

# From Quarks to Drugs

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Pietro Faccioli

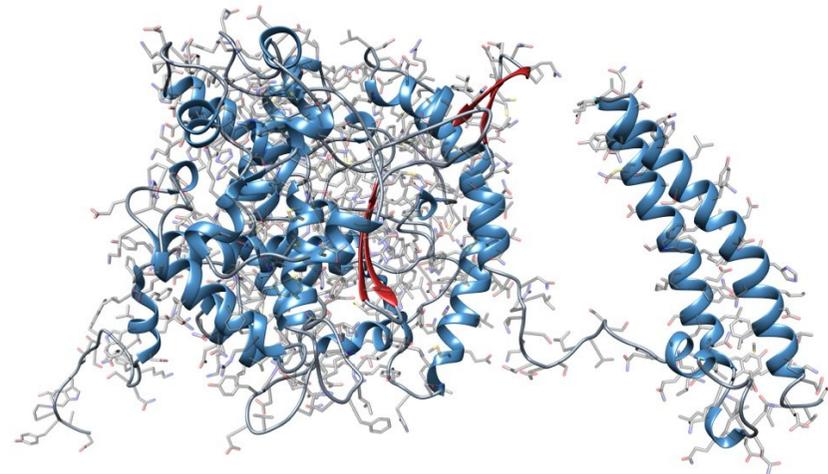


UNIVERSITÀ DEGLI STUDI  
DI TRENTO

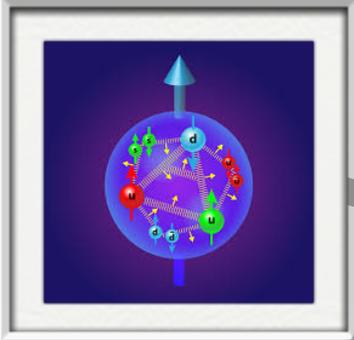
Dipartimento di Fisica



Trento Institute for  
Fundamental Physics  
and Applications



# A SCIENTIFIC JOURNEY

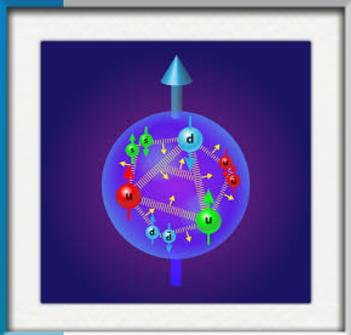


Fundamental

Applied



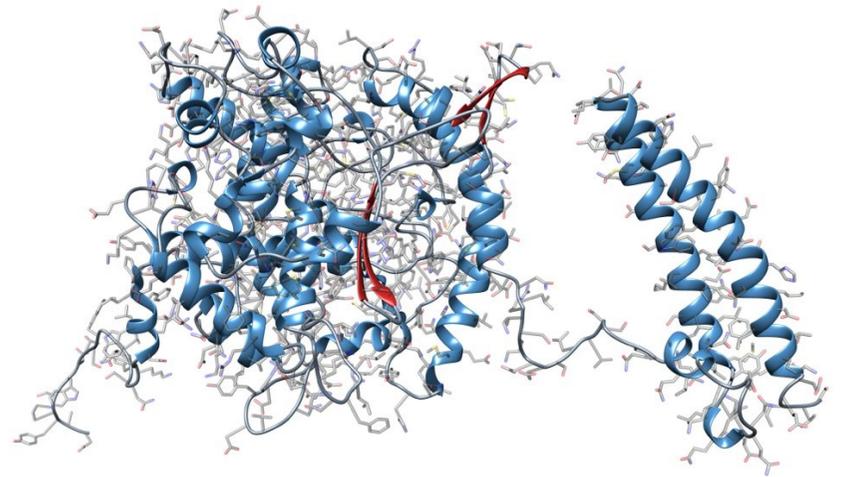
Physics



Biology

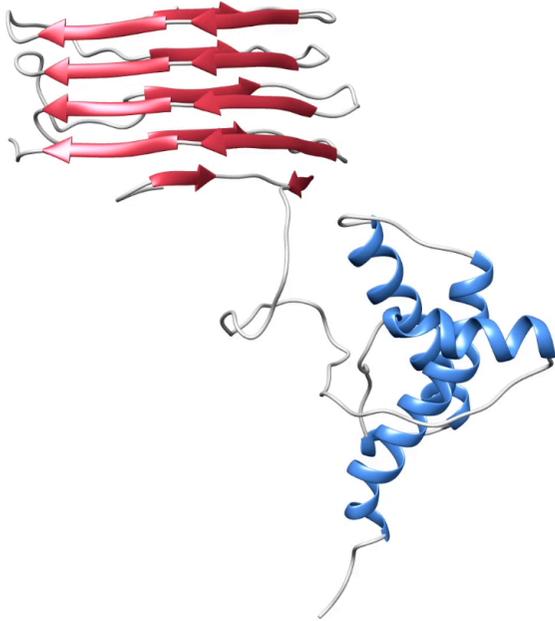


Prologue: proteins are complex many-body systems.



# REDUCTIONIST'S APPROACH TO MOLECULAR BIOLOGY

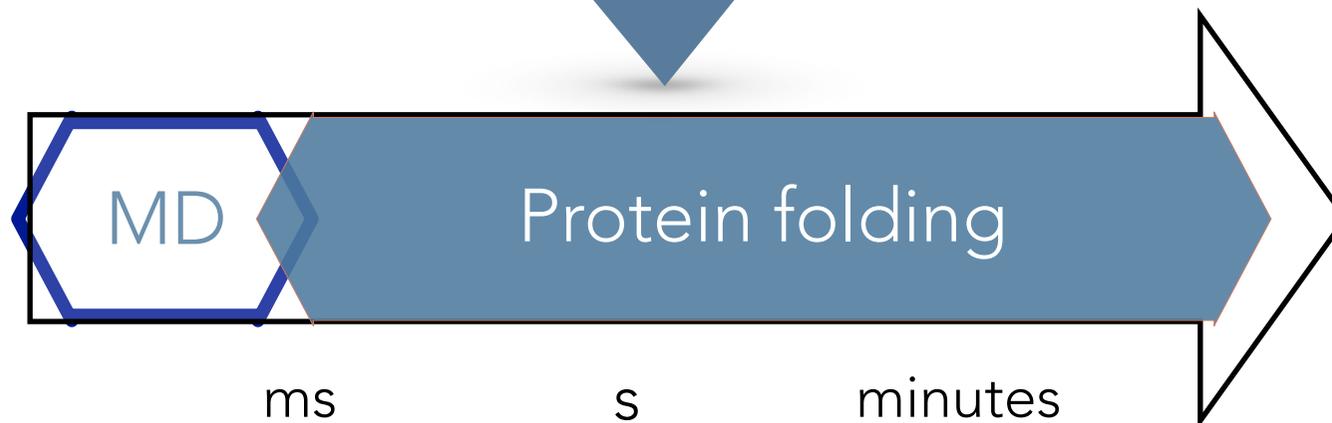
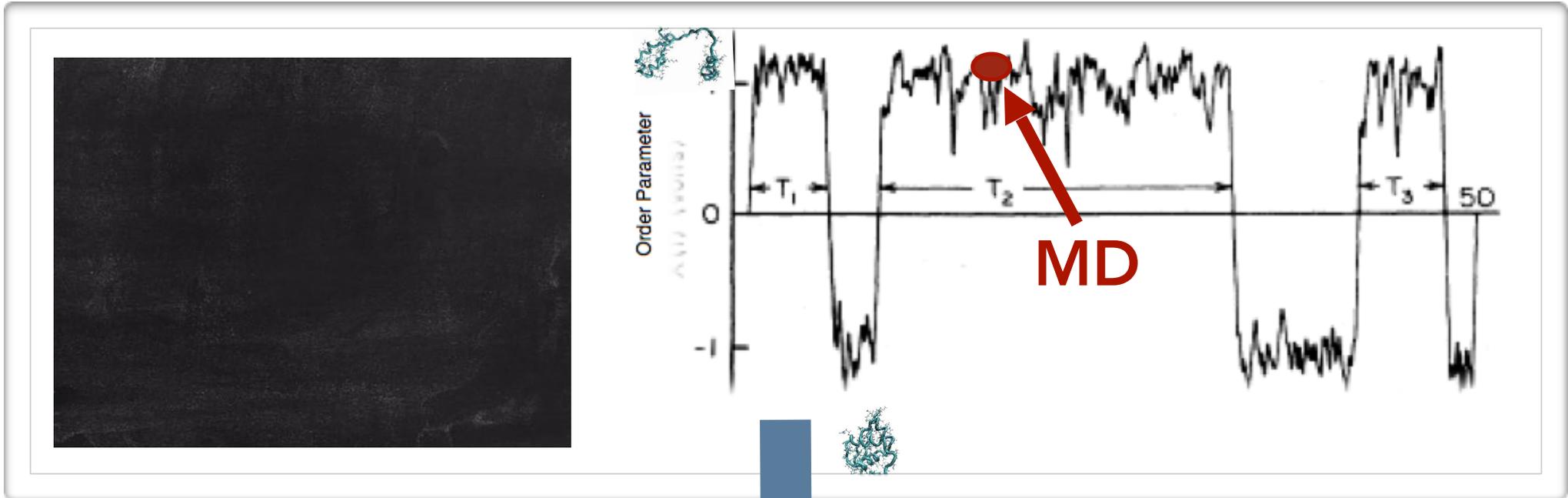
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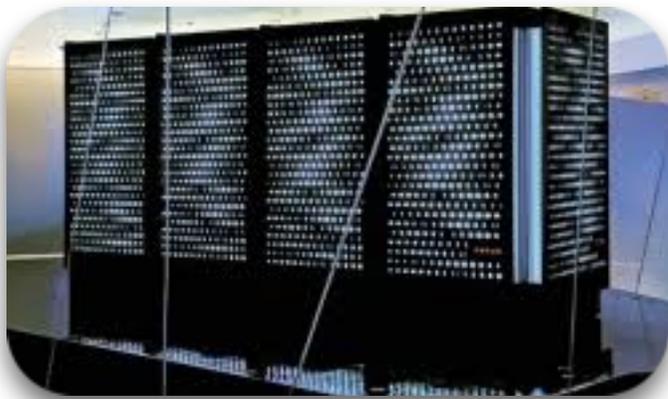
## Challenge:

Integrate  $\sim 10^6$  coupled  
Newton-type equations  
looking for **extremely  
rare events**

# RARE EVENT PROBLEMS



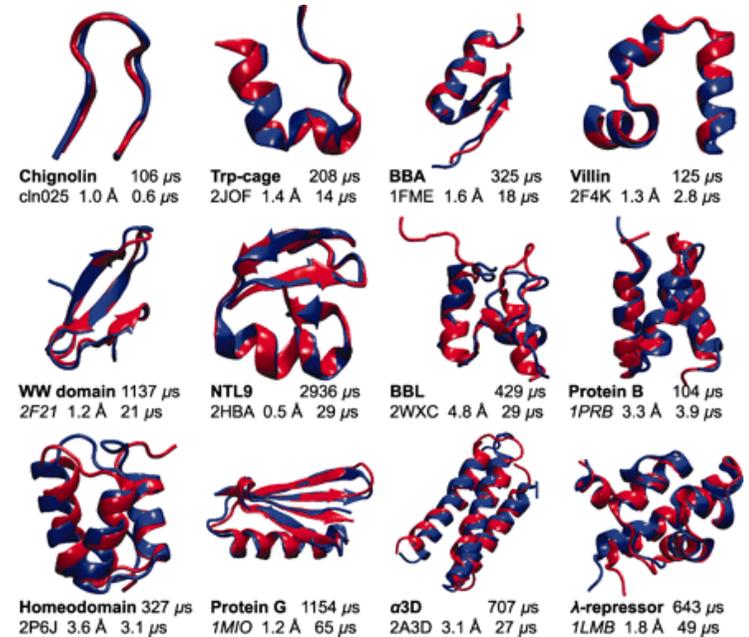
# MD YIELDS CORRECT PROTEIN NATIVE STATES



Anton supercomputer  
(DES Research)



MD



**Atomic-Level Characterization of the Structural Dynamics of Proteins**  
David E. Shaw, *et al.*  
*Science* **330**, 341 (2010);  
DOI: 10.1126/science.1187409

## How Fast-Folding Proteins Fold

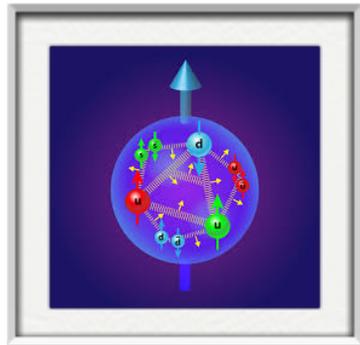
Kresten Lindorff-Larsen,<sup>1\*</sup>† Stefano Piana,<sup>1\*</sup>† Ron O. Dror,<sup>1</sup> David E. Shaw<sup>1,2†</sup>

# ZOOLOGY OF ENHANCED SAMPLING METHODS

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Markov State Models (Folding@Home), Milestoning, Transition Path Sampling, Transition Interface Sampling, Forward Flux Sampling, Temperature Accelerated Molecular Dynamics, Metadynamics, Umbrella Sampling, Blue Moon Sampling, String Method, Stochastic Difference, ... [and counting]

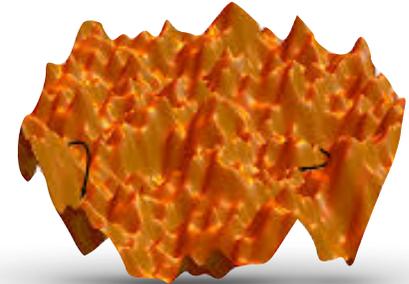
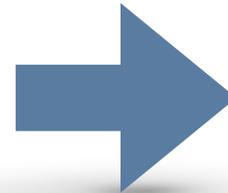
They are **all too computationally demanding** for many biologically relevant problems.



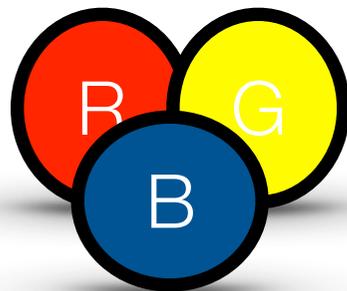
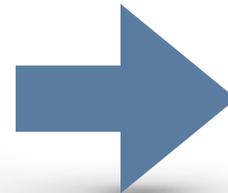
# PROTEINS AND HADRONS ARE VERY SPECIAL



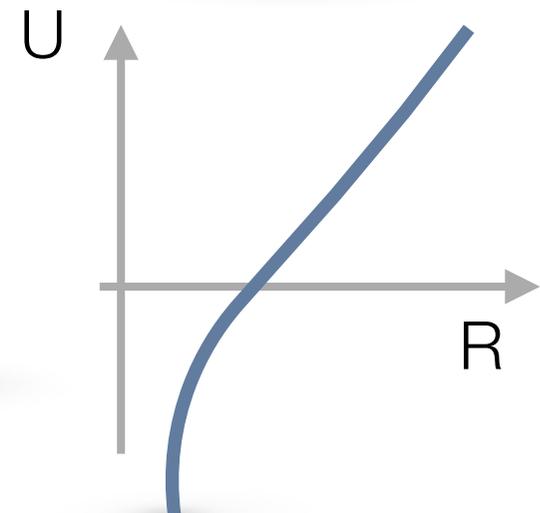
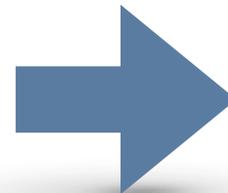
Random polypeptide



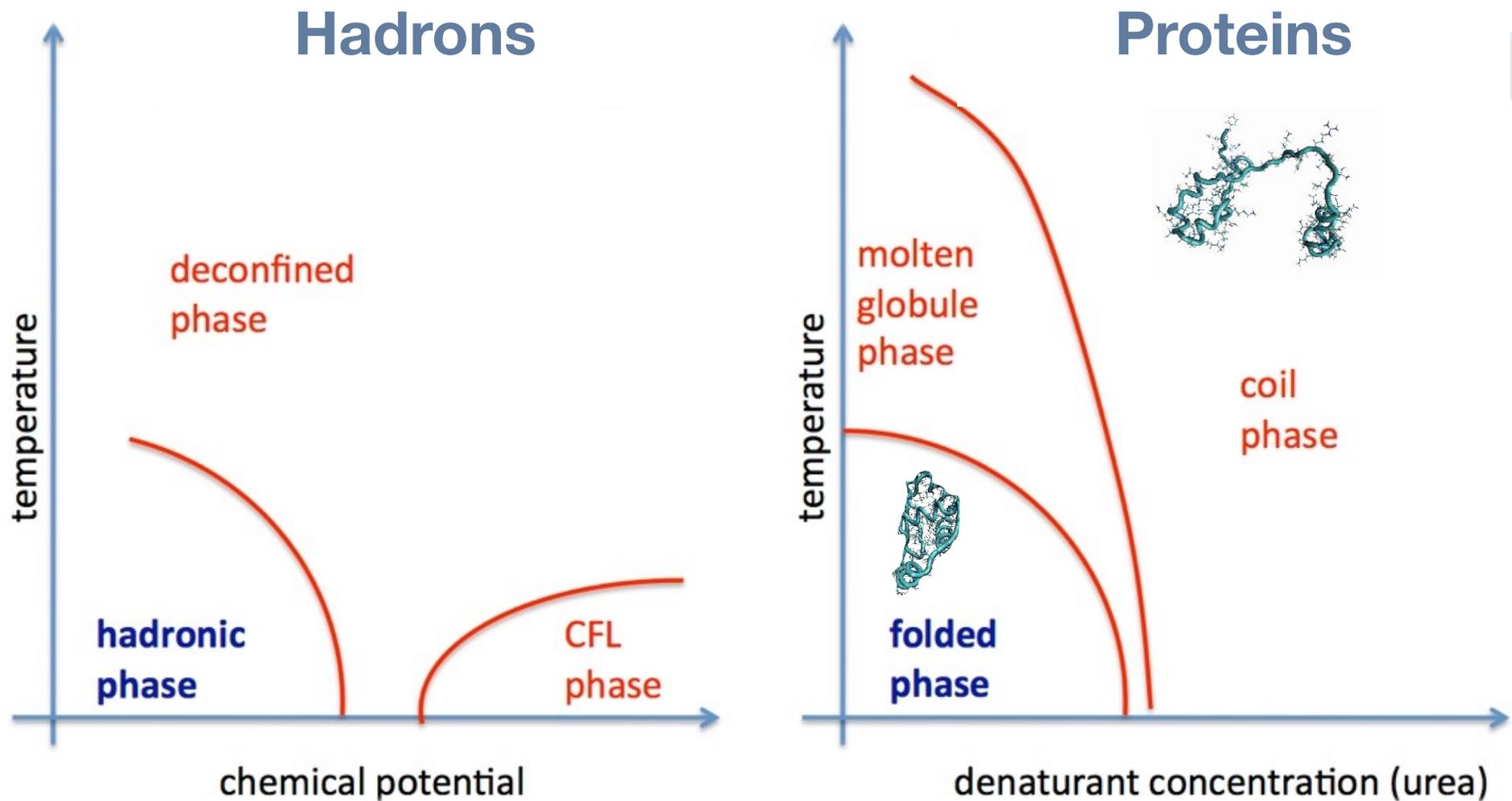
Protein



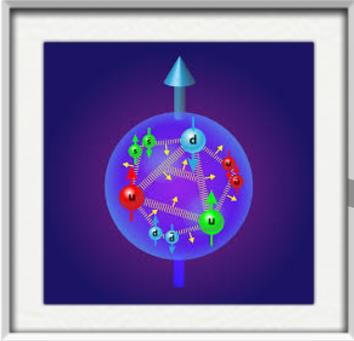
Baryon



# PHASE DIAGRAM



# PHASE 1: MATHEMATICAL FORMALISM & HIGH PERFORMANCE COMPUTING



$$\mathcal{L} = \frac{1}{4g^2} G_{\mu\nu}^a G_{\mu\nu}^a + \sum_f \bar{\psi}_f (i \not{\partial} + m_f) \psi_f$$

where  $G_{\mu\nu}^a \equiv \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + gf_{abc} A_\mu^b A_\nu^c$   
and  $D_\mu \equiv \partial_\mu + i t^a A_\mu^a$   
*That's it!*



# PATH INTEGRAL REPRESENTATION

Hamilton's equations



Langevin equations

$$M\ddot{\mathbf{r}}_i = -\nabla_i U(\mathbf{R}) - \gamma_i \dot{\mathbf{r}}_i + \eta_i(t)$$

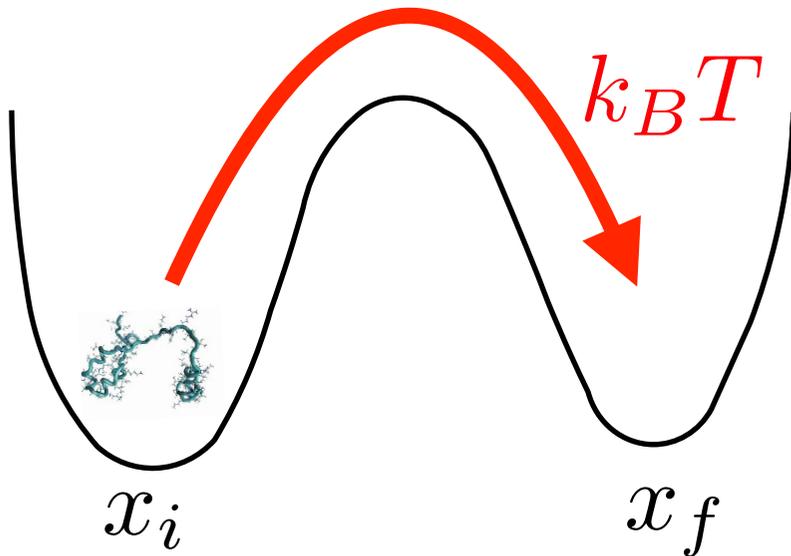


$$P(R_f, t | R_i, 0) = \int_{R_i}^{R_f} \mathcal{D}R e^{-\frac{\beta}{4m\gamma} \int_0^t d\tau (m\ddot{R} + m\gamma\dot{R} + \nabla U)^2}$$

# A USEFUL ANALOGY

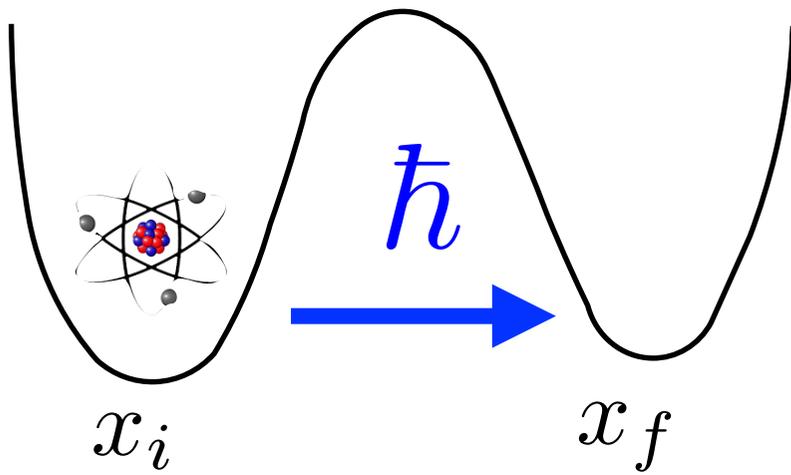
Thermal activation

$$(\beta = (K_B T)^{-1})$$



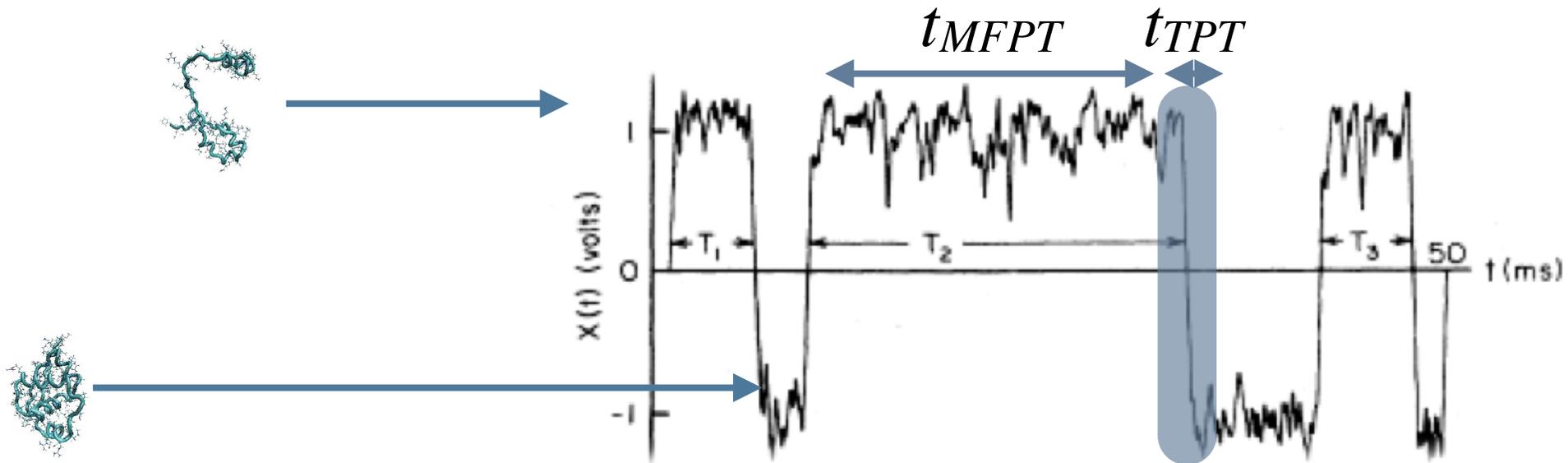
$$P(x_f, t | x_i) = \int_{x_i}^{x_f} \mathcal{D}q e^{-\frac{\beta}{4M\gamma} \int_0^t d\tau (M\ddot{q} + M\gamma\dot{q} + \nabla U(q))^2}$$

Quantum tunneling



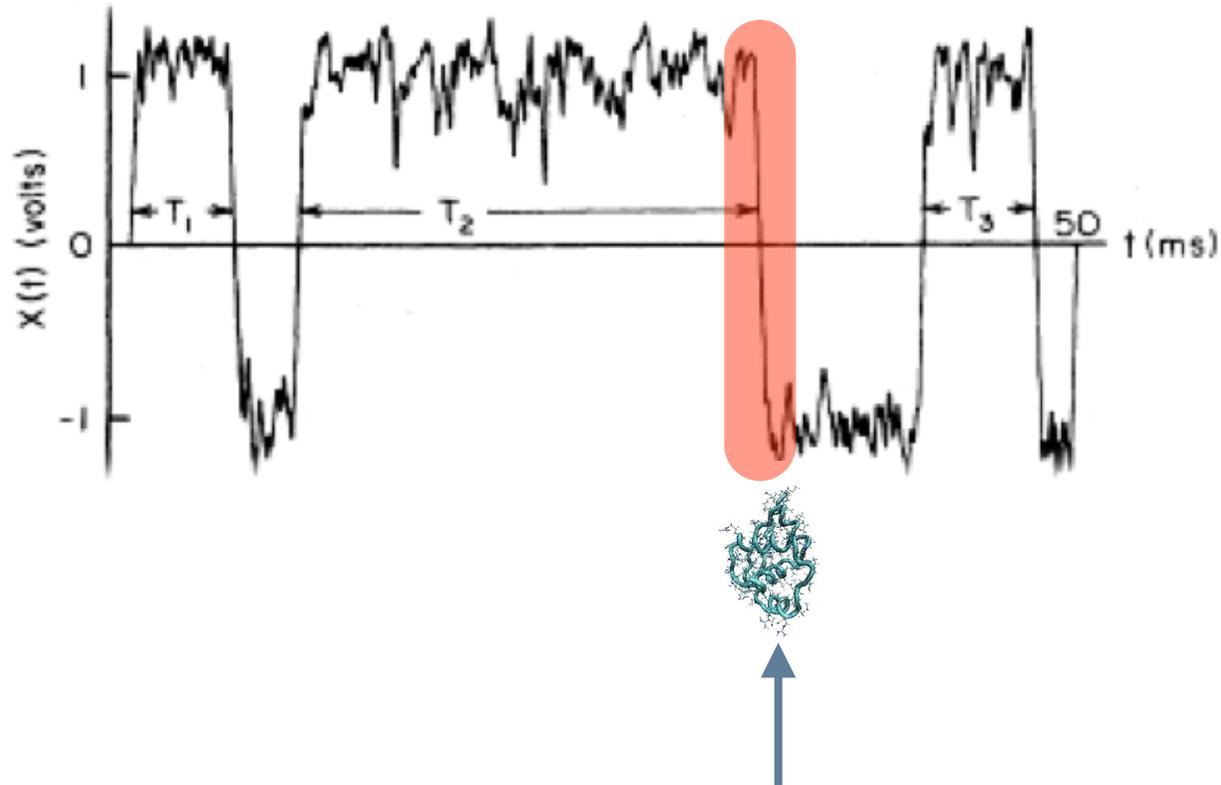
$$K_E(x_f, t | x_i) = \int_{x_i}^{x_f} \mathcal{D}q e^{-\frac{1}{\hbar} \int_0^t d\tau (\frac{M}{2} \dot{q}^2 + U(q))}$$

# ADVANTAGES



$$t_{TPT} \sim \tau_0 \log \left[ \log \left( \frac{t_{MFPT}}{\tau_0} \right) \right]$$

# IS THIS A "FREE LUNCH"?



All atom 3D structure of the native state **are given in input**, not predicted

# VARIATIONAL APPROACHES TO TRANSITION PATH SAMPLING

## Dominant Reaction Pathways

PRL 97, 108101 (2006)

PHYSICAL REVIEW LETTERS

week ending  
8 SEPTEMBER 2006

**Dominant Pathways in Protein Folding**

(2005)

PRL 99, 118102 (2007)

PHYSICAL REVIEW LETTERS

week ending  
14 SEPTEMBER 2007

**Quantitative Protein Dynamics from Dominant Folding Pathways**

(2006)

### Dominant folding pathways of a WW domain

Silvio a Beccara<sup>ab</sup>, Tatjana Škrbić<sup>ac</sup>, Roberto Covino<sup>ab</sup>, and Pietro Faccioli<sup>ab,1</sup>

<sup>a</sup>Dipartimento di Fisica, Università degli Studi di Trento, Via Sommarive 14, I-38123 Povo (Trento), Italy; <sup>b</sup>INFN Istituto Nazionale di Fisica Nucleare (National Institute for Nuclear Physics), Gruppo Collegato di Trento, Via Sommarive 14, I-38123 Povo (Trento) Italy; and <sup>c</sup>European Centre for Theoretical Studies in Nuclear Physics and Related Areas, Strada delle Tabarelle 286, I-38123 Villazzano (Trento), Italy

Edited by William A. Eaton, National Institutes of Health -NIDDK, Bethesda, MD, and approved December 19, 2011 (received for review July 27, 2011)

(2012)

## Bias Functional Approach

PRL 114, 098103 (2015)

PHYSICAL REVIEW LETTERS

week ending  
6 MARCH 2015

**Variational Scheme to Compute Protein Reaction Pathways Using Atomistic Force Fields with Explicit Solvent**

(2015)

## Self Consistent Path Sampling

THE JOURNAL OF CHEMICAL PHYSICS 147, 064108 (2017)

**Self-consistent calculation of protein folding pathways**

S. Orioli, S. a Beccara, and P. Faccioli<sup>(a)</sup>

(2017)

# FULLY EXPLOITING THEORETICAL PHYSICS TOOLS

072336-4 Bartolucci, Orioli, and Faccioli

between the Gibbs distribution and the SCR estimate forward- and backward-committors, as in Eq. (A3). Introducing the distribution

$$P^{(P)}(x, t) \equiv \int dx_i P^{(P)}(x, t | x_i, 0) \rho_0(x_i), \quad (22)$$

the density in Eq. (22) reads

$$m_{SCR}(x) = \frac{1}{t_f - \tau_0} \int_{\tau_0}^{t_f} dt Q^{(R)}(x, t_f - t) P^{(P)}(x, t).$$

Using the detailed balance condition, we find  $P^{(P)} = e^{-\beta U(x)} \frac{1}{Z_R} Q^{(P)}(x, t)$ . Then, inserting this result into Eq. we find

$$m_{SCR}(x) = \frac{e^{-\beta U(x)}}{Z_R (t_f - \tau_0)} \int_{\tau_0}^{t_f} dt Q^{(R)}(x, t_f - t) Q^{(P)}(x, t).$$

Finally, recalling that  $Q^{(R)}(x, t)$  and  $Q^{(P)}(x, t)$  are time-independent in the SCR and using Eqs. (17) and we recover a fundamental result of TPT [cf. Eq. (A. Appendix A)],

$$m_{SCR}(x) \propto e^{-\beta U(x)} q_{SCR}^+(x) (1 - q_{SCR}^+(x)).$$

Within the same framework, it is possible to do the reactive current in the SCR in complete analogy Eq. (22),

$$J_{SCR}^i(x) = \frac{-D}{t_f - \tau_0} \int_{\tau_0}^{t_f} dt Q^{(R)}(x, t_f - t) \times (\vec{\nabla} - \overleftarrow{\nabla} + \beta \nabla U(x)) P^{(P)}(x, t).$$

$$\begin{aligned} V_{eff}^R(\mathbf{X}) &\simeq \frac{D_0(1-b)}{\pi b \Omega} \nabla^2 V_{eff}(\mathbf{X}) \\ &+ \frac{1}{2} \left( \frac{D_0(1-b)}{\pi b \Omega} \right)^2 \nabla^4 V_{eff}(\mathbf{X}) \\ &+ \frac{1}{6} \left( \frac{D_0(1-b)}{\pi b \Omega} \right)^3 \nabla^6 V_{eff}(\mathbf{X}) - \frac{D_0^2(1-b^3)}{3\pi(b\Omega)^3} (\partial_i \partial_j V_{eff}(\mathbf{X}))^2. \end{aligned} \quad (24)$$

Note that the first line is the leading order term (i.e.  $L = 1$ ), while the second and third lines display the order  $L = 2$  and  $L = 3$  corrections, respectively.

We emphasize that the result of the EST construction is a new expression for the *same* path integral (15), in which the UV cutoff has been lowered from  $\Omega$  to  $b\Omega$ . Equivalently, the path integral is discretized according to a larger elementary time step,  $\Delta t \rightarrow \Delta t/b$ :

$$Z^{\Delta t}(t) \equiv \oint_{\Delta t} \mathcal{D}\mathbf{X} e^{-S_{eff}[\mathbf{X}]} \propto \oint_{\Delta t/b} \mathcal{D}\mathbf{X} e^{-S_{eff}[\mathbf{X}] - \int_0^t d\tau V_{eff}^R[\mathbf{X}(\tau)]} \equiv Z_{EST}^{\Delta t/b}(t) \quad (25)$$

In these expressions, the symbol  $\oint_{\Delta t}$  denotes the fact that the path integral is discretized according to an elementary time step  $\Delta t$  and we have suppressed the subscript " $<$ ", in the paths. It can be shown that the proportionality factor between  $Z^{\Delta t}(t)$  and  $Z_{EST}^{\Delta t/b}(t)$

PRL 114, 098103 (2015) PHYSICAL REVIEW LETTERS

$$\mathcal{P}_{\text{bias}}[X] = \int \mathcal{D}Y e^{-S_{\text{OM}}[X, Y] - U(X, Y)/k_B T}, \quad (3)$$

where the functional  $S_{\text{bias}}[X, Y]$  is defined as

$$\begin{aligned} S_{\text{bias}} &\equiv \frac{1}{4k_B T} \int_0^t d\tau \left[ \sum_{i=1}^N \frac{1}{\gamma_i m_i} (m_i \dot{x}_i + m_i \gamma_i \dot{y}_i + \nabla_i U - \mathbf{F}_i^{\text{bias}})^2 \right. \\ &\quad \left. + \sum_{j=1}^N \frac{1}{\gamma_j m_j} (m_j \dot{y}_j + m_j \gamma_j \dot{x}_j + \nabla_j U)^2 \right]. \end{aligned} \quad (4)$$

The Onsager-Machlup functional  $S_{\text{OM}}[X, Y]$  entering Eq. (2) is recovered, setting  $\mathbf{F}_i^{\text{bias}} = 0$  in Eq. (4).

Let us now return to the problem of computing the reaction pathways in the unbiased Langevin dynamics [Eq. (1)]. Using the standard reweighting trick we can write the variational condition  $(\delta/\delta X)\mathcal{P}[X] = 0$  as

$$\frac{\delta}{\delta X} [\mathcal{P}_{\text{bias}}[X] (e^{-S_{\text{OM}}[X, Y]} - S_{\text{bias}}[X, Y])_{\text{bias}}] = 0. \quad (5)$$

We now introduce our main approximation, by restricting the search for the optimum path  $X(\tau)$  within an ensemble of trajectories generated by integrating the biased Langevin equation. By definition, these paths have a large statistical weight in the biased dynamics, i.e., they lie in the functional vicinity of some path  $\tilde{X}(\tau)$  which satisfies  $(\delta/\delta X)\mathcal{P}[\tilde{X}] = 0$ . Thus, the typical biased paths approximately satisfy the stationary condition

This equation states that for which the force is least. In derived in the context of solvent-induced... Let us now emphasize that the history-dependent ratchet-and-... formalism attempts to terms of slow... z. Conversion... To define... (1) with a...  $-\frac{k_B}{2} \nabla$   
0  
 $z_m(t)$  dec... time  $t$  (we... obeys the... Let us

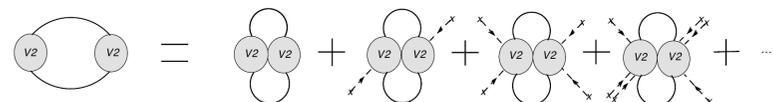


FIG. 3: Diagrammatic representation of the local time-derivative expansion of a non-local diagram —Eq. (49)—. Solid lines are fast-mode propagators, while dashed lines represent a single time derivative acting on the corresponding vertex function.

Notice that each term in the perturbative expansion (35) generates a new vertex, with an increasing power of the  $x_{>}(\tau)$  field. The couplings to the fast modes depend implicitly on the time  $\tau$ , through the slow modes  $x_{<}(\tau)$ .

By Wick theorem, each term in the series (34) can be related to a Feynman graph with vertices given by (36) and propagators given by —see appendix A —:

$$\langle x_{>}^i(\tau_1) x_{>}^j(\tau_2) \rangle_0 = \sum_{\{|\omega_n|, |\omega_m| \in S_b\}} G_{>}^{ij}(\omega_n, \omega_m) e^{i(\omega_n \tau_1 + \omega_m \tau_2)} = \sum_{\{|\omega_n| \in S_b\}} \delta_{ij} \frac{2}{\beta \gamma t \omega_n^2} e^{i\omega_n(\tau_2 - \tau_1)}. \quad (37)$$

The expansion (34) can be re-organized as the exponent of the sum performed over only connected diagrams:

$$e^{-\beta S_{>}[x_{<}(\tau)]} = e^{\Sigma(\text{all connected diagrams})}. \quad (38)$$

Hence, the path integral (26) for the slow modes can be given the following exact diagrammatic representation

$$Z(t) \equiv \oint \mathcal{D}x_{<} e^{-\beta S_{eff}[x_{<}(t)] + \Sigma(\text{all connected diagrams})}. \quad (39)$$

Below we give a classification of all the connected diagrams that may give a contribution to the expansion above.

064108-3 Orioli, a Beccara, and Faccioli

J. Chem. Phys. 147, 064108 (2017)

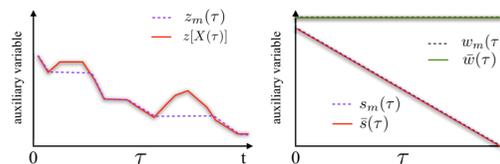


FIG. 1: Illustrative representation of the dynamics of the auxiliary variables introduced in the path integral representation of rMD (left panel) and in the derivation self-consistent path sampling algorithm (right panel).

of such a variable is frozen any time  $z_m$  becomes smaller than  $z(X)$  and any time the collective coordinate  $z(X)$  is increasing. Its time derivative is otherwise set equal to  $\dot{z}(X)$ . Therefore, by choosing the initial conditions  $z_m(0) = z(X(0))$ ,  $z_m(\tau)$  is identically set equal to the minimum value attained by the collective coordinate  $z$  until time  $\tau$  (see left panel of Fig. 1).

The functional  $S_{MD}[X, z_m]$  in the exponent of Eq. (8) coincides with an OM action with the addition of the unphysical biasing force  $\mathbf{F}_i$ ,

$$S_{MD} = \sum_{i=1}^N \Gamma_i \int_0^t d\tau [m_i \dot{x}_i + m_i \gamma_i \dot{y}_i + \nabla_i U - \mathbf{F}_i]^2. \quad (9)$$

In Eq. (8),  $\Phi[z_m, X]$  denotes a Jacobian factor that needs to be introduced in order to ensure that the statistical weight of the paths is not affected by the measure of the  $\int \mathcal{D}z_m$  integral, i.e.,

$$\int \mathcal{D}z_m \Phi[z_m, X] \delta \left[ z_m(\tau) - \int_0^\tau d\tau' \dot{z}(X(\tau')) \theta(-\dot{z}(X(\tau'))) \right]$$

### III. SELF-CONSISTENT PATH SAMPLING

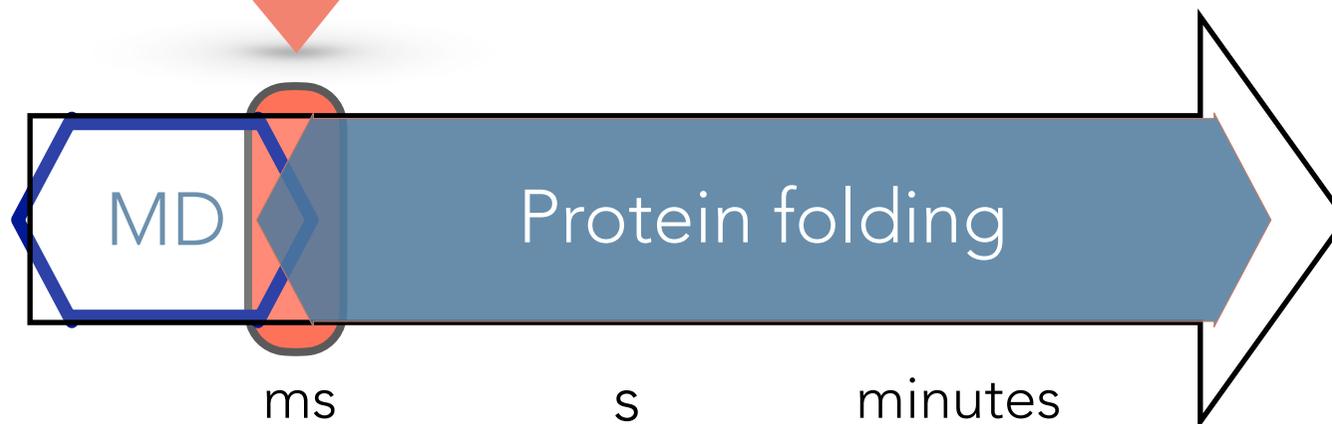
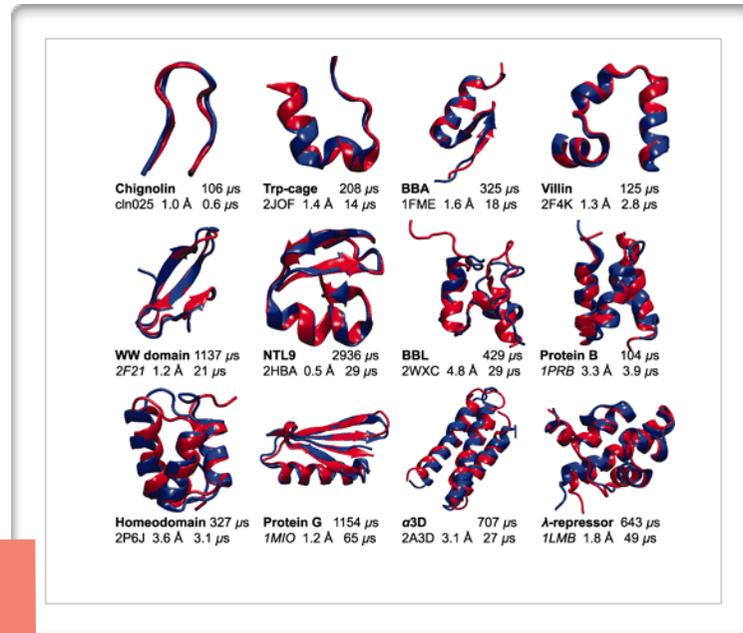
Let us now introduce our new algorithm, which provides major improvement with respect to the rMD and BF schemes discussed in Sec. II A. Indeed, it follows directly from the unbiased Langevin equation and allows us to remove the systematic errors associated to the choice of biasing coordinate.

Our starting point is path integral representation of the unbiased Langevin dynamics (2). We introduce two dumb auxiliary variables  $w_m(\tau)$  and  $s_m(\tau)$  into this path integral by means of appropriate functional Dirac deltas,

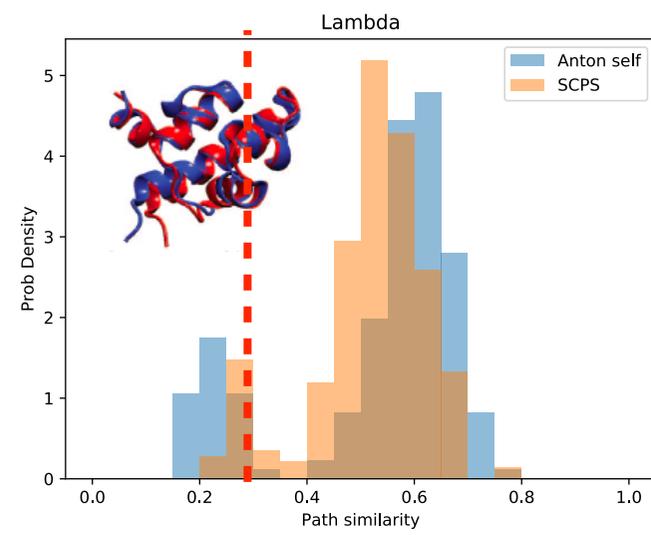
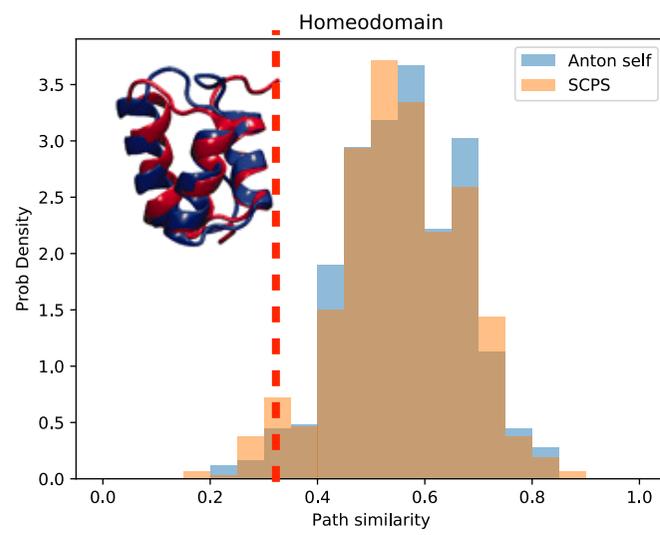
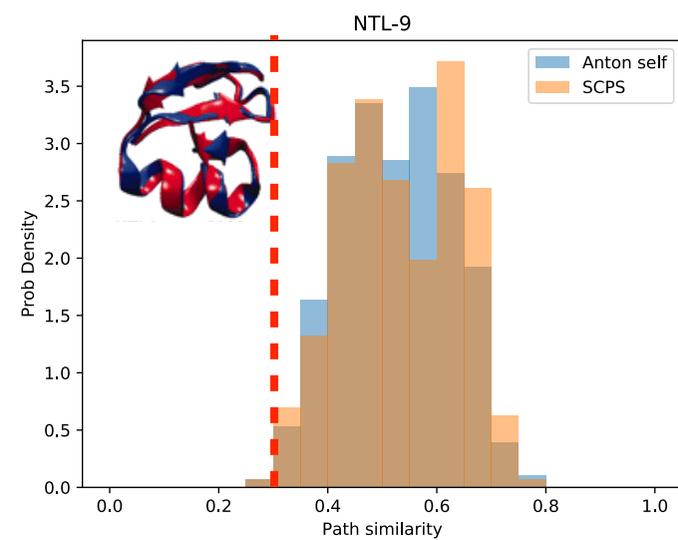
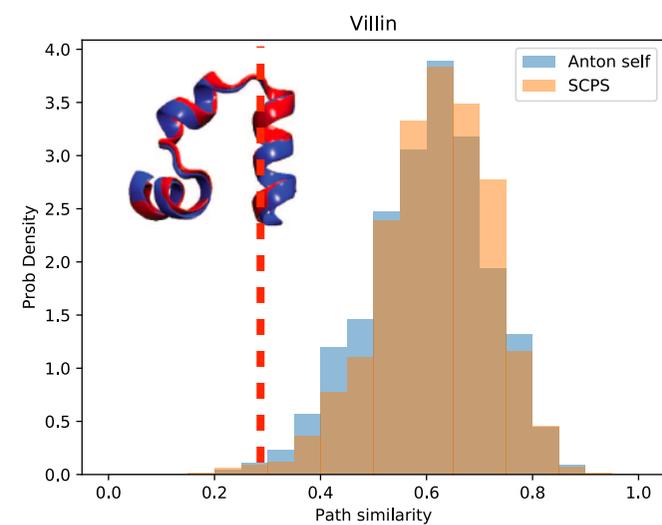
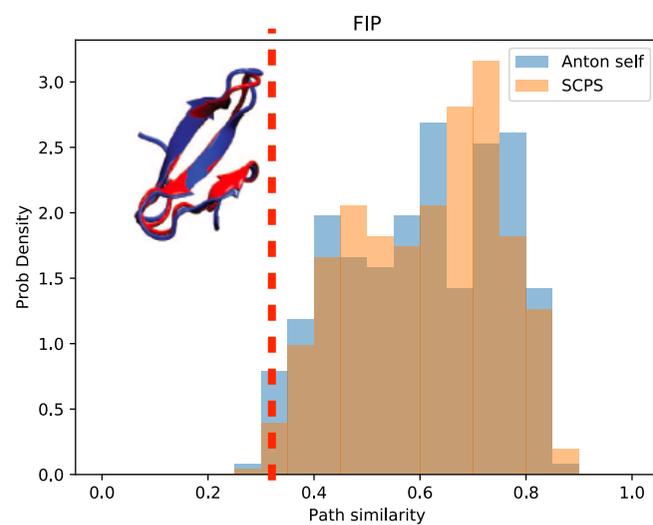
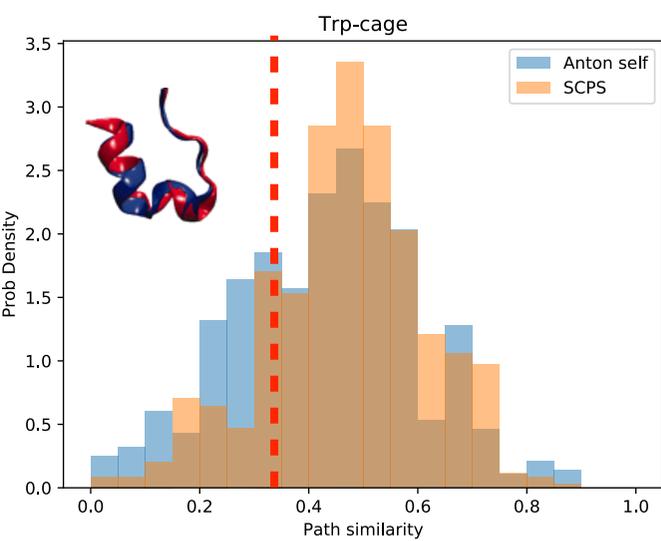
$$\begin{aligned} p(X_N, t | X_0) &= \int_{X_0}^{X_N} \mathcal{D}X \cdot e^{-S[X]} \int_{S(0)} \mathcal{D}s_m \int_{\hat{w}(0)} \mathcal{D}w_m \\ &\cdot \delta \left[ w_m(\tau) - \int_0^\tau d\tau' \dot{w}(\tau') \theta(-\dot{w}(\tau')) \theta(w_m(\tau') - \hat{w}(\tau')) \right] \\ &\cdot \delta \left[ s_m(\tau) - \int_0^\tau d\tau' \dot{s}(\tau') \theta(-\dot{s}(\tau')) \theta(s_m(\tau') - \bar{s}(\tau')) \right], \end{aligned} \quad (12)$$

where  $\bar{s}(\tau)$  and  $\hat{w}(\tau)$  are two external time-dependent functions to be defined below. In analogy with the path integral repre-

# VALIDATING SCPS AGAINST MD

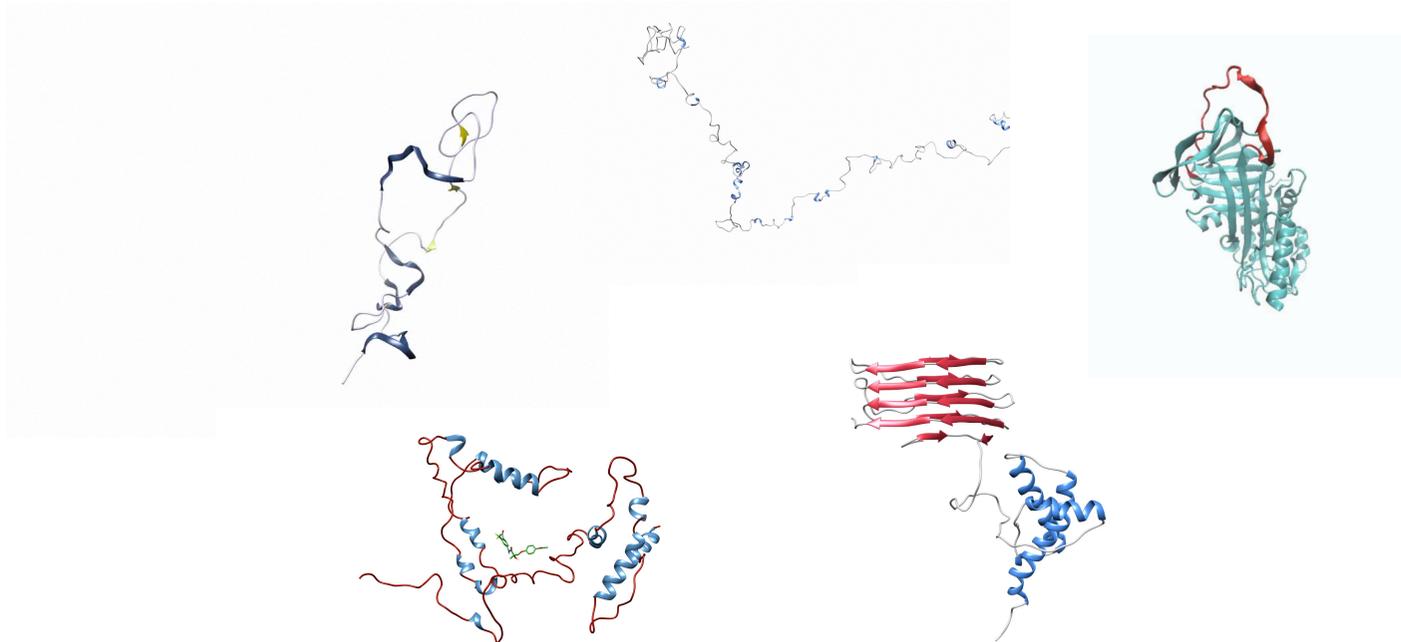
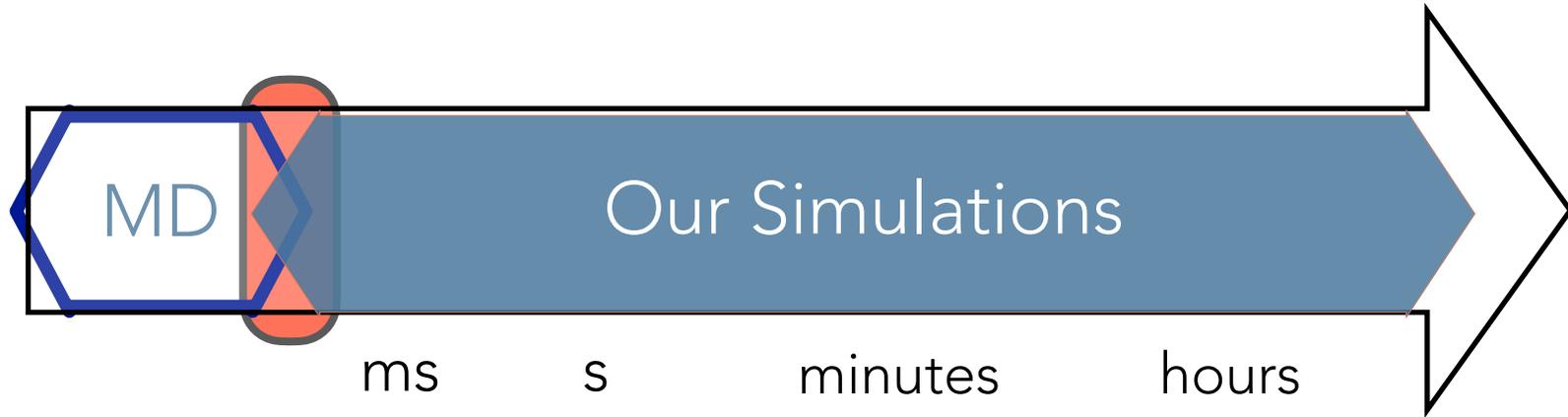


# VALIDATING SCPS AGAINST MD

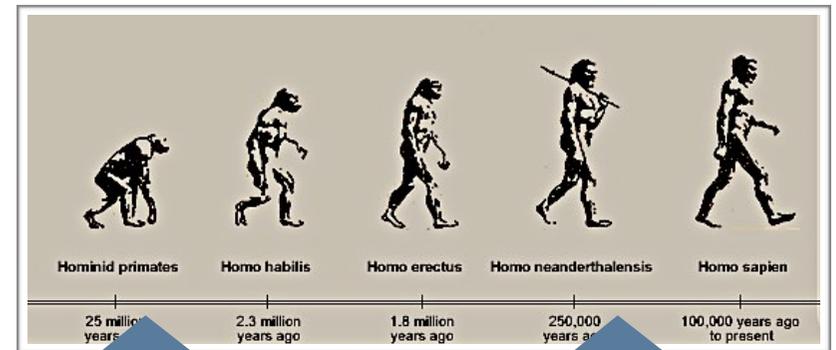
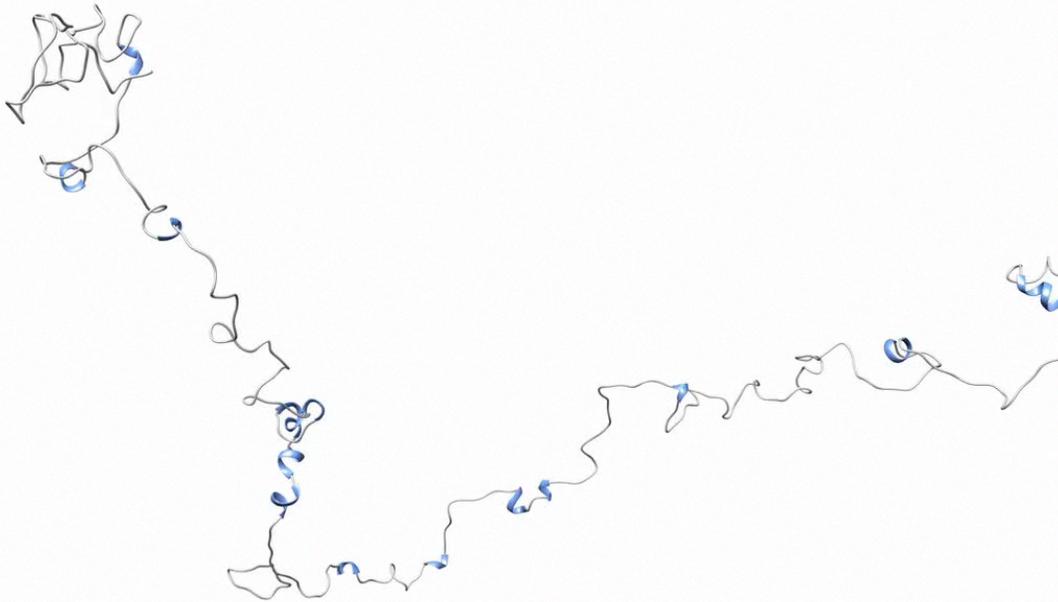


# VENTURING INTO THE BIO-ZONE

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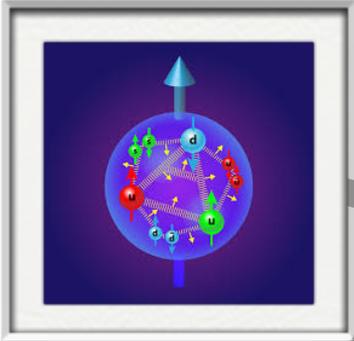
# HUGE COMPUTATIONAL GAIN



Using top all-purpose supercomputers

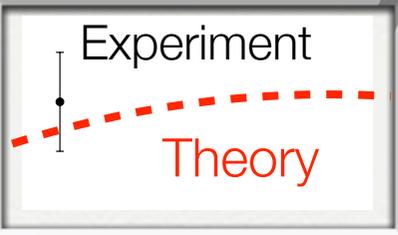
Using top special-purpose supercomputer

# PHASE 2: VALIDATION



$$\mathcal{L} = \frac{1}{4g^2} G_{\mu\nu}^a G_{\mu\nu}^a + \sum_f \bar{\psi}_f (i \not{\partial} \not{D}_\mu + m_f) \psi_f$$

where  $G_{\mu\nu}^a \equiv \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + gf_{abc} A_\mu^b A_\nu^c$   
and  $D_\mu \equiv \partial_\mu + i t^a A_\mu^a$   
*That's it!*



# VALIDATION AGAINST EXPERIMENT

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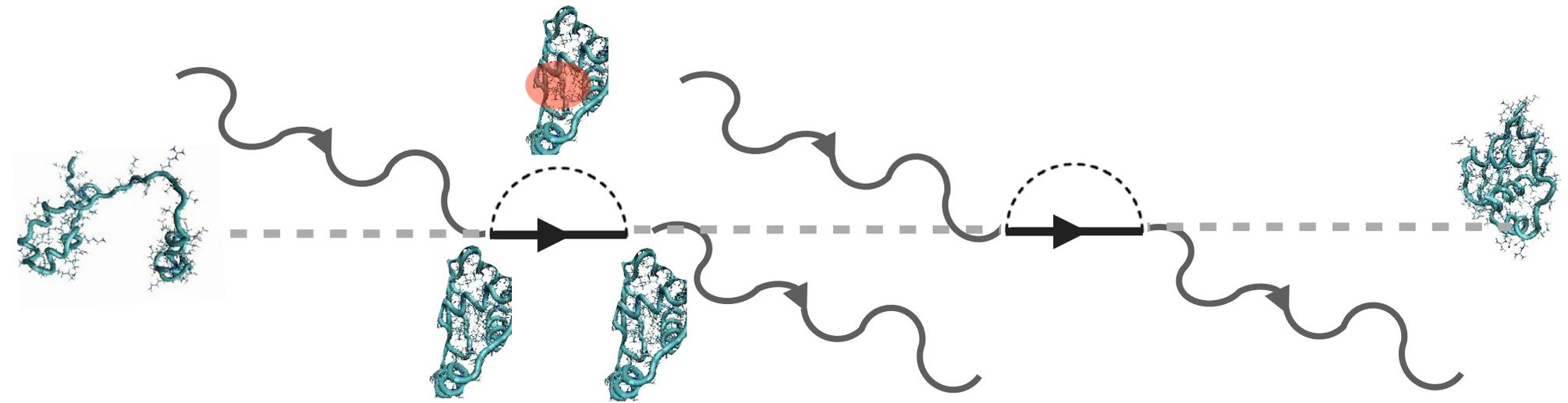
Experiment



**Challenge:**

Most available techniques provide only indirect probes, we seek for **direct validation**

# TIME-DEPENDENT LINEAR SPECTROSCOPY



--- Ground state  
→ One exciton

## Challenge:

Need a theory for  
**non-equilibrium dynamics**  
of **quantum** electronic  
excitations in conformationally  
evolving proteins

---

$$\hat{\rho}(t) = e^{\frac{i}{\hbar} \hat{H} t} \hat{\rho}(0) e^{-\frac{i}{\hbar} \hat{H} t}$$

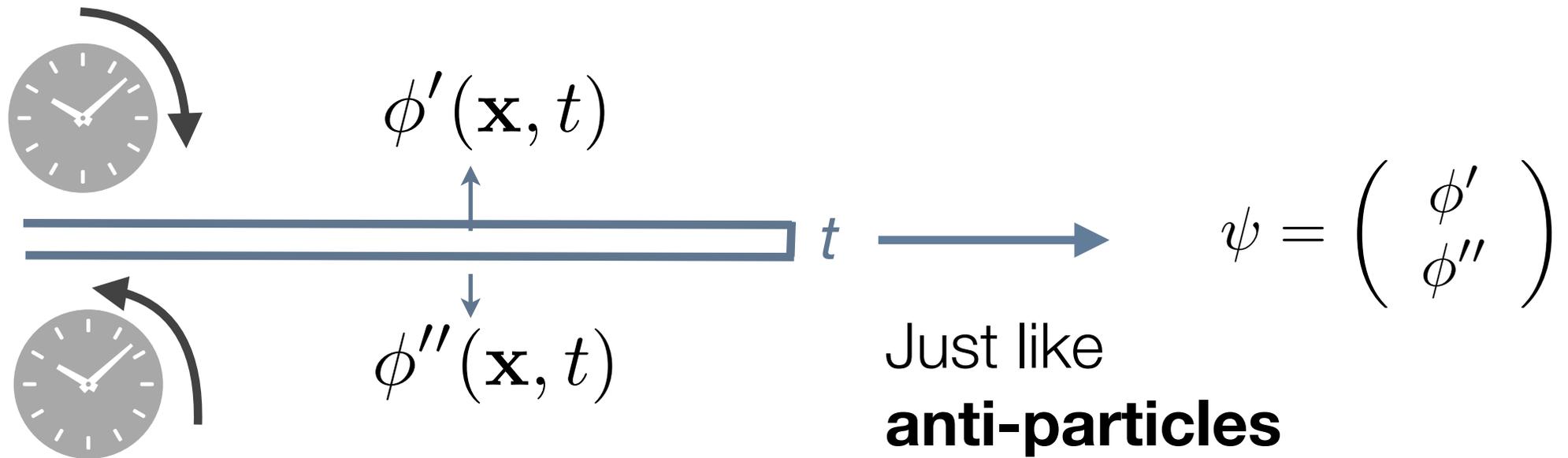


multiple time  
directions...

# USE QUANTUM FIELD THEORY!

---

Using QFT we get rid of the multiple time issue:



One “relativistic” field doublet but just one time

# MOLECULAR QUANTUM FIELD THEORY\*

---

$$Z = \int \mathcal{D}\psi \mathcal{D}\bar{\psi} \int \mathcal{D}q e^{-S_{MQFT}[\psi, \bar{\psi}, q]}$$

$$S_{MQFT}[q, \psi, \bar{\psi}] = S_{OM}[q] + S_S[\psi, \bar{\psi}] + S_{int}[q, \psi, \bar{\psi}]$$

$$S_{OM}[q] = \int_0^t d\tau \frac{\beta}{4M\gamma} (M\ddot{q} + M\gamma\dot{q} + \nabla U(q))^2$$

$$S_S[\psi, \bar{\psi}] = \sum_{n,m} \int_0^t d\tau \bar{\psi}_n(\tau) (i\hbar\partial_t - h_{nm}^0) \psi_m(\tau)$$

$$S_{int}[q, \psi, \bar{\psi}] = \sum_{nm} \sum_i \int_0^t d\tau f_{nm}^i \bar{\psi}_n \psi_m \delta q_i$$

# SOLVING MQFT: AN ARSENAL OF METHODS

---

Perturbation Theory



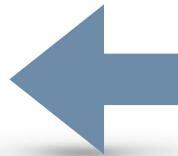
PRB 2012, PRB 2013, PRB 2016

Quantum MC  
(for real time)



PRB 2016

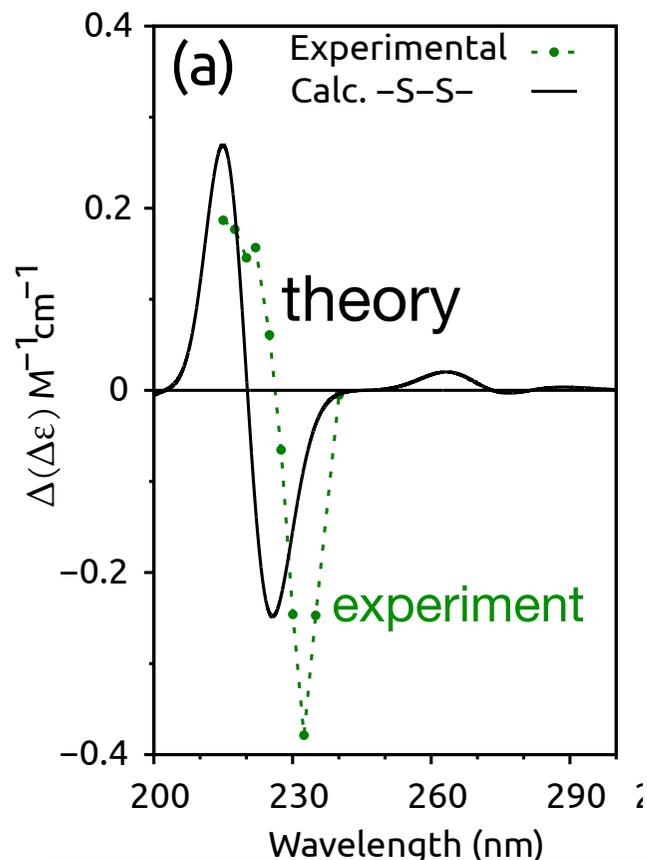
Renorm. Group &  
Eff. Field Theory



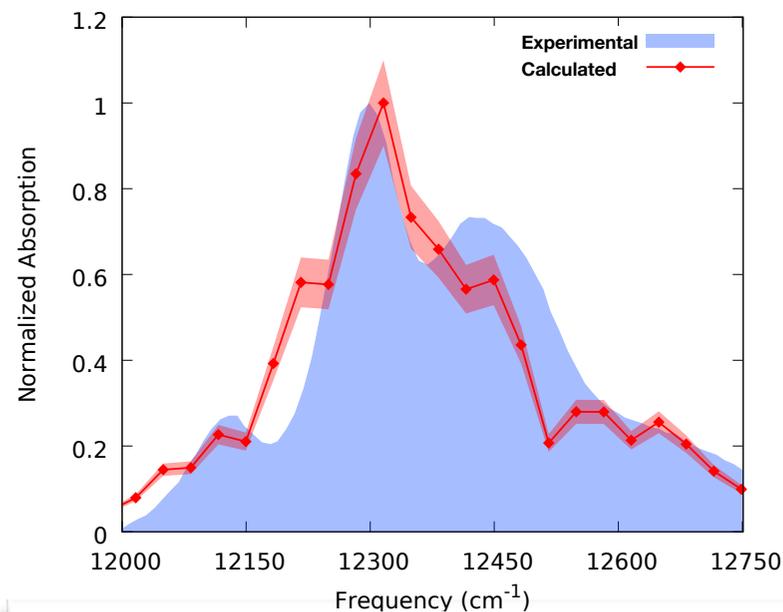
PRB 2013, JCP 2016

# EXAMPLES OF DIRECT COMPARISON WITH EXPERIMENTS

Time resolved near UV CD\*



Linear absorption spectrum



## Microscopic Calculation of Absorption Spectra of Macromolecules: an Analytic Approach

Matteo Carli

Physics Department of Trento University, Via Sommarive 14, Povo (Trento), 38123, Italy and  
Scuola Internazionale Superiore di Studi Avanzati (SISSA), via Bonomea 265, Trieste 34136, Italy.

Michele Turelli and Pietro Faccioli\*

Physics Department of Trento University, Via Sommarive 14, Povo (Trento), 38123, Italy and  
Trento Institute for Fundamental Physics and Applications (INFN-TIFPA), Via Sommarive 23, Povo (Trento), 38123, Italy

**J | A | C | S**  
JOURNAL OF THE AMERICAN CHEMICAL SOCIETY

Cite This: *J. Am. Chem. Soc.* 2018, 140, 3674–3682

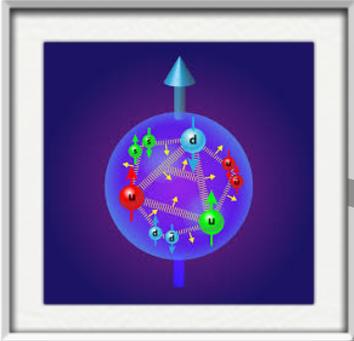
pubs.a

## Atomic Detail of Protein Folding Revealed by an Ab Initio Reappraisal of Circular Dichroism

Alan Ianeselli,<sup>†</sup> Simone Orioli,<sup>‡,||</sup> Giovanni Spagnoli,<sup>†</sup> Pietro Faccioli,<sup>\*,‡,||</sup> Lorenzo Cupellini,<sup>§,○</sup> Sandro Jurinovich,<sup>§</sup> and Benedetta Mennucci<sup>\*,§,○</sup>

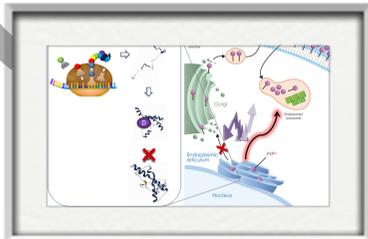
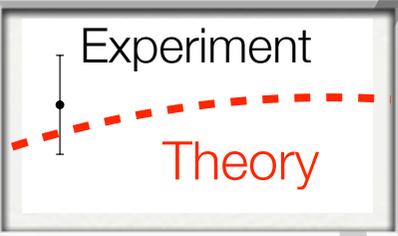
\* with B. Mennucci's Lab (U. Pisa)

# PHASE 3: EXPLOITATION IN MOLECULAR BIOLOGY



$$\mathcal{L} = \frac{1}{4g^2} G_{\mu\nu}^a G_{\mu\nu}^a + \sum_f \bar{\psi}_f (i\gamma^\mu \partial_\mu + m_f) \psi_f$$

where  $G_{\mu\nu}^a \equiv \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + gf_{abc} A_\mu^b A_\nu^c$   
and  $D_\mu \equiv \partial_\mu + i t^a A_\mu^a$   
*That's it!*



# EXPLORING BIOLOGICAL PROCESSES

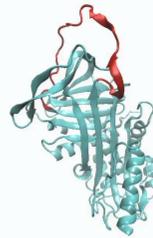
## Serpin latency transition at atomic resolution

Giorgia Cazzoli<sup>2,3</sup>, Fang Wang<sup>1</sup>, Silvio a Beccara<sup>3,4</sup>, Anne Gershenson<sup>5</sup>, Pietro Faccioli<sup>2,3,1</sup>, and Patrick L. Wintrode<sup>6,1</sup>

<sup>1</sup>Dipartimento di Fisica, Università degli Studi di Trento, 38100 Povo (Trento), Italy; <sup>2</sup>Trento Institute for Fundamental Physics and Applications, 38123 Povo (Trento), Italy; <sup>3</sup>Department of Pharmaceutical Sciences, School of Pharmacy, University of Maryland, Baltimore, MD 21201; <sup>4</sup>Interdisciplinary Laboratory for Computational Science, Fondazione Bruno Kessler, 38123 Povo (Trento), Italy; and <sup>5</sup>Department of Biochemistry and Molecular Biology, University of Massachusetts Amherst, Amherst, MA 01003

Edited by David E. Shaw, D. E. Shaw Research, New York, NY, and approved September 12, 2014 (received for review April 24, 2014)

Protease inhibition by serpins requires a large conformational transition from an active, metastable state to an inactive, stable state for polypeptide chains consisting of nearly 100 amino acids (6), which are considerably smaller than PAI-1. Additionally, the



Biophysical Journal  
Article

Biophysical Society

## All-Atom Simulations Reveal How Single-Point Mutations Promote Serpin Misfolding

Fang Wang,<sup>1</sup> Simone Orioli,<sup>2,3</sup> Alan Ianeselli,<sup>2,3</sup> Giovanni Spagnoli,<sup>2,3</sup> Silvio a Beccara,<sup>2,3</sup> Anne Gershenson,<sup>4,\*</sup> Pietro Faccioli,<sup>2,3,\*</sup> and Patrick L. Wintrode<sup>1,\*</sup>

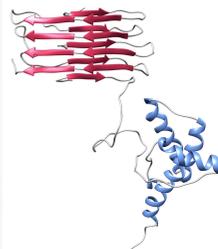


PLOS PATHOGENS

RESEARCH ARTICLE

## Full atomistic model of prion structure and conversion

Giovanni Spagnoli<sup>1\*</sup>, Marta Rigoli<sup>1,2</sup>, Simone Orioli<sup>2,3</sup>, Alejandro M. Sevillano<sup>4</sup>, Pietro Faccioli<sup>2,3</sup>, Holger Wille<sup>5</sup>, Emiliano Biasini<sup>1\*</sup>, Jesús R. Requena<sup>6\*</sup>



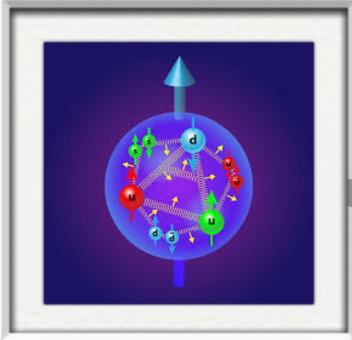
## All-Atom Simulation of the HET-s Prion Replication

Luca Terruzzi<sup>1,2\*</sup>, Giovanni Spagnoli<sup>2,3\*\*</sup>, Alberto Boldrini<sup>1,2</sup>, Jesús R. Requena<sup>4</sup>, Emiliano Biasini<sup>2,3#</sup> and Pietro Faccioli<sup>5,6#</sup>



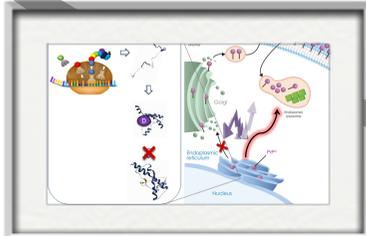
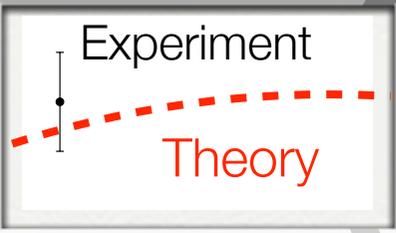
Teaming up with  
**E. Biasini's** lab (DICIBIO)

# PHASE 4: PHARMACOLOGICAL RESEARCH



$$\mathcal{L} = \frac{1}{4g^2} G_{\mu\nu}^a G_{\mu\nu}^a + \sum_f \bar{\psi}_f (i\gamma^\mu \partial_\mu + m_f) \psi_f$$

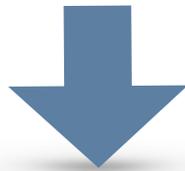
where  $G_{\mu\nu}^a \equiv \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + gf_{abc} A_\mu^b A_\nu^c$   
and  $D_\mu \equiv \partial_\mu + i t^a A_\mu^a$   
*That's it!*



# ROLE OF PROTEIN INACTIVATION

---

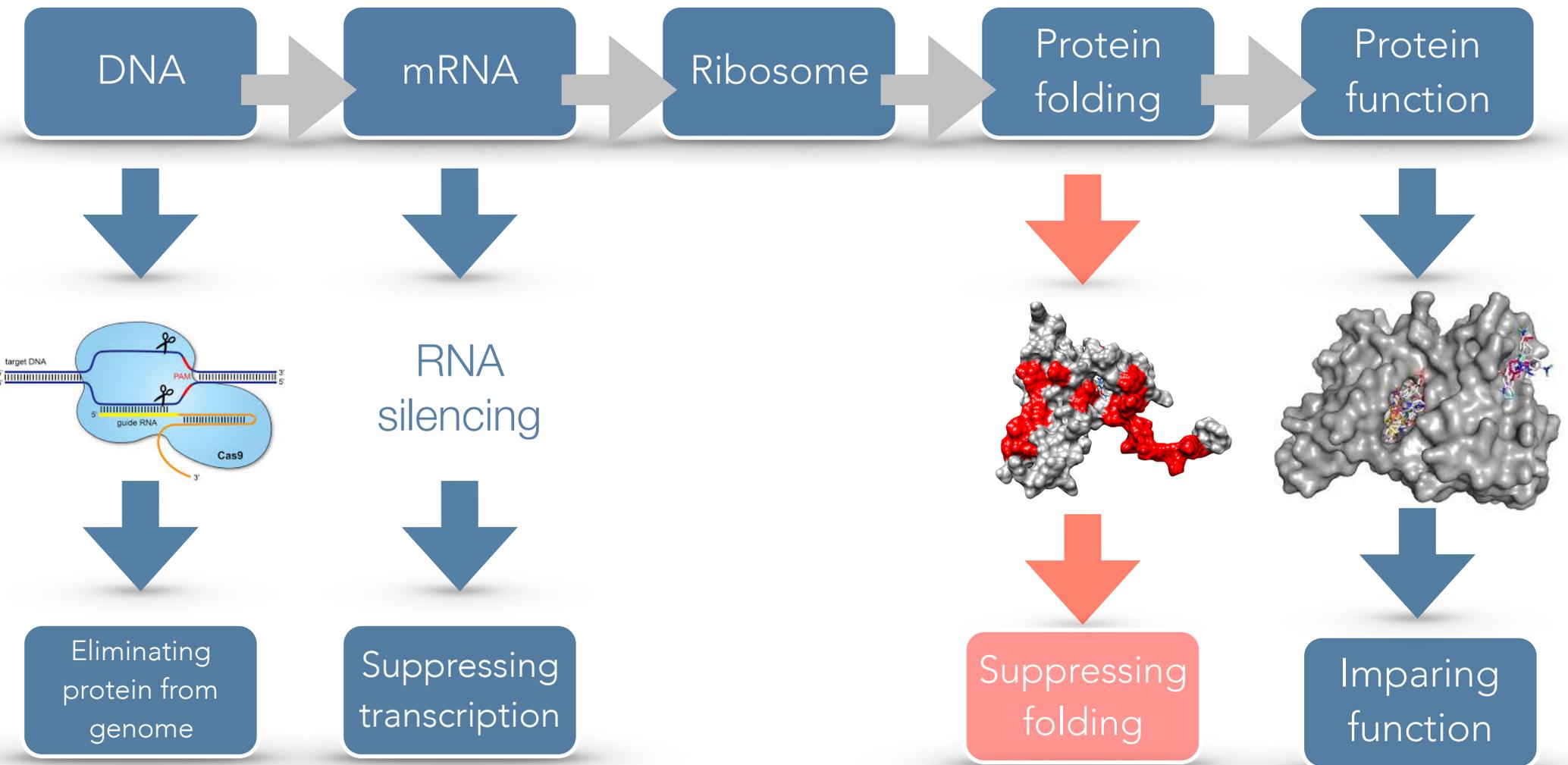
MOST OF BIOLOGICAL FUNCTIONS IN CELLS ARE CARRIED  
OUT BY **PROTEINS**



MOST OF MEDICINAL CHEMISTRY IS BASED ON  
**INHIBITING BIOLOGICAL FUNCTIONS OF PROTEINS**

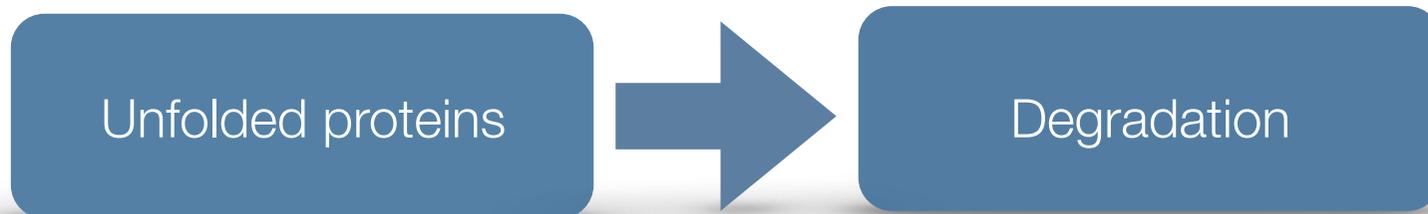
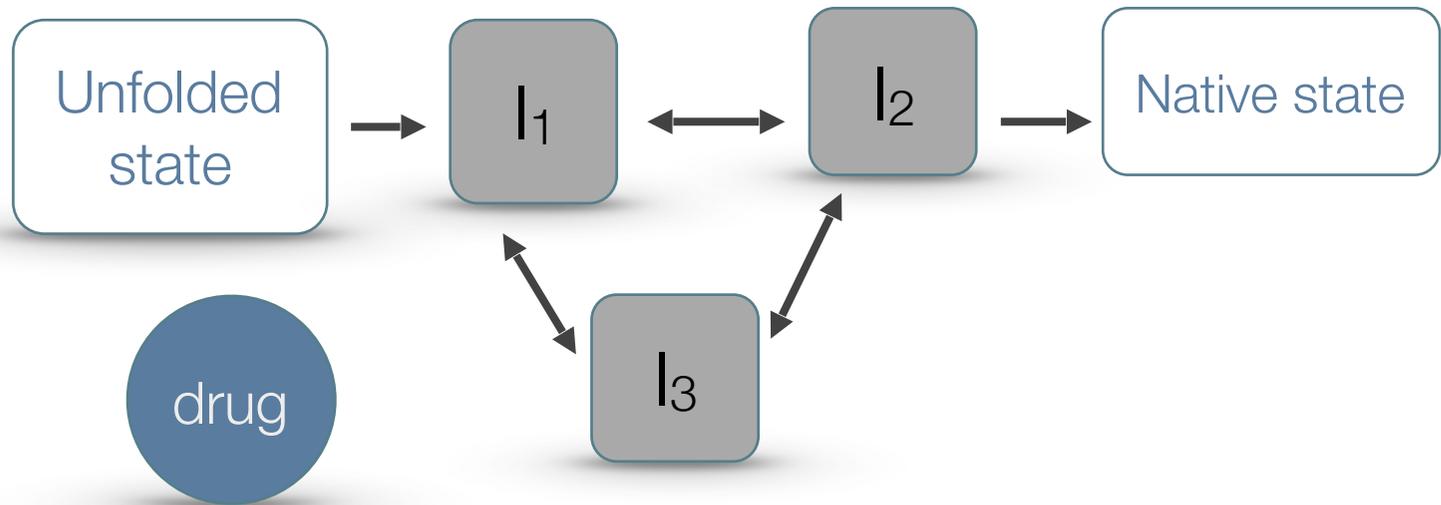
# PHARMACOLOGICAL PROTEIN INACTIVATION BY FOLDING INTERMEDIATE TARGETING

patent file # 102018000007535 (with E. Biasini)

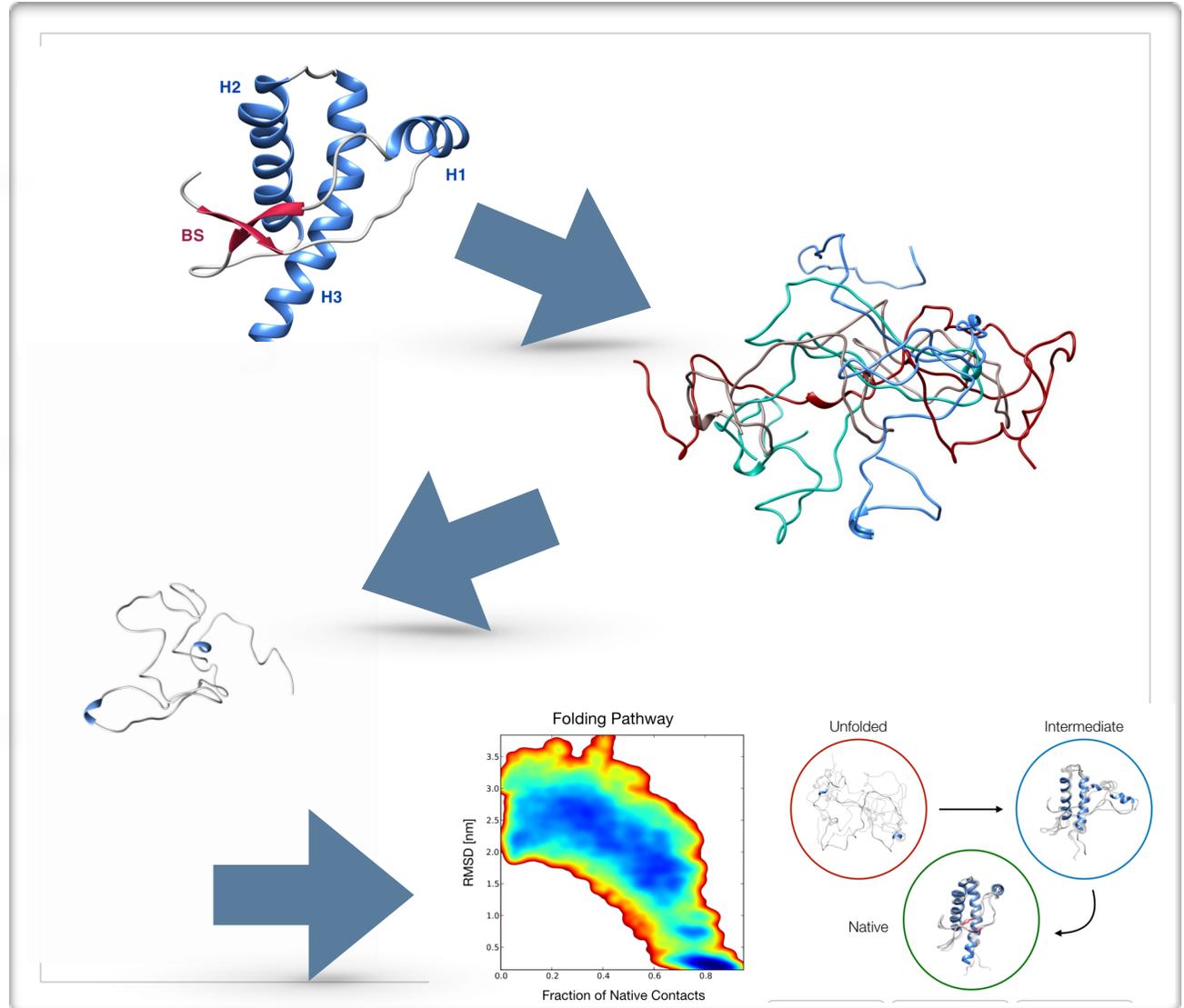
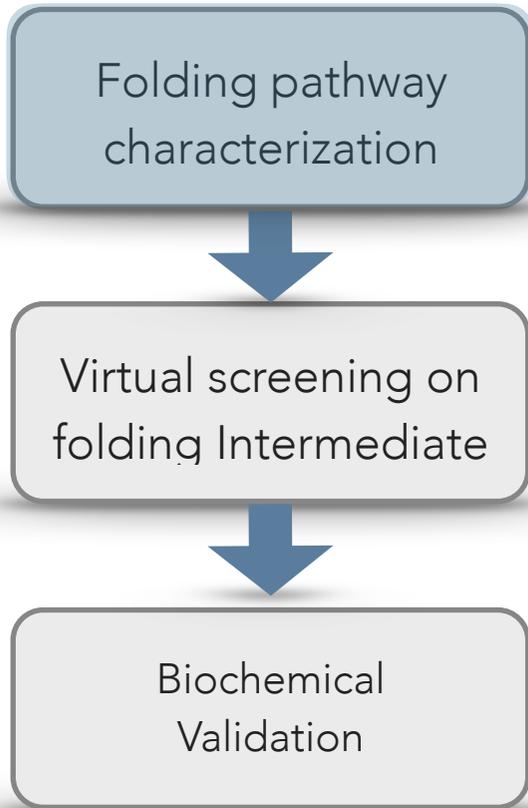


# PHARMACOLOGICAL PROTEIN INACTIVATION BY FOLDING INTERMEDIATE TARGETING

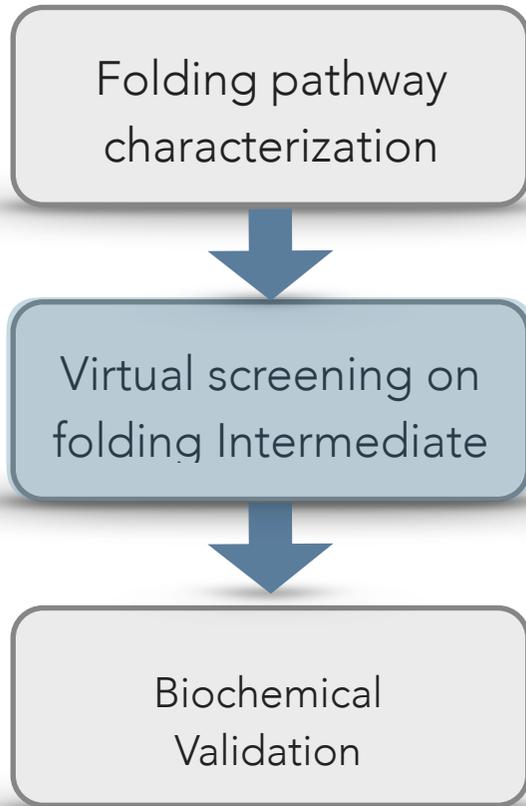
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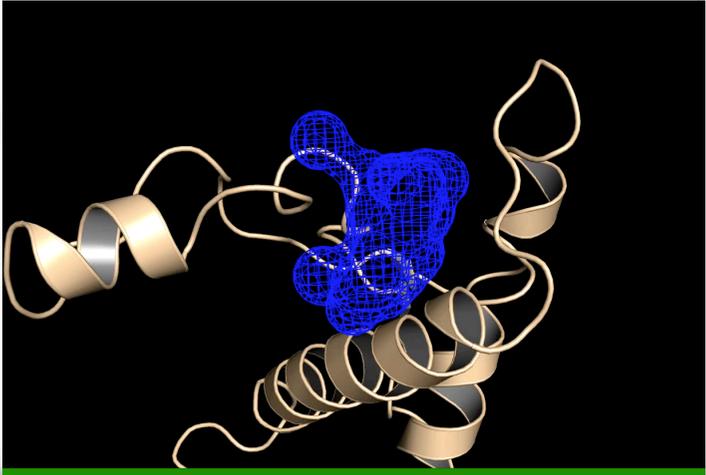
# PPI-FIT PIPELINE



# PPI-FIT PIPELINE



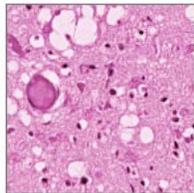
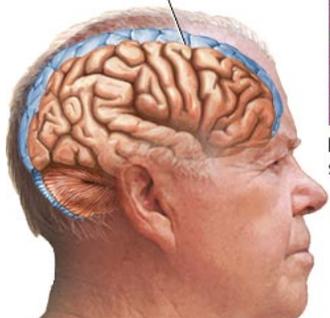
with  
L. Barreca's Lab



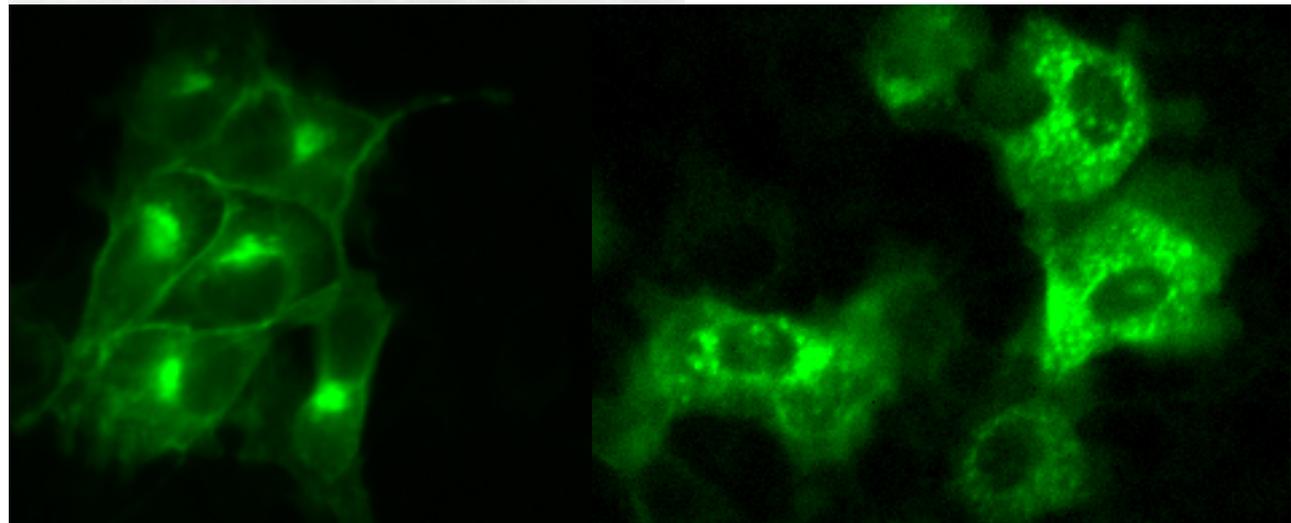
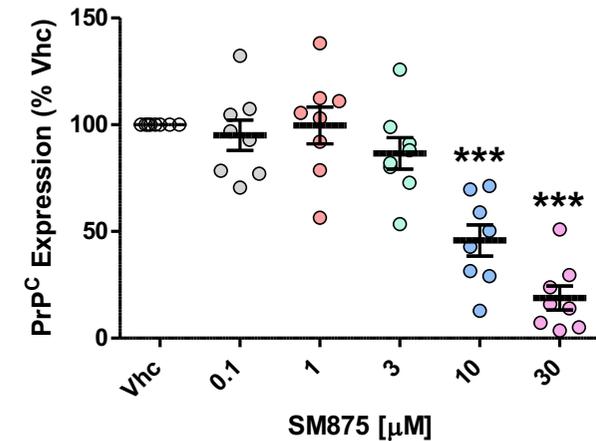
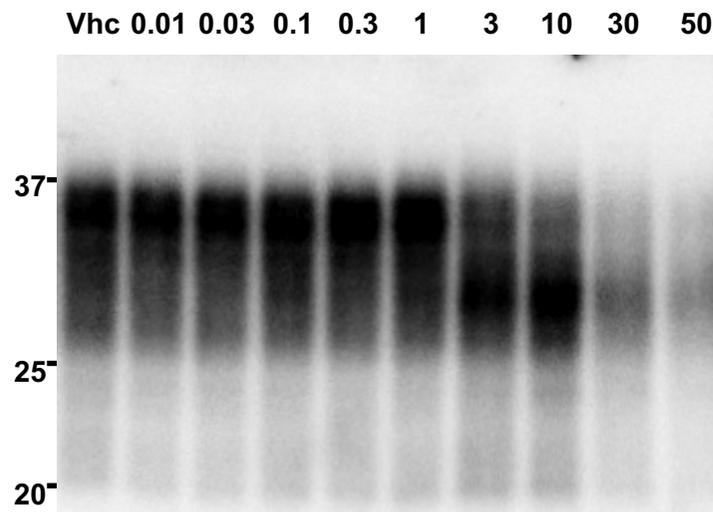
# DRUGGING THE UNDRUGGABLE

## Inactivation of Cellular Prion protein

Brain shrinkage and deterioration occurs rapidly



Brain section showing spongiform pathology characteristic of Creutzfeldt-Jakob



**COMMUNICATIONS  
BIOLOGY**

ARTICLE

<https://doi.org/10.1038/s42003-020-01385-x>

OPEN



Pharmacological inactivation of the prion protein by targeting a folding intermediate

# Technology Transfer Initiative



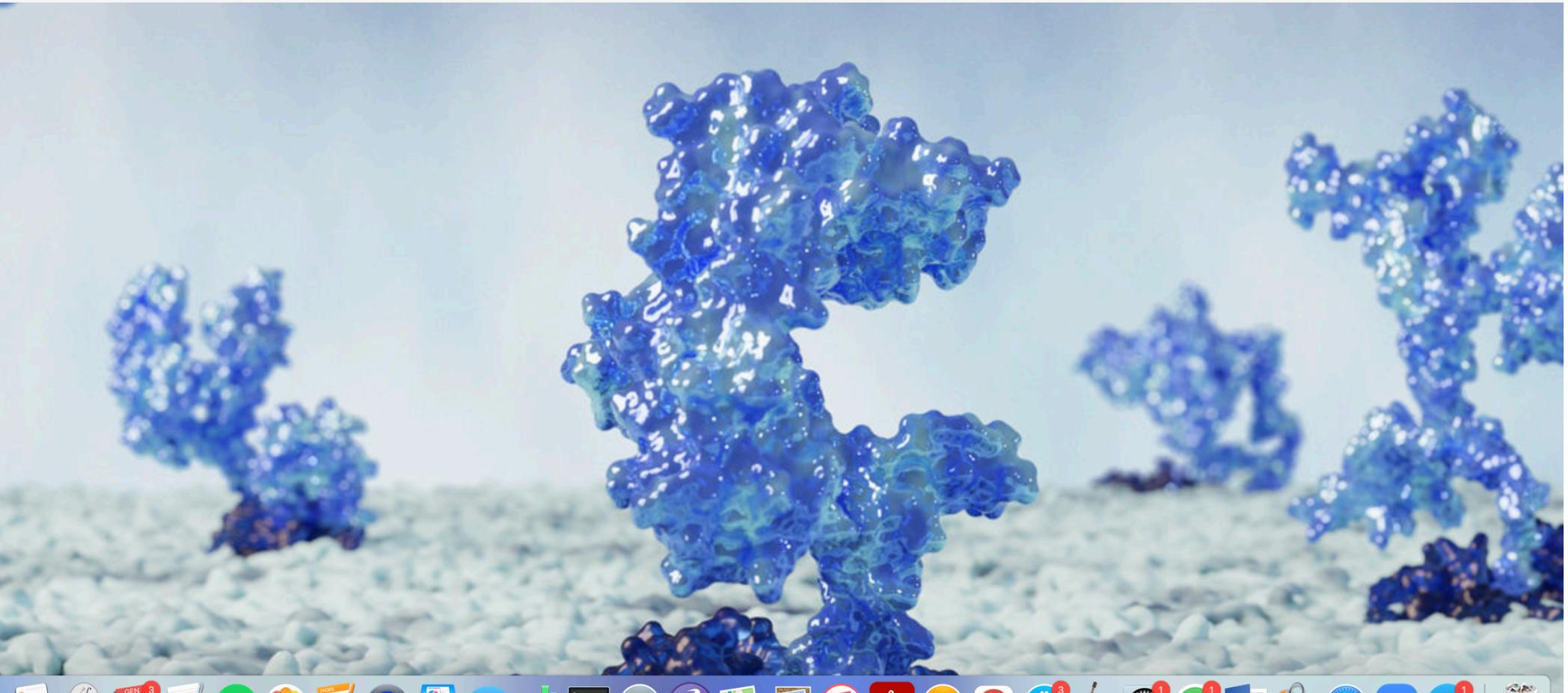
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[NEWS](#)

[CONTACT](#)

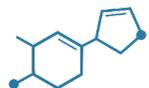


# Joining Forces against COVID-19

**Maria Letizia Barreca**




UNIVERSITÀ DEGLI STUDI DI PERUGIA



**Emiliano Biasini**




UNIVERSITÀ DI TRENTO

FONDAZIONE **telethon**



**Pietro Faccioli**




UNIVERSITÀ DI TRENTO

**TIFPA**



**Graziano Lolli**




UNIVERSITÀ DI TRENTO




**INFN**

Istituto Nazionale di Fisica Nucleare

30.000 cores in 8 data centers

**Lidia Pieri**




**Giovanni Spagnoli**




**Alberto Boldrini**




**Tania Massignan**



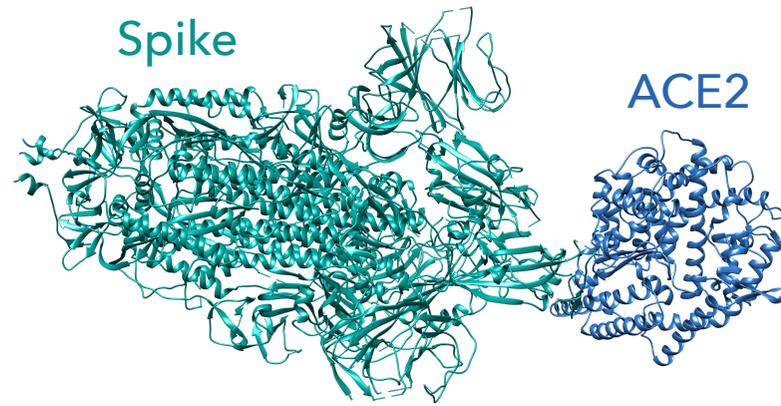
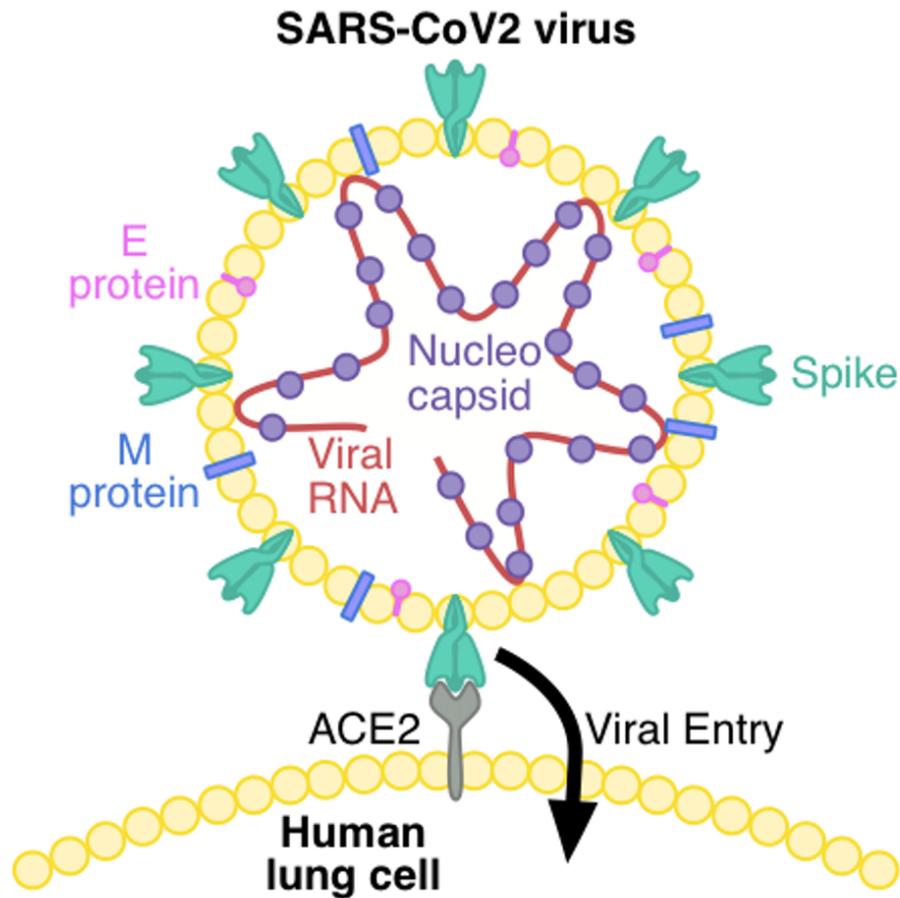

**Luca Terruzzi**




**Andrea Astolfi**




# SARS-CoV-2 Replication



Goals:

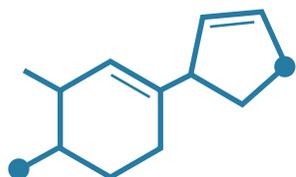
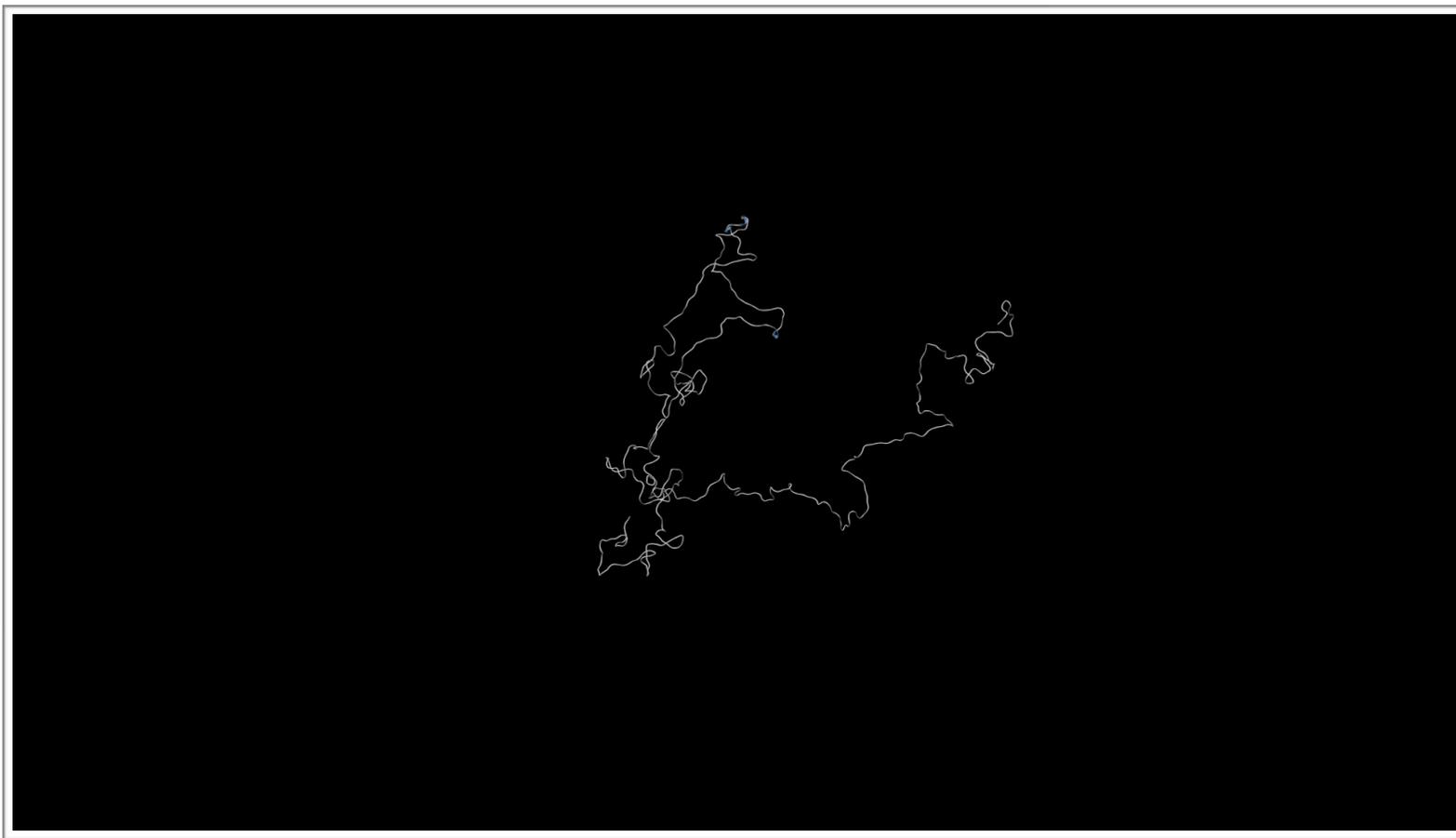
**Repurposing** of approved drugs!  
Looking for suppressors of ACE2  
expression levels

Figure taken from:

<https://theconversation.com/where-are-we-at-with-developing-a-vaccine-for-coronavirus-134784>

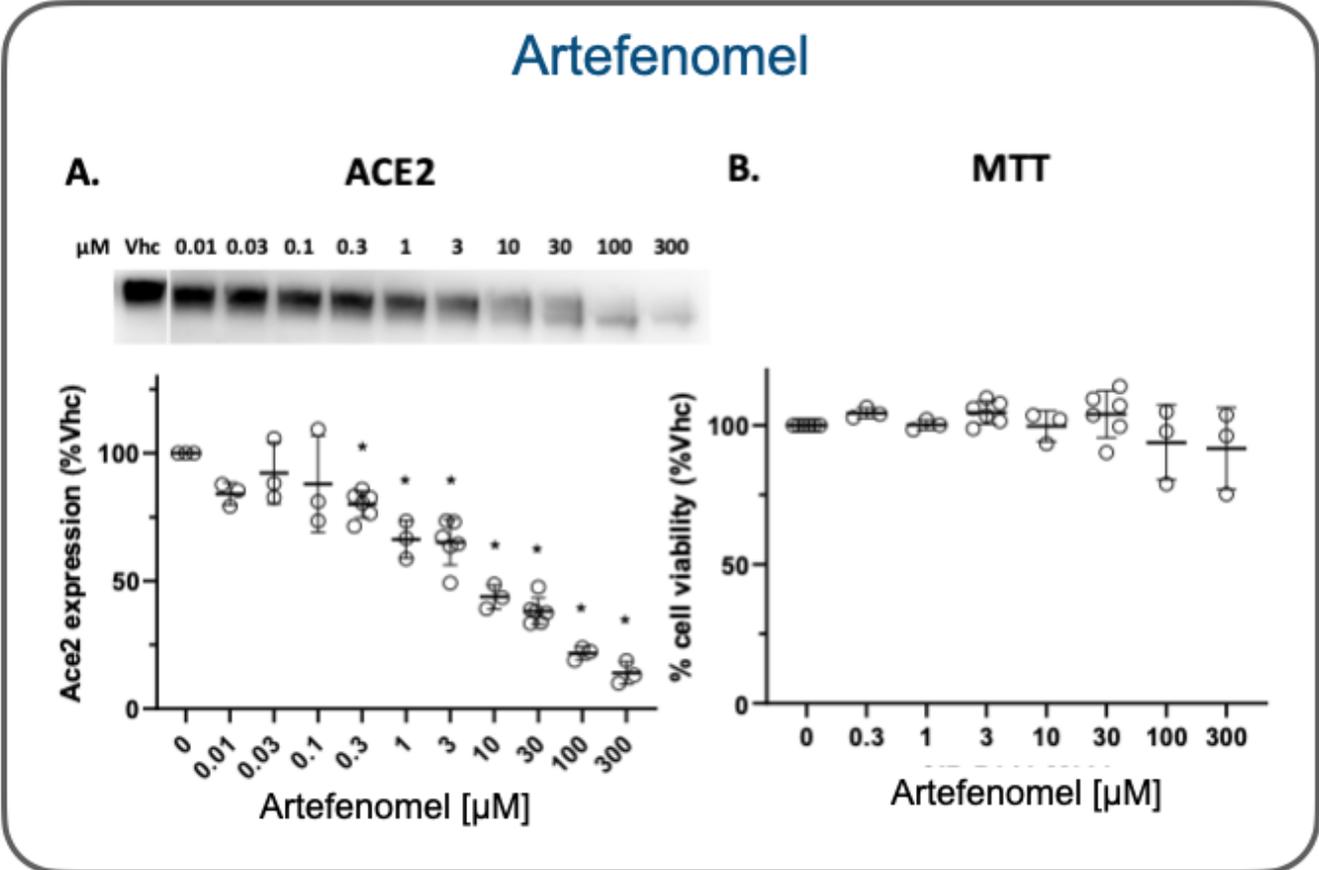
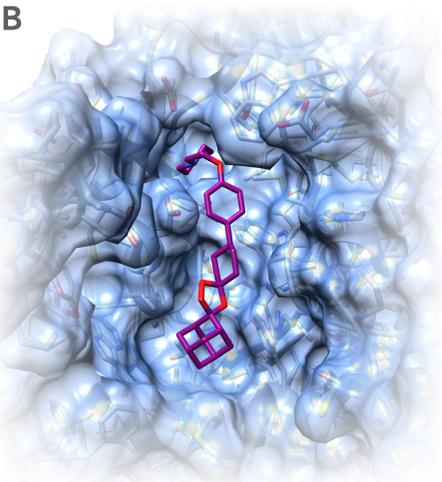
# PPI-FIT ON ACE2

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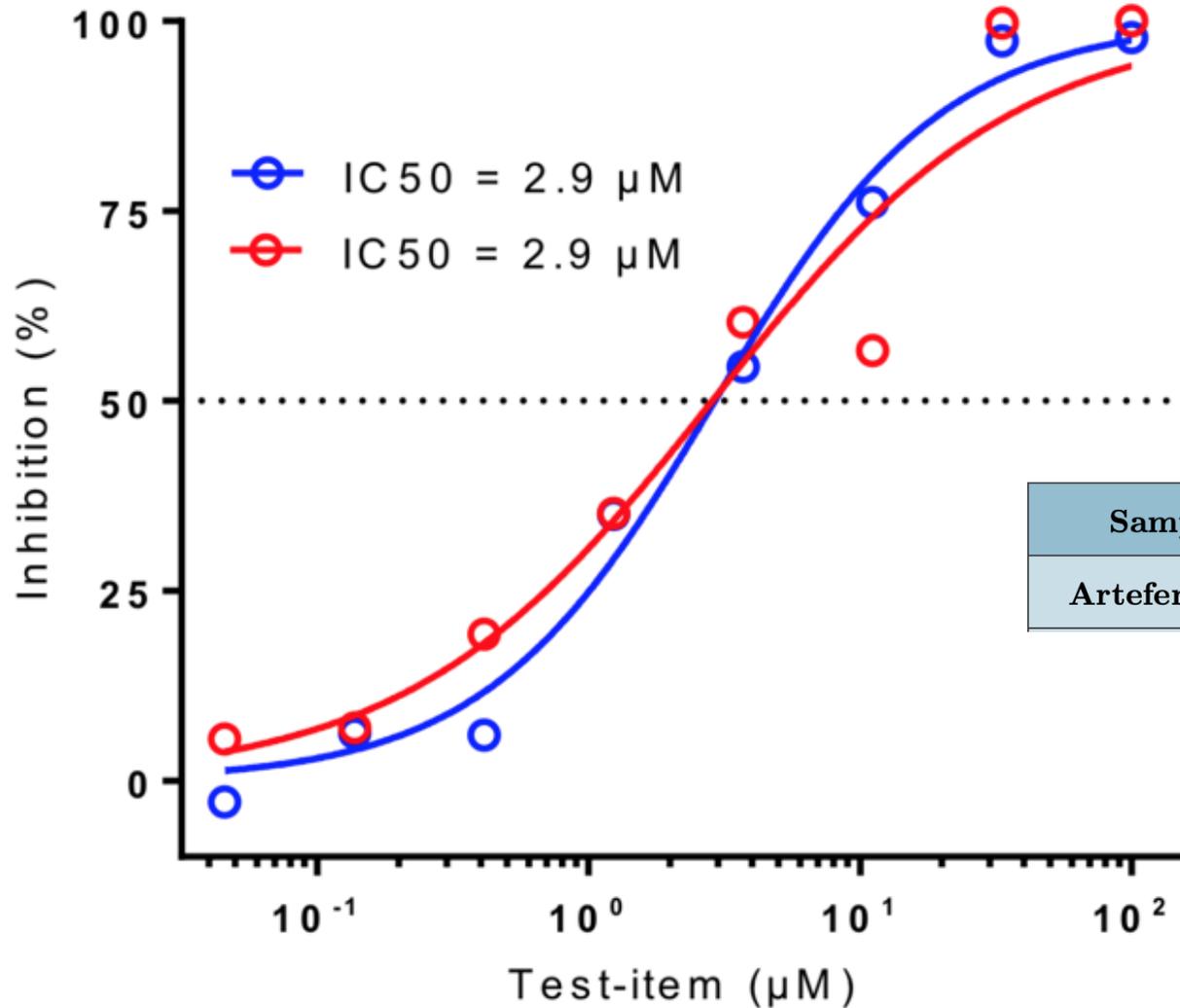


Out of 9000 candidates, we found 35 molecules binding in-silico the intermediate. Validation experiments on cellular bio-assays are ongoing.

# DOSE-DEPENDENT RESPONSE



# ANTI-VIRAL ACTIVITY AGAINST LIVE SARS-COV2



Concentration at which it becomes active



| Sample      | IC <sub>50</sub> [µM] | CC <sub>50</sub> [µM] |
|-------------|-----------------------|-----------------------|
| Artefenomel | 2.9                   | > 100                 |

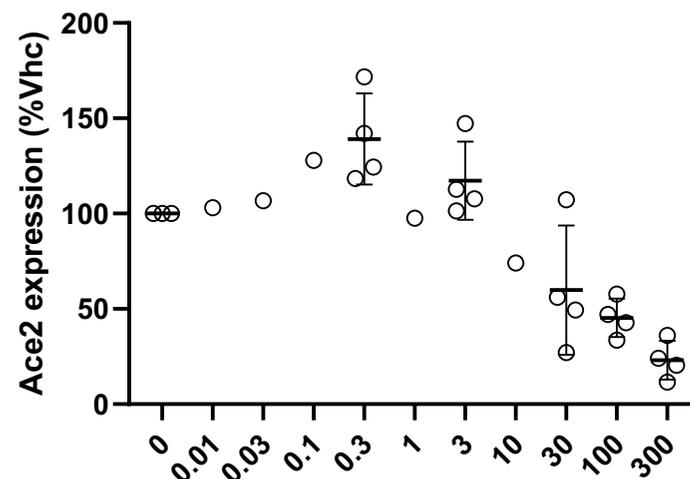
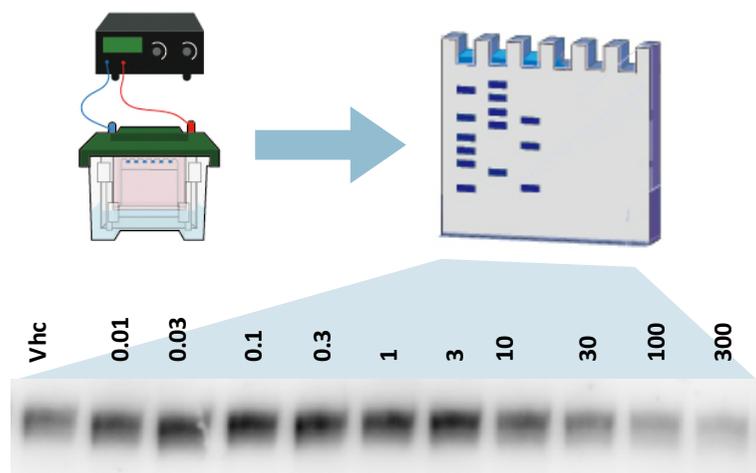
Concentration at which it becomes toxic

This value is *in principle* compatible with the maximum tolerated dose in humans. More to follow...

# BREAKING NEWS!! (17/05/2020)

So far, Sibylla Biotech has tested 14 virtual hits

ONE DISPLAYS A **PROMINENT EFFECT** WITH CLEAR **DOSE-RESPONSE** RELATIONSHIP AND VERY **LOW TOXICITY**



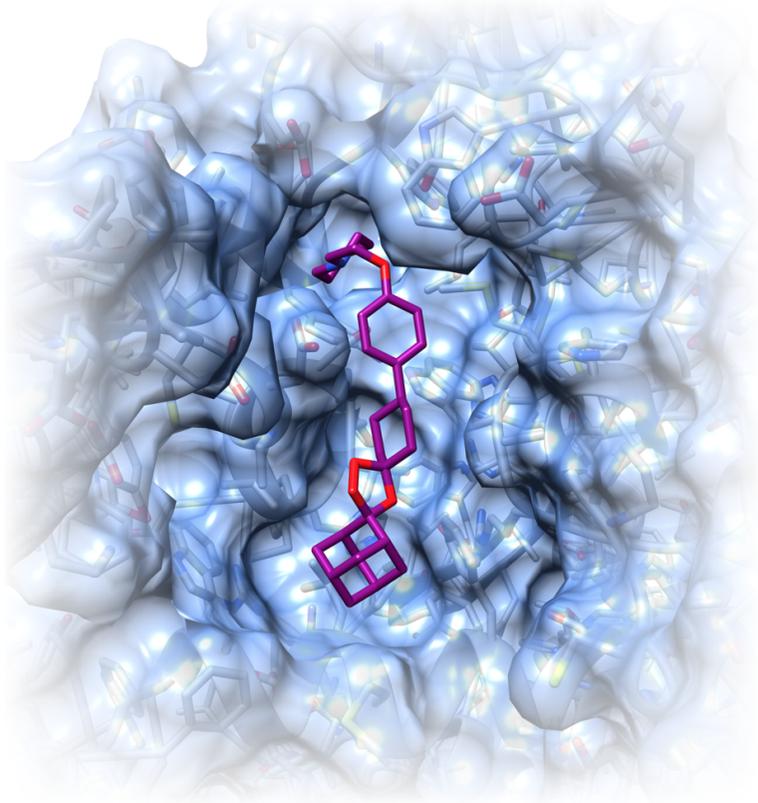
# SPACE IS THE NEXT FRONTIER!

---



# A MAIN LIMITING FACTOR

---



Impossible to crystallize  
folding intermediates  
on Earth



**Microgravity**  
**conditions** may  
provide the solution!

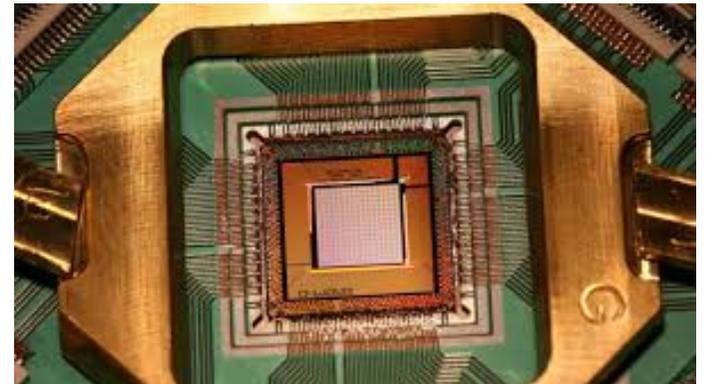
# Molecular Biology **PRIN**

(functional role of folding intermediates?)

## ZEFIR MISSION\*



## Quantum Computing + AI



PHYSICAL REVIEW LETTERS VOL..XX, 000000 (XXXX)

### Dominant Reaction Pathways by Quantum Computing

Philipp Hauke<sup>1</sup>, Giovanni Mattiotti<sup>2</sup>, and Pietro Facchioli<sup>2,3</sup>

<sup>1</sup>INO-CNR BEC Center and Department of Physics, University of Trento, Via Sommarive 14, I-38123 Trento, Italy

<sup>2</sup>Department of Physics, University of Trento, Via Sommarive 14, I-38123 Trento, Italy

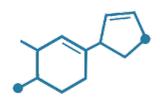
<sup>3</sup>INFN-TIFPA, Via Sommarive 14, I-38123 Trento, Italy

(Received 27 July 2020; accepted 18 December 2020)

(\* PRELIMINARY NAME)

# People

**Maria Letizia Barreca PhD**



**Emiliano Biasini PhD**



**Pietro Faccioli PhD**



**Graziano Loli PhD**



**Lidia Pieri PhD**



Founder - CEO



**Giovanni Spagnoli**



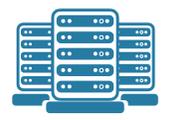
Founder  
Chief Scientist



**Alberto Boldrini**



Staff  
(Computational)



**Tania Massignan PhD**



Staff (Wet Lab)



**Luca Terruzzi**



Staff  
(Computational)



**Andrea Astolfi PhD**



Consultant  
Medicinal Chemist



# Acknowledgments



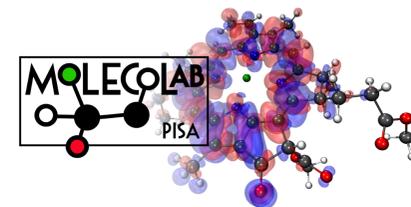
Trento Institute for  
Fundamental Physics  
and Applications



## Italy:

**Trento:** *E. Biasini, A. Ianeselli (2014-2017), G. Spagnoli S. A Beccara (2009-2017), S. Orioli (2014-2018), E. Schneider (2012-2015), M. Carli (2017), M. Turelli (2018), F. Mascherpa (2014), G. Garberoglio, F. Pederiva, M. Sega, R. Covino (2012-2015),*

**Pisa:** B. Mennucci, L. Cupellini, S. Jurinovich



**Perugia:** L. Barreca

**SISSA:** C. Micheletti, A. Laio

## Europe:

**U. Zurich:** B. Schuler

**U. Compostela:** J. Raquena

**CEA-Saclay:** H. Orland

**USA: U. Maryland:** P. Wintrode

**U. Mass.:** A. Gershenson



## MAIN TAKE-HOME MESSAGES

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**Fundamental research** matters!

The usefulness of **theoretical physics** extends beyond its natural cultural perimeter

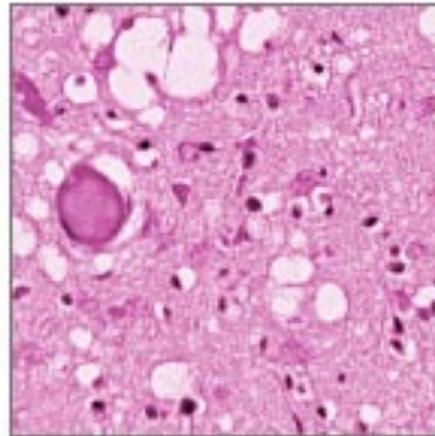
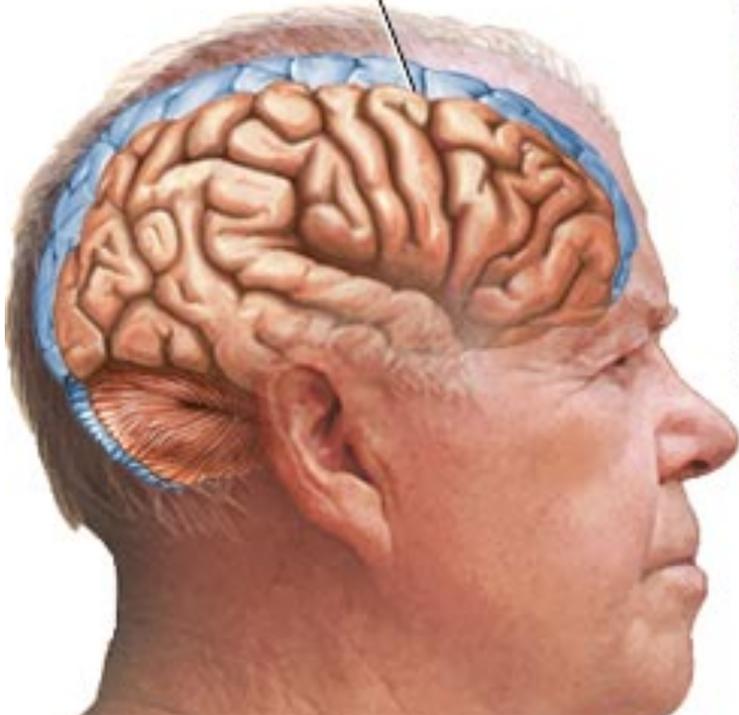
**Major research infrastructures** for fundamental research can be **re-purposed**

**Technological transfer** can boost research and help advance Science

# DRUGGING THE UNDRUGGABLE

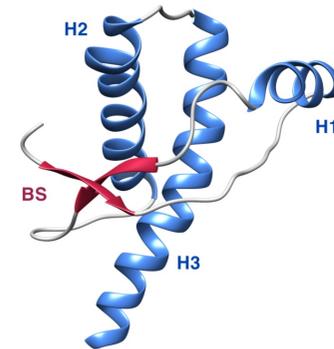
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Brain shrinkage and deterioration occurs rapidly



Brain section showing spongiform pathology characteristic of Creutzfeldt-Jakob

## PRION DISEASES



# ARE THERE **POTENTIAL** ADVANTAGES?

---

## **“More” (?)**

Applicable to  
“undruggable  
proteins”

Applicable to  
misfolding  
proteins

## **“Better” (?)**

More specificity

Low effective  
dissociation rate  
constant

Known mechanism of  
action

# Heavy quark diffusion in a QGP

Heavy quark bound states in a quark–gluon plasma:  
Dissociation and recombination

Jean-Paul Blaizot<sup>a</sup>, Davide De Boni<sup>b,d</sup>, Pietro Faccioli<sup>d,e</sup>,  
Giovanni Garberoglio<sup>c,e</sup>

EFFECTIVE  
STOCHASTIC  
DYNAMICS

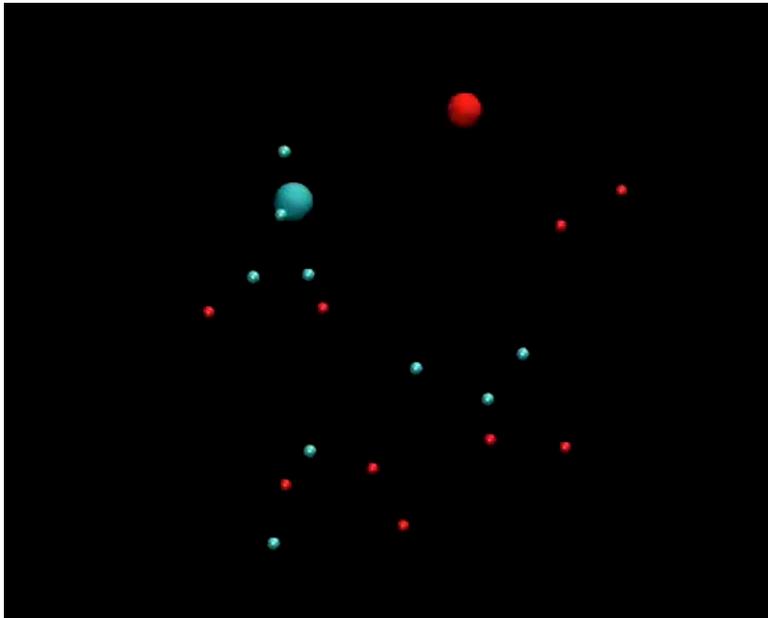
Model: NR relativistic particles coupled to an abelian plasma of fermions and gauge fields at finite temperature. After integrating out the gauge fields:

$$P(\mathbf{Q}_f, t_f | \mathbf{Q}_i, t_i) = \int_{\mathcal{C}} D\mathbf{Q} \int_{\mathcal{C}} D(\bar{\psi}, \psi) e^{iS[\mathbf{Q}, \psi, \bar{\psi}]},$$

After integrating out the fermions and making the Ohmic approximation => **Effective Generalized Langevin**

$$M \ddot{\mathbf{R}} = -M\boldsymbol{\gamma}(\mathbf{R}) \cdot \dot{\mathbf{R}} + \mathbf{F}(\mathbf{R}) + \boldsymbol{\xi}(\mathbf{R}, t),$$

$$\langle \xi_{i'}(\mathbf{R}, t) \rangle = 0, \quad \langle \xi_{k'}(\mathbf{R}, t) \xi_{m'}(\mathbf{R}, t') \rangle = \lambda_{k'm'}(\mathbf{R}) \delta(t - t').$$



↑  
QGP plasma polarization induced  
by heavy fermions

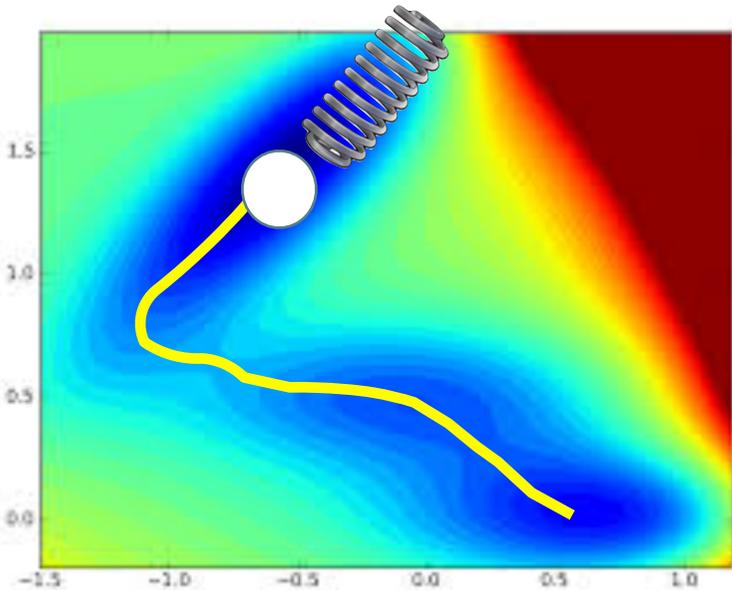
# RATCHET-AND-PAWL MD



*E. Paci and M. Karplus, J. Mol. Biol. **288**, 441 (1999).*

*C. Camilloni, R. A. Broglia, and G. Tiana, J. Chem. Phys. **134**, 045105 (2011).*

# IDEAL BIAS



**Theorem:** rMD along the ideal reaction coordinate RC (i.e. the committor function) yields the exact equilibrium distribution and reactive current

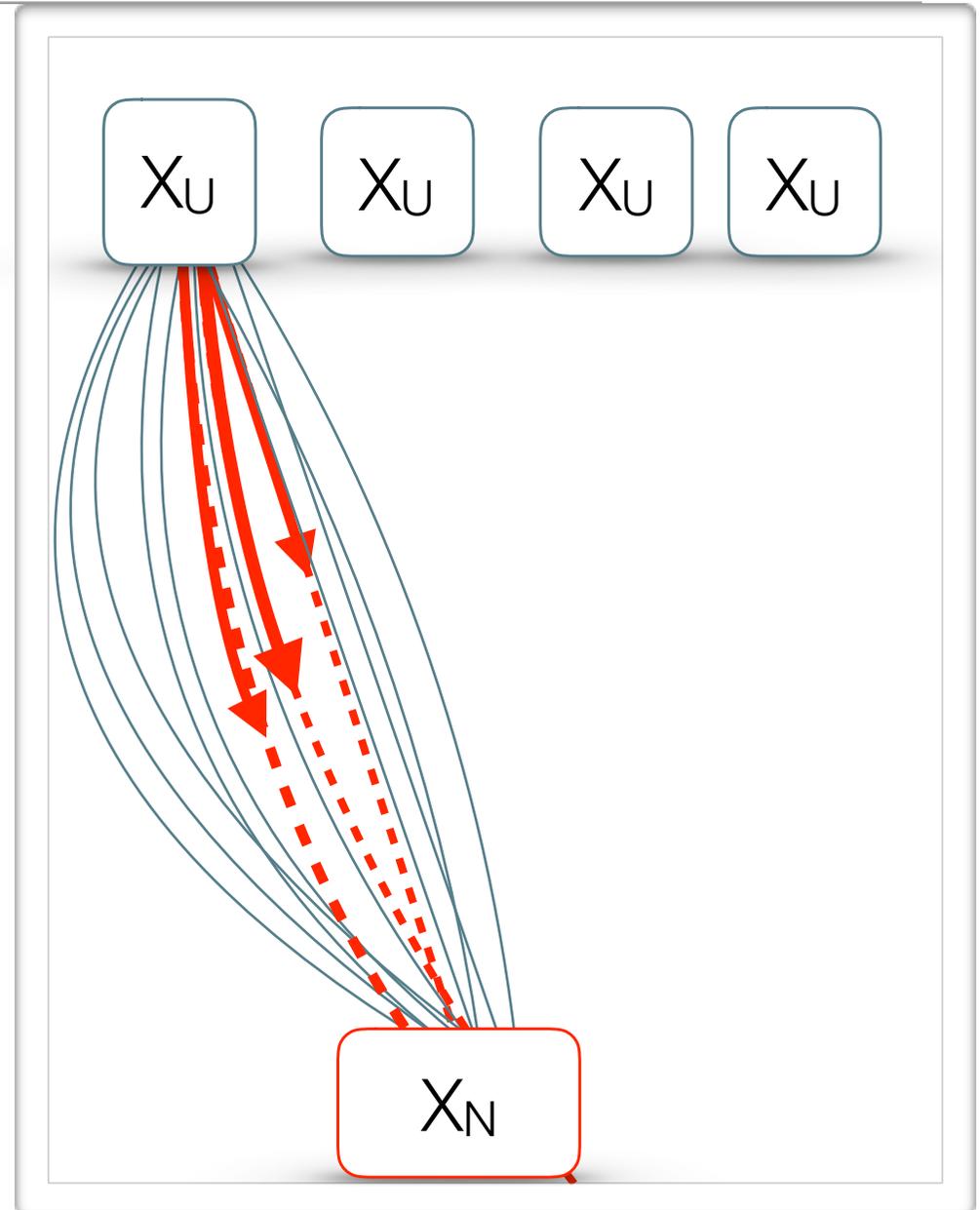
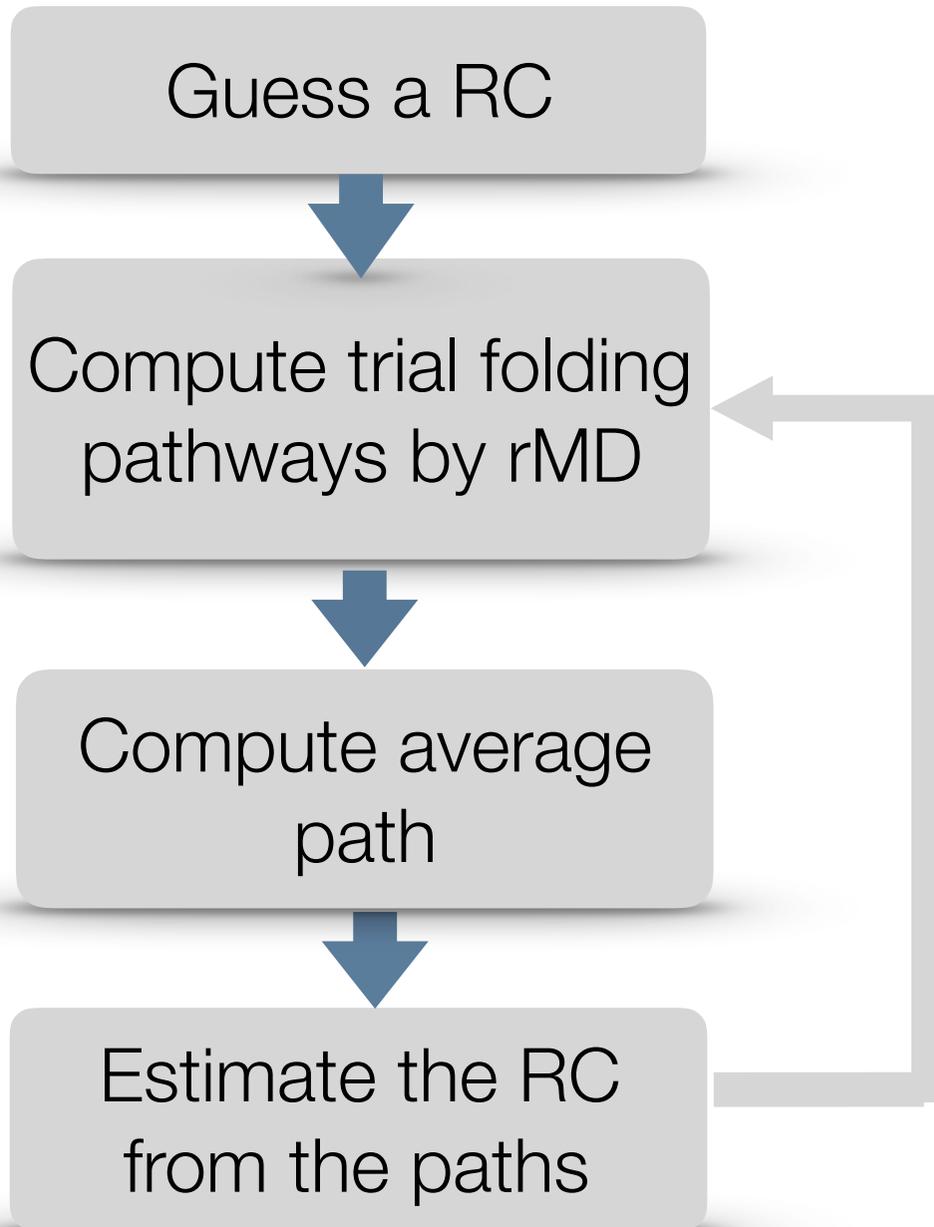
M. Cameron and E. Vanden-Eijnden, *J. Stat. Phys.* 156, 427 (2014).

G. Bartolucci, S. Orioli and P. Faccioli *J.Chem. Phys.* 149, 072336 (2018).

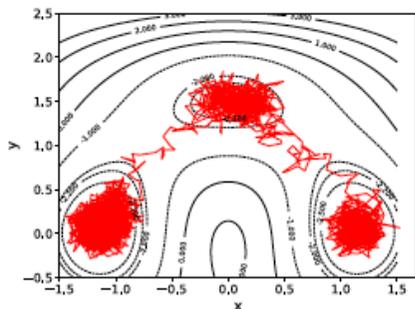
## Challenge:

How can we learn the RC self-consistently and compute the committor “on the fly” in a rMD calculation?

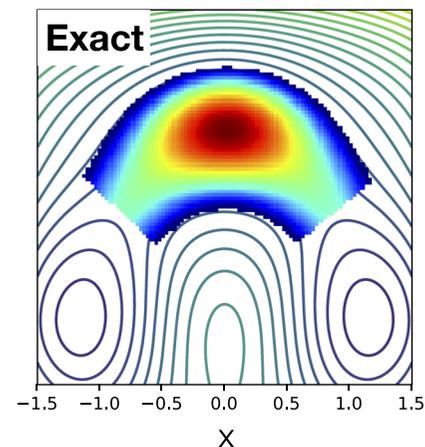
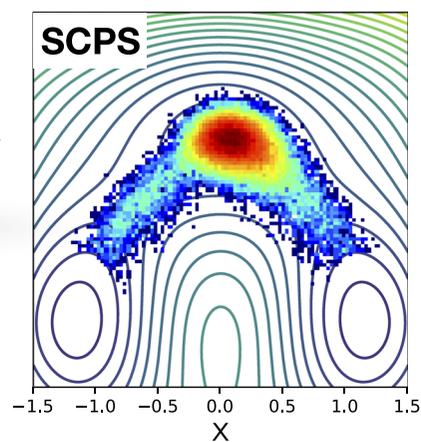
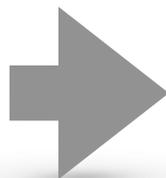
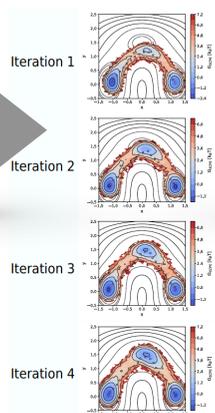
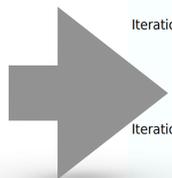
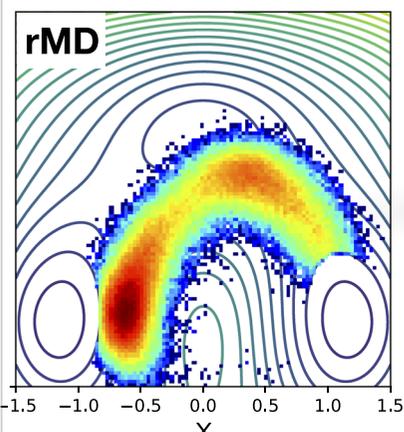
# SELF CONSISTENT PATH SAMPLING



# REACHING ACCURACY



three-state kinetics...



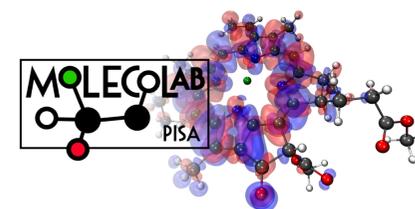
...more slides for discussion session

# Past, present and long term collaborators

---

**Trento:** *E. Biasini*, A. Ianeselli (2014-2017), G. Spagnolli S. A Beccara (2009-2017), S. Orioli (2014-2018), E. Schneider (2012-2015), M. Carli (2017), M. Turelli (2018), F. Mascherpa (2014), *G. Garberoglio*, *F. Pederiva*, *M. Sega*, R. Covino (2012-2015),

**Pisa:** B. Mennucci, L. Cupellini, S. Jurinovich



**Perugia:** L. Barreca    **SISSA:** C. Micheletti, A. Laio

**CEA-Saclay:** H. Orland, J.P. Blaizot

**U. Maryland Baltimore:** P. Wintrode

**U. Mass. Amherst:** A. Gershenson

**U. Zurich:** B. Schuler

Thank you for your attention!

# Implementation step 1: Trotter decomposition

---

Trotter decomposition: 
$$e^{-\frac{i}{\hbar}\hat{H}t} = e^{-\frac{i}{\hbar}dt\hat{H}} \dots e^{-\frac{i}{\hbar}dt\hat{H}} + \mathcal{O}(dt^2)$$

$$= e^{-\frac{i}{\hbar}dt\hat{H}} \mathbf{1} e^{-\frac{i}{\hbar}dt\hat{H}} \dots \mathbf{1} e^{-\frac{i}{\hbar}dt\hat{H}} + \mathcal{O}(dt^2)$$

$$1 = \int dQ \int dX \int \left( \prod_{k,s=1,2} \frac{d\phi_{k,s} d\phi_{k,s}^*}{2\pi i} \right) e^{-\sum_{s=1,2} \sum_{l=1} \phi_{l,s} \phi_{l,s}^*} |Q, X, \Phi\rangle \langle Q, X, \Phi|$$

Atomic nuclei, heat-bath variables  
in **first quantization**  
(i.e. use coordinates)

Hopping quantum excitation  
in **second quantization**  
(i.e. use coherent fields)

**Implementation step 2:** Integrate out solvent  
(Gaussian integral)

$$\int_{\mathcal{C}} \mathcal{D}X \int_{\mathcal{C}} \mathcal{D}Q \int_{\mathcal{C}} \mathcal{D}\psi \mathcal{D}\bar{\psi} (\dots) = \int_{\mathcal{C}} \mathcal{D}Q \int_{\mathcal{C}} \mathcal{D}\psi \mathcal{D}\bar{\psi} (\dots) e^{-\Phi[Q]}$$

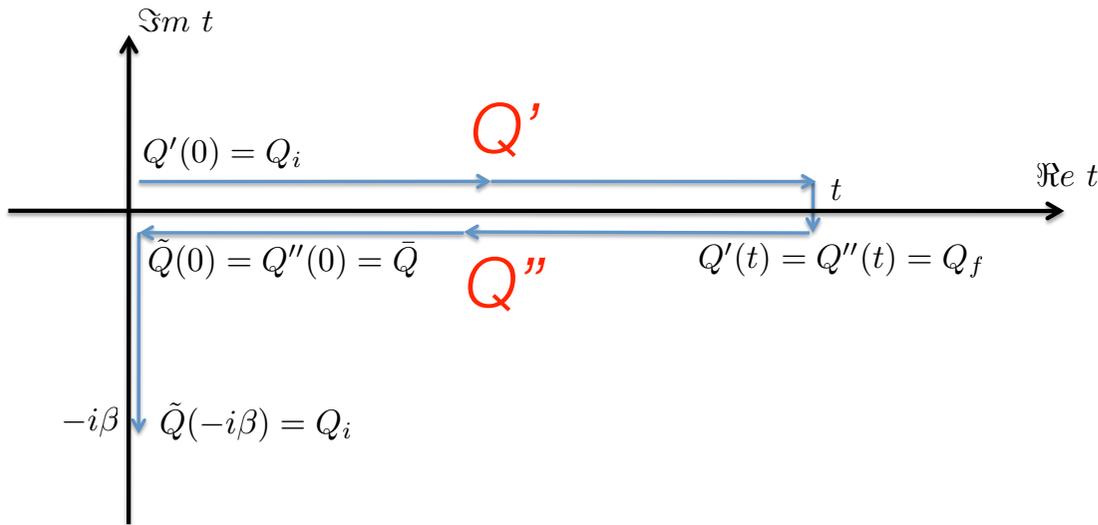
**Implementation step 3:** Take the Ohmic limit in the  
Green's function of the Caldeira-Leggett bath

$$\Delta(\omega) \simeq C_0 + C_1 \omega$$

**Implementation step 4:** Classical limit on atomic  
motion using saddle-point approximation to  
*quadratic level.*

# Implementing the two approximations:

## 1. The dynamics of the atomic nuclei is classical:



$$R \equiv \frac{1}{2} (Q' + Q'')$$

$$y \equiv Q' - Q''$$

classical limit

$$R(t) \gg y(t)$$

expand to order  $o(y^2)$

perform  $\int \mathcal{D}y$

$$P(Q_f, k_f, t | Q_i, k_i) = \int_{Q_i}^{Q_f} \mathcal{D}R \int \mathcal{D}\phi'^* \mathcal{D}\phi' \int \mathcal{D}\phi''^* \mathcal{D}\phi'' (\dots)$$

# Implementing the two approximations

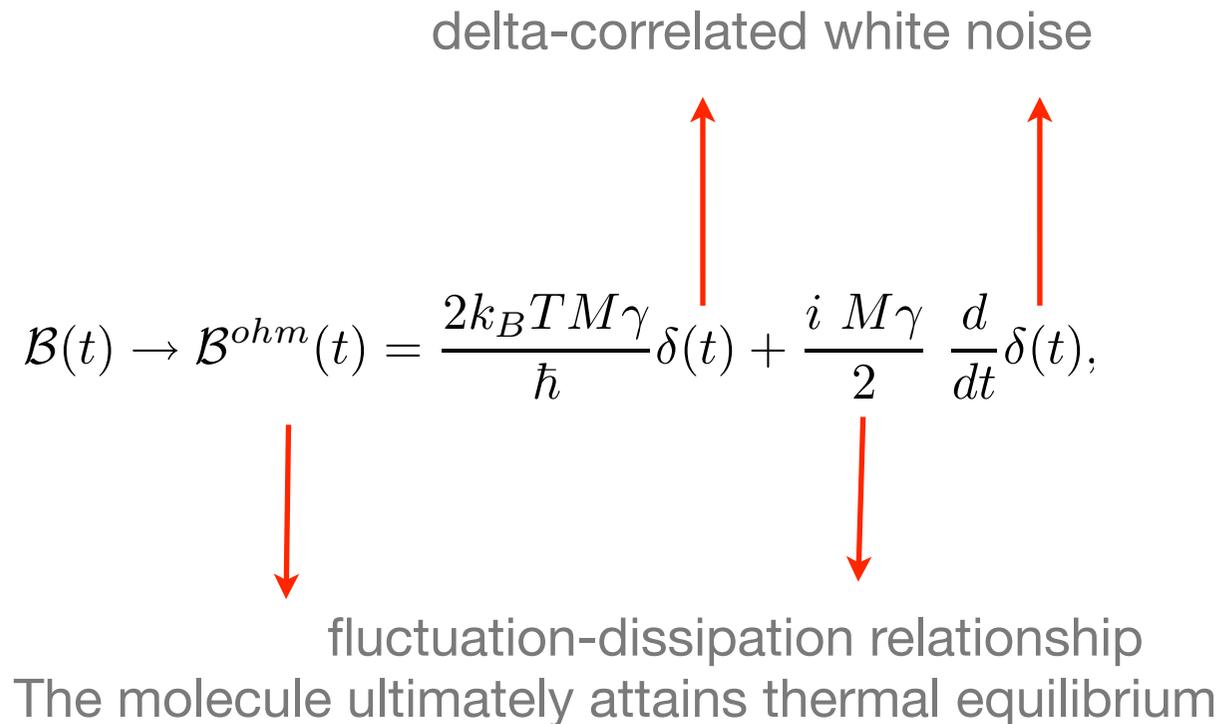
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## 2. The heat-bath quickly loses its “memory”

delta-correlated white noise

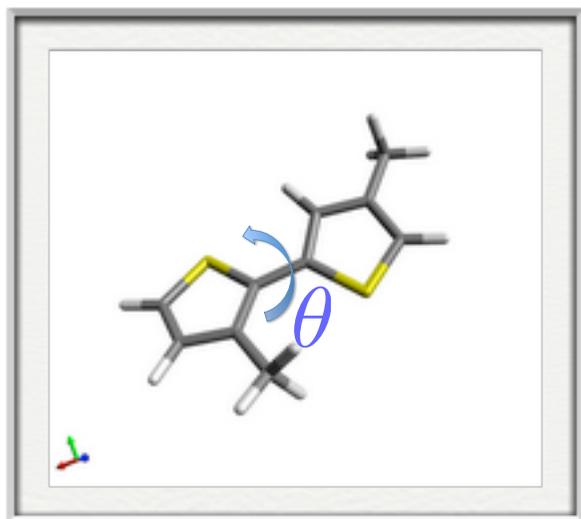
$$\mathcal{B}(t) \rightarrow \mathcal{B}^{ohm}(t) = \frac{2k_B T M \gamma}{\hbar} \delta(t) + \frac{i M \gamma}{2} \frac{d}{dt} \delta(t),$$

fluctuation-dissipation relationship  
The molecule ultimately attains thermal equilibrium

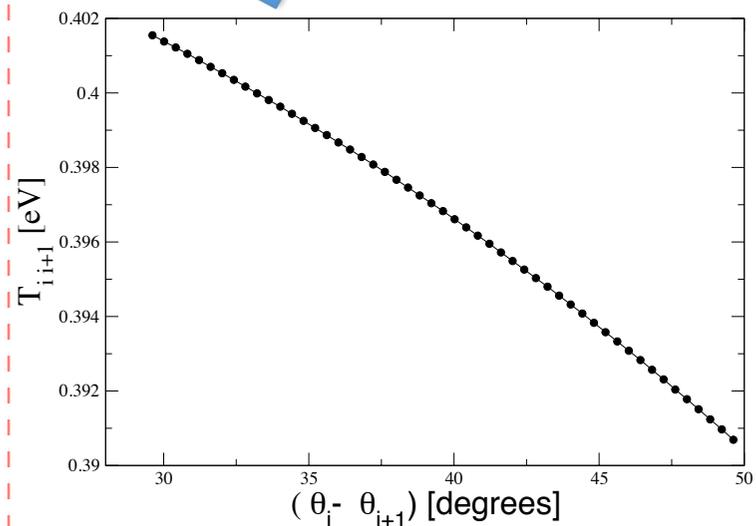
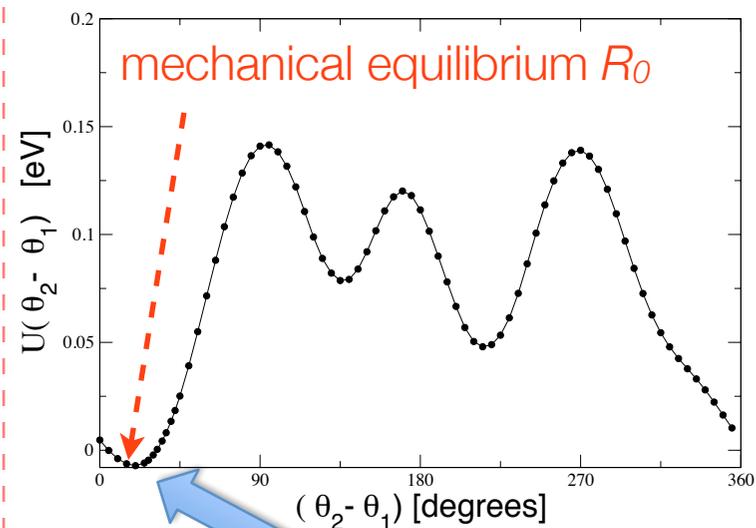


Molecular dynamics of atomic nuclei => Langevin dynamics

# Ingredients from quantum chemistry calculations



DFT-B  
density functional theory



# Quantum Monte Carlo

---

$$Z[\eta, \bar{\eta}] = \int \mathcal{D}\delta Q e^{-(S_{OM}[\delta Q] + \text{Log Det} G_{\delta Q}^{-1})} e^{\frac{i}{\hbar} \sum_{mn} \int_0^t d\tau \bar{\eta}_n(\tau) G_{\delta Q}(n, \tau | m, \tau') \eta_m(\tau')}$$

1) **Sample** nuclear trajectories by integrating the Langevin equation:

$$S_{OM}[\Delta Q] = \frac{\beta}{4M\gamma} \int_0^t d\tau \left( M\delta\ddot{Q} + \gamma\delta\dot{Q} + \nabla U(\delta Q) \right)^2$$

2) **Re-weigh** configurations (quantum backaction):

$$\text{log Det} G_{\Delta Q}^{-1} = \frac{1}{2} \sum_{s \neq t} C_{st}^i C_{ts}^j \int_0^t d\tau \int_0^t d\tau' \delta q^i(\tau) \delta q^j(\tau') \times \cos \left[ (\tau - \tau') \frac{(E_s - E_t)}{\hbar} \right].$$

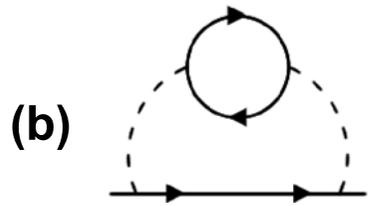
3) **Compute** Quantum propagator (and then use Wick theorem!)

$$G_{\delta Q}(n, \tau | m, \tau') = \frac{\int \mathcal{D}\bar{\psi} \mathcal{D}\psi \psi_n(\tau) \bar{\psi}_m(\tau') e^{\frac{i}{\hbar} (S_0[\psi, \bar{\psi}] + S_{int}[\psi, \bar{\psi}, \delta Q])}}{\int \mathcal{D}\bar{\psi} \mathcal{D}\psi e^{\frac{i}{\hbar} (S_0[\psi, \bar{\psi}] + S_{int}[\psi, \bar{\psi}, \delta Q])}}$$

# Non-Perturbative Method 2: Dynamical mean-field approximation:

---

(a) 

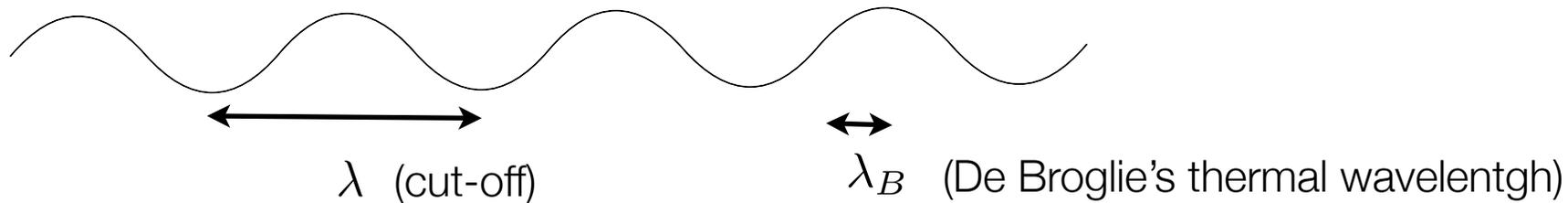


(c) 

Analytic (or semi-analytic) expression for green's functions!

# Non-Perturbative Method 3: Effective Field Theory

Use **Renormalization Group** formalism to perform **coarse-graining** and lower the time & spatial-resolution power. Obtain an **effective theory** which yields the same results in the long-time long-distance limit:



from the microscopic theory we get

$$P(\mathbf{y}, t | \mathbf{x}, 0) \simeq \int_{\mathbf{x}} \mathcal{D}\mathbf{R} e^{-\int_0^t dT \left[ \frac{1}{4D_2^b} \dot{\mathbf{R}}^2 + \left( \frac{\lambda_B}{\lambda} \right)^2 C_4^b \dot{\mathbf{R}}^4 + \dots \right]}$$

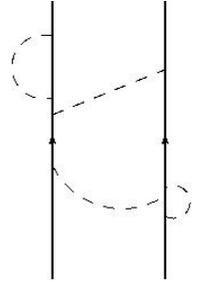
$\dots = \mathcal{O} \left( \frac{\lambda_B}{\lambda} \right)^2$

where  $\mathbf{A} \cdot \mathbf{B} = \sum_{ij} g_{ij} A_i B_j$

quantum correction  
terms

# Different sectors of the density matrix for different physics ...

$$\rho = \begin{pmatrix} \rho_{gg} & \rho_{ge_1} & \cdots & \rho_{ge_N} & \rho_{g\alpha_1} & \cdots & \rho_{g\alpha_{N_2}} \\ \rho_{e_1g} & \rho_{e_1e_1} & \cdots & \rho_{e_1e_N} & \rho_{e_1\alpha_1} & \cdots & \rho_{e_1\alpha_{N_2}} \\ \vdots & \vdots & \ddots & \vdots & \vdots & \ddots & \vdots \\ \rho_{e_Ng} & \rho_{e_Ne_1} & \cdots & \rho_{e_Ne_N} & \rho_{e_N\alpha_1} & \cdots & \rho_{e_N\alpha_{N_2}} \\ \rho_{\alpha_1g} & \rho_{\alpha_1e_1} & \cdots & \rho_{\alpha_1e_N} & \rho_{\alpha_1\alpha_1} & \cdots & \rho_{\alpha_1\alpha_{N_2}} \\ \vdots & \vdots & \ddots & \vdots & \vdots & \ddots & \vdots \\ \rho_{\alpha_{N_2}g} & \rho_{\alpha_{N_2}e_1} & \cdots & \rho_{\alpha_{N_2}e_N} & \rho_{\alpha_{N_2}\alpha_1} & \cdots & \rho_{\alpha_{N_2}\alpha_{N_2}} \end{pmatrix}$$



exciton/hole mobility  $\rho_{e_k e_l}(t) \propto \int \mathcal{D}\delta R \int \mathcal{D}\psi \mathcal{D}\bar{\psi} e^{iS_{tot}} \bar{\psi}(e_l, t) \gamma_- \gamma_5 \psi(e_k, t) \bar{\psi}(e_n, 0) \gamma_+ \gamma_5 \psi(e_m, 0)$

# Diffusion of a quantum excitation:

---

The analytic solution (after renormalization):

$$\bar{P}(\mathbf{y}, t | \mathbf{x}, 0) \simeq P_0(\mathbf{y}, t | \mathbf{x}, 0; D_{ren}) \times \left[ 1 - C_{ren} \left( \frac{(\mathbf{y} - \mathbf{x})^4}{t^3 D_{ren}} - 20 \frac{(\mathbf{y} - \mathbf{x})^2}{t^2} + \frac{60 D_{ren}}{t} \right) \right].$$

diffusion of quantum excitation

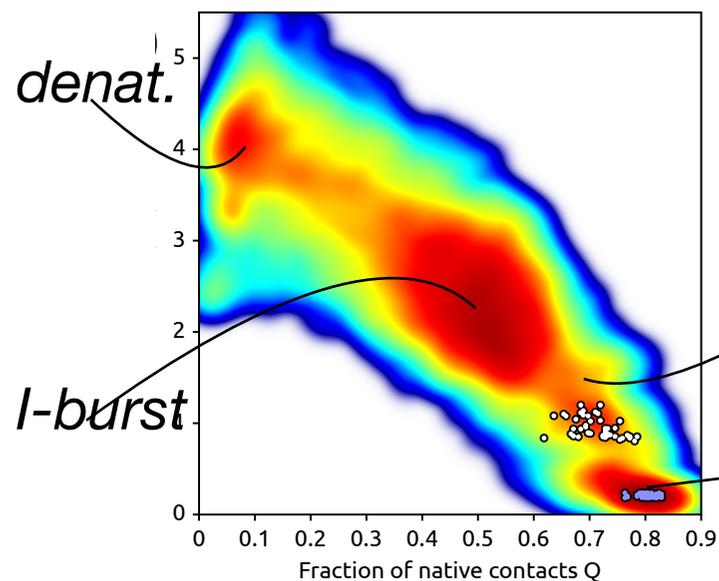
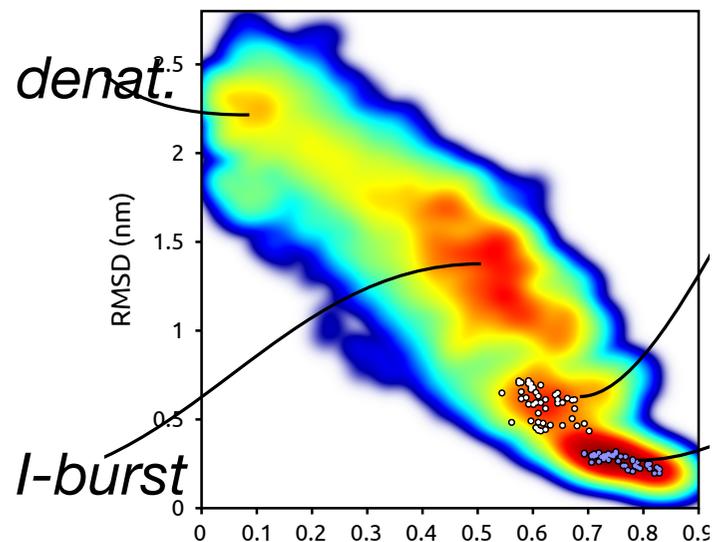
quantum correction terms

Renormalized constants, to be determined from experiments or micr. sim.s

# How sensitive is this probe?

Remove the disulfide bridges:

Cys30–Cys115, Cys127–Cys6, Cys94–Cys76 Cys65–Cys80

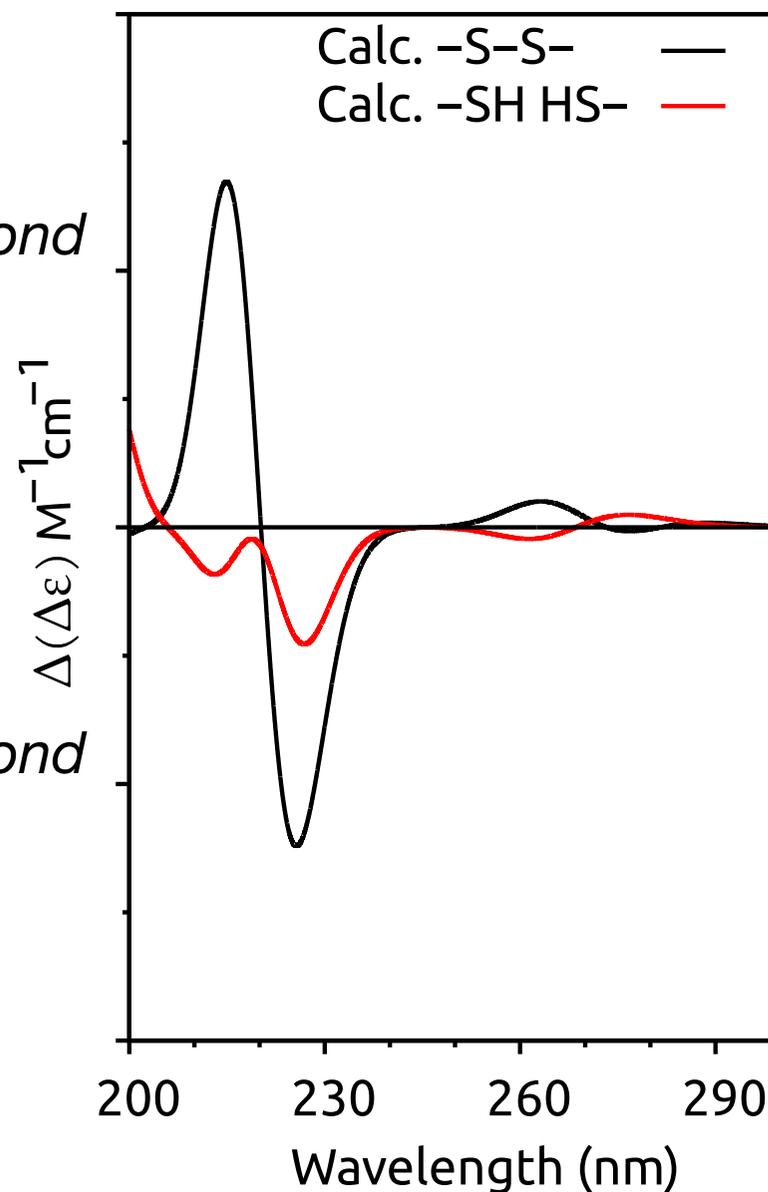


*I-second*

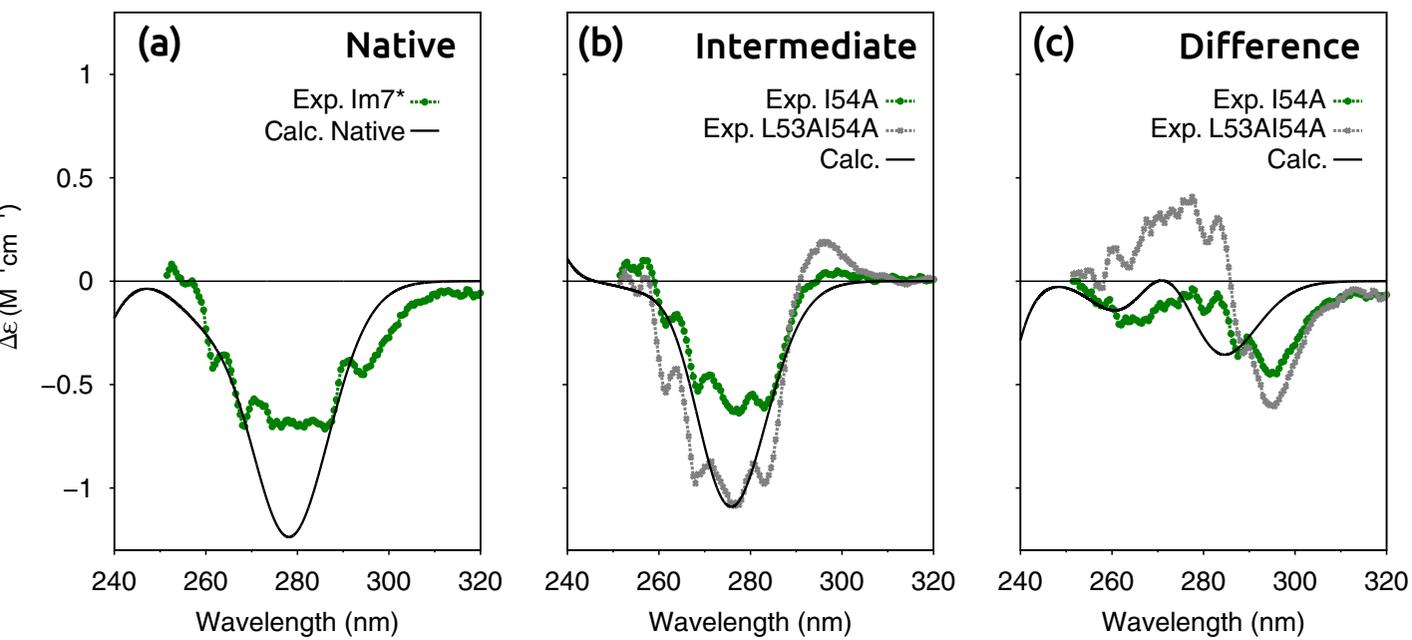
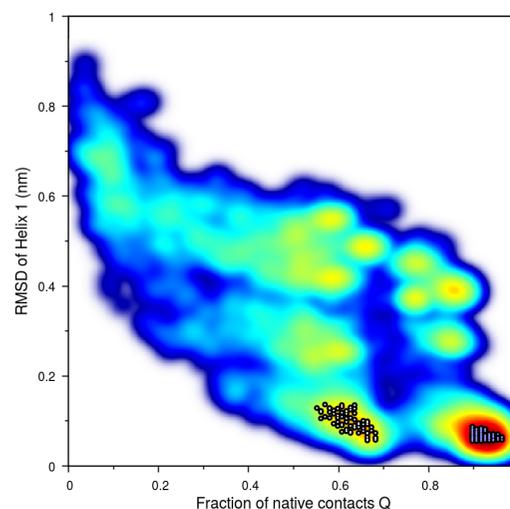
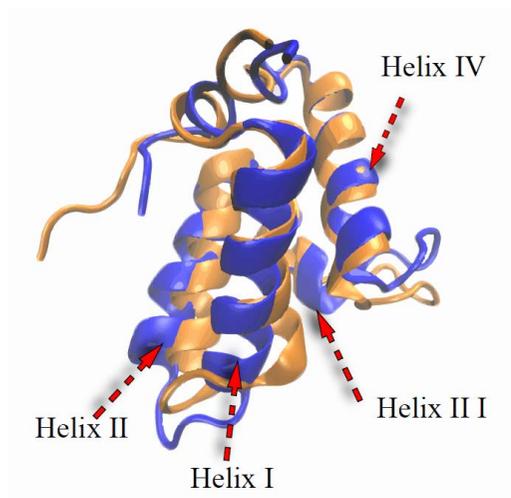
Native

*I-second*

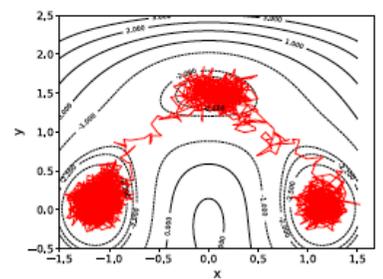
Native



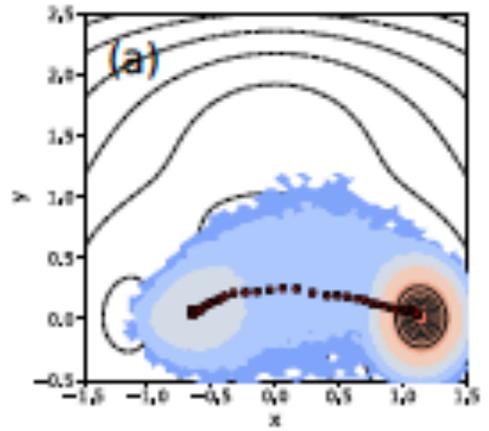
# Folding of protein Im7



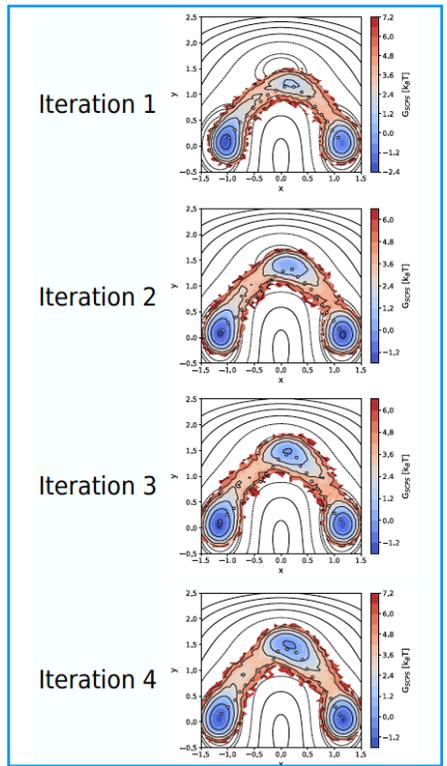
# Illustrative example:



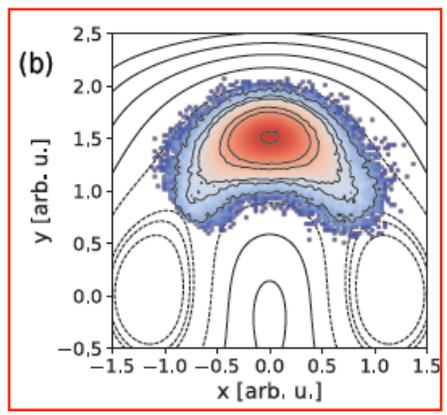
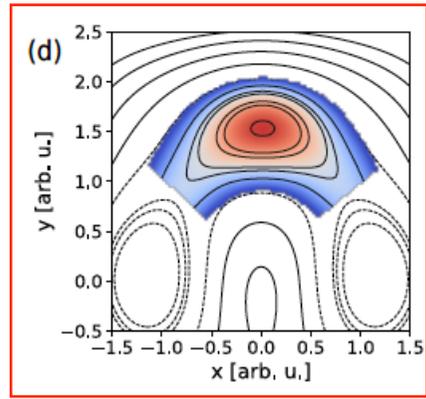
Plain steering



SCPS

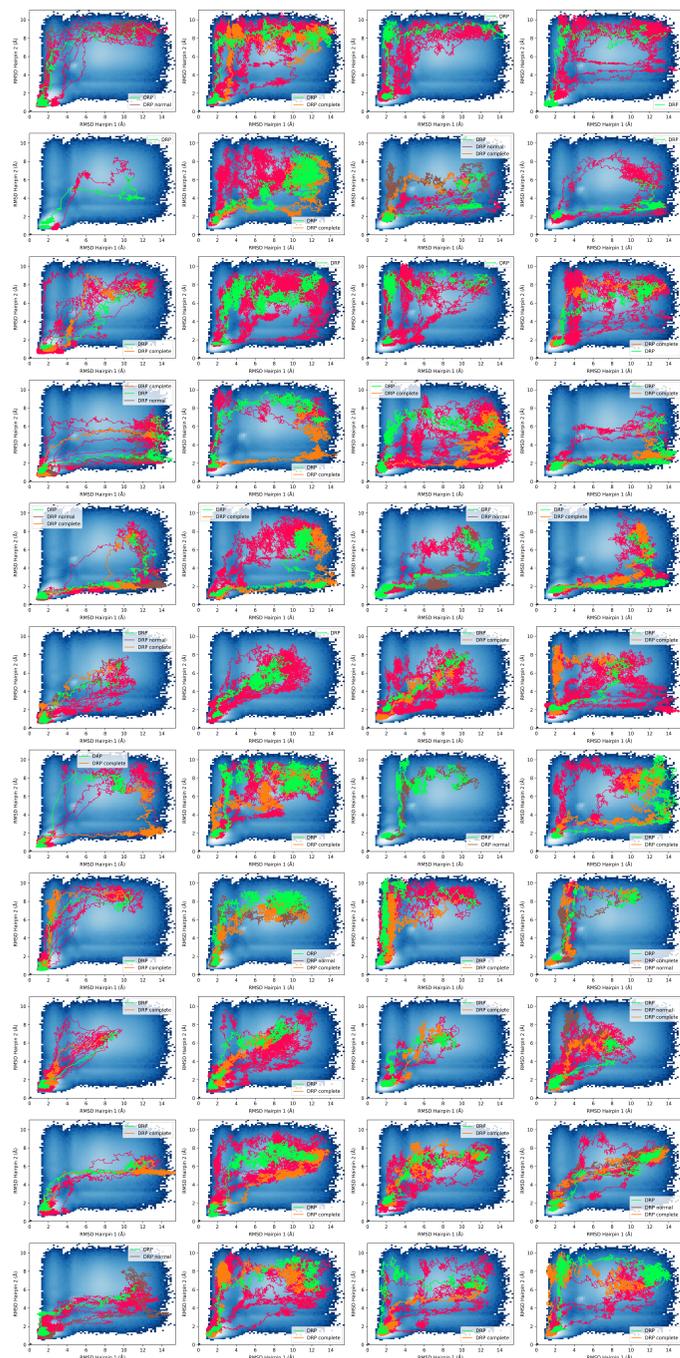


Exact (plain MD)



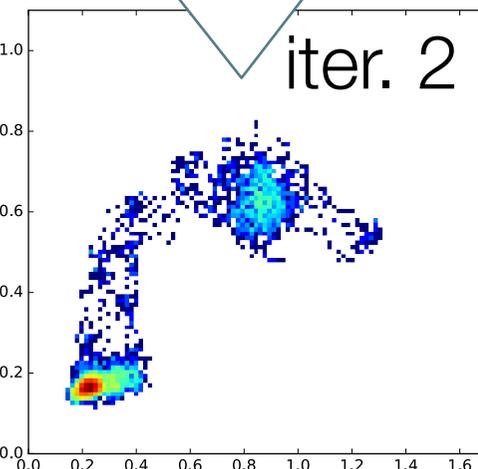
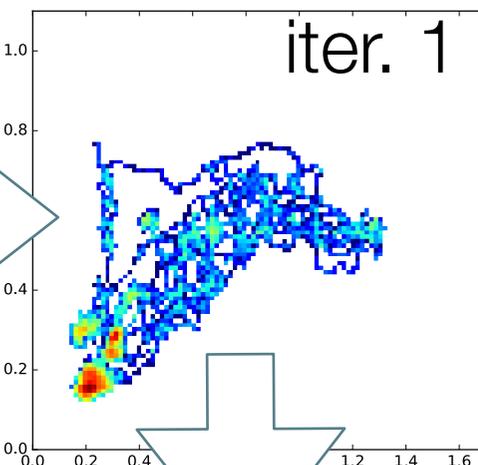
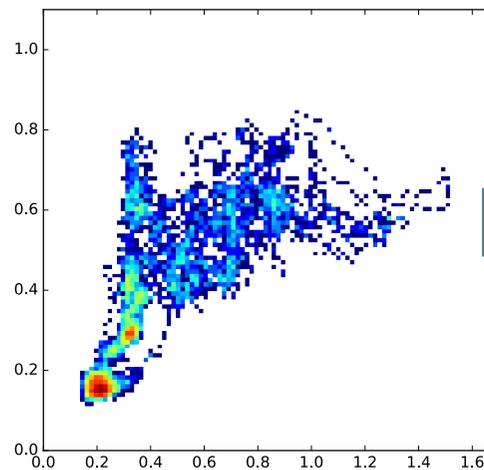
# Typical calculation

Initial conditions

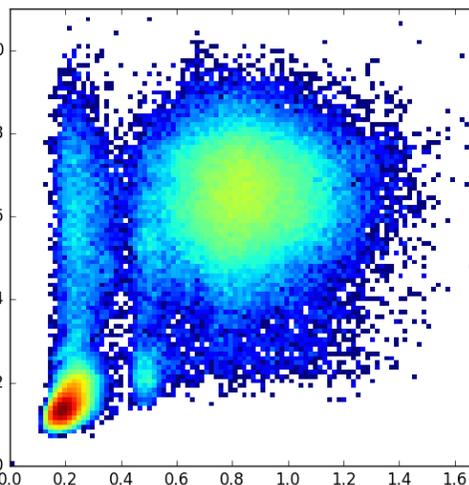


SCPS iterations

## Initial guess of RC



RMSD hairpin 2



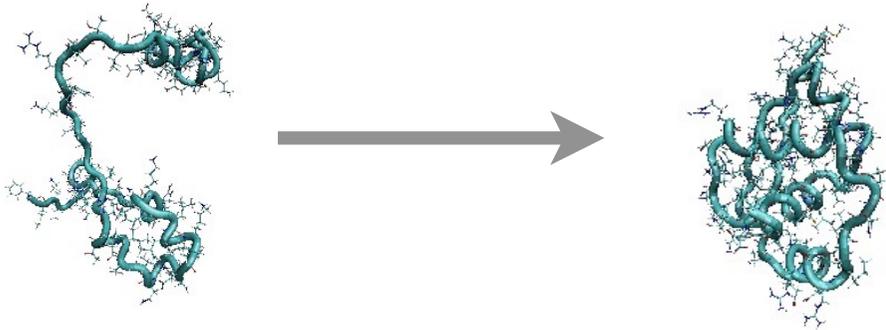
RMSD hairpin 1



# What would we like to know?

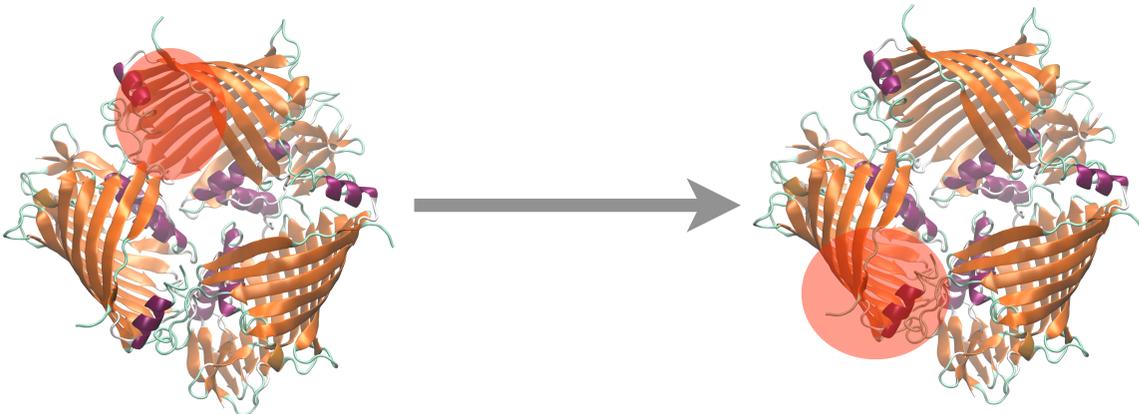
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Conformational dynamics:



(adiabatic)

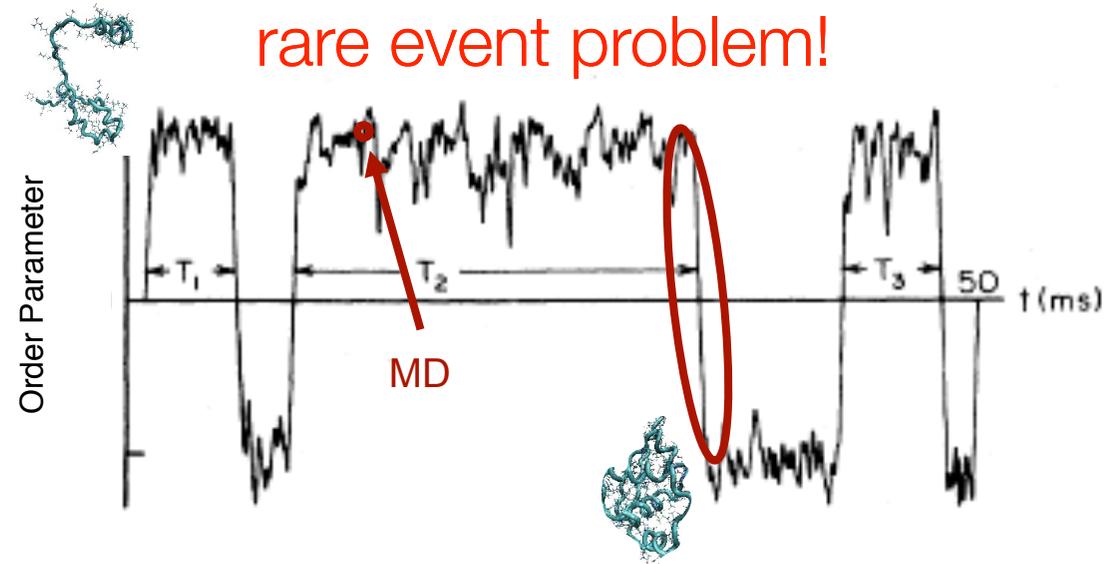
Exciton dynamics:



(non-adiabatic)

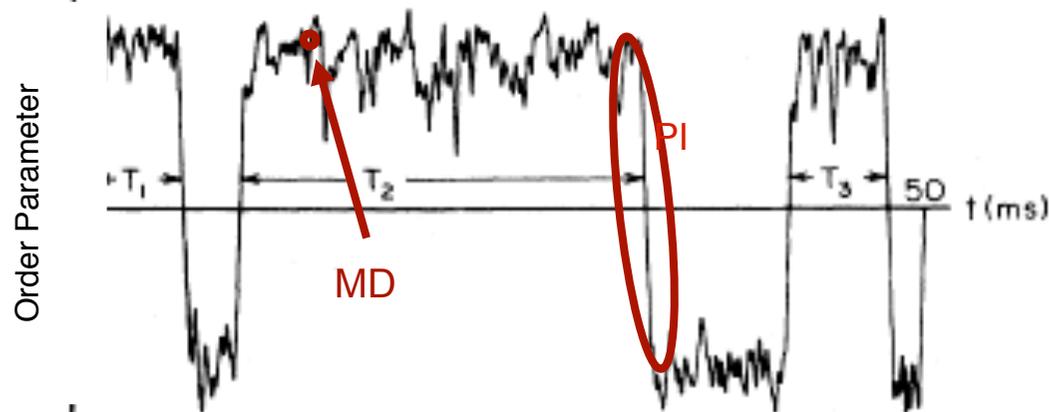
# What are the main theoretical challenges?

Conformational dynamics:



Excitons' dynamics:

Non-equilibrium open quantum system



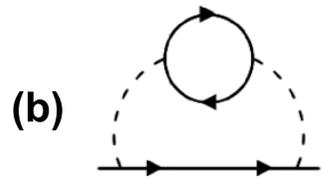
$$k_B, \hbar, t$$

# Dynamical Mean Field Approximation

---

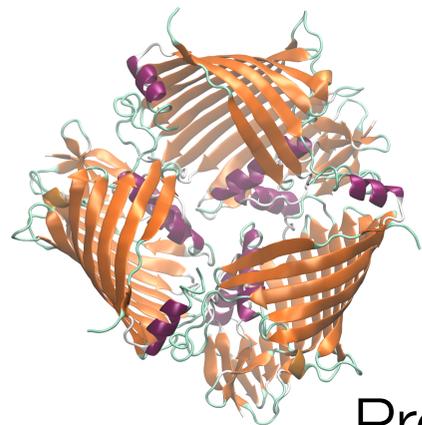
(a) 

$$\mathbf{G} = \frac{G_0}{1 - G_0 \Sigma}$$

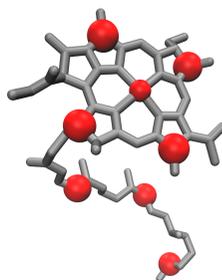


In general: Dyson-Schwinger equations

# Linear Absorption of Fenna Matthews Olson complex



Protein scaffold



Chlorophyll

Linear Response theory:

$$\kappa_a(\omega) = \frac{4\pi\omega}{n(\omega)} \text{Im}[R^{(1)}(\omega)],$$

Using MQFT

$$R^{(1)}(t) = \frac{i}{\hbar} \sum_{n=1}^N \frac{|\mu_{ng}|^2}{Z(t)} \int \mathcal{D}\delta Q e^{-S_{OM}[\delta Q] - S_{back}[\delta Q] - \beta H_Q(0)} \times [G_{\delta Q}^f(n, t|n, 0) - G_{\delta Q}^b(n, 0|n, t)].$$

We need to compute dressed exciton propagator

## Microscopic calculation of absorption spectra of macromolecules: An analytic approach

Cite as: J. Chem. Phys. 150, 144103 (2019); doi: 10.1063/1.5084120

Submitted: 4 December 2018 • Accepted: 14 March 2019 •

Published Online: 8 April 2019



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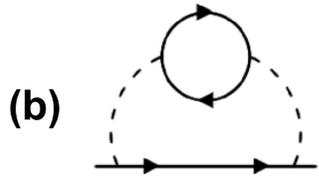
Export Citation

Matteo Carli,<sup>1,2</sup> Michele Turelli,<sup>1,3</sup> and Pietro Faccioli<sup>1,3,a)</sup> 

# Dynamical Mean Field Approximation

(a) 

$$\mathbf{G} = \frac{G_0}{1 - G_0 \Sigma}$$

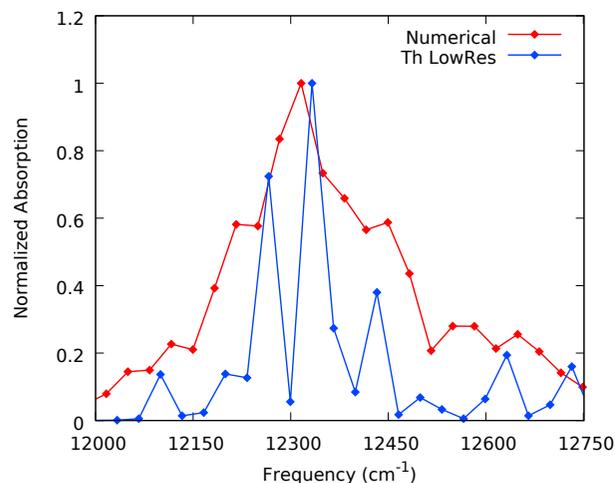
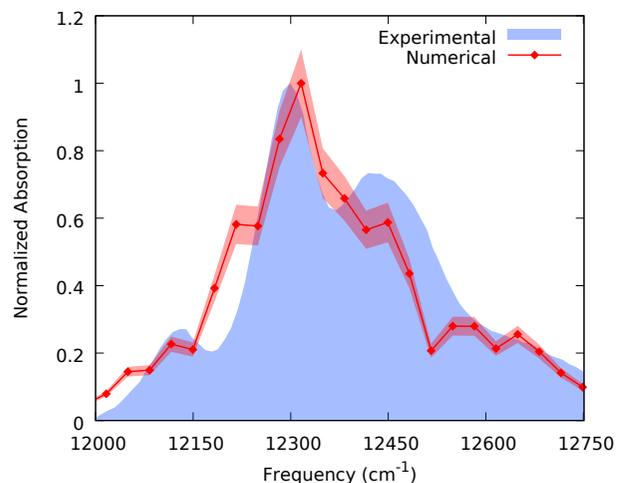


$$\text{Im}R(\omega) = - \sum_n \frac{2\text{Re}\Sigma_n^f(\omega) \left( (\omega - E_n)^2 + |\Sigma_n^f(\omega)|^2 \right)}{\left( (\omega - E_n)^2 - |\Sigma_n^f(\omega)|^2 \right)^2 + 4 \left( (\omega - E_n) \text{Re}\Sigma_n^f(\omega) \right)^2}$$

$$\Sigma_{nm}^{f/b}(\omega) \simeq \frac{f_{nm'}^l U_{lj'}^\dagger V_{m's}^\dagger [i(E_s - \omega) \pm \gamma] V_{sn'} U_{j'h} f_{n'm}^h}{\beta M \Omega_{j'}^2 [\Omega_{j'}^2 - (E_s - \omega)(E_s \mp i\gamma - \omega)]}$$

# Comparing MC and DMFA results against exper.

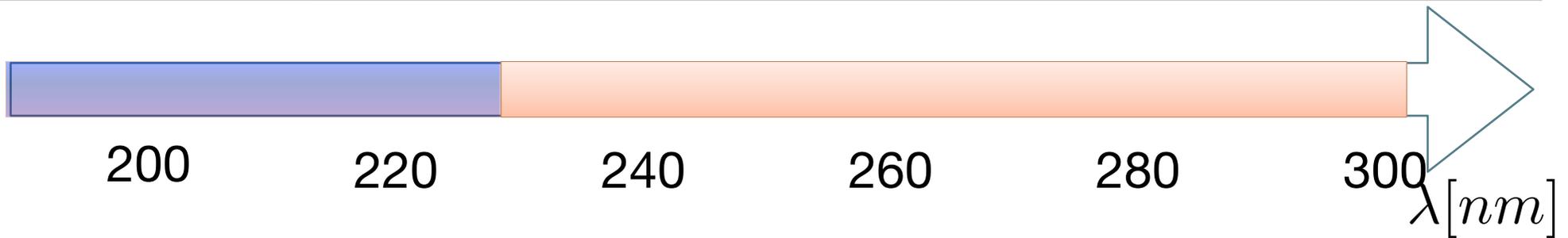
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How differences in the molecular vibrational normal modes, both temperature and viscosity can affect the spectrum

Gateway to rationale to design macromolecules with specific optical properties?

# Example: Time resolved **NEAR UV** CD

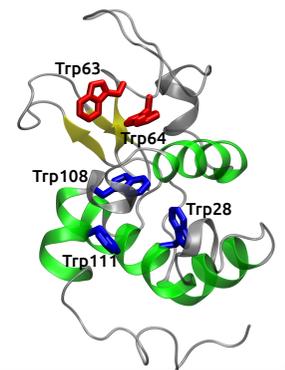
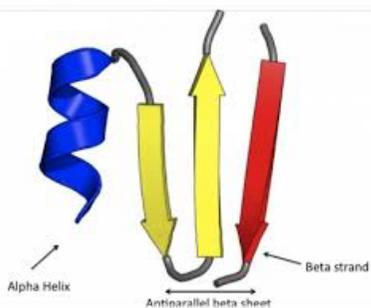


## Far UV regime:

signal dominated by secondary structures

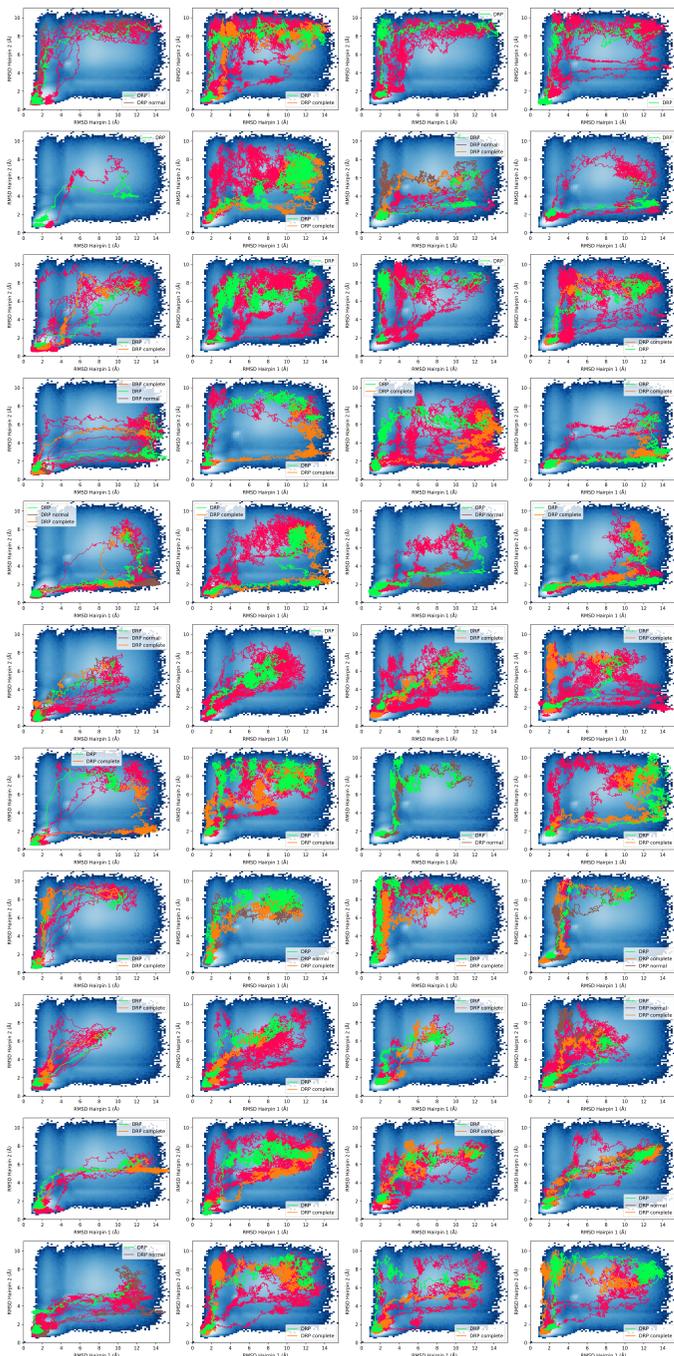
## Near UV regime:

signal dominated by the coupling between  $\pi$ - $\pi^*$  excitations in aromatic residues



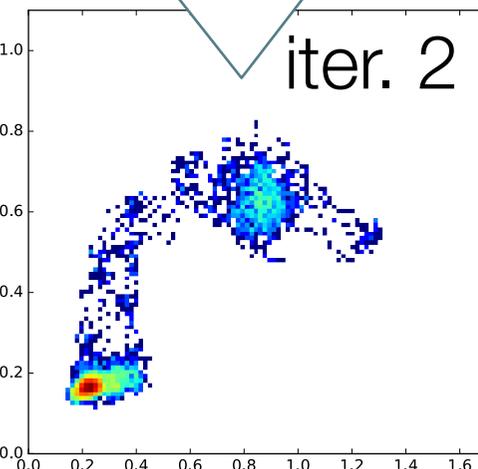
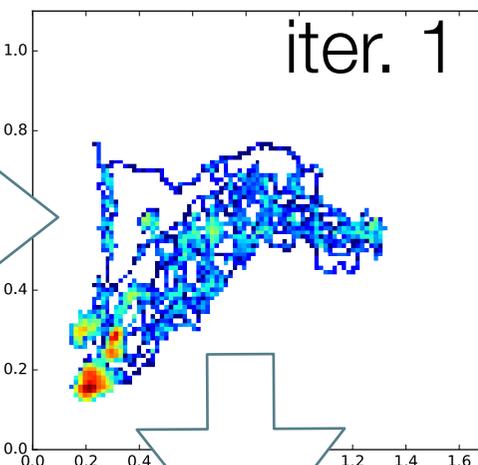
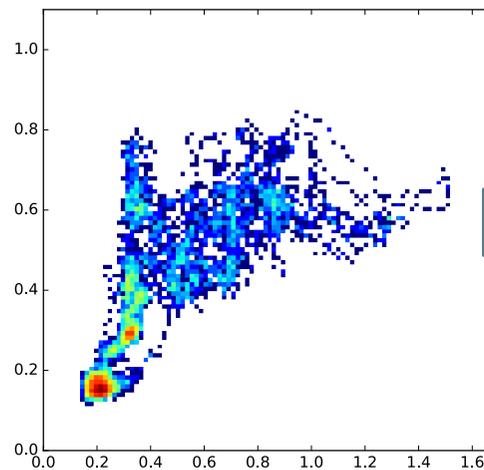
# Typical calculation

Initial conditions

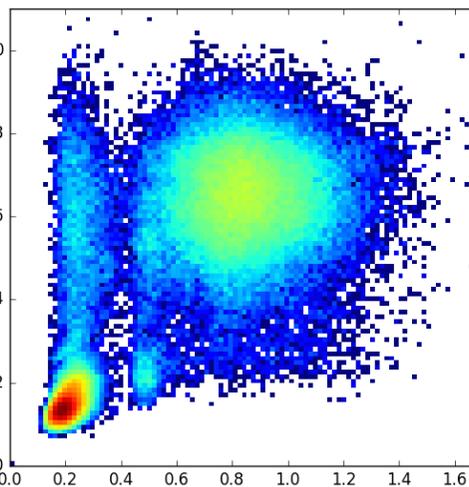


SCPS iterations

## Initial guess of RC



RMSD hairpin 2



RMSD hairpin 1



# Theoretical foundation

- Formal derivation of SCPS from Langevin dynamics

THE JOURNAL OF CHEMICAL PHYSICS **147**, 064108 (2017)

## Self-consistent calculation of protein folding pathways

S. Orioli, S. a Beccara, and P. Faccioli<sup>a)</sup>

- Calculation of the committor function and TPT distributions from SCPS

THE JOURNAL OF CHEMICAL PHYSICS **149**, 072336 (2018)

## Transition path theory from biased simulations

G. Bartolucci,<sup>1</sup> S. Orioli,<sup>1,2</sup> and P. Faccioli<sup>1,2</sup>

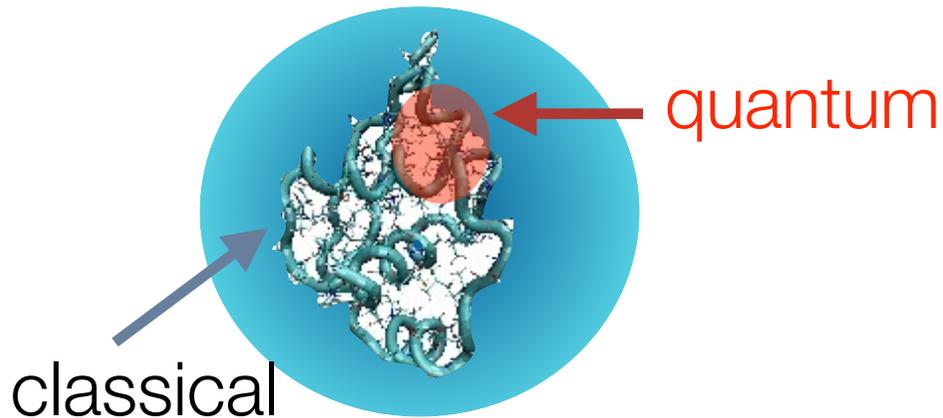
# Connections with other approaches

- Self-consistent calculations of tube variables are explored also by **Ensing et al.** within *meta-dynamics*
- SCPS may be viewed as a dynamical variant of the **string method**, which can be applied to reactions as complex as protein folding

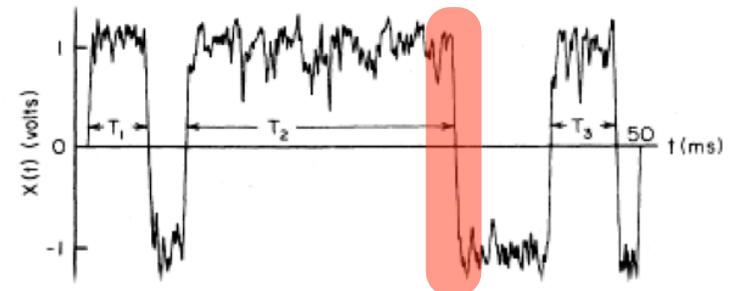
# WHY PATH INTEGRALS?

Advantages

Theoretical



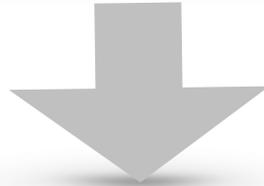
Computational



# A USEFUL DUALITY

---

Quantum open dynamics



Quantum "relativistic"  
dynamics

REDUCED  
DENSITY MATRIX

quantum excitations

$$\psi_n(t), \bar{\psi}_n(t)$$

nuclear coords

$$R_i(t)$$

N-POINT FUNCTIONS  
OF MQFT

"matter fields"

$$\psi(x, t), \bar{\psi}(x, t)$$

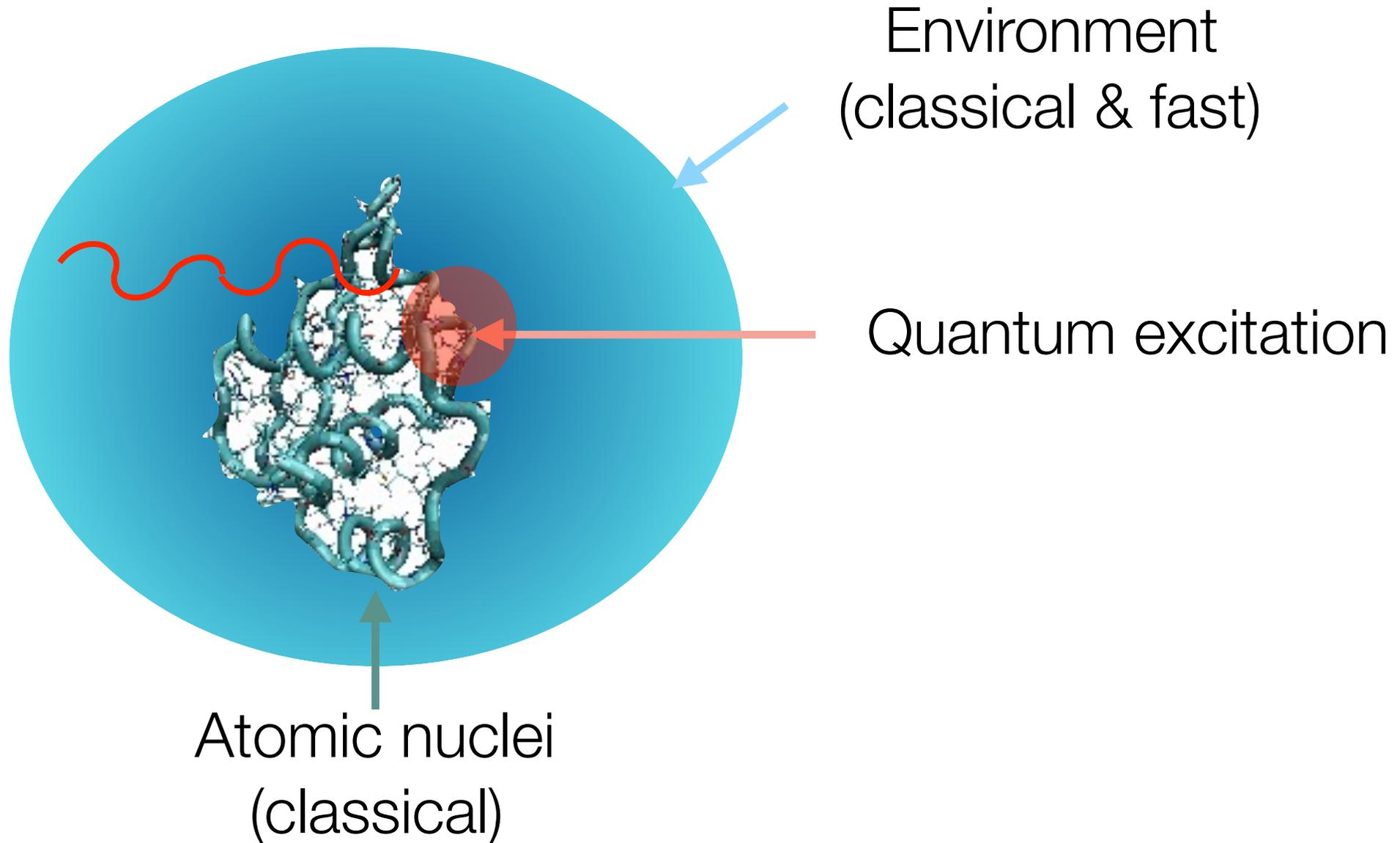
"gauge bosons"

$$A_\mu(x, t)$$

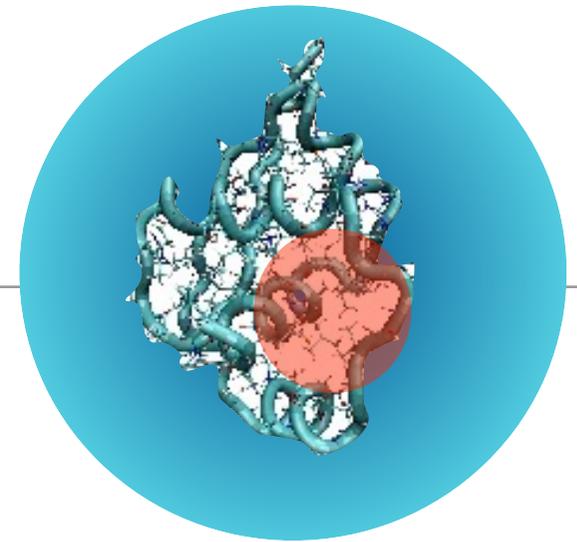


# MODEL DEFINITION

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# FULLY QUANTUM HAMILTONIAN



$$\hat{H}_{tot} = \hat{H}_{BO} + \hat{H}_{bath} + \hat{H}_{ex.}$$

$$\hat{H}_{BO} = \sum_i \frac{\hat{\mathbf{p}}_i^2}{2m_i} + U_{BO}(\mathbf{q}_1, \dots, \mathbf{q}_N)$$

Adiabatic dynamics

$$\hat{H}_{bath} = \sum_{i=1}^{3N} \sum_{\alpha=1}^{\infty} \left( \frac{\hat{\pi}_{\alpha}^2}{2\mu_{\alpha}} + \frac{1}{2} \mu_{\alpha} \omega_{\alpha}^2 \hat{x}_{\alpha}^2 - c_{\alpha} \hat{x}_{\alpha} \hat{q}_i + \frac{c_{\alpha}^2}{2\mu_{\alpha} \omega_{\alpha}^2} \hat{q}_{\alpha}^2 \right).$$

Ohmic bath

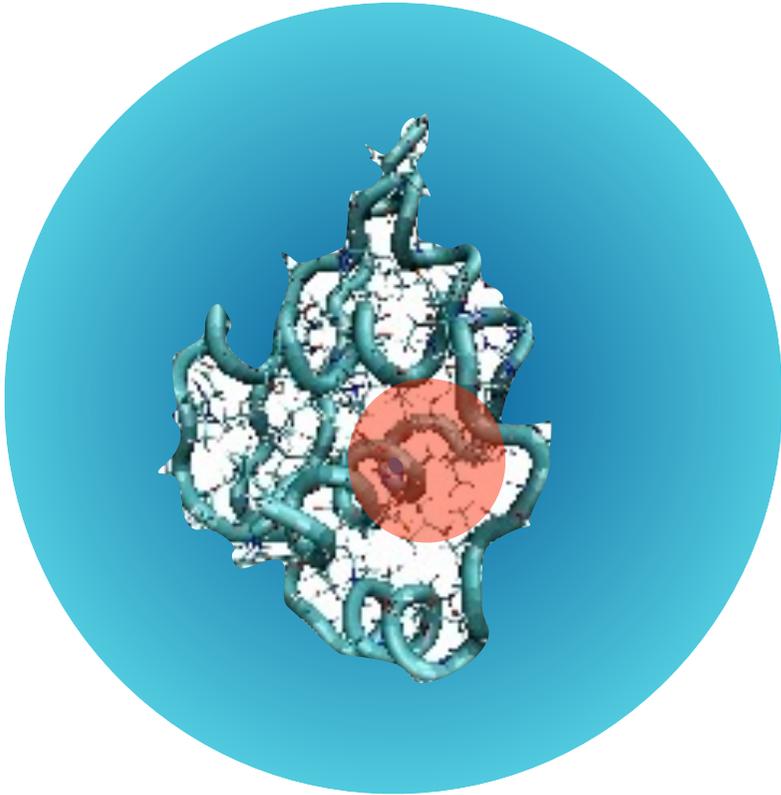
$$\hat{H}_{ex.} = \sum_s \sum_{mn} f_{mn}[Q] \hat{a}_{m,s}^{\dagger} \hat{a}_{n,s}$$

↑  
 $\langle \phi_m | \hat{\mathcal{H}}_{el} | \phi_n \rangle,$

Non-adiabatic dynamics

# DYNAMICS IN OPEN SYSTEMS

---

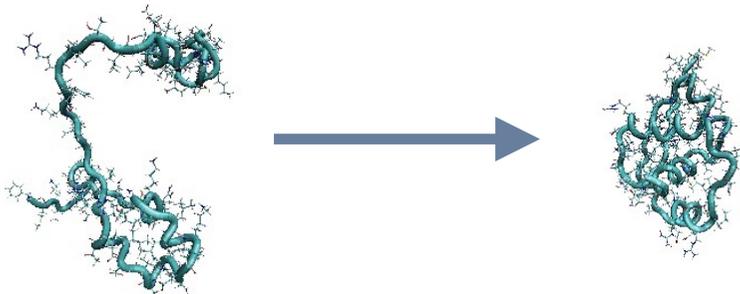


$$\hat{\rho}(t_0) \rightarrow \hat{\rho}(t)$$

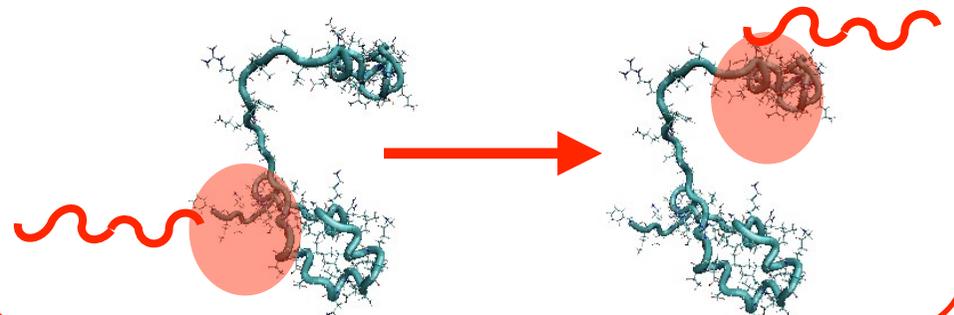
# DYNAMICS IN OPEN SYSTEMS

$$\hat{\rho}(t) = \begin{pmatrix} \rho_{gg} & \rho_{ge_1} & \cdots & \rho_{ge_N} & \rho_{g\alpha_1} & \cdots & \rho_{g\alpha_{N_2}} \\ \rho_{e_1g} & \rho_{e_1e_1} & \cdots & \rho_{e_1e_N} & \rho_{e_1\alpha_1} & \cdots & \rho_{e_1\alpha_{N_2}} \\ \vdots & \vdots & \ddots & \vdots & \vdots & \ddots & \vdots \\ \rho_{e_Ng} & \rho_{e_Ne_1} & \cdots & \rho_{e_Ne_N} & \rho_{e_N\alpha_1} & \cdots & \rho_{e_N\alpha_{N_2}} \\ \rho_{\alpha_1g} & \rho_{\alpha_1e_1} & \cdots & \rho_{\alpha_1e_N} & \rho_{\alpha_1\alpha_1} & \cdots & \rho_{\alpha_1\alpha_{N_2}} \\ \vdots & \vdots & \ddots & \vdots & \vdots & \ddots & \vdots \\ \rho_{\alpha_{N_2}g} & \rho_{\alpha_{N_2}e_1} & \cdots & \rho_{\alpha_{N_2}e_N} & \rho_{\alpha_{N_2}\alpha_1} & \cdots & \rho_{\alpha_{N_2}\alpha_{N_2}} \end{pmatrix}$$

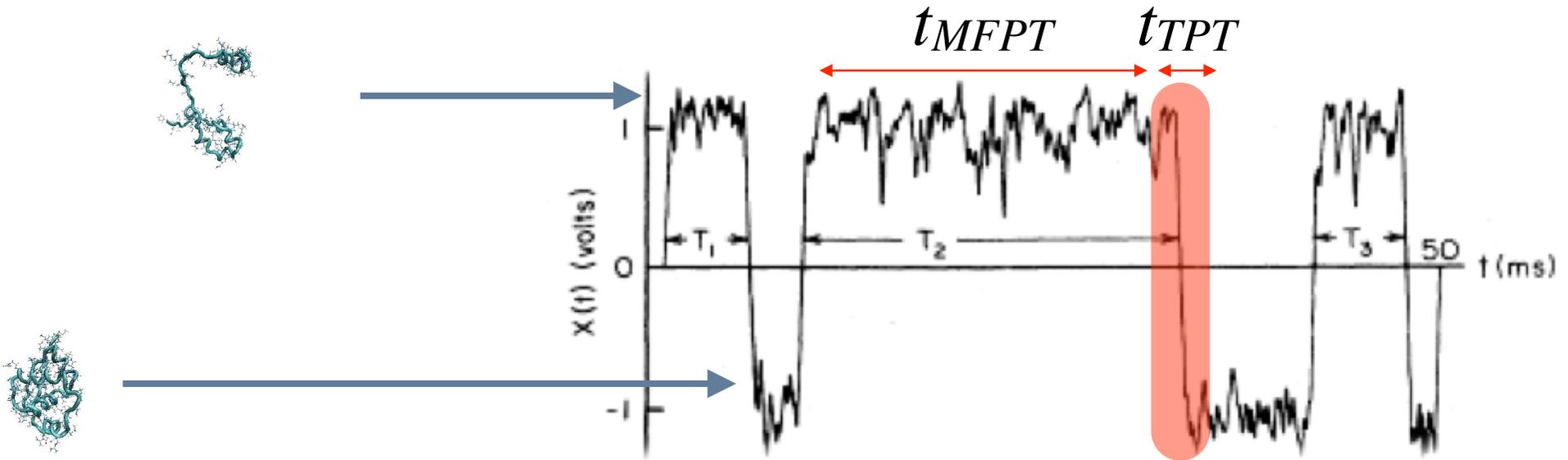
Classical structural dynamics:



Quantum electro-dynamics:



# THERMAL ACTIVATION AND RARE EVENTS

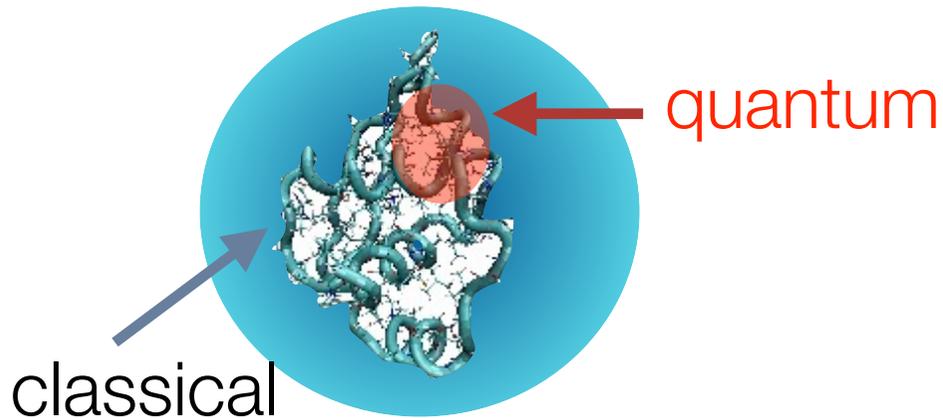


$$t_{TPT} \sim \tau_0 \log \left[ \log \left( \frac{t_{MFPT}}{\tau_0} \right) \right]$$

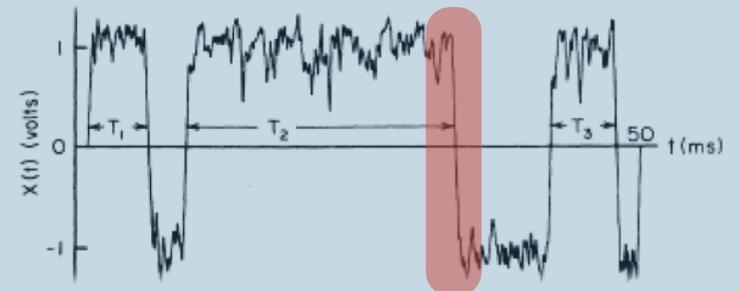
# WHY PATH INTEGRALS?

Advantages

Theoretical



Computational



# INSTANTON THEORY OF CONFORMATIONAL TRANSITIONS

---

Thermal activation:  $k_B T > 0$

$$P(x_f, t | x_i) = \frac{e^{-\frac{1}{2k_B T} U(x_f)}}{e^{-\frac{1}{2k_B T} U(x_i)}} \int_{x_i}^{x_f} \mathcal{D}Q e^{-\frac{1}{k_B T} \int_0^t d\tau \left( \frac{M\gamma}{4} \dot{Q}^2 + V_{eff}(Q) \right)}$$

Quantum Tunneling:  $\hbar > 0$

$$K(x_f, t | x_i) = \int_{x_i}^{x_f} \mathcal{D}Q e^{-\frac{1}{\hbar} \int_0^t d\tau \left( \frac{m}{2} \dot{Q}^2 + U(Q) \right)}$$

# STRUCTURAL DYNAMICS IN PATH INTEGRAL FORM

$$\rho = \begin{pmatrix} \rho_{gg} & \rho_{ge_1} & \cdots & \rho_{ge_N} & \rho_{g\alpha_1} & \cdots & \rho_{g\alpha_{N_2}} \\ \rho_{e_1g} & \rho_{e_1e_1} & \cdots & \rho_{e_1e_N} & \rho_{e_1\alpha_1} & \cdots & \rho_{e_1\alpha_{N_2}} \\ \vdots & \vdots & \ddots & \vdots & \vdots & \ddots & \vdots \\ \rho_{e_Ng} & \rho_{e_Ne_1} & \cdots & \rho_{e_Ne_N} & \rho_{e_N\alpha_1} & \cdots & \rho_{e_N\alpha_{N_2}} \\ \rho_{\alpha_1g} & \rho_{\alpha_1e_1} & \cdots & \rho_{\alpha_1e_N} & \rho_{\alpha_1\alpha_1} & \cdots & \rho_{\alpha_1\alpha_{N_2}} \\ \vdots & \vdots & \ddots & \vdots & \vdots & \ddots & \vdots \\ \rho_{\alpha_{N_2}g} & \rho_{\alpha_{N_2}e_1} & \cdots & \rho_{\alpha_{N_2}e_N} & \rho_{\alpha_{N_2}\alpha_1} & \cdots & \rho_{\alpha_{N_2}\alpha_{N_2}} \end{pmatrix}$$



$$P(R_f, t | R_i, 0) = \int_{R_i}^{R_f} \mathcal{D}R e^{-\frac{\beta}{4m\gamma} \int_0^t d\tau (m\ddot{R} + m\gamma\dot{R} + \nabla U)^2}$$

Langevin dynamics:  $M\ddot{R} = -\gamma M\dot{R} - \nabla U(R) + \eta$

# DENSITY MATRIX IN MQFT

$$\rho = \begin{pmatrix} \rho_{gg} & \rho_{ge_1} & \cdots & \rho_{ge_N} & \rho_{g\alpha_1} & \cdots & \rho_{g\alpha_{N_2}} \\ \rho_{e_1g} & \rho_{e_1e_1} & \cdots & \rho_{e_1e_N} & \rho_{e_1\alpha_1} & \cdots & \rho_{e_1\alpha_{N_2}} \\ \vdots & \vdots & \ddots & \vdots & \vdots & \ddots & \vdots \\ \rho_{e_Ng} & \rho_{e_Ne_1} & \cdots & \rho_{e_Ne_N} & \rho_{e_N\alpha_1} & \cdots & \rho_{e_N\alpha_{N_2}} \\ \rho_{\alpha_1g} & \rho_{\alpha_1e_1} & \cdots & \rho_{\alpha_1e_N} & \rho_{\alpha_1\alpha_1} & \cdots & \rho_{\alpha_1\alpha_{N_2}} \\ \vdots & \vdots & \ddots & \vdots & \vdots & \ddots & \vdots \\ \rho_{\alpha_{N_2}g} & \rho_{\alpha_{N_2}e_1} & \cdots & \rho_{\alpha_{N_2}e_N} & \rho_{\alpha_{N_2}\alpha_1} & \cdots & \rho_{\alpha_{N_2}\alpha_{N_2}} \end{pmatrix}$$

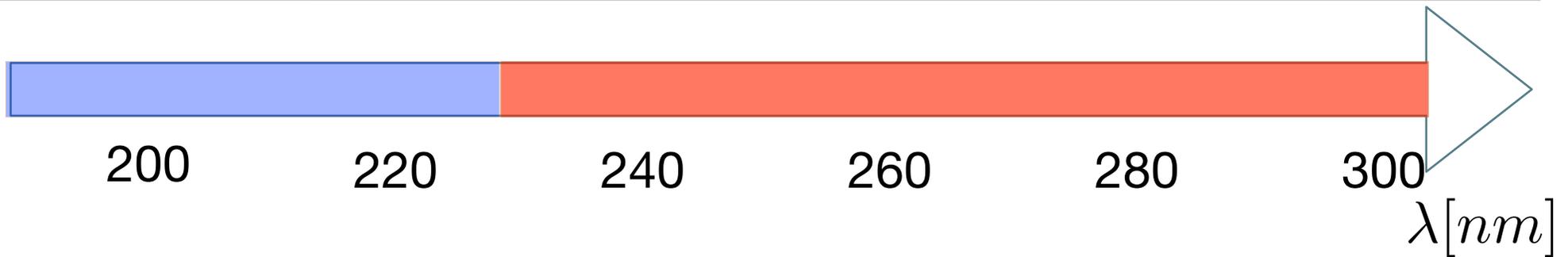
Structural dynamics  $\rho_{gg} \propto \int DRe^{-S_{OM}[R]}$

Linear Spectroscopy:  $\rho_{e_kg}(t) \propto \int \mathcal{D}\delta R \int \mathcal{D}\psi \mathcal{D}\bar{\psi} e^{iS_{tot}} \psi(e_l, t) \bar{\psi}(e_n, 0)$

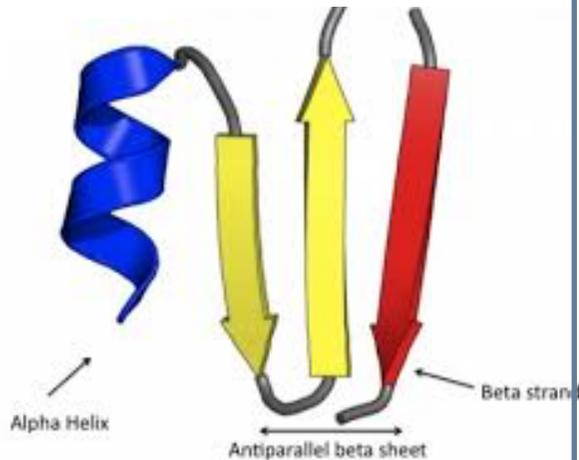
Mobility:  $\rho_{e_ke_l}(t) \propto \int \mathcal{D}\delta R \int \mathcal{D}\psi \mathcal{D}\bar{\psi} e^{iS_{tot}} \bar{\psi}(e_l, t) \gamma_- \gamma_5 \psi(e_k, t) \bar{\psi}(e_n, 0) \gamma_+ \gamma_5 \psi(e_m, 0)$

Non-linear spectroscopy: .....

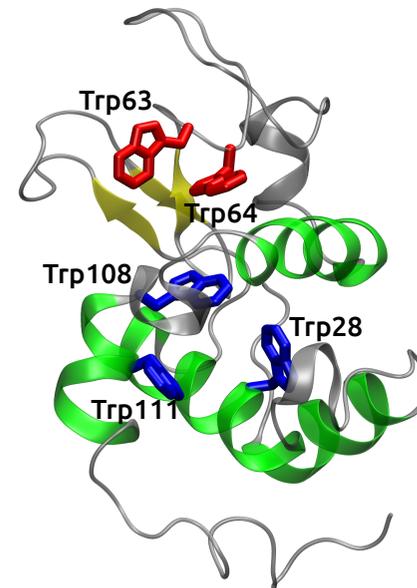
# TIME RESOLVED NEAR UV CIRCULAR DICHROISM



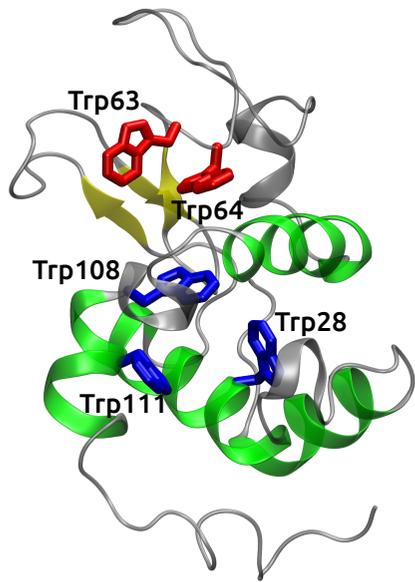
Far UV regime:



Near UV regime:



# EXISTING EXPERIMENTS

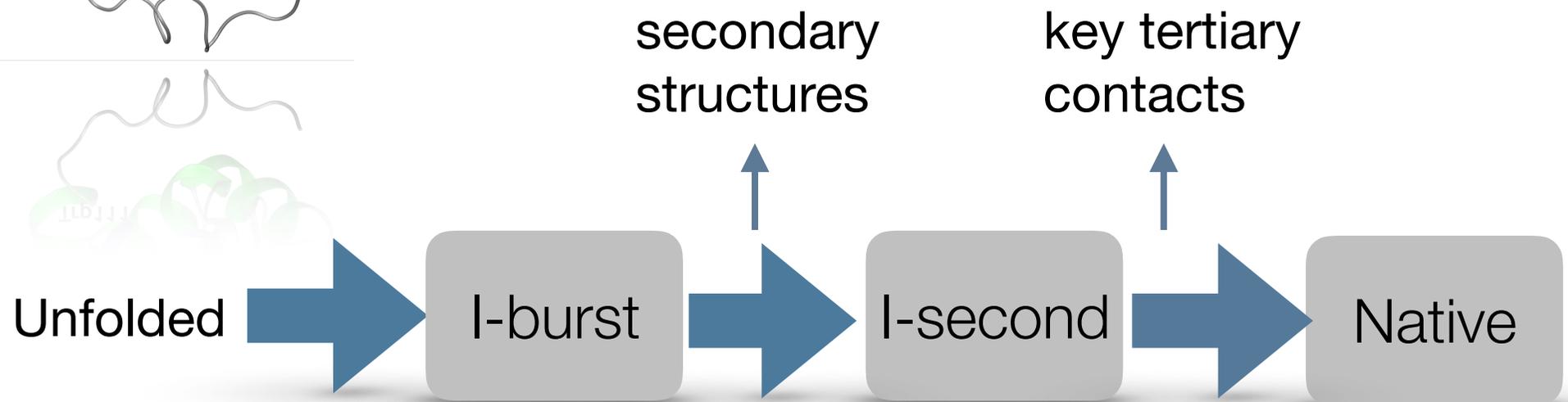


*Biochemistry* 2005, 44, 6685–6692

6685

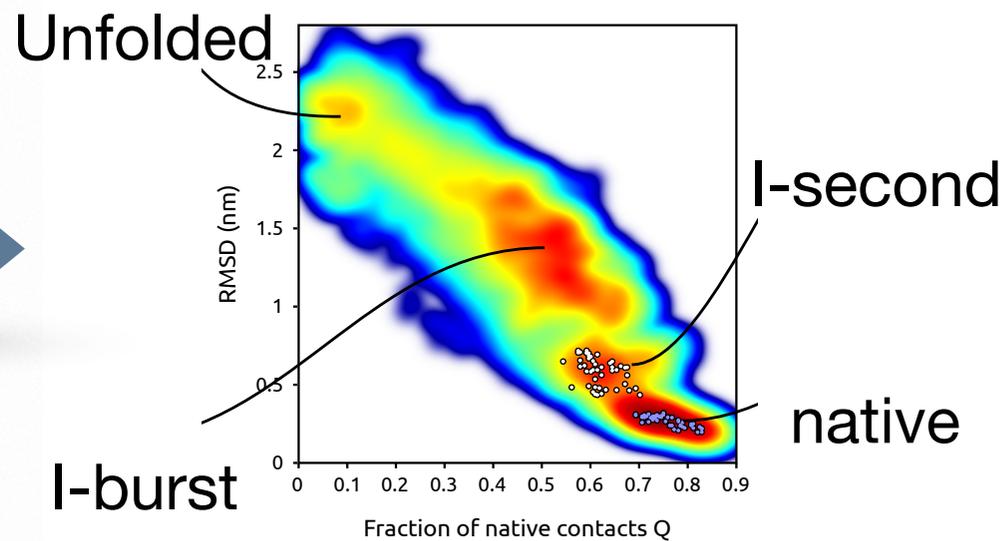
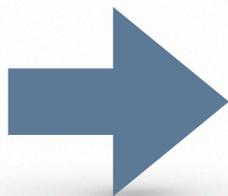
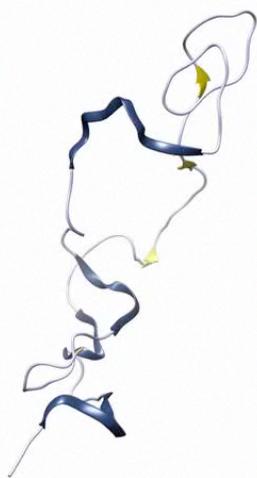
## Characterization of Kinetic Folding Intermediates of Recombinant Canine Milk Lysozyme by Stopped-Flow Circular Dichroism<sup>†</sup>

Masaharu Nakao,<sup>‡</sup> Kosuke Maki,<sup>‡</sup> Munehito Arai,<sup>§</sup> Takumi Koshiba,<sup>||,⊥</sup> Katsutoshi Nitta,<sup>||</sup> and Kunihiro Kuwajima<sup>\*‡</sup>



# MICROSCOPIC CALCULATION: STRUCTURAL DYNAMICS

$$\rho = \begin{pmatrix} \rho_{gg} & \rho_{ge_1} & \cdots & \rho_{ge_N} & \rho_{g\alpha_1} & \cdots & \rho_{g\alpha_{N_2}} \\ \rho_{e_1g} & \rho_{e_1e_1} & \cdots & \rho_{e_1e_N} & \rho_{e_1\alpha_1} & \cdots & \rho_{e_1\alpha_{N_2}} \\ \vdots & \vdots & \ddots & \vdots & \vdots & \ddots & \vdots \\ \rho_{e_Ng} & \rho_{e_Ne_1} & \cdots & \rho_{e_Ne_N} & \rho_{e_N\alpha_1} & \cdots & \rho_{e_N\alpha_{N_2}} \\ \rho_{\alpha_1g} & \rho_{\alpha_1e_1} & \cdots & \rho_{\alpha_1e_N} & \rho_{\alpha_1\alpha_1} & \cdots & \rho_{\alpha_1\alpha_{N_2}} \\ \vdots & \vdots & \ddots & \vdots & \vdots & \ddots & \vdots \\ \rho_{\alpha_{N_2}g} & \rho_{\alpha_{N_2}e_1} & \cdots & \rho_{\alpha_{N_2}e_N} & \rho_{\alpha_{N_2}\alpha_1} & \cdots & \rho_{\alpha_{N_2}\alpha_{N_2}} \end{pmatrix}$$



# MICROSCOPIC CALCULATION: QUANTUM DYNAMICS

$$\rho = \begin{pmatrix} \rho_{gg} & \rho_{ge_1} & \cdots & \rho_{ge_N} & \rho_{g\alpha_1} & \cdots & \rho_{g\alpha_{N_2}} \\ \rho_{e_1g} & \rho_{e_1e_1} & \cdots & \rho_{e_1e_N} & \rho_{e_1\alpha_1} & \cdots & \rho_{e_1\alpha_{N_2}} \\ \vdots & \vdots & \ddots & \vdots & \vdots & \ddots & \vdots \\ \rho_{e_Ng} & \rho_{e_Ne_1} & \cdots & \rho_{e_Ne_N} & \rho_{e_N\alpha_1} & \cdots & \rho_{e_N\alpha_{N_2}} \\ \rho_{\alpha_1g} & \rho_{\alpha_1e_1} & \cdots & \rho_{\alpha_1e_N} & \rho_{\alpha_1\alpha_1} & \cdots & \rho_{\alpha_1\alpha_{N_2}} \\ \vdots & \vdots & \ddots & \vdots & \vdots & \ddots & \vdots \\ \rho_{\alpha_{N_2}g} & \rho_{\alpha_{N_2}e_1} & \cdots & \rho_{\alpha_{N_2}e_N} & \rho_{\alpha_{N_2}\alpha_1} & \cdots & \rho_{\alpha_{N_2}\alpha_{N_2}} \end{pmatrix}$$

Electric moment



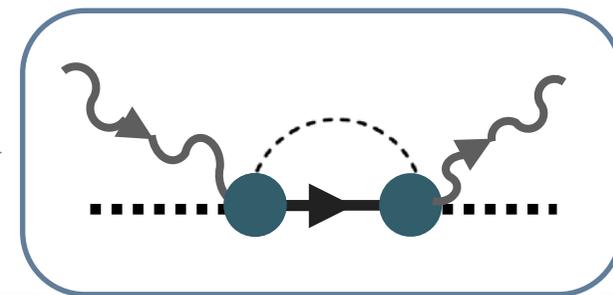
$$R_{0K} = \Im \langle 0 | \hat{\mu} | K \rangle \cdot \langle K | \hat{m} | 0 \rangle$$



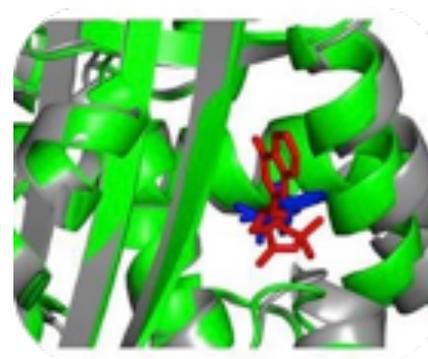
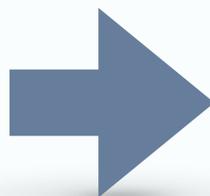
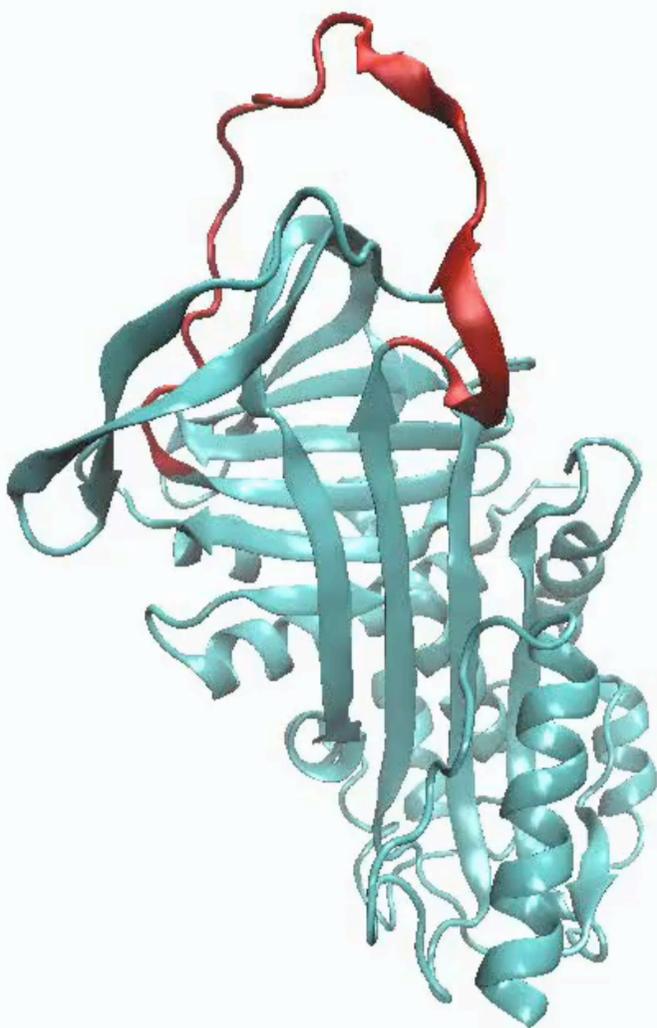
Rotatory strength  
(vertex)



Magnetic moment



# THE SERPIN LATENCY TRANSITION PUZZLE



## Serpin latency transition at atomic resolution

Giorgia Cazzoli<sup>a,b</sup>, Fang Wang<sup>c</sup>, Silvio A. Beccara<sup>b,d</sup>, Anne Gershenson<sup>e</sup>, Pietro Faccioli<sup>a,b,1</sup>, and Patrick L. Wintrodde<sup>c,1</sup>

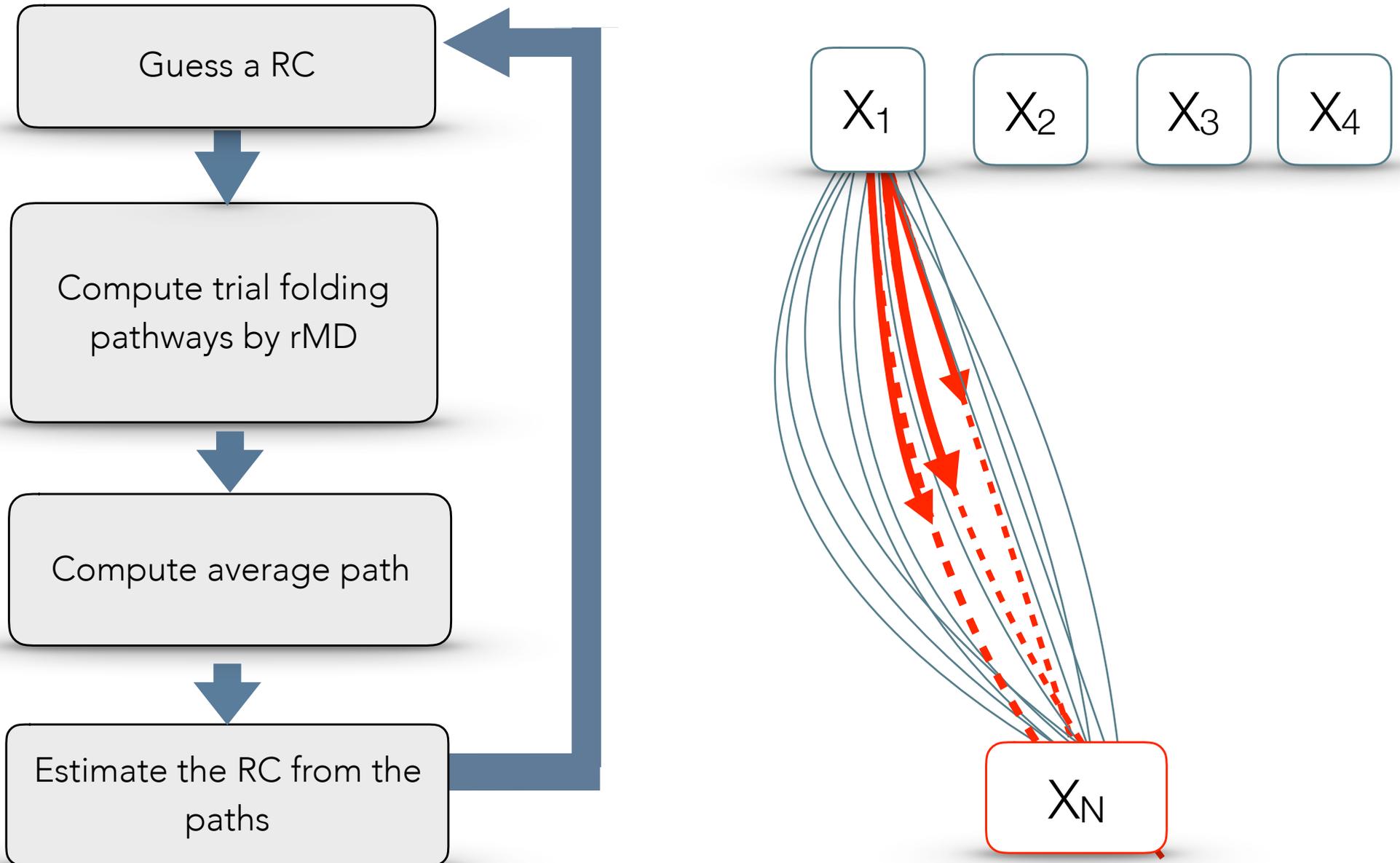
<sup>a</sup>Dipartimento di Fisica, Università degli Studi di Trento, 38100 Povo (Trento), Italy; <sup>b</sup>Trento Institute for Fundamental Physics and Applications, 38123 Povo (Trento), Italy; <sup>c</sup>Department of Pharmaceutical Sciences, School of Pharmacy, University of Maryland, Baltimore, MD 21201; <sup>d</sup>Interdisciplinary Laboratory for Computational Science, Fondazione Bruno Kessler, 38123 Povo (Trento), Italy; and <sup>e</sup>Department of Biochemistry and Molecular Biology, University of Massachusetts Amherst, Amherst, MA 01003

Edited by David E. Shaw, D. E. Shaw Research, New York, NY, and approved September 12, 2014 (received for review April 24, 2014)

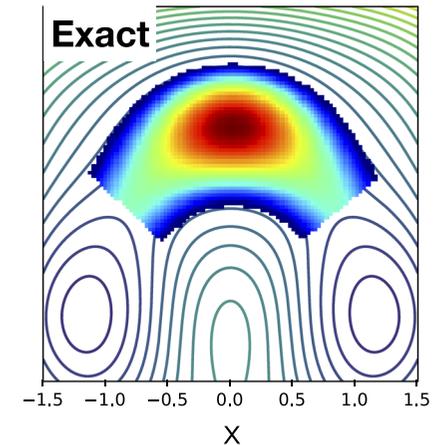
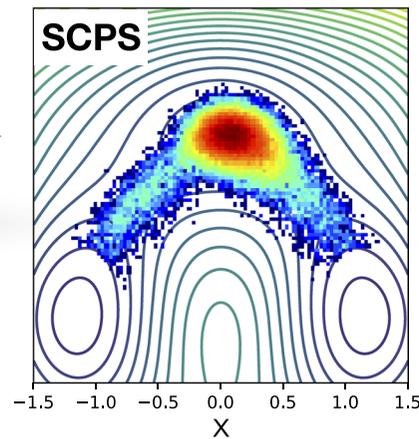
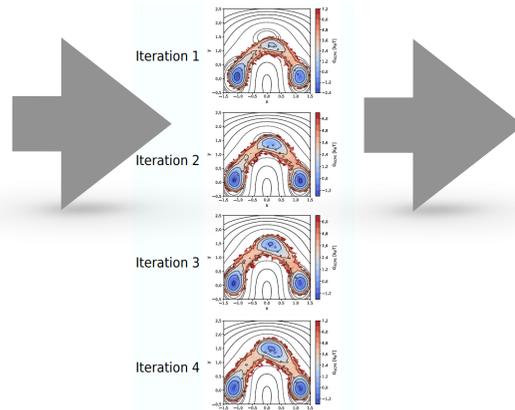
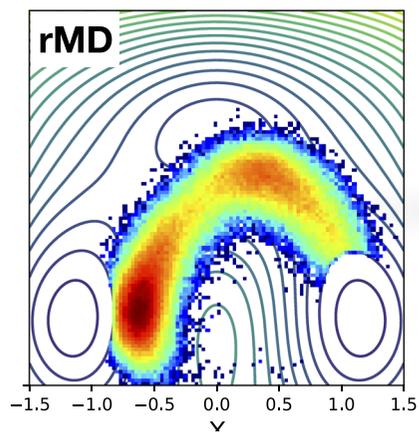
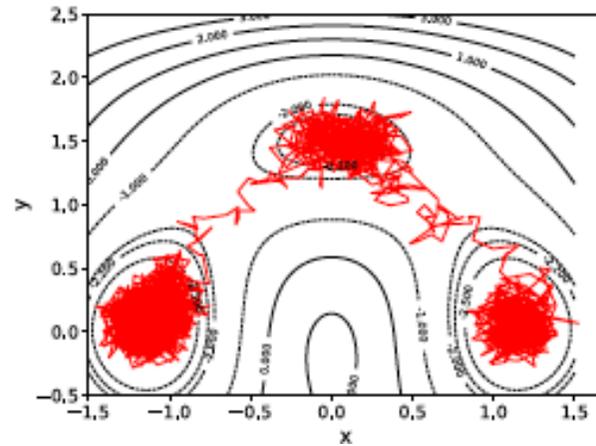
**Protease inhibition by serpins requires a large conformational transition from an active, metastable state to an inactive, stable** for polypeptide chains consisting of nearly 100 amino acids (6), which are considerably smaller than PAI-1. Additionally, the

# SELF CONSISTENT PATH SAMPLING

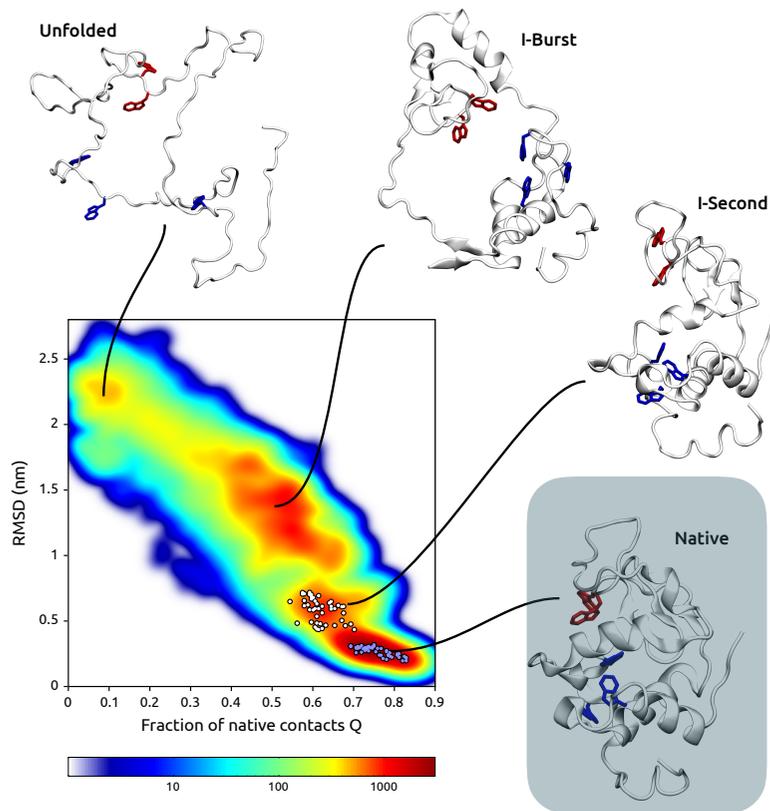
...first discussed in Bressanone...



# REACHING ACCURACY

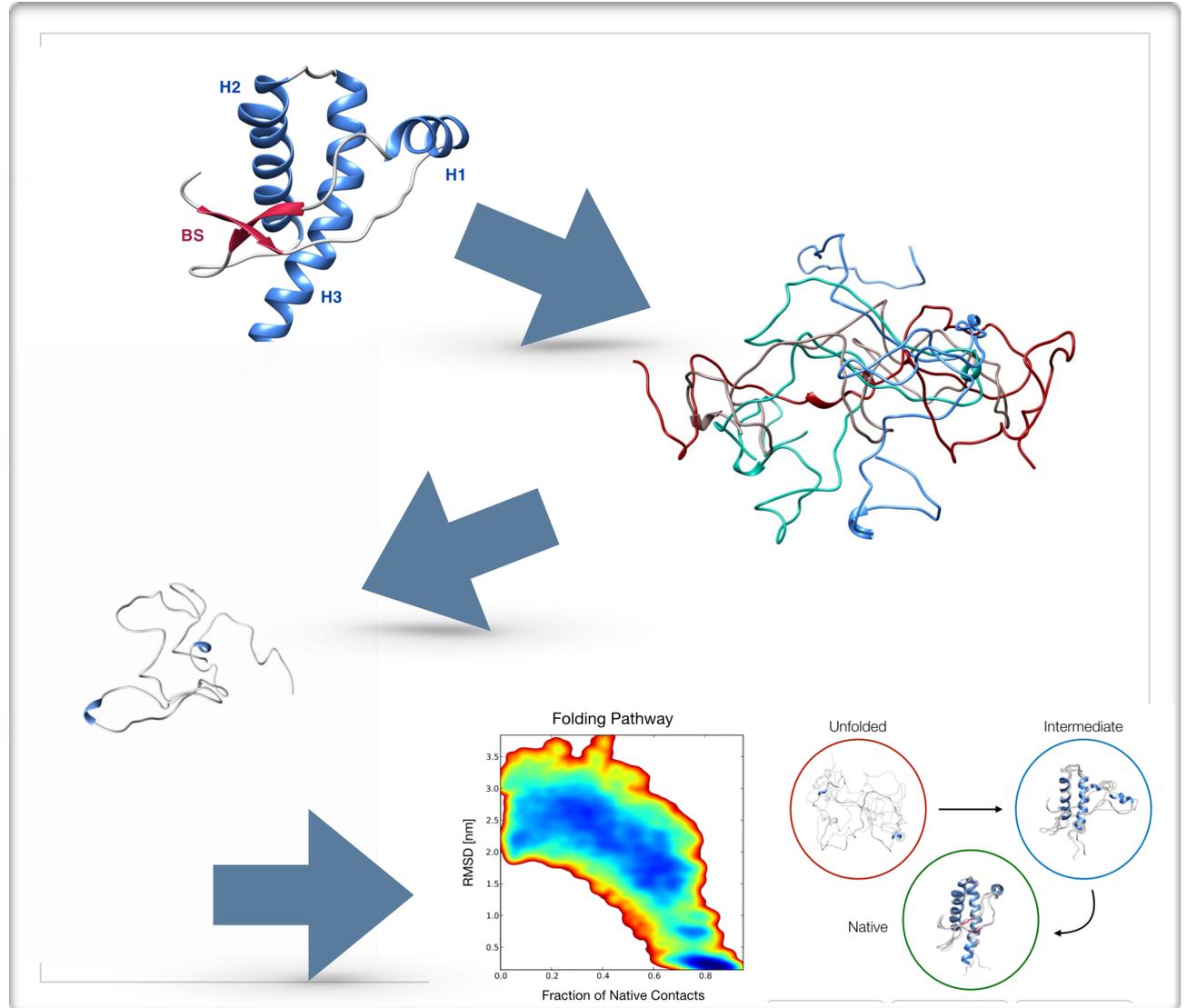
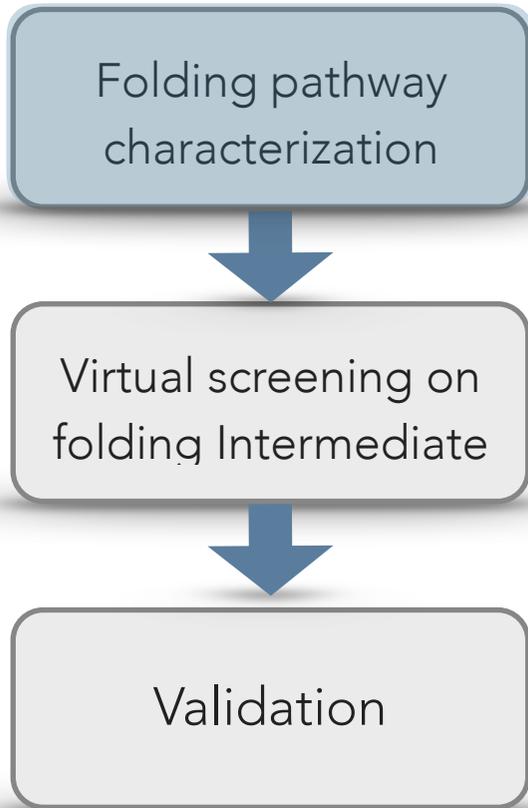


# IS THIS A FREE LOUNCH?

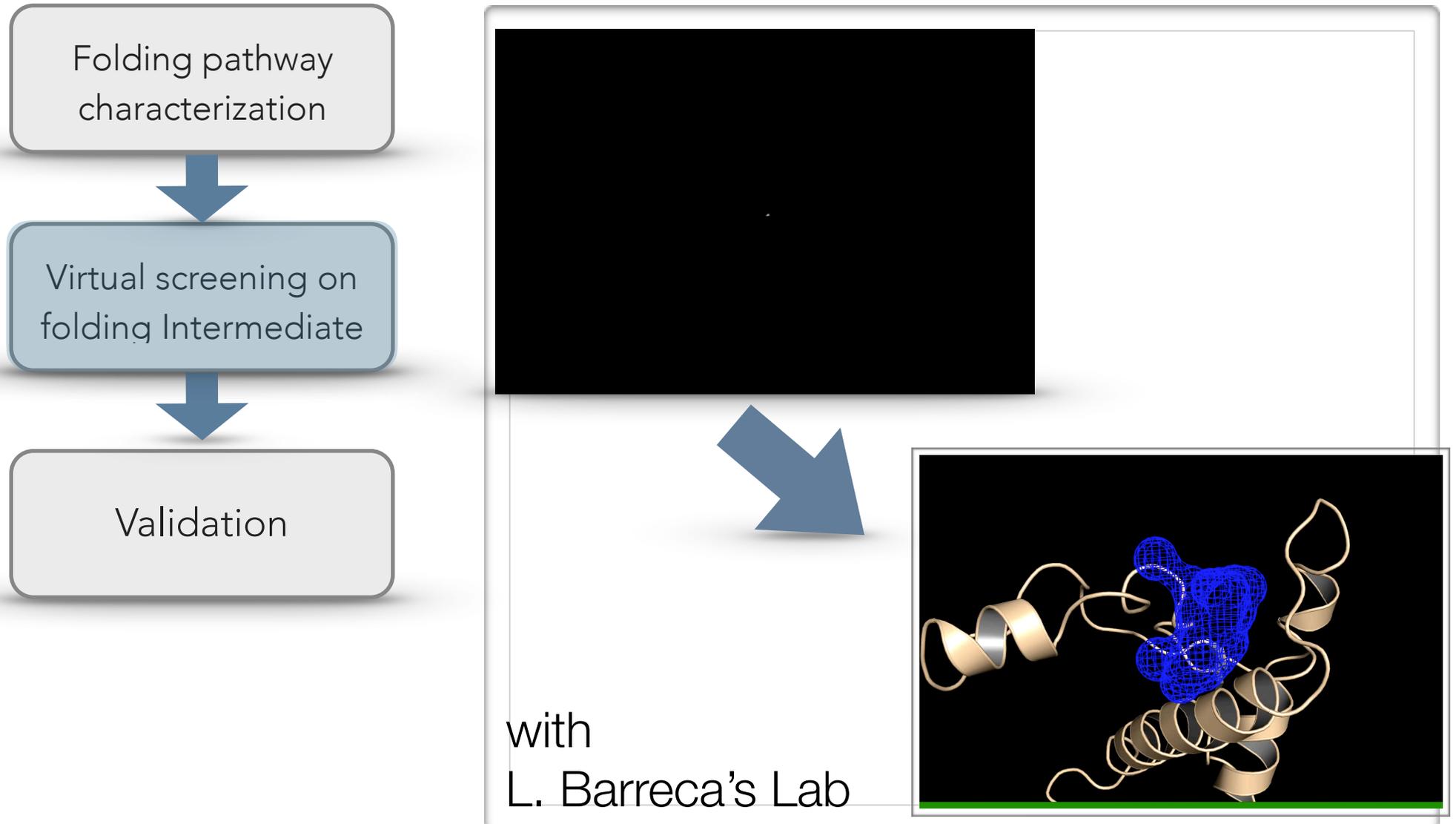


All atom  
3D structure of  
the native state  
**are given**, not  
predicted

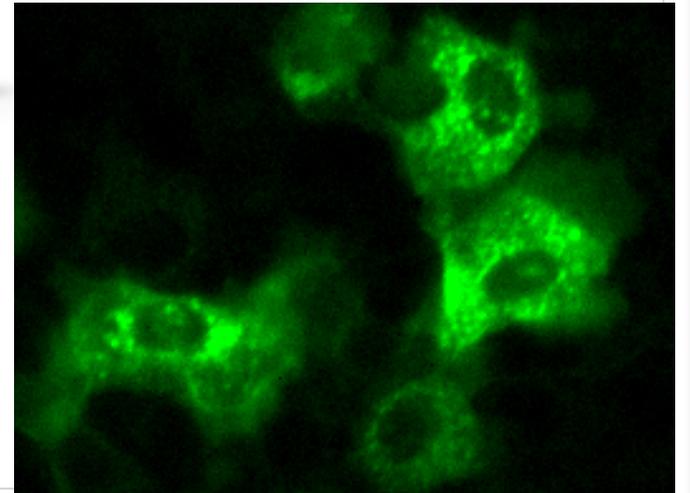
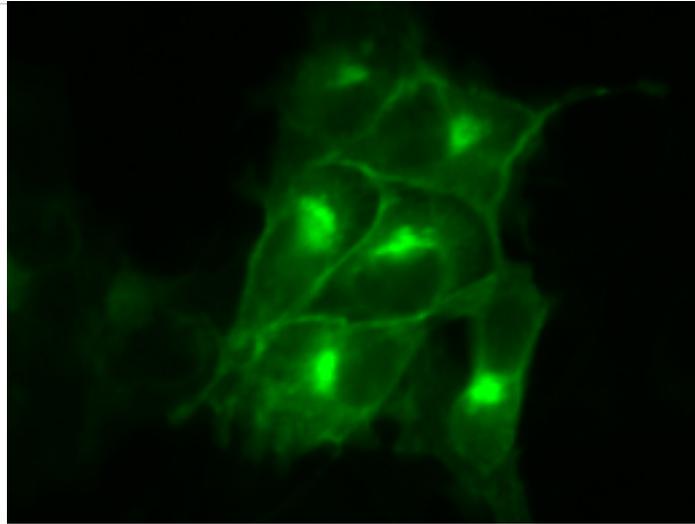
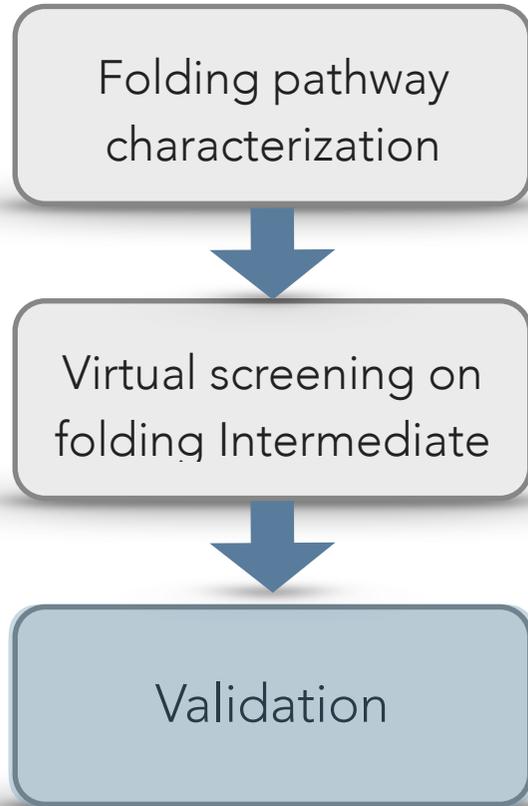
# PPI-FIT PIPELINE



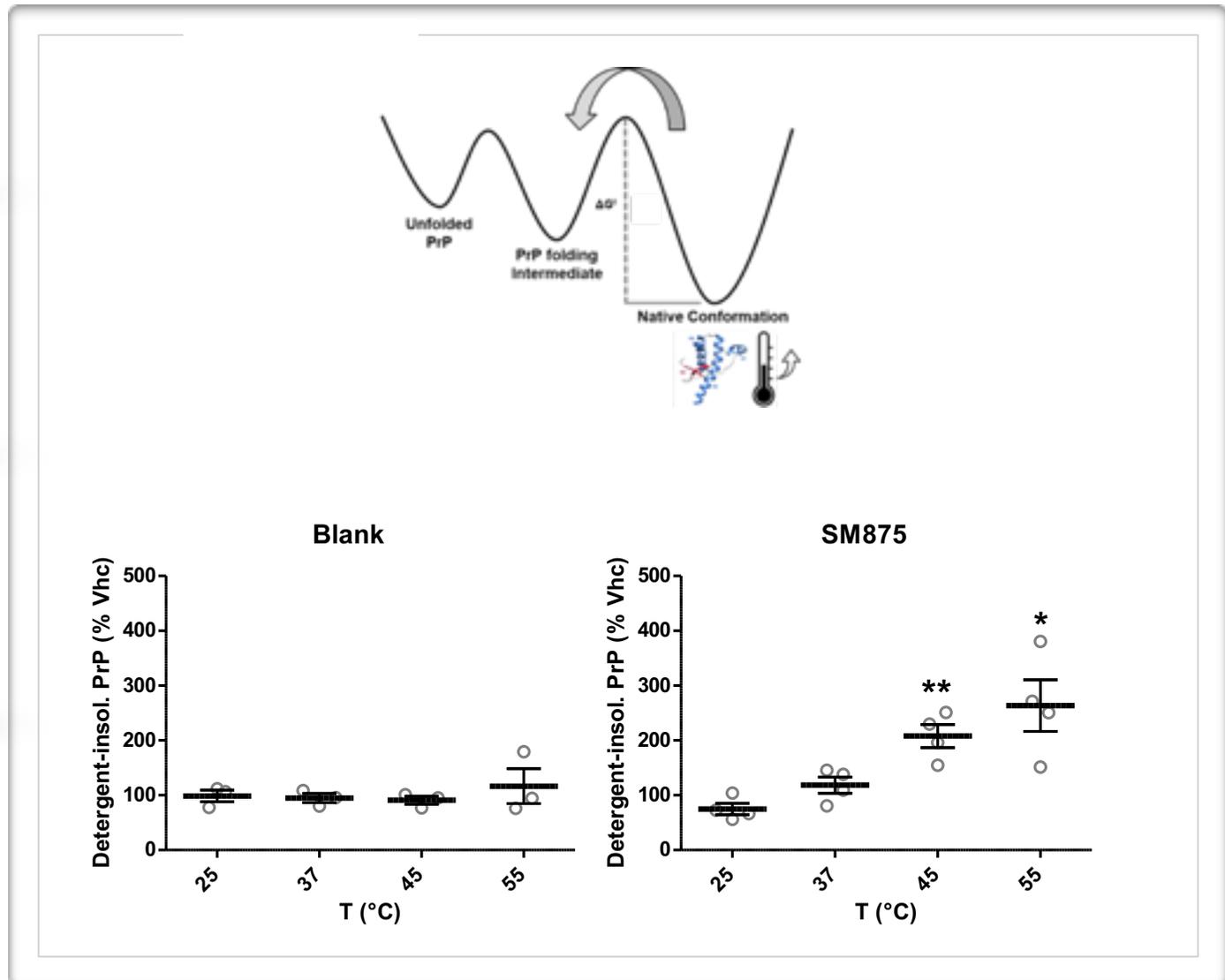
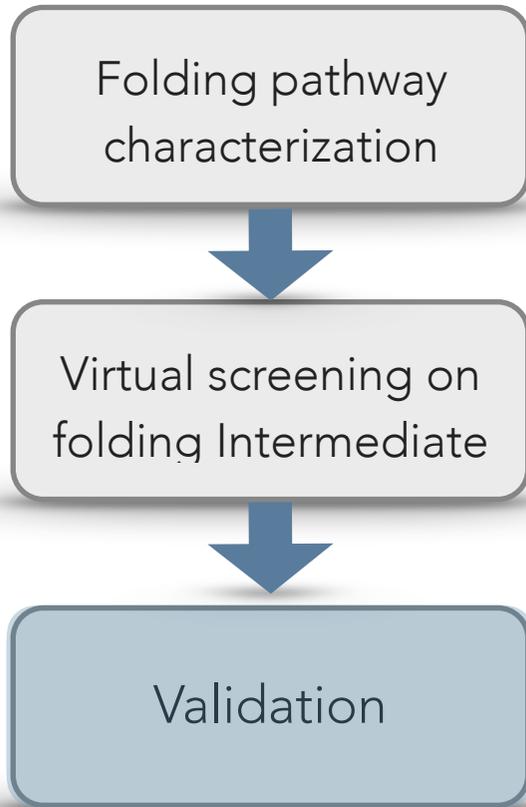
# PPI-FIT PIPELINE



# PPI-FIT PIPELINE



# PPI-FIT PIPELINE



# MOLECULAR QUANTUM FIELD THEORY

$$\rho_{lm}(t) \propto \int \mathcal{D}R \int \mathcal{D}\psi \mathcal{D}\bar{\psi} O_{lm}[\psi, \bar{\psi}, R] e^{\frac{i}{\hbar} (i\hbar S_{OM}[R] + S_S[\psi, \bar{\psi}] + S_{int}[R, \psi, \bar{\psi}])}$$

$$S_{OM}[R] = \frac{1}{4M\gamma k_B T} \sum_i \int_0^t d\tau (m_i \ddot{\mathbf{r}}_i + m_i \gamma \dot{\mathbf{r}}_i + \nabla_i U(R))^2$$

$$S_S[\psi, \bar{\psi}] = \sum_{n,m} \int_0^t d\tau \bar{\psi}_n(\tau) (i\hbar \partial_t - h_{nm}^0) \psi_m(\tau)$$

$$S_{int}[R, \psi, \bar{\psi}] = \sum_{nm} \sum_i \int_0^t d\tau f_{nm}^i \bar{\psi}_n \psi_m \delta \mathbf{r}_i$$

Just one time direction!

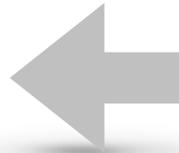
Irreversible

Microscopic

# SOLVING MQFT

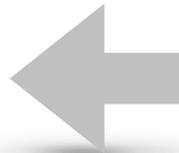
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Perturbation Theory



PRB 2012, PRB 2013, PRB 2016

Quantum MC  
(real time)



PRB 2016

Renorm. Group &  
Eff. Field Theory



PRB 2013, JCP 2016

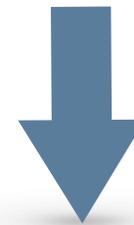
# PATH INTEGRAL REPRESENTATION

Hamilton's equations



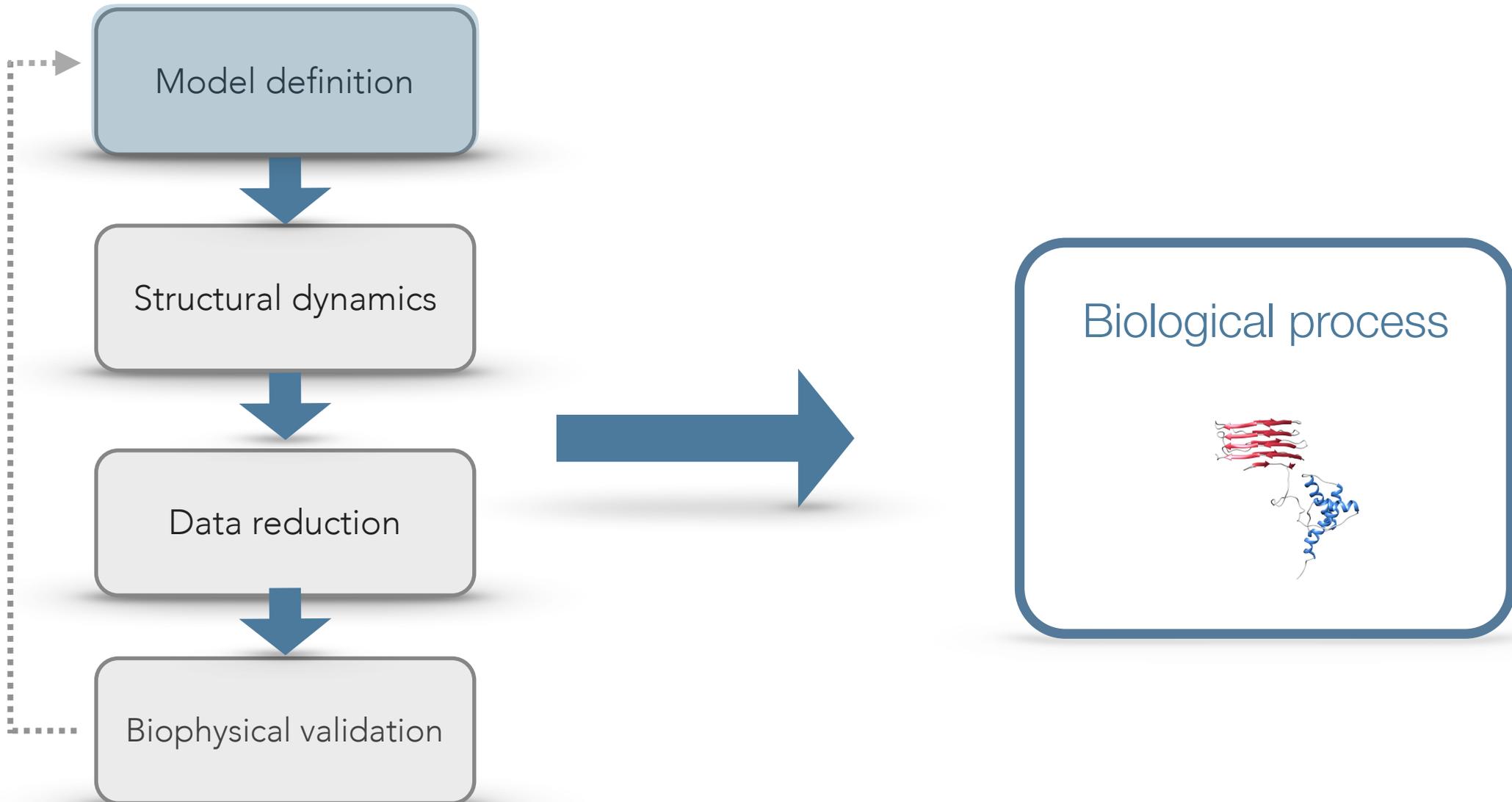
Langevin equations

$$M\ddot{\mathbf{r}}_i = -\nabla_i U(\mathbf{R}) - \gamma_i \dot{\mathbf{r}}_i + \eta_i(t)$$

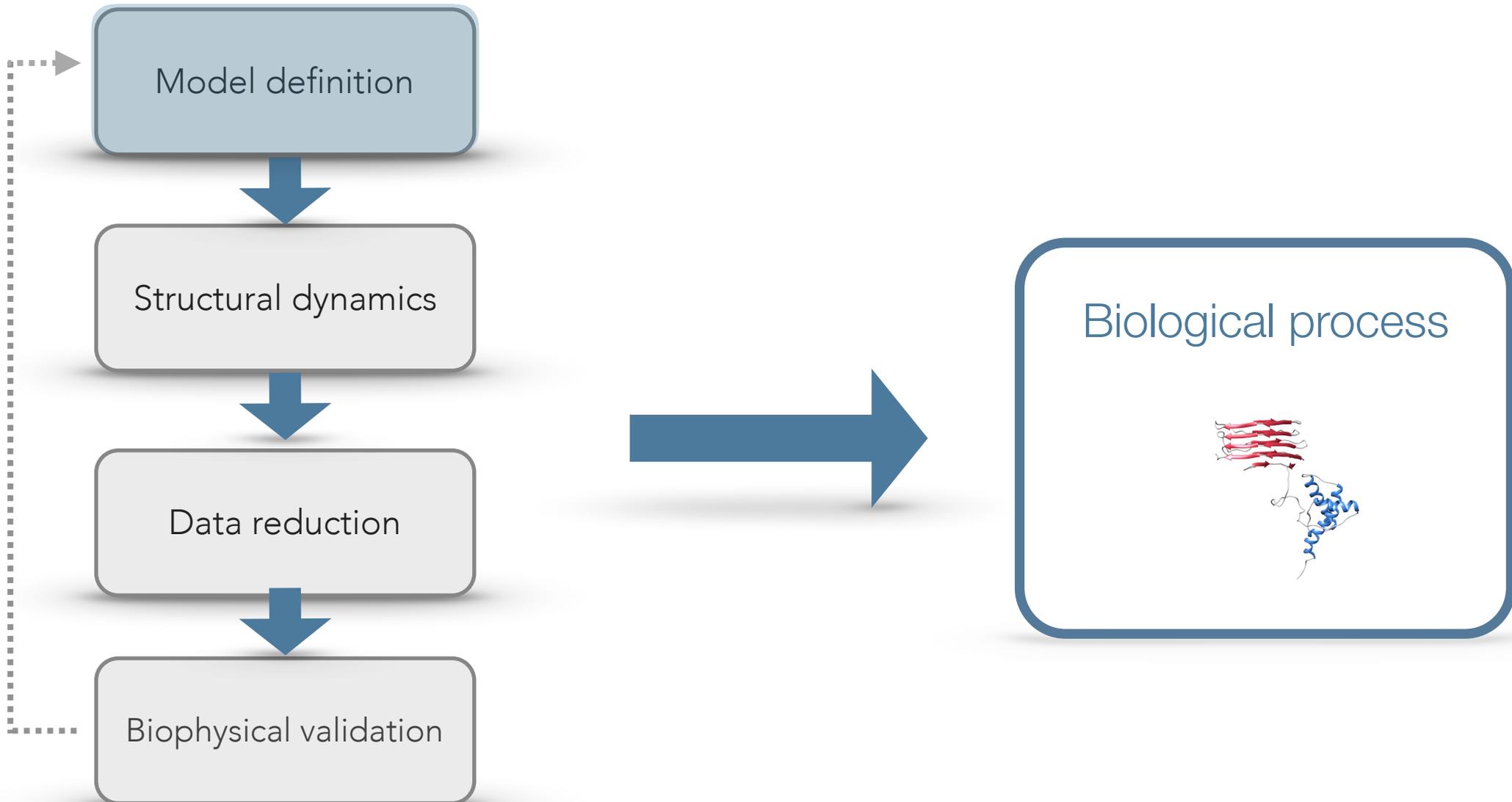


$$P(R_f, t | R_i, 0) = \int \mathcal{D}R e^{-\frac{\beta}{4m\gamma} \int_0^t d\tau (m\ddot{R} + m\gamma\dot{R} + \nabla U)^2}$$

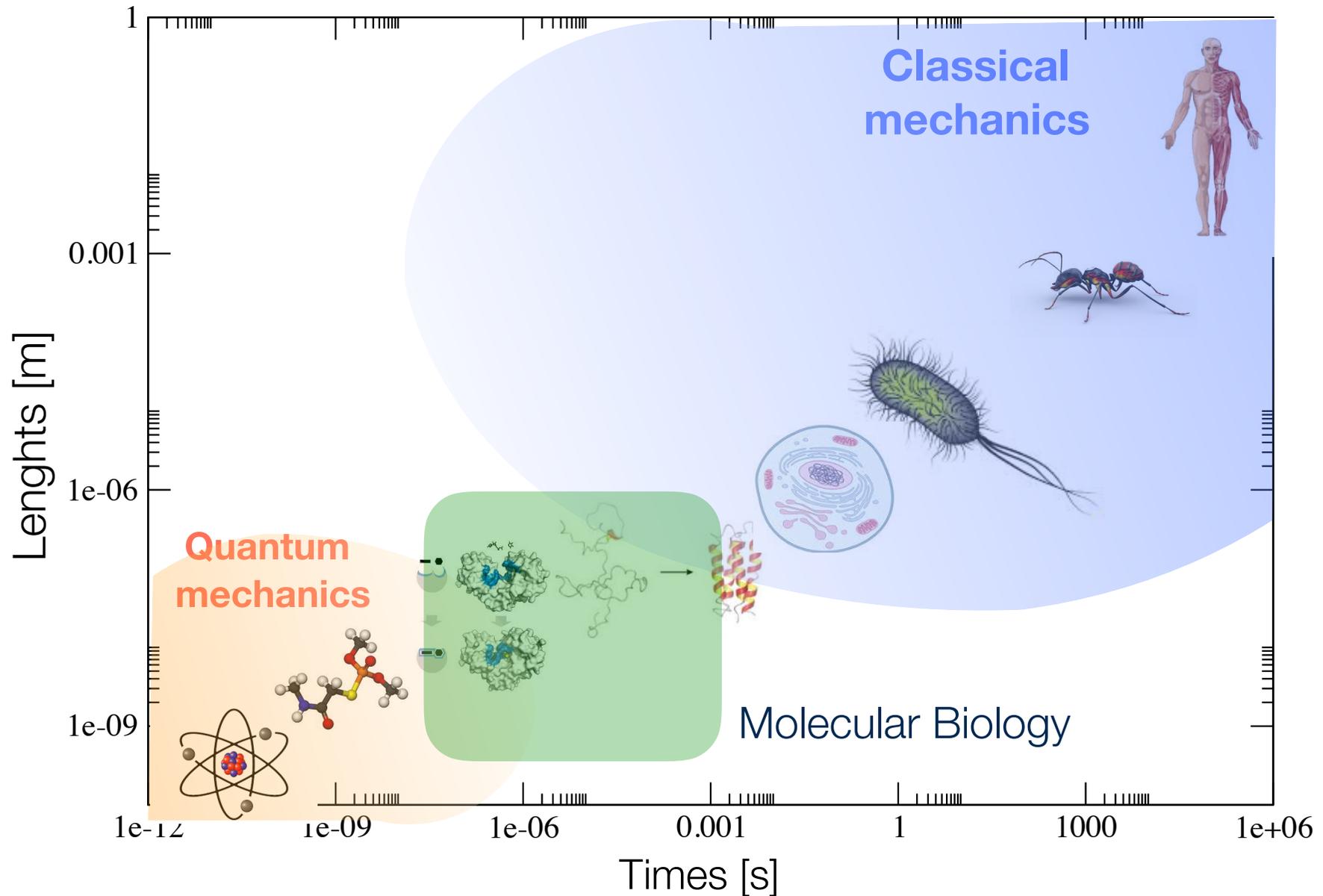
# ROADMAP FROM PHYSICS TO MOLECULAR BIOLOGY



# ROADMAP FROM PHYSICS TO MOLECULAR BIOLOGY



# AT THE BORDERLINE BETWEEN TWO REALMS



# ROADMAP TO MOLECULAR BIOLOGY

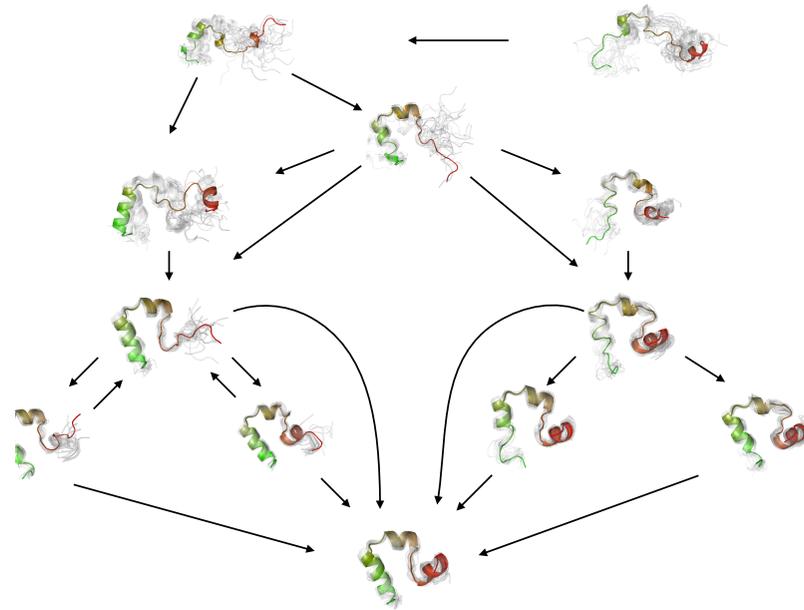
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Model definition

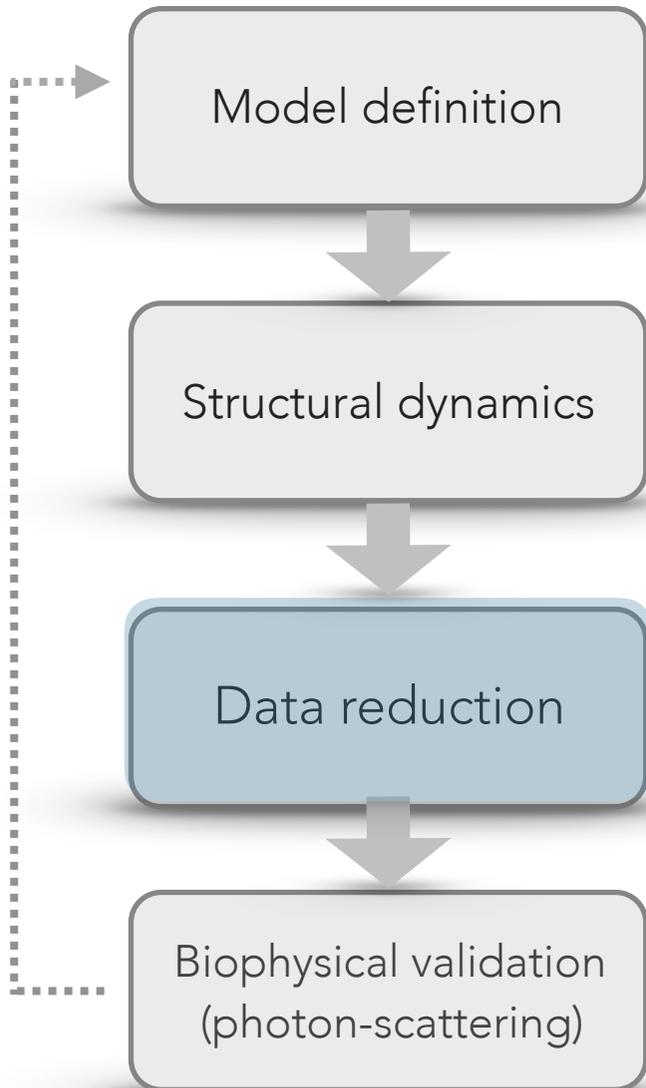
Structural dynamics

Data reduction

Biophysical validation  
(photon-scattering)



# ROADMAP TO MOLECULAR BIOLOGY

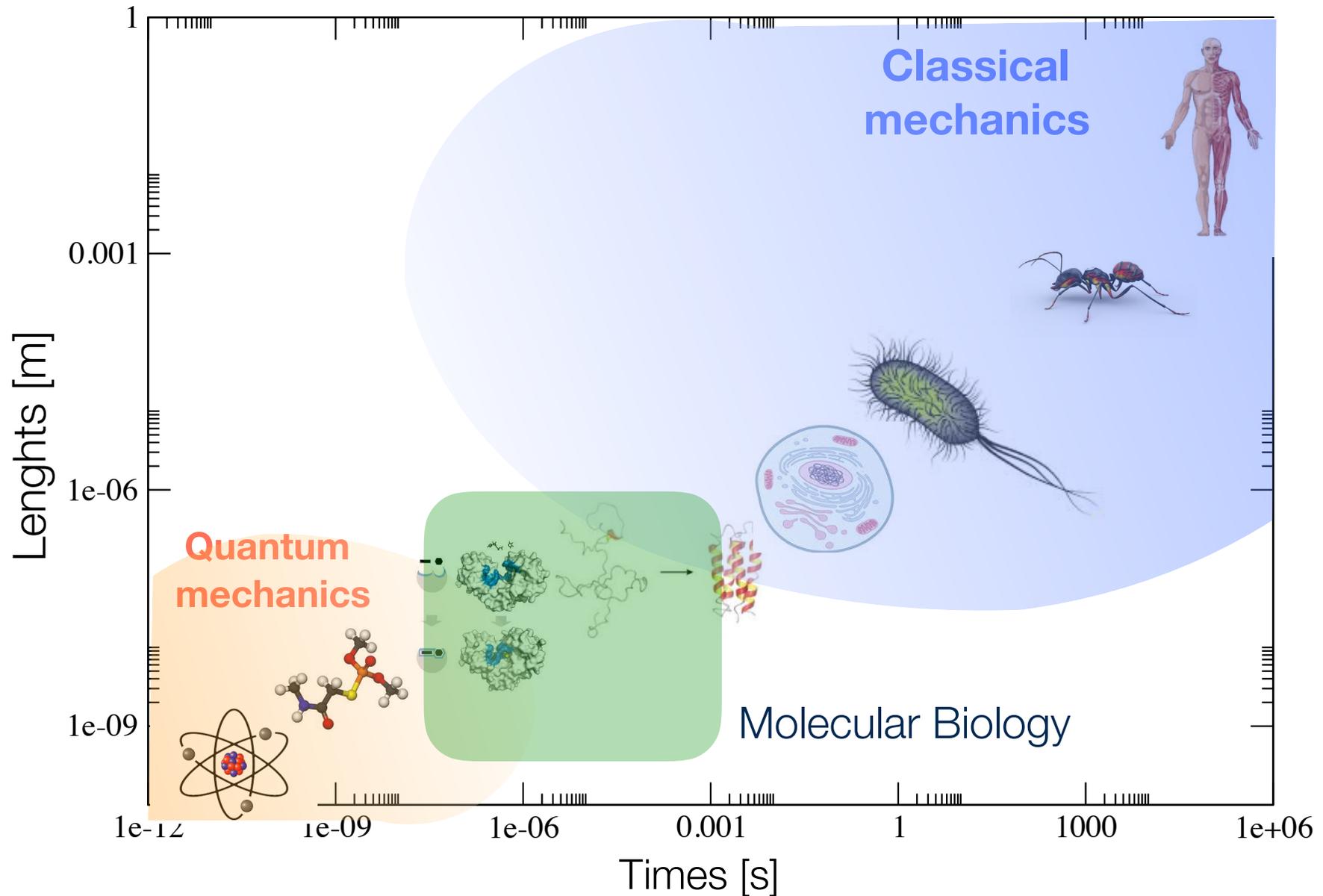


Data Science  
+  
Statistical computing  
+  
Renormalization Group  
methods

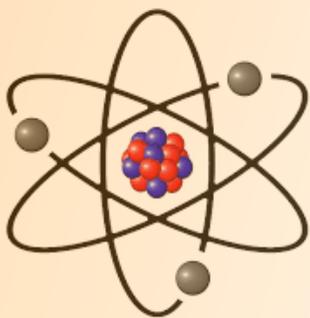
**Dimensional reduction of Markov state models from renormalization group theory**

S. Orioli and P. Faccioli

# AT THE BORDERLINE BETWEEN TWO REALMS



# MOLECULAR DYNAMICS



Electronic clouds obey  
**quantum mechanics**

$$i\hbar \frac{\partial}{\partial t} \psi = \hat{H} \psi$$



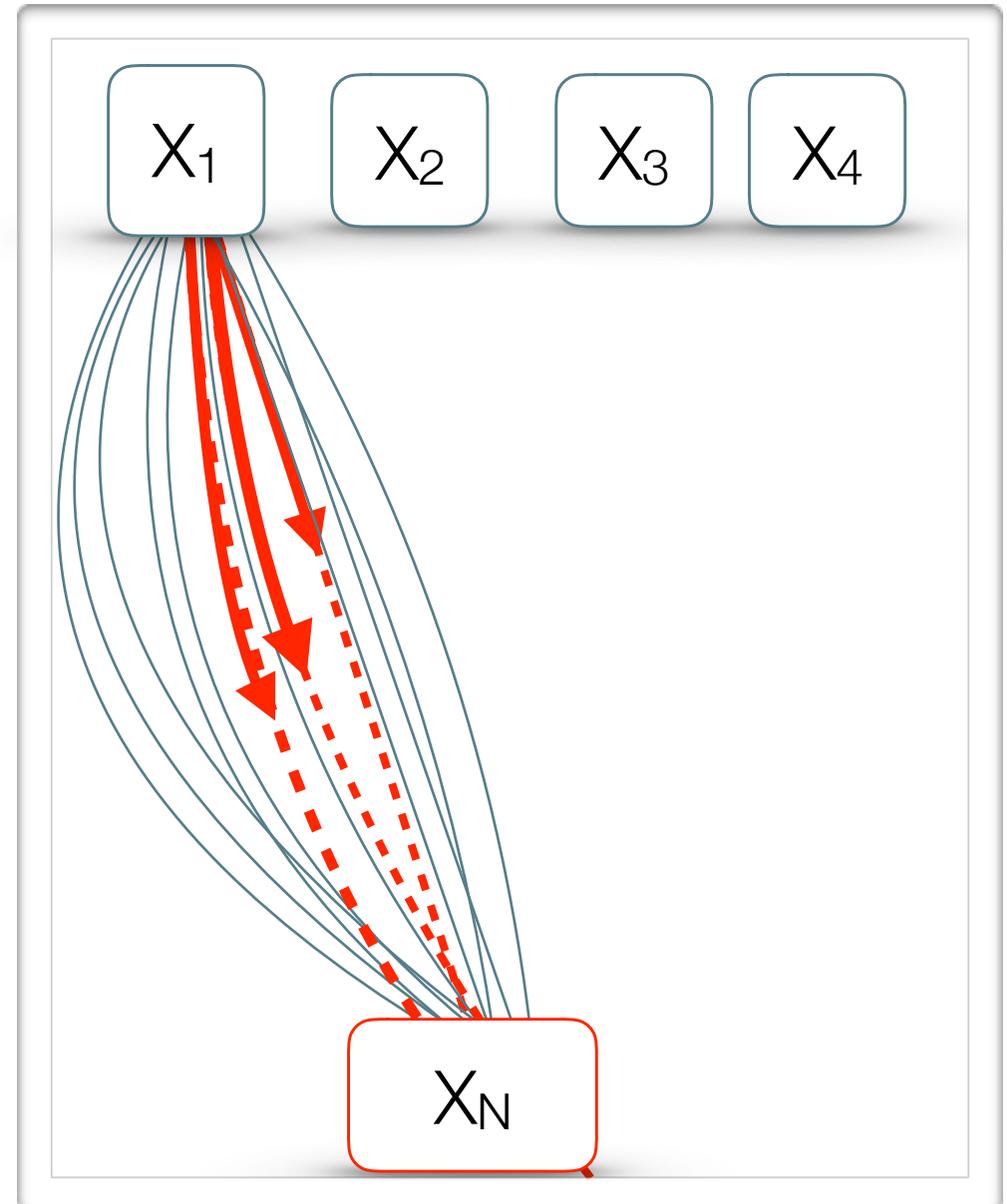
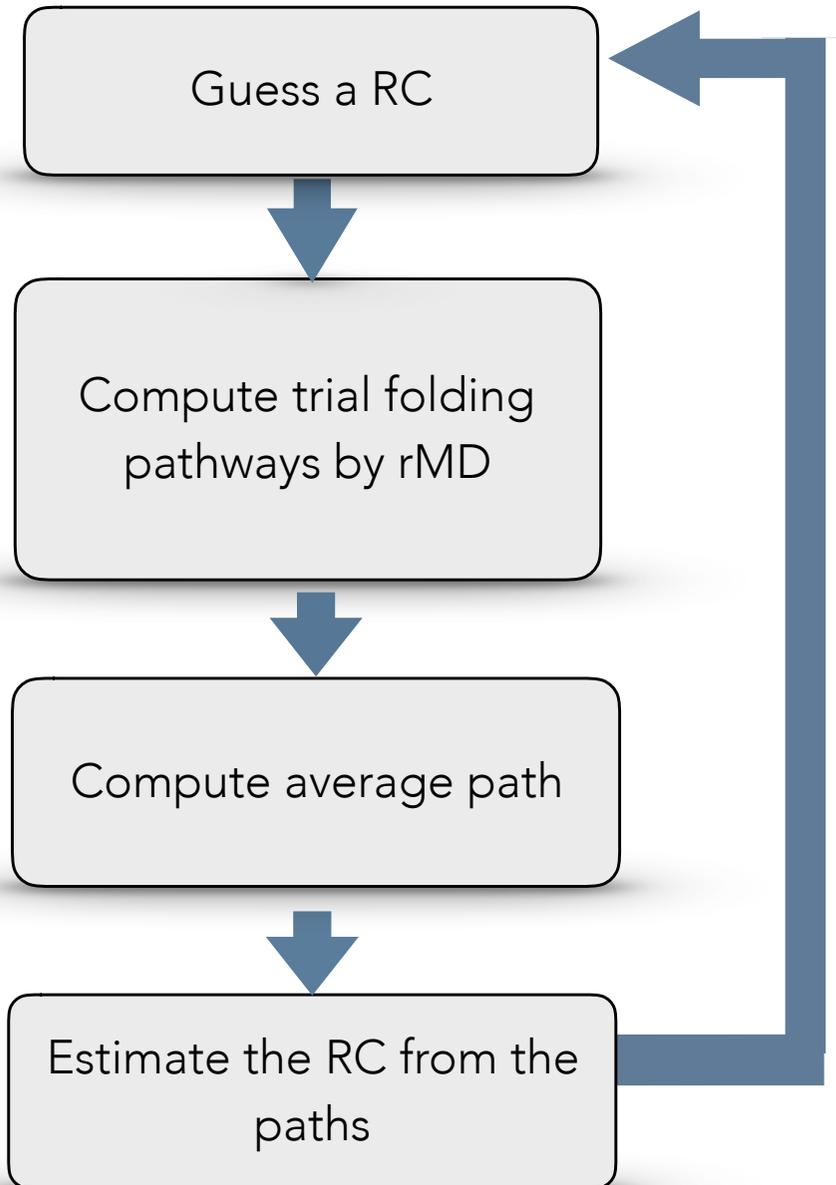
The motion of atomic  
nuclei obey  
**classical mechanics**

$$\vec{F} = m\vec{a}$$

Multi-scale approach

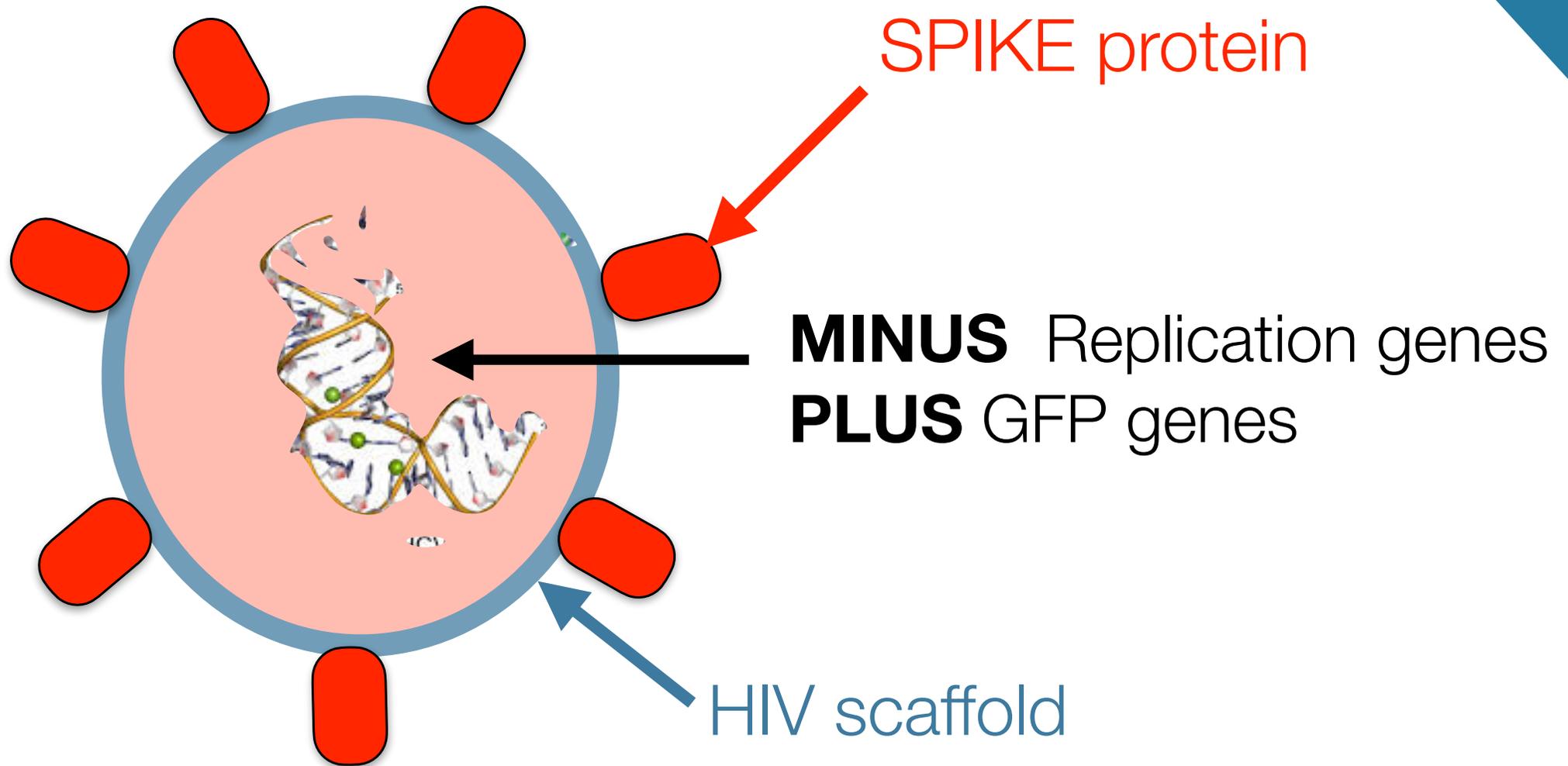
(2013 Nobel prize for chemistry)

# SELF CONSISTENT PATH SAMPLING



# PSEUDOTYPED RETROVIRAL VECTOR

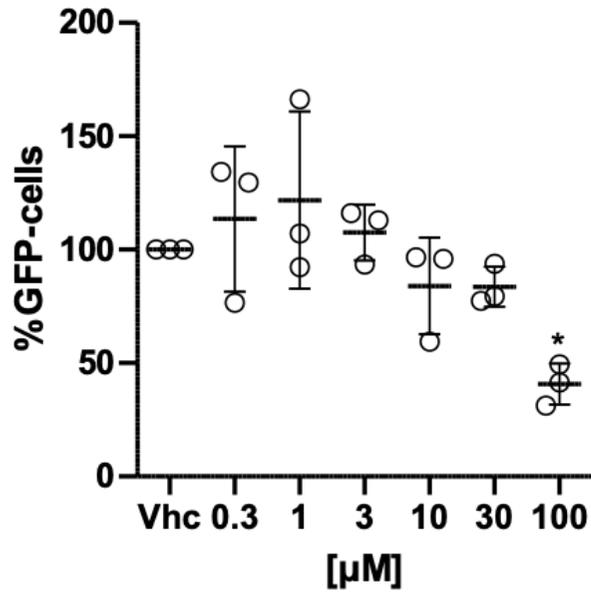
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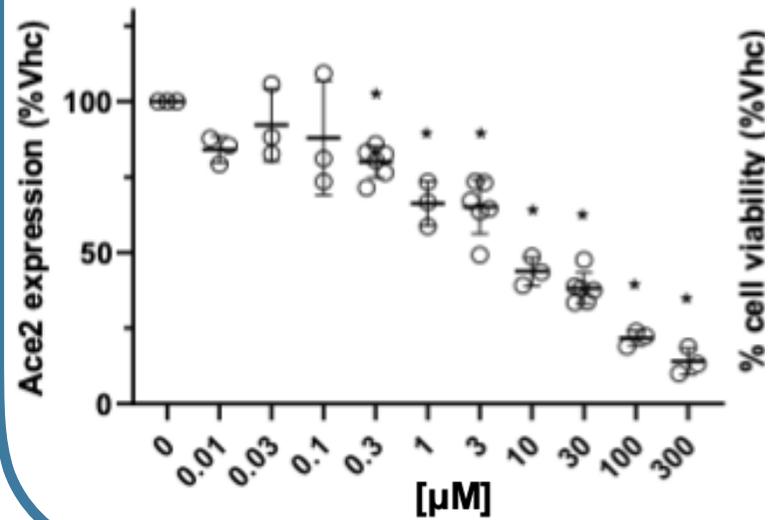
# ACTION ON A PSEUDOVIRAL VECTOR



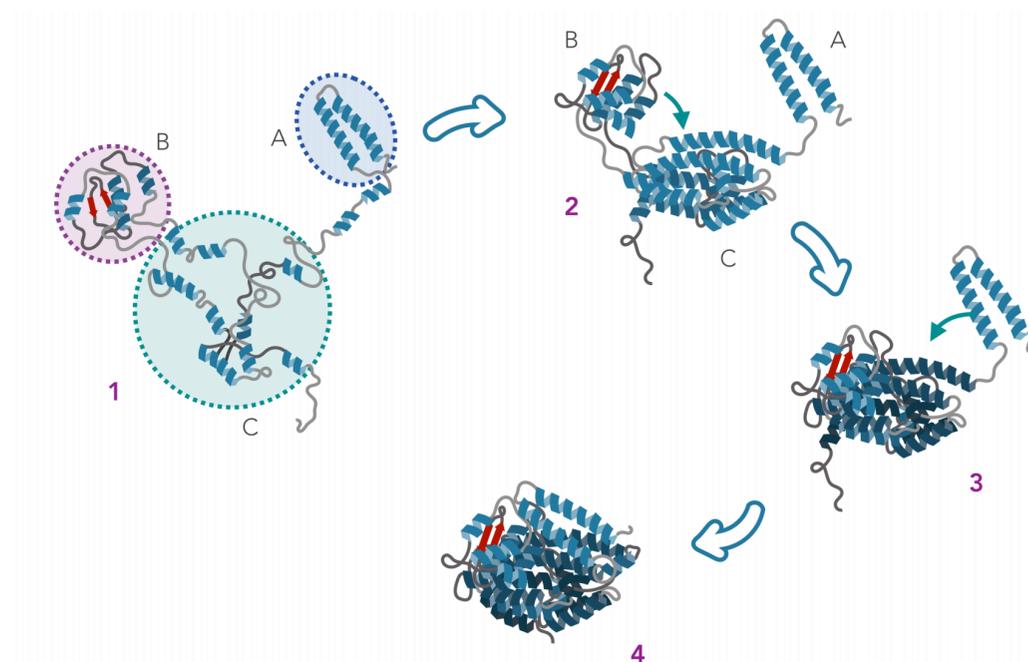
Pseudo-virus  
Transduction  
Efficiency



ACE-2 cellular  
expression level



# Results on ACE2



30.000 cores in 8 different data centers were supplied by **INFN** to perform ACE2 folding simulation in 2 weeks.