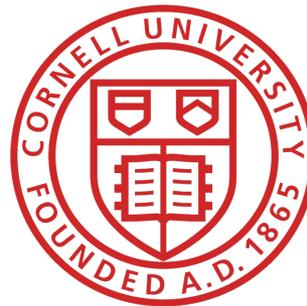


Crunching Away the Hierarchy Problem

Csaba Csáki (Cornell)
with

Raffaele d'Agnolo, Michael Geller, Ameen Ismail

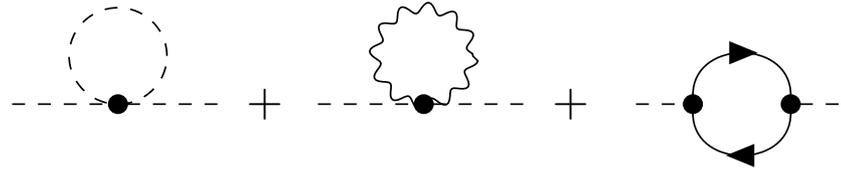
2021 La Thuile Conference
March 11, 2021



Hierarchy problem

All elementary scalars expected to be **ultra heavy**

$$\Delta m_H^2 \propto \frac{g^2}{16\pi^2} \Lambda^2$$



Mass of Higgs **not protected** by symmetries (like fermion, gauge boson)

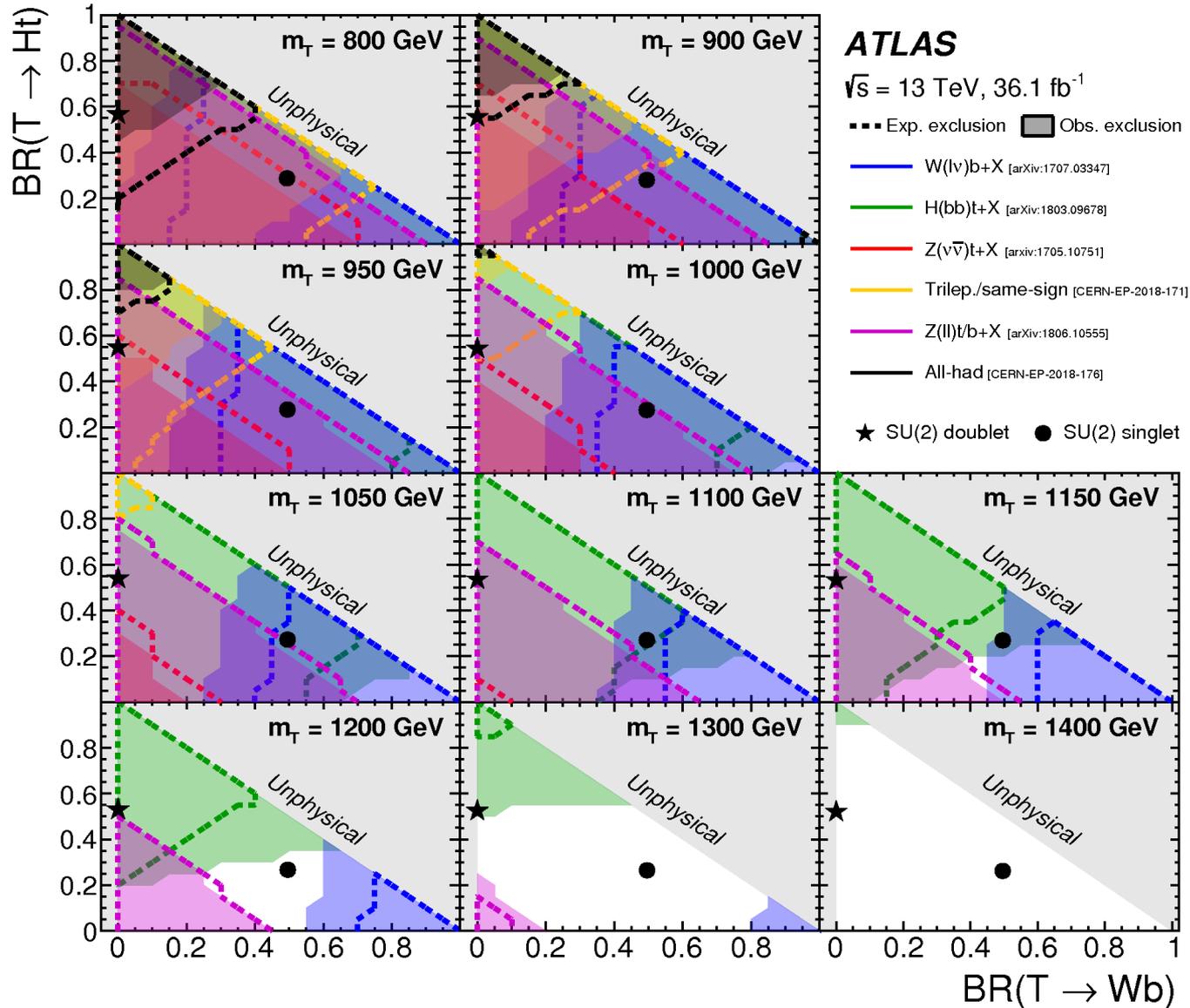
- **Sensitive** to any **UV scale** physics - Λ a **stand-in** for mass of whatever new physical particle appears there

Symmetry based approach

- New physics at the TeV scale shields from UV corrections - SUSY, compositeness/XD
- Typically expect new colored particles at the TeV scale “top partners”
- Not observed at the LHC - putting these models under serious stress

• Direct bounds

Spin 1/2 top partners



Symmetry based approach

- New physics at the TeV scale shields from UV corrections - SUSY, compositeness/XD
- Typically expect new colored particles at the TeV scale “top partners”
- Not observed at the LHC - putting these models under serious stress
- Could still avoid them via “neutral naturalness/ Twin Higgs” type models
- Those still possible, though deviation to Higgs coupling will test those eventually as well

Cosmological selection/relaxation

- Correction to Higgs mass **not suppressed**
- **Cosmological dynamics** of some light field leads to **selection** of realistic vacuum
- Examples: **relaxion**, **N-naturalness**, ...
- Very **interesting** direction, quite baroque models (or regions of parameter space)

Anthropic approach

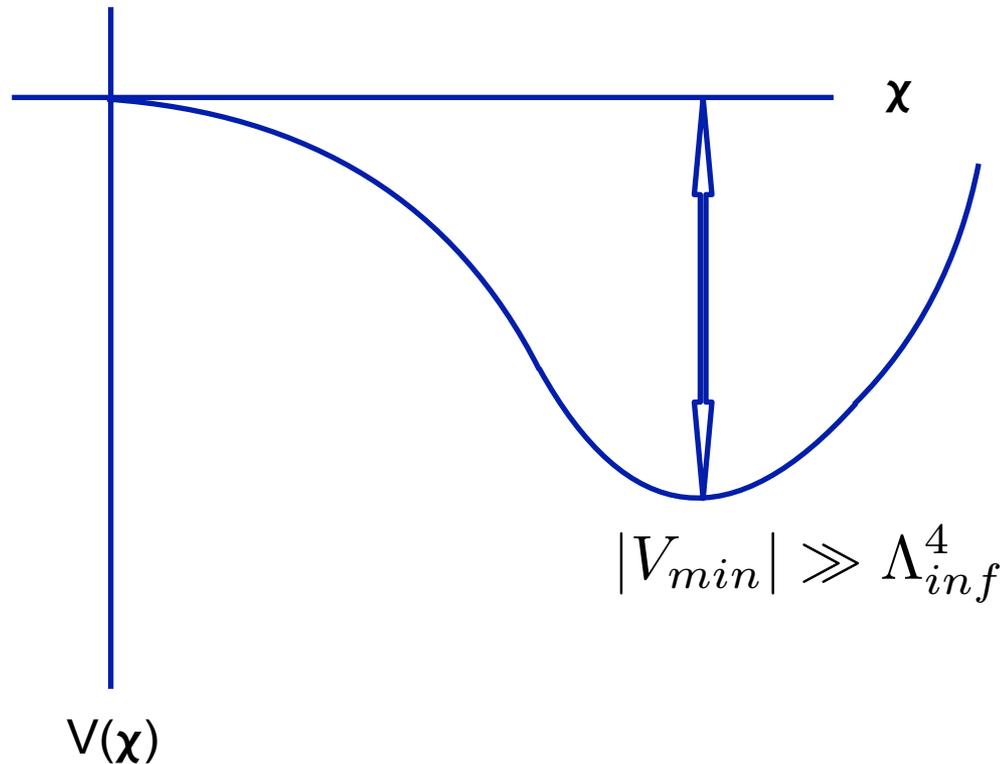
- **Multiverse** with different patches - each **patch** has a **different Higgs mass** and $O(1)$ quartics.
- Only patches with **small Higgs VEV** can support life (otherwise no chemistry?)
- **No** way to experimentally verify
- Also motivation for **split SUSY**

Crunching solution to hierarchy problem

- Our proposal: somewhere in between, take best aspects of each approach
- Assume we still have a multiverse with the various patches having different Higgs masses/VEVs
- There is also a hidden CFT that is spontaneously broken - producing a (light) dilaton
- True ground state of CFT has large negative vacuum energy leading to the rapid crunch of the patch in that vacuum

Crunching solution to hierarchy problem

- The **true minimum** has a very large negative CC

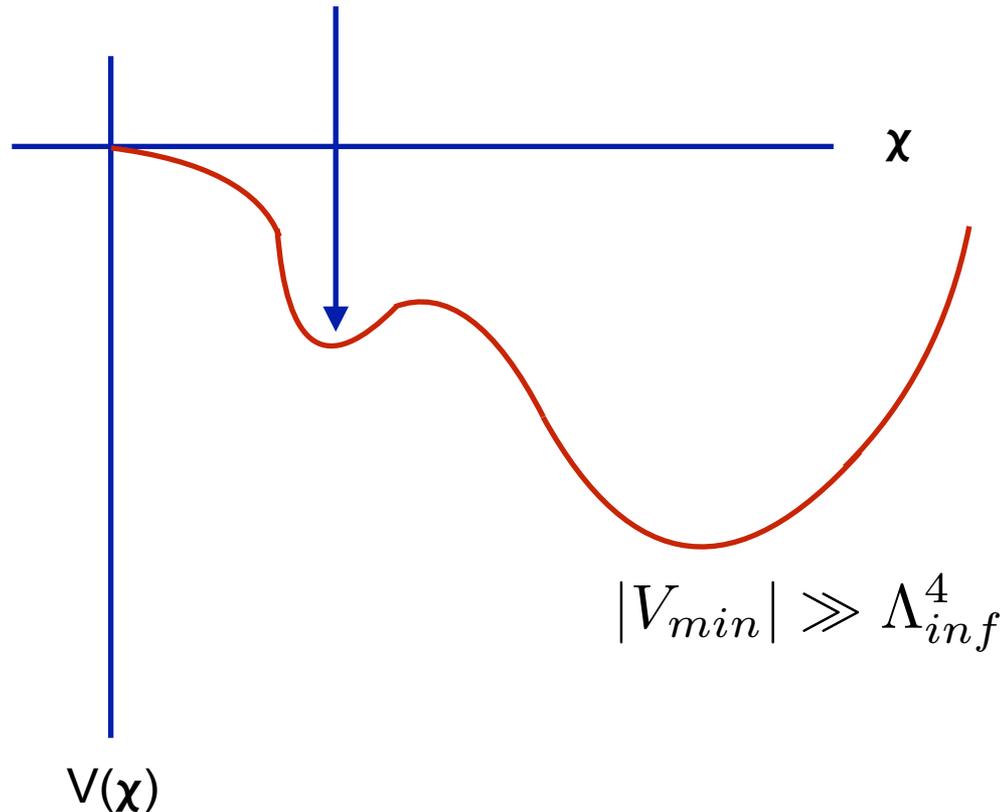


Crunching solution to hierarchy problem

- The **techniquarks** of the CFT charged under $SU(2)$ EW symmetry - leads to interaction between **dilaton** and **SM Higgs**
- If Higgs VEV non-zero $< \text{TeV}$ - **second metastable minimum** of the dilaton potential appears at **small vacuum energy**
- **Patches with large** or vanishing Higgs VEV will **quickly dynamically crunch**, only patches with small Higgs VEVs will survive over a long period
- Patches with **small Higgs VEV** will **dominate** after long time (unlike anthropics)

Crunching solution to hierarchy problem

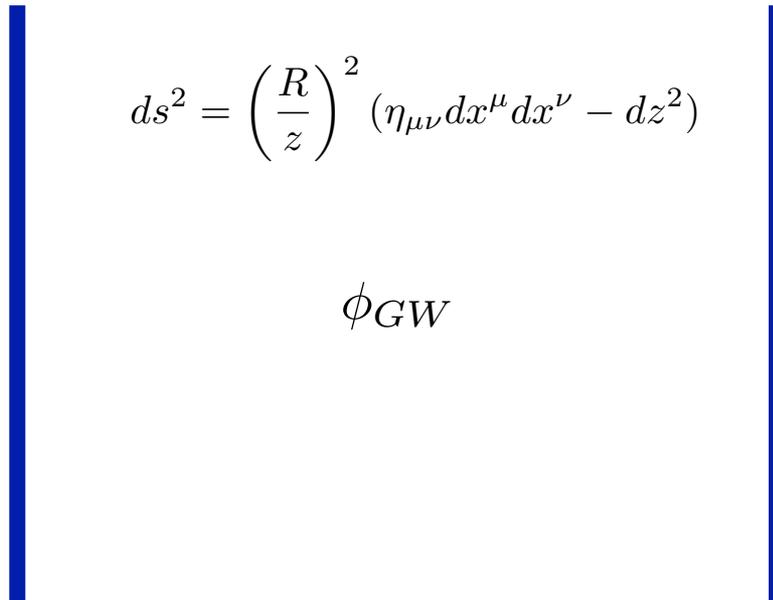
- **New minimum** of potential due to $\langle H \rangle \sim \text{TeV}$



- At new minimum **CC** should be **smaller** so that universe can undergo normal inflation and expansion

The RS/GW setup

- GW field ϕ in the bulk, with small mass δ



The diagram illustrates the RS/GW setup. Two vertical blue lines represent the UV and IR boundaries. The UV boundary is on the left, labeled "UV z=R", and the IR boundary is on the right, labeled "IR z=R'". The bulk region between them contains the metric $ds^2 = \left(\frac{R}{z}\right)^2 (\eta_{\mu\nu} dx^\mu dx^\nu - dz^2)$ and the GW field ϕ_{GW} . To the right of the IR boundary, the coordinate $\chi = \frac{1}{R'}$ and the mass parameter $k = 1/R'$ are defined.

$$ds^2 = \left(\frac{R}{z}\right)^2 (\eta_{\mu\nu} dx^\mu dx^\nu - dz^2)$$
$$\chi = \frac{1}{R'}$$
$$\phi_{GW}$$
$$k = 1/R'$$

UV z=R

IR z=R'

- Effective dilaton potential after integrating out bulk

$$V_{GW}(\chi) = -\lambda\chi^4 + \lambda_{GW} \frac{\chi^{4+\delta}}{k^\delta}$$

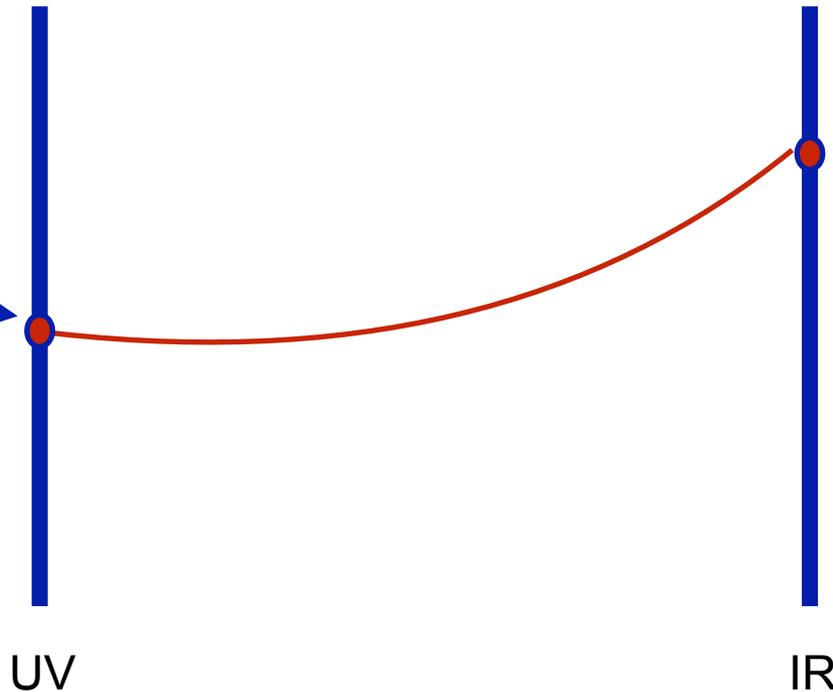
Effect of the Higgs

- **Higgs also in the bulk** (otherwise can not influence dilaton)

SM Higgs potential on UV:

$$V_H(H) = -m_{H,i}^2 H^\dagger H + \lambda (H^\dagger H)^2$$

Acts as source for bulk



Localized Higgs coupl. generates interaction with dilaton

- Assume **UV brane Higgs potential is varying** in different patches and $m_{H,i}^2$ is $\mathcal{O}(\Lambda^2)$

Effect of the Higgs

- Assume **bulk Higgs mass** (Higgs approx. linear)

$$\frac{m_b^2}{k^2} \approx -3 + \alpha$$

- General **z-dependence** $\sim z^{2 \pm \sqrt{4 + m_b^2}}$

- Effect of **UV source** on IR brane: $H_{UV} \chi^{\sqrt{4 + m_b^2} - 2} = H_{UV} \chi^{\frac{\alpha}{2} - 1}$

- Adding **IR localized Higgs terms** will result in terms

$$|H|^2 \chi^{2+\alpha}$$

$$|H|^4 \chi^{2\alpha}$$

$$|H|^2 \chi^{2+\alpha+\epsilon}$$

The CFT interpretation

- A CFT which is charged under $SU(2)$. Turn on two operators:

- **singlet** \mathcal{O}_ϵ of dimension $4 - \epsilon$

- **doublet** \mathcal{O}_H of dimension $3 + \alpha/2$.

- We couple the doublet operator to the Higgs in the UV:

$$\tilde{\lambda}_H \mathcal{O}_H^\dagger H + \tilde{\lambda}_\epsilon \mathcal{O}_\epsilon$$

- In the IR, we get the effective potential:

$$V_{eff} = a_0 \chi^4 + a_1 \tilde{\lambda}_H^2 H^2 \chi^{2+\alpha} + a_2 \tilde{\lambda}_H^4 H^4 \chi^{2\alpha} \\ + a_3 \tilde{\lambda}_\epsilon \chi^{4+\epsilon} + a_4 \tilde{\lambda}_\epsilon \tilde{\lambda}_H^2 H^2 \chi^{2+\alpha+\epsilon} + \dots$$

The full potential

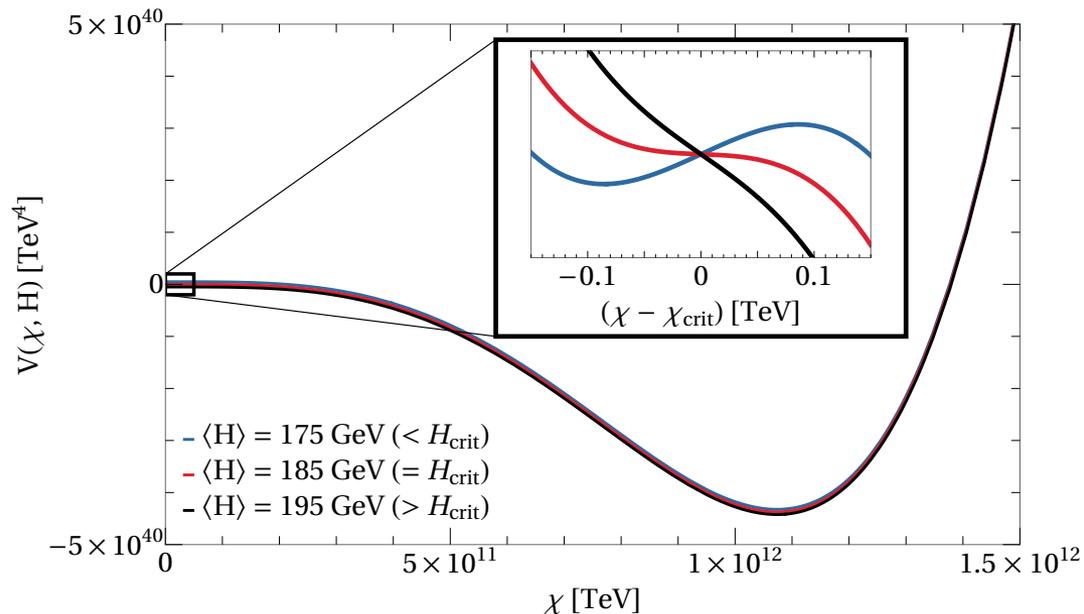
- The **full potential**: $V(\chi, H) = V_{\text{GW}}(\chi) + V_{H\chi}(\chi, H) + V_H(H)$.

$$V_H(H) = -m_{H,i}^2 H^\dagger H + \lambda (H^\dagger H)^2$$

$$V_{\text{GW}}(\chi) = -\lambda\chi^4 + \lambda_{\text{GW}} \frac{\chi^{4+\delta}}{k^\delta}$$

$$V_{H\chi}(\chi, H) = \lambda_2 |H|^2 \frac{\chi^{2+\alpha}}{k^\alpha} - \lambda_{H\epsilon} |H|^2 \frac{\chi^{2+\alpha+\epsilon}}{k^{\alpha+\epsilon}} - \lambda_4 |H|^4 \frac{\chi^{2\alpha}}{k^{2\alpha}}$$

- Second minimum** (close to the origin) exists **only if** $\langle H \rangle$ is smaller than a critical value



Generating the hierarchies

- The scale of the Higgs VEV is set by

$$h_{crit} \sim k \left(\frac{\lambda_2}{\lambda_{H\epsilon}} \right)^{\frac{1}{\epsilon}}$$

- To get $h_{crit} \ll k$ need $\epsilon \ll 1$ and $\lambda_2 < \lambda_{H\epsilon}$
- Technically similar to the GW implementation of RS hierarchy (but here Higgses are elementary, totally different physics driving the hierarchy)
- In CFT language again need operators with small anomalous dimensions

Generating the hierarchies

- Since Higgs is in the bulk, we will also have SU(2) bulk gauge bosons and their KK modes. Those have to be $> 3\text{-}4$ TeV from LHC bounds.

- Implies little hierarchy $\frac{h}{\chi_{\min}} \simeq \frac{h_{\text{crit}}}{\chi_{\min}} \lesssim 0.1$

- Since $\chi_{\min} \simeq \left(\frac{h^2}{k^\alpha} \frac{2\alpha\lambda_4}{(2+\alpha)\lambda_2} \right)^{\frac{1}{2-\alpha}}$ need $\lambda_2, \lambda_{H\epsilon} < 10^{-2}\alpha\lambda_4$

- To avoid low Landau-pole $\lambda_4 \lesssim 3$, leading to $\lambda_2 \lesssim 10^{-2}$

- To ensure $V_{\chi H}$ dominates over V_{GW} at χ_{crit} also need $\lambda \sim \lambda_{\text{GW}} \lesssim \frac{\lambda_2^2}{\lambda_4}$ $\lambda, \lambda_{\text{GW}} \lesssim 10^{-5}$

A light dilaton

- Consequence of little hierarchy: **dilaton** must be quite **light** and **weakly coupled**

- **Mixing** with Higgs: $\sin \theta \sim \frac{(\lambda_2 - \lambda_{H\epsilon})}{N} \frac{h\chi_{\min}}{m_h^2}$
- **Dilaton mass** $m_\chi \simeq m_h \sqrt{\frac{h}{\chi_{\min}} \frac{\pi \sin \theta}{\sqrt{6}N} - \frac{8\pi^2(\lambda - \lambda_{\text{GW}})}{N^2} \frac{\chi_{\min}^2}{m_h^2}}$
- **Mass bound:** $0.2m_h \gtrsim m_\chi \gtrsim 2\pi \frac{\chi_{\min}}{N} \sqrt{2(\lambda - \lambda_{\text{GW}})}$
- **Since** $\chi_{\min} \simeq \text{TeV}$, $N \lesssim 40$ and $\lambda, \lambda_{\text{GW}} \gtrsim 10^{-6}$
- **Numerically** $0.1 \text{ GeV} \lesssim m_\chi \lesssim 10 \text{ GeV}$

A weakly coupled dilaton

- Dilaton will inherit Higgs interactions with SM matter from small mixing $\sin \theta \sim m_\chi^2/m_h^2$

- Numerically $10^{-7} \leq \sin \theta \leq 10^{-2}$

- Direct coupling to bulk gauge bosons via

$$\frac{\chi}{2\chi_{\min} \log \frac{R'}{R}} (F_{\mu\nu}^2 + Z_{\mu\nu}^2 + 2W_{\mu\nu}^2)$$

- Significant for photons $\frac{1}{4\Lambda_{\gamma\gamma}} \tilde{\chi} F_{\mu\nu}^2$, sub-leading for W,Z

Scan of parameter space

- **Generated** 10^5 points in region

$k = 10^{11}$ GeV, $\delta = 0.01$, $N = 3$ and $\alpha = 0.05$, while uniformly sampling the other parameters from the ranges $\lambda_{\text{GW}} \in (0.5, 1.5) \times 10^{-5}$, $\lambda_2 \in (0.5, 1.5) \times 10^{-2}$, $\lambda_{H\epsilon} \in (2, 4) \cdot \lambda_2$, $\lambda_4 \in (2, 3)$, and $\epsilon \in (0.03, 0.1)$. We also took $\lambda = 1.1 \lambda_{\text{GW}}$ and set the Higgs VEV $\langle H \rangle \simeq 174$ GeV.

- **Requiring:**

- The metastable vacuum must exist and be located at $\chi_{\text{crit}} > 1$ TeV.
- $h_{\text{crit}} \leq 2$ TeV so the Higgs VEV is natural.
- The metastable vacuum reproduces the SM values of the Higgs mass and VEV and corresponds to a stable local minimum of the 2 dimensional potential.
- The $O(4)$ bounce action S_4 between the two potential minima is at least $\mathcal{O}(200)$ so that tunnelling is suppressed.

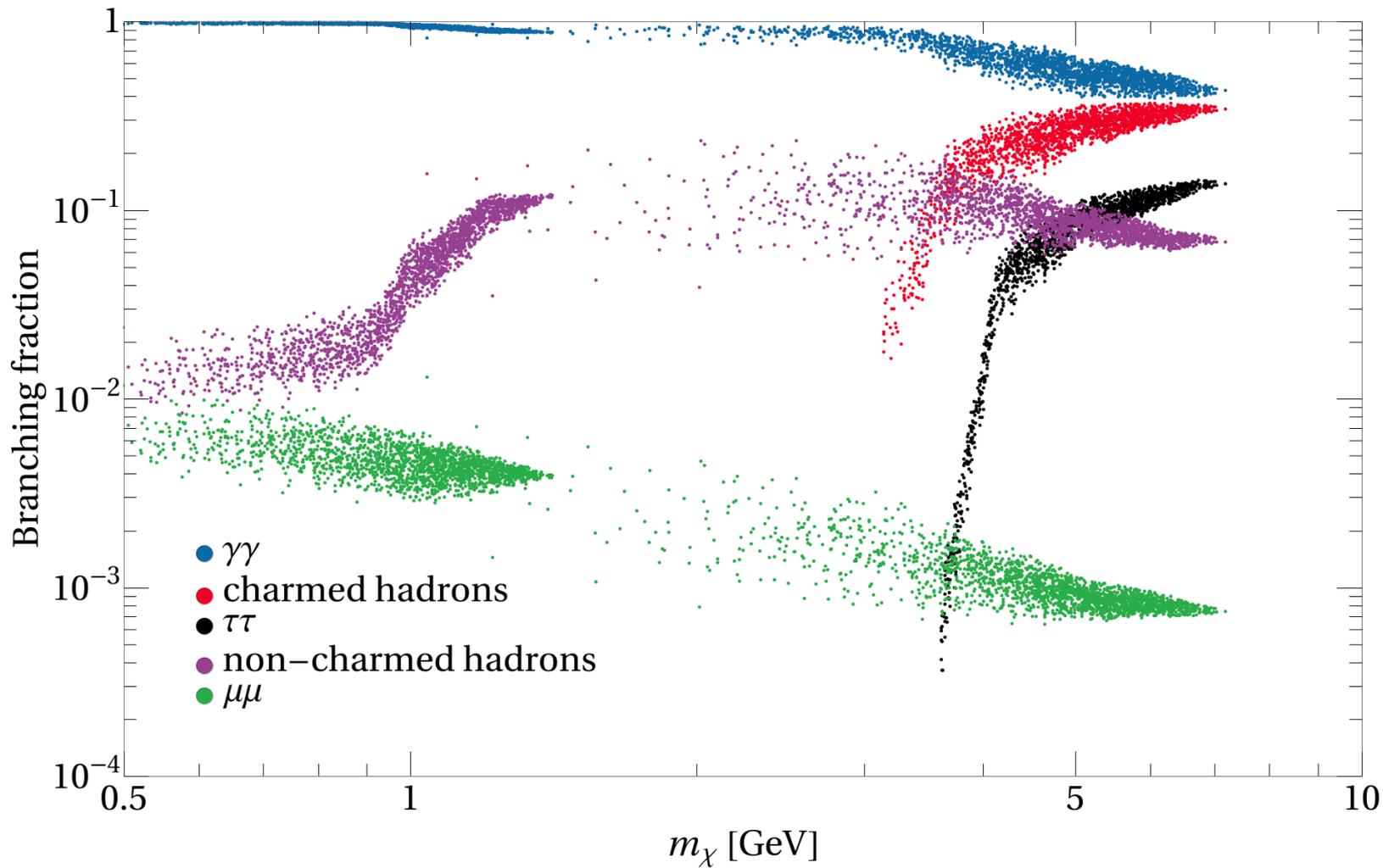
Scan of parameter space

- **Second scan** 5×10^4 points to test region with smaller dilaton masses

$$N = 8, \alpha = 0.1, \lambda_{\text{GW}} = 2 \times 10^{-6},$$
$$\lambda_2 \in (0.5, 1) \times 10^{-2}, \text{ and } \epsilon \in (0.05, 0.1)$$

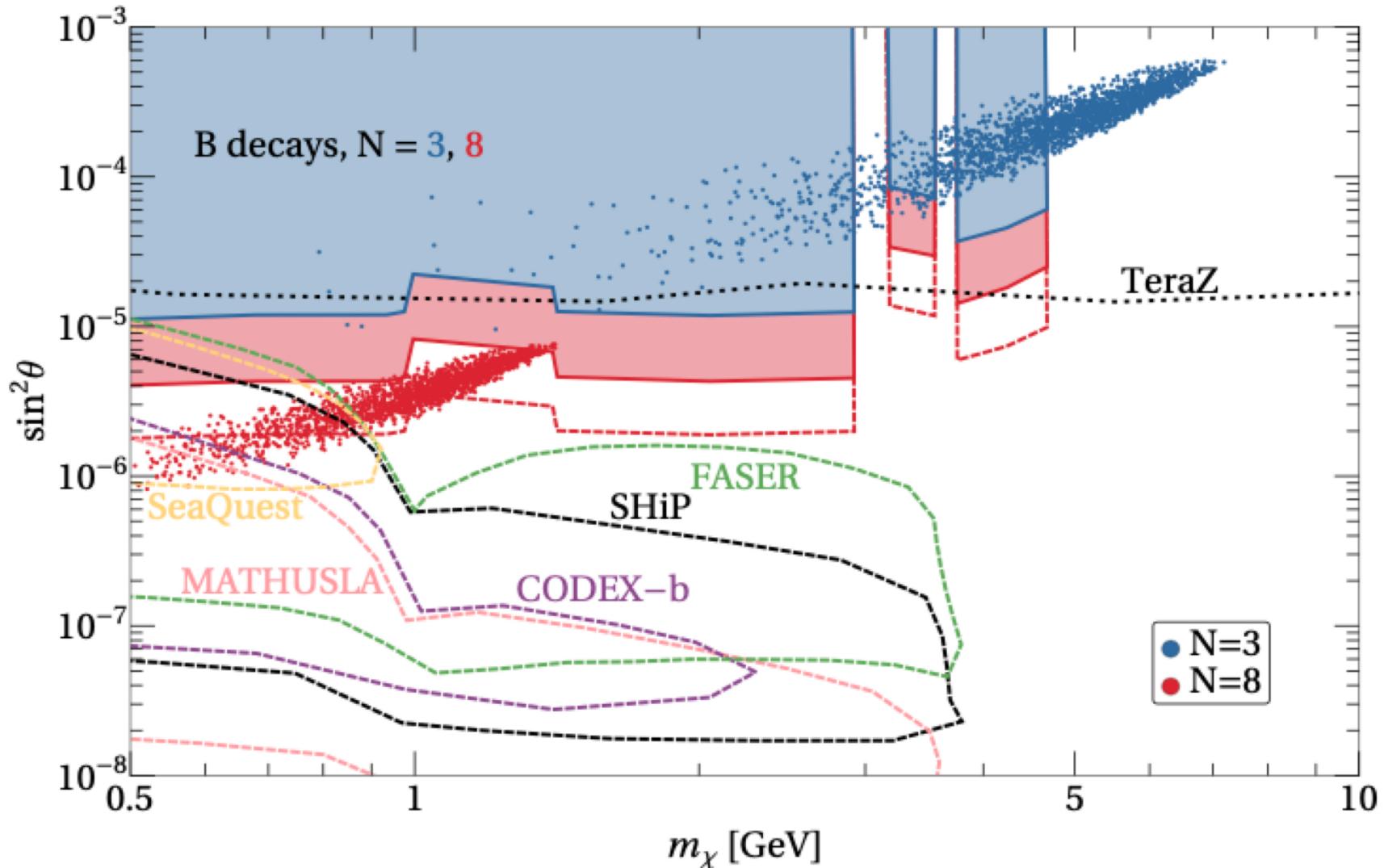
- And same requirements

Dilaton couplings



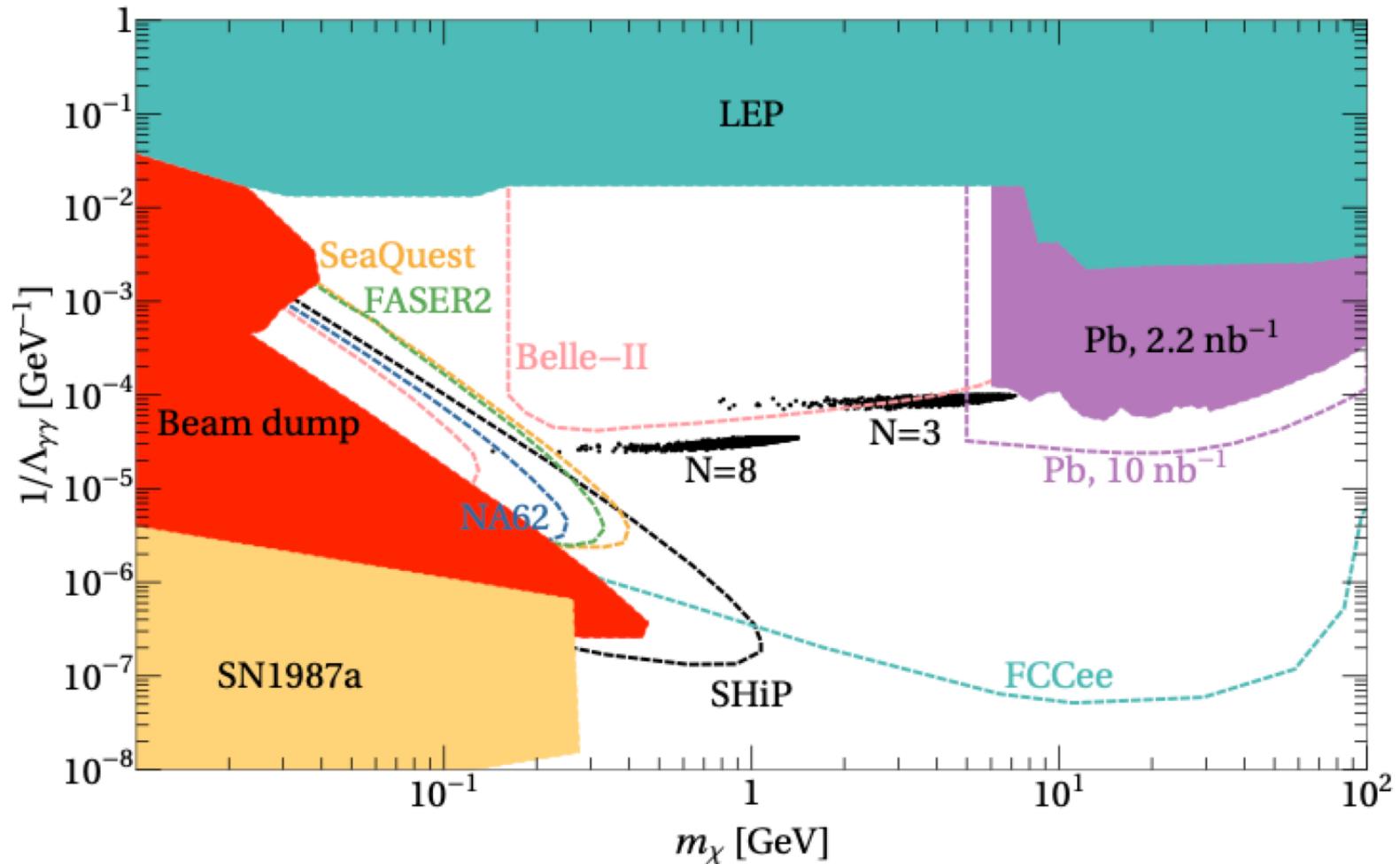
Constraints on dilaton

- Rare B-meson decays - LHCb and future LHCb projections
- $e^+e^- \rightarrow Z\chi$ at FCCee on the Z-pole
- Projections for searches for hidden light particles



Constraints on dilaton

- Direct photon coupling - tested at LEP from $e^+e^- \rightarrow \gamma\chi \rightarrow 3\gamma$
- FCCee will cover full region
- Future heavy ion collisions will also have some sensitivity



Experimental signals

- **Light dilaton** that can be observed (large regions already excluded)
- Also have **W,Z KK modes** - but these **don't** play a role in **stabilizing hierarchy**
- **No top partners!**
- While the construction is based on RS model, the **Higgs is elementary** here
- Physics (and signals) are completely **different from** holographic composite Higgs/**MCHM**-type constructions

Cosmological constraints

- During inflation **Hubble** scale should be **below EW** so that dilaton potential sensitive to Higgs VEV

$$M_I < \sqrt{M_W M_{\text{Pl}}} \simeq 10^7 \text{ TeV}$$

- **Cutoff** should be **below** this $\Lambda < M_I < 10^7 \text{ TeV}$
- **Energy** density in true vacuum **really negative**

$$\lambda \chi_{GW}^4 > M_I^4 \quad \longrightarrow \quad k \gtrsim 17 M_I \text{ for } \lambda \simeq 10^{-5}$$

- If **CC** problem solved by **anthropics** - maximal CC should **not overwhelm** negative CC at GW

minimum:

$$\Lambda_{max} < \lambda \chi_{GW}^4$$

Avoiding Eternal Inflation

- Ensure that **patch actually crunches** for VEV's with small or large $\langle H \rangle$
- **Field should roll** down to true minimum, not get stuck eternally inflating. To ensure: **quantum diffusion never dominates** over classical evolution
- At **large Higgs VEVs** second derivative of potential at least $O(v^2)$ - and Hubble already required to be smaller
- At **zero Higgs VEV** situation **more subtle** - only have χ^4 term very small. Need to add new gauge group in bulk - a la **Servant/von Harling**

Summary

- New approach to the hierarchy problem
- Regions in space with large (or 0) Higgs VEV dynamically crunch
- Implementation via RS/GW construction
- Predicts light dilaton, can be measured
- No top partners, but W,Z KK modes
- Can also find a similar “solution” to the CC problem (but didn’t fit on the margins)

Backup slides

Properties of the potential

- Find **critical value** of h by neglecting GW piece

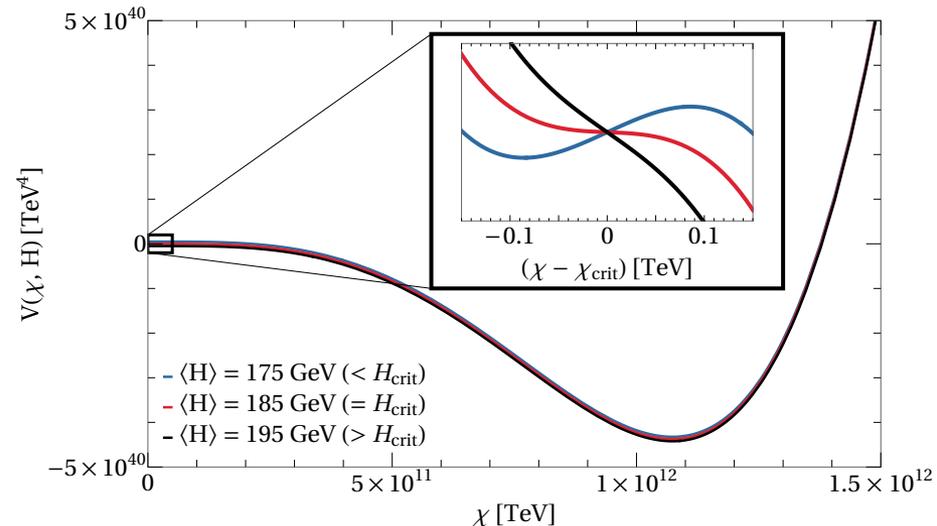
$$V_{H\chi}(\chi, H) = \lambda_2 |H|^2 \frac{\chi^{2+\alpha}}{k^\alpha} - \lambda_{H\epsilon} |H|^2 \frac{\chi^{2+\alpha+\epsilon}}{k^{\alpha+\epsilon}} - \lambda_4 |H|^4 \frac{\chi^{2\alpha}}{k^{2\alpha}}$$

$$h_{crit} \sim k \left(\frac{\lambda_2}{\lambda_{H\epsilon}} \right)^{\frac{1}{\epsilon}}$$

- Value of χ at **inflection point**: $\chi_{crit} = k \left(\frac{\lambda_2}{\lambda_{H\epsilon}} \frac{4 - \alpha^2}{(2 + \epsilon)^2 - \alpha^2} \right)^{1/\epsilon}$

- The **minimum**:

$$\chi_{min} \simeq \left(\frac{h^2}{k^\alpha} \frac{2\alpha\lambda_4}{(2 + \alpha)\lambda_2} \right)^{\frac{1}{2-\alpha}}$$



The small χ region

- To ensure we **don't** get **stuck** at small χ need to add **additional** piece to **dilaton** potential $\lambda_\gamma \chi^\gamma \tilde{\Lambda}^{4-\gamma}$
- Effect of **additional** small explicit breaking of scale invariance at **scale** $\tilde{\Lambda} \ll k$.
- **Until** scale $\chi_* \sim \tilde{\Lambda} \lambda_\gamma^{\frac{1}{4-\gamma}}$ effect **negligible**, but below description in terms of **dilaton breaks down**. Effectively as if **negative mass** of order χ_*^2
- Can get this by putting **another gauge group** in the bulk (for example QCD itself)

$$\frac{1}{g^2(Q, \chi)} = \frac{\log \frac{k}{\chi}}{kg_5^2} - \frac{b_{UV}}{8\pi^2} \log \frac{k}{Q} - \frac{b_{IR}}{8\pi^2} \log \frac{\chi}{Q} + \tau$$

The small χ region

- The **dynamical scale** of the bulk gauge group:

$$\tilde{\Lambda}(\chi) = \left(k^{b_{\text{UV}}} \chi^{b_{\text{IR}}} e^{-8\pi^2 \tau} \left(\frac{\chi}{k} \right)^{-b_{\text{CFT}}} \right)^{\frac{1}{b_{\text{UV}} + b_{\text{IR}}}} = \Lambda_0 \left(\frac{\chi}{\chi_{\text{min}}} \right)^n$$

- For **QCD** and benchmark point $\chi_{\text{min}} \simeq 1 \text{ TeV}$ and $\langle H \rangle = 0$ we get $\tilde{\Lambda}(\chi_{\text{min}}) \sim \Lambda_{\text{QCD}} \sim 100 \text{ MeV}$ and $\chi_* \sim$

$$10 - 100 \text{ MeV} \sim \Lambda_{\text{QCD}}$$

- This will **ensure no eternal** inflation as long as

$$\Lambda < \sqrt{\chi_* M_{\text{Pl}}} \lesssim 10^5 \text{ TeV}$$

- With other bulk gauge groups can push **Λ to 10^7 TeV**

- This will also give $h_{\text{min}} \sim 0.1 \chi_*$