

# $|V_{us}|$ and Charge Lepton Universality from $\tau$ Decays



The banner features a central image of the Earth surrounded by several colored spheres representing particles: a red sphere labeled  $\tau$ , a purple sphere labeled  $\nu$ , a pink sphere labeled  $s$ , a cyan sphere labeled  $c$ , a yellow sphere labeled  $b$ , and a green sphere labeled  $t$ . On the left is a diamond-shaped logo with 'HQ' and 'L<sub>10</sub>'. On the right is the INFN logo. The text 'Heavy Quarks & Leptons' is written in a serif font, with 'INFN - Laboratori Nazionali di Frascati' and '11-15 October, 2010' below it.

Heavy Quarks & Leptons

INFN - Laboratori Nazionali di Frascati

11-15 October, 2010

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*On behalf of BaBar & Belle Collaborations*

*Email: [inugent@triumf.ca](mailto:inugent@triumf.ca)*



University  
of Victoria

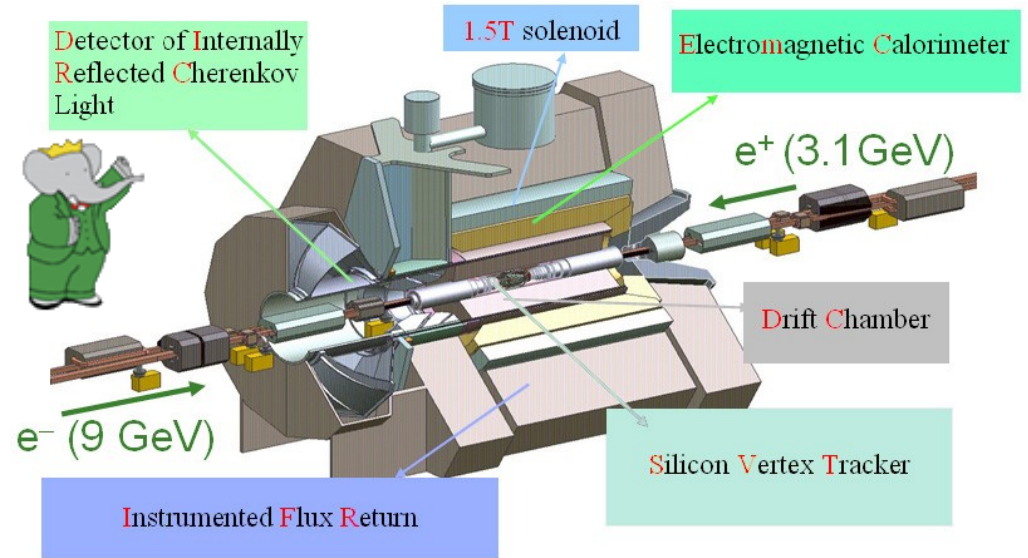
British Columbia  
Canada



# BaBar & BELLE Experiments

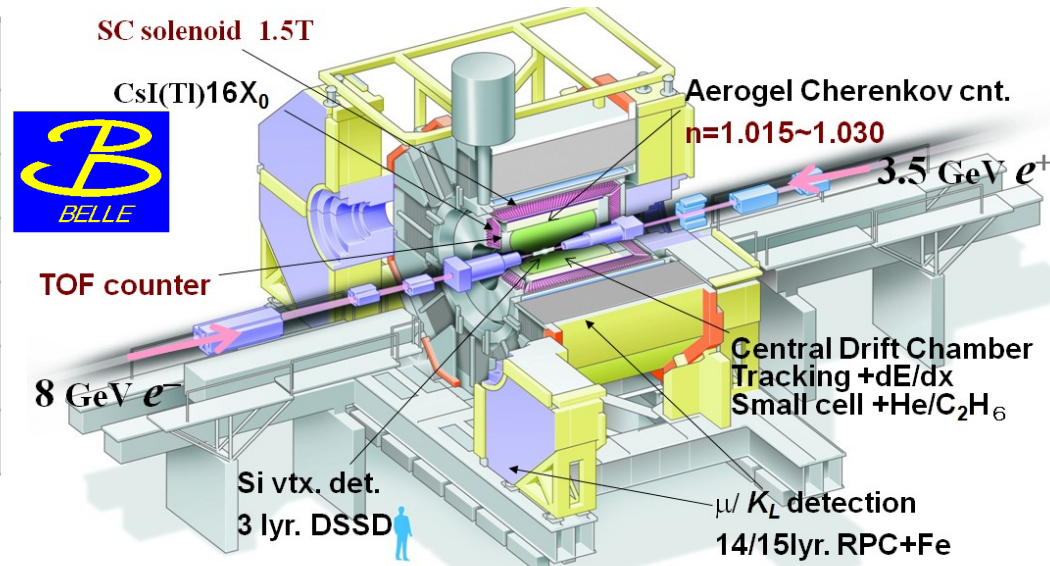
## Asymmetric Detectors

- Good Vertexing
- Good  $K/\pi$  Separation
- Good  $e, \mu$  Identification
- Good  $\gamma$  Detection/Resolution



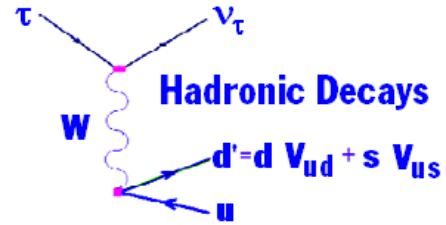
## High Luminosity.....

Decay Mode	Cross-Section (nb)
$\Upsilon(4s) \rightarrow B\bar{B}$	1.1
$\tau$ Pair	$0.919 \pm 0.003$
$q\bar{q}$ $q=u,d,s,c$	3.4
$\mu$ Pair	$1.147 \pm 0.005$
Two-Photon (Barrel)	2.4
Bhabha (Barrel)	25.52

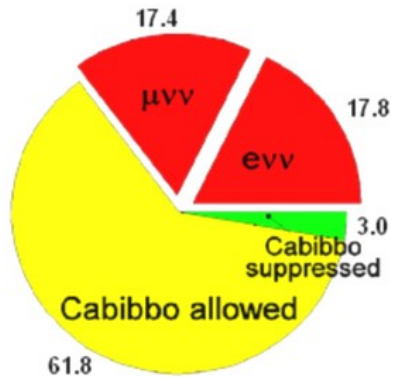


# Strange $\tau$ Decays

$$B_{\text{had}} = 1 - B_e - B_\mu$$



$$R_{\tau, \text{Strange}} = R_\tau - R_{\tau, \text{non-Strange}}$$



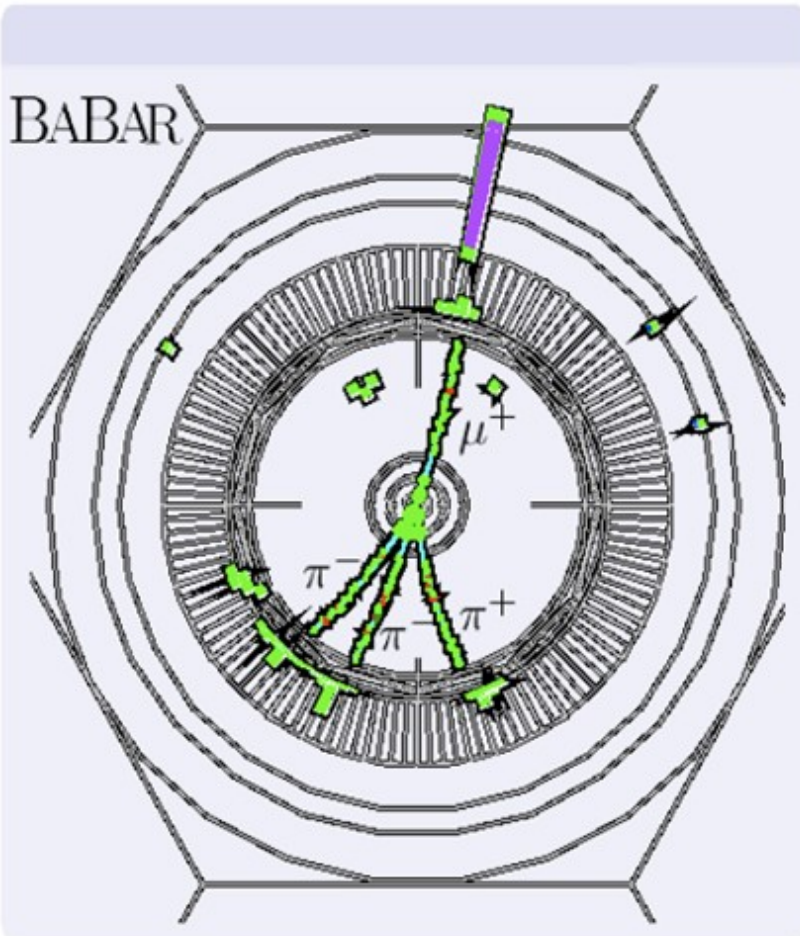
Decay Mode	BF (%)	Belle	BaBar
$K^-$	$0.697 \pm 0.010$		PRL 105, 051602 (2010)
$K^- \pi^0$	$0.431 \pm 0.015$		PRD-RC 76, 051104 (2007)
$K^- \pi^0 \pi^0$ (ex. $K^0$ )	$0.060 \pm 0.022$		
$K^- \pi^0 \pi^0 \pi^0$ (ex. $K^0, \eta$ )	$0.039 \pm 0.022$		
$K^0 \pi^-$	$0.831 \pm 0.018$	PLB 654, 65 (2007)	Prelim Nucl.Phys.Proc.Suppl.189 (2009) Prelim arXiv:0910.2884 [hep-ex]
$K^0 \pi^- \pi^0$	$0.350 \pm 0.015$		
$K^0 \pi^- \pi^0 \pi^0$	$0.031 \pm 0.023$		
$K^0 h^- h^+ h^-$	$0.029 \pm 0.020$		
$K^- \pi^- \pi^+$ (ex. $K^0$ )	$0.294 \pm 0.007$	PLB 672, 209 (2009)	PRL 100, 011801 (2008)
$K^- \pi^- \pi^+ \pi^0$ (ex. $K^0, \eta$ )	$0.078 \pm 0.012$		
$K^- \eta$	$0.016 \pm 0.001$	PLB 672, 209 (2009)	
$K^- \eta \pi^0$	$0.005 \pm 0.001$	PLB 672, 209 (2009)	
$K^0 \eta \pi^-$	$0.009 \pm 0.001$	PLB 672, 209 (2009)	
$K^- K^+ K^-$	$0.0024 \pm 0.0008$	PLB 643, 5-10 (2006)	PRL 100, 011801 (2008)
$K^- K^0 K^0$	$0.0015 \pm 0.0001$	estimated from $K^- K^+ K^-$ ( $\tau \rightarrow K^- \phi \nu$ saturates $\tau \rightarrow K^- K^+ K^- \nu$ )	
<b>Total</b>	<b><math>2.9155 \pm 0.0510</math></b>	<b>Error depends on correlations</b>	
BF from HFAG constrained fit $\chi^2/\text{d.o.f.} = 135.2/115$ CL=9.6% HFAG: arXiv:1010.1589			

**Cross Section at  $\Upsilon(4s)$**   
 $\sigma(\tau^+ \tau^-) = (0.919 \pm 0.003) \text{ nb}$   
**Phys. Rev. D 77, 054012 (2008)**

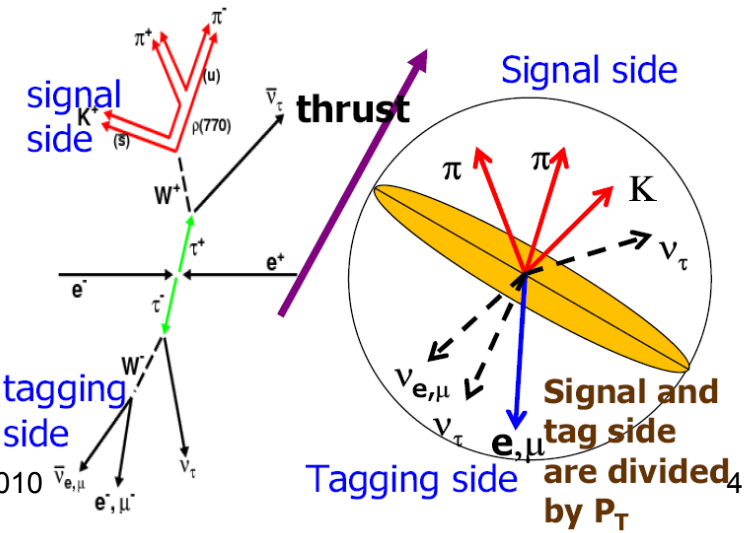
**Belle**  $\mathcal{L} = 1 \text{ ab}^{-1} \Rightarrow \sim 10 \times 10^8 \tau \text{ Pairs}$   
**BaBar**  $\mathcal{L} = 531 \text{ fb}^{-1} \Rightarrow \sim 5 \times 10^8 \tau \text{ Pairs}$

# Hadronic $\tau$ Decays at B-Factories

$\tau$ -Pair Signature:  
**Leptonic+Hadronic** Decay



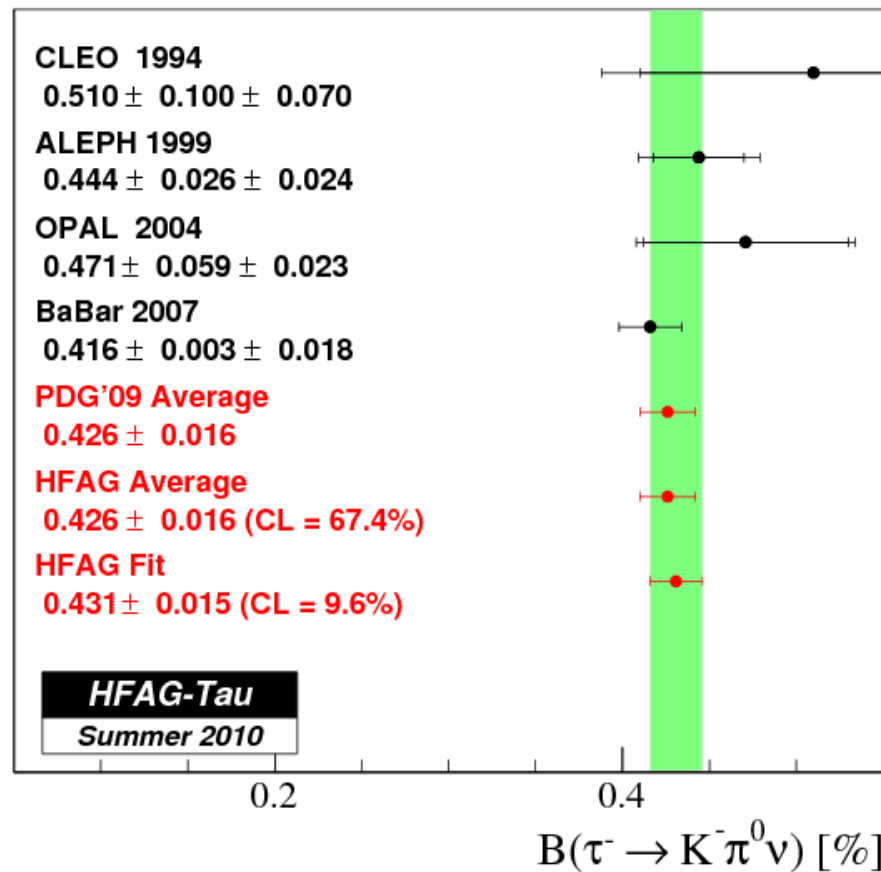
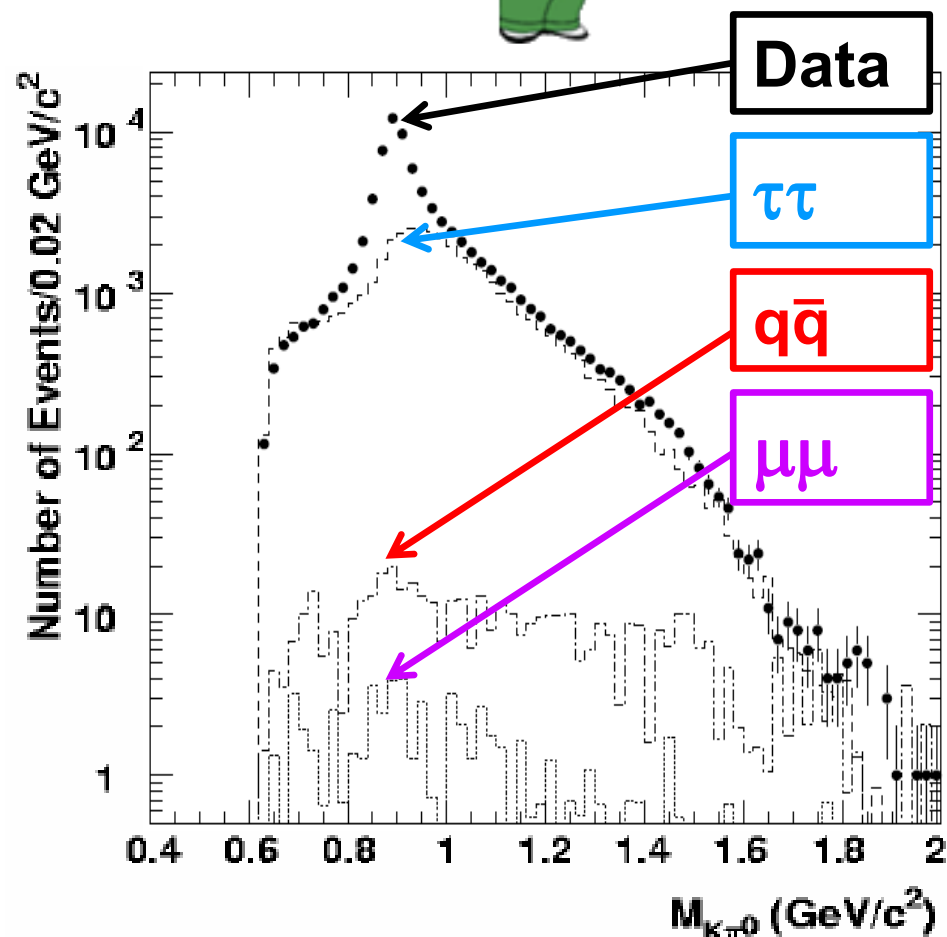
Backgrounds	Discriminates
Bhabha, di-muons	Lepton Momentum Multiplicity Conversion veto $\cos(\theta)$
Two-Photon	Missing Transverse Momentum Missing Mass $\cos(\theta^{Miss})$ Thrust Total Reconstructed Energy
$e^+e^- \rightarrow qq$ $q=u,d,s,c,b$	Thrust Invariant mass Multiplicity
Other $\tau$ decays	$K/\pi$ separation Neutral Identification: $\pi^0, \eta, \gamma$



$$\tau \rightarrow K^- \pi^0 \nu$$



## BaBar-PRD 76:051104 (2007)



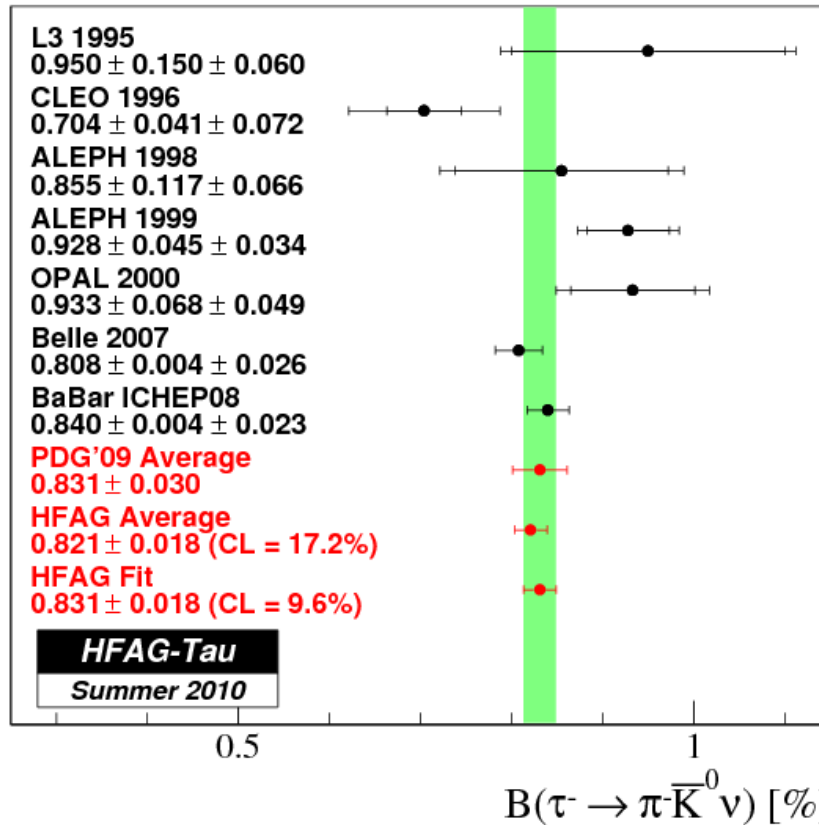
# $\tau \rightarrow K_S^0 \pi^- \nu$ and $\tau \rightarrow K_S^0 \pi^- \pi^0 \nu$



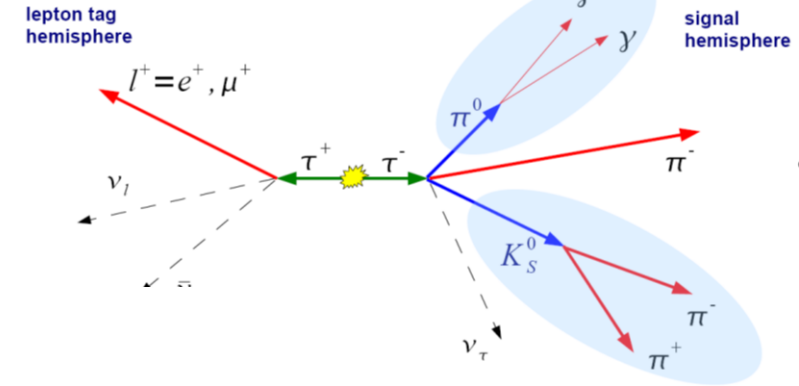
Belle-PLB 654, 65 (2007)



BaBar-prelim  
Nucl.Phys.Proc.Suppl.189 (2009)



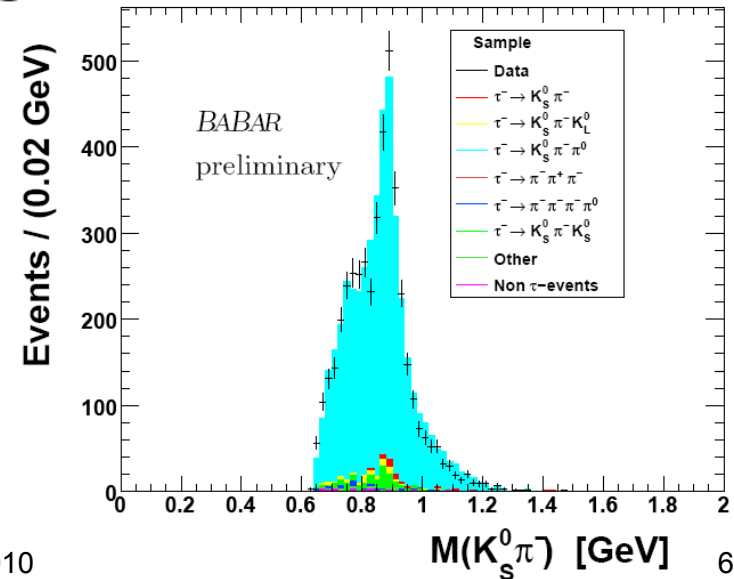
Selected event topology



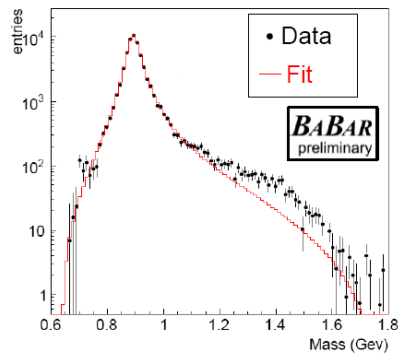
drawing in CMS



$B(\tau \rightarrow K_S^0 \pi^- \pi^0 \nu) = [0.342 \pm 0.006 \pm 0.015]\%$   
BaBar-prelim arXiv:0910.2884 [hep-ex]



# $\tau \rightarrow K_S^0 \pi^- \nu$



Fit model:

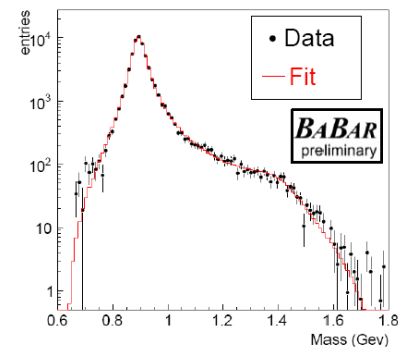
$K^*(892)$

$Mass(K^*(892)) = 894.54 \pm 0.17 \pm 0.19 \text{ MeV}$

$Width(K^*(892)) = 47.67 \pm 0.44 \pm 0.57 \text{ MeV}$

$\chi^2/ndf = 399.8/97$

$Prob. < 0.0001$



Fit model:

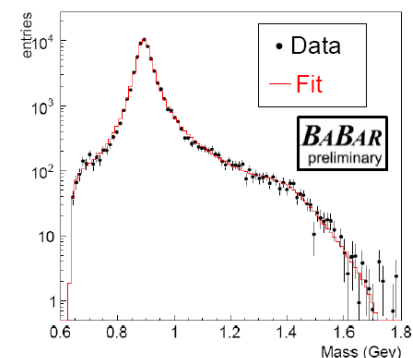
$K^*(892) + K^*(1410)$

$Mass(K^*(892)) = 894.41 \pm 0.19 \pm 0.19 \text{ MeV}$

$Width(K^*(892)) = 46.21 \pm 0.46 \pm 0.57 \text{ MeV}$

$\chi^2/ndf = 130.0/95$

$Prob. = 0.0098$



$K^*(800)$  mass and width  
from BES collaboration  
(Phys.Lett.B633:681-690,2006)

Fit model:

$K^*(892) + K^*(1410) + K^*(800)$

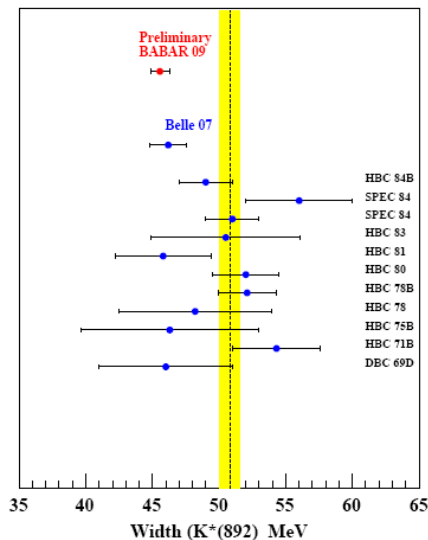
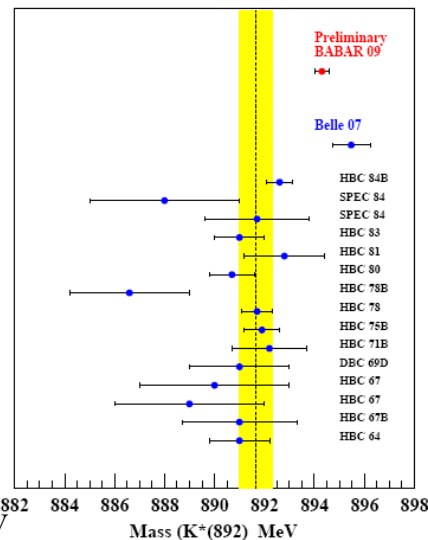
$Mass(K^*(892)) = 894.57 \pm 0.19 \pm 0.19 \text{ MeV}$

$Width(K^*(892)) = 45.89 \pm 0.43 \pm 0.57 \text{ MeV}$

$\chi^2/ndf = 113.0/94$

$Prob. = 0.0880$

Best fit



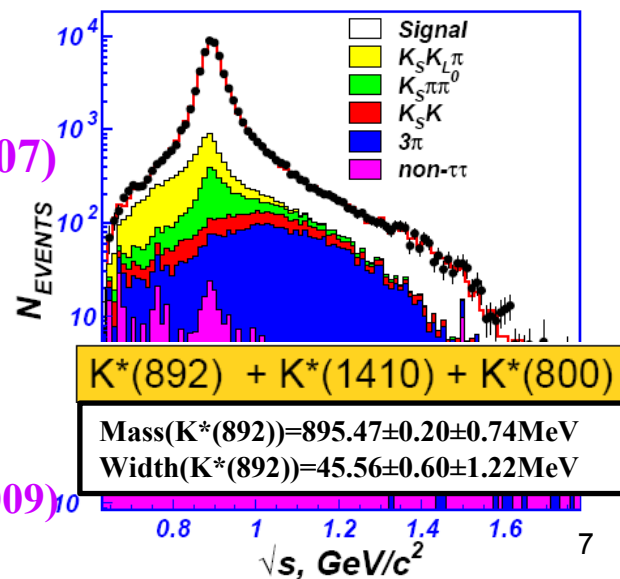
Belle-PLB 654, 65 (2007)



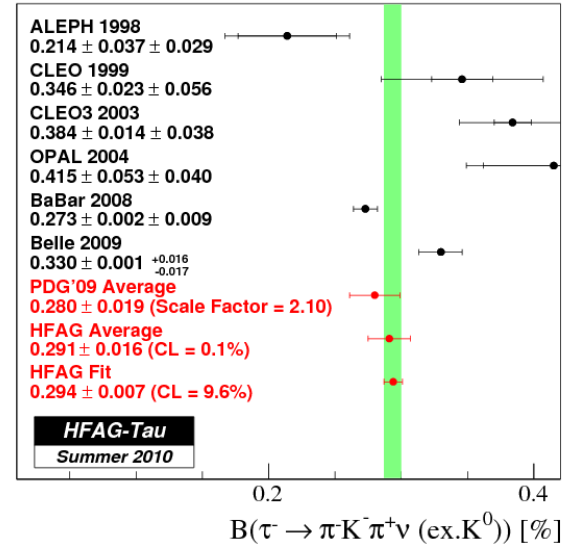
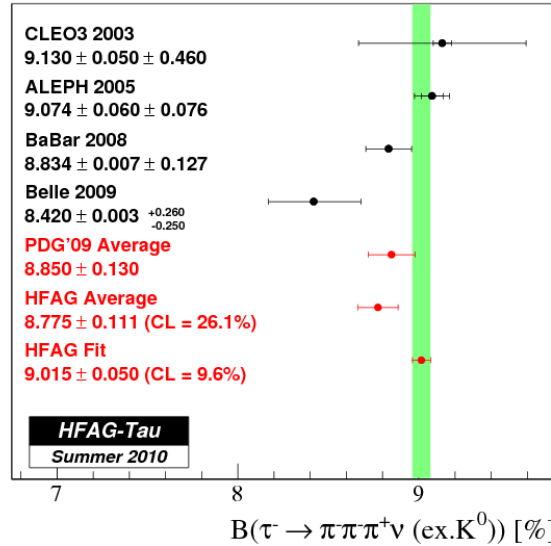
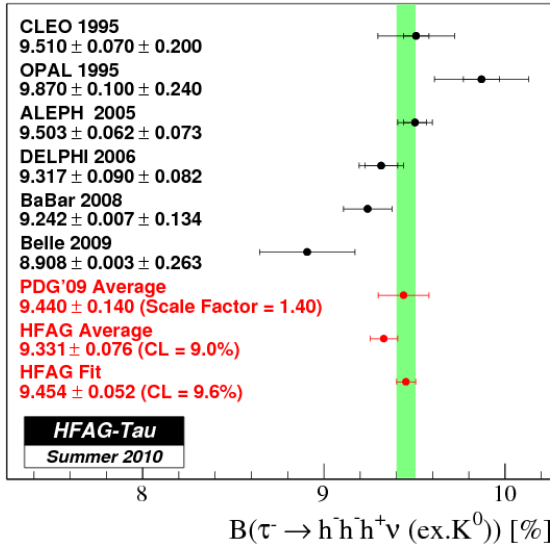
BaBar-prelim

Nucl.Phys.Proc.Suppl.189 (2009)

Heavy Quark & Lepton 2010



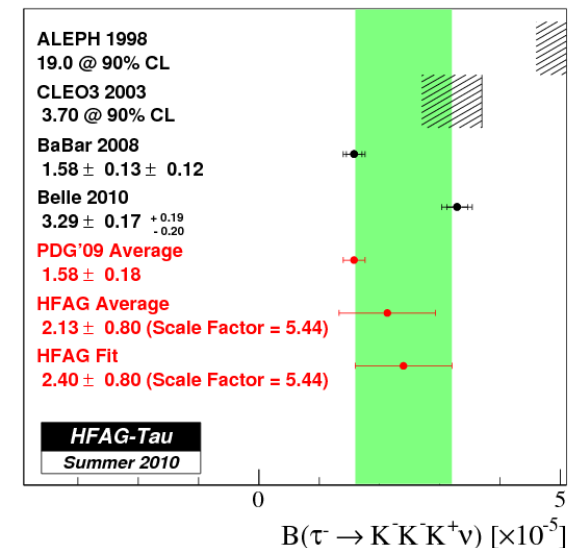
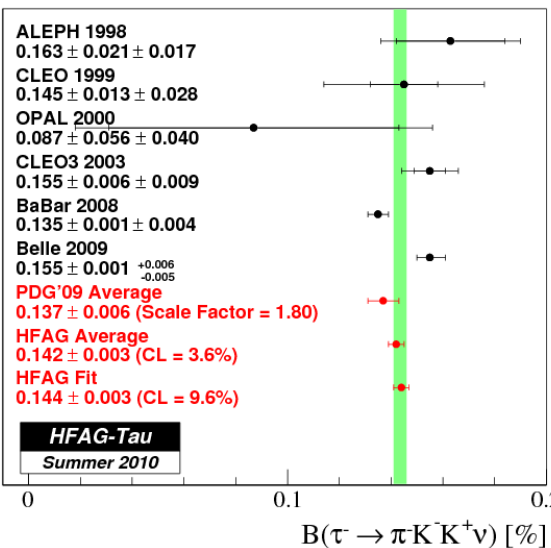
# $\tau \rightarrow K^- \pi^+ \pi^0 \nu$ and $\tau \rightarrow K^- K^+ K^0 \nu$



Belle-PLB 672, 209 (2009)

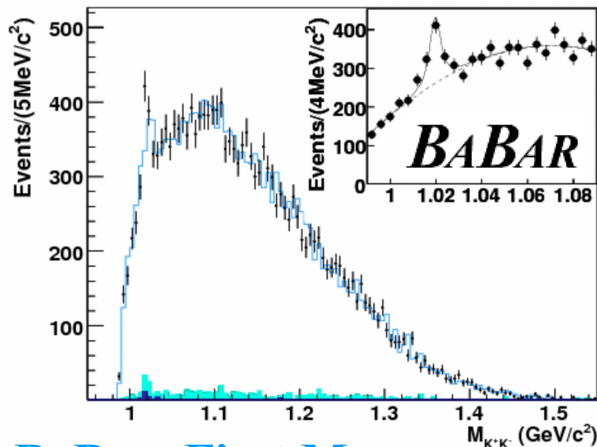


BaBar-PRL100, 011801 (2008)



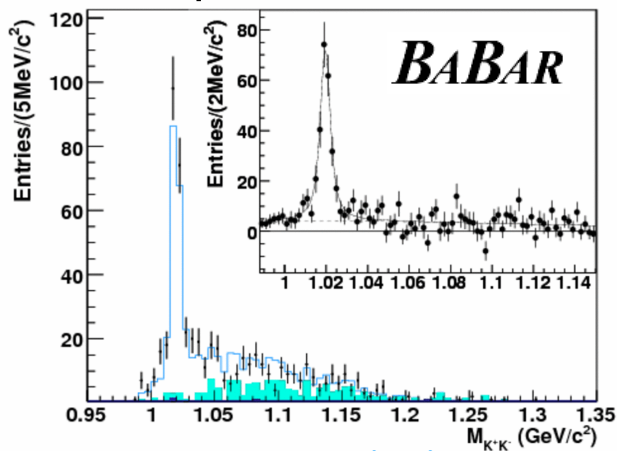


# $\tau \rightarrow K^- K^- K^+ \nu$ and $\tau \rightarrow K^- \phi \nu$



**BaBar: First Measurement**

$$B(\tau \rightarrow \pi^- \phi \nu) = (3.42 \pm 0.55 \pm 0.25) \times 10^{-5}$$



**BaBar: Upper Limit**

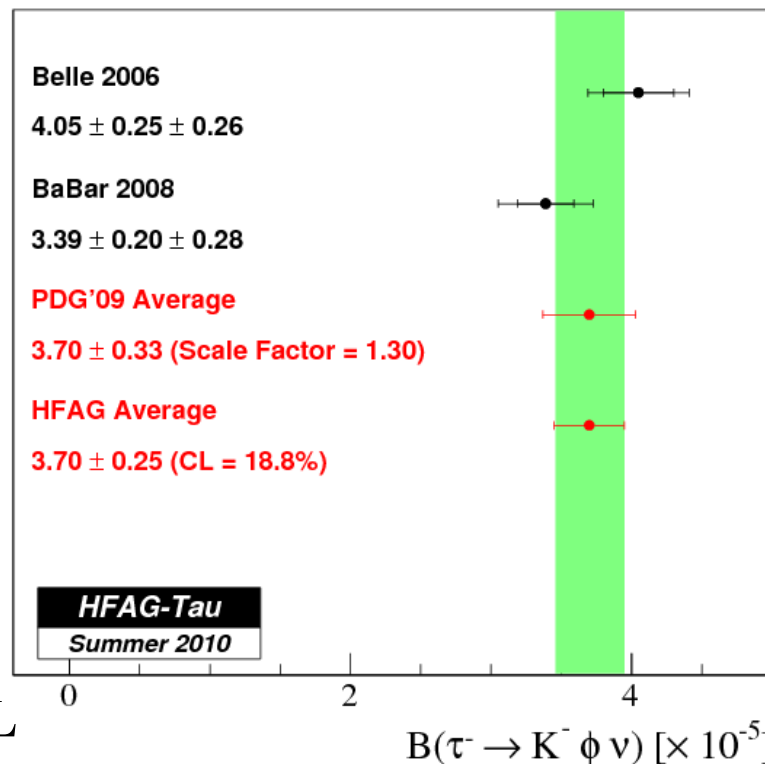
$$B(\tau \rightarrow K^- K^- K^+ \nu [\text{ex. } \phi]) < 0.25 \times 10^{-5} \text{ @ 90\% CL}$$



Belle-Phys.Lett.B643:5-10,2006



BaBar-PRL100, 011801 (2008)



# $\tau \rightarrow K^- \pi^- \pi^+ \nu$ and $\tau \rightarrow K^- K^- K^+ \nu$



$$\sum_i A_{ij} x_i = b_j$$

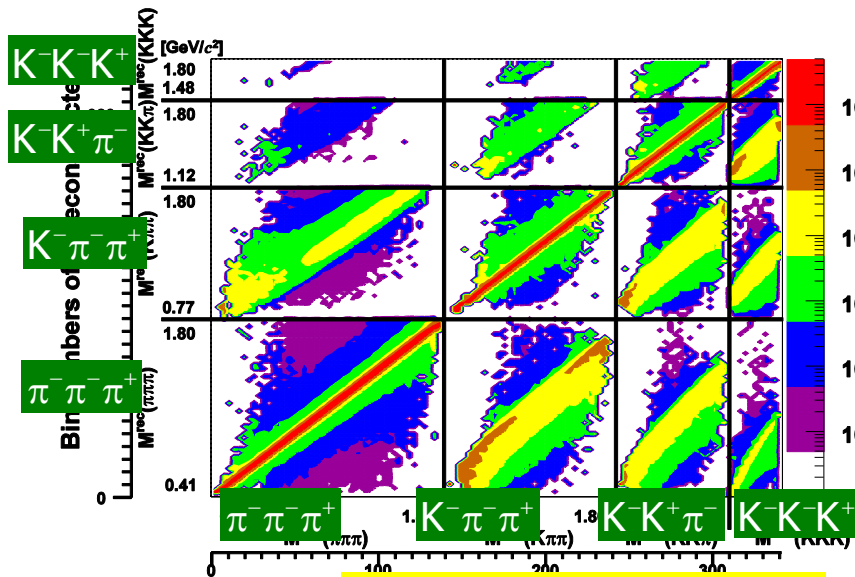
Belle-PLB 672, 209 (2009)

Grey line: Unfolded spectrum

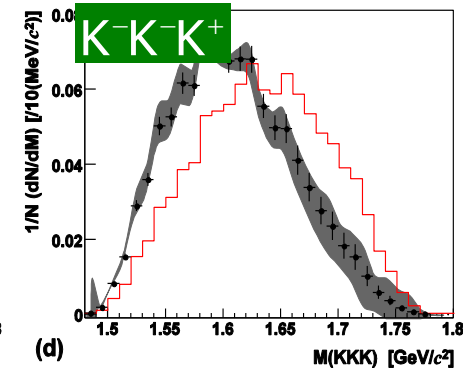
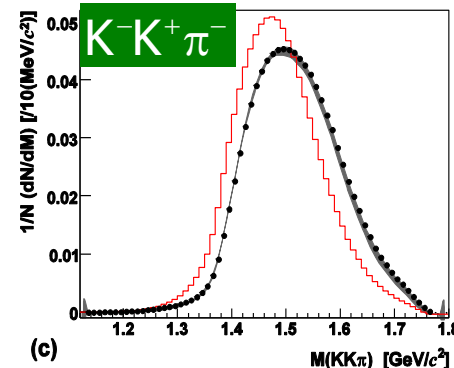
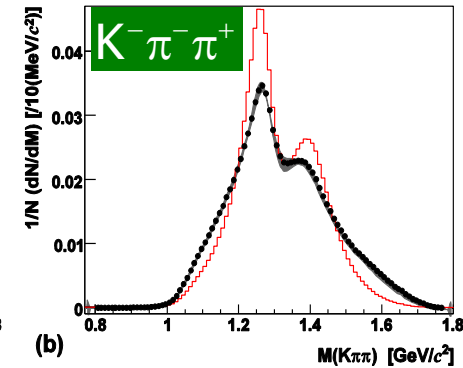
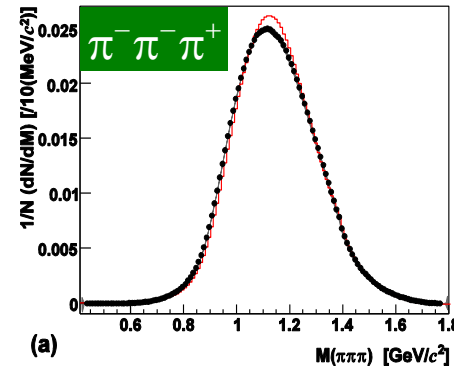
Histogram: Tauola

The inverse of A is obtained by **Singular Value Decomposition Technique**.  
 $A_{ij}$ : Response matrix  
 $x_i$ : Unfolded spectrum  
 $b_j$ : Observed spectrum

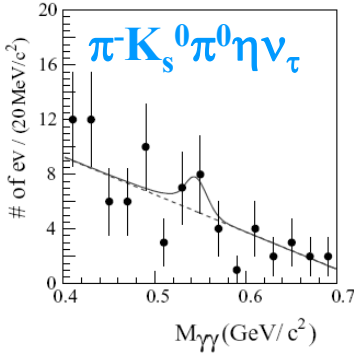
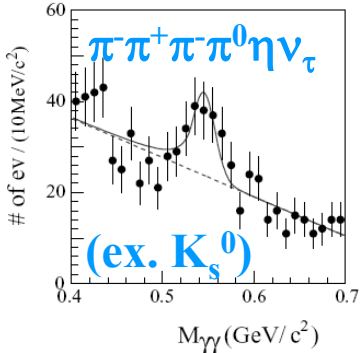
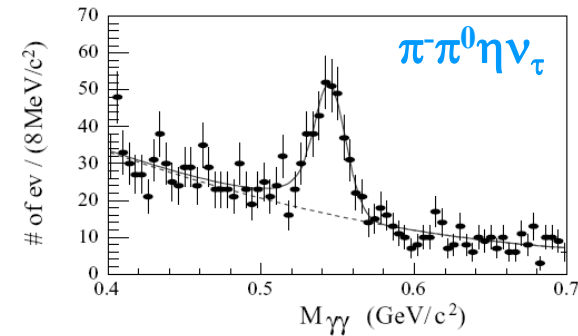
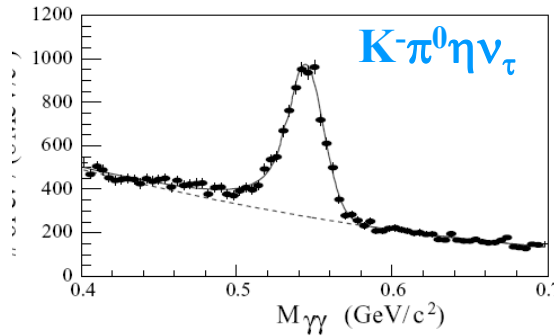
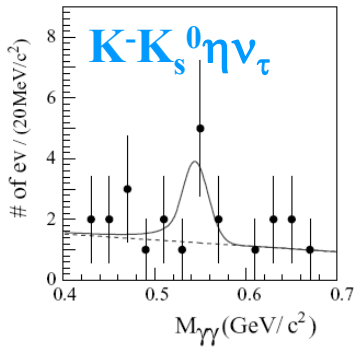
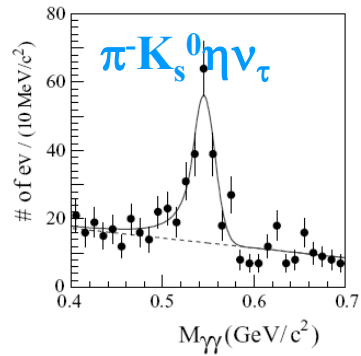
measured mass bin j



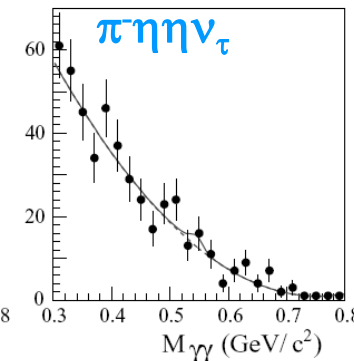
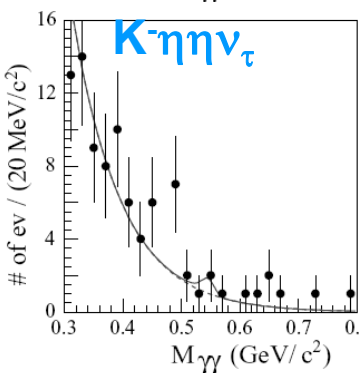
generated mass bin i



# Strange $\tau$ Decays with a $\eta$



Belle-Phys. Lett. B672, 209 (2009)

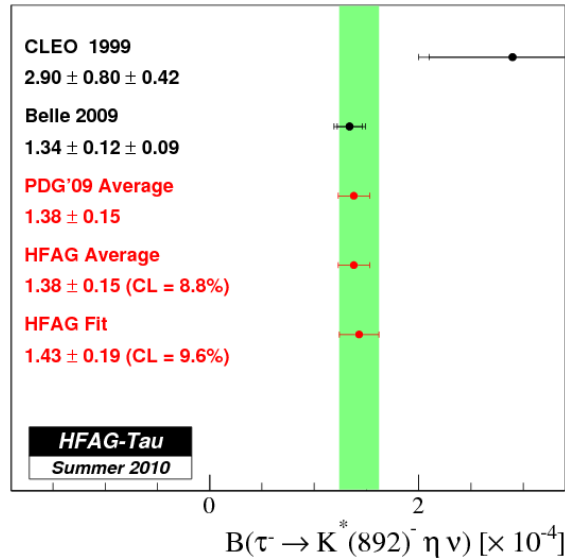
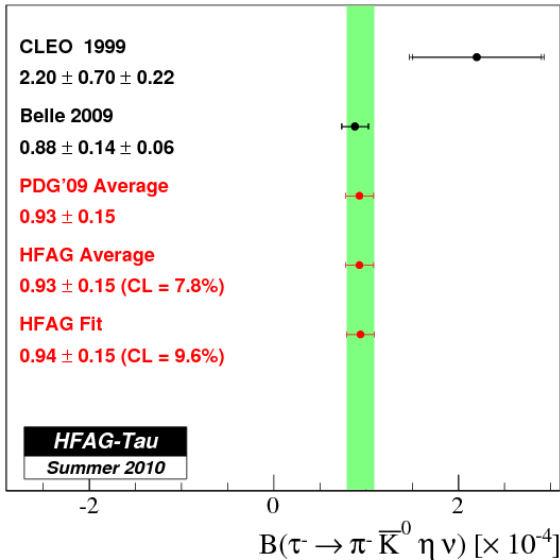
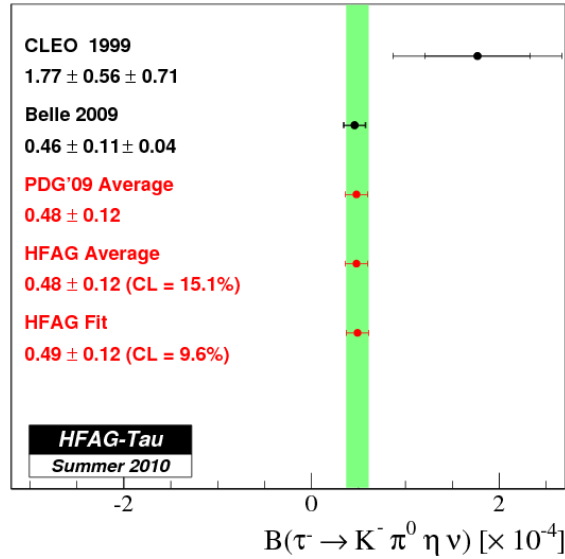
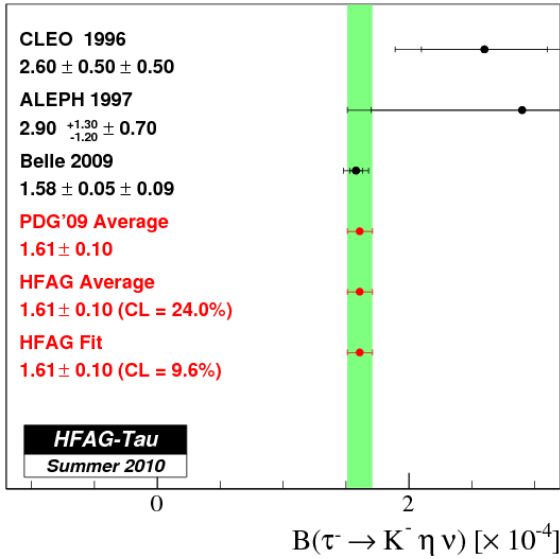


Decay Mode

BF ( $10^{-4}$ )

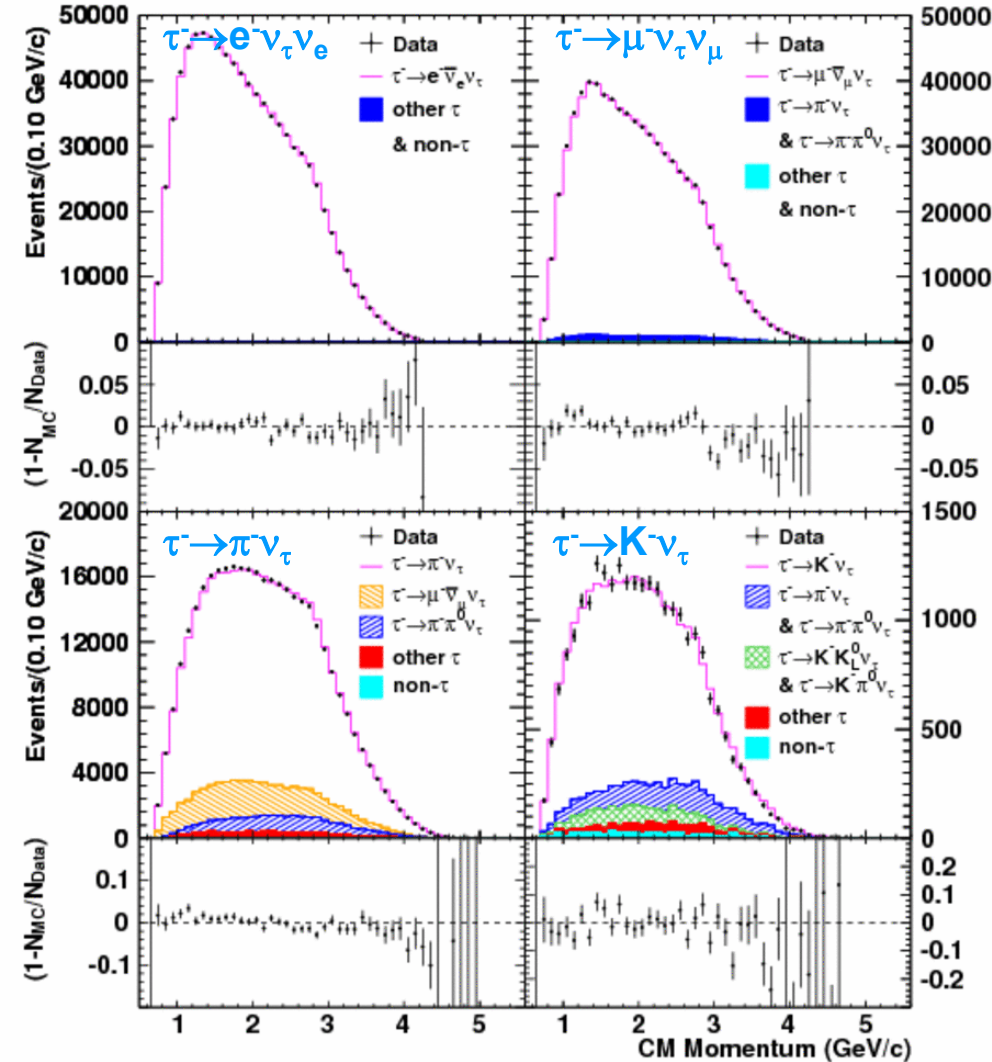
$\pi \pi^0 \eta \nu_\tau$	$13.5 \pm 0.3 \pm 0.7$
$K^- \eta \nu_\tau$	$1.58 \pm 0.05 \pm 0.09$
$K^- \pi^0 \eta \nu_\tau$	$0.46 \pm 0.11 \pm 0.04$
$\pi K_s^0 \eta \nu_\tau$	$0.44 \pm 0.07 \pm 0.03$
$K^* \eta \nu_\tau$	$1.34 \pm 0.12 \pm 0.09$
$\pi K_s^0 \pi^0 \eta \nu_\tau$	$< 0.25$ @90%CL
$\pi \eta \eta \nu_\tau$	$< 0.074$ @90%CL
$K^- K_s^0 \pi^0 \eta \nu_\tau$	$< 0.045$ @90%CL
$K^- \eta \eta \nu_\tau$	$< 0.03$ @90%CL

# Strange $\tau$ Decays with a $\eta$



Belle  
Phys. Lett. B672, 209 (2009)

# 1 Prong $\tau$ Decays



BaBar-Phys. Rev. Lett. 105:051602, 2010

$$R_X = \frac{B(\tau^- \rightarrow X^- \nu_\tau)}{B(\tau^- \rightarrow e^- \nu_e \nu_\tau)}$$

$$R_\mu = 0.9796 \pm 0.0016 \pm 0.0036$$

$$R_\pi = 0.5945 \pm 0.0014 \pm 0.0061$$

$$R_K = 0.03882 \pm 0.00032 \pm 0.00057$$

Major Systematic Uncertainties:

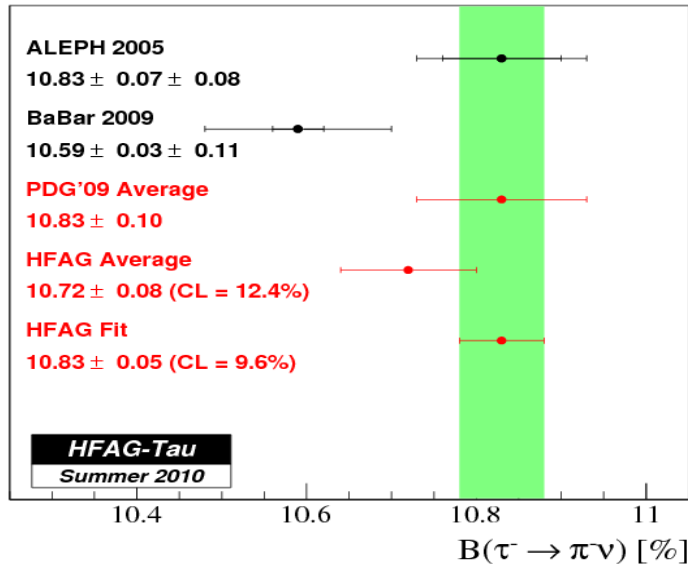
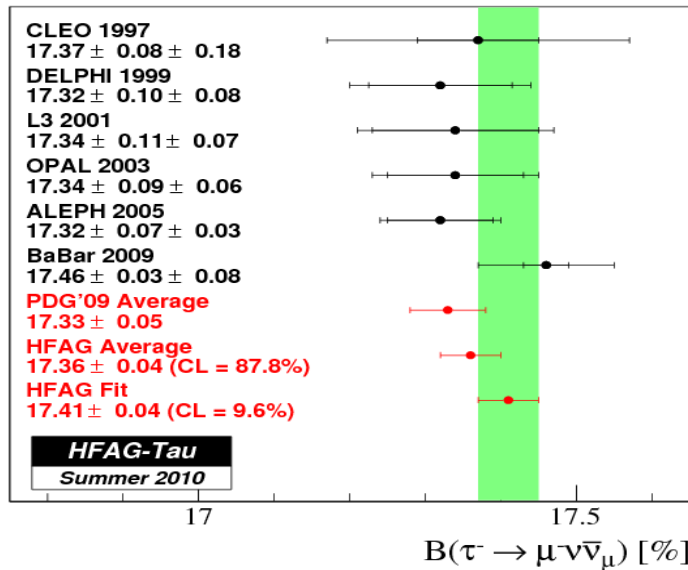
Particle ID

Detector Response

Backgrounds



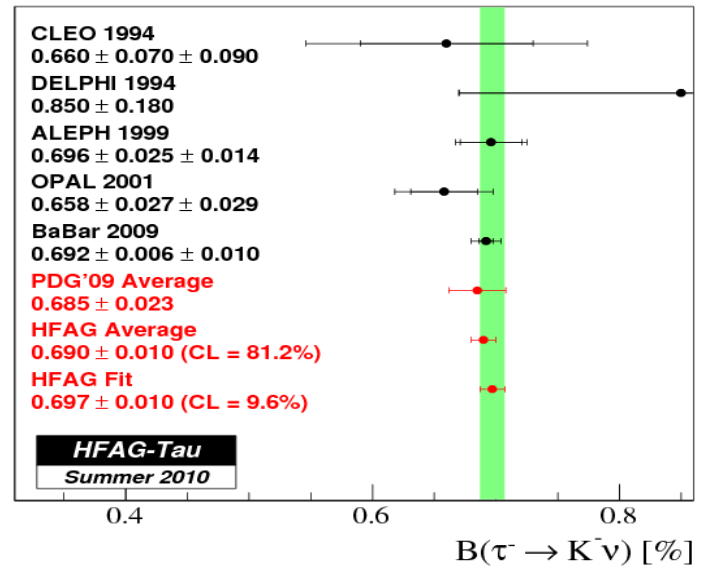
# 1 Prong $\tau$ Decay



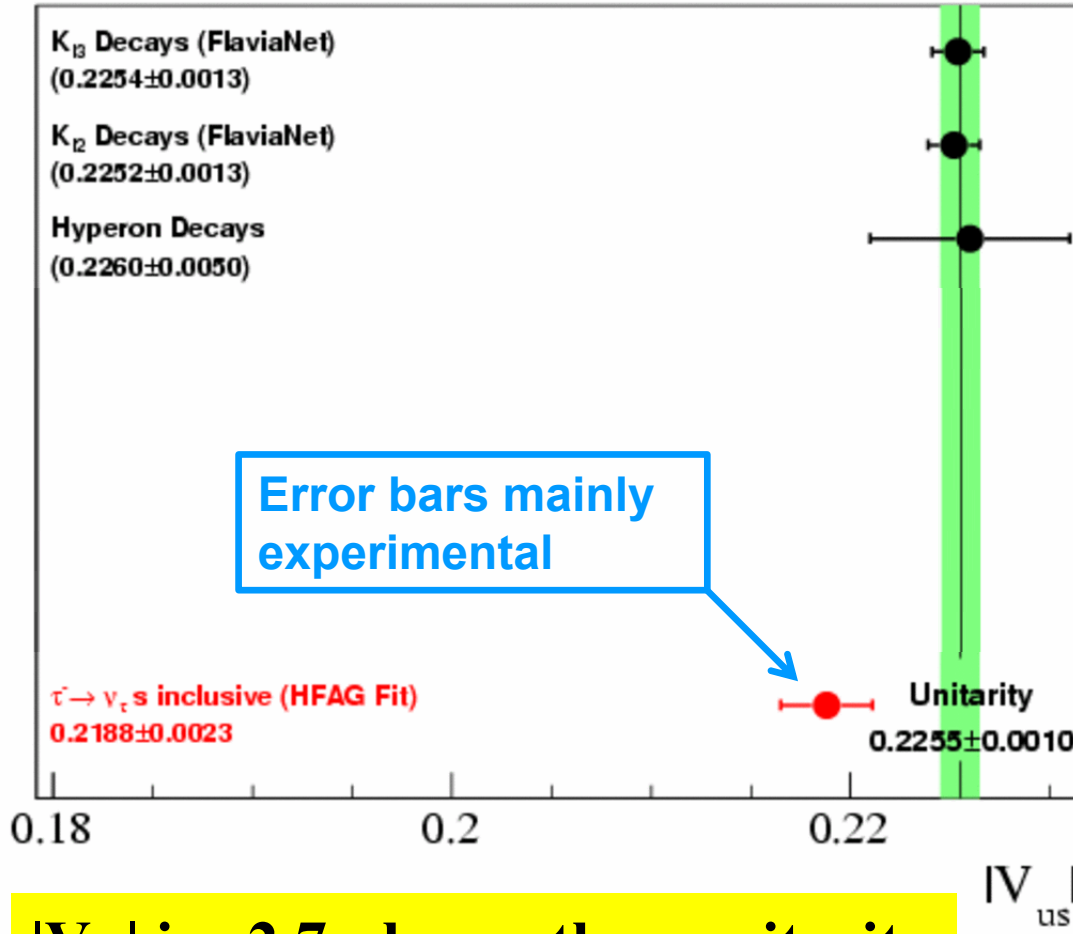
**BaBar**

**Phys. Rev. Lett. 105:051602, 2010**

Branching fraction based on:  
 $B(\tau^- \rightarrow e^- \nu_\tau \nu_e) = (17.82 \pm 0.05)\%$   
**PDG2008**



# $|V_{us}|$ from $\tau$ 's using FESR



$|V_{us}|$  is  $\sim 2.7\sigma$  lower than unitarity

$$R_\tau = \frac{\Gamma(\tau^- \rightarrow \text{hadrons}^- \nu_\tau(\gamma))}{\Gamma(\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau(\gamma))} = R_{\tau, \text{non-strange}} + R_{\tau, \text{strange}}$$

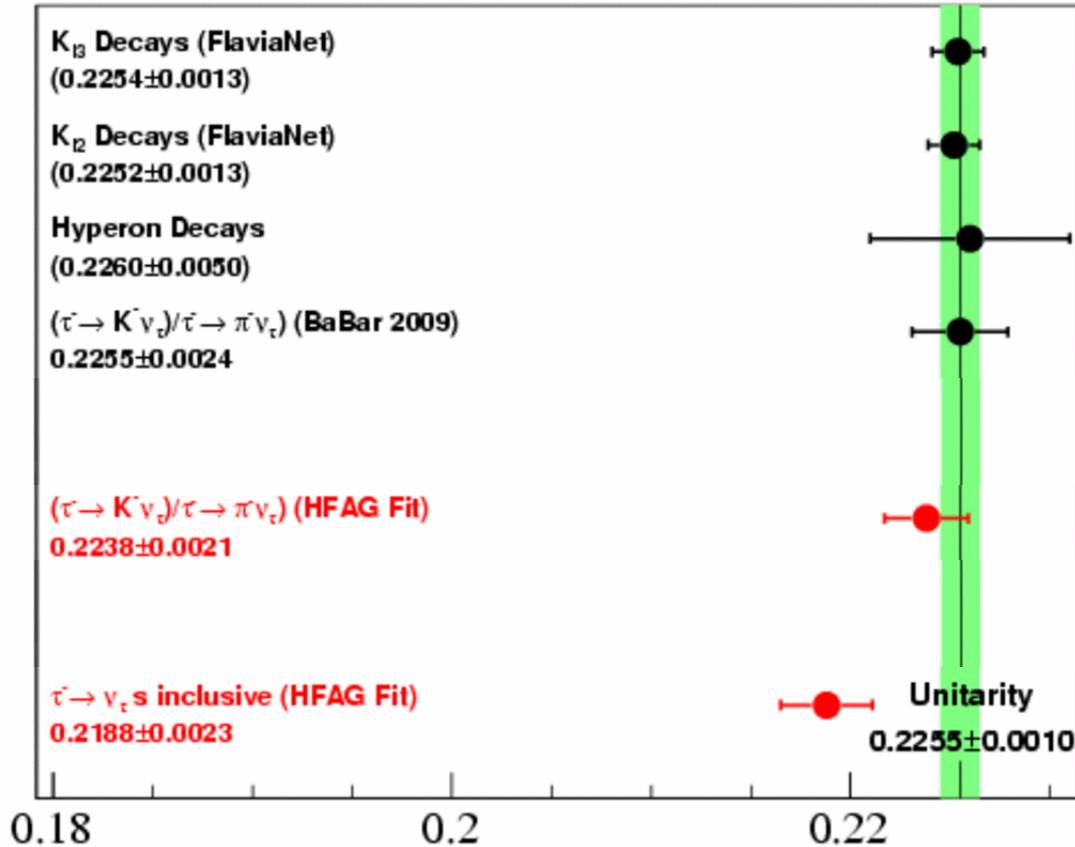
The branching fractions and invariant mass distributions are the experimental input to determine

$$|V_{us}|^2 = \frac{R_{\tau, \text{strange}}^w}{R_{\tau, \text{non-strange}}^w / |V_{ud}|^2 - \delta R_\tau^w}$$

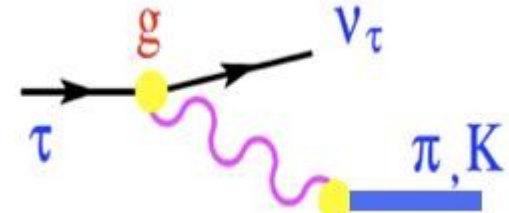
$|V_{ud}|$  is well measured from measured from superallowed beta decays

The  $\delta R_\tau^w$  is determined from theory (using the Operator Product Expansion [OPE] and compared to experiment with the Finite Energy Sum Rule [FESR]).

# $|V_{us}|$ from $\tau^- \rightarrow K^- \nu_\tau / \tau^- \rightarrow \pi^- \nu_\tau$



$|V_{us}|$  is  $\sim 0.6\sigma$  lower than unitarity



$$\frac{B(\tau^- \rightarrow K^- \nu_\tau)}{B(\tau^- \rightarrow \pi^- \nu_\tau)} = \frac{f_K^2 |V_{us}|^2 (1 - m_K^2 / m_\tau^2)^2}{f_\pi^2 |V_{ud}|^2 (1 - m_\pi^2 / m_\tau^2)^2}$$

$f_K/f_\pi$  taken from Lattice QCD.

$$f_K/f_\pi = 1.189 \pm 0.007$$

E. Follana, et al. PRL 100, 062002 (2008)

$|V_{ud}|$  measured from super allowed beta decays .

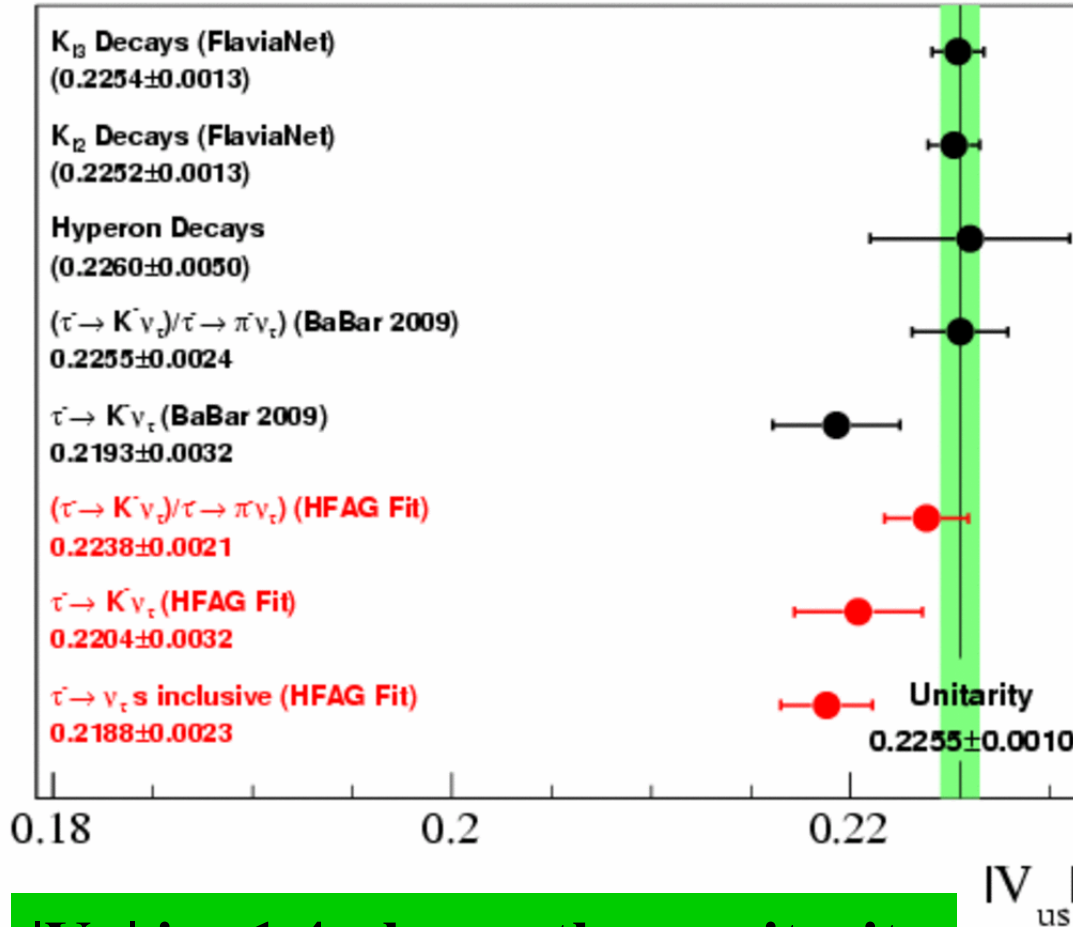
$$|V_{ud}| = 0.97408 \pm 0.00026$$

T. Eronen, et al. PRL 100, 132502 (2008)

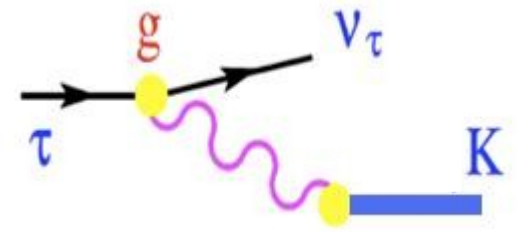
J. C Hardy, I. S. Towner, Nucl. Phys. News 16N4, 11 (2006).



# $|V_{us}|$ from $\tau^- \rightarrow K^- \nu_\tau$



$|V_{us}|$  is  $\sim 1.4\sigma$  lower than unitarity

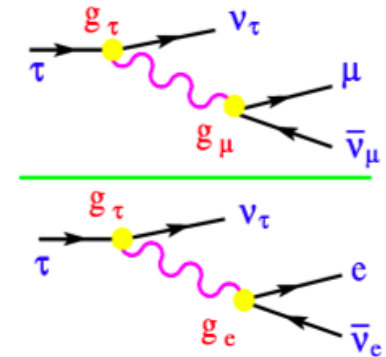
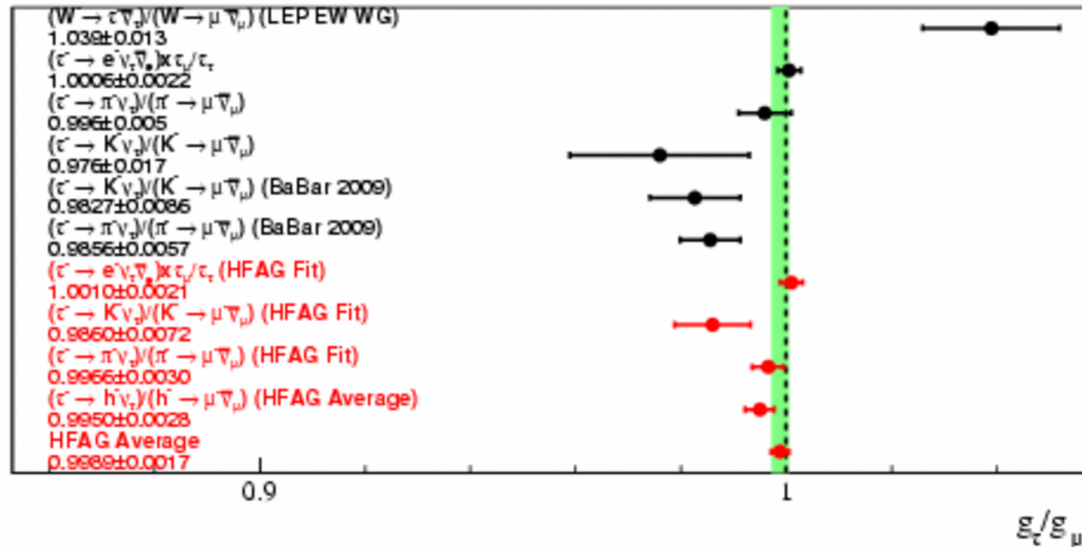
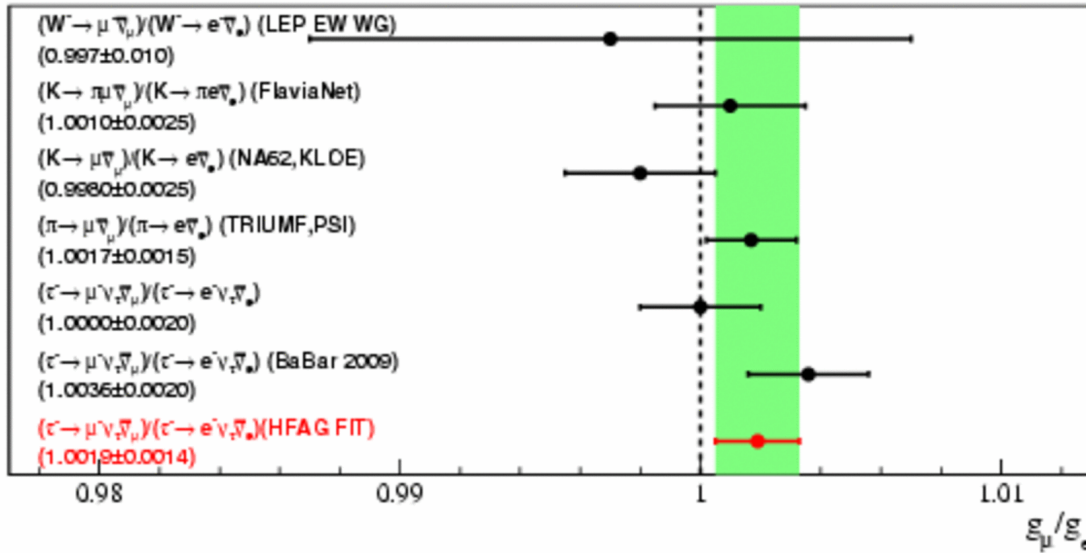


$$B(\tau \rightarrow K \nu) = \frac{G^2 \tau_\tau m_\tau^3 f_K^2 S_{EW} |V_{us}|^2}{16\pi\hbar} (1 - m_K^2 / m_\tau^2)^2$$

$f_K$  taken from .  
 $f_K = 157 \pm 2$  MeV from Lattice QCD  
 E. Follana, et al. PRL 100, 062002 (2008)

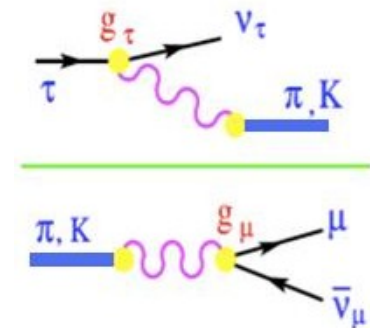
$S_{EW} = 1.0201 \pm 0.0003$   
 J. Erler, Rev. Mex. Fis. 50, 200 (2004).

# Charged Lepton Universality



$$\left(\frac{g_\mu}{g_e}\right)^2 = \frac{B(\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau) f(m_e^2 / m_\tau^2)}{B(\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau) f(m_\mu^2 / m_\tau^2)}$$

$$f(x) = 1 - 8x + 8x^3 - x^4 + 12x^2 \log x$$



$$\left(\frac{g_\tau}{g_\mu}\right)^2 = \frac{B(\tau^- \rightarrow h^- \nu_\tau) 2m_h m_\mu^2 \tau_h (1 - m_\mu^2 / m_h^2)}{B(h^- \rightarrow \mu^- \nu_\tau) (1 + \delta_h) m_\tau^3 \tau_\tau (1 - m_h^2 / m_\tau^2)}$$

Radiative corrections:

$$\delta_\pi = (0.16 \pm 0.14)\% \quad \delta_K = (0.90 \pm 0.22)\%$$

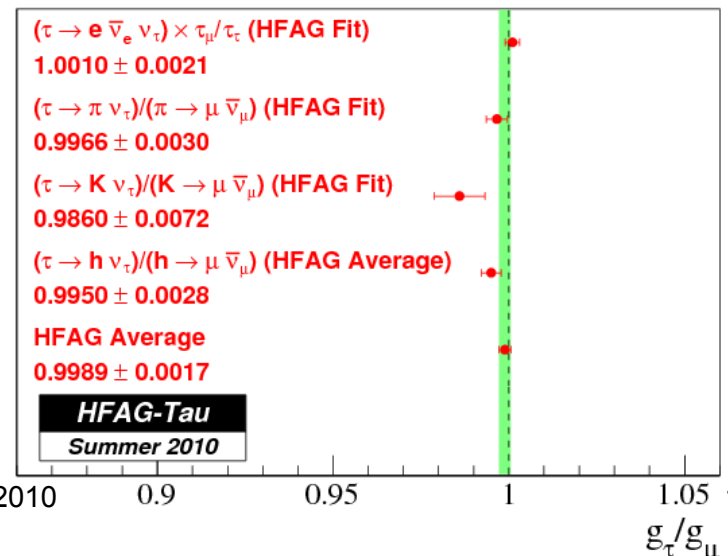
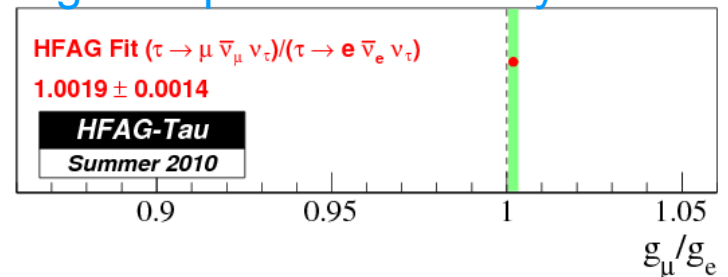
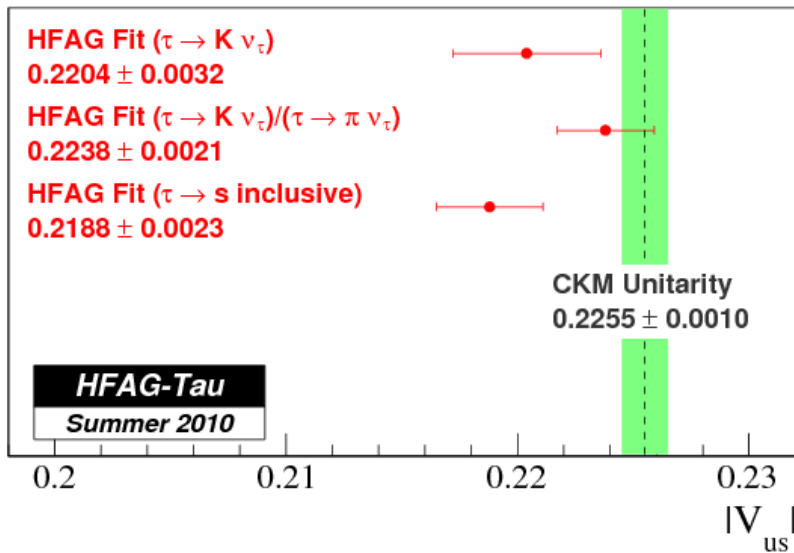
# Summary

In summary BaBar & Belle have measured 9 of the main  $\tau$  strange branching fractions.



The results have been combined with previous  $\tau$  measurements to extract:  $|V_{us}|$  extracted from  $\tau$ 's

Charged Lepton Universality from  $\tau$ 's



HFAG: arXiv:1010.1589