



# CMB @ small scales: tSZ power spectrum

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Marian Douspis

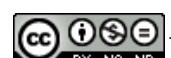


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European Research Council  
Established by the European Commission

*"Probing the CMB small scales with Planck and SPT data",  
Douspis, Salvati, Gorce, A&A to be submitted.*



for all document

- CMB @ small scales [focus on SZ signals]
- Standard analyses at high ell
- Alternative analysis
  - Power spectrum computation shortcut: ML
- Results on cosmological parameters
- Results on tSZ and kSZ amplitude
- Conclusion

# USING tSZ SIGNAL : FOR COSMOLOGY

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- tSZ detected in clusters : number counts or baryon fraction as cosmological probe
- Diffuse hot gas exists outside detected clusters : low mass systems, filaments
- Dedicated reconstruction of  $y$ -map
- Present in CMB frequency maps, thus in angular power spectra
  - Power spectrum of tSZ needed

*Talk: Salvati  
Talk: Bocquet  
Talk: Wicker*

*Talk: Radiconi  
Talk: Lestrade  
**Bonjean et al**  
**Tanimura et al.***

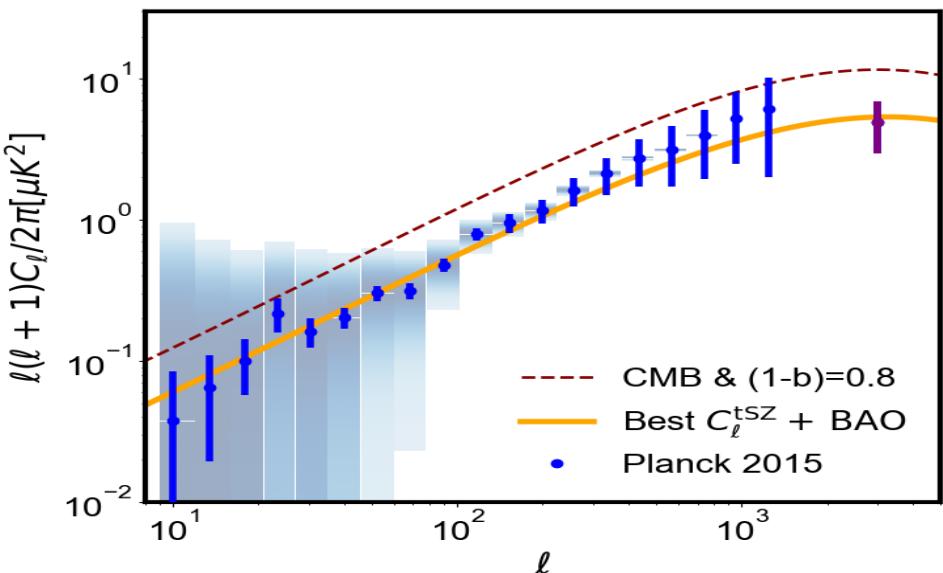
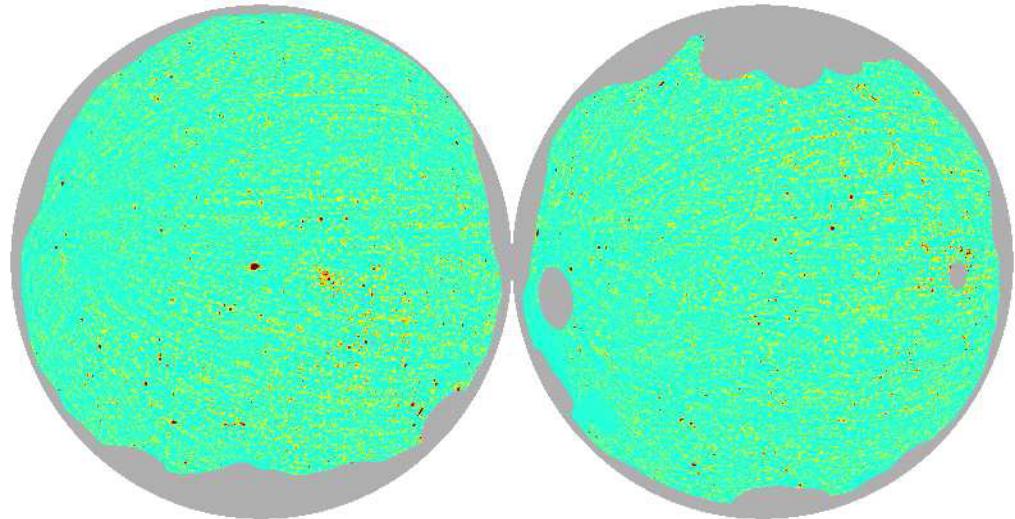
***Hurier et al.**  
**Remazeille et al.***

***Planck collab**  
**SPT collab**  
**ACT collab**  
**Taburet et al.**  
**Douspis et al. in prep***

***Talk: Rotti**  
**Taburet et al. 2009**  
**Salvati et al.***

# PLANCK YMAP

- Adapted component separation based on :
- Constraints on emission spectra
- Localisation in multiple domain
- 100:857Ghz maps
- First SZ Angular power spectrum and cosmological constraints

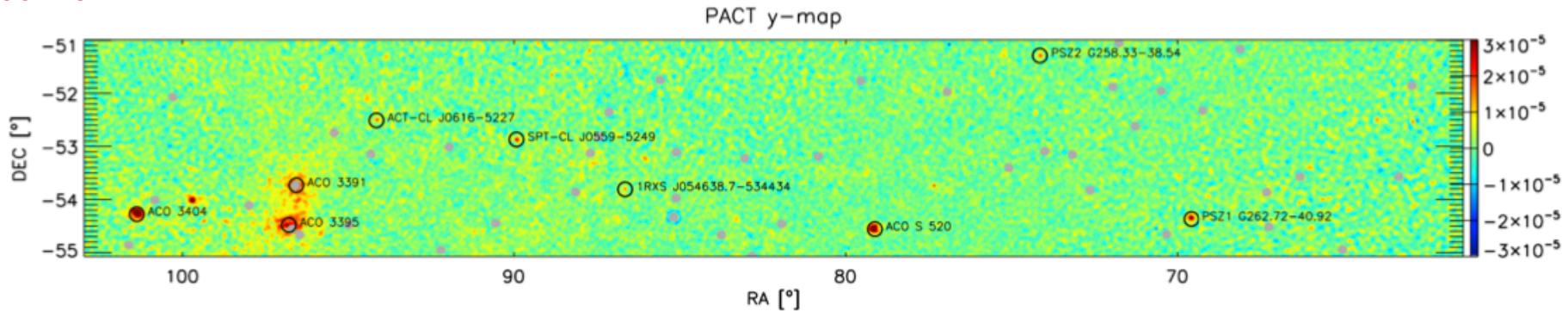


Planck 2014, Planck 2016  
Douspis et al. Salvati et al.

# OTHER YMAP

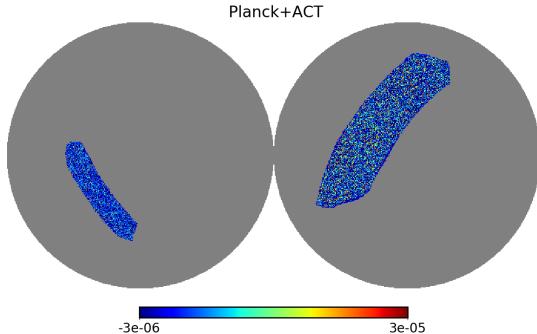
- Planck + ACT: PACT map: 1st combination of CMB experiments

*Aghanim et al 2019*



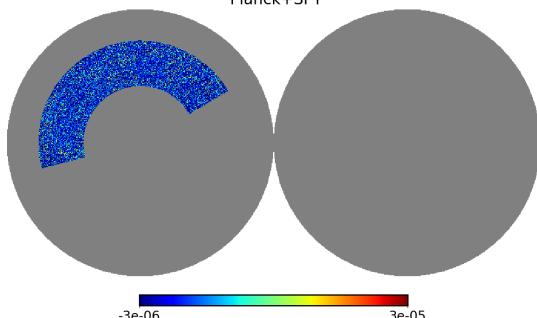
- Planck+ACT

*Madhavacheril et al 2020*



- Planck+SPT

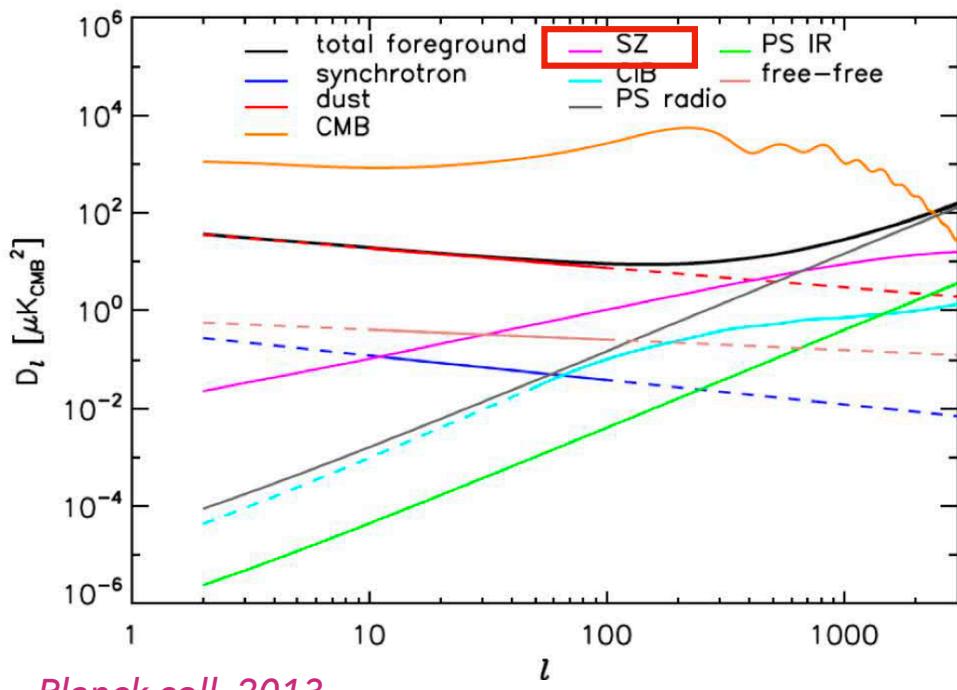
*Bleem et al 2021*



# tSZ IN FREQUENCY MAPS (SMALL SCALES)

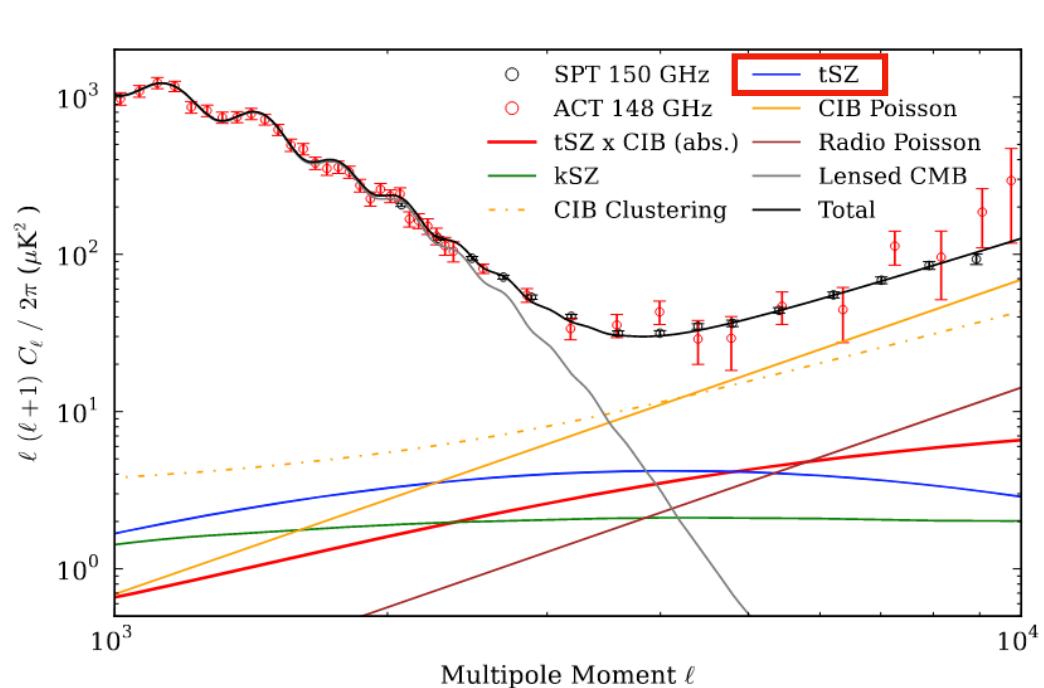
- Primordial CMB becomes negligible
- tSZ is hidden among many other signals

Planck/Large scales



Planck coll. 2013

SPT/small scales

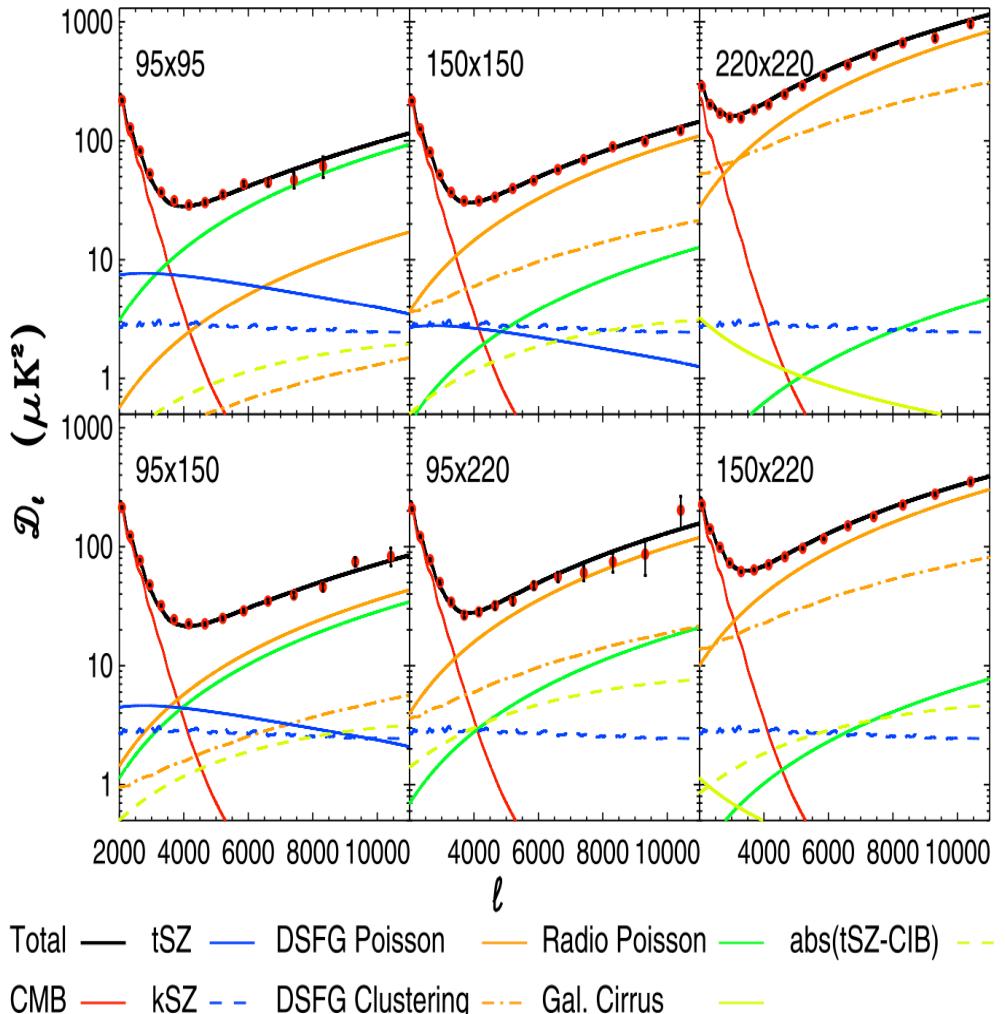


Addison et al. 2012

# FOCUS ON SPT HIGH ELL ANALYSIS

- SPT-SZ +SPTpol data
- 3 frequencies: 95, 150, 220
- 6 cross-spectra
- 8 components
- ell in [2000:11000]

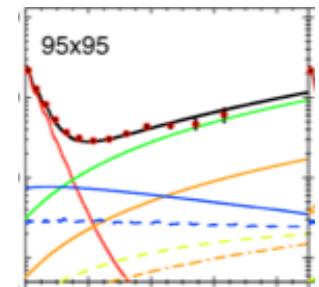
Reichardt et al. 2020



# FOCUS ON SPT HIGH ELL ANALYSIS

$$C_{\ell}^{obs} = C_{\ell}^{CMB} + C_{\ell}^{tSZ} + C_{\ell}^{kSZ} + \dots$$

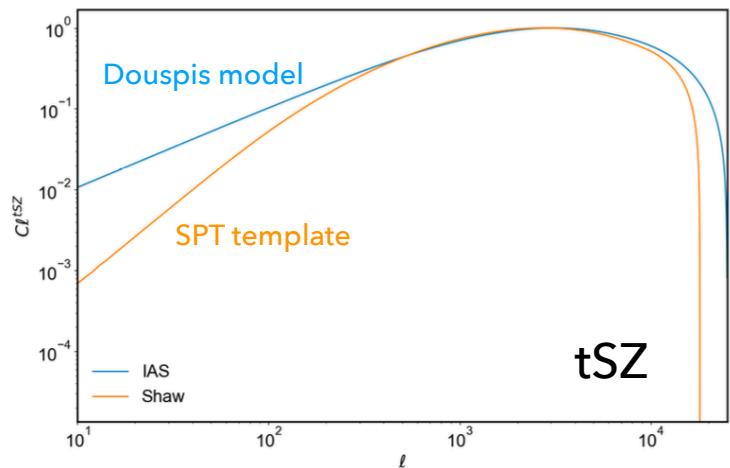
For all 6 cross spectra simultaneously



SPT analysis uses templates for tSZ and kSZ

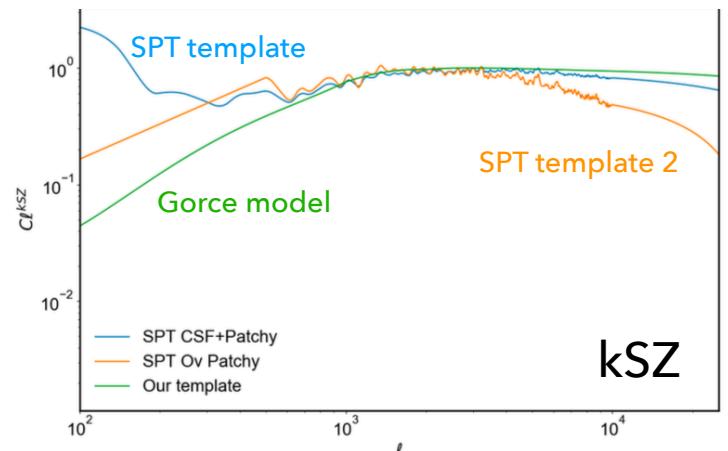
$$C_{\ell}^{tSZ} = A^{tSZ} \times C_{\ell}^{template}$$

Sims with cosmo1



$$C_{\ell}^{kSZ} = A^{kSZ} \times C_{\ell}^{template}$$

Sims with cosmo2



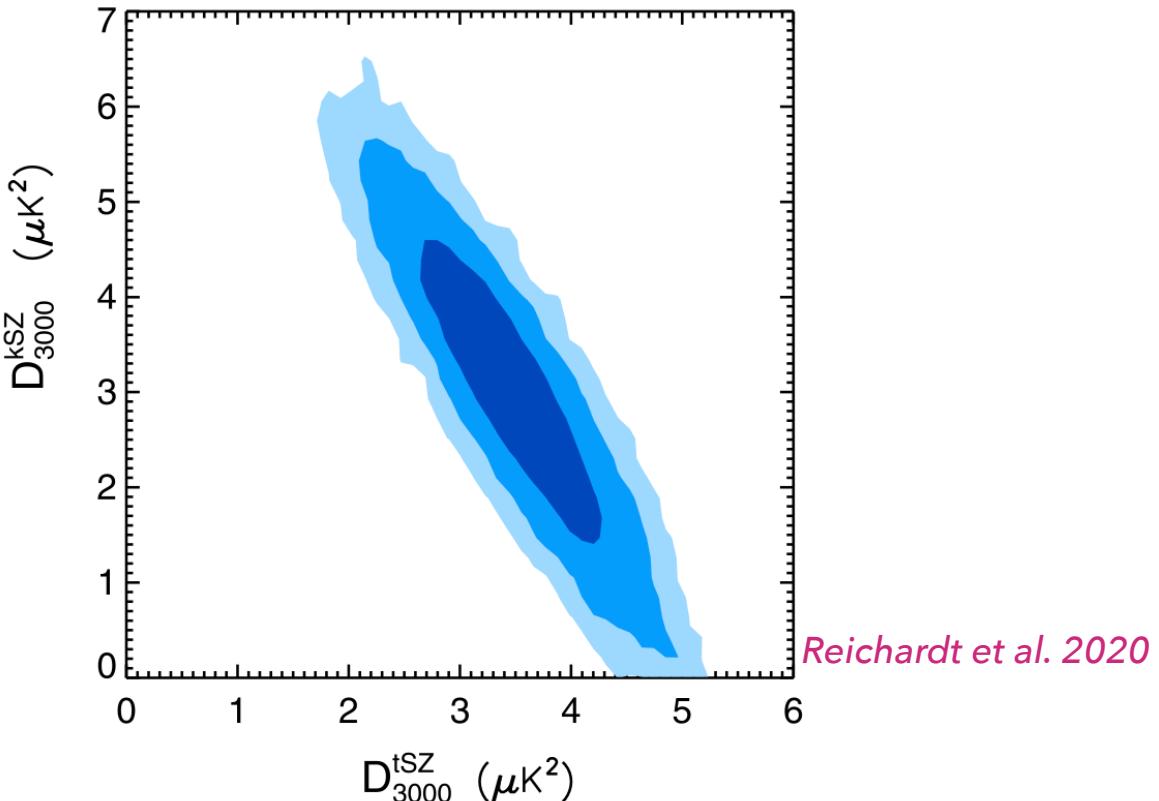
- ▶ Not coherent analysis
- ▶ Depends on assumed template

# SPT CONSTRAINTS ON SZ EFFECTS

SZ Constraints

tSZ Template	kSZ Template	$D_{3000}^{\text{tSZ}} (\mu\text{K}^2)$	$D_{3000}^{\text{kSZ}} (\mu\text{K}^2)$	$\xi$
Shaw	CSF+patchy	$3.42 \pm 0.54$	$3.0 \pm 1.0$	$0.076 \pm 0.040$
Shaw	CSF	$3.39 \pm 0.58$	$3.1 \pm 1.3$	$0.077 \pm 0.047$
Shaw	Patchy	$3.45 \pm 0.56$	$3.5 \pm 1.2$	$0.086 \pm 0.050$
Battaglia	CSF+patchy	$3.74 \pm 0.54$	$2.4 \pm 1.0$	$0.051 \pm 0.033$
Bhattacharya	CSF+patchy	$3.46 \pm 0.54$	$3.0 \pm 1.0$	$0.071 \pm 0.036$
Sehgal	CSF+patchy	$3.59 \pm 0.54$	$2.8 \pm 1.0$	$0.064 \pm 0.039$
Shaw w. Bispectrum	CSF+patchy	$3.53 \pm 0.48$	$2.8 \pm 0.9$	$0.069 \pm 0.036$

Cosmology fixed to Planck 2018



- tSZ spectrum contains cosmological information and baryonic information in clusters
- kSZ contains mainly information on reionisation
- CIB contains cosmological information and SFR evolution information
- ...

*Hu & Seljak  
Taburet et al.  
Planck 2013  
Bolliet et al.  
Salvati et al.*

*Sunyaev & Zel'dovich  
Mc Quin et al.  
Mesinger et al.  
Zahn et al.  
Planck 2016  
Gorce et al. 2020*

*Puget et al.  
Lagache et al.  
Knox et al.  
Maniya et al.*

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Zahn  
Planck 2016*

*Puget  
Lagache  
Knox  
Maniyar*

# GOAL

We need :

- Consistent ingredients and analyses
- Exploit the full cosmological information in the signal

Replace in SPT analysis

$$C_\ell^{obs} = C_\ell^{CMB}(\Theta, xe = \tanh) + \underbrace{A^{tSZ} C_\ell^{temp-t}}_{\substack{\text{Reionisation} \\ \uparrow \\ \text{Cosmology}}} + A^{kSZ} C_\ell^{temp-k} + \dots$$

By

$$C_\ell^{obs} = C_\ell^{CMB}(\Theta, xe = asym) + C_\ell^{tSZ}(\Theta) + C_\ell^{kSZ}(\Theta, xe = asym) + \dots$$

And for Planck

$$C_\ell^{obs} = C_\ell^{tSZ}(\Theta) \quad \text{Because we extracted a tSZ map thus tSZ spectrum}$$

*Planck coll. 2014, 2016*

# TSZ POWER SPECTRUM FROM HALO MODEL



$$Cl_{\Theta}[\underline{\Theta}] \equiv \iiint dM dz \frac{dV}{-\chi(obs)} S(obs - M) \frac{dN}{dM dz} p(M, z)$$

## Scaling Relation

Needed to relate the observable (flux, size) to the mass and redshift. Given by comparison HM with simulations or WL measurements [Planck 2013., Nagai et al. , ...]

$$E^{-\beta}(z) \left[ \frac{D_A^2(z) Y_{500}}{10^{-4} \text{Mpc}^2} \right] = Y^* \left[ \frac{h}{0.7} \right]^{-2+\alpha} \left[ \frac{(1-b)}{6 \cdot 10^{14} M_\odot} M_{500} \right]^\alpha$$

## Cosmology $\Theta$

SZ power spectrum as geometrical and growth probe

## Mass function

Number of halos in bins of mass and redshift. From numerical simulations, known 10% scatter between teams [Tinker et al., Watson et al. , Despali et al.]

$$\frac{dN(M_{500}, z)}{dM_{500}} = f(\sigma) \frac{\rho_m(z=0)}{M_{500}} \frac{d\ln\sigma^{-1}}{dM_{500}}$$

$$f(\sigma) = A \left[ 1 + \left( \frac{\sigma}{b} \right)^{-a} \right] \exp \left( -\frac{c}{\sigma^2} \right)$$

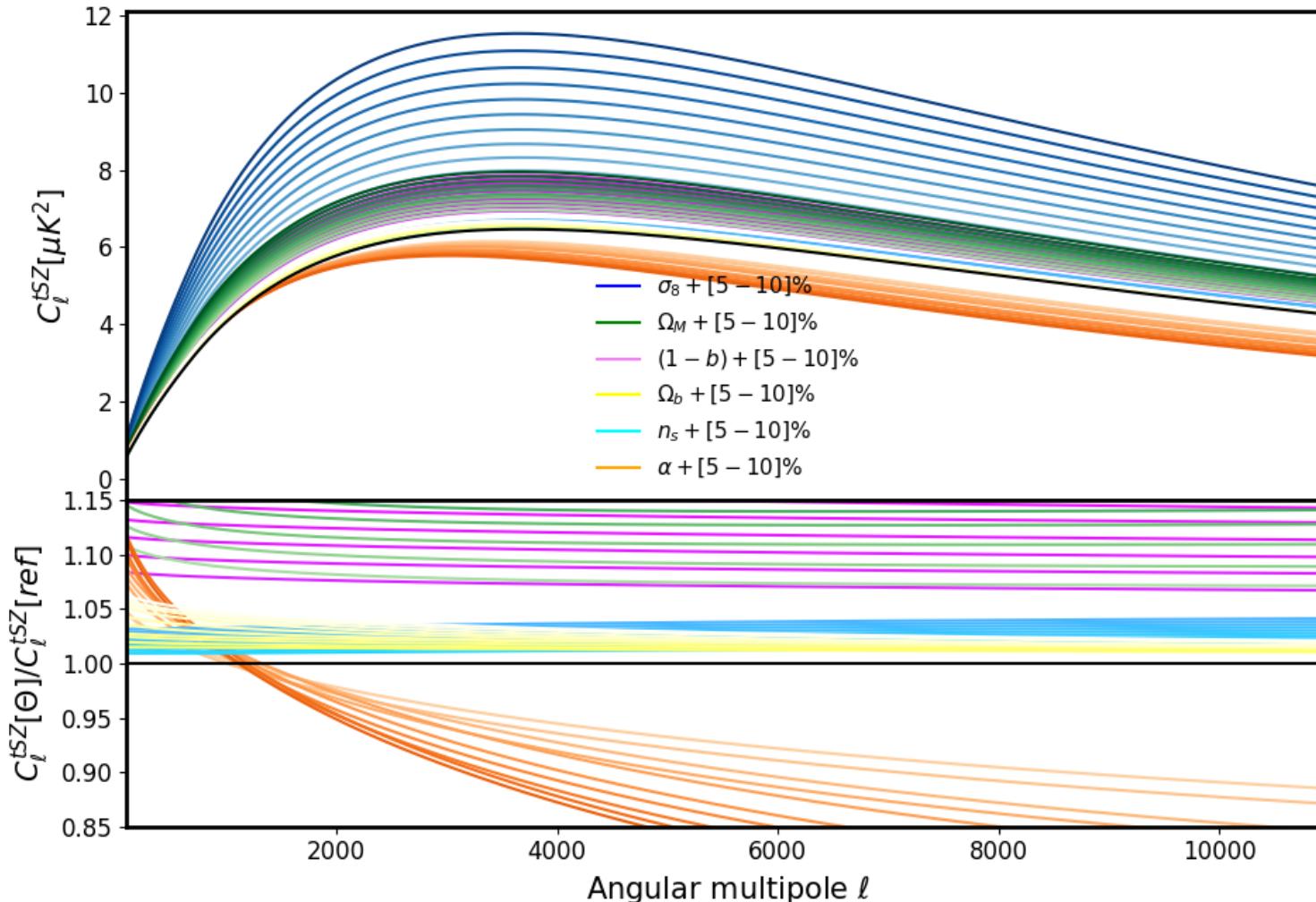
$\sigma$  needs  $\int P(k)$

## Profile

Describes the spatial distribution of the hot gas. Assume Universal pressure profile, the GNFW [Nagai et al., Arnaud et al. , Planck 2014]

# tSZ AND COSMOLOGY

- tSZ effect contains cosmological information



# TSZ POWER SPECTRUM

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$$Cl_s[\Theta] \equiv \iiint dM dz \ dV \ \chi(obs) \ S(obs - M) \ \frac{dN}{dM dz} \ p(M, z)$$

Cl<sub>s</sub> depends on 6 cosmological parameters and  
4 (up to 8) cluster physics parameters  
Amplitude and shape depend on params

In practice we need to compute:  
Redshifts from z=0 and z=3  
Masses from 1e13 to 1e16

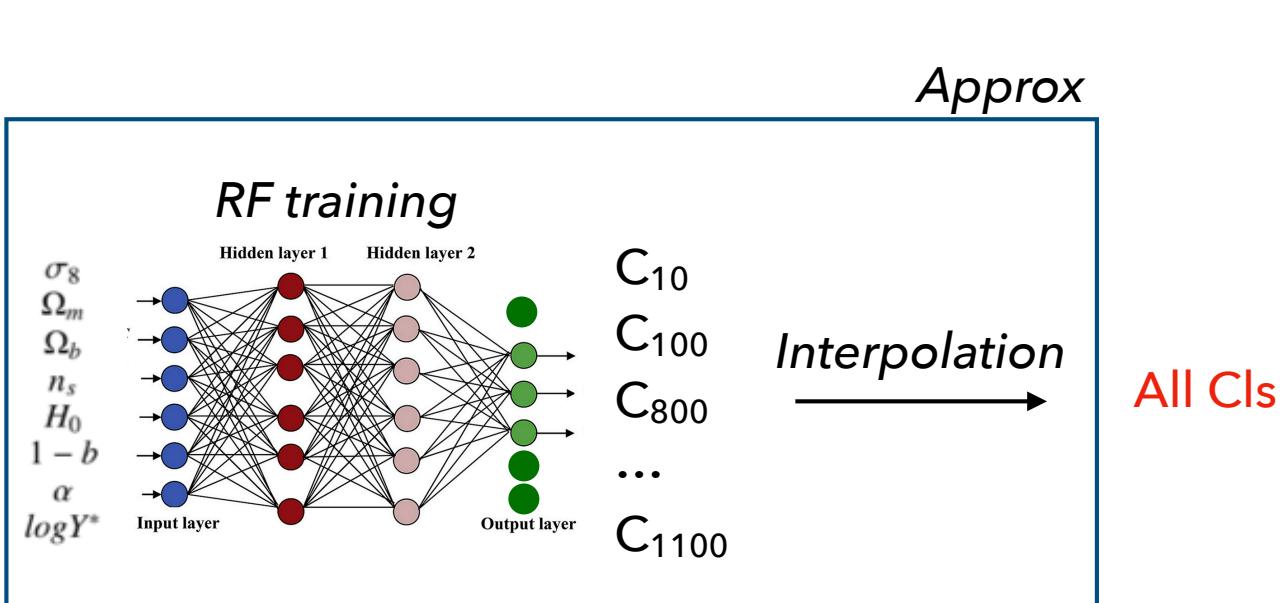
To cover large scales (Planck l=60 ~3deg/sky)  
to small scales (SPT l=12000 ~1arcmin)

Heavy and slow to compute, and slows to  
converge in MCMC

Alternative → Random forest

# MACHINE LEARNING

- Training Random forest with random values of 8 params on 10 l-values of the Cls ( $l=10$  to  $l=11000$ ) [scikit-learn]
- Training 6000 models (test on 2000)
- RF Score of 95%

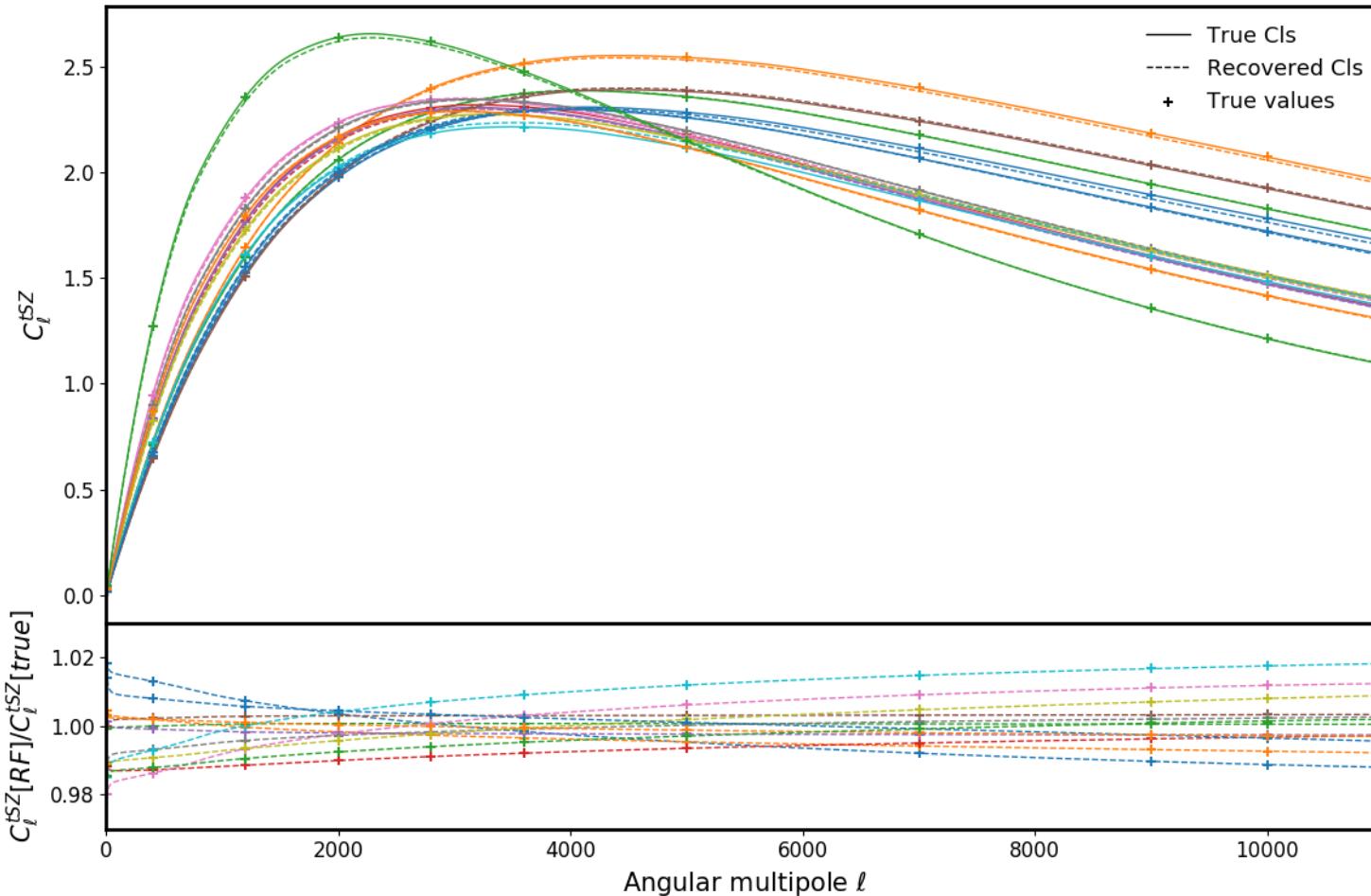


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$\sigma_8$	Amplitude of fluctuations
$\Omega_m$	Matter density
$\Omega_b$	Baryon density
$n_s$	Spectral index
$H_0$	Hubble constant
$1 - b$	Mass bias parameter
$\alpha$	SR Mass exponent
$\log Y^*$	SR amplitude

# RF SZ SPECTRUM

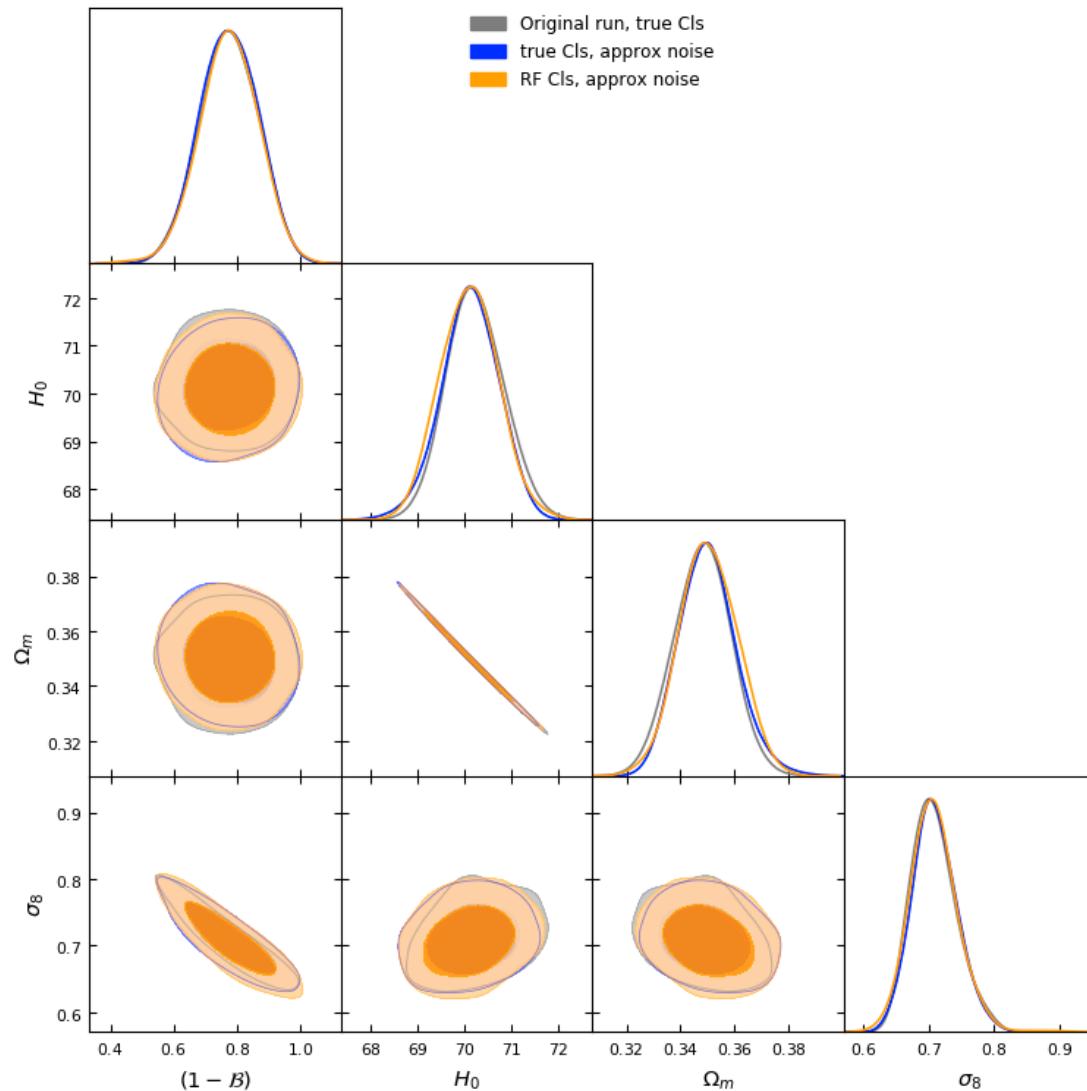
- Prediction on 10 l-values then interpolation



100 times faster to compute

±2% while obs errors are ~20%

- Reproducing constraints from true Cls



More than 10 times  
faster to run chains

*Douspis et al. in prep*

# NEW ANALYSIS OF SPT AND SPT+PLANCK

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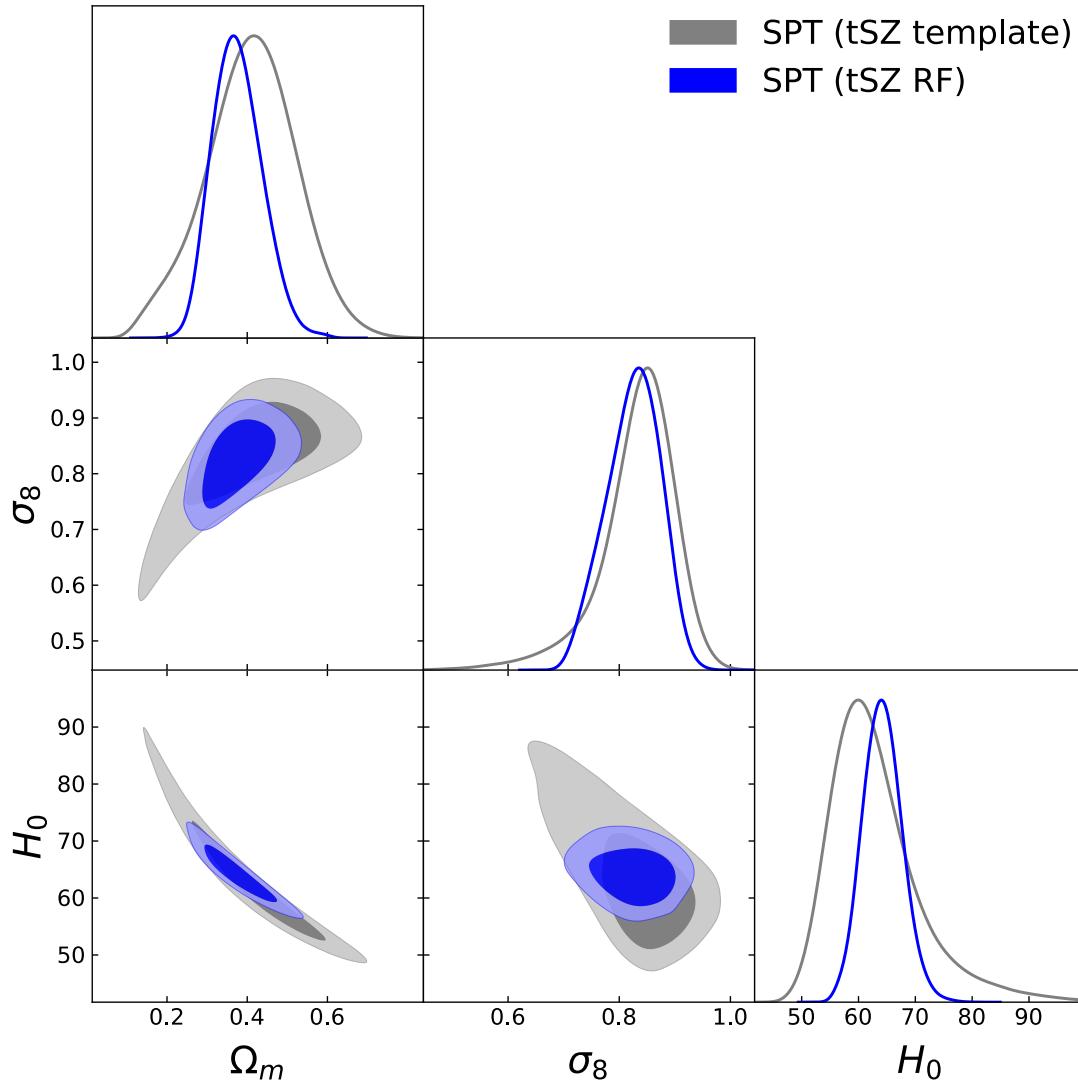


- 6 cross spectra from SPT
- tSZ spectrum from Planck  $y$ -map

# NEW ANALYSIS OF SPT

## Effect of cosmological information of tSZ

$\Omega_M$   
 $\Omega_b$   
 $H_0$   
 $n_s$   
 $\sigma_8$   
 $A_{tSZ}$   
 $Y^*$   
 $\alpha$   
 $(1 - b)$   
+ 6 foreg  
+ 4 instrum  
prior on  $\Omega_b h^2$   
prior on  $n_s$   
prior on  $\alpha$   
prior on  $Y^*$



Stronger constraints  
on  $(\Omega_M, \sigma_8)$

Better  $\chi^2$  with free  
cosmological  
parameters:

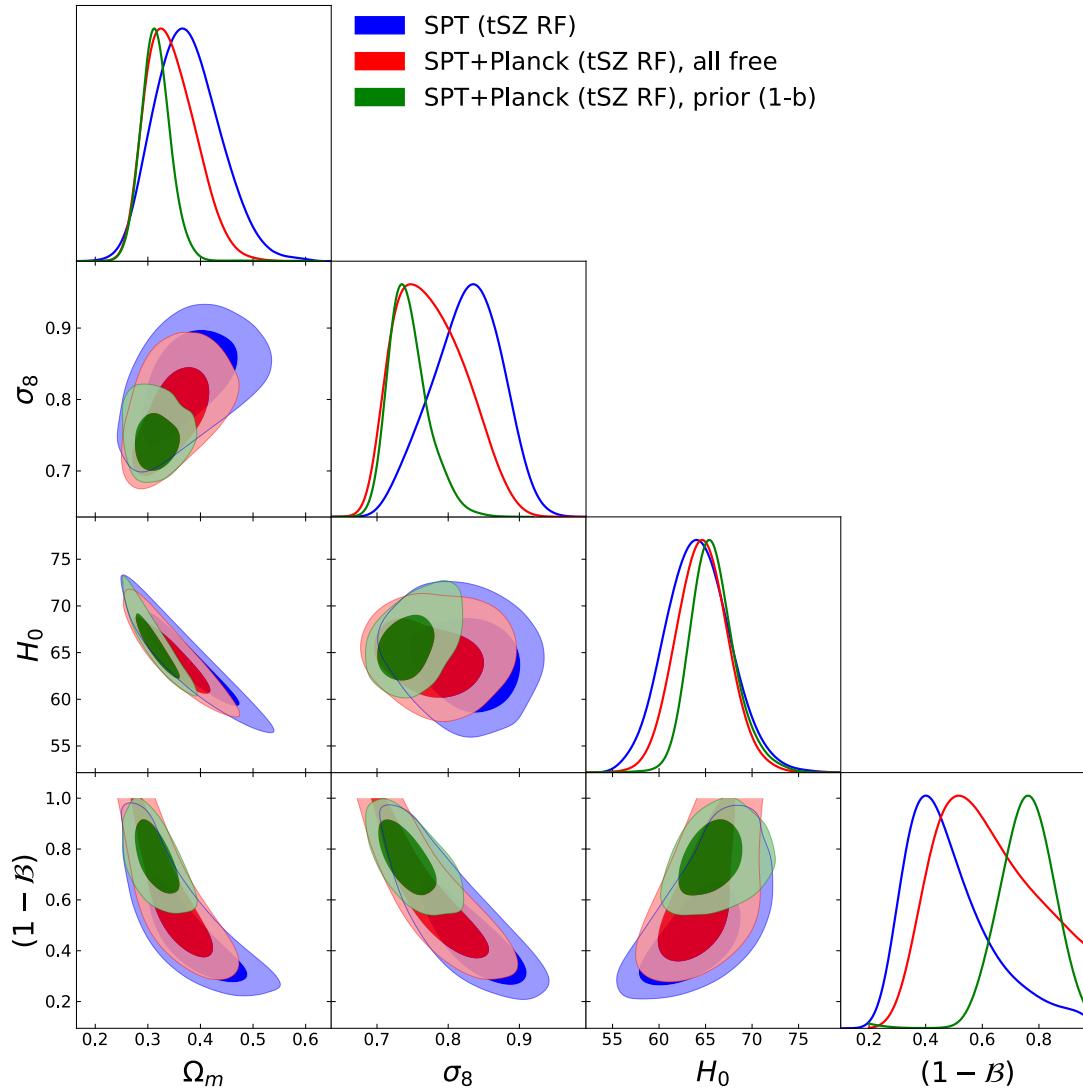
Fixed Cosmo Template	Free Cosmo Template	Free Cosmo RF( $\Theta$ )
236	216	215
dof	$\sim$ dof-3	$\sim$ dof-3

Douspis et al. in prep

# NEW ANALYSIS OF SPT AND SPT+PLANCK

## ● Adding more information

$\Omega_M$   
 $\Omega_b$   
 $H_0$   
 $n_s$   
 $\sigma_8$   
  
 $Y^*$   
 $\alpha$   
 $(1 - b)$   
+ 6 foreg  
+ 4 instrum  
  
prior on  $\Omega_b h^2$   
prior on  $n_s$   
prior on  $\alpha$   
prior on  $Y^*$



Adding Planck tSZ spectrum shifts parameters to more usual values of ( $\Omega_M$ ,  $\sigma_8$ )  
 But do not improve drastically the error bars

Adding Planck tSZ spectrum and prior on the mass bias reduces by factor 2 error bars

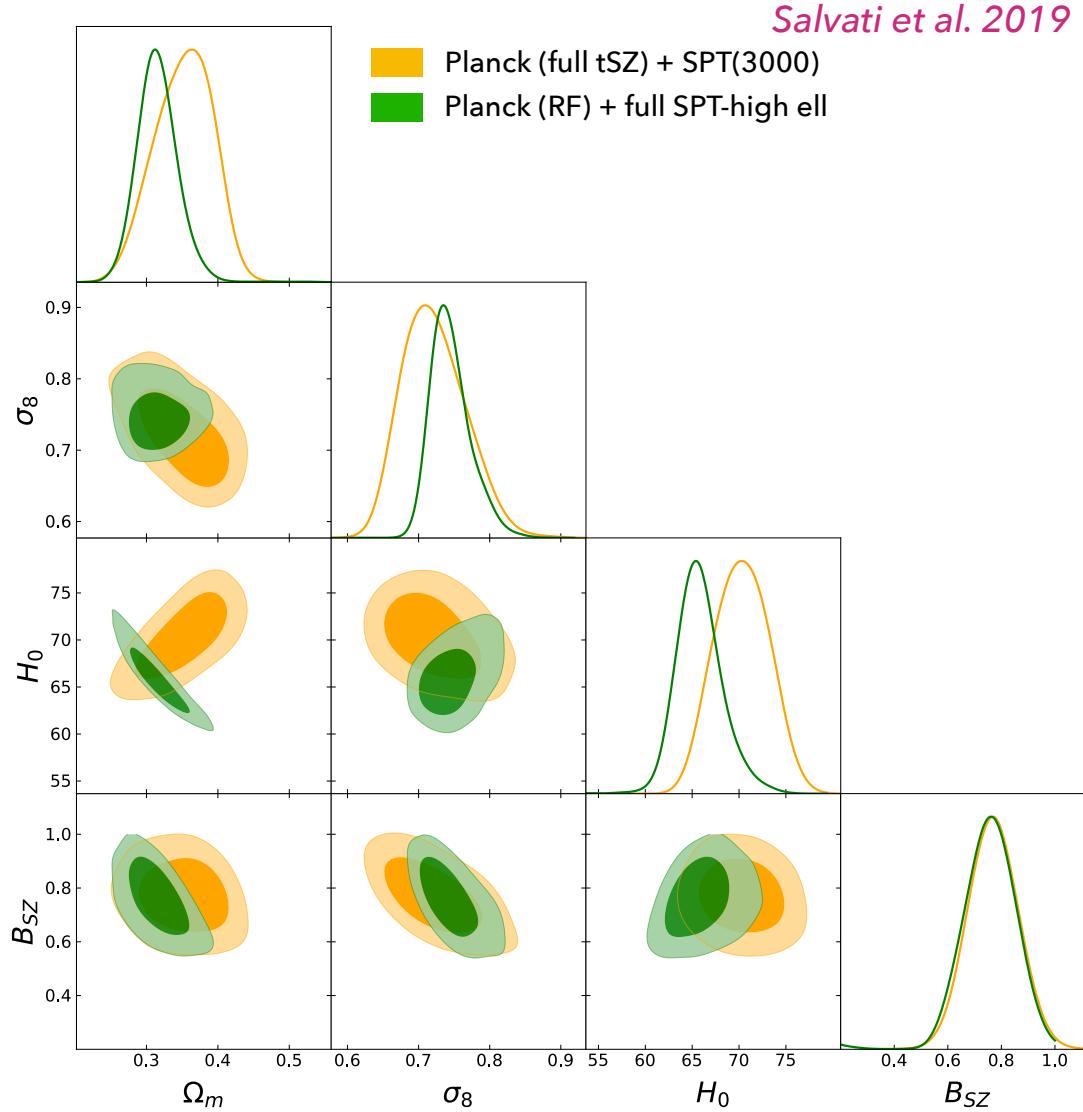
CCCP: Hoekstra et al.

Douspis et al. in prep

# COMPARISON WITH PLANCK + SPT [ELL=3000]

## ● Adding SPT to Planck

$\Omega_M$   
 $\Omega_b$   
 $H_0$   
 $n_s$   
 $\sigma_8$   
  
 $Y^*$   
 $\alpha$   
 $(1 - b)$   
+ 6 foreg  
+ 4 instrum  
  
prior on  $\Omega_b h^2$   
prior on  $n_s$   
prior on  $\alpha$   
prior on  $Y^*$   
prior on  $(1 - b)$

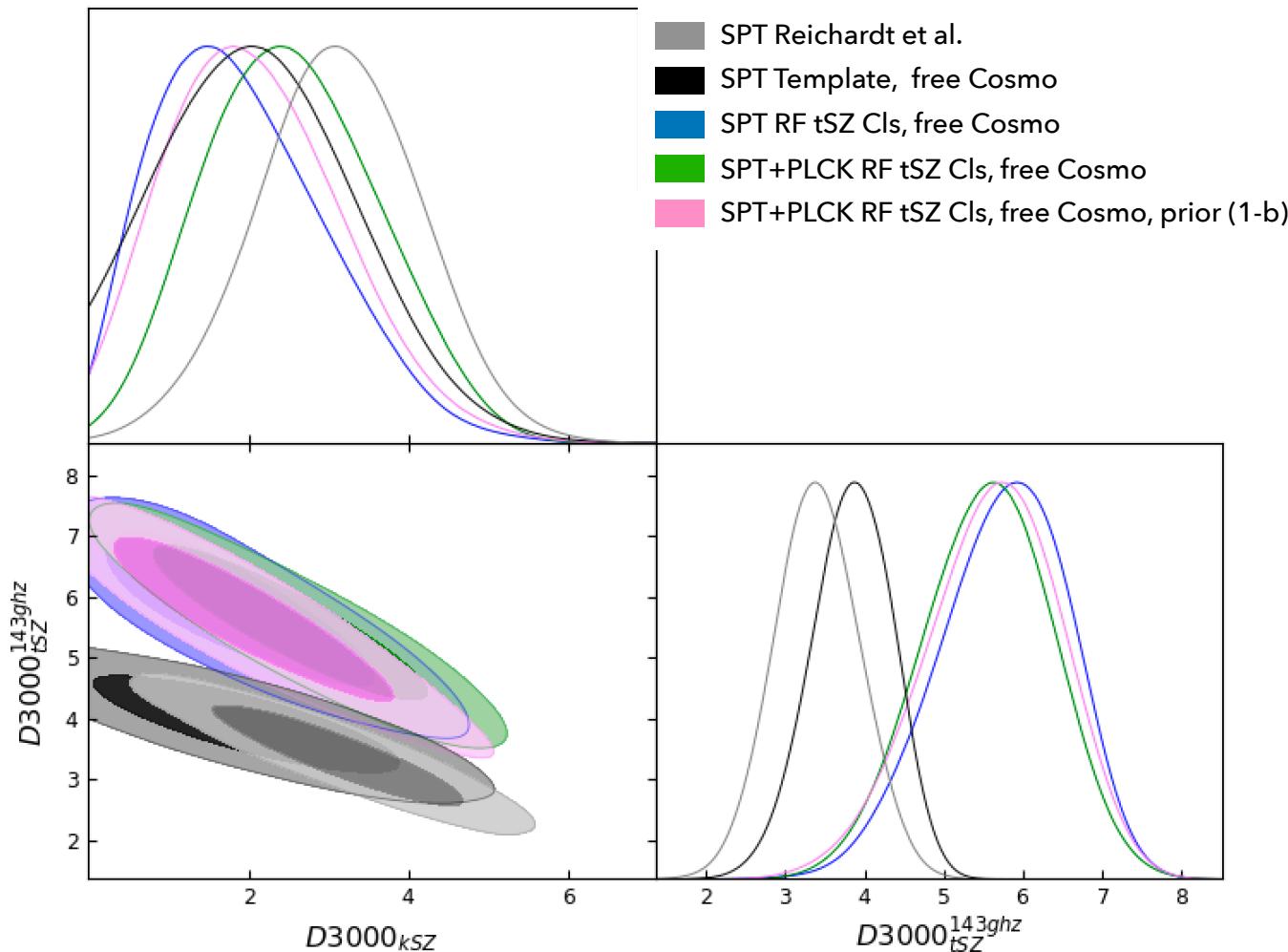


Adding SPT to Planck bring usual values of  $(\Omega_M, \sigma_8)$   
 And breaks degeneracies (because of some CMB in SPT)

*Douspis et al. in prep*

# CONSEQUENCES ON OTHER FOREGROUNDS: kSZ

## ● Degeneracy tSZ / kSZ



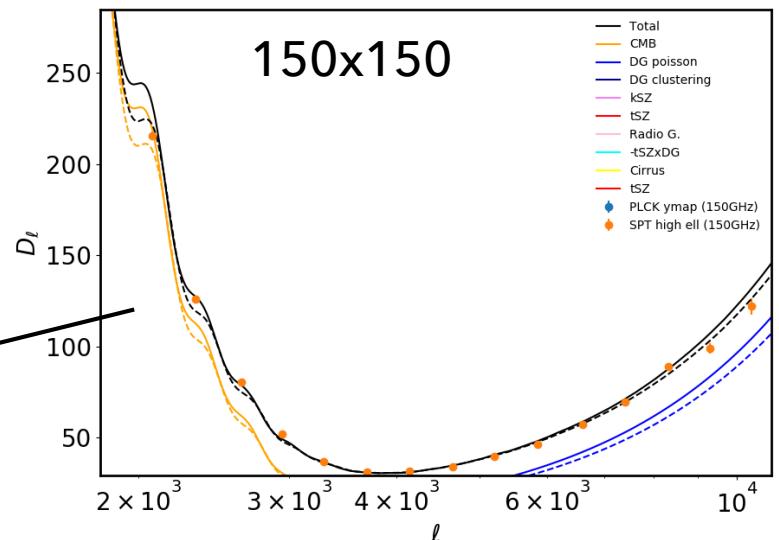
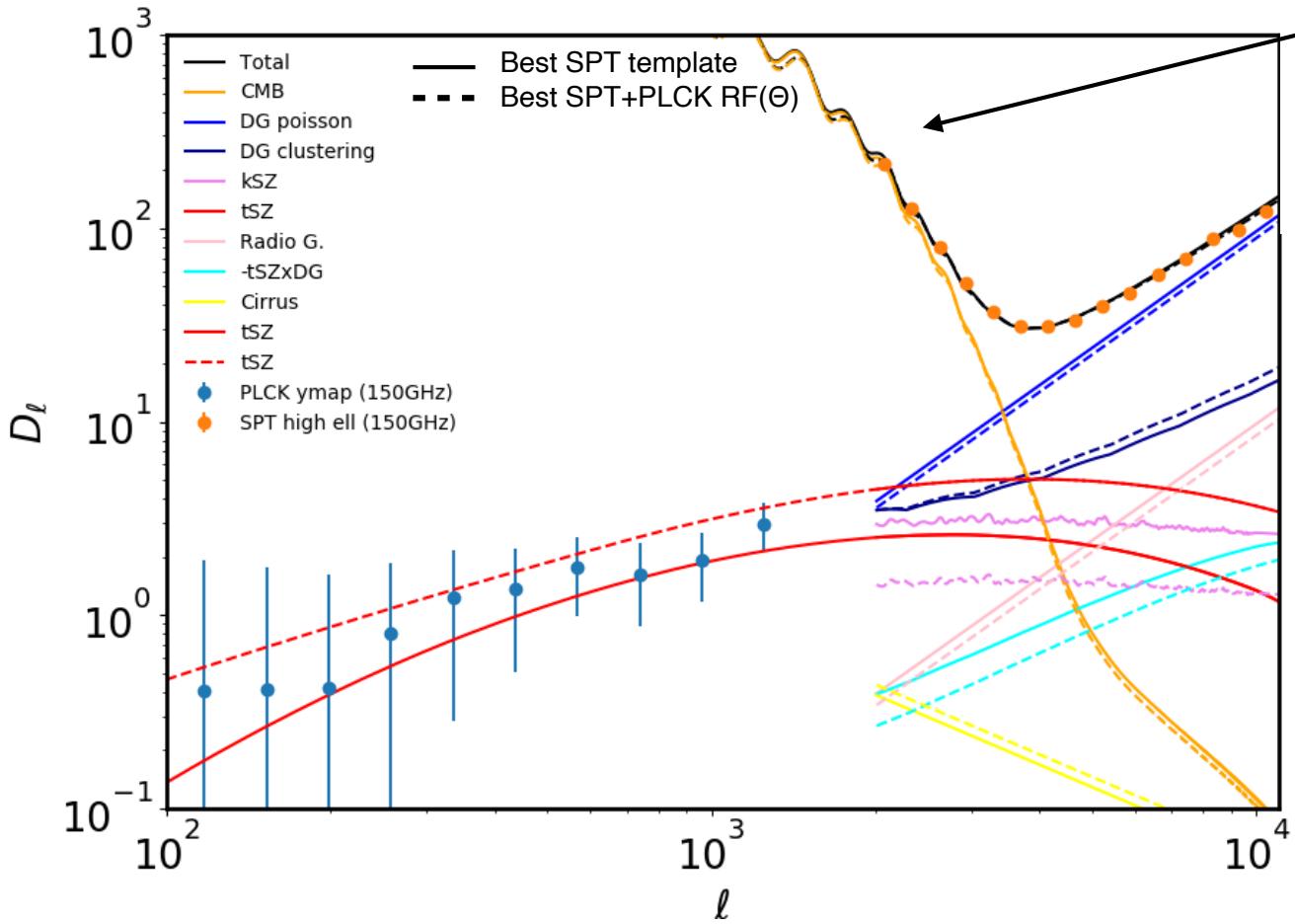
Opening cosmological parameters weakens kSZ detection  
But stays between 1 and 2.5 sigmas depending of combinations

Introducing cosmological dependency of kSZ (Gorce et al.) in future work

*Douspis et al. in prep*

# BACK TO SPECTRA

## Best fits template vs RF( $\Theta$ )



Other 5 cross spectra to be considered

*Douspis et al. in prep*

# CONCLUSIONS

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- First attempt to bring full information of high ell components (focus only on tSZ)
- Moving from template to cosmology dependency brings more constraints
- First combination of Planck tSZ spectrum with SPT-High-ell
  - Lower  $\sigma_8$  preferred
  - Higher amplitude of tSZ spectrum
  - Less room for kSZ

# CONCLUSIONS

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- Inclusion in cosmoMC (f90) code instead of using template or computing halo model, by using Python sklearn Random forest output
- Computation 100 times faster and allow for many tests
- Distributing python tSZ approx for fast computation (Paper 1)
- Moving all to python and training on larger set (and more parameters) and to kSZ (*Gorce et al.*), CIB (*Maniyar et al.*) ... for a full high-ell cosmological analysis (Paper2)

# Thank you !