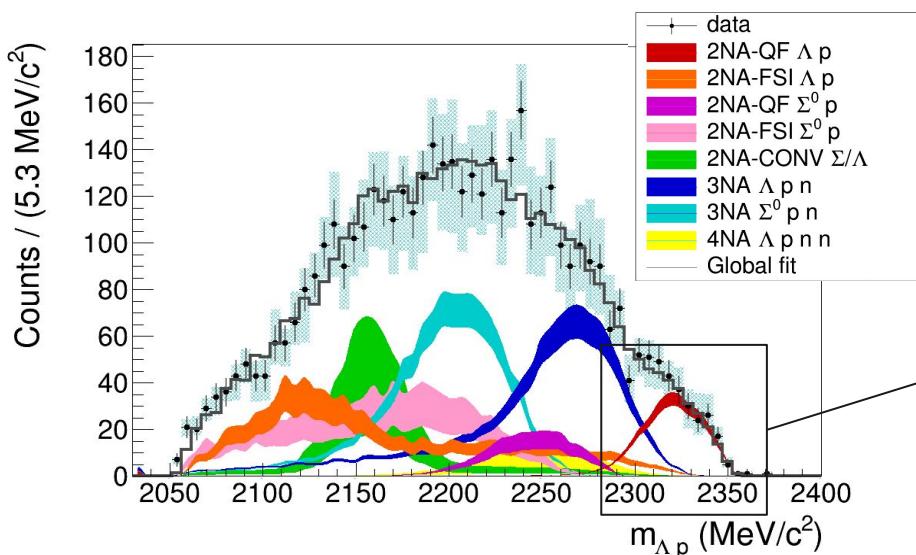
detected particles



Using the missing mass information, three components to the invariant mass spectrum are found:

- **1NA:** K^- single nucleon absorption
- **2NA:** K^- two nucleon absorption
- **2NA + conversion, multi-nucleon, or Bound State?**

Λp analysis: $K^- pp$ bound state

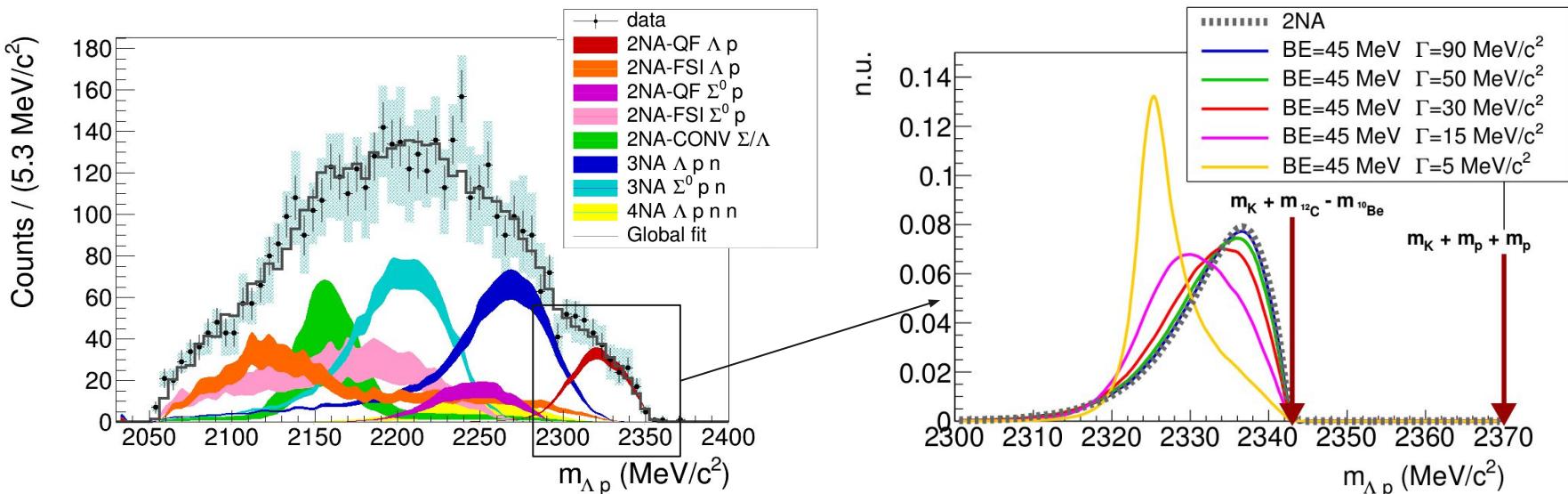


$K^- pp$ bound state contribution completely overlaps with the $K^- 2NA$

[R. Del Grande, K. Piscicchia, O. Vazquez Doce et al., Eur.Phys.J. C79 (2019) no.3, 190]

[R. Del Grande, K. Piscicchia, S. Wycech, Acta Phys. Pol. B 48 (2017) 1881]

Λp analysis: $K^- pp$ bound state

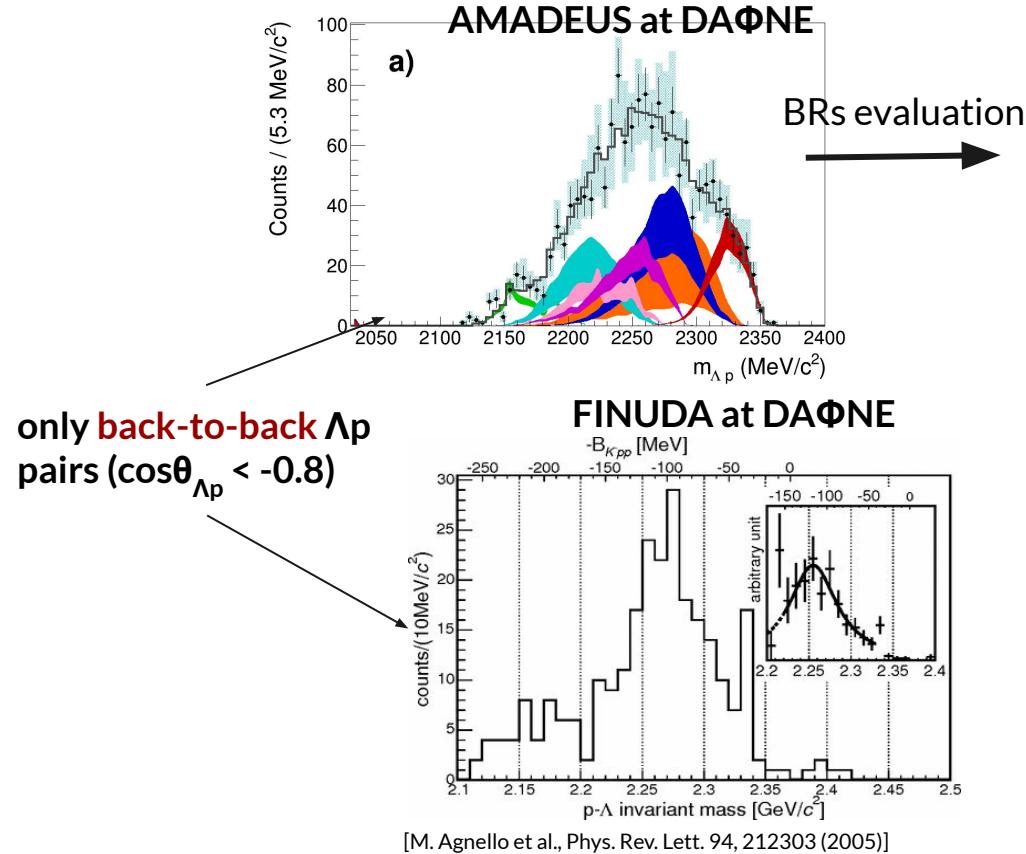


$K^- pp$ bound state contribution completely overlaps with the $K^- 2NA$

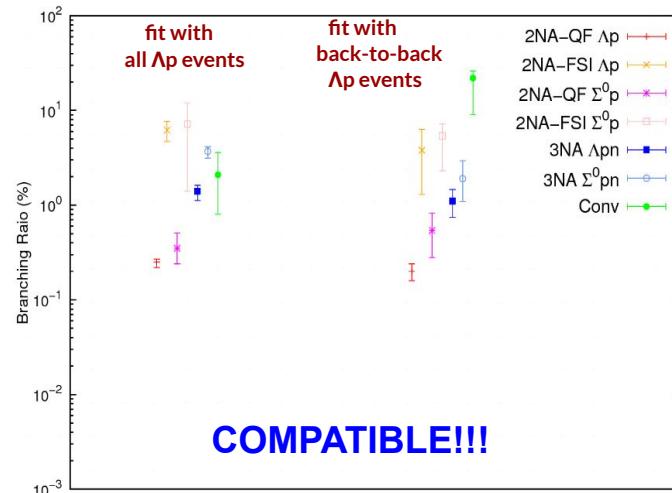
[R. Del Grande, K. Piscicchia, O. Vazquez Doce et al., Eur.Phys.J. C79 (2019) no.3, 190]

[R. Del Grande, K. Piscicchia, S. Wycech, Acta Phys. Pol. B 48 (2017) 1881]

Λp analysis: $K^- pp$ bound state search



Process	Branching Ratio (%)
2NA-QF Λp	$0.20 \pm 0.04(\text{stat.}) \pm 0.02(\text{syst.})$
2NA-FSI Λp	$3.8 \pm 2.3(\text{stat.}) \pm 1.1(\text{syst.})$
2NA-QF $\Sigma^0 p$	$0.54 \pm 0.20(\text{stat.})^{+0.20}_{-0.16}(\text{syst.})$
2NA-FSI $\Sigma^0 p$	$5.4 \pm 1.5(\text{stat.})^{+1.0}_{-2.7}(\text{syst.})$
2NA-CONV Σ/Λ	$22 \pm 4(\text{stat.})^{+1}_{-12}(\text{syst.})$
3NA $\Lambda p n$	$1.1 \pm 0.3(\text{stat.}) \pm 0.2(\text{syst.})$
3NA $\Sigma^0 p n$	$1.9 \pm 0.7(\text{stat.})^{+0.8}_{-0.4}(\text{syst.})$



Λ t analysis: Cross section and BR for 4NA

GOLDEN CHANNEL to extrapolate the K^- 4NA



Previous data:

- in ^4He : bubble chamber experiment

/M. Roosen, J. H. Wickens, Il Nuovo Cimento 66, 101 (1981)/

only 3 events compatible with Λ t kinematics found

$$\text{BR}(K^- \text{He} \rightarrow \Lambda t) = (3 \pm 2) \times 10^{-4} / K_{\text{stop}} \rightarrow \text{global, no 4NA}$$

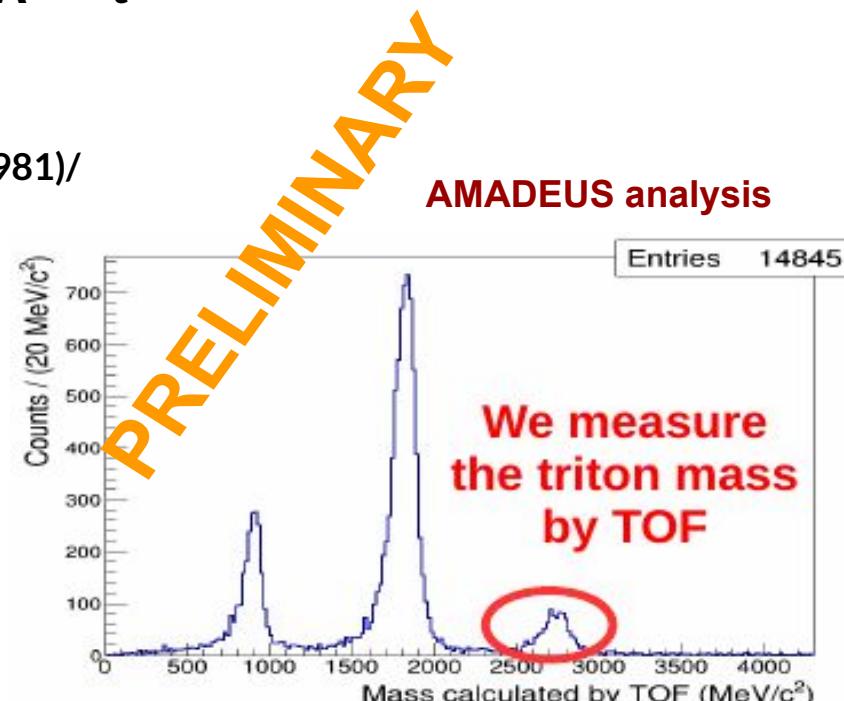
- in solid targets: $^{6,7}\text{Li}$, ^9Be (FINUDA)

/Phys. Lett. B, 229 (2008)/

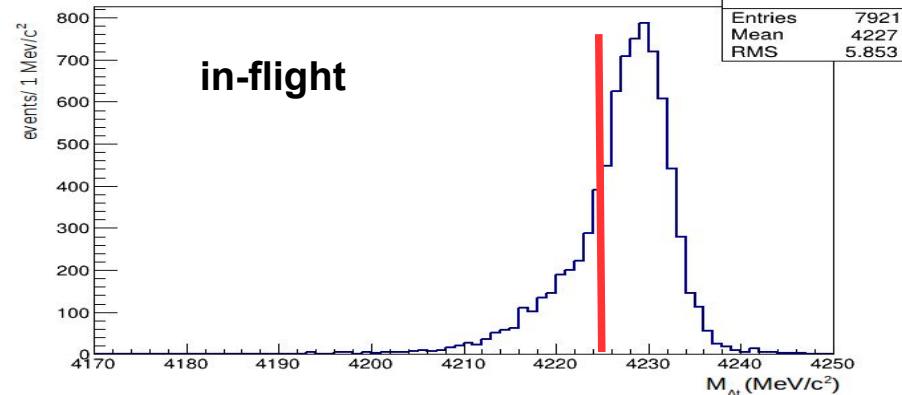
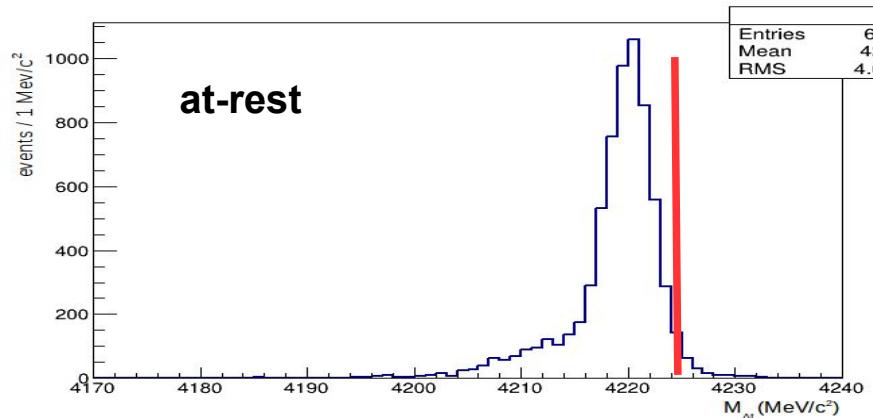
40 events, only back-to-back data

$$\Lambda t \text{ emission yield} \rightarrow 10^{-3} - 10^{-4} / K_{\text{stop}}$$

\rightarrow global, no 4NA



MC simulations: efficiency & resolution



mass threshold at-rest

$$M_{\Lambda t} \text{ invariant mass resolution} = 2.2 \text{ MeV}/c^2$$

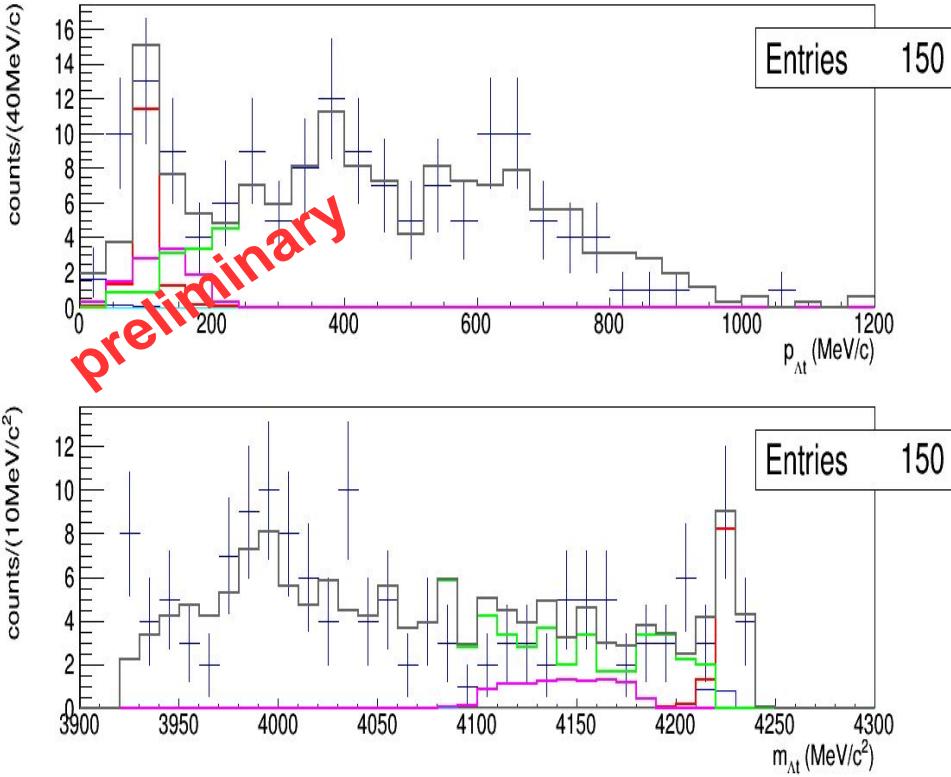
overall detection + reconstruction efficiency for 4NA direct Λt production :

$$\epsilon_{4\text{NA},ar,\Lambda t} = 0.0493 \pm 0.0006 \quad ; \quad \epsilon_{4\text{NA},if,\Lambda t} = 0.0578 \pm 0.0006,$$

at-rest

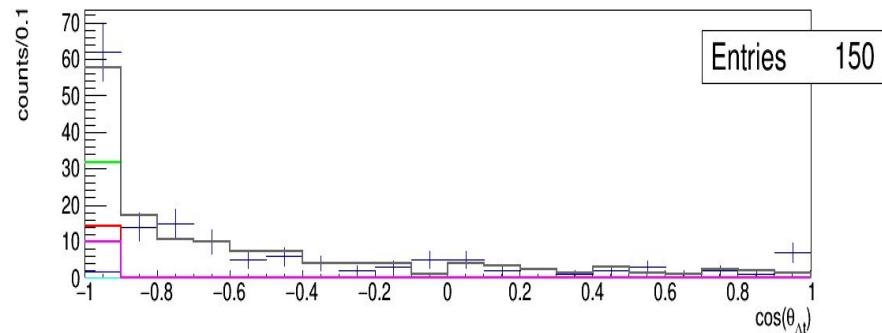
in-flight

Λt analysis: Cross section and BR for 4NA in $K^- {}^4He \rightarrow \Lambda t$ process



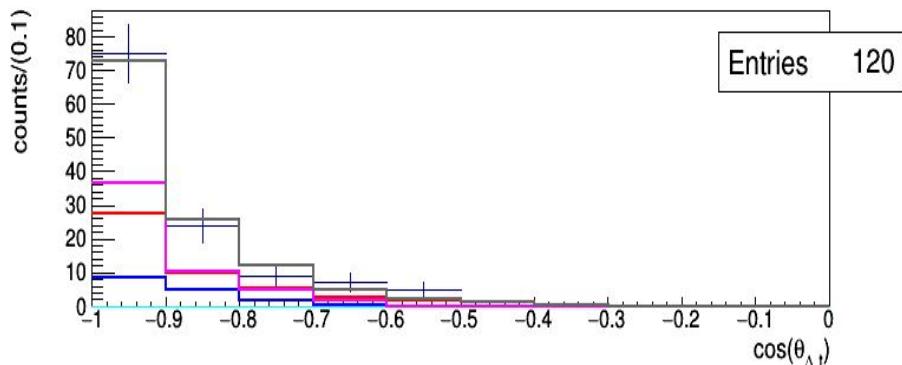
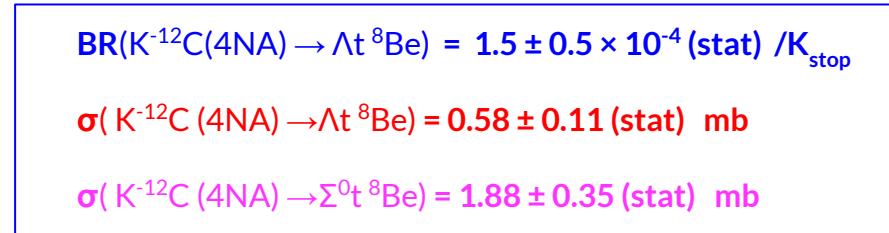
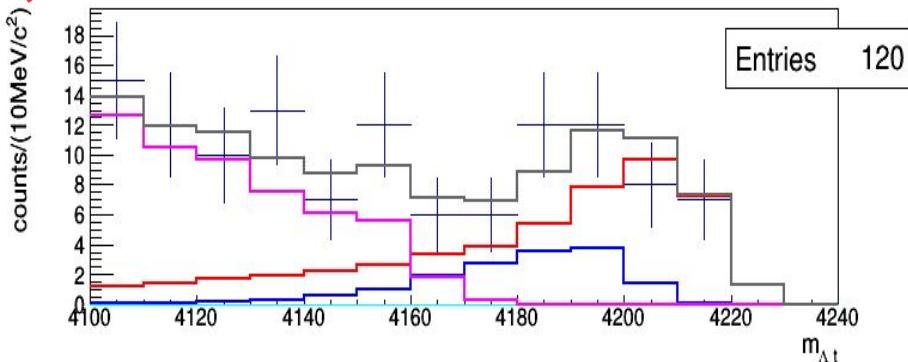
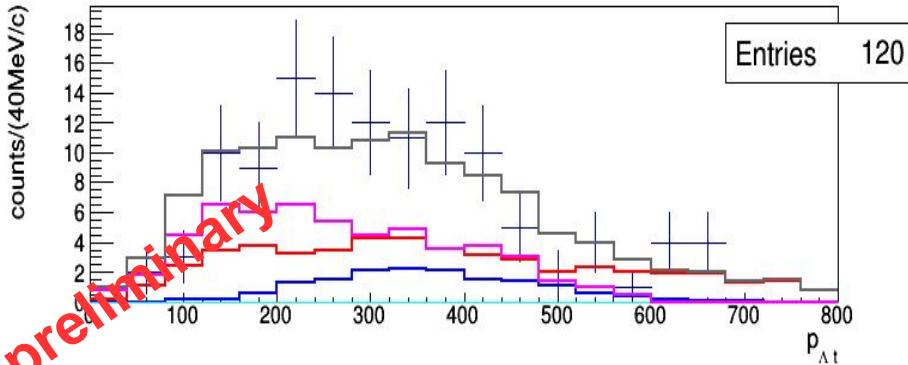
$BR(K^- {}^4He(4NA) \rightarrow \Lambda t) < 2.0 \times 10^{-4} / K_{stop}$ (95% c. l.)

$\sigma(100 \pm 19 \text{ MeV/c}) (K^- {}^4He(4NA) \rightarrow \Lambda t) =$
 $= (0.81 \pm 0.21 \text{ (stat)} {}^{+0.03}_{-0.04} \text{ (syst)}) \text{ mb}$



Λ t analysis: Cross section and BR for 4NA in $K^- {}^4He \rightarrow \Lambda t$ process

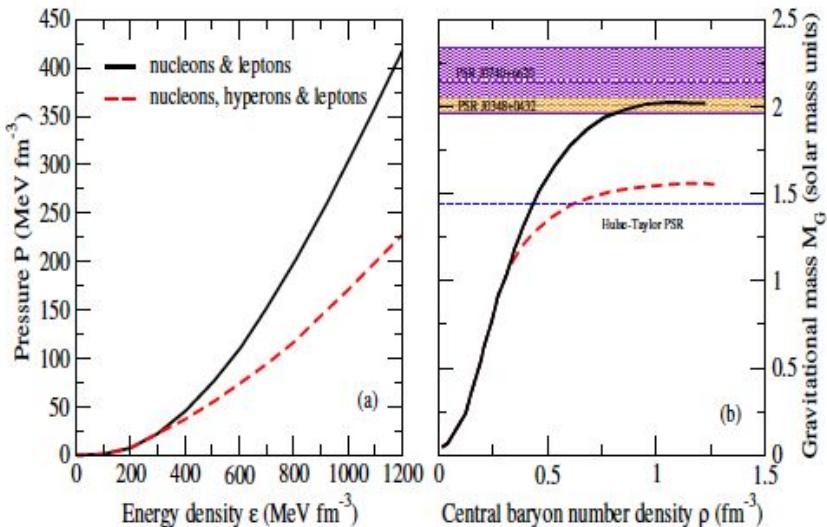
preliminary



NEUTRON STARS - the Hyperon puzzle

Hyperons may appear in the inner n.s. core for $2-3 \rho_0 \rightarrow$ nucleons into hyperons conversion
relieves Fermi pressure \rightarrow softer EoS \rightarrow less mass can be sustained

see e.g. S. Balberg, A. Gal, Nucl. Phys. A625 (1997) 435, L. Tolos, M. Centelles, A. Ramos, Astron. Soc. Austral. 34 (2017), D. Lonardoni, F. Pederiva, S. Gandolfi, Phys. Rev. C89 (1) (2014) 014314., H. J. Schulze, A. Polls, A. Ramos, I. Vidana, Phys. Rev. C73 (2006), Wiktorowicz, G.; Drago, A.; Pagliara, G.; Popov, S.B. Astrophys. J. 2017, 846, 163.



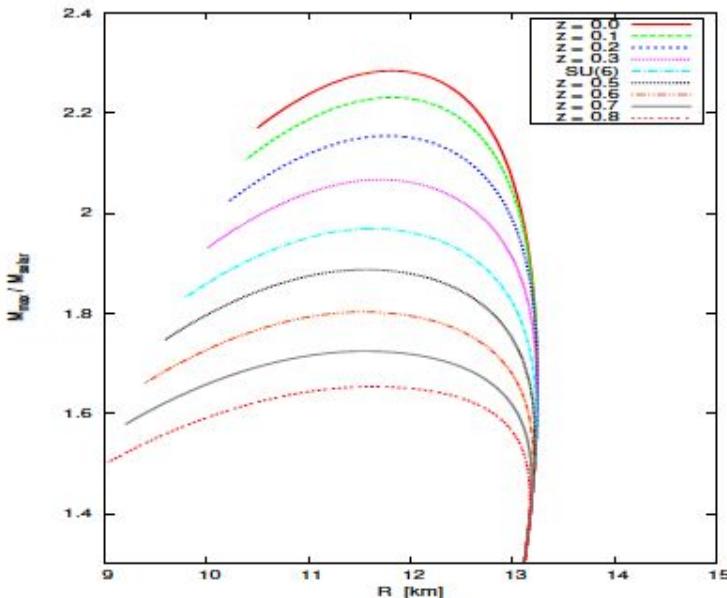
Especially in microscopic models
the maximum reachable mass is
not compatible with the 2 solar
mass observations!

Figure from L. Tolos, L. Fabbietti,
Progress in Particle and
Nuclear Physics, Volume 112,
2020

Hyperon puzzle - Y-N, Y-Y interaction

possible way out stiff Y-N / Y-Y interaction explored in RMF models → vectors mesons exchange among baryons leads to a repulsive behaviour of the baryon-baryon interaction

see e.g. K. A. Maslov, E. E. Kolomeitsev, D. N. Voskresensky, Phys. Lett. B748 (2015), S. Weissenborn, D. Chatterjee, J. Schaner-Bielich, Phys. Rev. C85 (6) (2012)

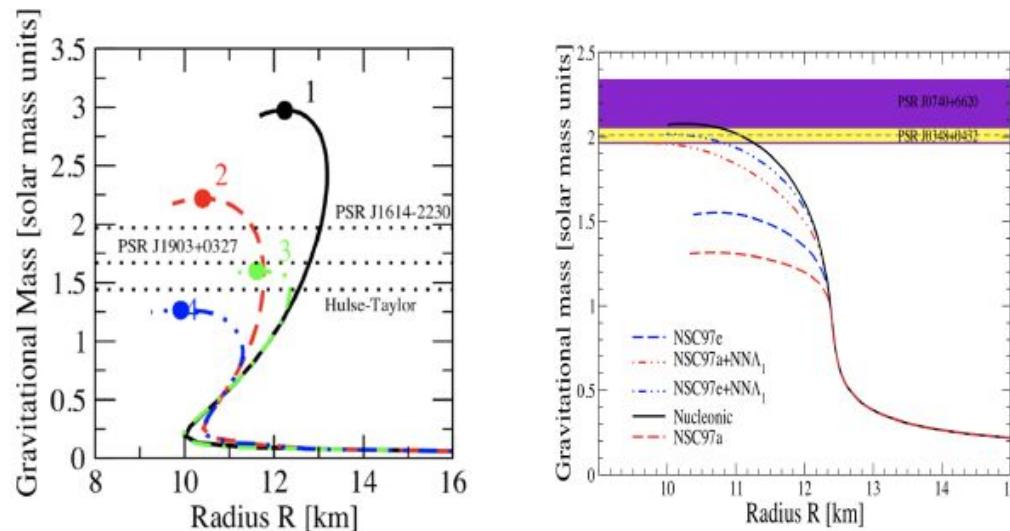


**z parameter accounts for the singlet
and octet meson coupling
constants to baryons**

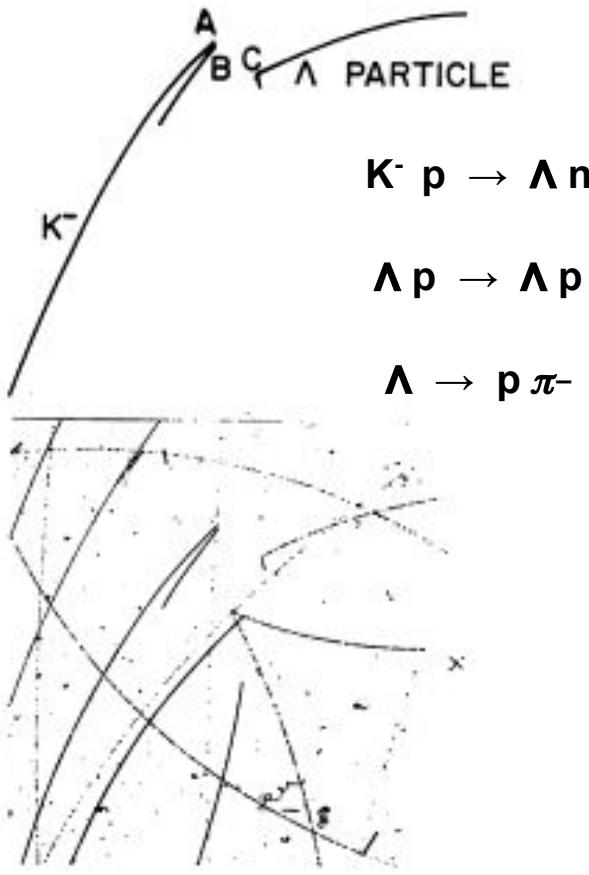
Hyperon puzzle - three body forces

The hyperonic three-body forces, as in the case of three-nucleon forces, might induce an additional repulsion at high densities so as to make the EoS stiff enough

strongly model dependent: see e.g. I. Vidana, D. Logoteta, C. Providencia, A. Polls, I. Bombaci, EPL 94 (1) (2011) (**Fig. left curves 1,2 nucleons only, curves 3,4 nucleons and hyperons**), D. Logoteta, I. Vidana, I. Bombaci, Eur. Phys. J. A55 (11) (2019) (**Fig. right dashed dotted lines with 3BF NNA reaches 2Sol Mass**), D. Lonardoni, A. Lovato, S. Gandolfi, F. Pederiva, Phys. Rev. Lett. 114 (9) (2015)



Y-N experimental information from scattering experiments



- Hydrogen bubble chamber exposed to a secondary K- beam.
- The stopped K- particle and the resulting charged products identified looking at the recorded photographs of the bubble chamber reactions.
- The following scattering of hyperons on protons and their weak decays are then tagged.

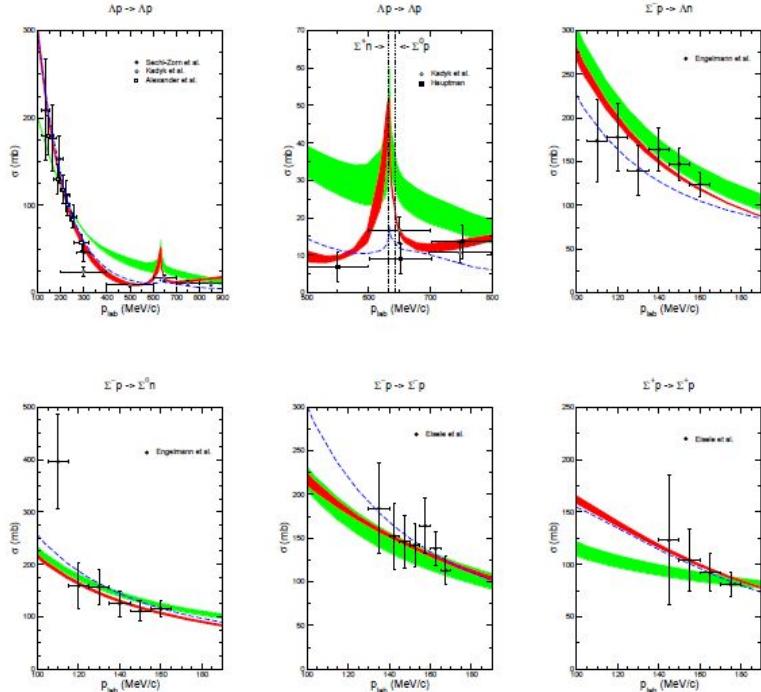
Phys. Lett. B37 (1971) 204-206.

Phys. Rev. 173 (1968) 1452-1460.

Phys. Rev. 175 (1968) 1735-1740.

J-PARC E40 aims to measure the differential cross sections of: $\Sigma^\pm p$ elastic scatterings, $\Sigma-p \rightarrow \Lambda n$ conversion, by means of the reaction $p(\pi^\pm, K^\pm)\Sigma^\pm$ using LH₂ target

No experimental information on Σ^0 -N/NN and in general on Y-NN interaction from scattering experiments



See e.g. Nucl. Phys. A 915 (2013) 24-58
Eur. Phys. J. A 51, 53 (2015),

and talk U. G. Meißner
for a discussion on hypernuclei physics

Figure 2: "Total" cross section σ (as defined in Eq. (24)) as a function of p_{lab} . The experimental cross sections are taken from Refs. [52] (filled circles), [53] (open squares), [65] (open circles), and [66] (filled squares) ($\Lambda p \rightarrow \Lambda p$), from [54] ($\Sigma^- p \rightarrow \Lambda n$, $\Sigma^+ p \rightarrow \Sigma^0 n$) and from [55] ($\Sigma^- p \rightarrow \Sigma^- p$, $\Sigma^+ p \rightarrow \Sigma^+ p$). The red/dark band shows the chiral EFT results to NLO for variations of the cutoff in the range $\Lambda = 500, \dots, 650$ MeV, while the green/light band are results to LO for $\Lambda = 550, \dots, 700$ MeV. The dashed curve is the result of the Jülich '04 meson-exchange potential [36].

Σ^0 -p & Λ - Λ by femtoscopy technique

Measurement of the correlation in the momentum space for (Y-p) (Y-Y) pairs exploiting the femtoscopy technique, a correlation function due to the background computed as baseline for Σ^0 -p.

arXiv:1910.14407.

S. Acharya, et al., Phys. Lett. B797 (2019)

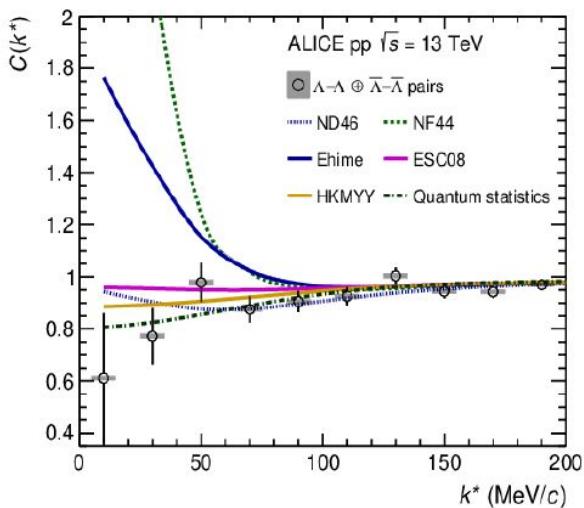
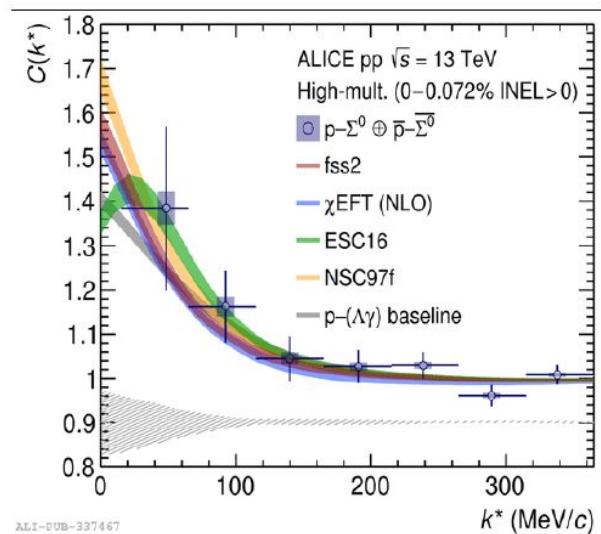


Figure from L. Tolos, L. Fabbietti,
Progress in Particle and Nuclear
Physics, Volume 112, 2020

Figure 31: (Color online) Left panel: $p\Sigma^0$ correlation function measured in pp collisions at $\sqrt{s} = 13$ TeV at the LHC by the ALICE collaboration [200]. Right panel: $\Lambda\Lambda$ correlation measured in pp collisions at $\sqrt{s} = 13$ TeV at the LHC by the ALICE collaboration [202].

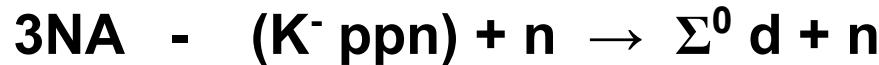


3NA in ${}^4\text{He}$

for the investigation of the

$\Sigma^0\text{-N}$ & $\Sigma^0\text{-(NN)}$ interaction

Involved reactions:



- The Σ^0 identification (with respect to Λ) enables to **avoid the internal conversion background**. Moreover there is presently no available Σ^0 -N scattering data.
- ${}^4\text{He}$ target → **no nuclear fragmentation can follow the 3NA primary process.**

+

3NA can be followed by two possible elastic FSI

- 1) $\text{n d} \rightarrow \text{n d}$ we may take advantage of the well known σ_{NN} data
- 2) $\Sigma^0 \text{n/d} \rightarrow \Sigma^0 \text{n/d}$ from which to extract information on Σ^0 -N , Σ^0 -(NN) interaction.

Involved reactions - signal:



- We show that the most energetic part of the $m_{\Sigma^0 d}$ invariant mass spectrum is correlated to high p_{Σ^0} and p_d momenta, this corresponds to the $3\text{NA} - (\text{K}^- \text{ppn})$ process.

The $\Sigma^0 \text{d}$ statistics from K- captures in the gas filling the KLOE DC is poor. Moreover K- in ^{12}C (from isobutane) are not distinguishable from K- captures on ^4He .

A dedicated measurement with pure ^4He target (^3He target also helpful for comparison) is mandatory for this purpose.

3NA



without FSI

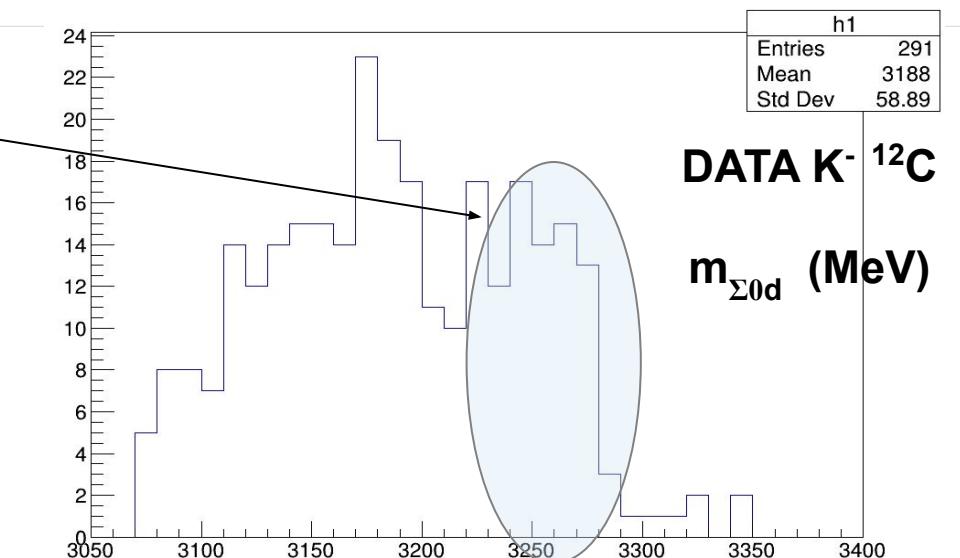
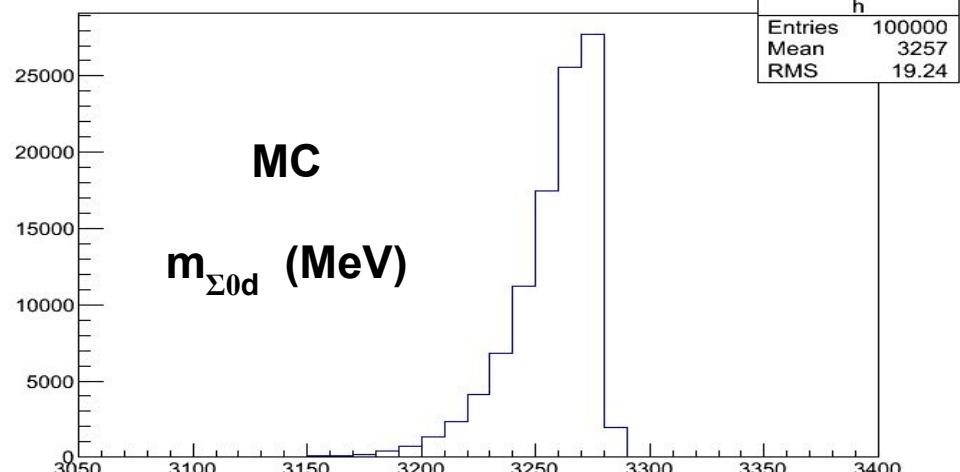
Corresponds to the highest part of the invariant mass spectrum

the blue region is populated by free 3NA,

at slightly lower energy is the 3NA followed by 2B & 3B FSI.

Our aim is to measure the relative contributions of the two processes.

At lower energies 2NA is involved and complex FSI processes with fragmentation of the residual ${}^8\text{Be}$ (not present in ${}^4\text{He}$ target).



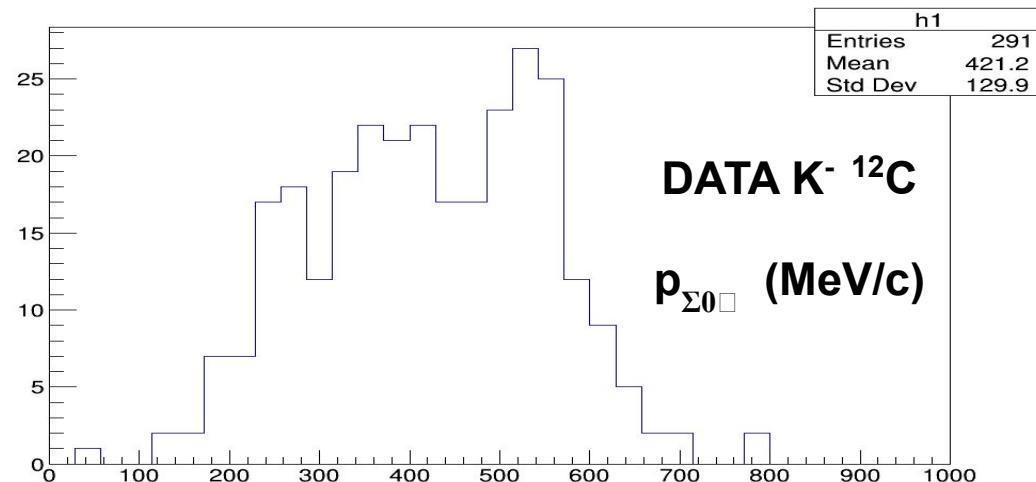
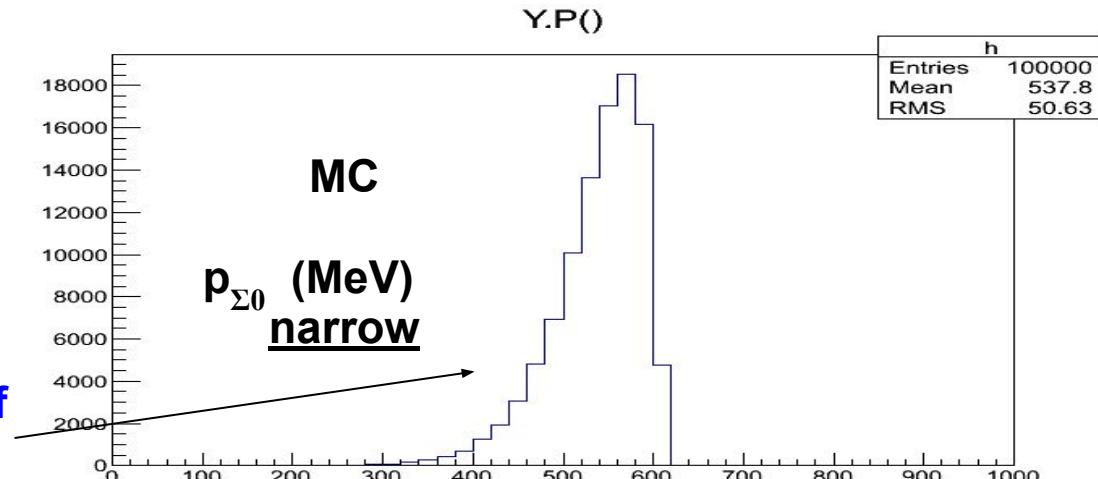
3NA



without FSI

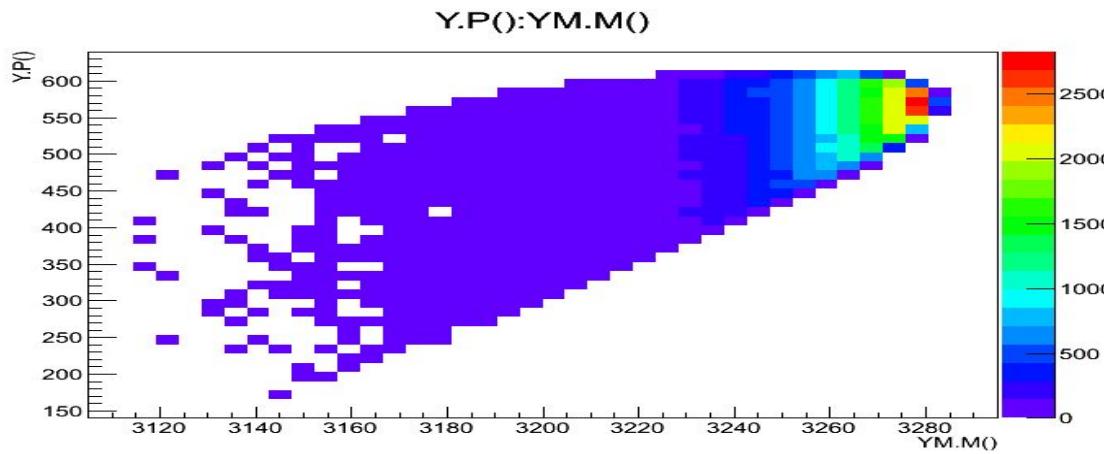
Corresponds to the highest part of
the Σ^0 momentum spectrum.

The narrow Σ^0 momentum
distribution will enable to measure
 Σ^0 -N and Σ^0 -NN cross section at
 550 ± 50 MeV/c.



3NA $(K^- ppn) + n \rightarrow \Sigma^0 d + n$ wo FSI

- clean momentum mass correlation

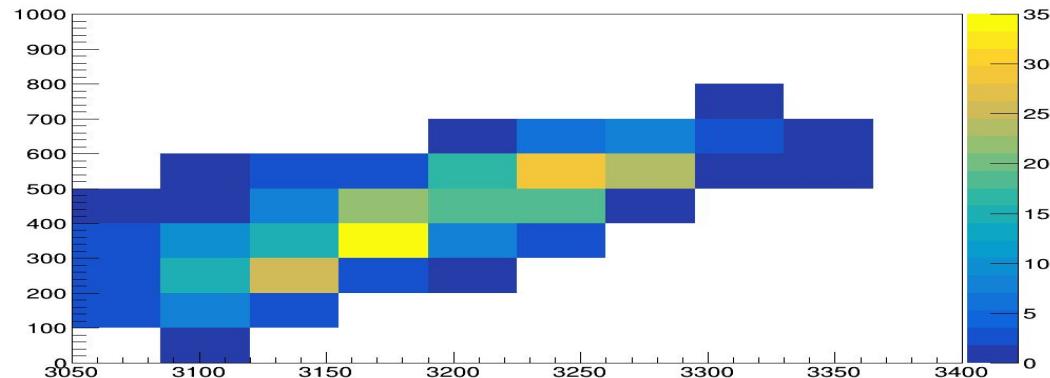


MC

$p_{\Sigma 0}$ vs $m_{\Sigma 0 d}$

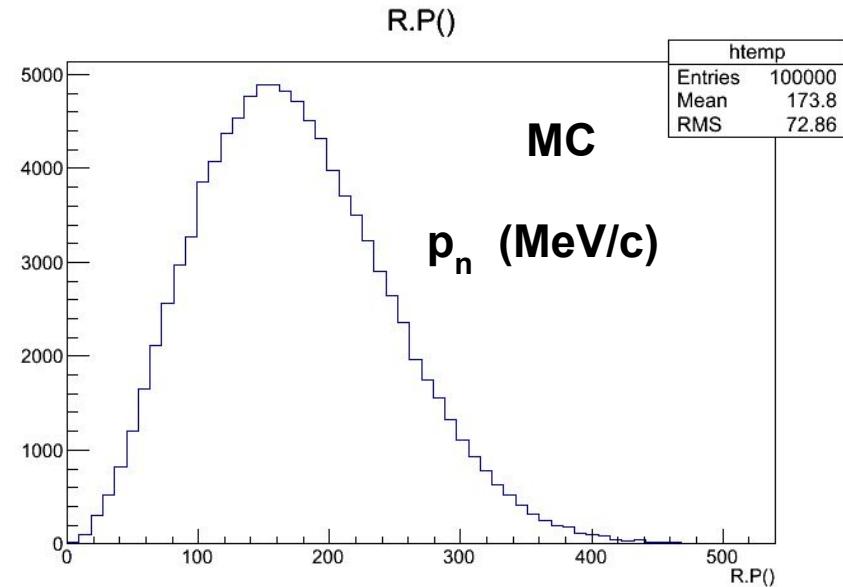
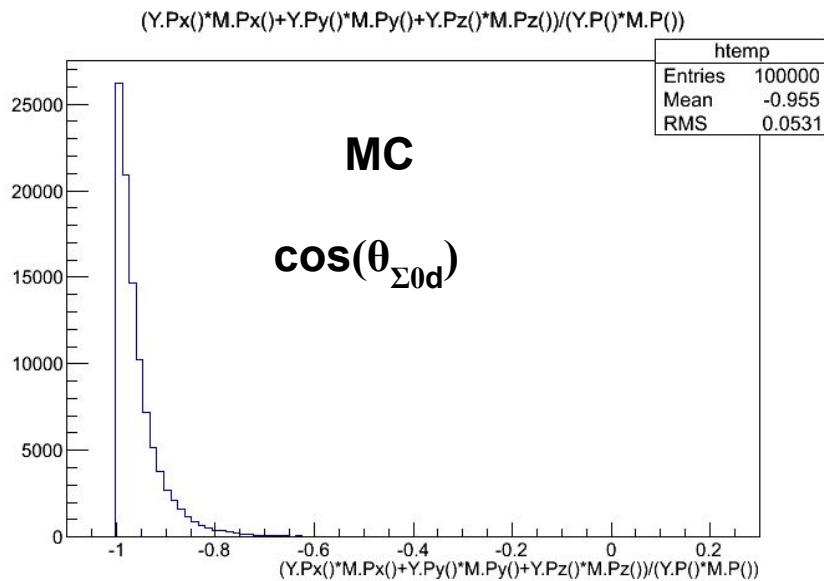
DATA $K^- {}^{12}C$

$p_{\Sigma 0}$ vs $m_{\Sigma 0 d}$

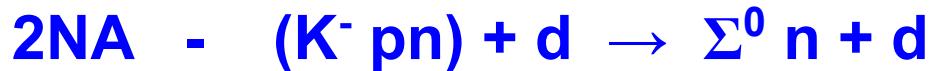


$3\text{NA} - (\text{K- ppn}) + \text{n} \rightarrow \Sigma^0 \text{ d} + \text{n}$ signature:

Highest Σ^0 - d angular correlation - low Fermi momentum neutron



Involved reactions - background:



+

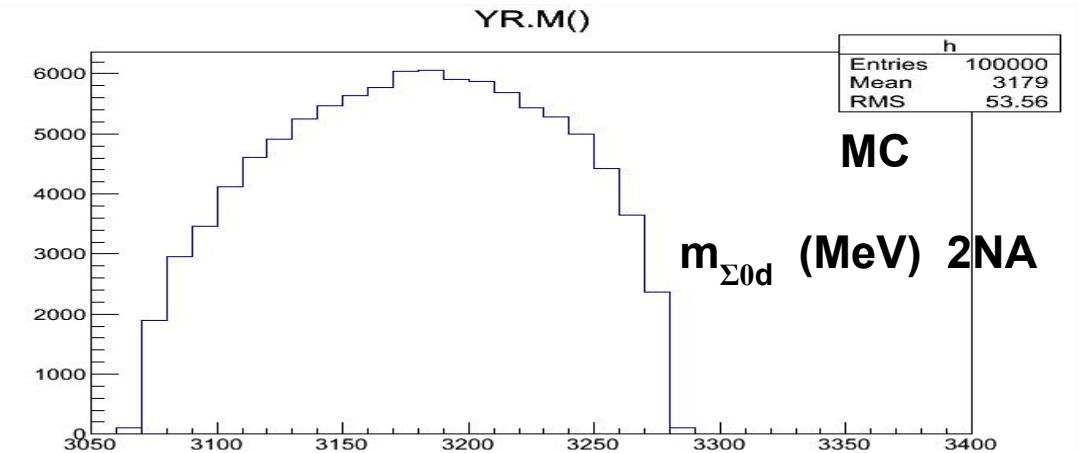
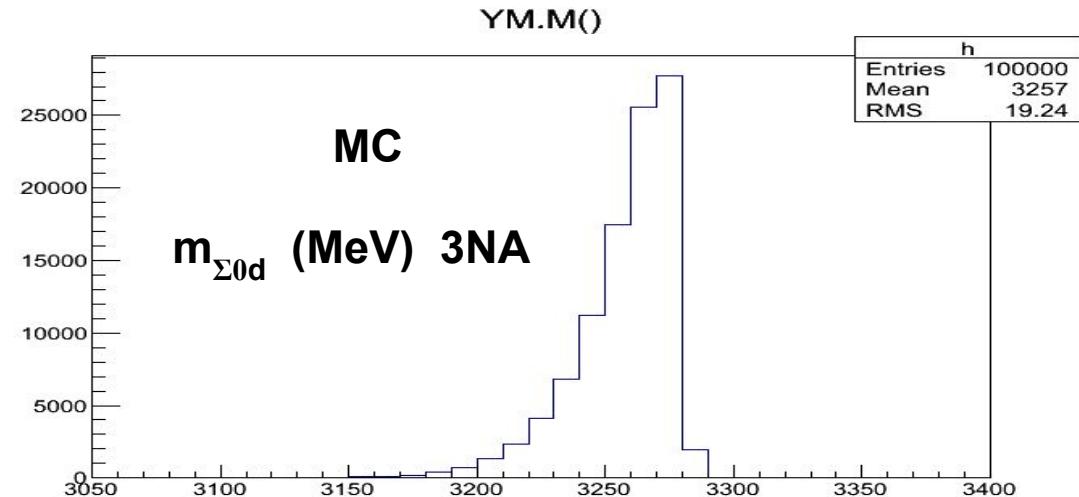
2 possible elastic FSI

1) $\text{n d} \rightarrow \text{n d}$ we may take advantage of the well known σ_{NN} data

2) $\Sigma^0 \text{d/n} \rightarrow \Sigma^0 \text{d/n}$ *well separated in the lower energy part of the final state phase space*

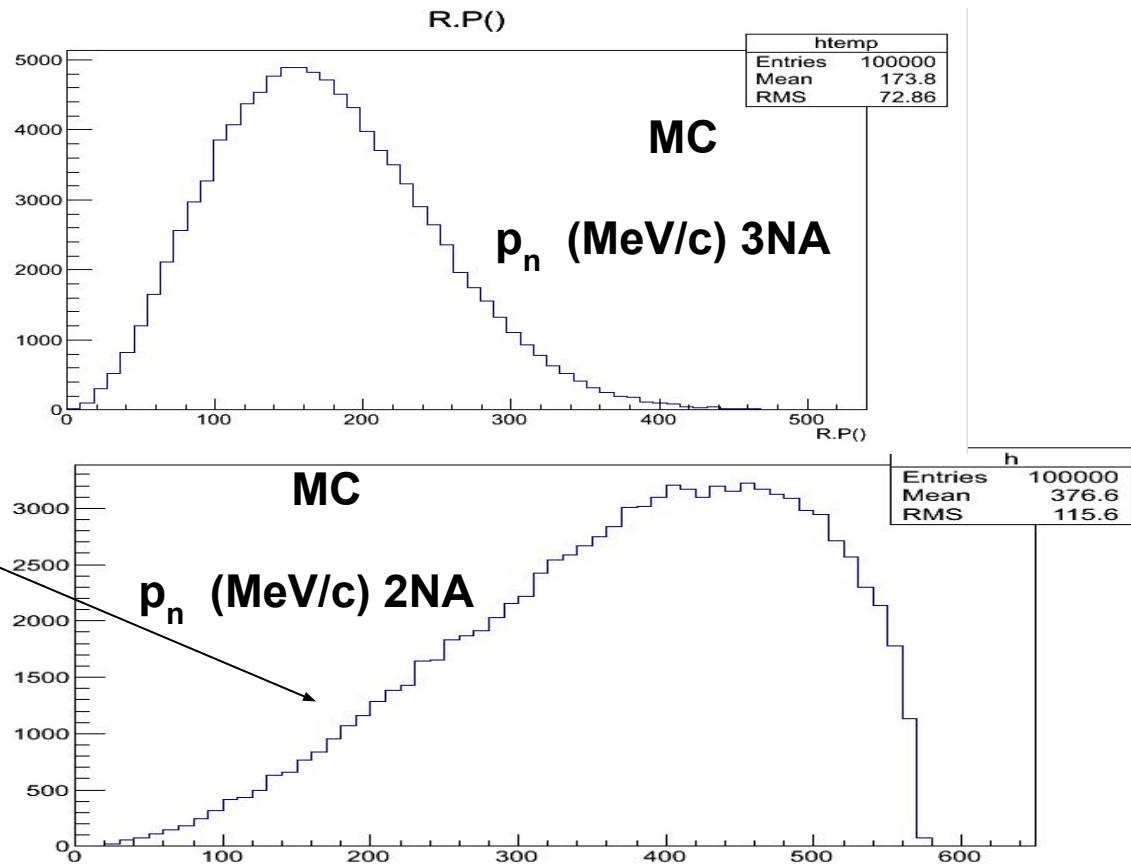
2NA

- $(K^- pn) + d \rightarrow \Sigma^0 n + d$
- lower invariant mass

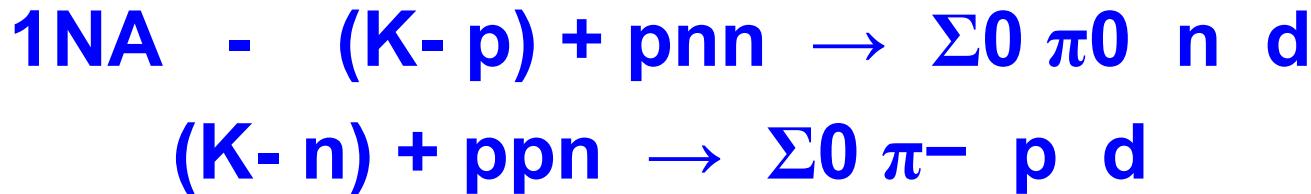


2NA

- $(K^- pn) + d \rightarrow \Sigma^0 n + d$
- high momentum neutrons



Involved reactions - background:



- low energy (took away by the pion) not correlated Σ^0 d pairs.
It is easy to be disentangled (similar to the Σ^0 p analysis).

Accurate model of the:



3NA in ${}^4\text{He}$

+

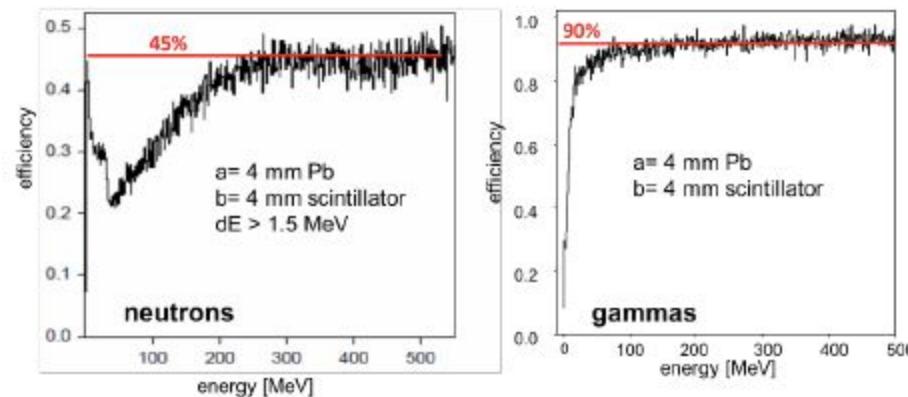
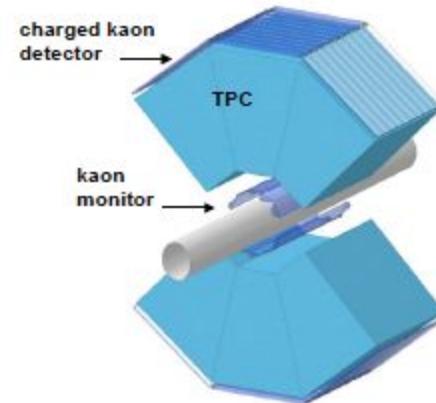


is needed to extract the corresponding cross sections from the measured shapes.

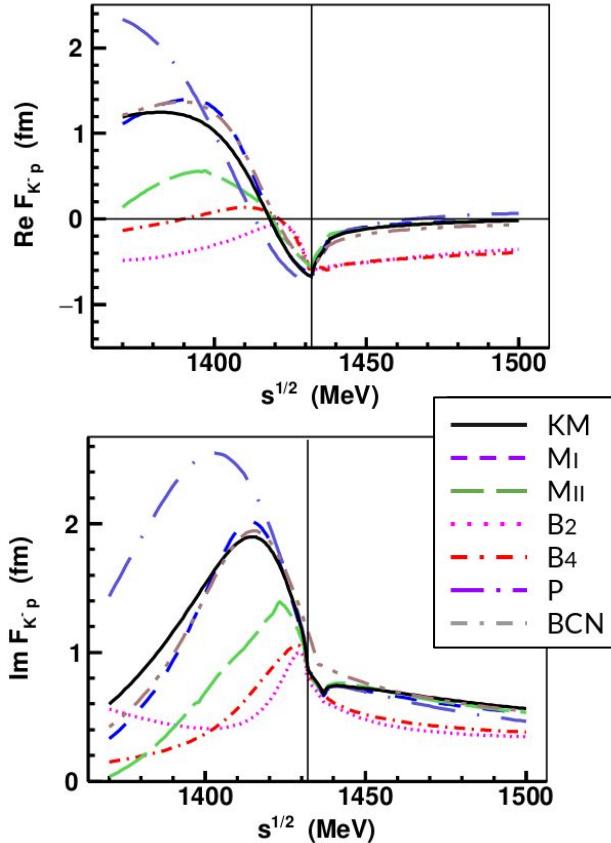
Ideal detector system for the proposed measurement is the combination of KN1 and KN2 experiments proposed by our collaboration:

- The kaon monitor: plastic scintillator pads read out on both sides with Silicon Photo-Multipliers, arranged around the interaction region, covering the TPC kaon entrance window
- active GEM-TPC: filled with very pure light gases (hydrogen, deuterium, helium-3, helium-4)
- charged kaon detector: made of plastic scintillator pads, read out with SiPMs, covering the outer part of the TPC window completely
- lead plates separated by a liquid scintillator: for detection of neutral particles.

see the talk by J. Zmeskal for details



$K^- p$ scattering amplitude

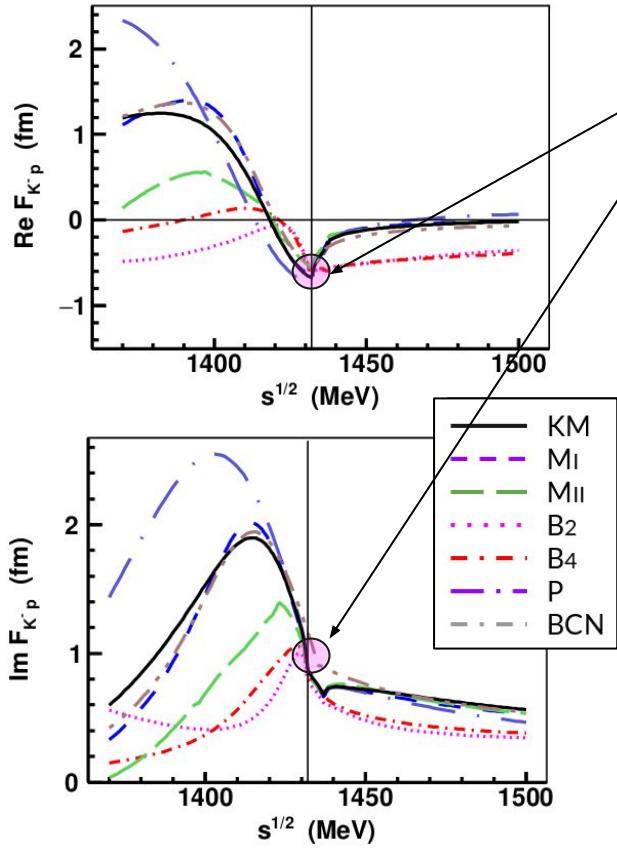


$K^- p$ scattering amplitude in Chiral calculations

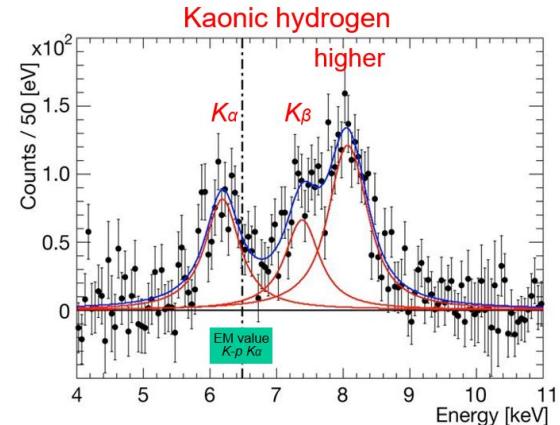
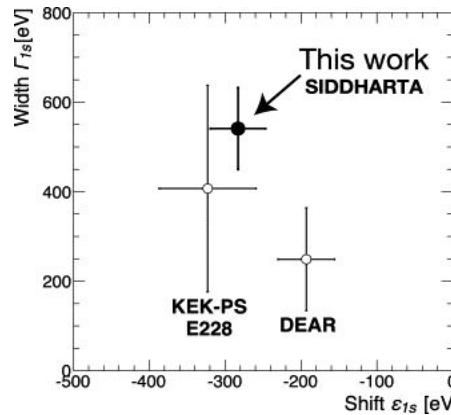
- Kyoto-Munich (KM)
Y. Ikeda, T. Hyodo, W. Weise, Nucl. Phys. A 881 (2012) 98
- Murcia (MI , MII)
Z. H. Guo, J. A. Oller, Phys. Rev. C 87 (2013) 035202
- Bonn (B2 , B4)
M. Mai, U.-G. Meißner - Eur. Phys. J. A 51 (2015) 30
- Prague (P)
A. Cieply, J. Smejkal, Nucl. Phys. A 881 (2012) 115
- Barcelona (BCN)
A. Feijoo, V. Magas, À. Ramos, Phys. Rev. C 99 (2019) 035211

[from A. Cieply talk at MENU2019 conference]

Experimental constraints at KN threshold



Precise SIDDHARTA measurement of kaonic hydrogen 1s level shift and width



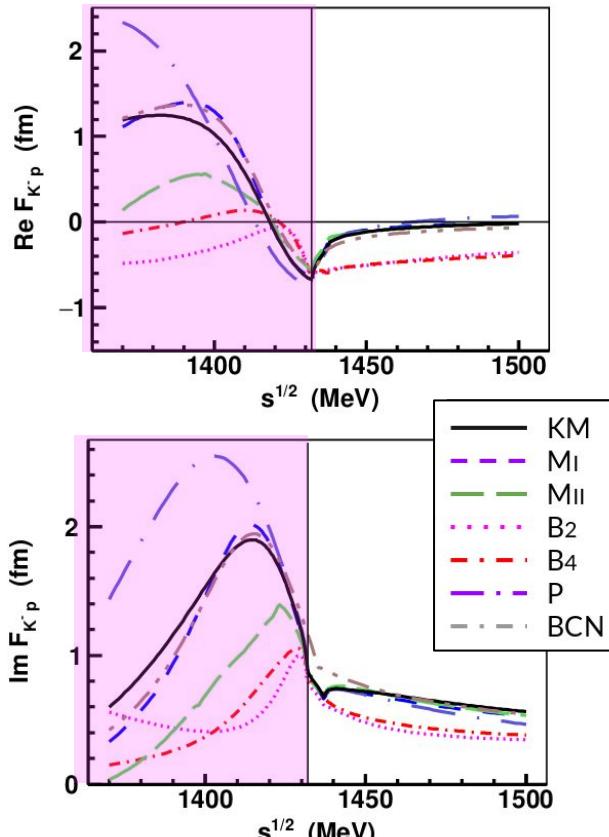
M. Bazzi et al.. 2011. (SIDDHARTA Coll.), Phys. Lett. B704, 113

$$\Delta E_N(1s) = 283 \pm 36(\text{stat.}) \pm 6(\text{syst.}) \text{ eV}$$

$$\Gamma(1s) = 541 \pm 89(\text{stat.}) \pm 22(\text{syst.}) \text{ eV}$$

$$\varepsilon + \frac{i\Gamma}{2} = 2\alpha^3 \mu^2 a_{K^- p} = 412 \frac{\text{eV}}{\text{fm}} a_{K^- p}$$

$K^- p$ scattering amplitude



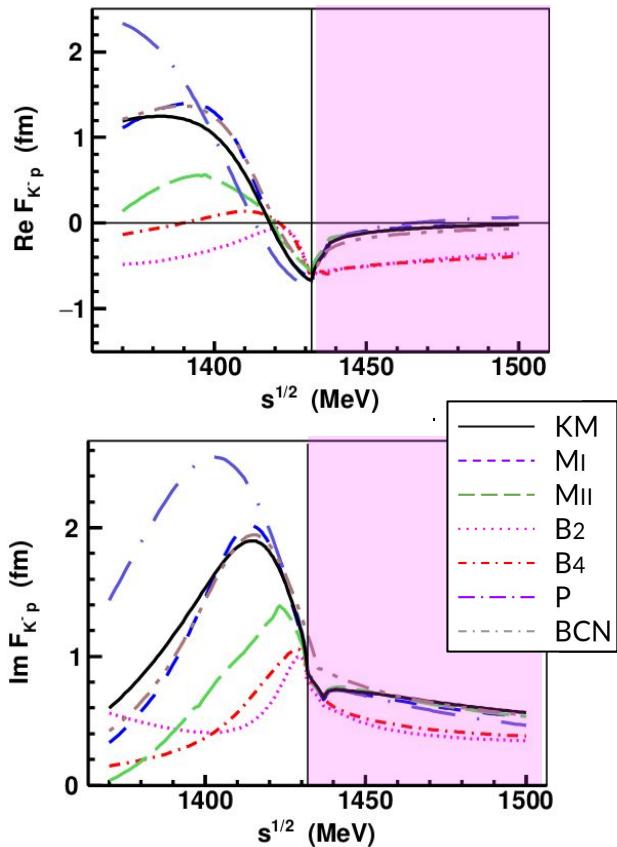
[from A. Cieply talk at MENU2019 conference]

$K^- p$ scattering amplitude in Chiral calculations

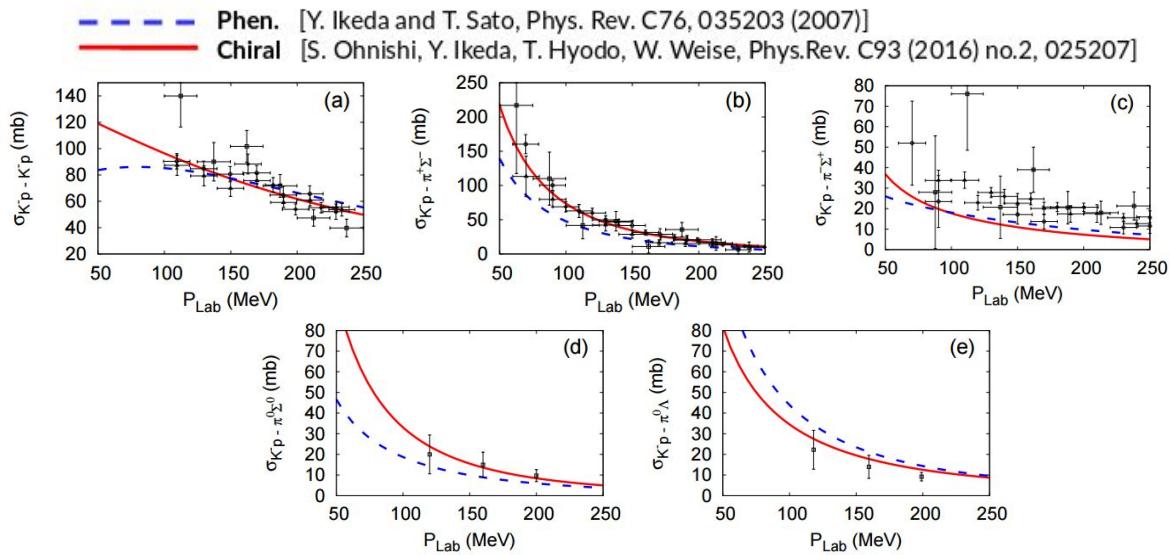
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Y. Ikeda, T. Hyodo, W. Weise, Nucl. Phys. A 881 (2012) 98
- Murcia (M_I, M_{II})
Z. H. Guo, J. A. Oller, Phys. Rev. C 87 (2013) 035202
- Bonn (B₂, B₄)
M. Mai, U.-G. Meißner - Eur. Phys. J. A 51 (2015) 30
- Prague (P)
A. Cieply, J. Smejkal, Nucl. Phys. A 881 (2012) 115
- Barcelona (BCN)
A. Feijoo, V. Magas, À. Ramos, Phys. Rev. C 99 (2019) 035211

**Large discrepancies in
the region below threshold!**

What above the threshold?

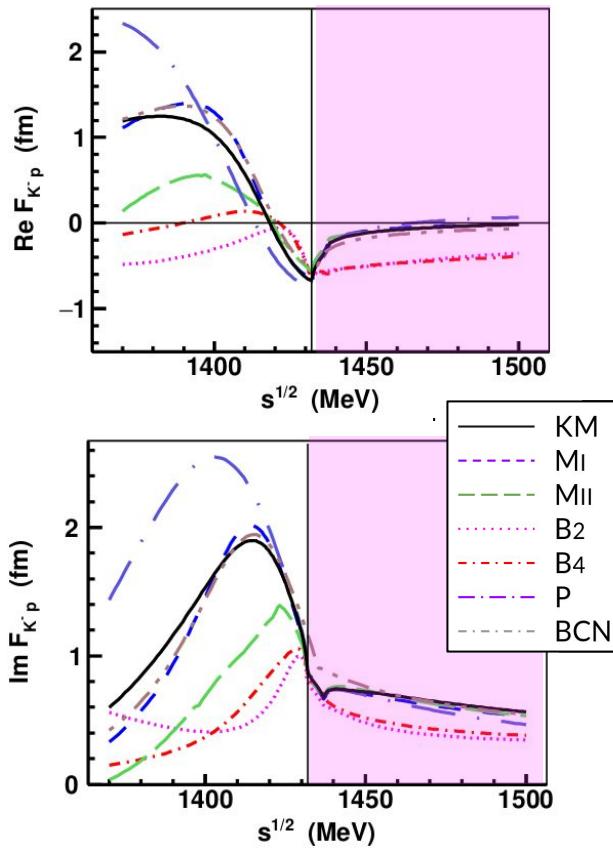


K-p elastic and inelastic low-energy cross sections



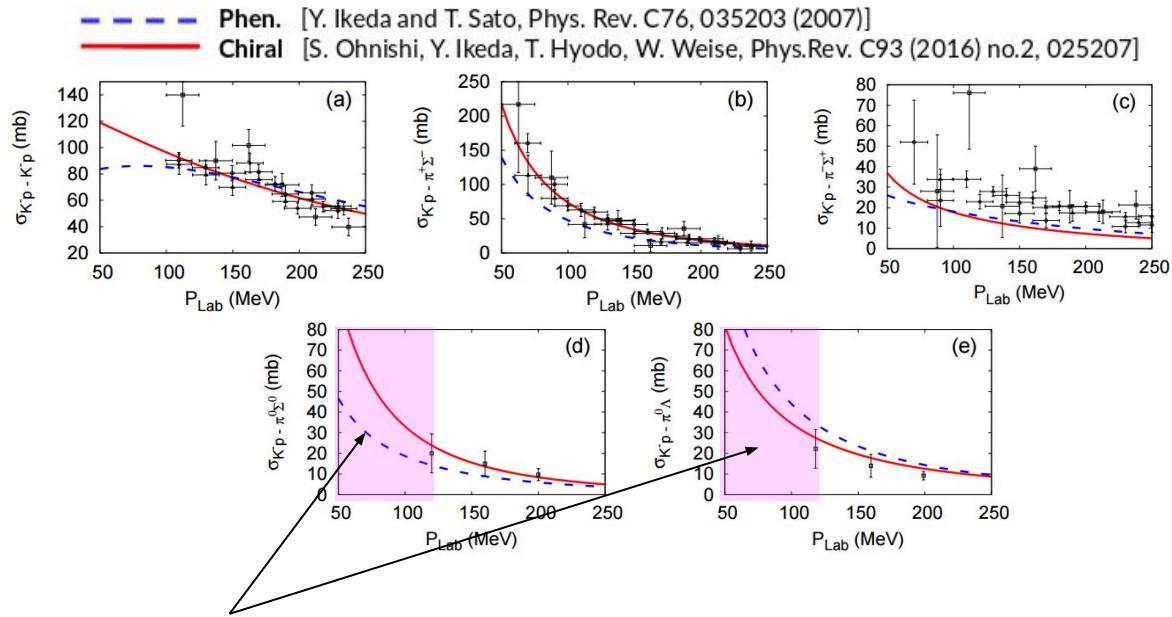
[from A. Cieply talk at MENU2019 conference]

What above the threshold?



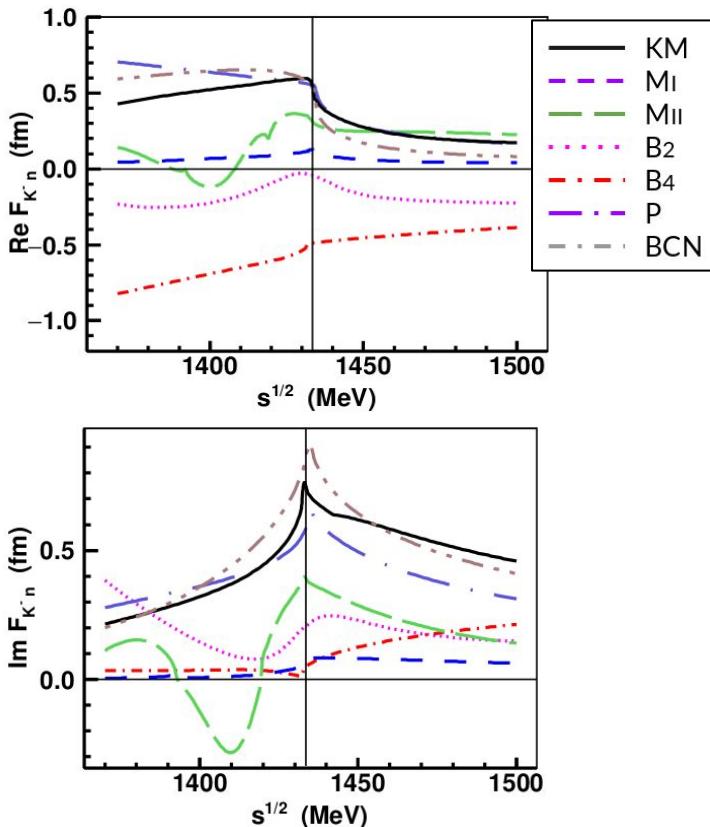
[from A. Cieply talk at MENU2019 conference]

K-p elastic and inelastic low-energy cross sections



lack of data for $p_K < 120 \text{ MeV}/c$ → see the talk by J. Zmeskal for KN1 & KN2 proposals

K^-n scattering amplitude



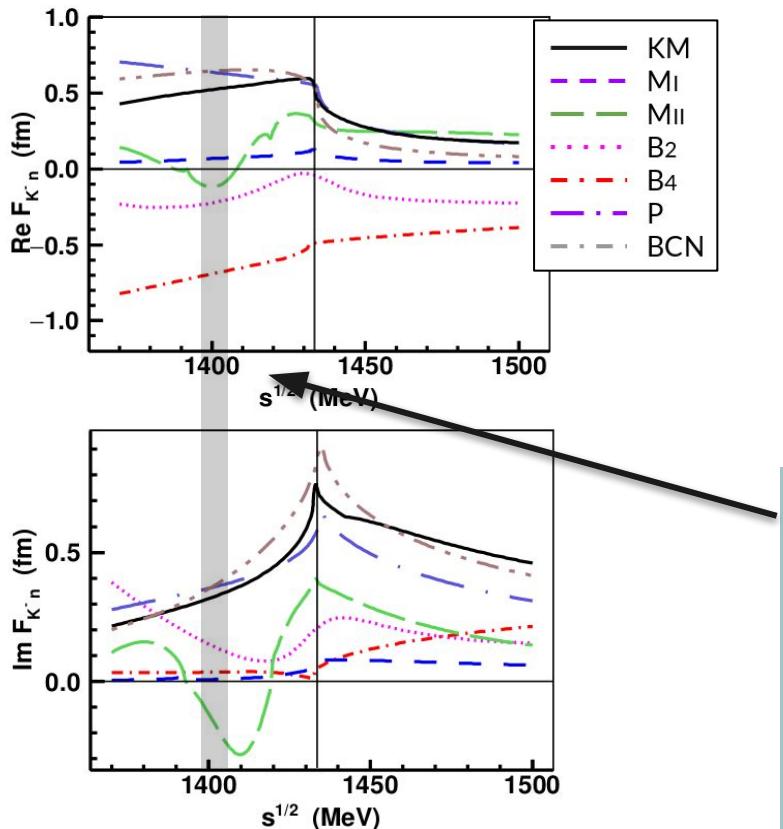
K^-n scattering amplitude (s-wave .. non resonant)
in chiral calculations

Even larger spread in $I=1$ channel

Experimental information is missing:

- SIDDHARTA-2 → first experimental constraint at threshold
- AMADEUS → first experimental constraint below threshold

Experimental constraints below threshold



K^-n scattering amplitude with Chiral models

Large spread in $l=1$ channel

Experimental information is totally missing:

- SIDDHARTA-2 → first experimental constraint at threshold
- AMADEUS → First determination of the non-resonant (s-wave) transition amplitude below threshold

Investigated using:

$K^- n \rightarrow \Lambda \pi^-$ to extract $|f_{\Lambda \pi}^{N-R}(l=1)|$
with bound neutron in 4He

$K^- p \rightarrow \Lambda\pi^-$ events selection and interpretation

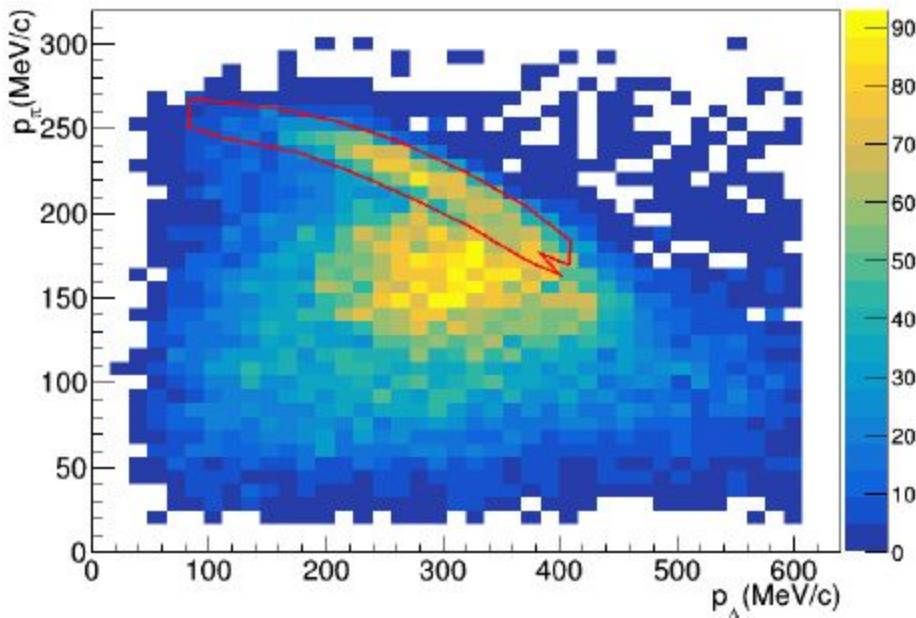


FIG. 2. (Color online) Experimental distribution of the π^- vs Λ momenta. The red line represents the selection of the direct $\Lambda\pi^-$ production events. See the text for details.

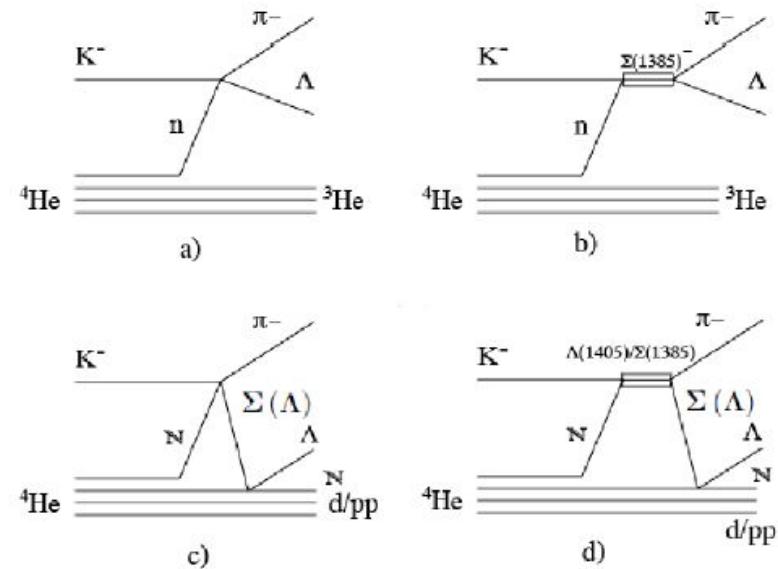
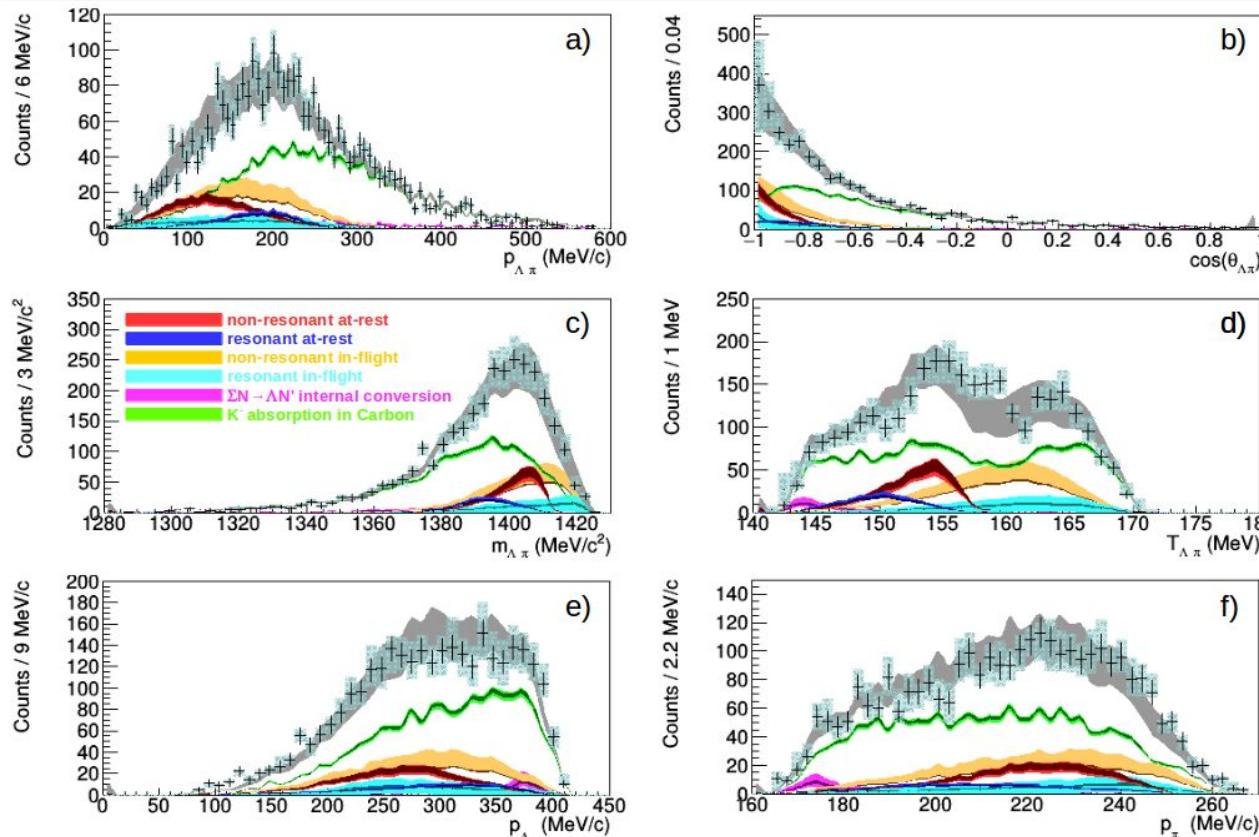


FIG. 1. Panels a) and b) show the non-resonant and resonant $\Lambda\pi^-$ direct productions, respectively. Panels c) and d) show the primary hyperon-pion formation, followed by the inelastic/elastic scattering of the Σ/Λ hyperon on a single nucleon, for the resonant and non-resonant cases, respectively.

Simultaneous fit : $p_{\Lambda\pi^-}$ - $m_{\Lambda\pi^-}$ - $\cos\theta_{\Lambda\pi^-}$



Investigated using:
 $K^- "n" ^3He \rightarrow \Lambda\pi^- ^3He$

$$E_{Kn} \sim -B_n - < \frac{p_{\Lambda\pi}^2}{2\mu_{\pi,\Lambda,^3He}} >$$

33 ± 6 MeV below threshold
see also

- A. Cieply et al., Phys. Lett. B 702 (2011) 402
 T. Hoshino et al., Phys. Rev. C 96 (2017) 045204
 N. Barnea, E. Friedman,
 A. Gal, Nucl. Phys. A968 (2017)

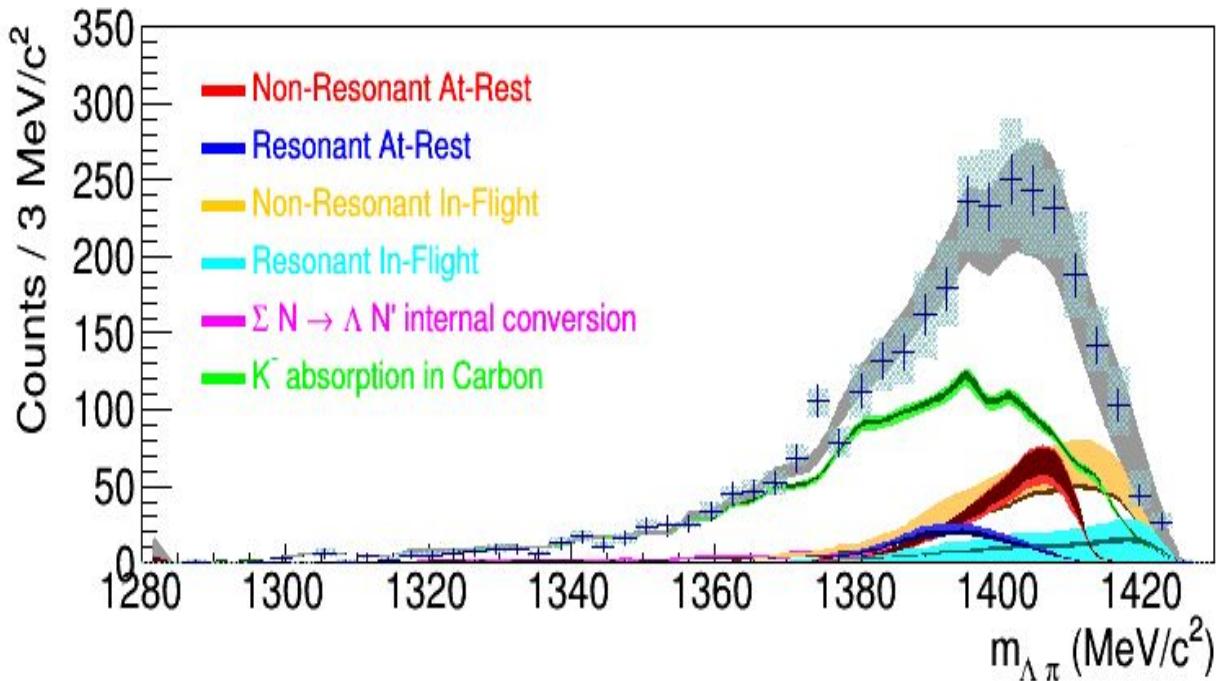
[K. Piscicchia, S. Wycech, L. Fabbietti et al. Phys.Lett. B782 (2018) 339-345]
 [K. Piscicchia, S. Wycech, C. Curceanu, Nucl. Phys. A 954 (2016) 75-93]

Outcome of the measurement

Investigated using:
 $K^- "n" ^3He \rightarrow \Lambda \pi^- ^3He$

Energy of the $K^- n$ system:

$$E_{Kn} \sim -B_n - < \frac{p_{\Lambda\pi}^2}{2\mu_{\pi,\Lambda,3He}} >$$

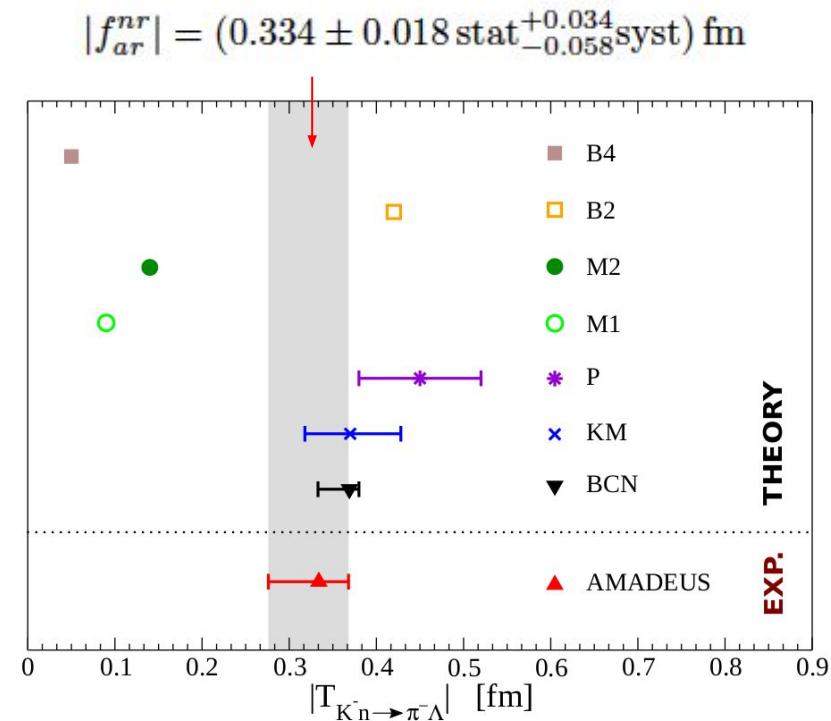
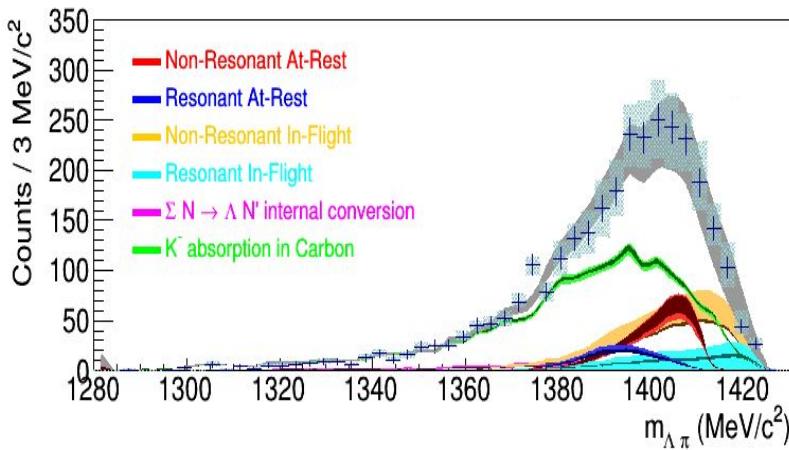


[K. Piscicchia, S. Wycech, L. Fabbietti et al. Phys.Lett. B782 (2018) 339-345]

[K. Piscicchia, S. Wycech, C. Curceanu, Nucl. Phys. A 954 (2016) 75-93]

Outcome of the measurement

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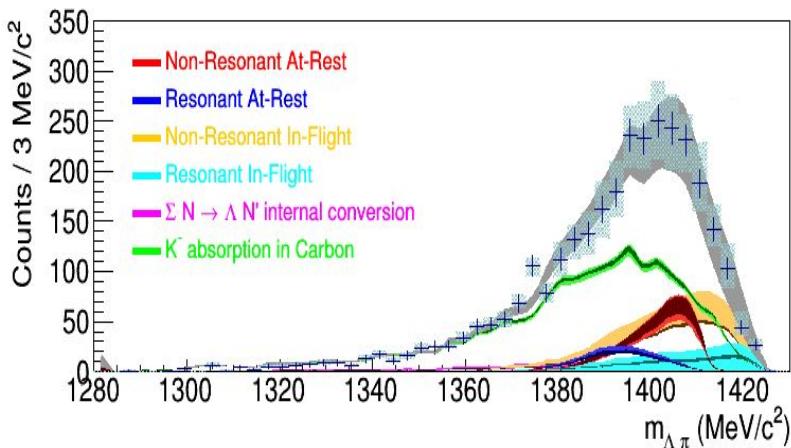


[K. Piscicchia, S. Wycech, L. Fabbietti et al. Phys.Lett. B782 (2018) 339-345]

[K. Piscicchia, S. Wycech, C. Curceanu, Nucl. Phys. A 954 (2016) 75-93]

Outcome of the measurement

Investigated using: $K^- "n" ^3He \rightarrow \Lambda\pi^- ^3He$



$$|f_{ar}^{nr}| = (0.334 \pm 0.018 \text{ stat}^{+0.034}_{-0.058} \text{ syst}) \text{ fm}$$

$E = -33 \text{ MeV}$	$0.334 \pm 0.018 \text{ stat}^{+0.034}_{-0.058} \text{ syst}$
$p_{lab} = 120 \text{ MeV}$	0.33 ± 0.11
$p_{lab} = 160 \text{ MeV}$	0.29 ± 0.10
$p_{lab} = 200 \text{ MeV}$	0.24 ± 0.06
$p_{lab} = 245 \text{ MeV}$	0.28 ± 0.02

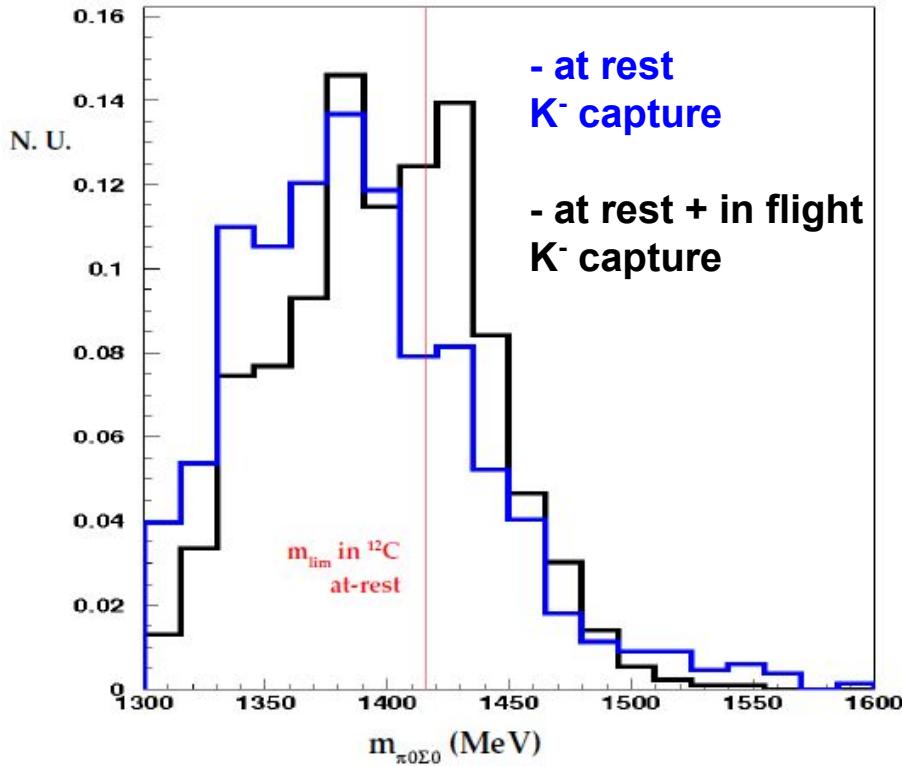
TABLE II. The S-wave non-resonant amplitude ($|f^{nr}|$ fm) extracted from $K^- p \rightarrow \Lambda\pi^0$ scattering [34, 35] and from this experiment ($E = -33 \text{ MeV}$).

J. K. Kim, Columbia University Report, Nevis 149 (1966)
J. K. Kim, Phys. Rev. Lett. 19 (1977) 1074

[K. Piscicchia, S. Wycech, L. Fabbietti et al. Phys.Lett. B782 (2018) 339-345]

[K. Piscicchia, S. Wycech, C. Curceanu, Nucl. Phys. A 954 (2016) 75-93]

Next step...



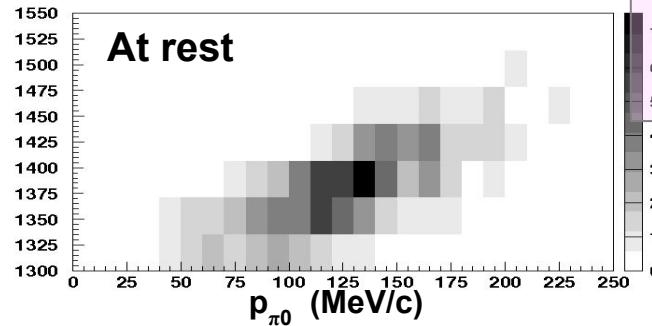
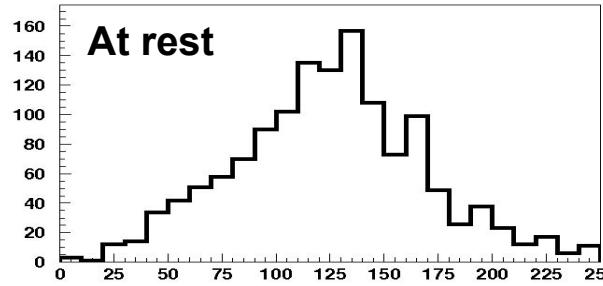
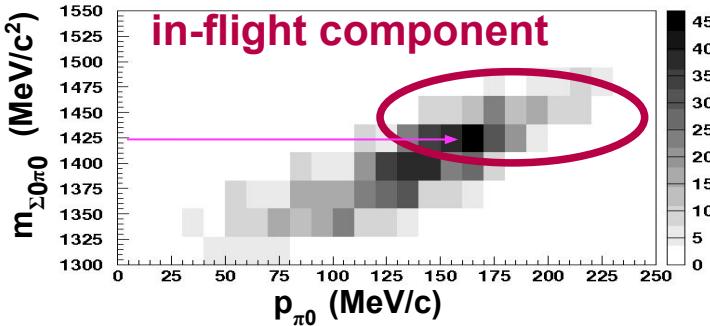
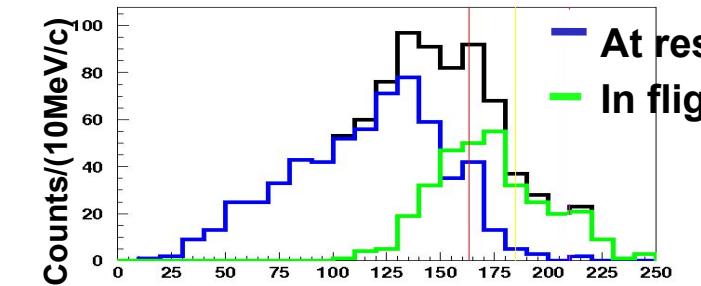
Same analysis for the $I = 0$ counterpart.

measured channel:

$K^- p \rightarrow \Sigma^0 \pi^0$
(bound proton in ¹²C)

for the extraction of the
 $\Lambda(1405)$ shape

π_0 resolution: $\sigma_p \approx 12 \text{ MeV/c}$



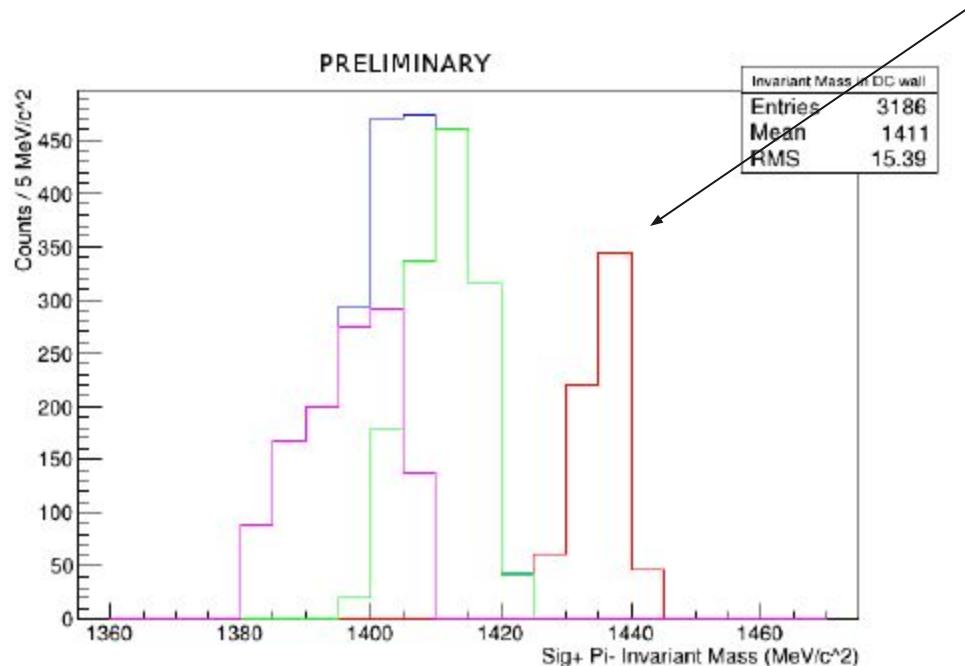
IN-FLIGHT
K- 12C
opens a window
between 1416 MeV
and K-Nth

difficulty: epoxy resin, contained in the carbon fibre target, contains H

H atoms in the molecules mainly contribute to **K- H absorption in-flight**, resulting in a **non-resonant background in the $\Sigma^0 \pi^0$ spectra**

measured channel: $K^- p \rightarrow \Sigma^+ \pi^-$ (bound proton in ^{12}C)

p_π resolution about 1MeV → K^- capture at-rest/in-flight/on H can be distinguished



but, neglecting the small $I = 2$ component

$$\frac{d\sigma(\pi^+\Sigma^-)}{dM_I} \propto \frac{1}{3}|T^{(0)}|^2 + \frac{1}{2}|T^{(1)}|^2 + \frac{2}{\sqrt{6}}\text{Re}(T^{(0)}T^{(1)*}),$$
$$\frac{d\sigma(\pi^-\Sigma^+)}{dM_I} \propto \frac{1}{3}|T^{(0)}|^2 + \frac{1}{2}|T^{(1)}|^2 - \frac{2}{\sqrt{6}}\text{Re}(T^{(0)}T^{(1)*}),$$
$$\frac{d\sigma(\pi^0\Sigma^0)}{dM_I} \propto \frac{1}{3}|T^{(0)}|^2,$$

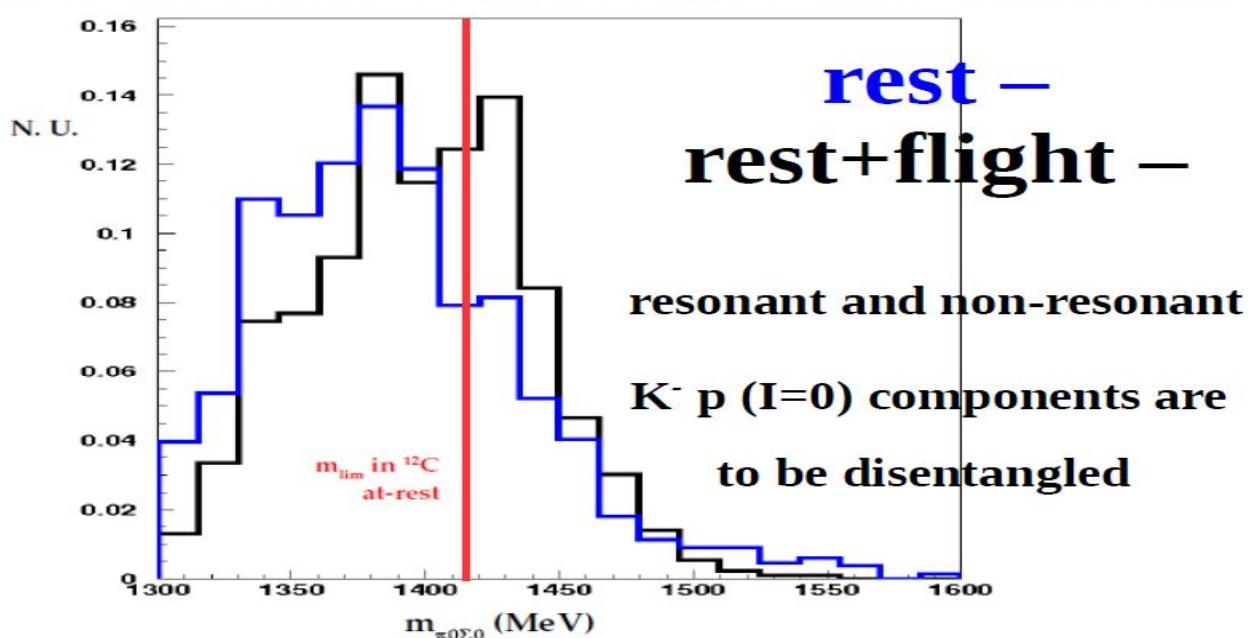
Figure 3: (Colour online.) $m_{\Sigma\pi}$ invariant mass distributions in-flight (green) and at-rest (violet) in ^{12}C . Blue histogram represents the sum of green and violet histograms. The red distribution refers to K^- absorptions on Hydrogen

$\Lambda(1405)$: extracting the resonant $I = 0$ contribution

PID optimised, data fit is ongoing

necessary the input of the $\Lambda\pi^-$ measurement

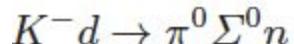
- K. Piscicchia et al., APP B48 (2017) 10, 1875
- C. Curceanu, K. Piscicchia et al., APP B46 (2015) 1, 203



IN-FLIGHT
K- ${}^{12}\text{C}$
opens a window
between 1416 MeV
and $K\text{-Nth}$

Measurement of the $\Lambda(1405)$ high mass pole in KN1 and KN2 experiments

Jido, D., Oset, E. & Sekihara, T. *Eur. Phys. J. A* 47, 42 (2011) see also *Eur. Phys. J. A* 42, 257 (2009):



- in flight reactions of low momentum (about 130 MeV) kaons, distinguish the resonant from non-resonant $\Sigma\pi$ production.
- Both the single scattering (non resonant) and the double scattering (resonant) give rise to a peak in the region of 1420 MeV.
- Single scattering is drastically reduced, in this region of inv. mass, at forward angles of the neutron, leading to a cleaner signal of the $\Lambda(1405)$ resonance.

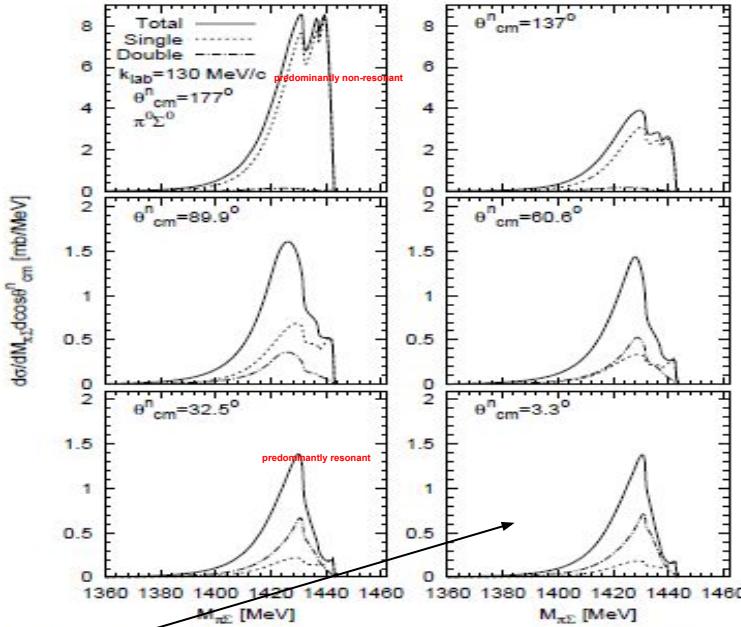


Fig. 5. Differential $\pi\Sigma$ invariant mass spectra of $K^- d \rightarrow \pi^0 \Sigma^0 n$ for 130 MeV/c of incident K^- momentum fixing the angle between the emitted neutron and the incident K^- in the CM frame. In each panel, the solid line denotes the total contributions of the three diagrams, while the dotted and dash-dotted lines show the calculations from the single and double scatterings, respectively.

- with the combination of the KN1 and KN2 detectors the kinematics of the K-
 $d \rightarrow \Sigma^0 \pi^0 n$ reaction would be closed,
- forward neutrons (angle between the outgoing neutron and the incident K- in the CM frame) can be selected
- optimization of the neutrals detector ongoing based on MC simulations.
- simulation of the neutrons momentum distribution for the non-resonant process, (simulation for double scattering ongoing):

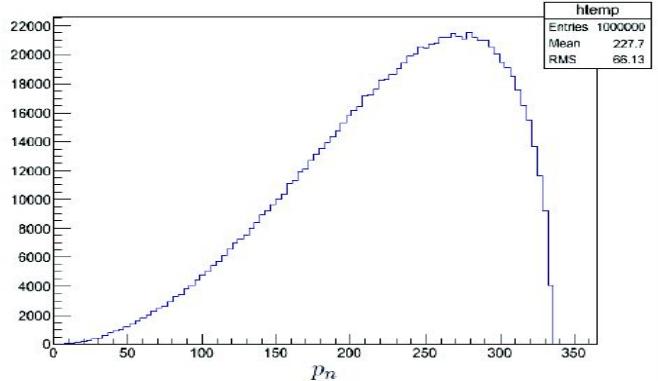
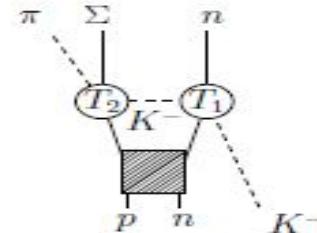


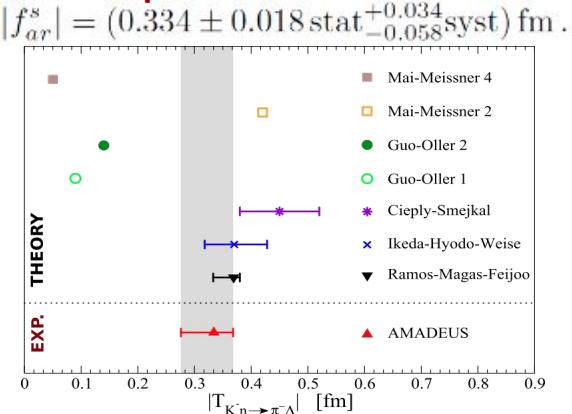
Fig. 6. neutrons momentum distribution.



in double scattering the neutron gets some energy from the $K^- \rightarrow$ higher efficiency.

Summary

K⁻n amplitude below threshold



Λ p channel: 2NA, 3NA and 4NA BRs and σ

Process	Branching Ratio (%)	σ (mb)	@	p_K (MeV/c)
2NA-QF Λp	$0.25 \pm 0.02 \text{ (stat.)} {}^{+0.01}_{-0.02} \text{ (syst.)}$	$2.8 \pm 0.3 \text{ (stat.)} {}^{+0.1}_{-0.2} \text{ (syst.)}$	@	128 ± 29
2NA-FSI Λp	$6.2 \pm 1.4 \text{ (stat.)} {}^{+0.5}_{-0.6} \text{ (syst.)}$	$69 \pm 15 \text{ (stat.)} \pm 6 \text{ (syst.)}$	@	128 ± 29
2NA-QF $\Sigma^0 p$	$0.35 \pm 0.09 \text{ (stat.)} {}^{+0.13}_{-0.06} \text{ (syst.)}$	$3.9 \pm 1.0 \text{ (stat.)} {}^{+1.4}_{-0.7} \text{ (syst.)}$	@	128 ± 29
2NA-FSI $\Sigma^0 p$	$7.2 \pm 2.2 \text{ (stat.)} {}^{+4.2}_{-5.4} \text{ (syst.)}$	$80 \pm 25 \text{ (stat.)} {}^{+46}_{-60} \text{ (syst.)}$	@	128 ± 29
2NA-CONV Σ/Λ	$2.1 \pm 1.2 \text{ (stat.)} {}^{+0.9}_{-0.5} \text{ (syst.)}$	-		
3NA Λpn	$1.4 \pm 0.2 \text{ (stat.)} {}^{+0.1}_{-0.2} \text{ (syst.)}$	$15 \pm 2 \text{ (stat.)} \pm 2 \text{ (syst.)}$	@	117 ± 23
3NA $\Sigma^0 pn$	$3.7 \pm 0.4 \text{ (stat.)} {}^{+0.2}_{-0.4} \text{ (syst.)}$	$41 \pm 4 \text{ (stat.)} {}^{+2}_{-5} \text{ (syst.)}$	@	117 ± 23
4NA Λpnn	$0.13 \pm 0.09 \text{ (stat.)} {}^{+0.08}_{-0.07} \text{ (syst.)}$	-		
Global $\Lambda(\Sigma^0)p$	$21 \pm 3 \text{ (stat.)} {}^{+5}_{-6} \text{ (syst.)}$	-		

Λ t channel: 4NA BRs and σ

$$\text{BR}(K^{-4}\text{He(4NA)} \rightarrow \Lambda t) < 2.0 \times 10^{-4} / K_{\text{stop}} \quad (95\% \text{ c. l.})$$

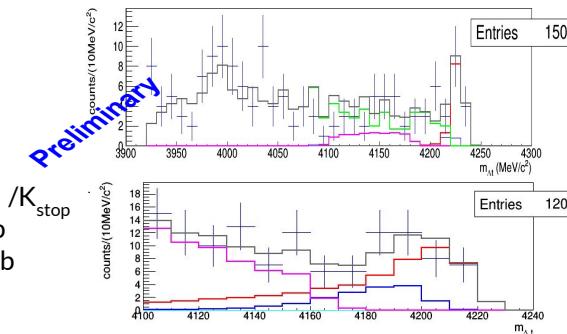
$$\sigma(100 \pm 19 \text{ MeV/c}) (K^{-4}\text{He(4NA)} \rightarrow \Lambda t) =$$

$$= (0.81 \pm 0.21 \text{ (stat)} {}^{+0.03}_{-0.04} \text{ (syst)}) \text{ mb}$$

$$\text{BR}(K^{-12}\text{C(4NA)} \rightarrow \Lambda t {}^8\text{Be}) = 1.5 \pm 0.5 \times 10^{-4} \text{ (stat) / } K_{\text{stop}}$$

$$\sigma(K^{-12}\text{C(4NA)} \rightarrow \Lambda t {}^8\text{Be}) = 0.58 \pm 0.11 \text{ (stat) mb}$$

$$\sigma(K^{-12}\text{C(4NA)} \rightarrow \Sigma^0 t {}^8\text{Be}) = 1.88 \pm 0.35 \text{ (stat) mb}$$



Thank You