

# Electroweak corrections to the angular coefficients of finite- $p_T$ Z-boson production at $pp$ colliders<sup>1</sup>

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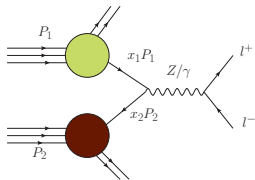
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<sup>1</sup>R. Frederix, T. Vitos, [arXiv:2007.08867](https://arxiv.org/abs/2007.08867)

## The (neutral current) Drell-Yan process



- At LHC:  $pp \rightarrow Z/\gamma + X \rightarrow l^+ l^- + X$
- Clear signature, large cross section  $\rightarrow$  optimal for PDF fits
- **Measurements** with data:
  - pion beams <sup>2</sup>
  - $p\bar{p}$  at Tevatron <sup>34</sup>
  - $pp$  at LHC <sup>56</sup>
- Interesting for non-zero  $p_T$  of Z-boson

### Expansion for non-zero $p_T$

for some observable  $\Sigma$ :

$$\Sigma(\alpha, \alpha_S) = \underbrace{\alpha^2 \alpha_S \Sigma_{2,1}}_{\text{LO}} + \underbrace{\alpha^2 \alpha_S^2 \Sigma_{2,2}}_{\text{NLO QCD}} + \underbrace{\alpha^3 \alpha_S \Sigma_{3,1}}_{\text{NLO EW}} + \mathcal{O}(\alpha^4 \alpha_S^2)$$

<sup>2</sup>Conway *et al.*, [10.1103/PhysRevD.39.92](https://arxiv.org/abs/10.1103/PhysRevD.39.92)

<sup>3</sup>CDF Collaboration, [arXiv:0908.3914](https://arxiv.org/abs/0908.3914)

<sup>4</sup>D0 Collaboration, [arXiv:hep-ex/0702025](https://arxiv.org/abs/hep-ex/0702025)

<sup>5</sup>CMS Collaboration, [arXiv:1504.03512](https://arxiv.org/abs/1504.03512)

<sup>6</sup>ATLAS Collaboration, [arXiv:1606.00689](https://arxiv.org/abs/1606.00689)

## Angular coefficients for the Drell-Yan process

- Expand the matrix element into **hadronic** and **leptonic tensor**

$$\mathcal{M} = H_{\mu\nu} L^{\mu\nu}$$

- Lepton ( $l^-$ ) angular coordinates in the **Collins-Soper frame**:  $(\theta, \phi)$
- Differential cross section** in Z-boson kinematics expanded in **real spherical harmonics**  $Y_{lm}(\theta, \phi)$ :

$$\begin{aligned} \frac{d\sigma}{dp_{T,Z} dy_Z dm_{ll} d\Omega} \propto & \left( (1 + \cos^2 \theta) + A_0 \frac{1}{2} (1 - 3 \cos^2 \theta) + A_1 \sin 2\theta \cos \phi \right. \\ & + A_2 \frac{1}{2} \sin^2 \theta \cos 2\phi + A_3 \sin \theta \cos \phi + A_4 \cos \theta \\ & \left. + A_5 \sin^2 \theta \sin 2\phi + A_6 \sin 2\theta \sin \phi + A_7 \sin \theta \sin \phi \right) \end{aligned}$$

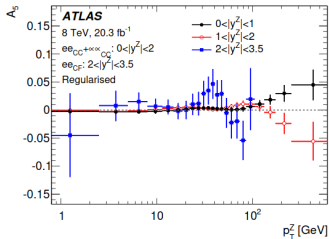
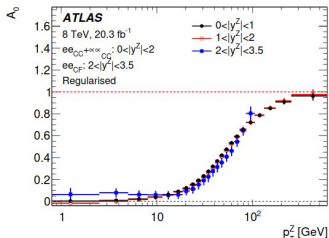
with eight **angular coefficients**  $A_i(p_{T,Z}, y_Z, m_{ll})$

# Angular coefficients for the Drell-Yan process

## On the properties of the coefficients

- $A_0$  and  $A_2$  are an order of magnitude larger
- $A_{5,6,7}$  are zero at LO and very small at NLO QCD
- All even under parity except  $A_3, A_4 \rightarrow$  sensitive to  $\theta_w$
- All vanish except  $A_4$  in the  $p_{T,Z} \rightarrow 0$  limit

- ATLAS measurements for  $A_0$  and  $A_5$ <sup>7</sup>



<sup>7</sup>ATLAS Collaboration, arXiv:1606.00689

## Lam-Tung relation

- Up to order  $\alpha^2\alpha_S$  (LO): Lam-Tung relation  $A_0 = A_2$
- Predictions available <sup>8</sup> at order  $\alpha^2\alpha_S^3$  (NNLO QCD)
- LHC and Tevatron data all show **higher violation** of Lam-Tung than predicted by NNLO QCD at  $p_{T,Z} \gtrsim 20$  GeV
- NNLO QCD moves SM prediction closer to data**
- Let us see the effects of NLO EW corrections!

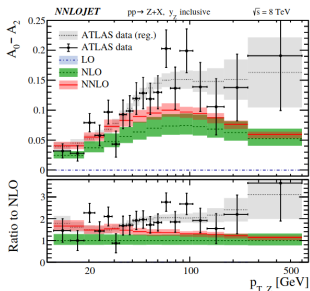


Figure: Figure from R. Gauld et al.

<sup>8</sup>R. Gauld, et al., arXiv:1708.00008



## Calculational setup

- **Fixed-order:**  $pp \rightarrow l^+ l^- j$  at 8 TeV with **MadGraph5\_aMC@NLO**
- Final state:  $e^+ e^-$ ,  $\mu^+ \mu^-$  and no jet requirements
- Lepton pair invariant mass window

$$m_{ll} \in [80.0, 100.0] \text{ GeV}$$

- **Photon recombination** with  $R < 0.1$  (but results **insensitive** to this)
- Electroweak parameters: **complex  $G_\mu$ -scheme** and complex mass scheme

### On the $\theta_w$

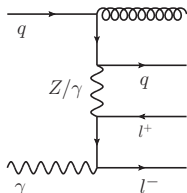
- High sensitivity to  $\theta_w$
- Include one-loop correction to  **$\rho$ -parameter**<sup>9</sup>

$$\Delta\rho = \frac{\sqrt{2}G_\mu}{16\pi} 3m_t^2$$

in the LO and NLO QCD calculations

<sup>9</sup>J Fleischer *et al.*, [10.1016/0370-2693\(93\)90810-5](https://arxiv.org/abs/10.1016/0370-2693(93)90810-5)

## Calculational setup: technicalities



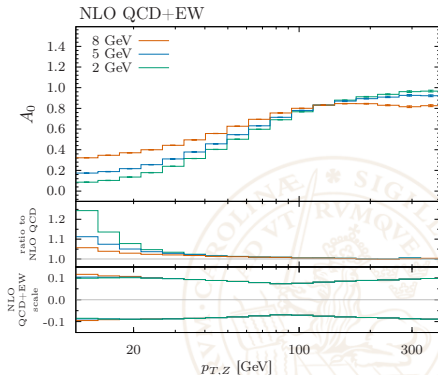
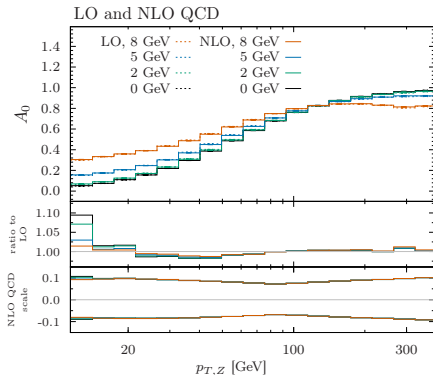
- **Double collinear singularity** for lepton + gluon
- **Introduce massive leptons**  $\rightarrow$  large  $\log \frac{m^2}{\mu^2}$
- Introduce **single lepton  $p_T$  cut**
- Expansion in spherical harmonics then not valid
- $\rightarrow$  **Extrapolate to the full phase-space by varying the cut value:**

$$(p_T)_{\text{cut}} \in \{2.0, 5.0, 8.0\} \text{ GeV}$$



## Angular coefficients: results

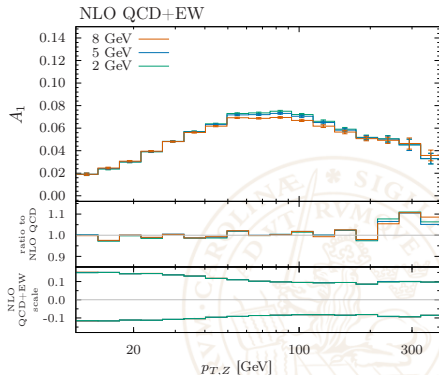
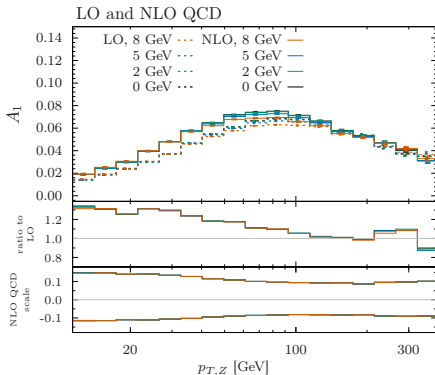
- Distributions for  $A_0$
- No safe extrapolation in low- $p_{T,Z}$  region





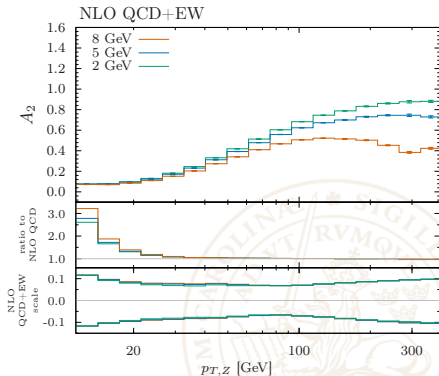
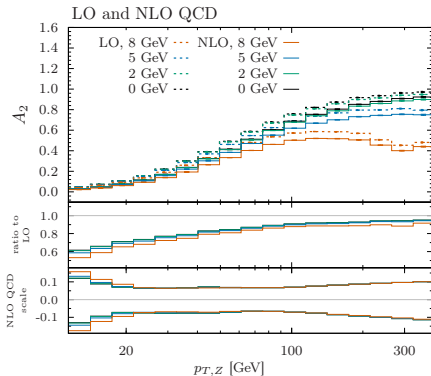
## Angular coefficients: results

- Distributions for  $A_1$
- Negligible electroweak corrections



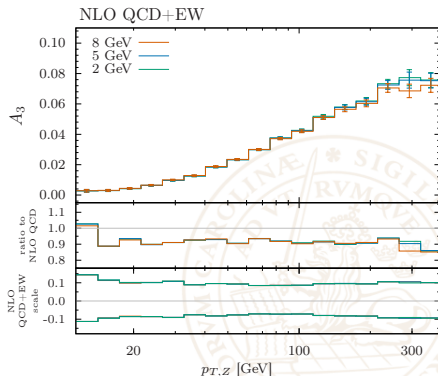
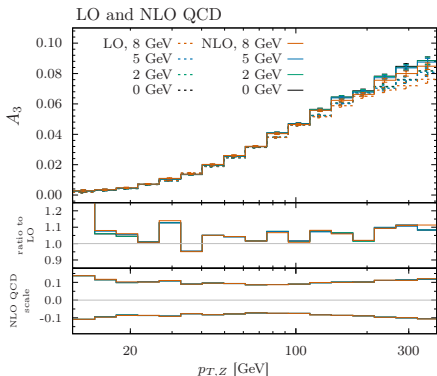
# Angular coefficients: results

- Distributions for  $A_2$



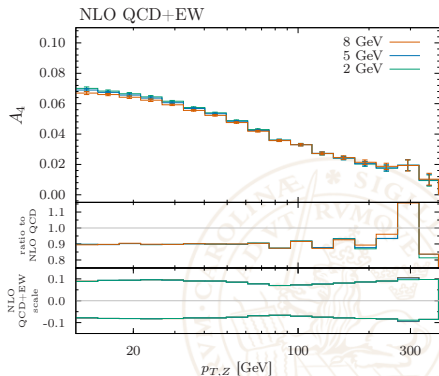
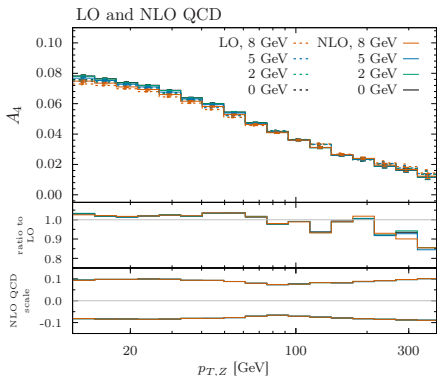
## Angular coefficients: results

- Distributions for  $A_3$
- Overall  $-10\%$  electroweak corrections
- Would be  $-30\%$  if no one-loop  $\rho$ -parameter in NLO QCD



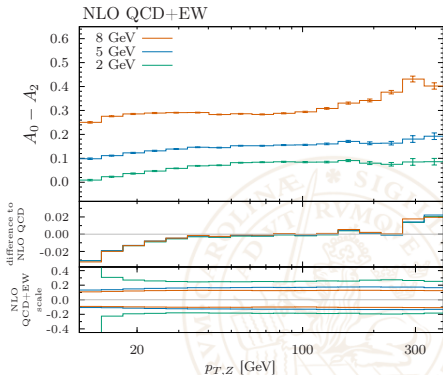
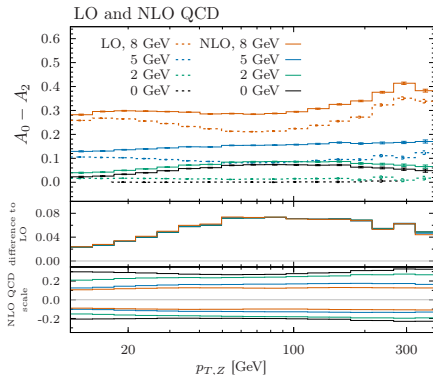
## Angular coefficients: results

- Distributions for  $A_4$
- Same  $-10\%$  electroweak corrections



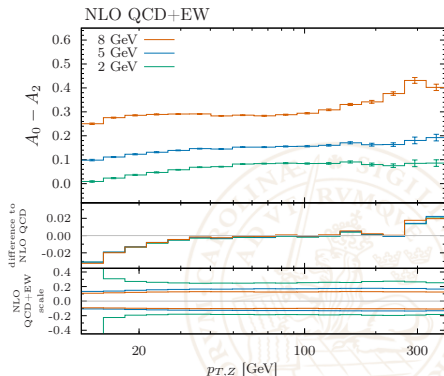
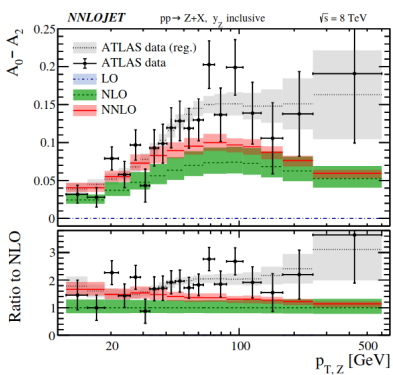
## Angular coefficients: results

- Lam-Tung relation  $A_0 - A_2$
- Difference rather than ratio as  $K$ -factor



## Angular coefficients: results

- Lam-Tung relation  $A_0 - A_2$
- Difference rather than ratio as  $K$ -factor
- Qualitative comparison to ATLAS data and NNLO QCD prediction<sup>10</sup>



<sup>10</sup>R. Gauld, et al., arXiv:1708.00008

## Summary

### Technical cut

$K$ -factors: negligible dependence on single lepton  $p_T$  cut  
Lam-Tung relation difference: no dependence on the cut

### Low- $p_T$ range

Found sizeable effect on the Lam-Tung relation for  $p_{T,Z} \lesssim 20$  GeV

### High- $p_T$ range

No electroweak effect for  $p_{T,Z} \gtrsim 20$  GeV  
→ electroweak logs are not expected to contribute largely

Thank you for listening!

