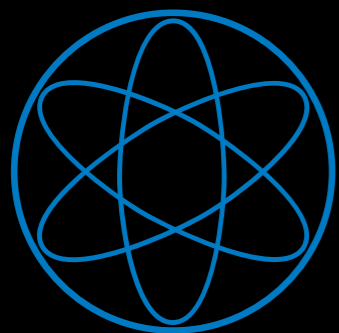


**NORA BRAMBILLA**

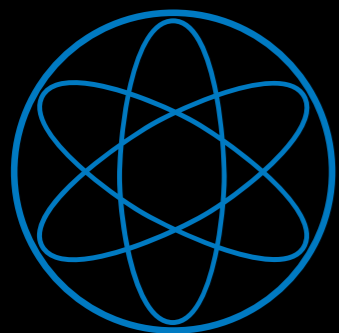


# Recent developments in heavy quarkonium theory:



**NORA BRAMBILLA**

# Recent developments in heavy quarkonium theory: an Effective Field Theory Perspective



**NORA BRAMBILLA**





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#### Heavy quarkonium: progress, puzzles, and opportunities

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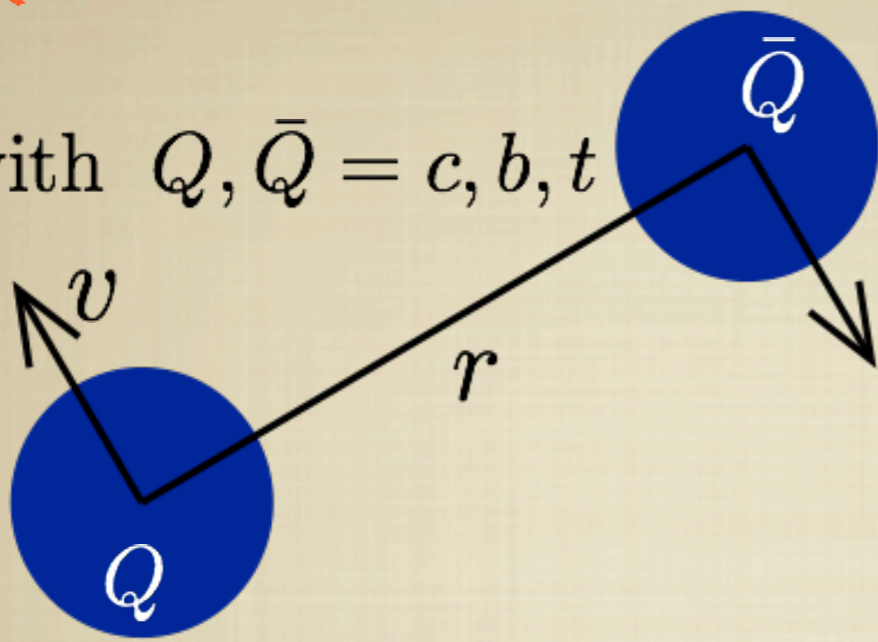
it contains:

Spectroscopy,  
Decay,  
Production,  
Quarkonium  
in media,  
Beyond the  
standard  
model



# Quarkonium

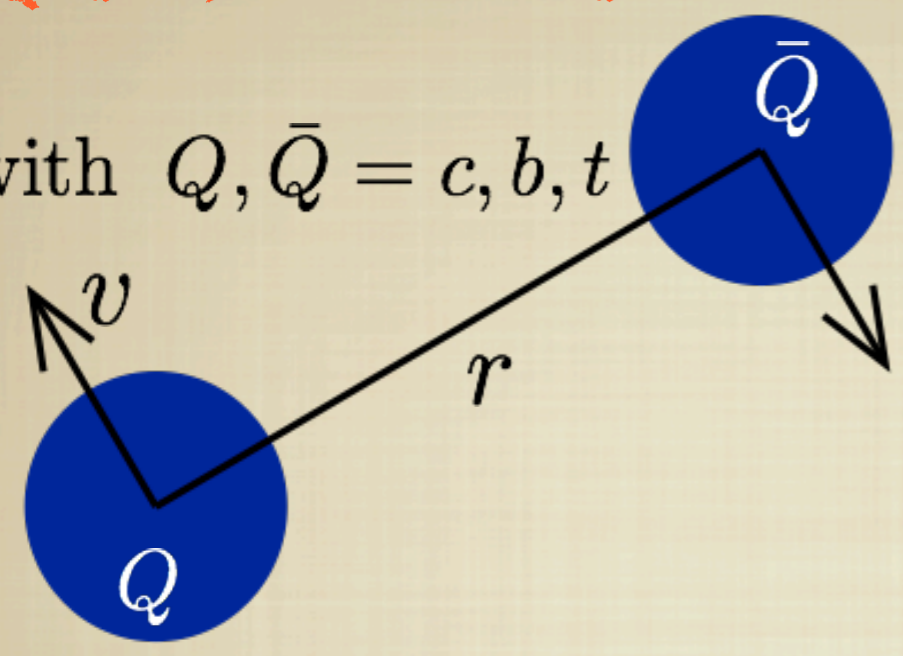
with  $Q, \bar{Q} = c, b, t$





Quarkonium is an ideal system to study strong interactions

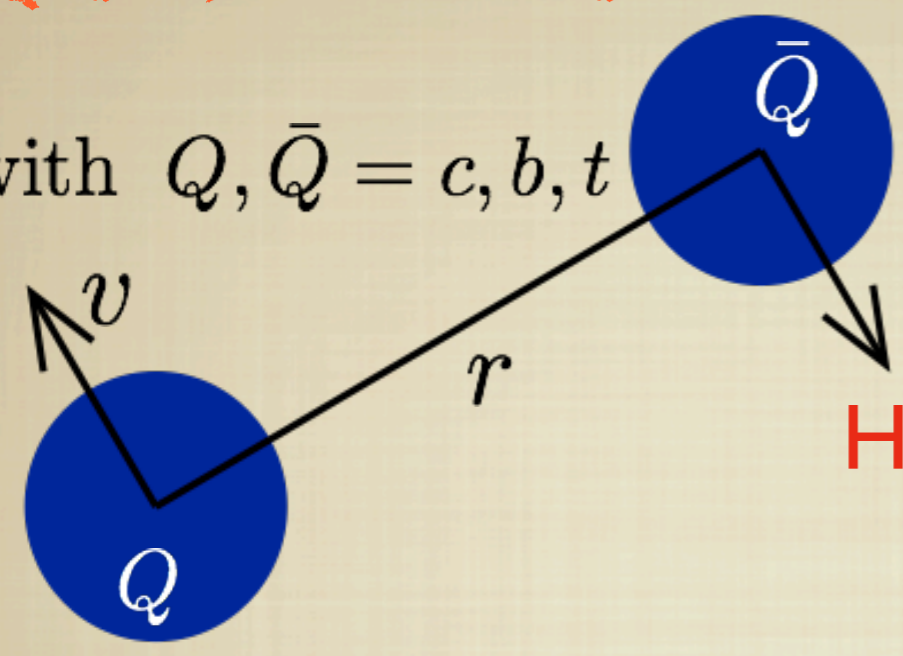
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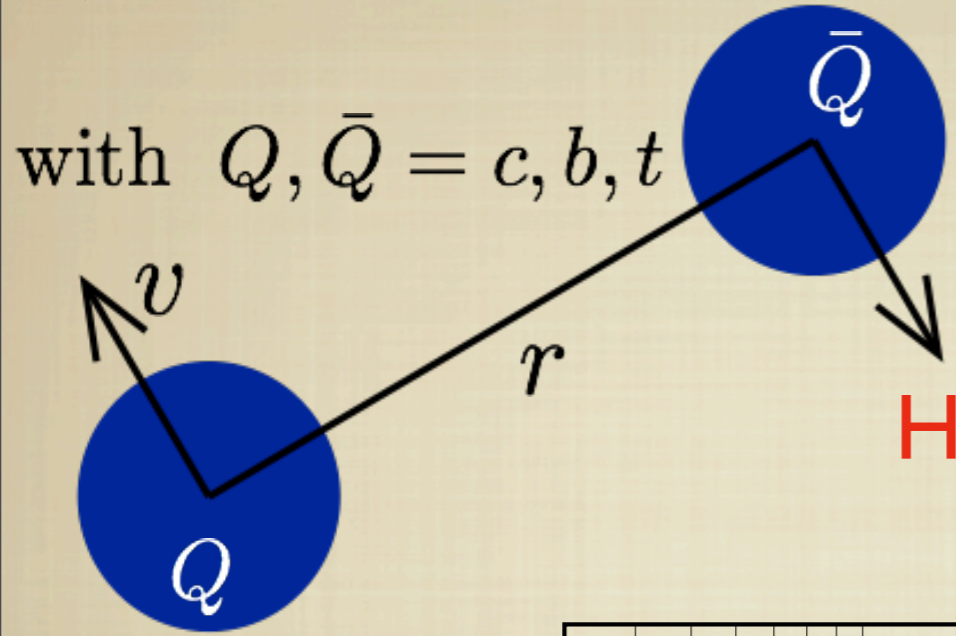
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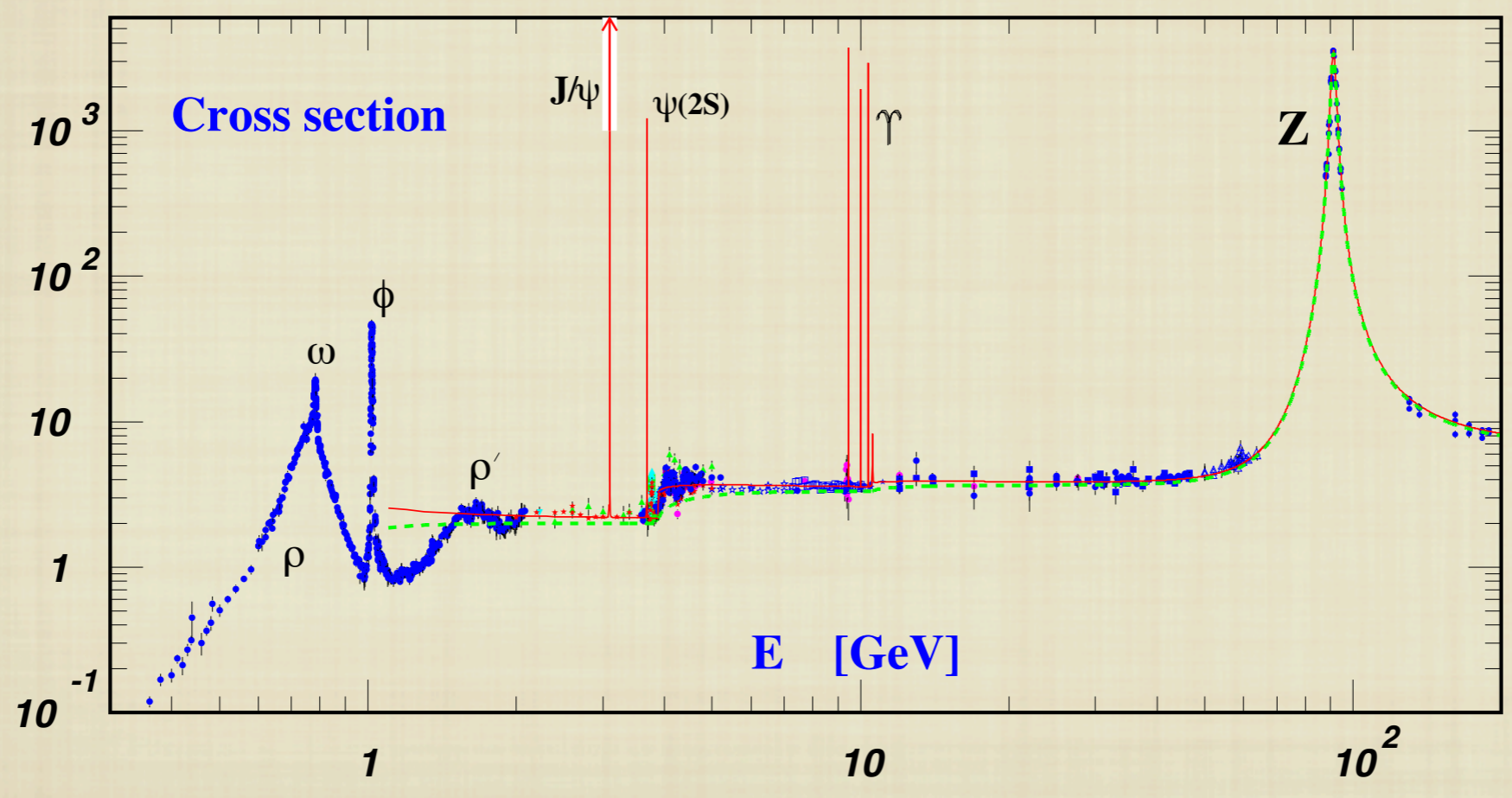
Heavy quarks offer a privileged access



# Quarkonium is an ideal system to study strong interactions

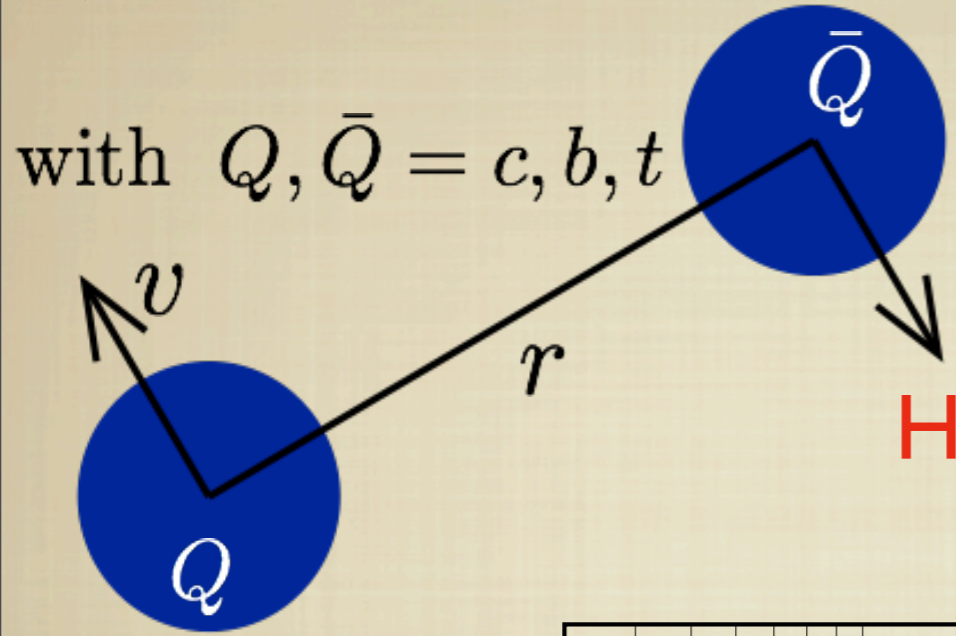


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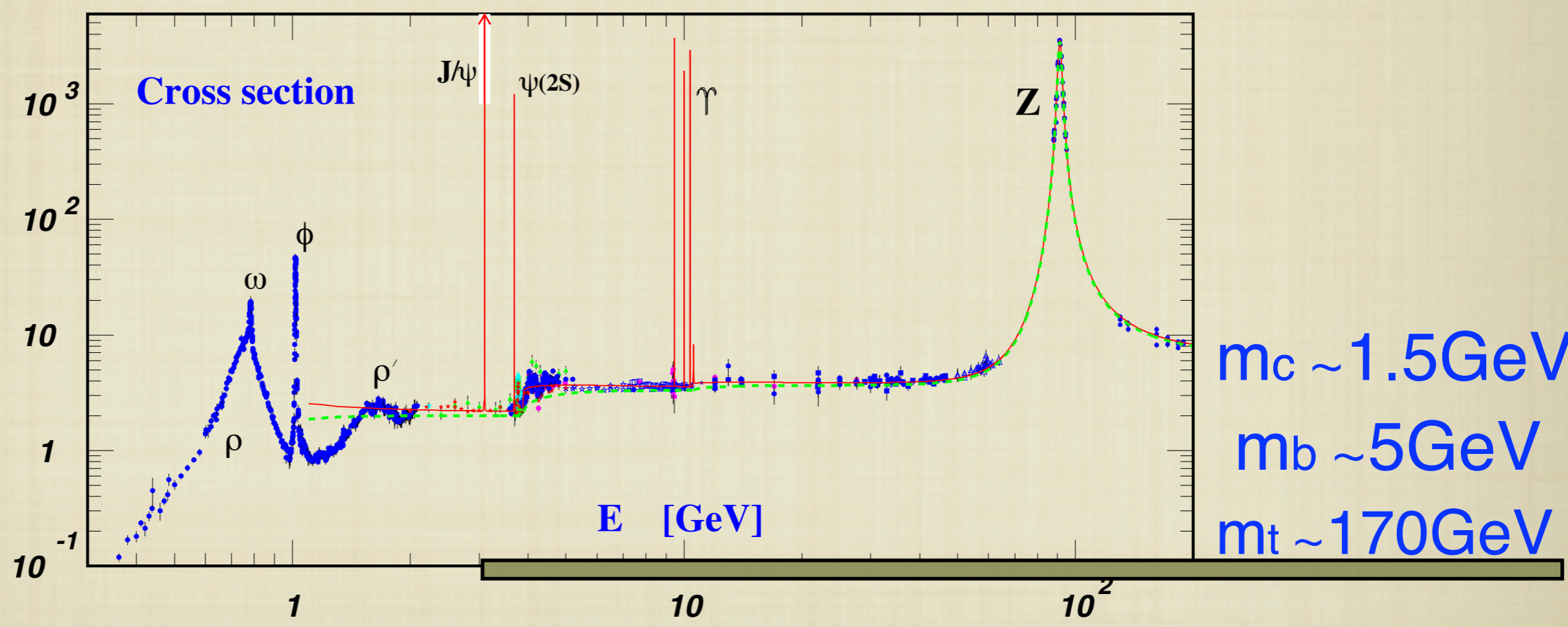




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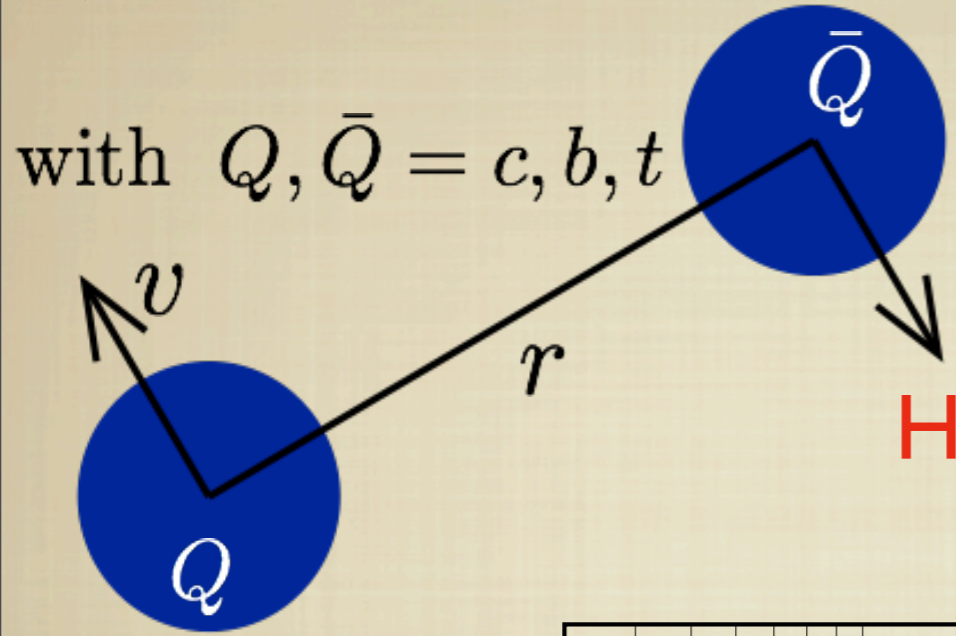


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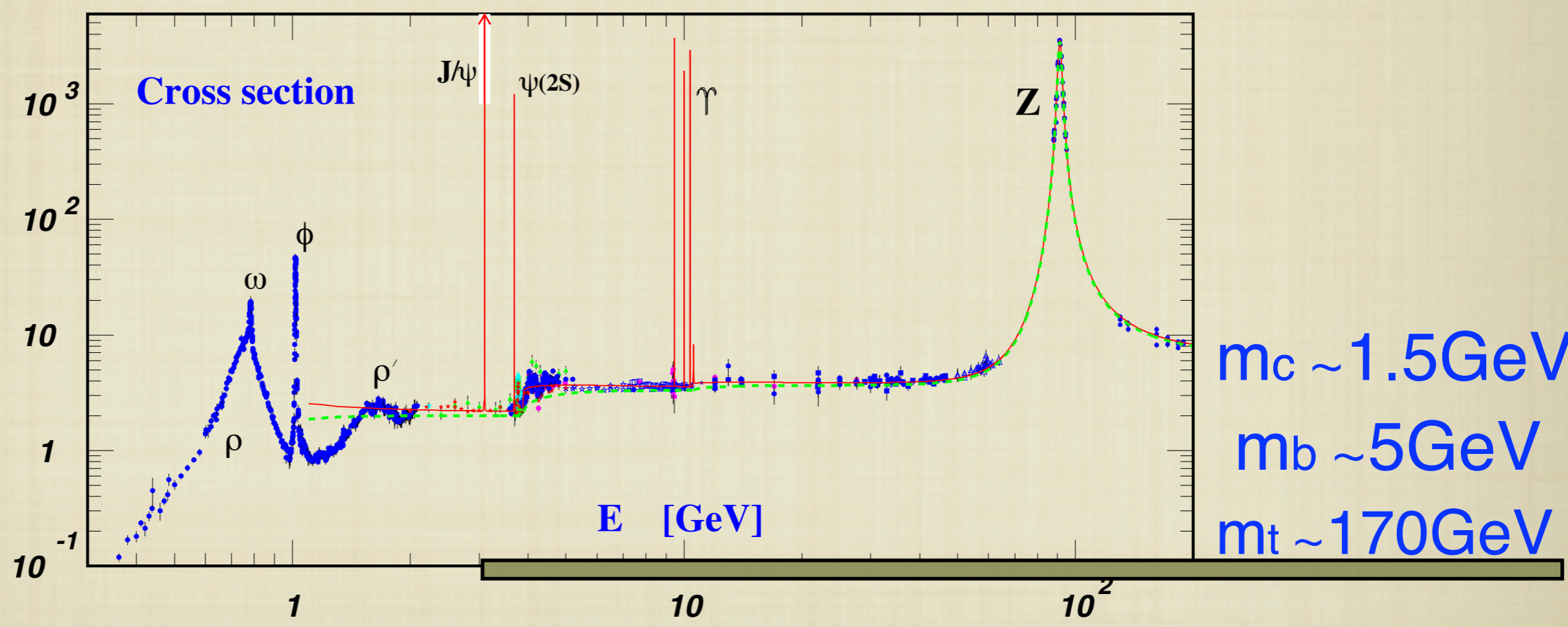




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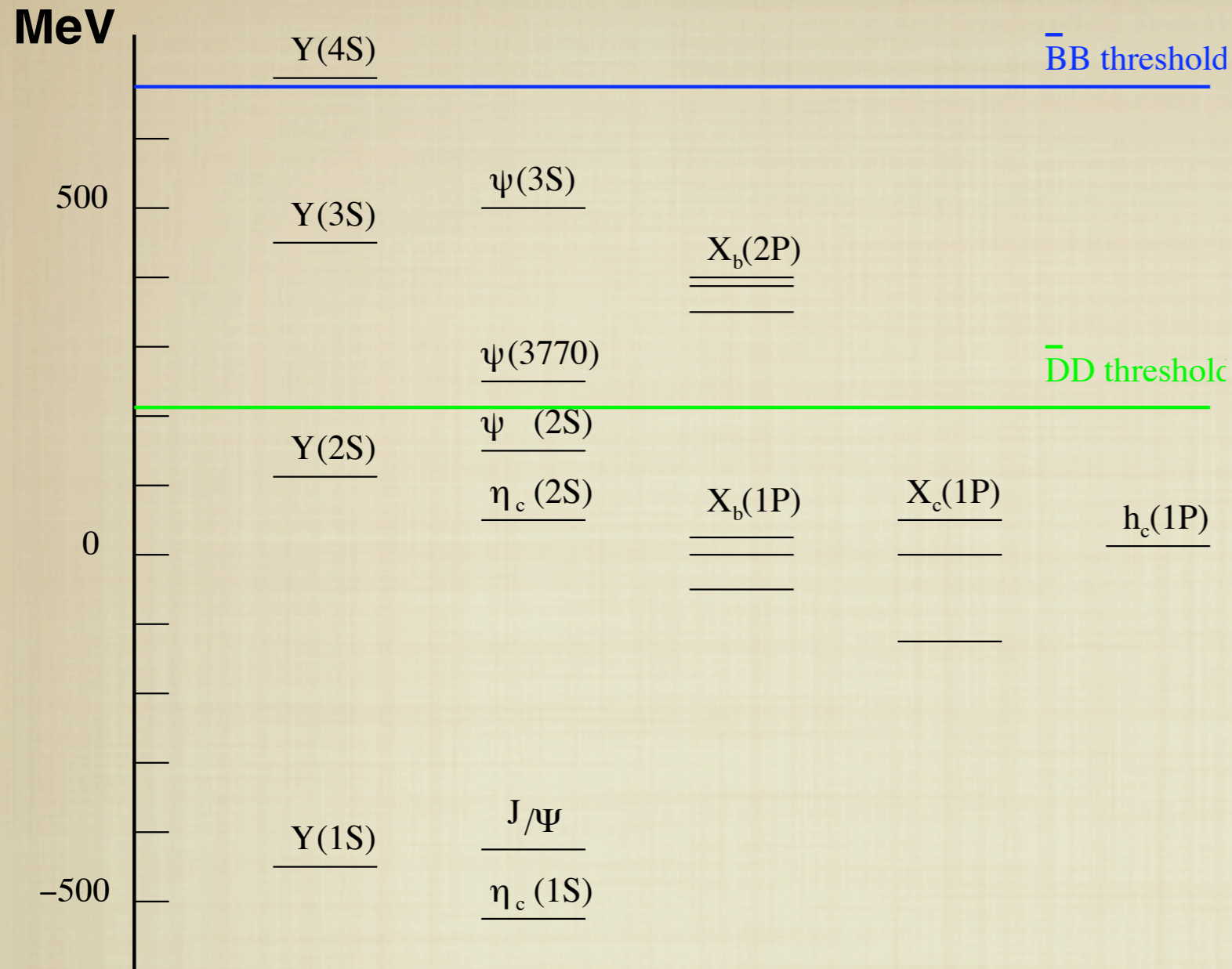
Heavy quarks offer a privileged access



A large scale  $m_Q \gg \Lambda_{\text{QCD}}$   $\alpha_s(m_Q) \ll 1$



# Quarkonium scales



S states

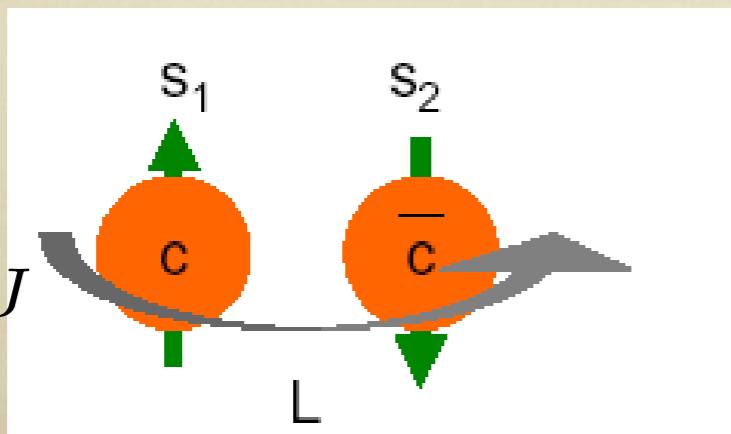
P states

Normalized with respect to  $\chi_b(1P)$  and  $\chi_c(1P)$

$$M(Y(1S)) = 9460 \text{ GeV}$$

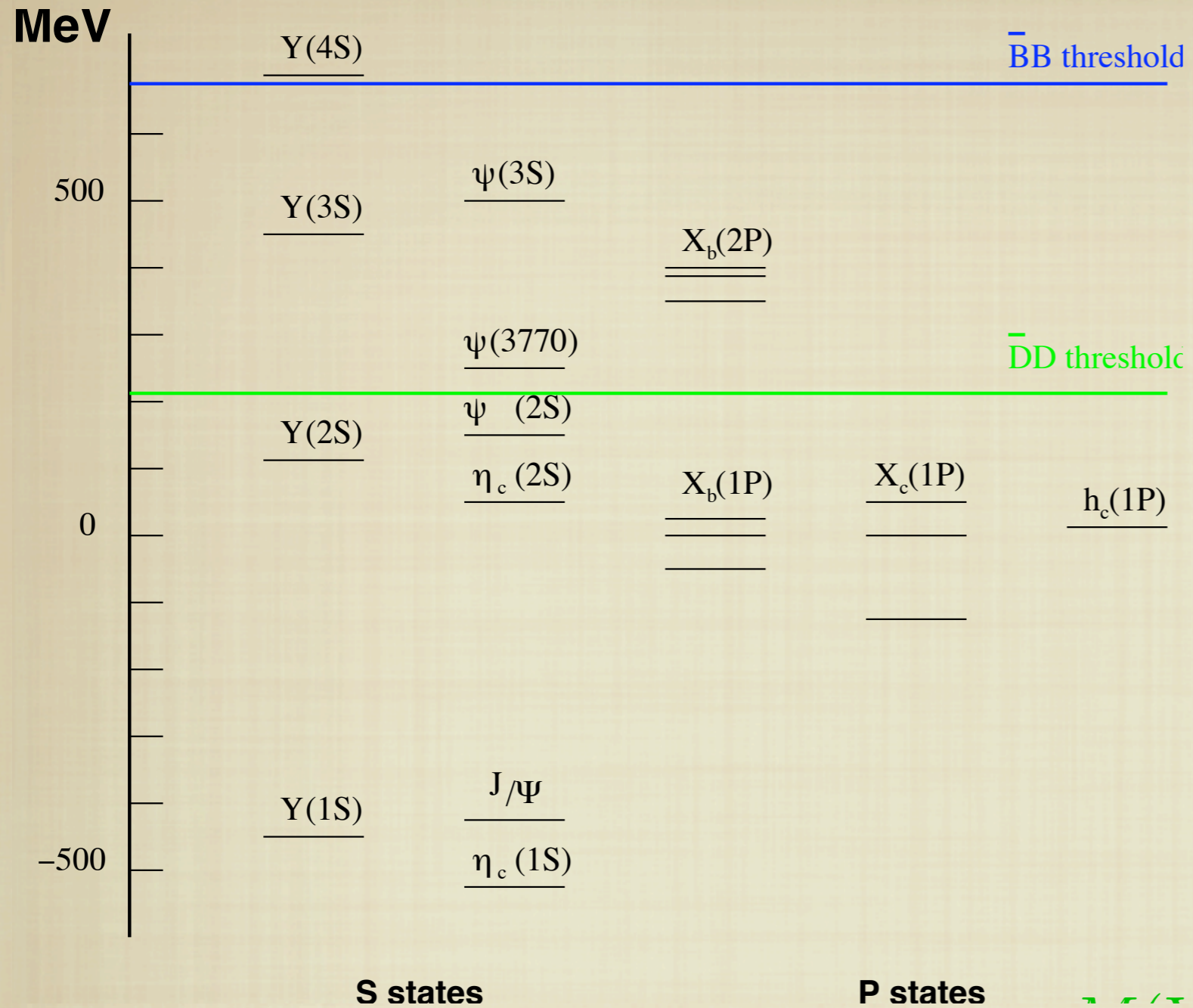
$$M(J/\Psi) = 3097 \text{ GeV}$$

$$2S+1 L_J$$

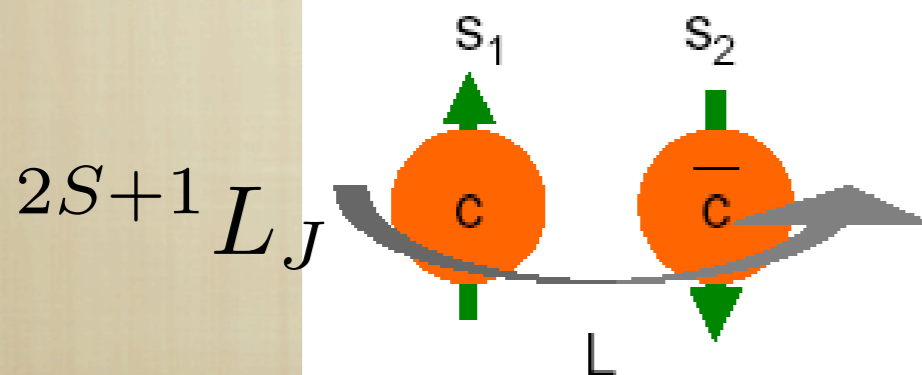




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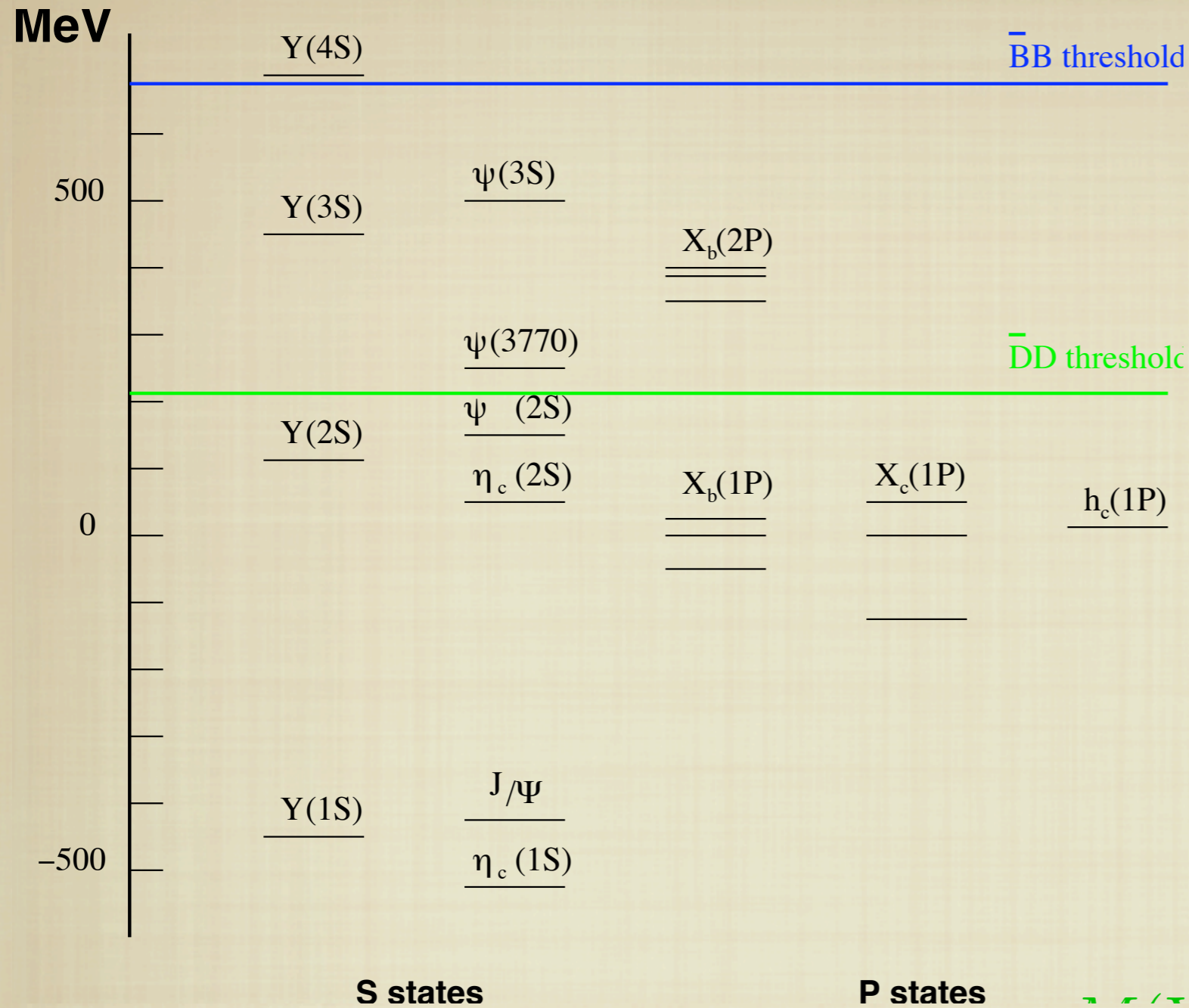


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# Quarkonium scales

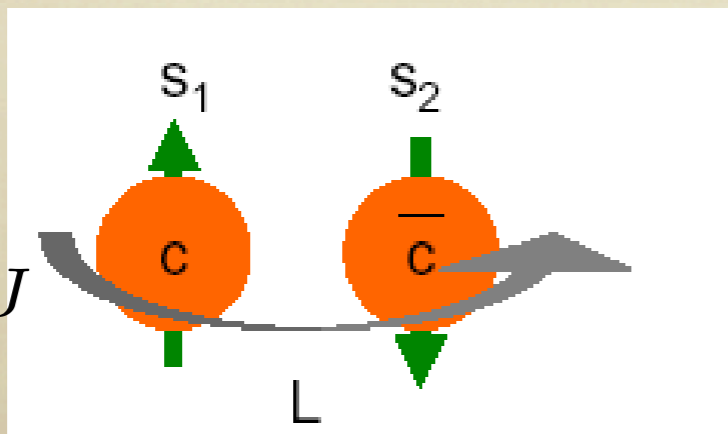


THE MASS SCALE IS PERTURBATIVE

$$m_Q \gg \Lambda_{\text{QCD}}$$

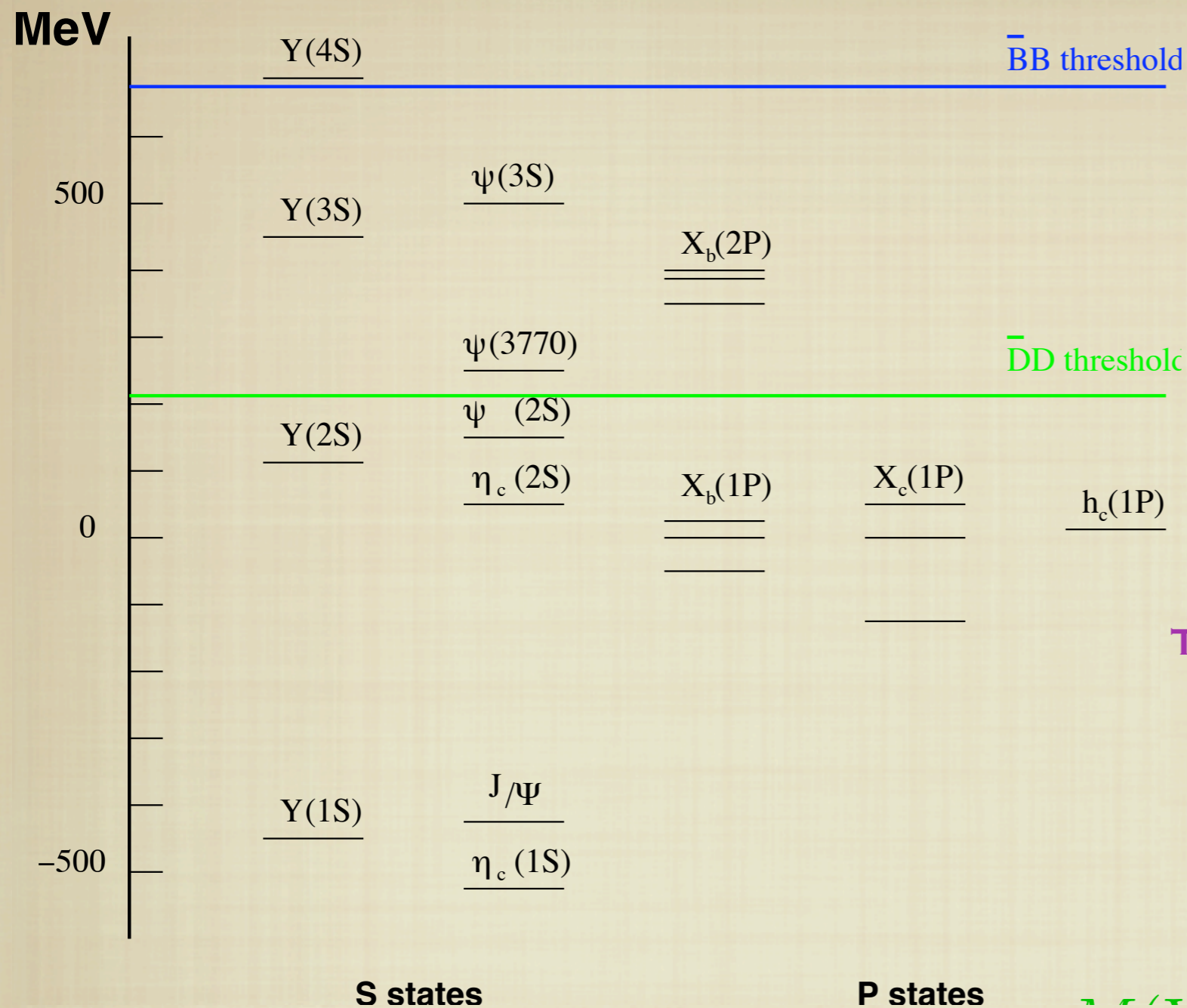
$$m_b \simeq 5 \text{ GeV}; m_c \simeq 1.5 \text{ GeV}$$

$$2S+1 L_J$$





# Quarkonium scales



THE SYSTEM IS NONRELATIVISTIC(NR)

$$\Delta E \sim mv^2, \Delta_{fs} E \sim mv^4$$

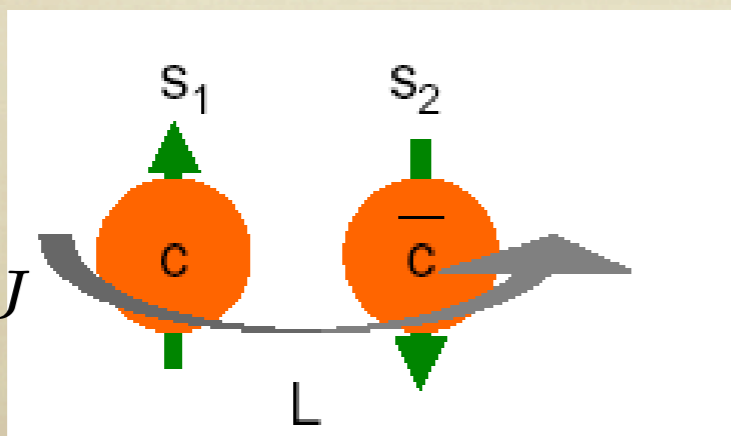
$$v_b^2 \sim 0.1, v_c^2 \sim 0.3$$

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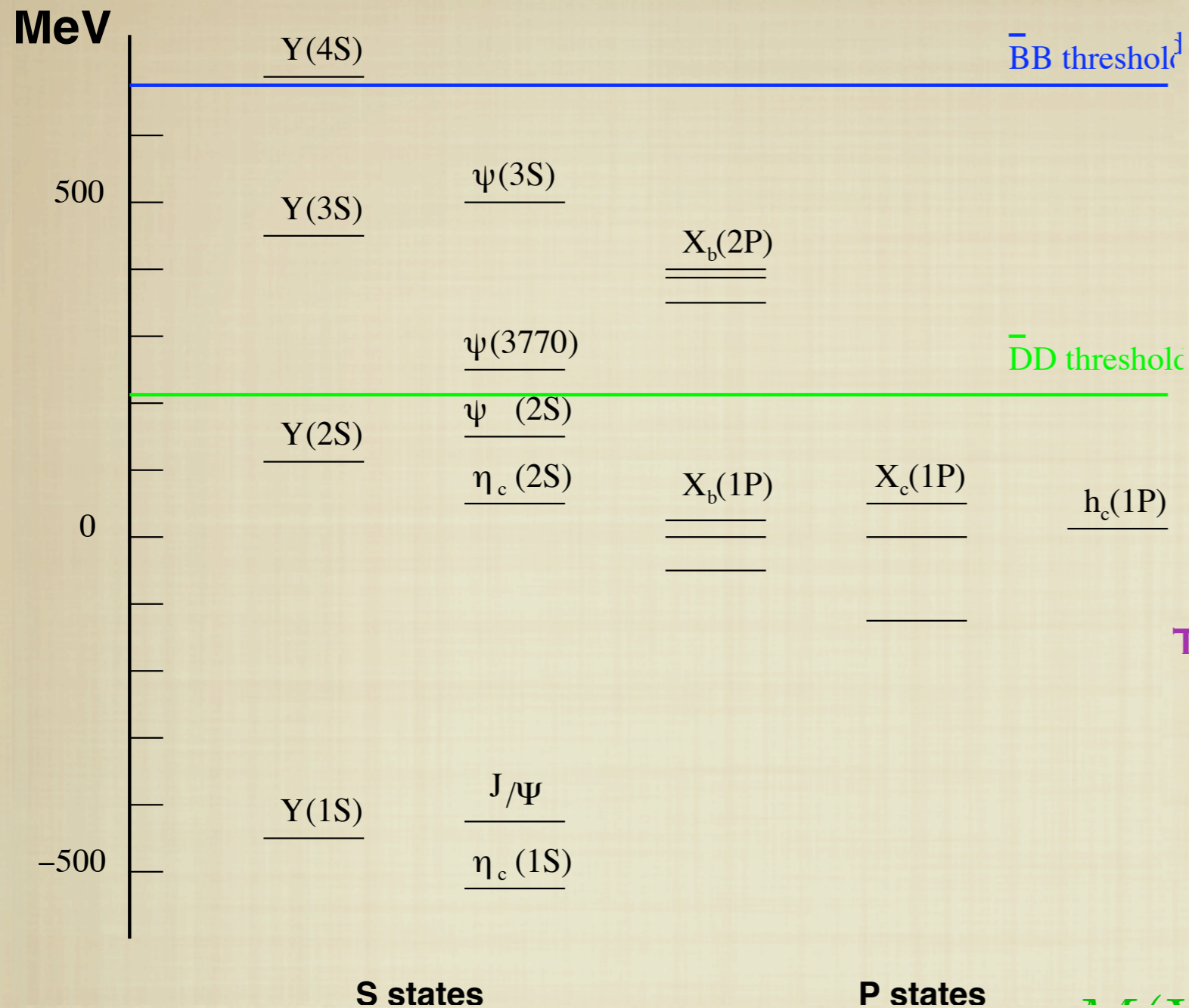
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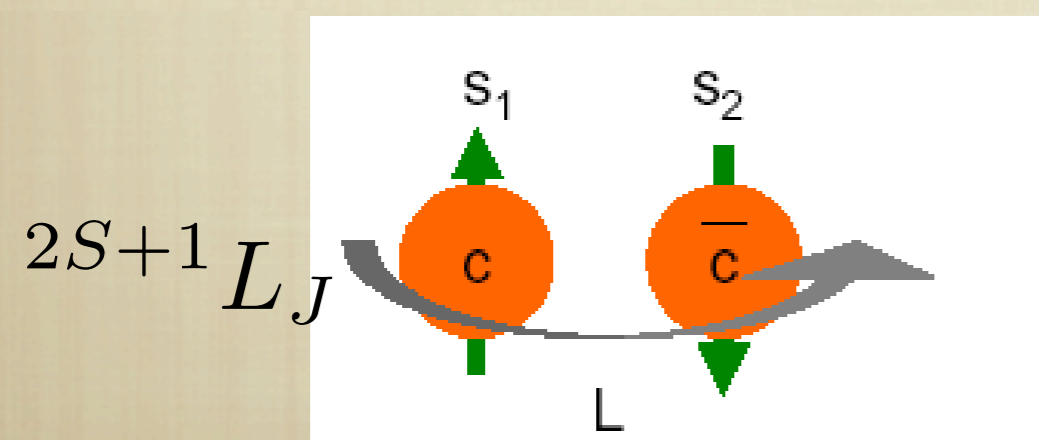




# Quarkonium scales



Normalized with respect to  $\chi_b(1P)$  and  $\chi_c(1P)$



NR BOUND STATES HAVE AT LEAST 3 SCALES

$$m \gg mv \gg mv^2 \quad v \ll 1$$

THE SYSTEM IS NONRELATIVISTIC(NR)

$$\Delta E \sim mv^2, \Delta_{fs} E \sim mv^4$$

$$v_b^2 \sim 0.1, v_c^2 \sim 0.3$$

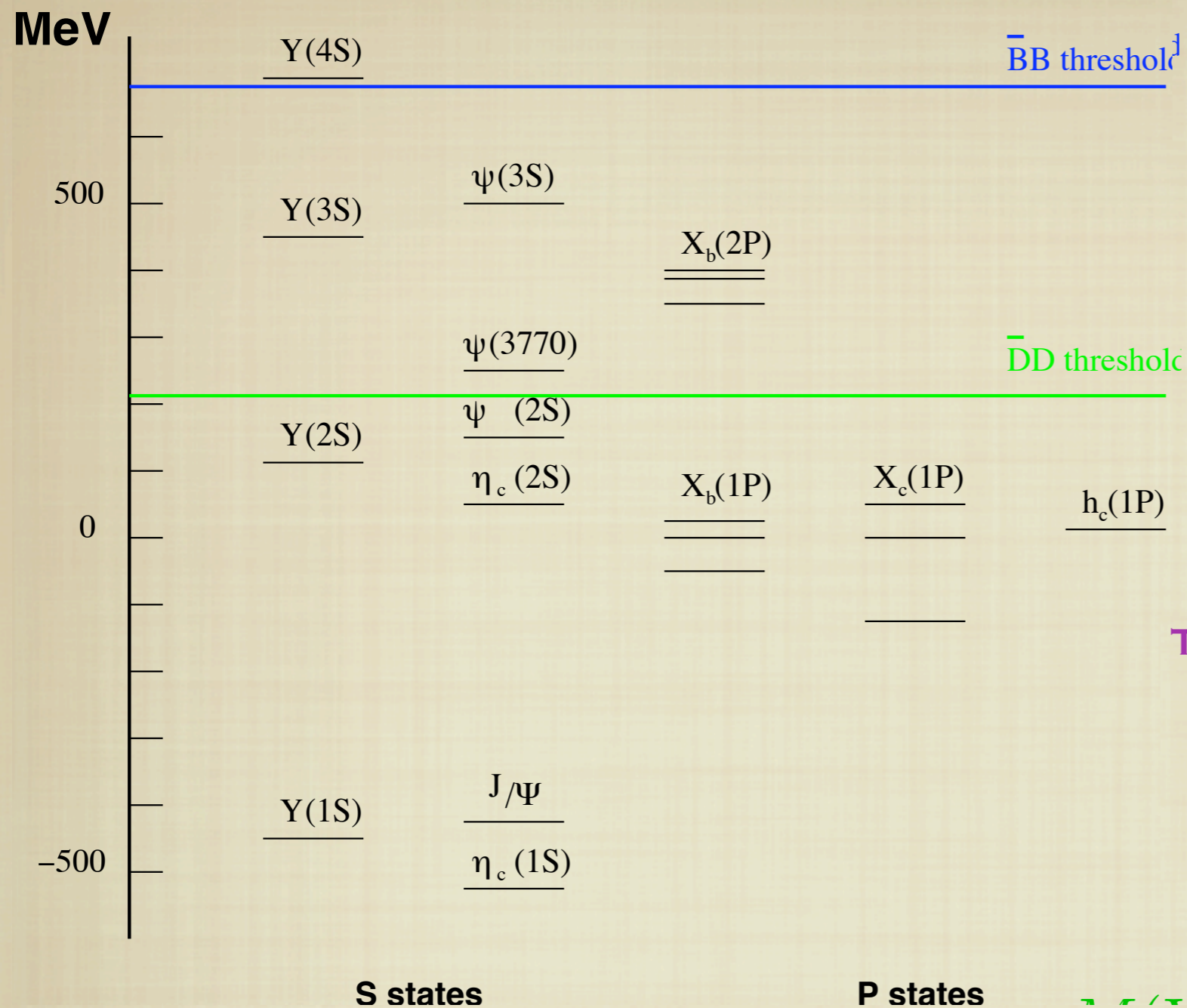
THE MASS SCALE IS PERTURBATIVE

$$m_Q \gg \Lambda_{\text{QCD}}$$

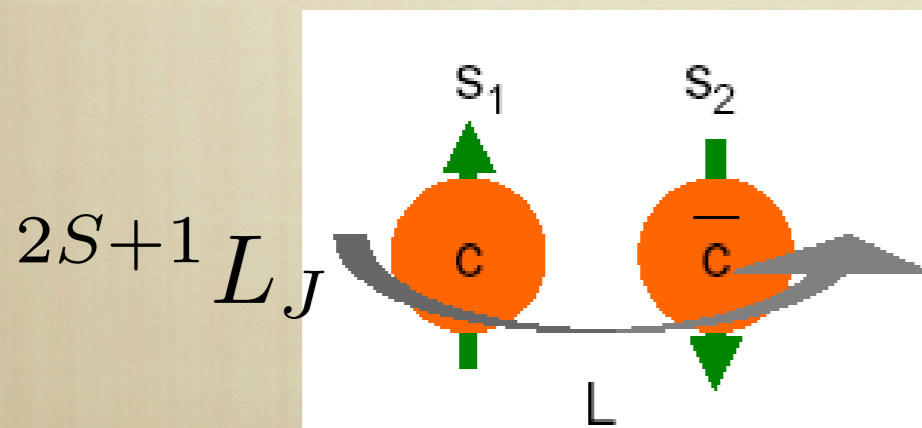
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$$mv \sim r^{-1}$$

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$$v_b^2 \sim 0.1, v_c^2 \sim 0.3$$

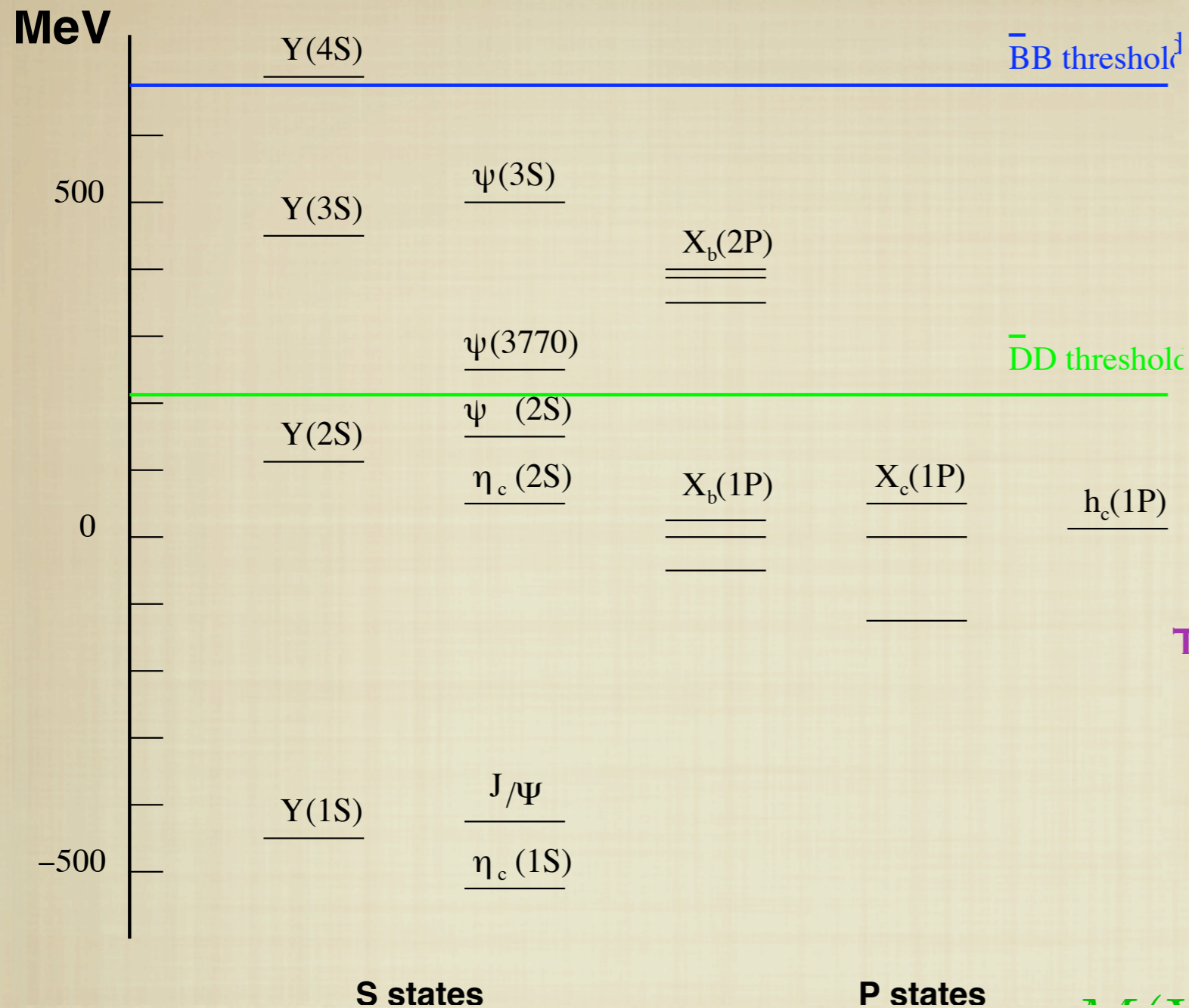
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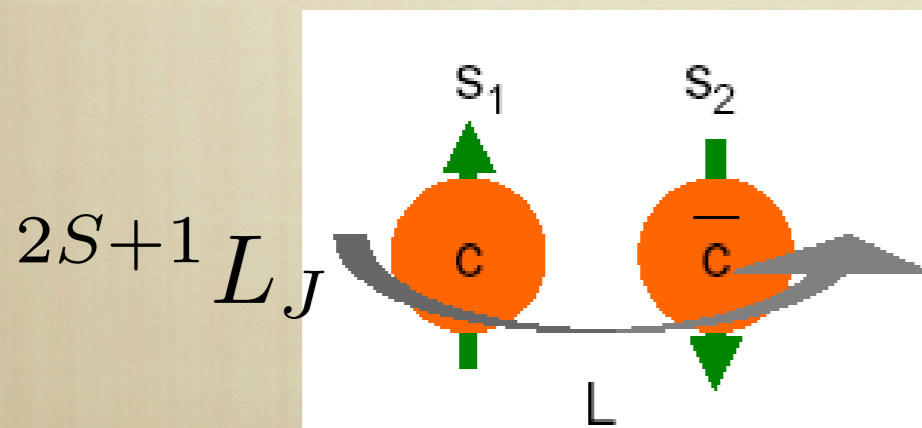
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$$m \gg mv \gg mv^2 \quad v \ll 1$$

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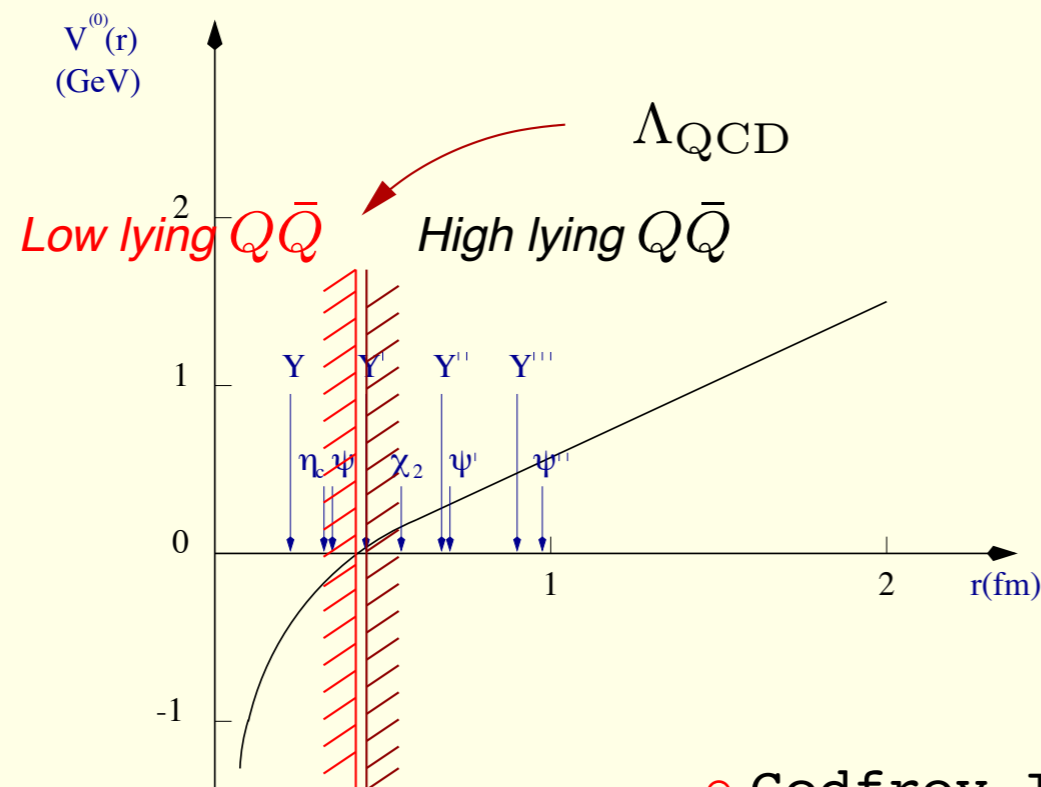
$$m_b \simeq 5 \text{ GeV}; m_c \simeq 1.5 \text{ GeV}$$

# Quarkonium as a confinement and deconfinement probe

The rich structure of separated energy scales makes  $Q\bar{Q}$  an ideal probe

At zero temperature

- The different quarkonium radii provide different measures of the transition from a Coulombic to a confined bound state.



○ Godfrey Isgur PRD 32(85)189

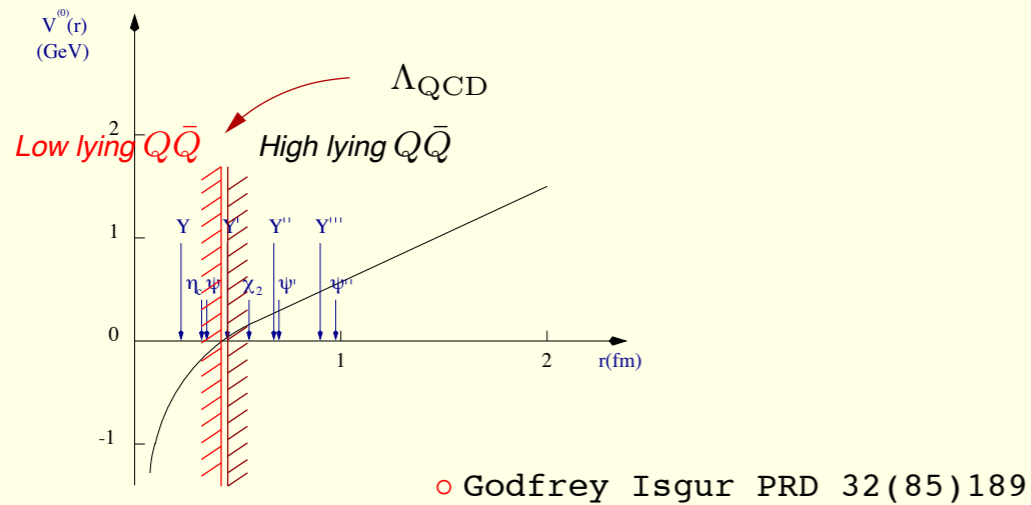
quarkonia probe the perturbative (high energy) and non perturbative region (low energy) as well as the transition region in dependence of their radius  $r$



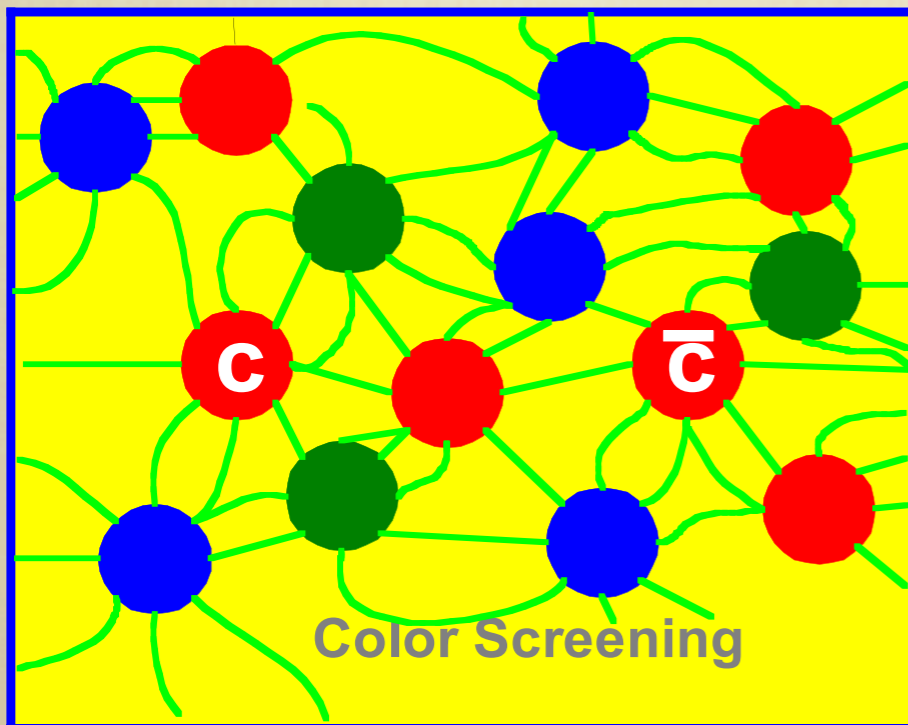
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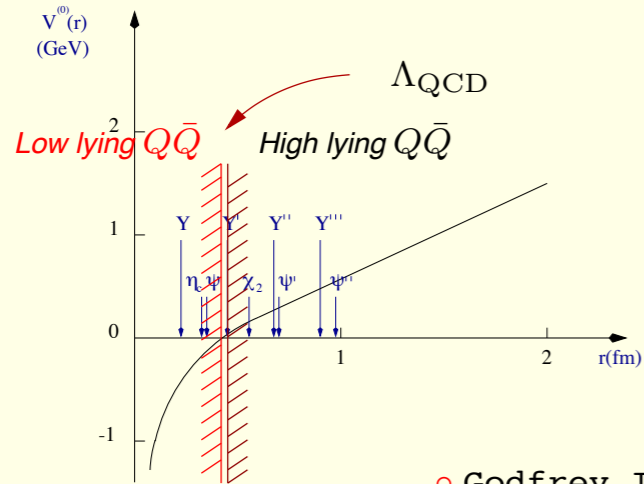
## At finite temperature



# Quarkonium as a confinement and deconfinement probe

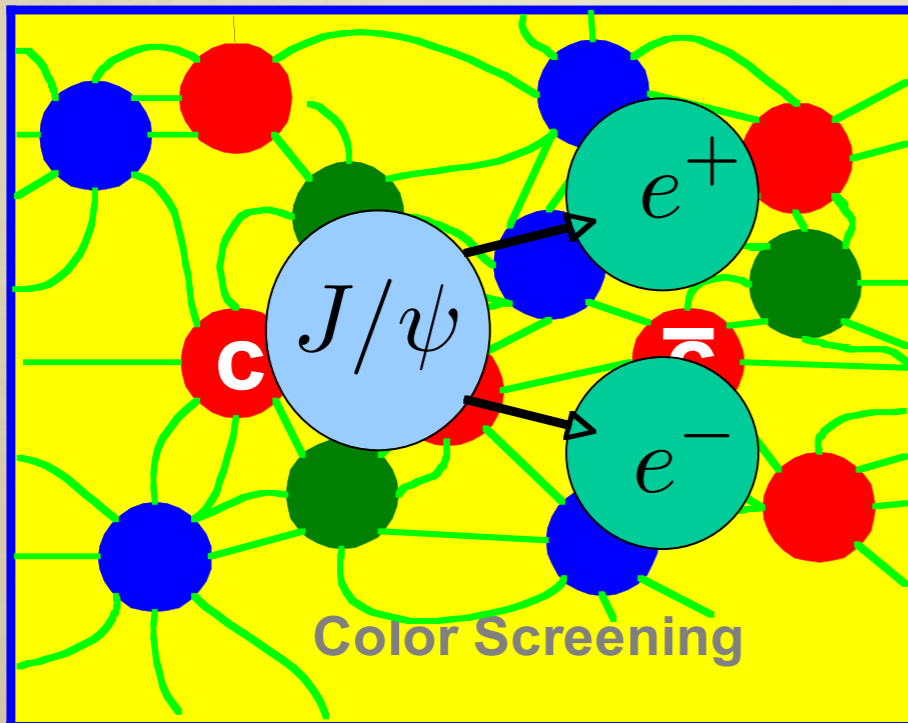
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## At finite temperature

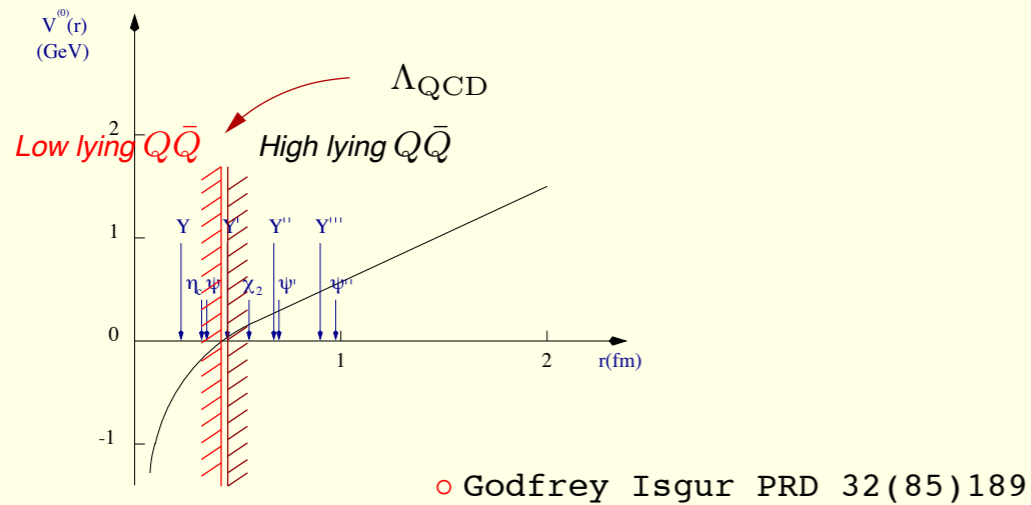




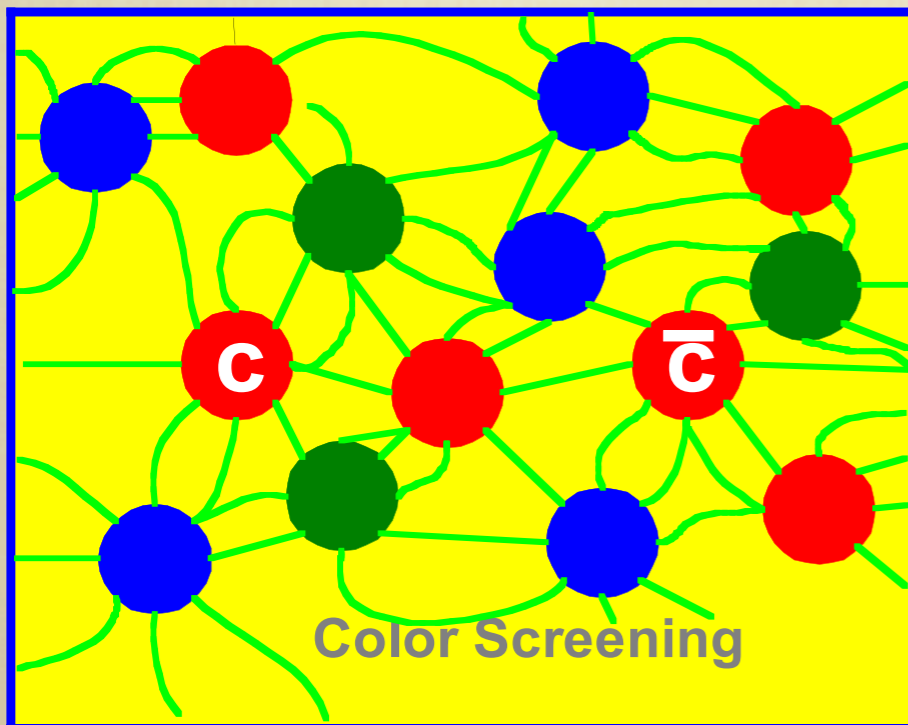
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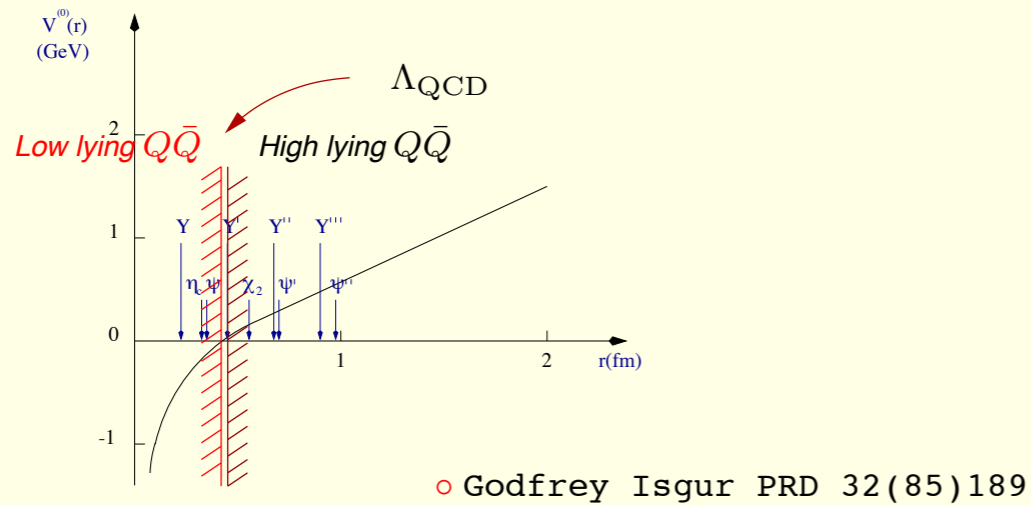
## At finite temperature



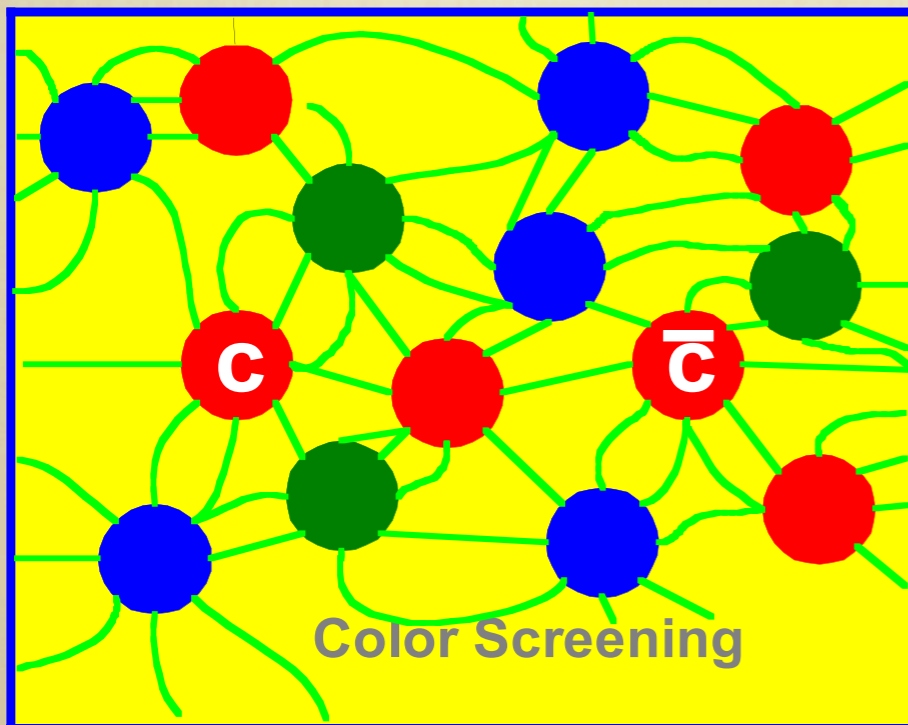
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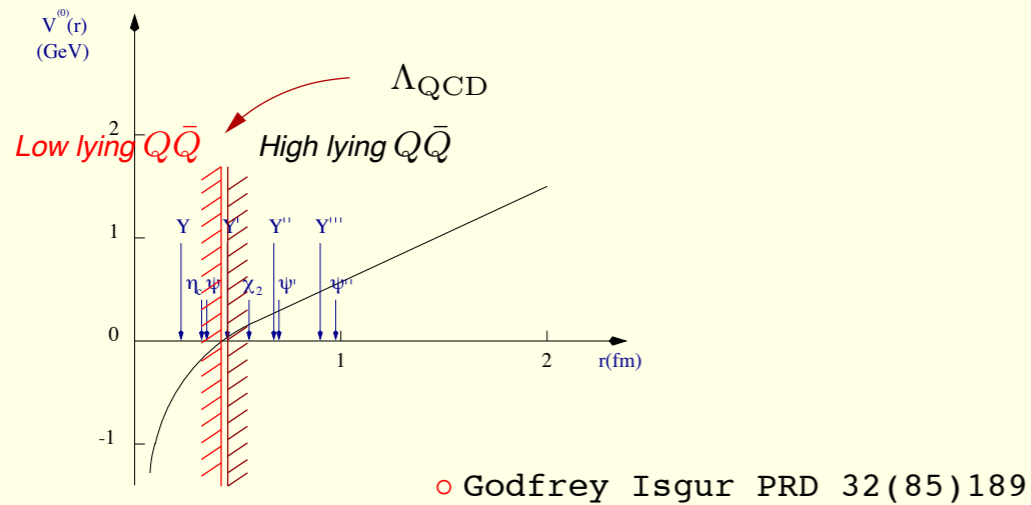
quarkonia dissociate  
at different  
temperature in  
dependence of their  
radius: they  
are a Quark Gluon  
Plasma thermometer



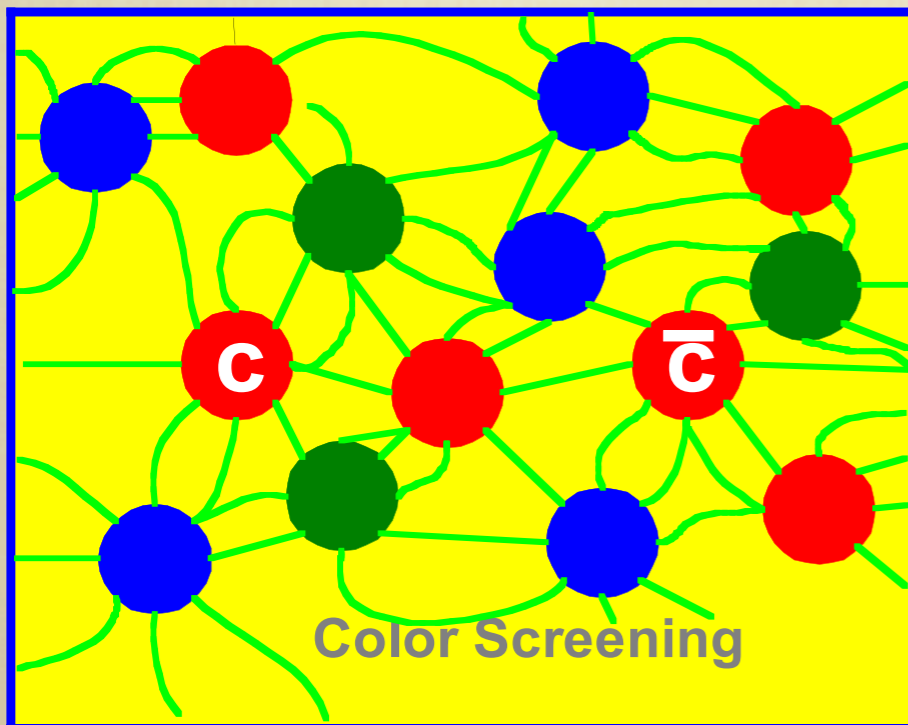
# Quarkonium as a confinement and deconfinement probe

## At zero temperature

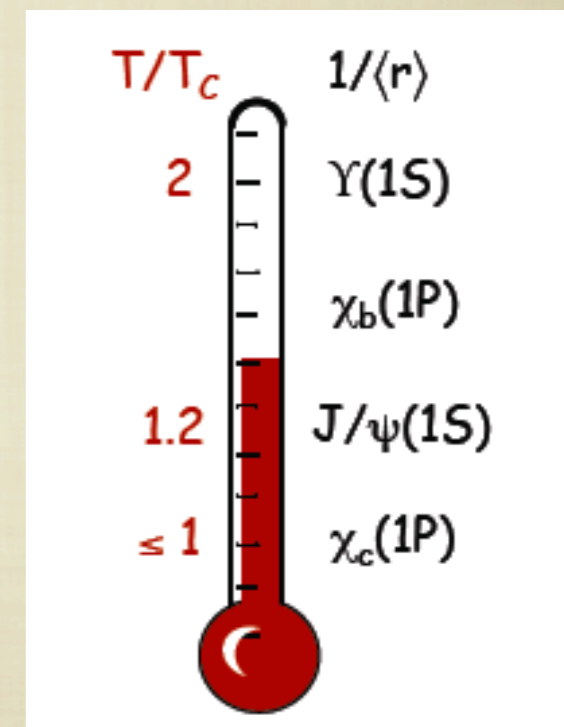
- The different quarkonium radii provide different measures of the transition from a Coulombic to a confined bound state.



## At finite temperature



quarkonia dissociate at different temperature in dependence of their radius: they are a Quark Gluon Plasma thermometer





# Quarkonium and experiments

B-FACTORIES: Heavy Mesons Factories

CLEO-c BESII tau charm factories

CLEO-III bottomonium factory

Fermilab CDF, D0, E835

Hera RHIC (Star, Phenix), NA60



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Discovery of New States, New  
Production Mechanisms, Exotics, New  
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More is expected in the future

BESIII, LHC-b

qqbar production at CMS and Atlas

Alice

Panda

Super B, ILC



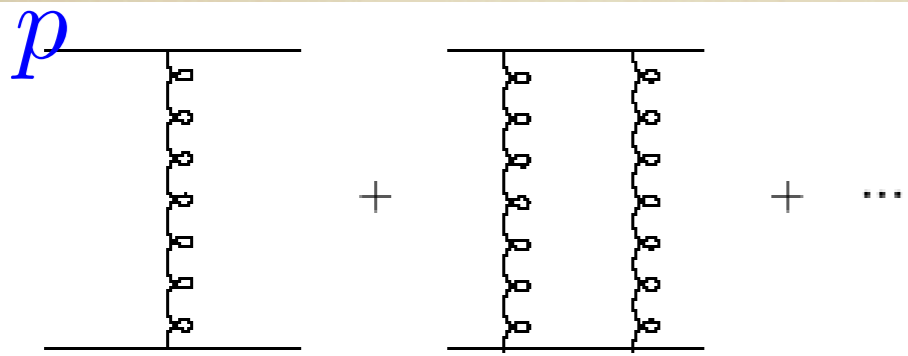
Quarkonium in QCD : a very hard problem

Close to the bound state  $\alpha_s \sim v$



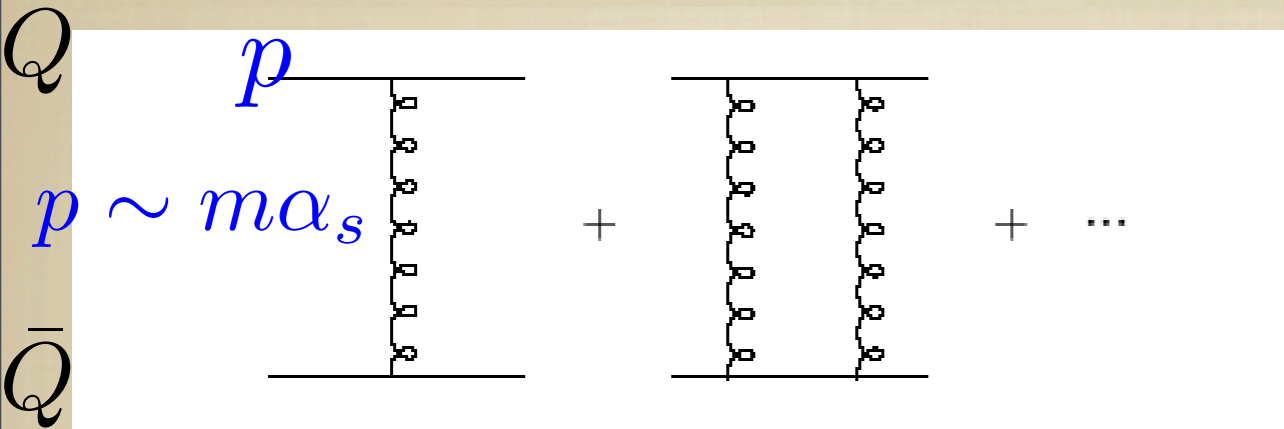
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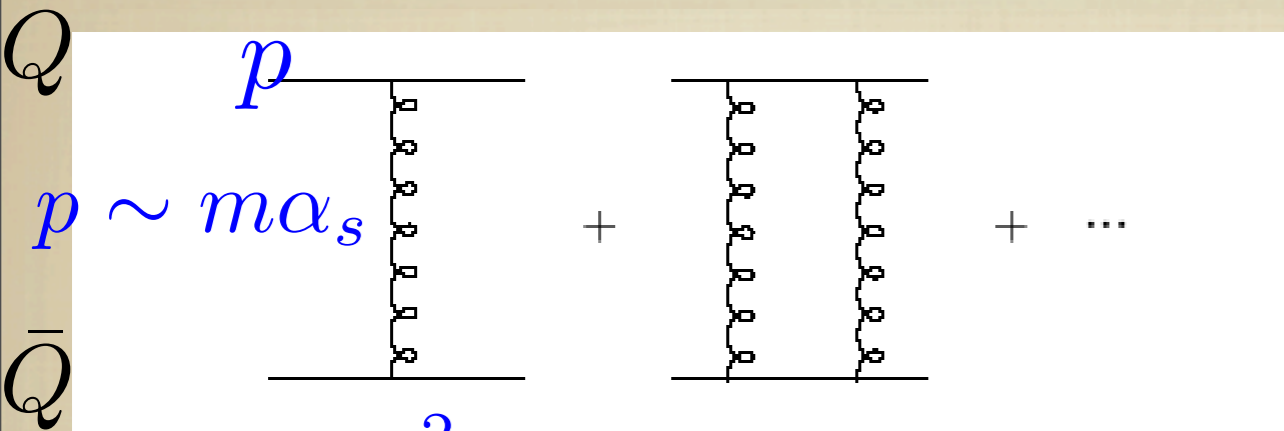
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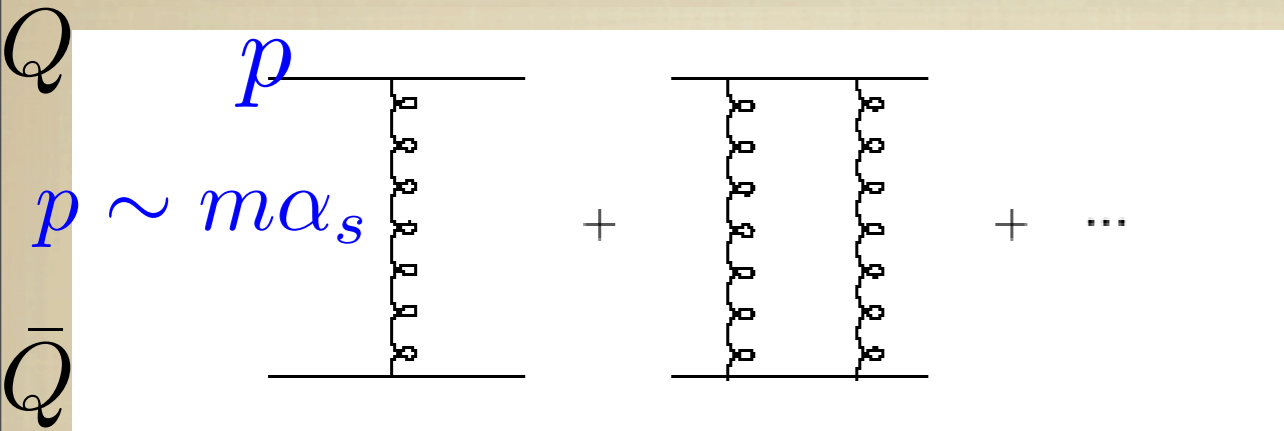
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$$\frac{g^2}{p^2} \left( 1 + \frac{m\alpha_s}{p} \right)$$

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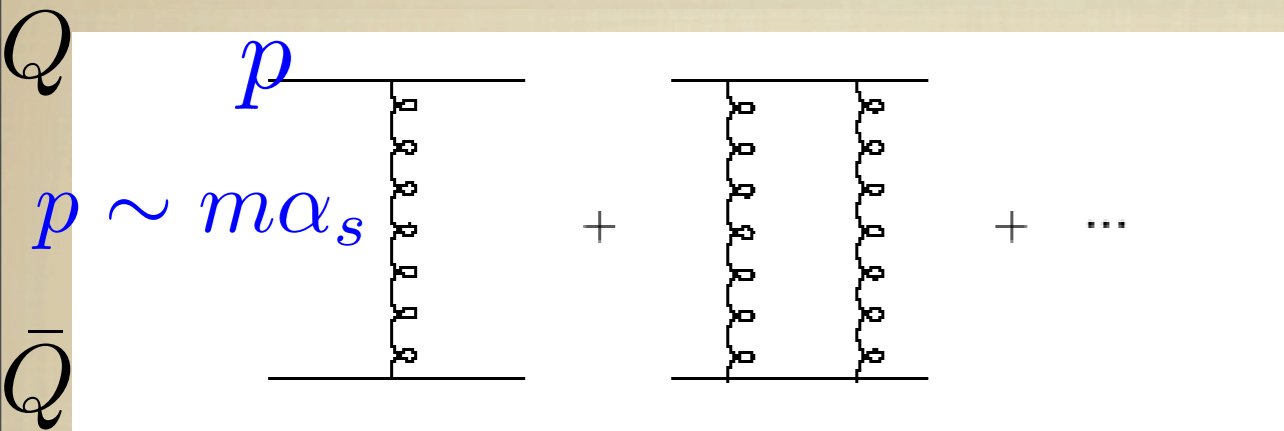
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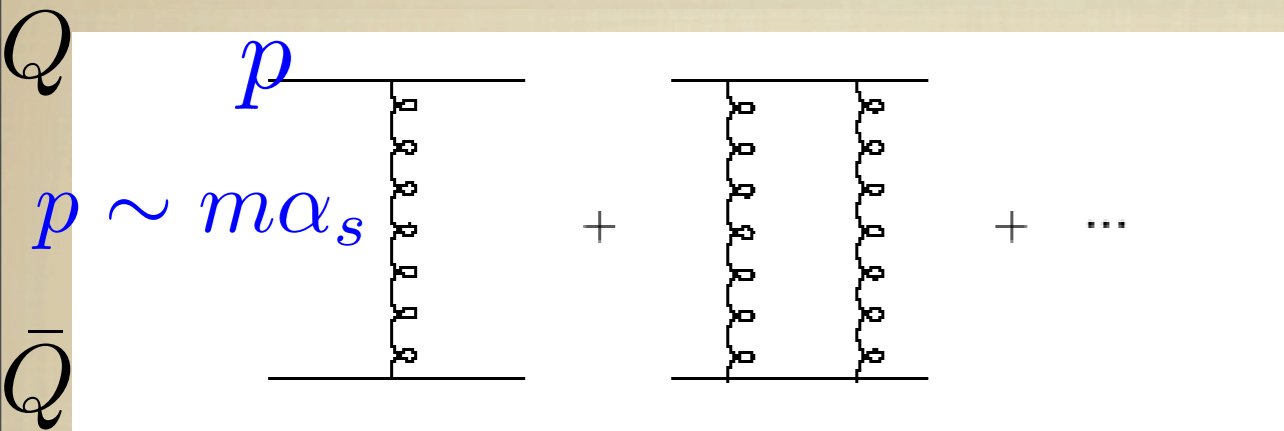


$$\sim \frac{1}{E - \left(\frac{p^2}{m} + V\right)}$$



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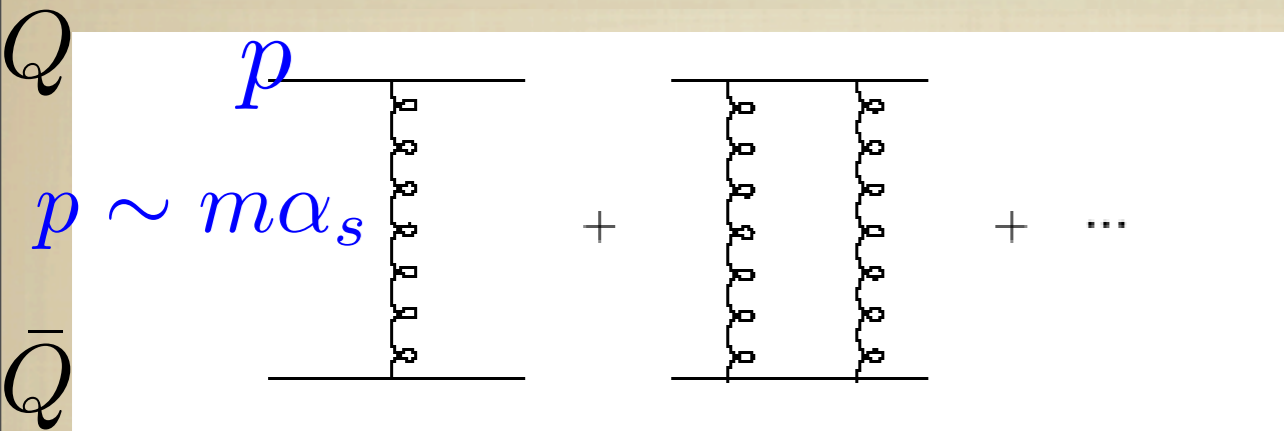


$$\sim \frac{1}{E - \left(\frac{p^2}{m} + V\right)}$$

- From  $\left(\frac{p^2}{m} + V\right)\phi = E\phi \rightarrow p \sim mv$  and  $E = \frac{p^2}{m} + V \sim mv^2$ .

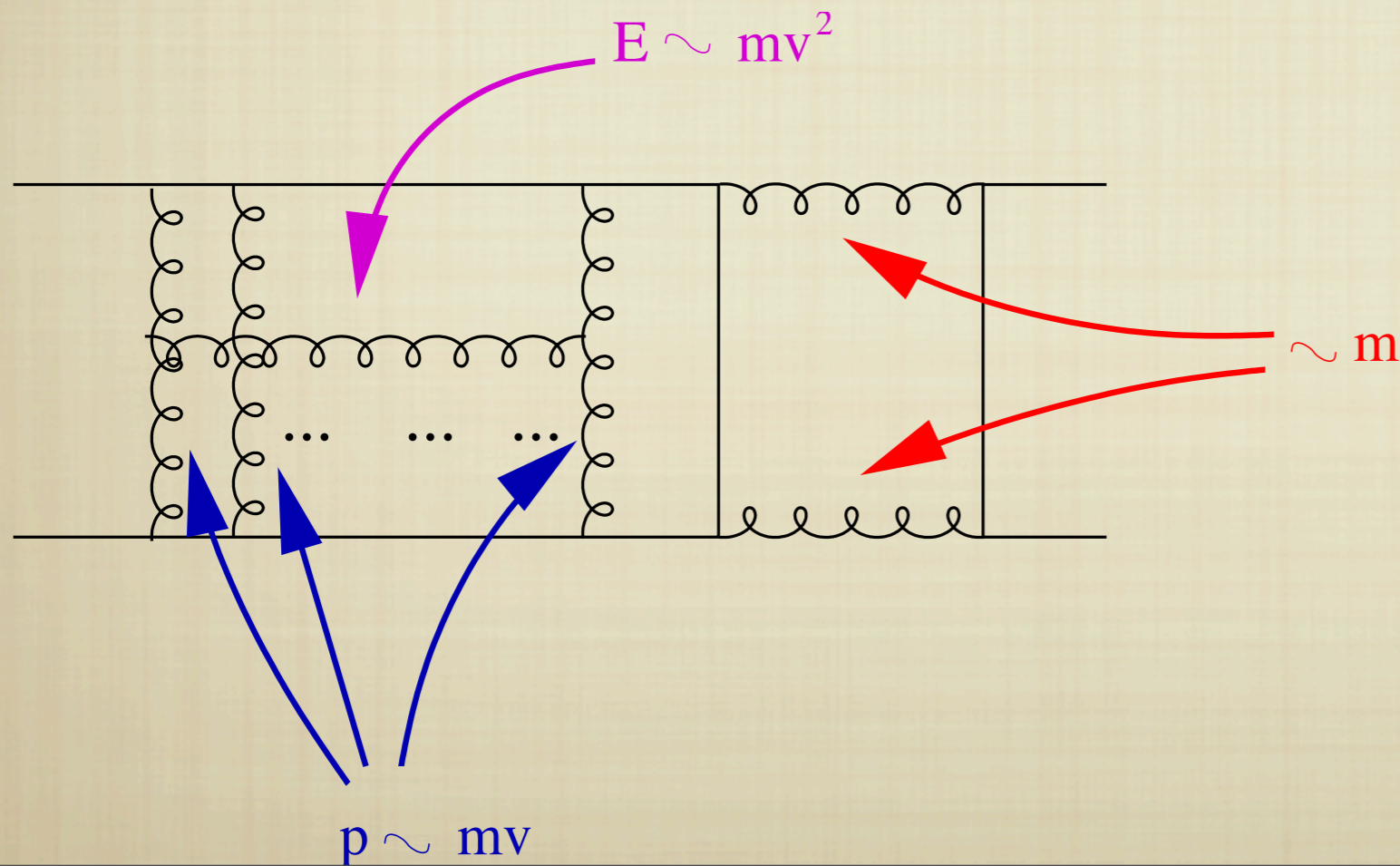
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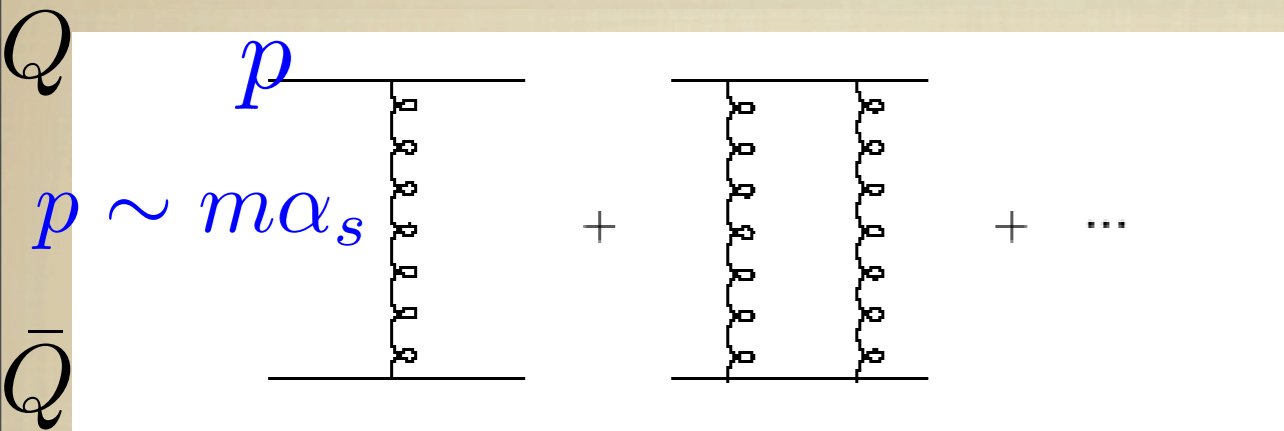
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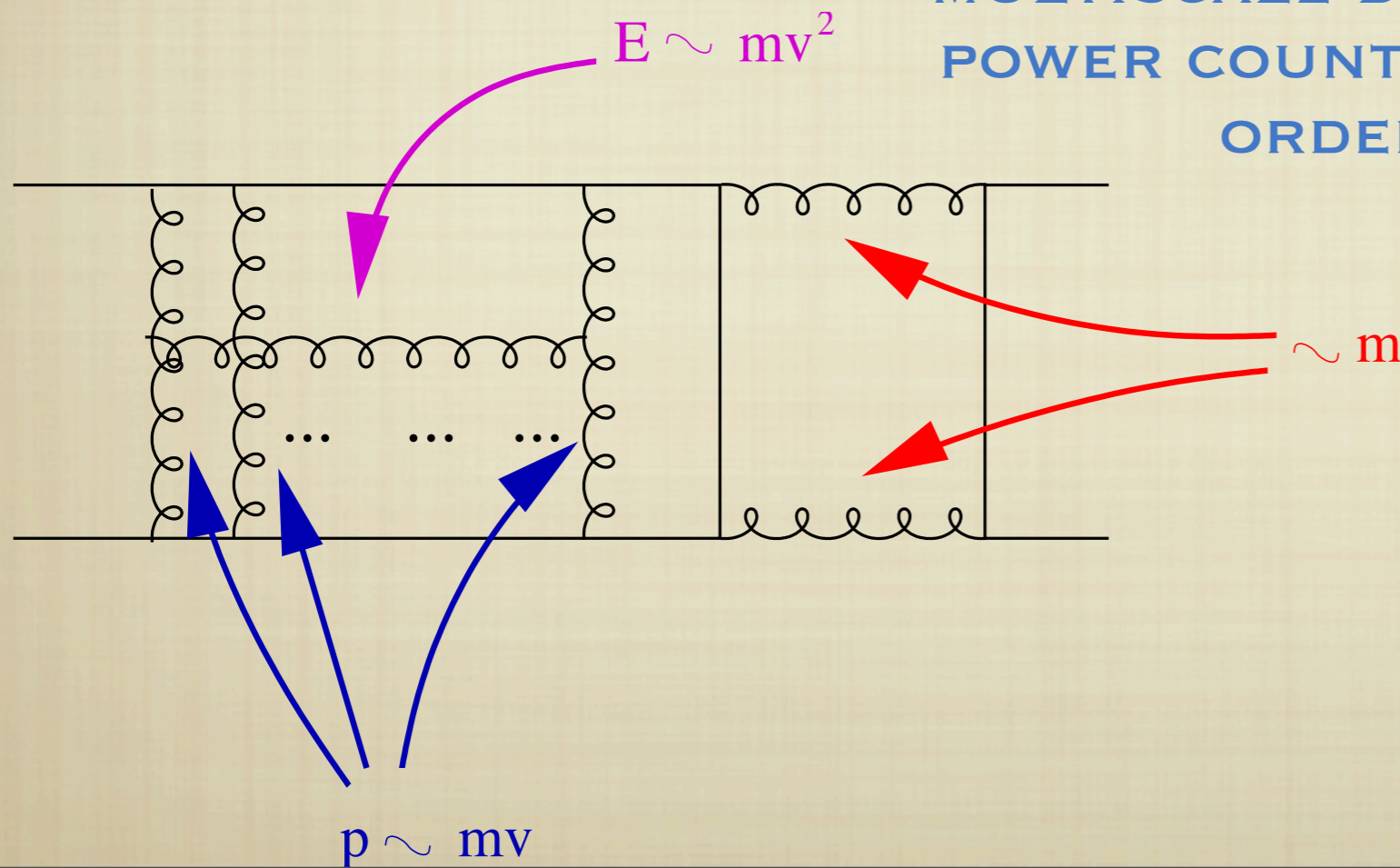
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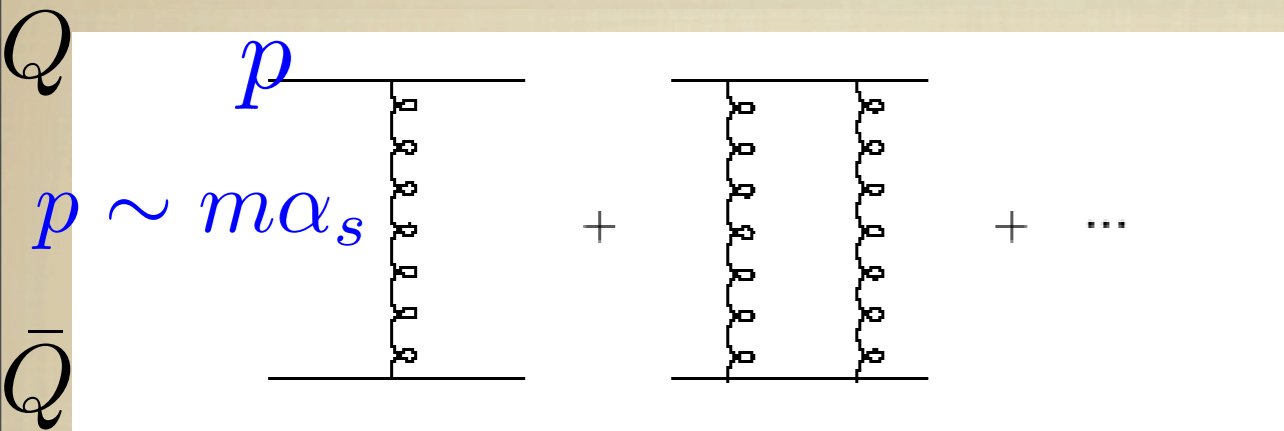
MULTISCALE DIAGRAMS HAVE A COMPLICATE POWER COUNTING AND CONTRIBUTE TO ALL ORDERS IN THE COUPLING





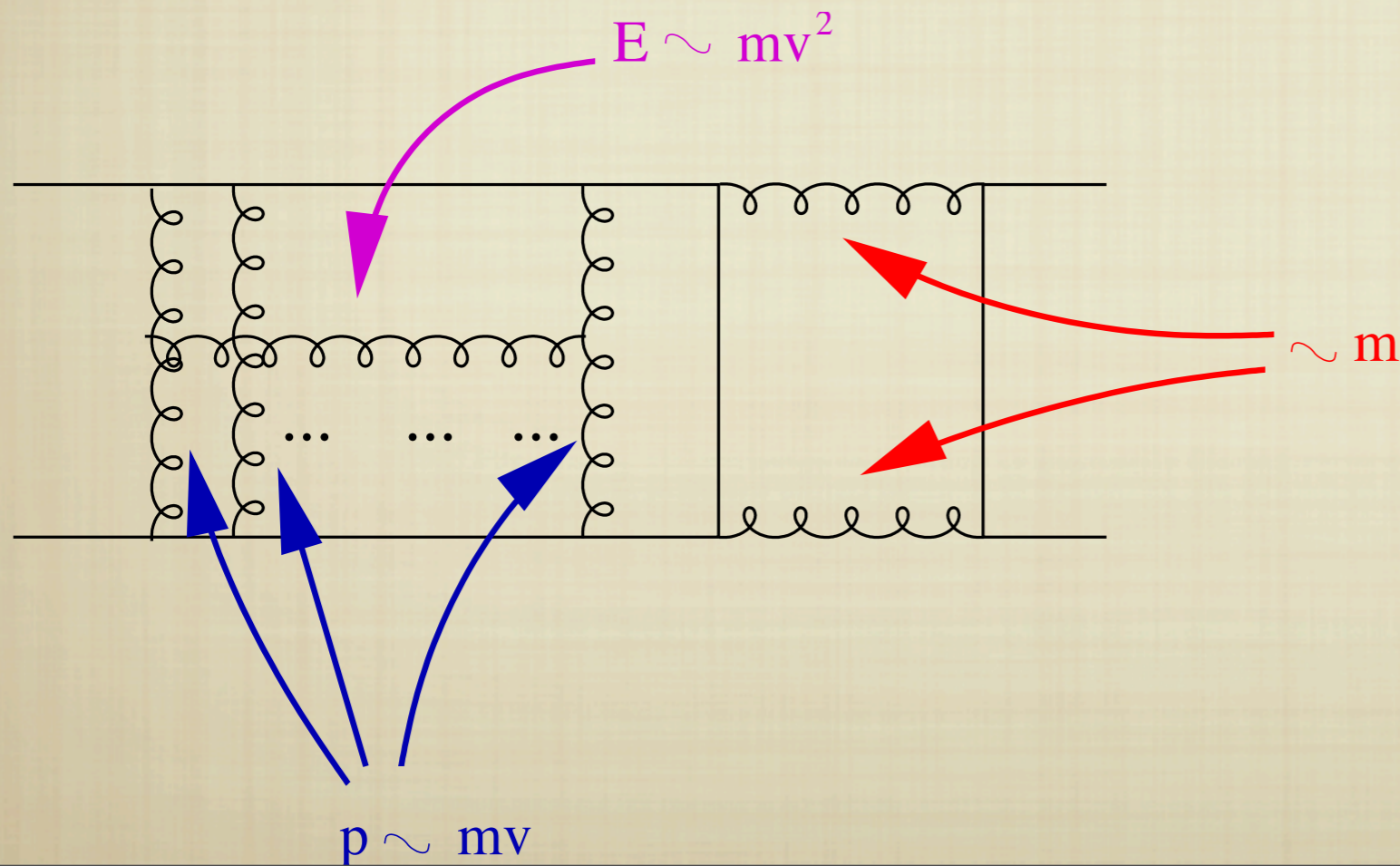
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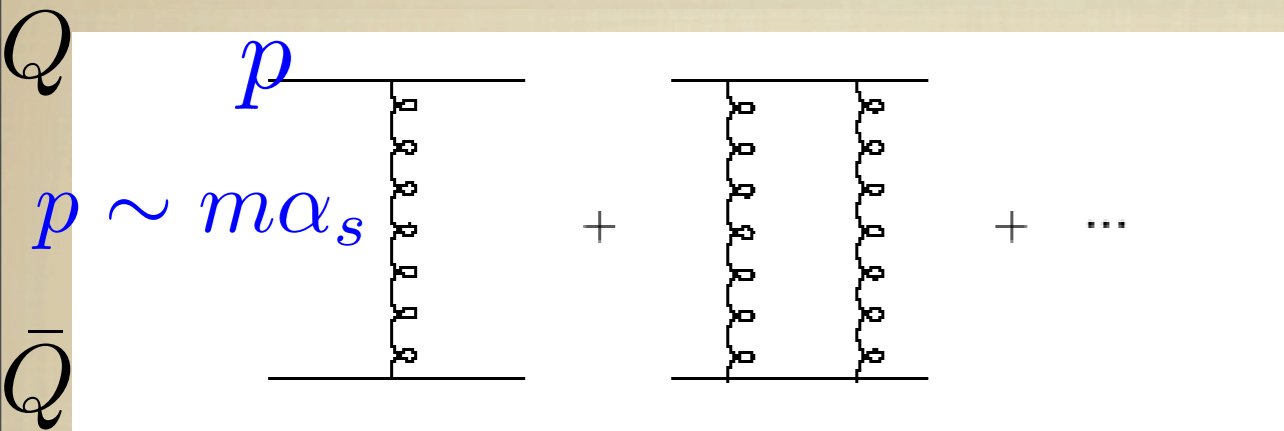
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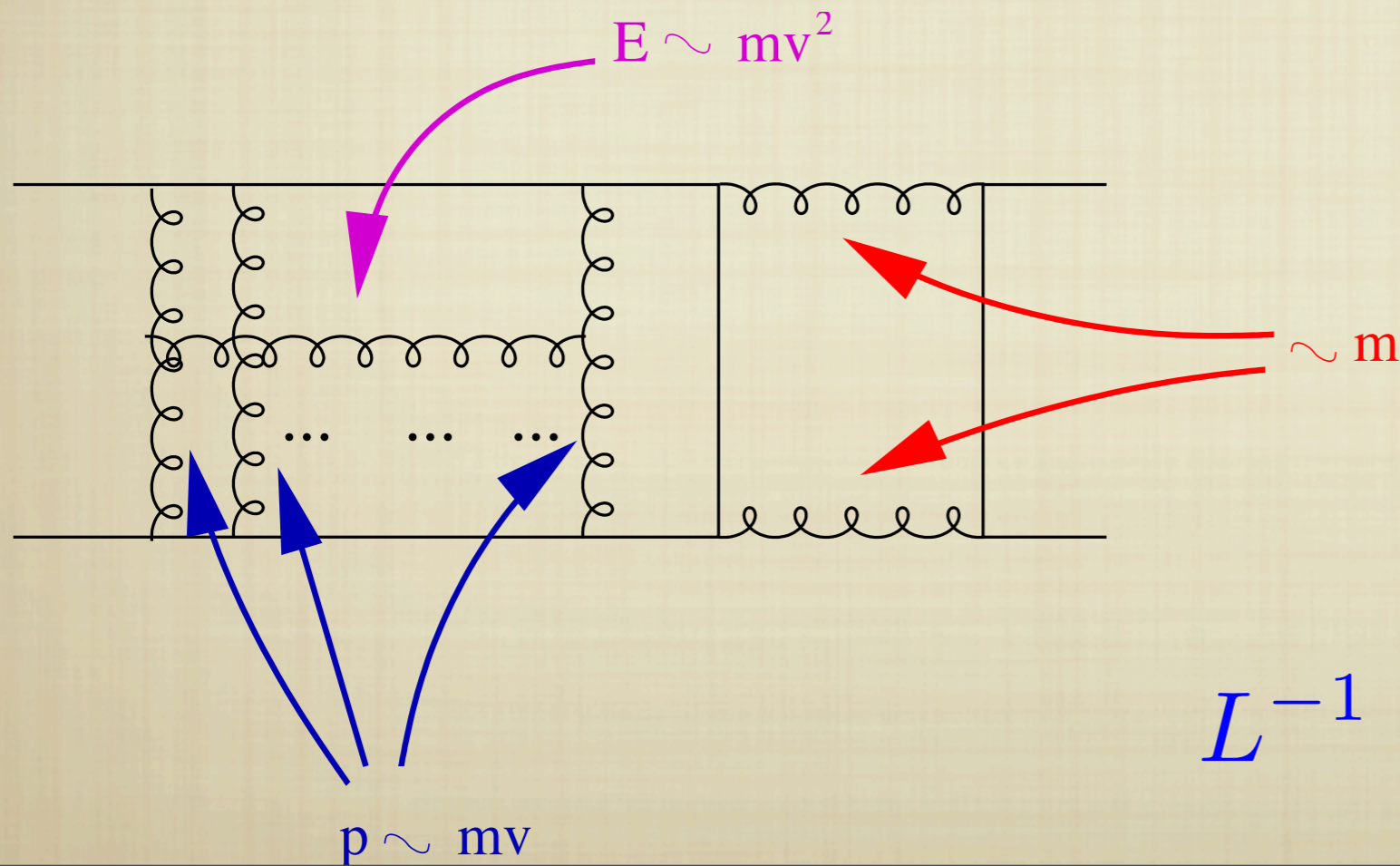
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**DIFFICULT ALSO FOR THE LATTICE!**

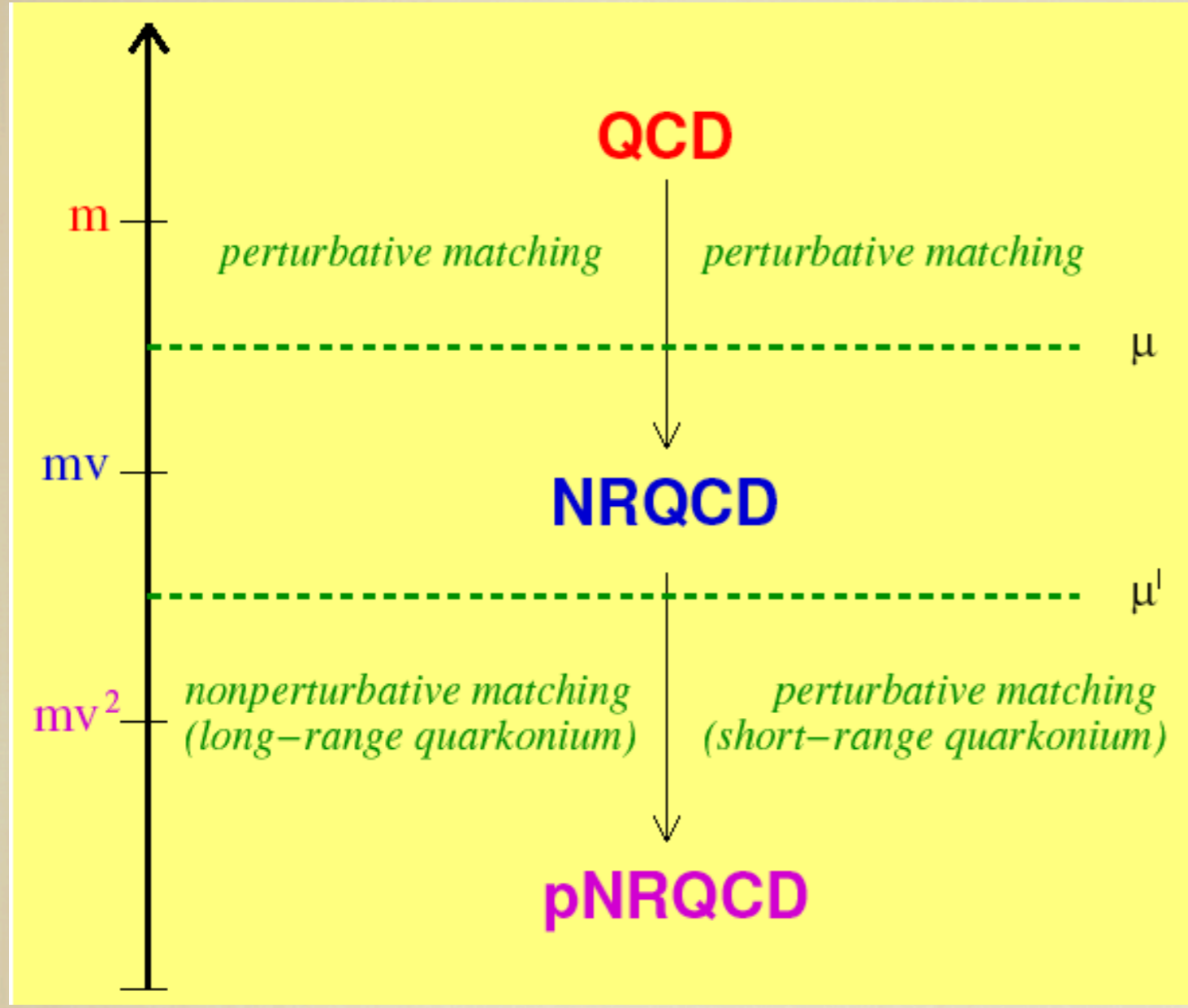
$$L^{-1} \ll \lambda \ll \Lambda \ll a^{-1}$$

# Quarkonium with EFT

Color degrees of freedom

$$3 \times 3 = 1 + 8$$

singlet and octet  $Q\bar{Q}$



Hard

Soft  
(relative momentum)

Ultrasoft  
(binding energy)

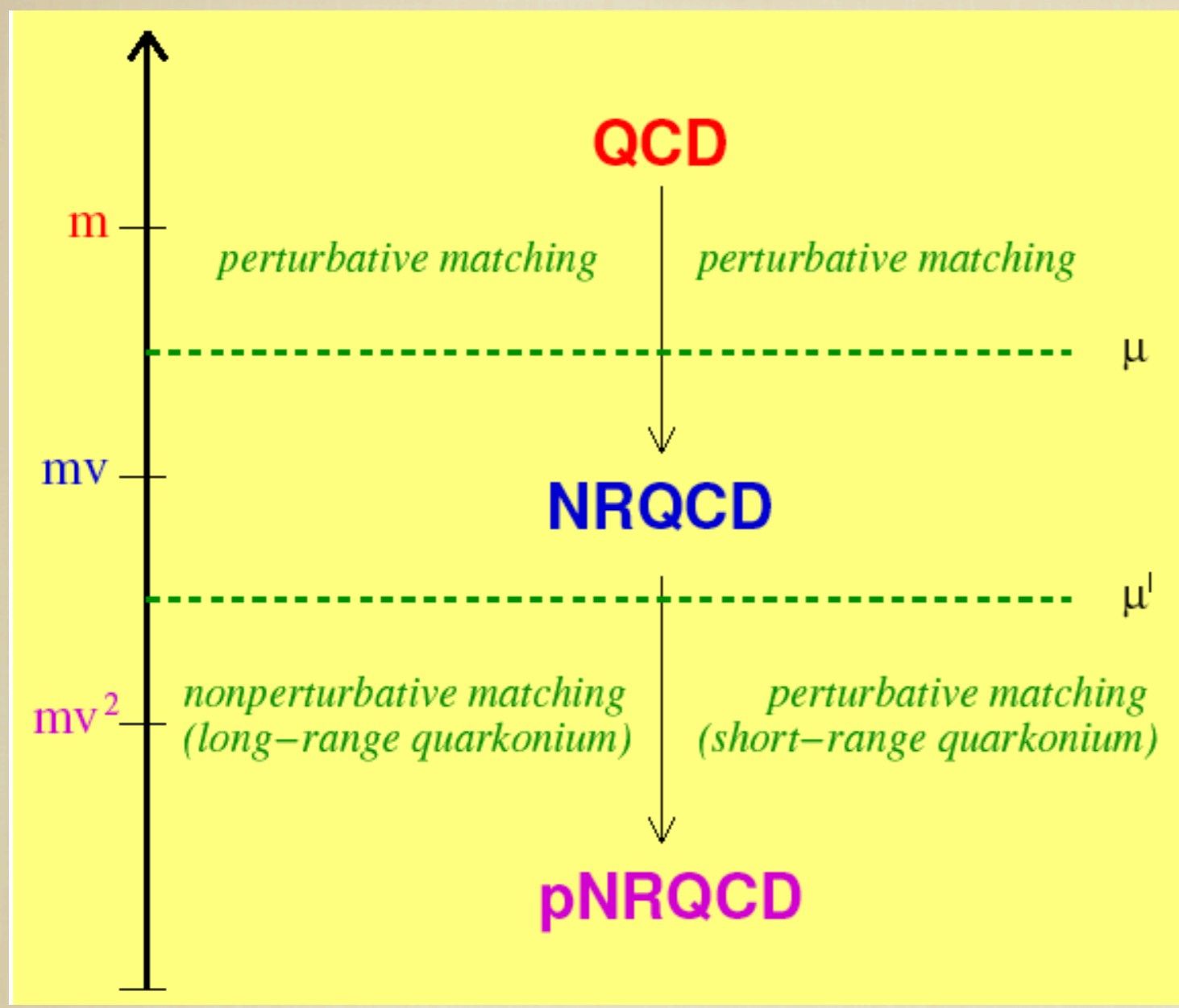


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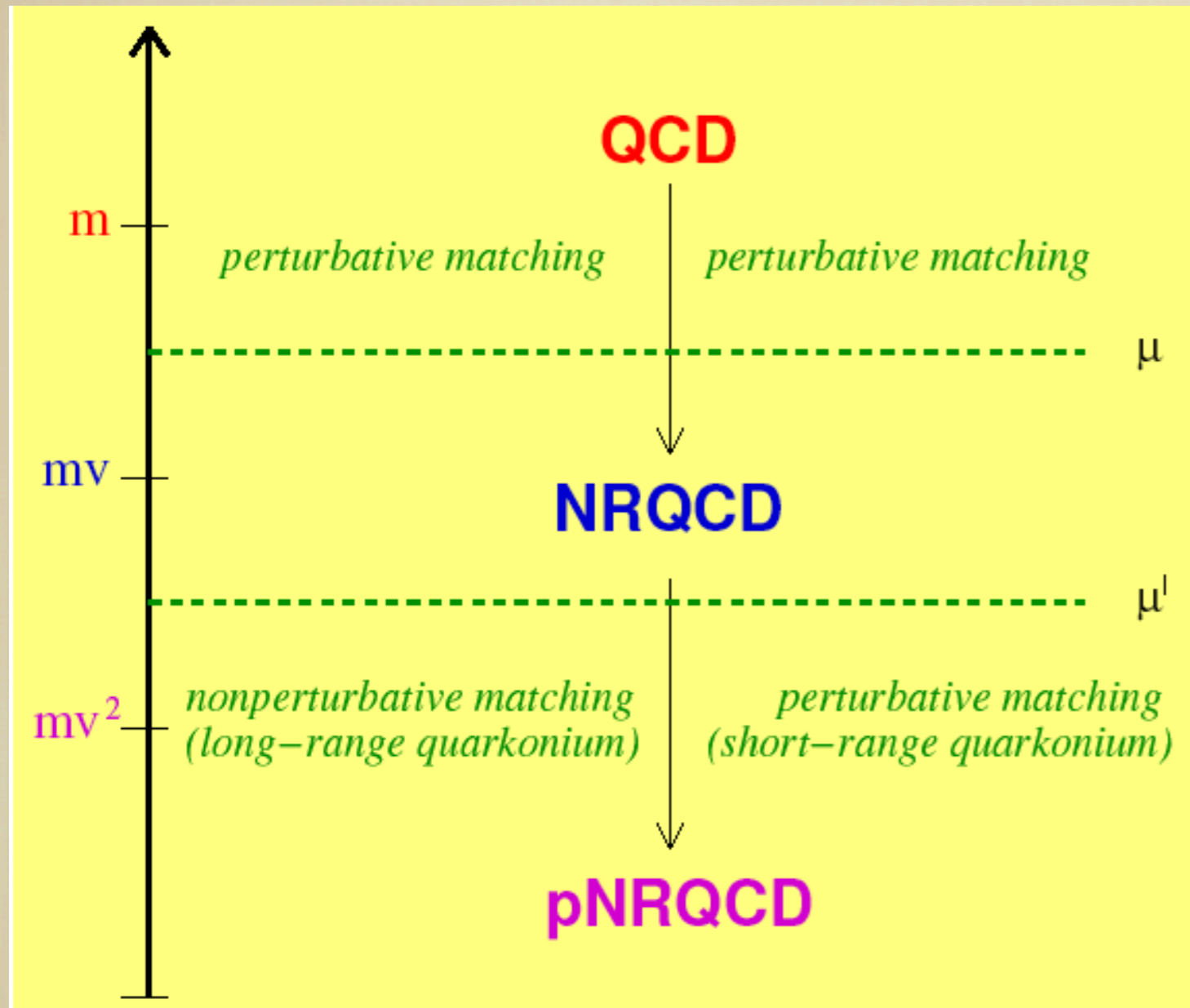
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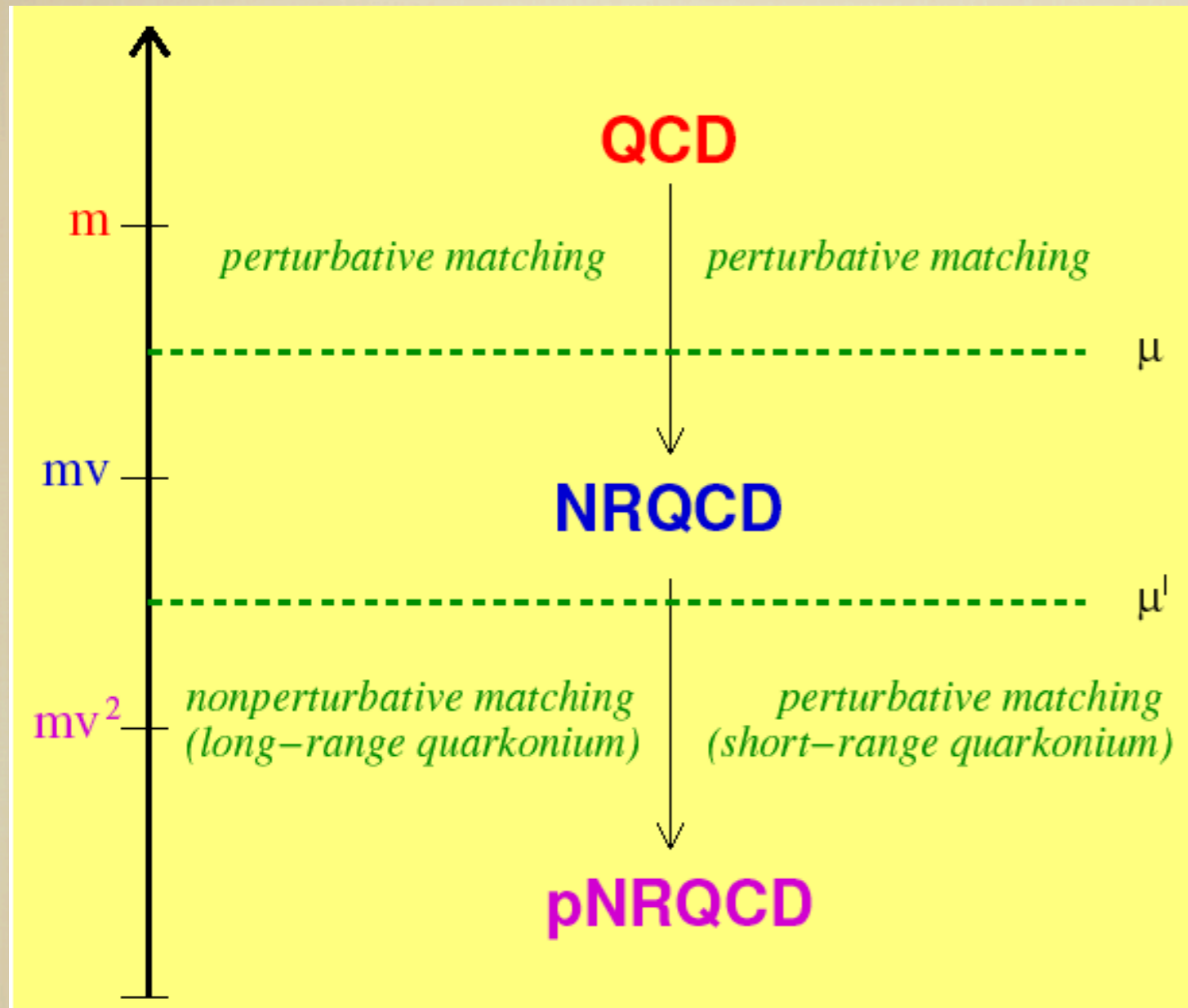


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$$\frac{E_\lambda}{E_\Lambda} = \frac{mv}{m}$$

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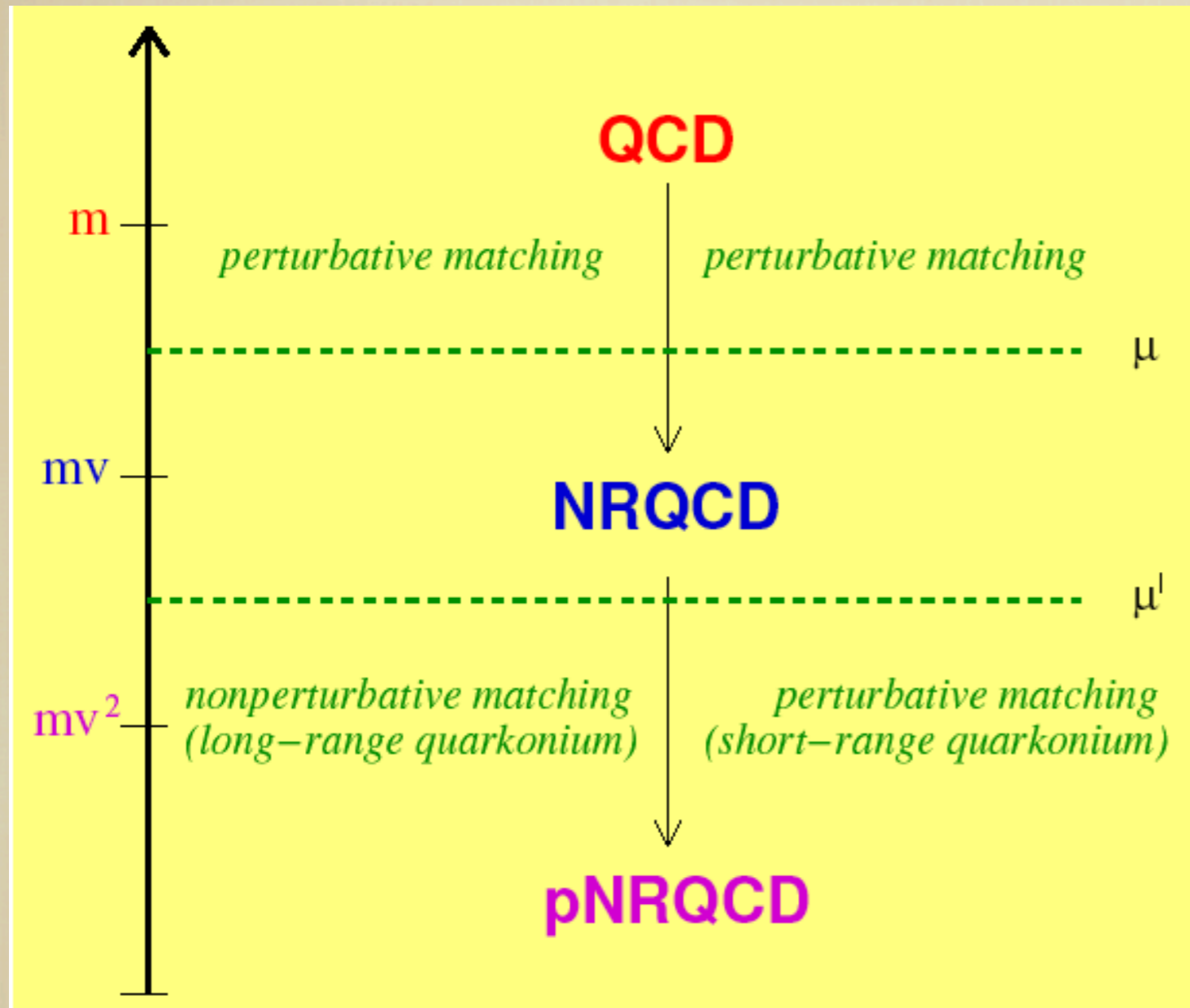
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(relative momentum)

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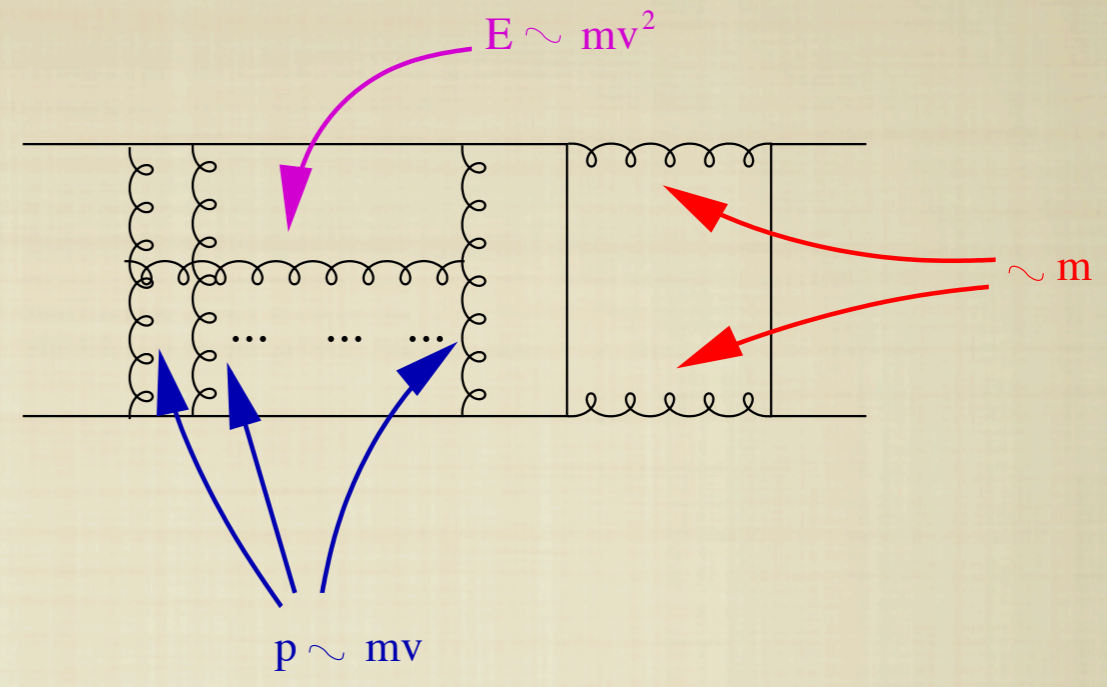
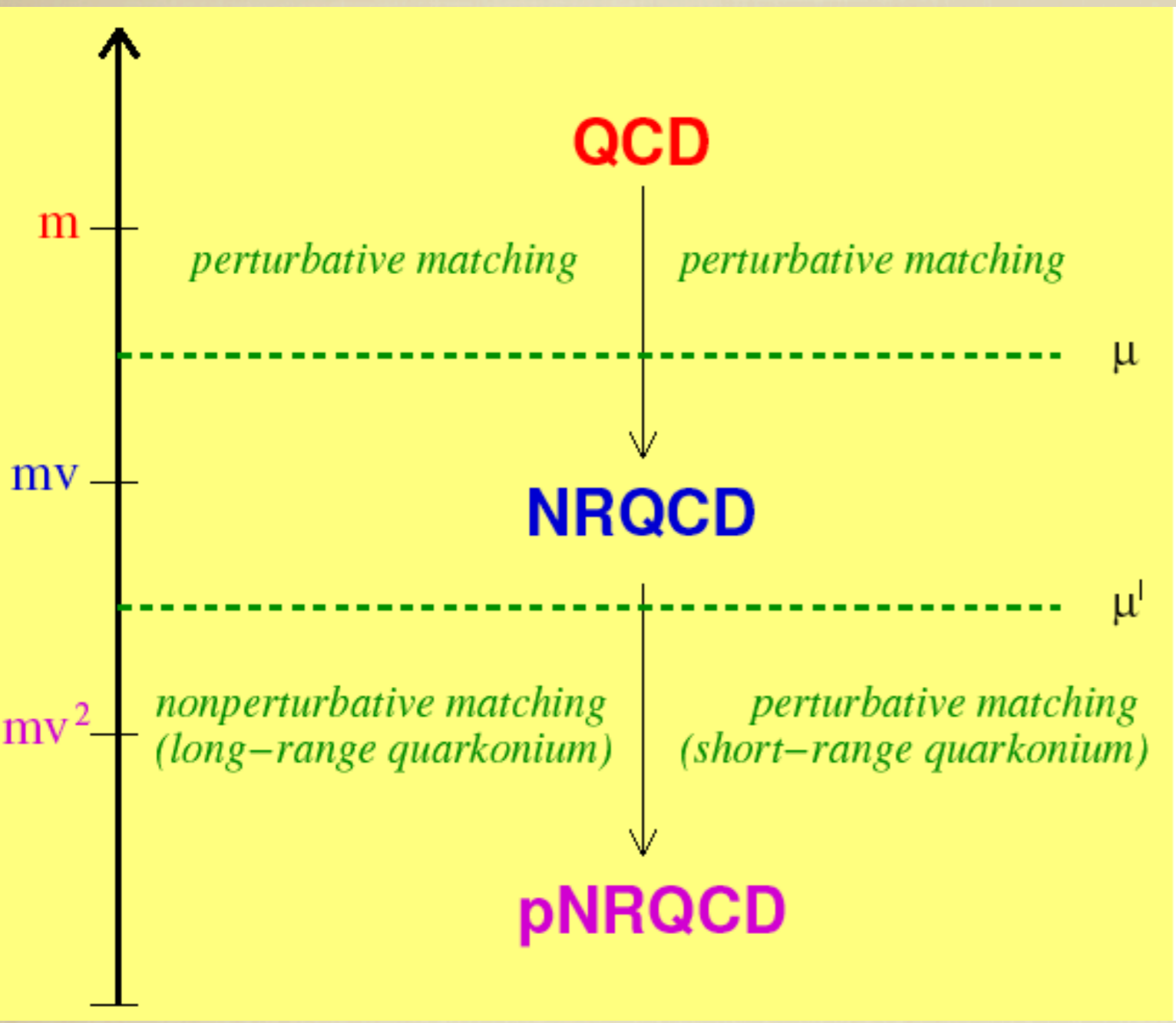
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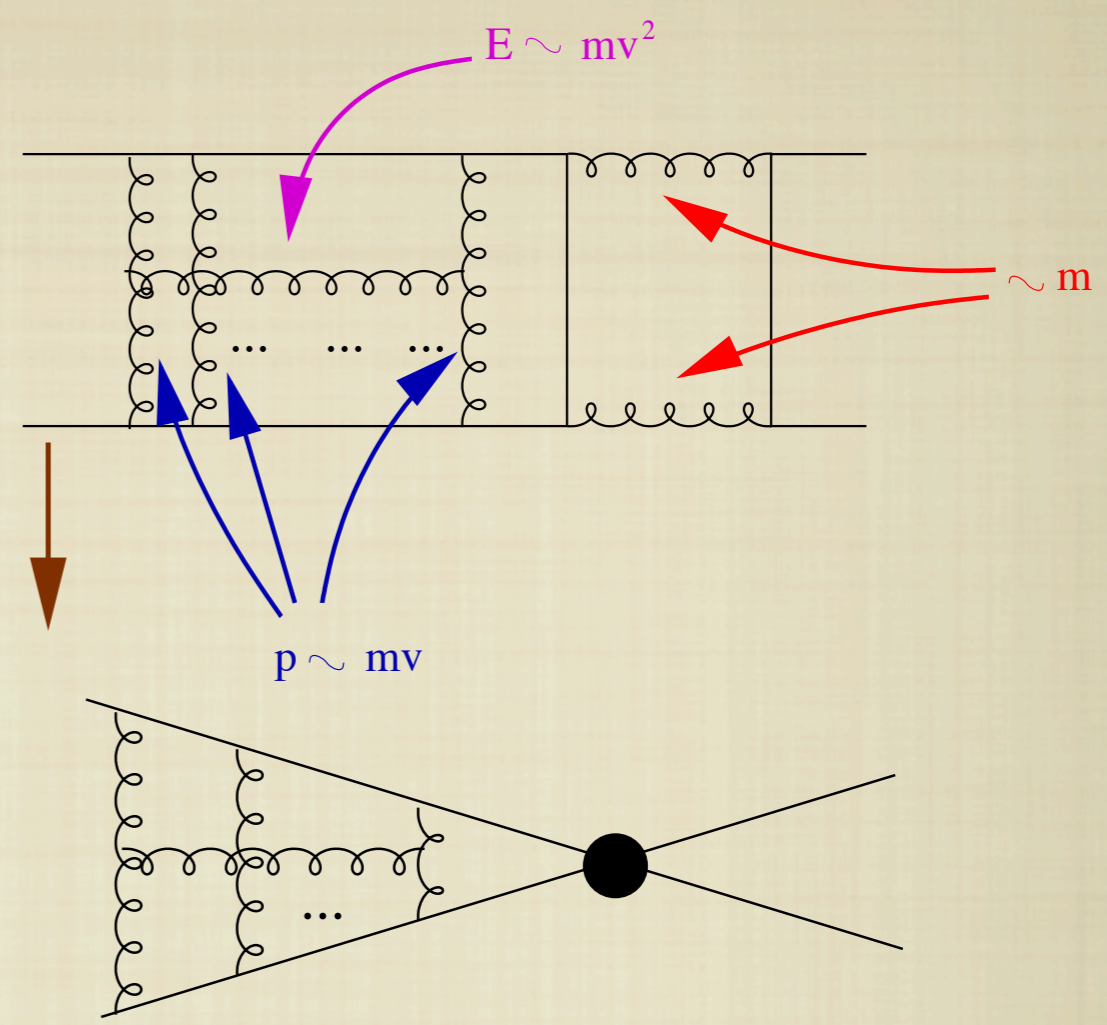
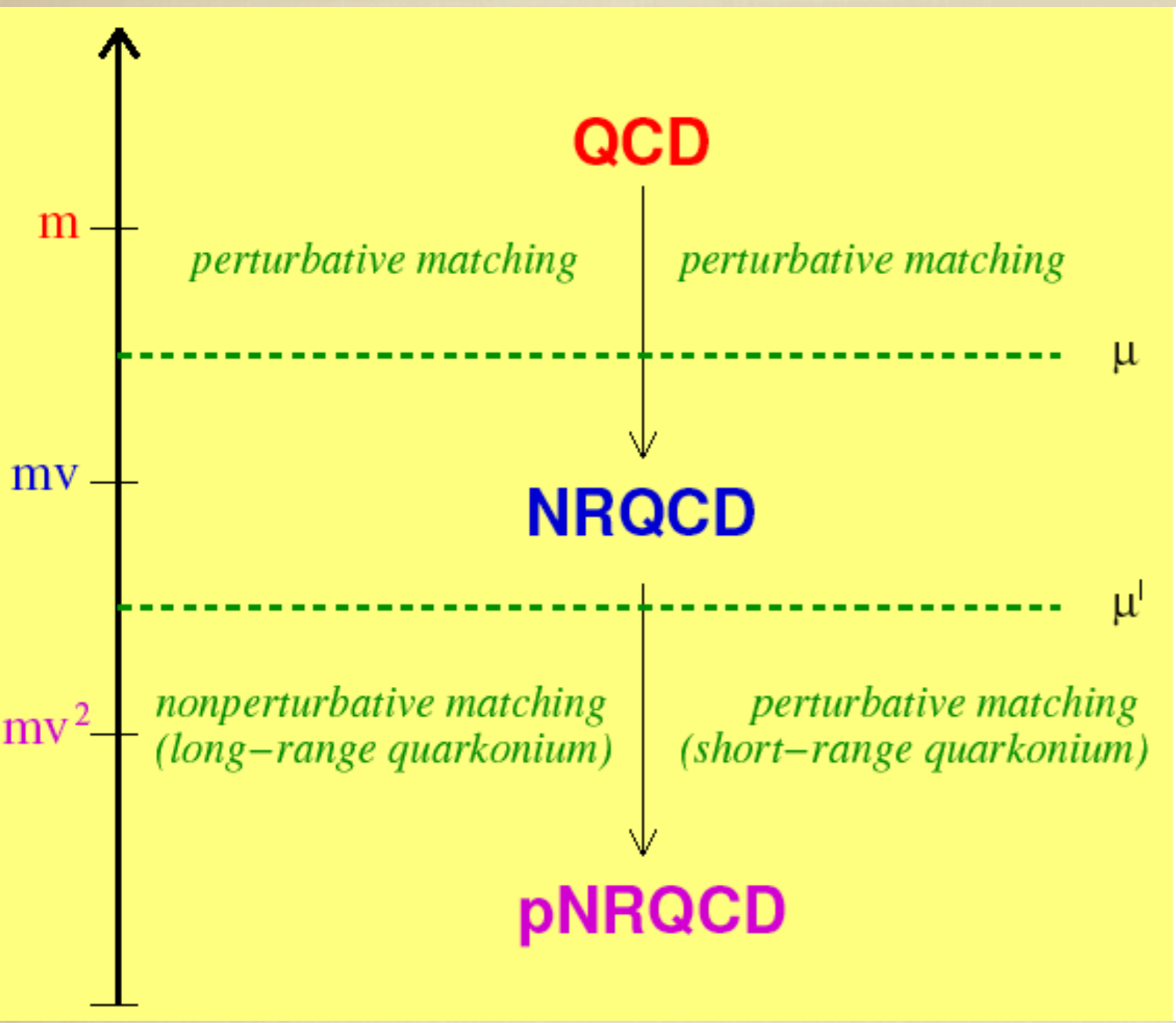
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# Quarkonium with EFT: Non Relativistic QCD (NRQCD)

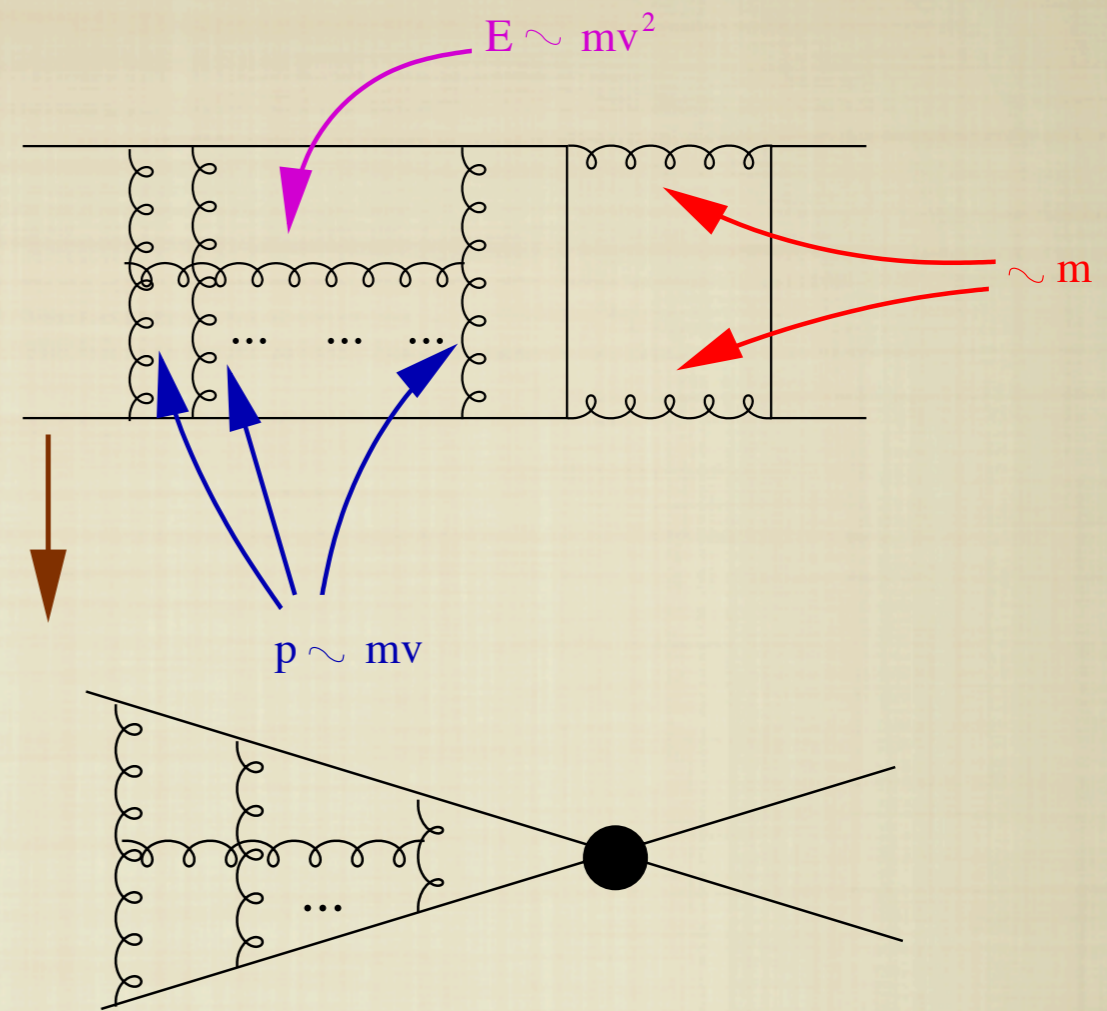
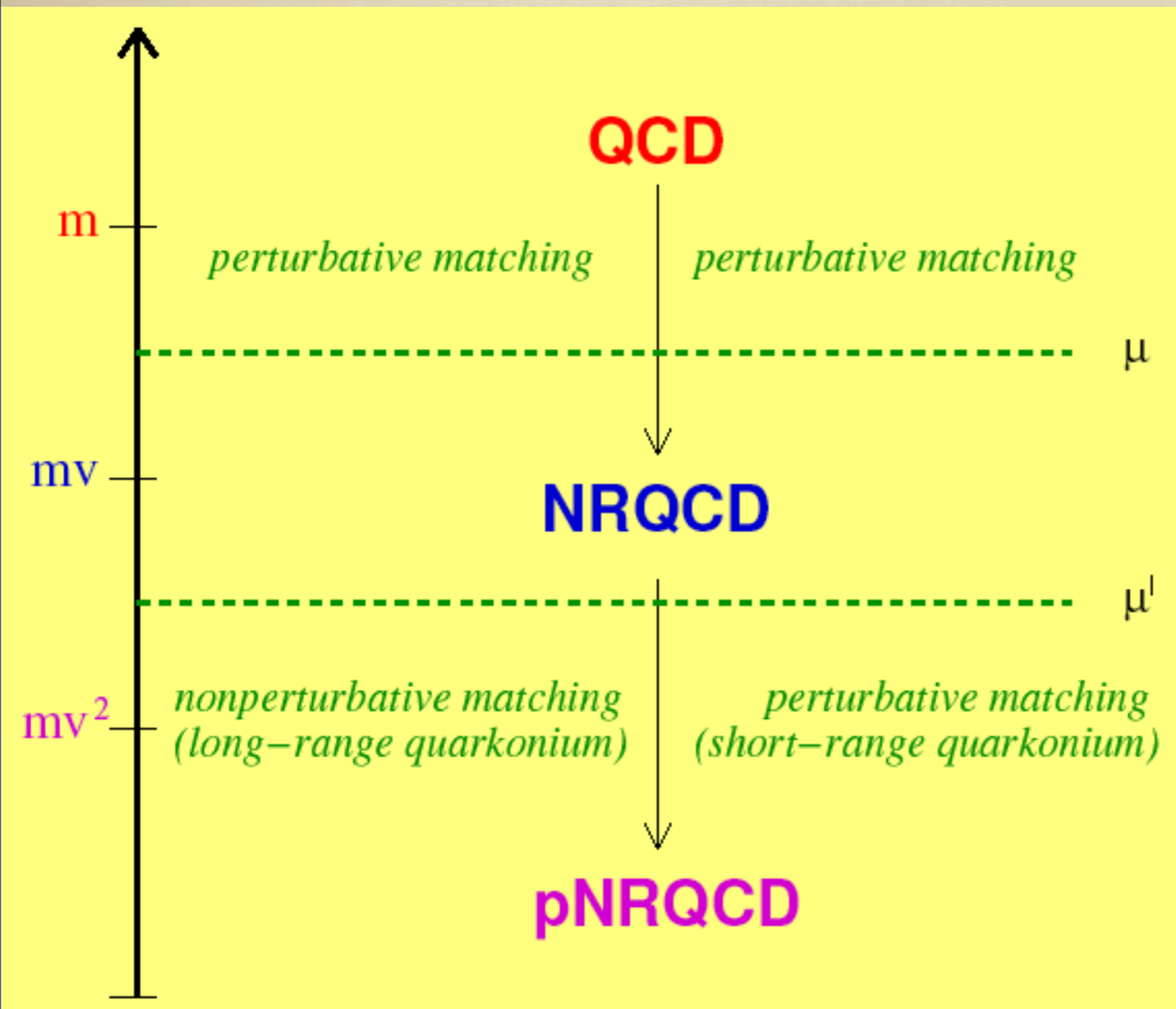


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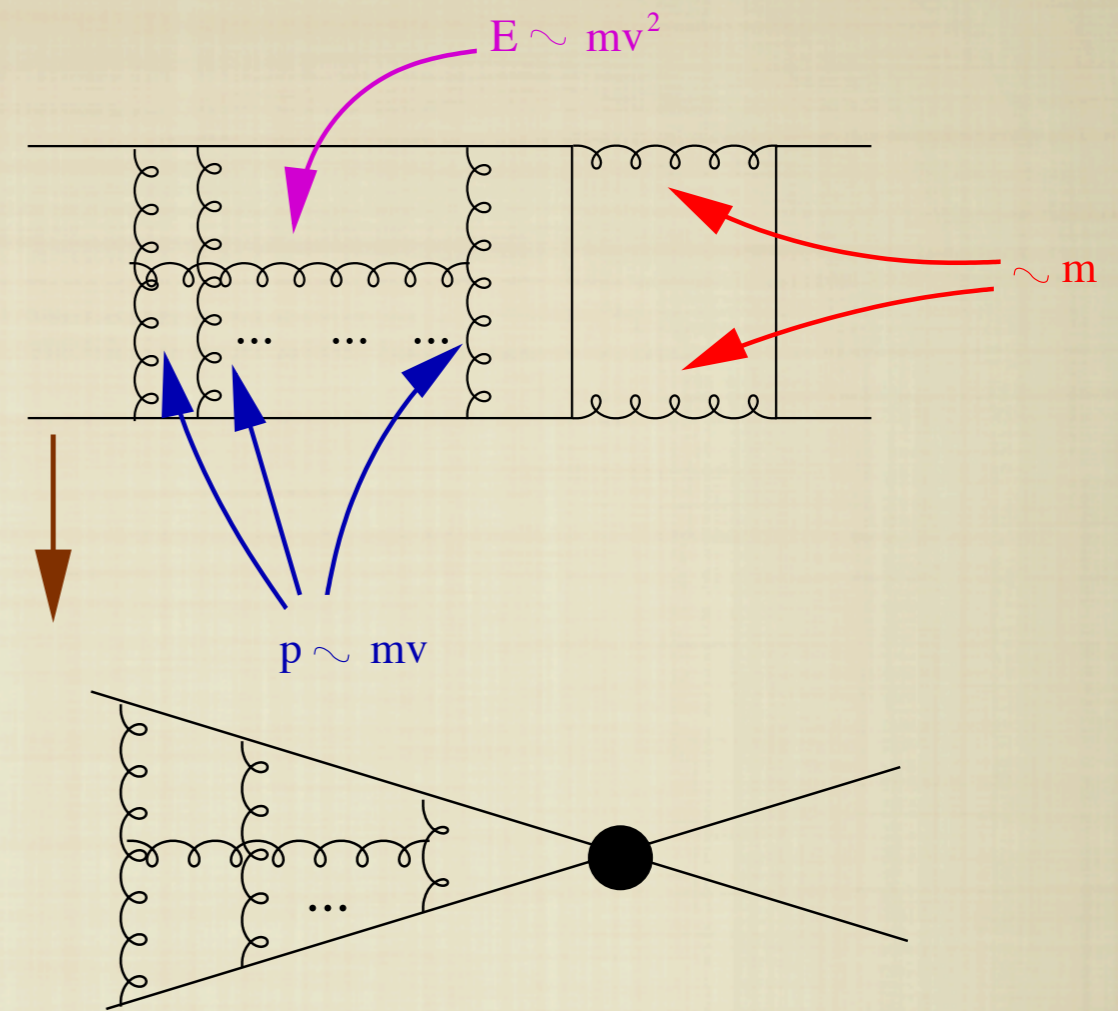
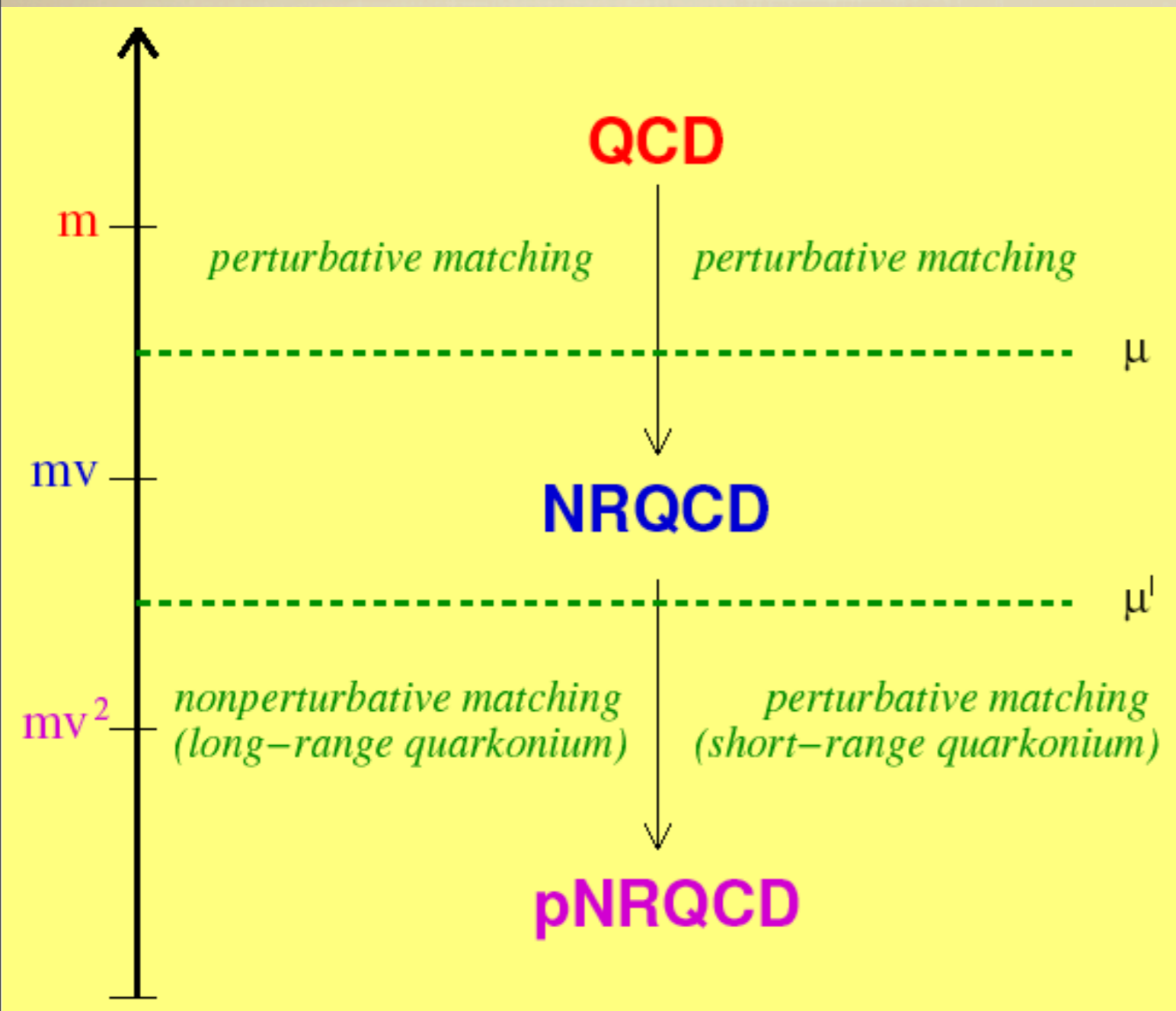


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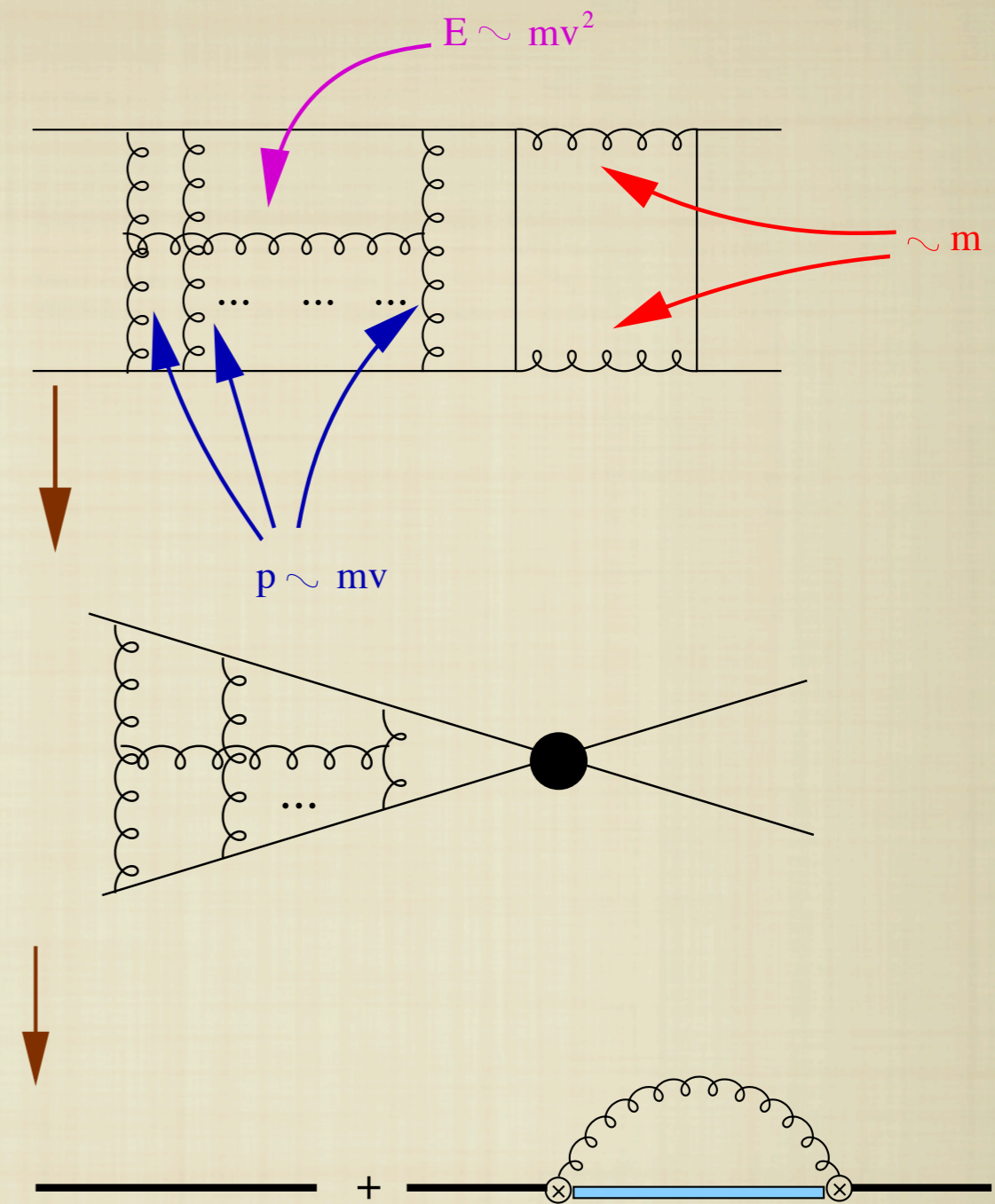
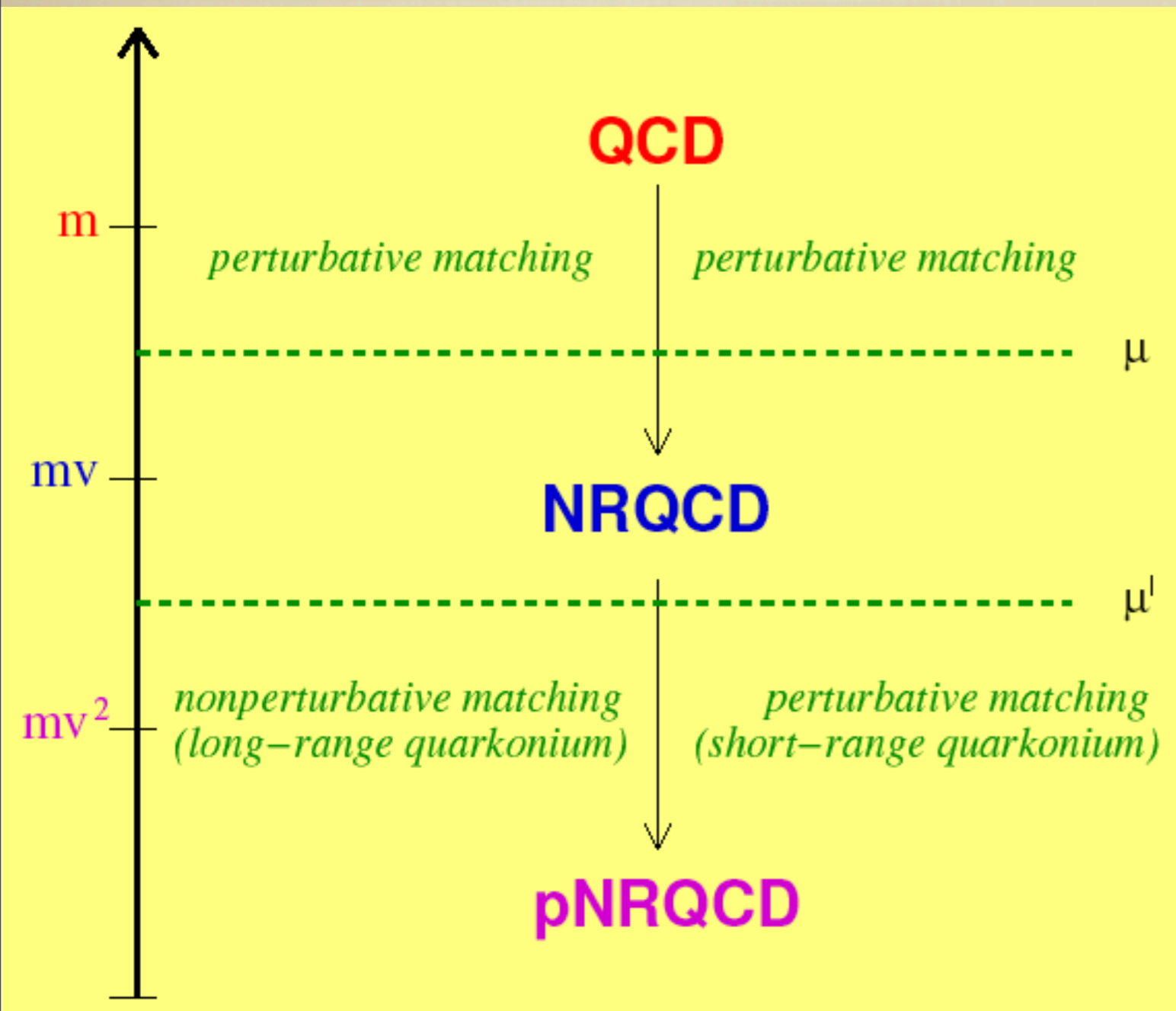
$$\mathcal{L}_{\text{NRQCD}} = \sum_n c(\alpha_s(m/\mu)) \times \frac{O_n(\mu, \lambda)}{m^n}$$

# Quarkonium with EFT: potential NonRelativistic QCD (pNRQCD)

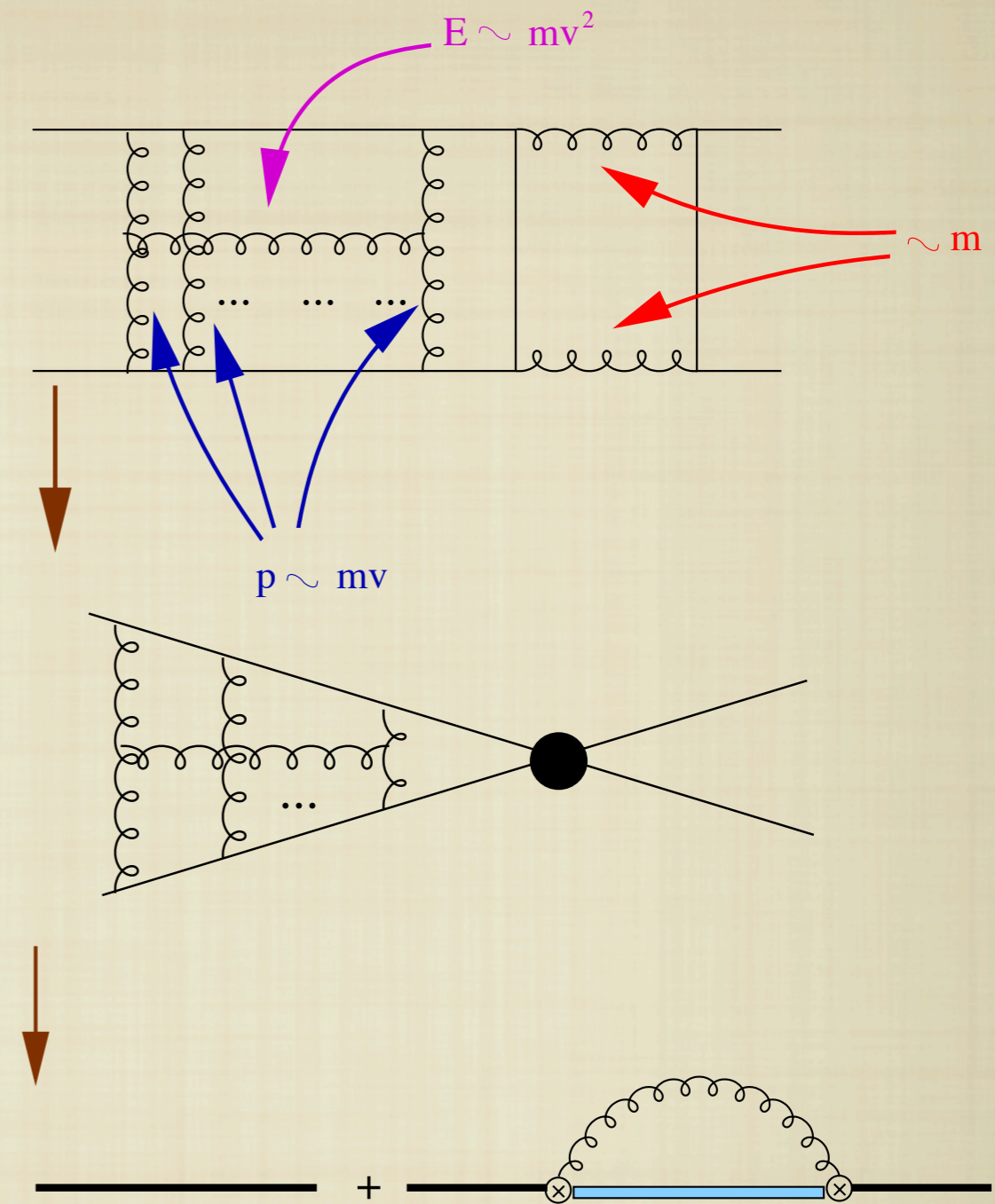
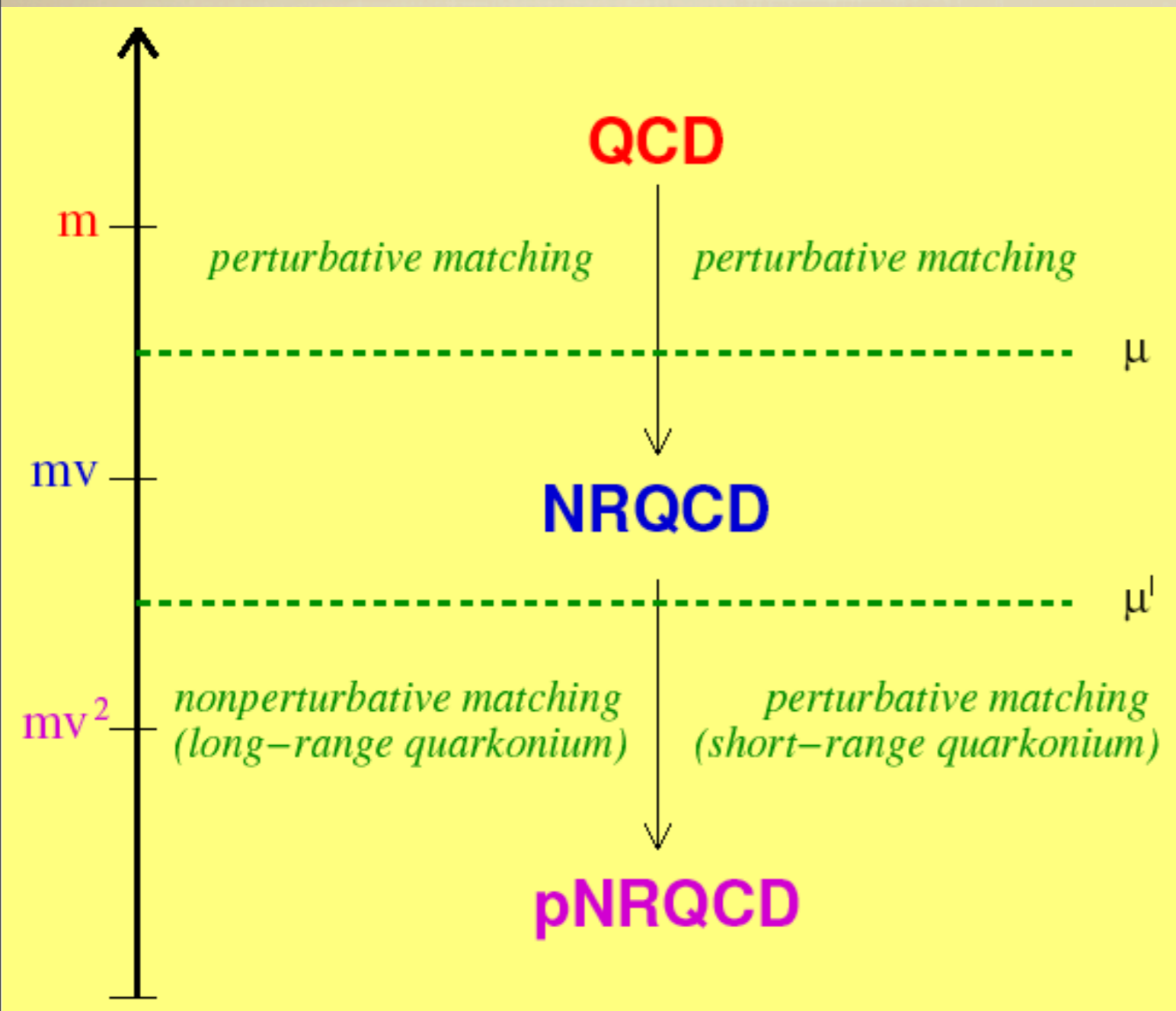




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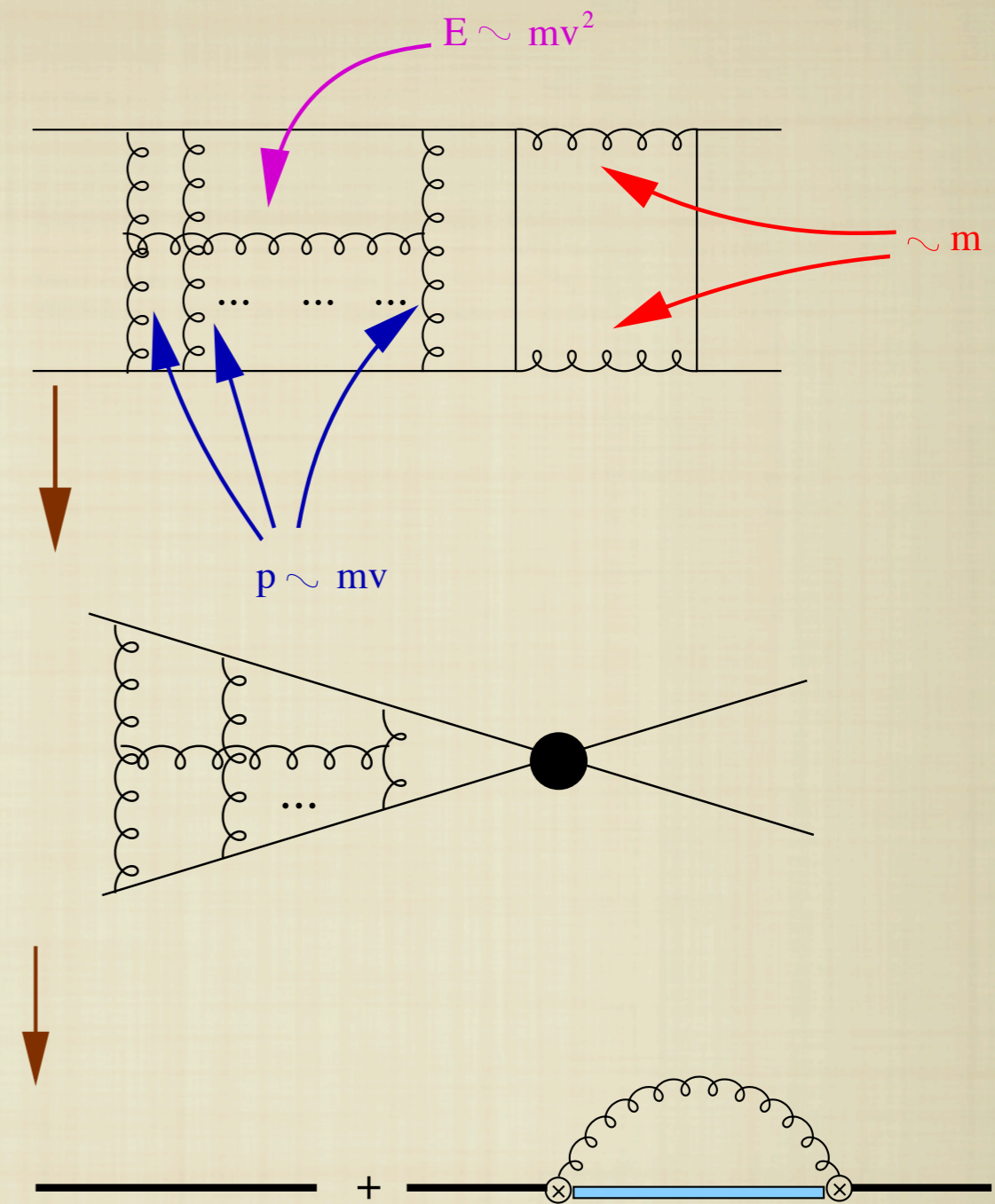
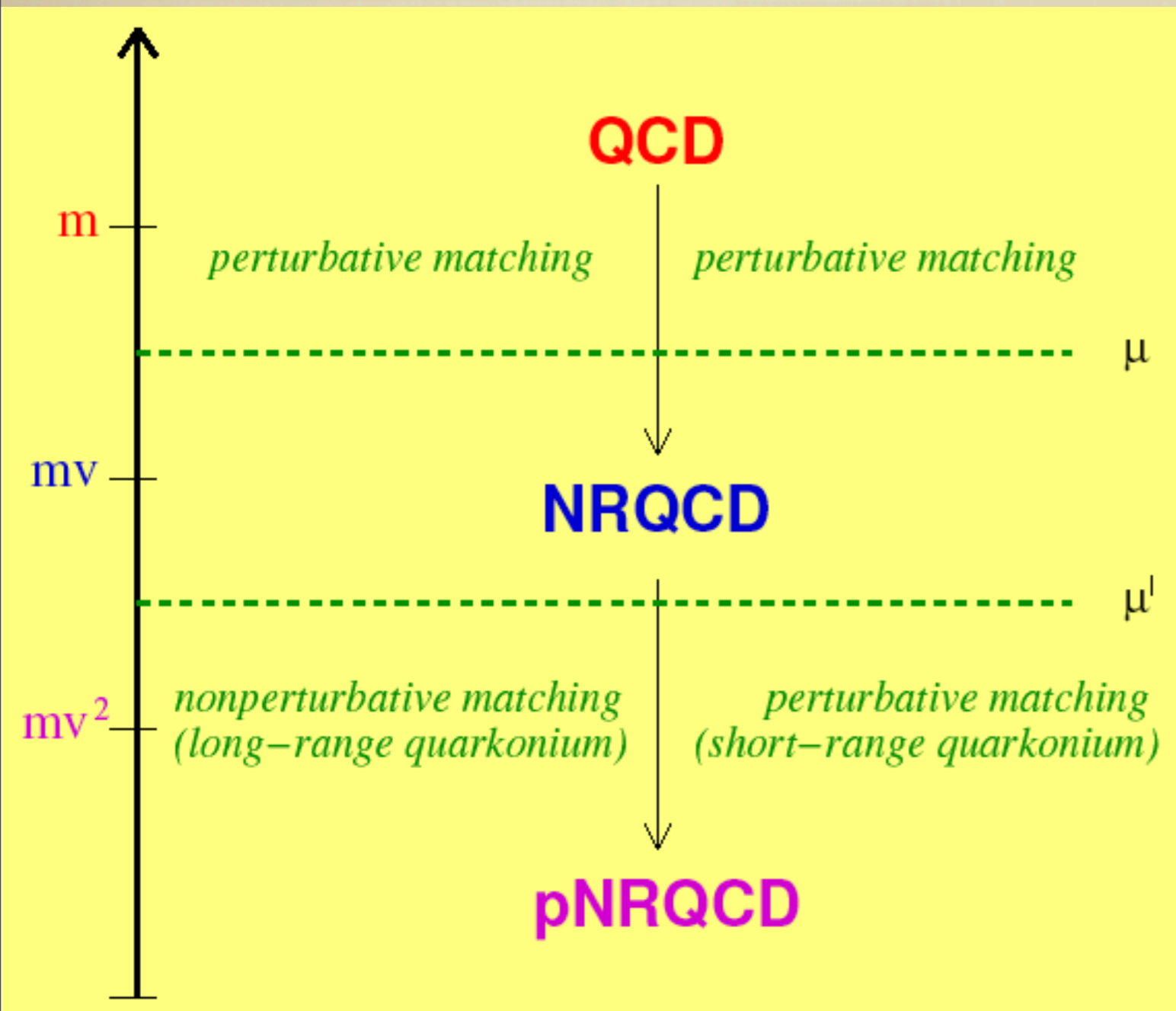
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$$\mathcal{L}_{\text{pNRQCD}} = \sum_k \sum_n \frac{1}{m^k} c_k(\alpha_s(m/\mu)) \times V(r\mu', r\mu) \times O_n(\mu', \lambda) r^n$$

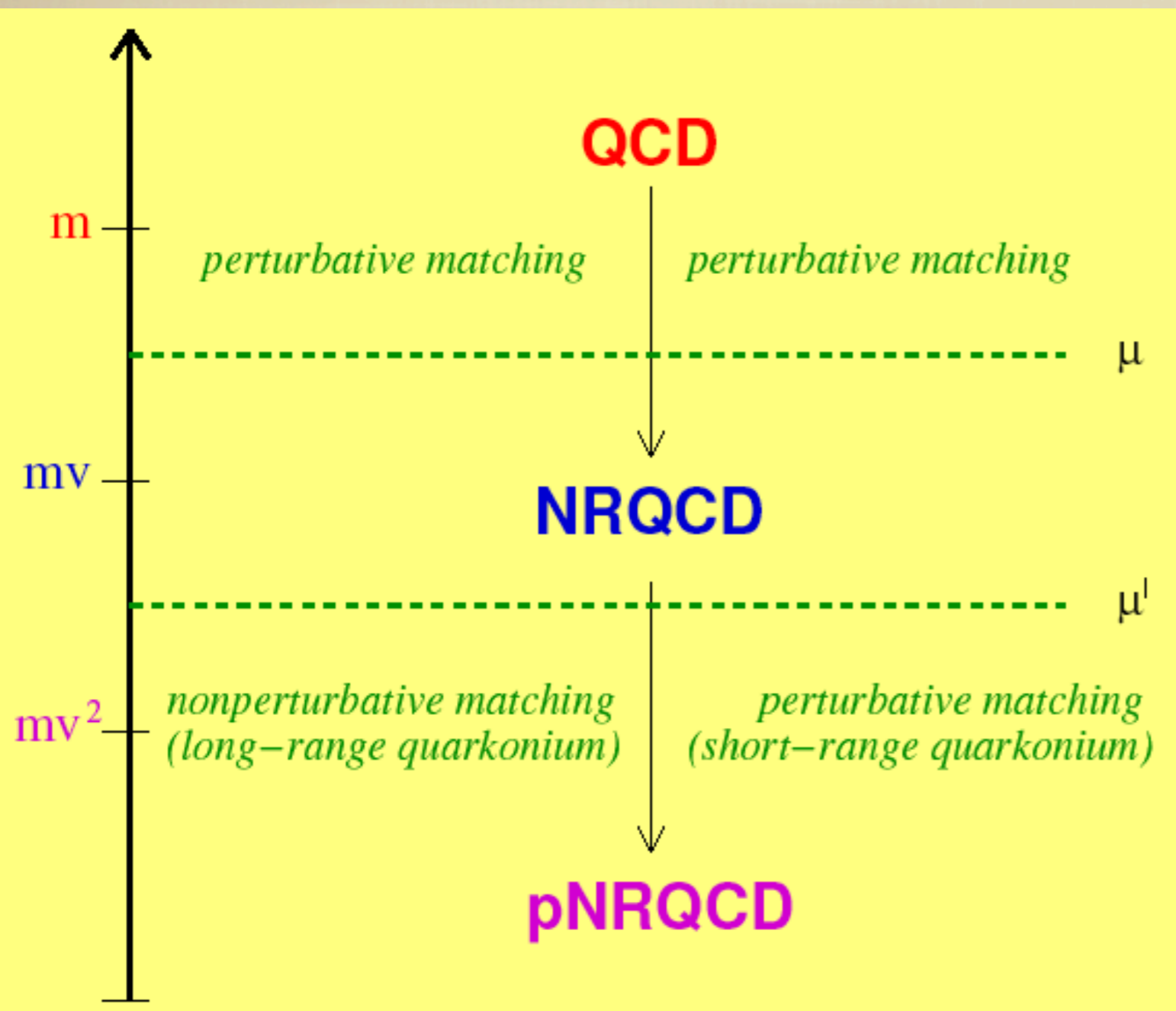


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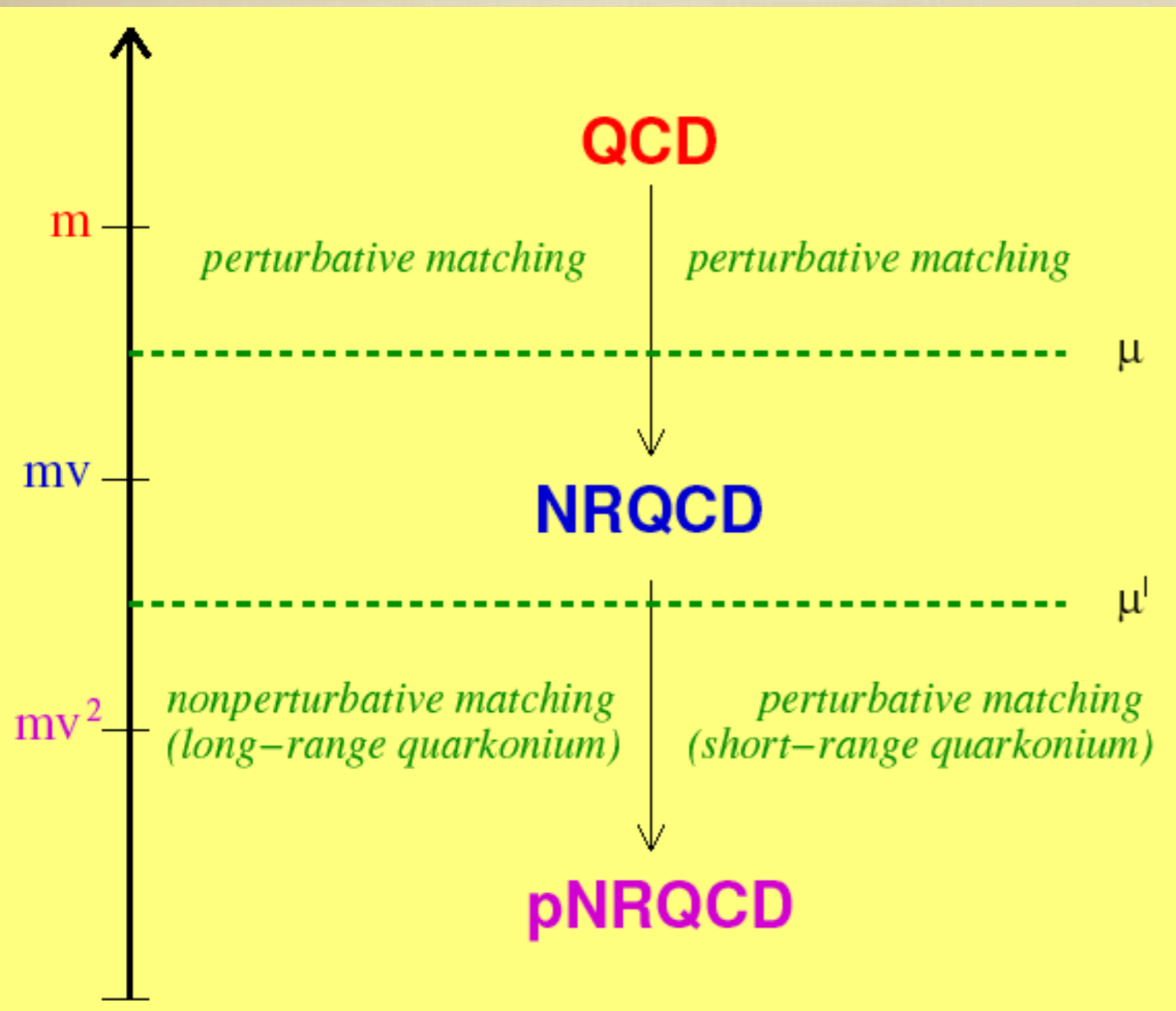
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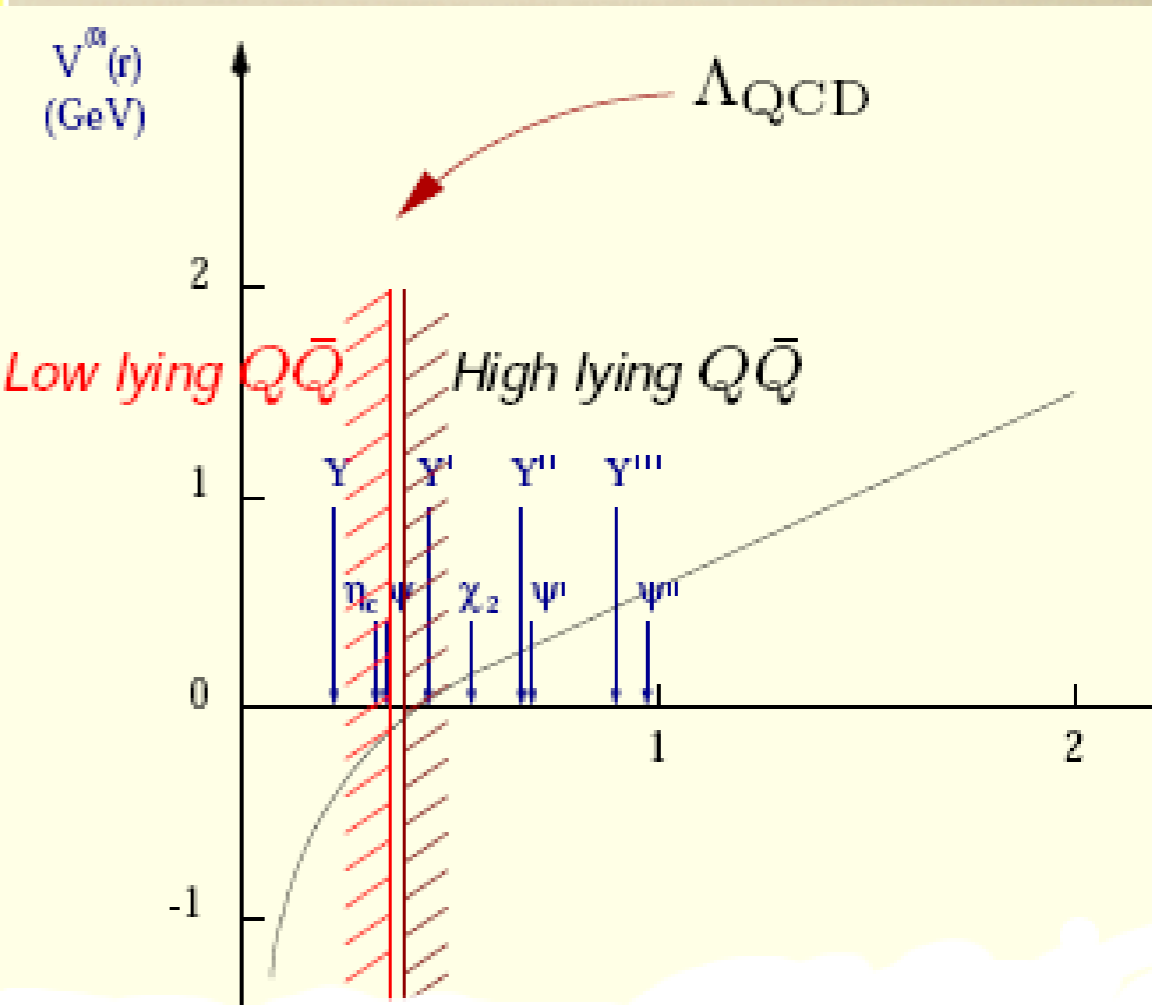
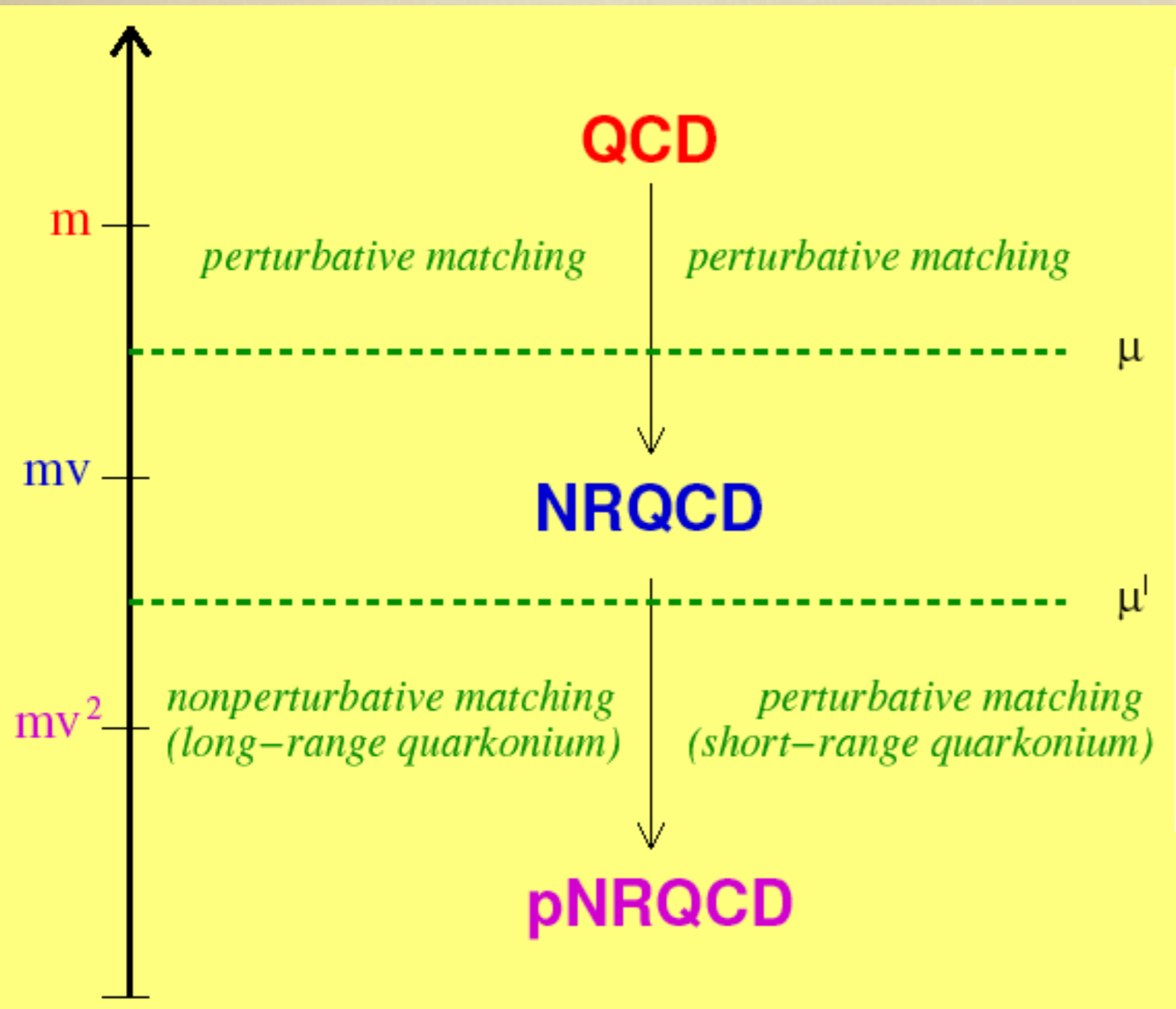
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In QCD another scale is relevant

$$\Lambda_{\text{QCD}}$$

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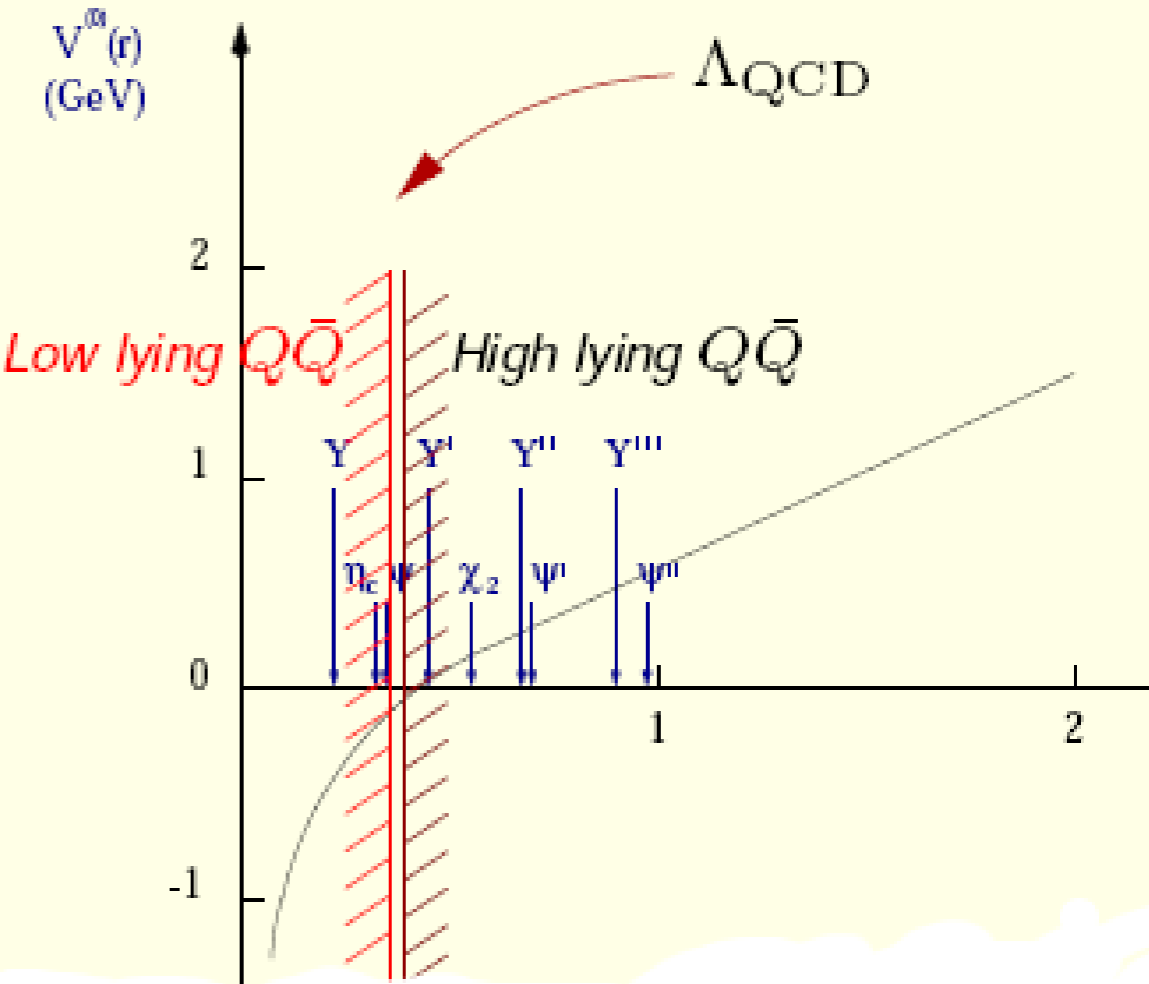
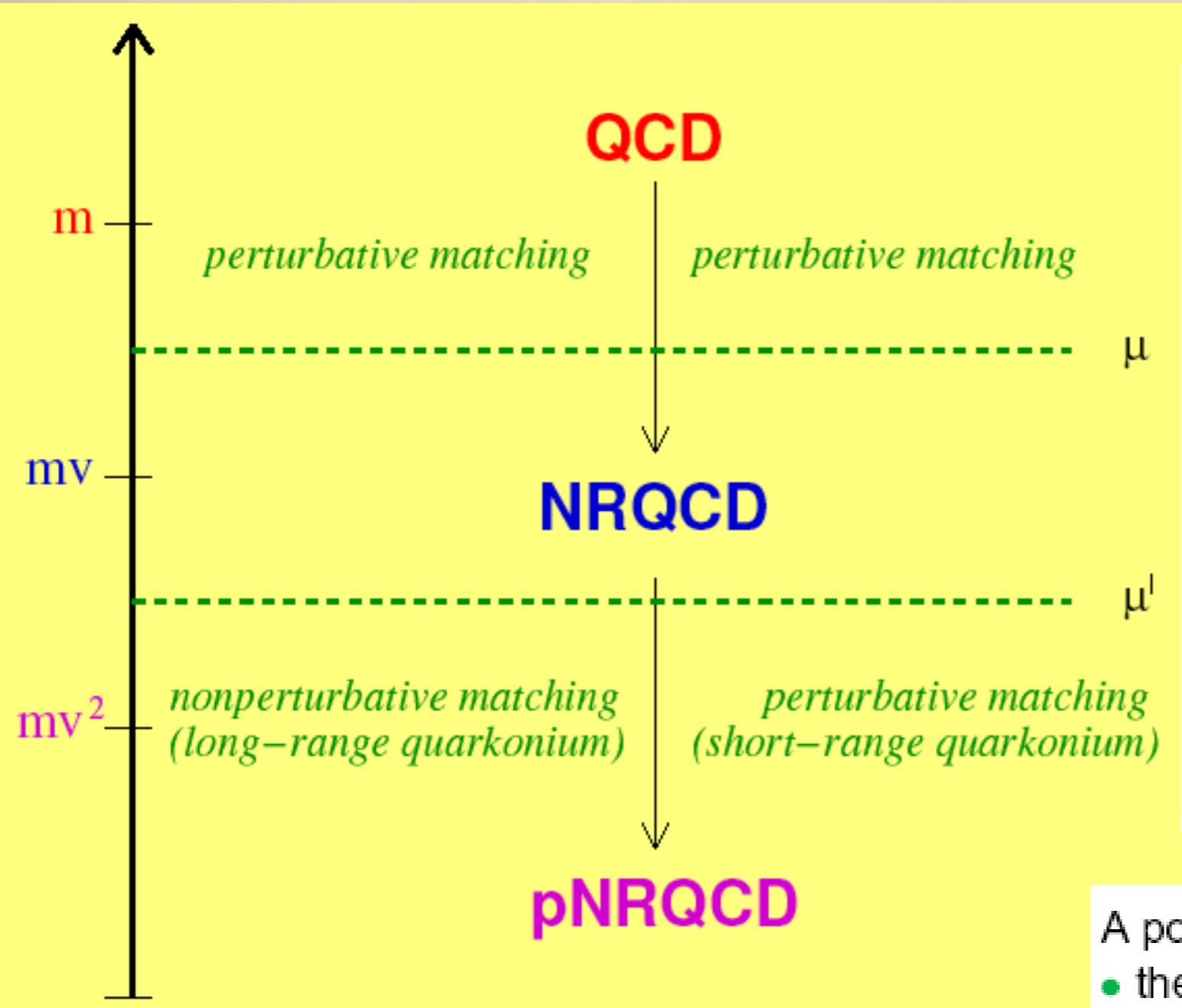


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# Quarkonium with EFT: pNRQCD



A potential picture arises at the level of pNRQCD:

- the potential is perturbative if  $mv \gg \Lambda_{\text{QCD}}$
- the potential is non-perturbative if  $mv \sim \Lambda_{\text{QCD}}$

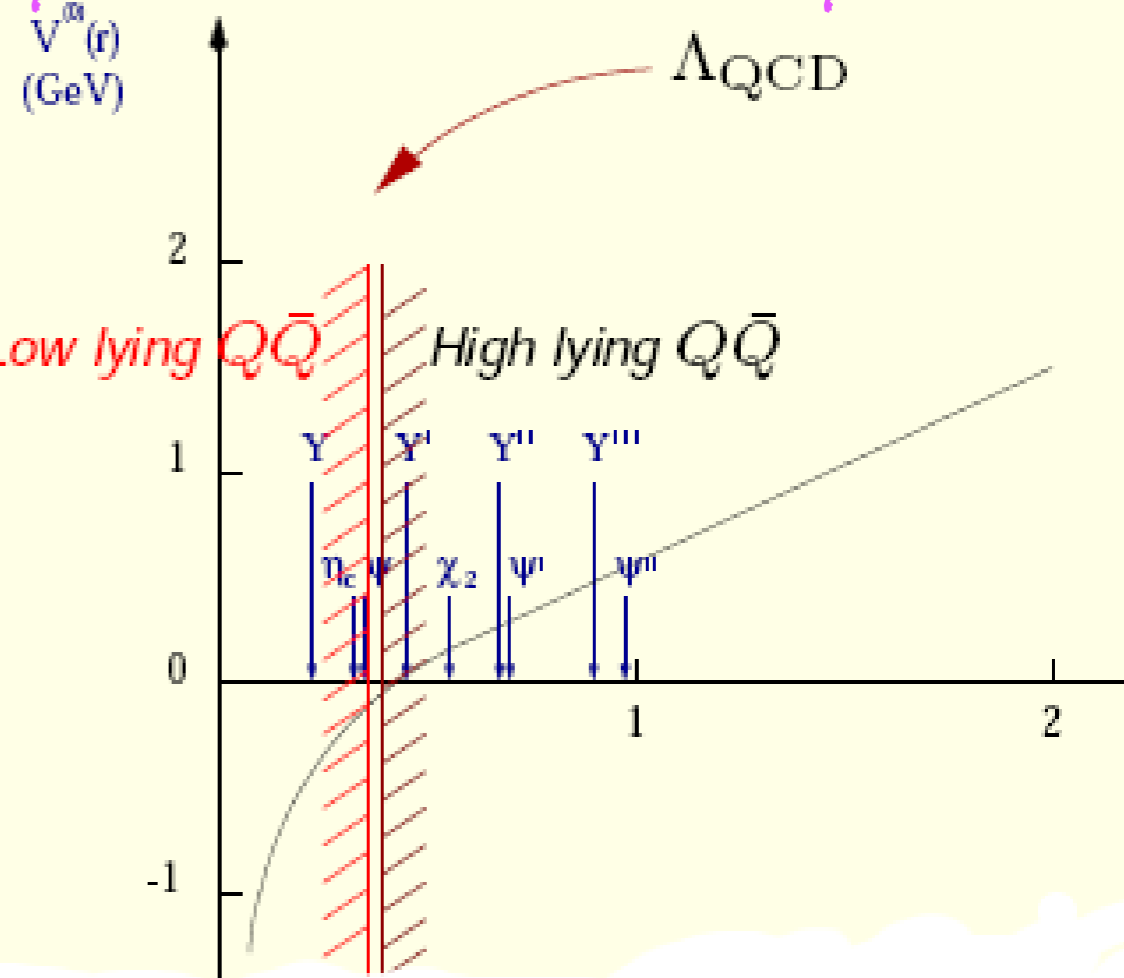
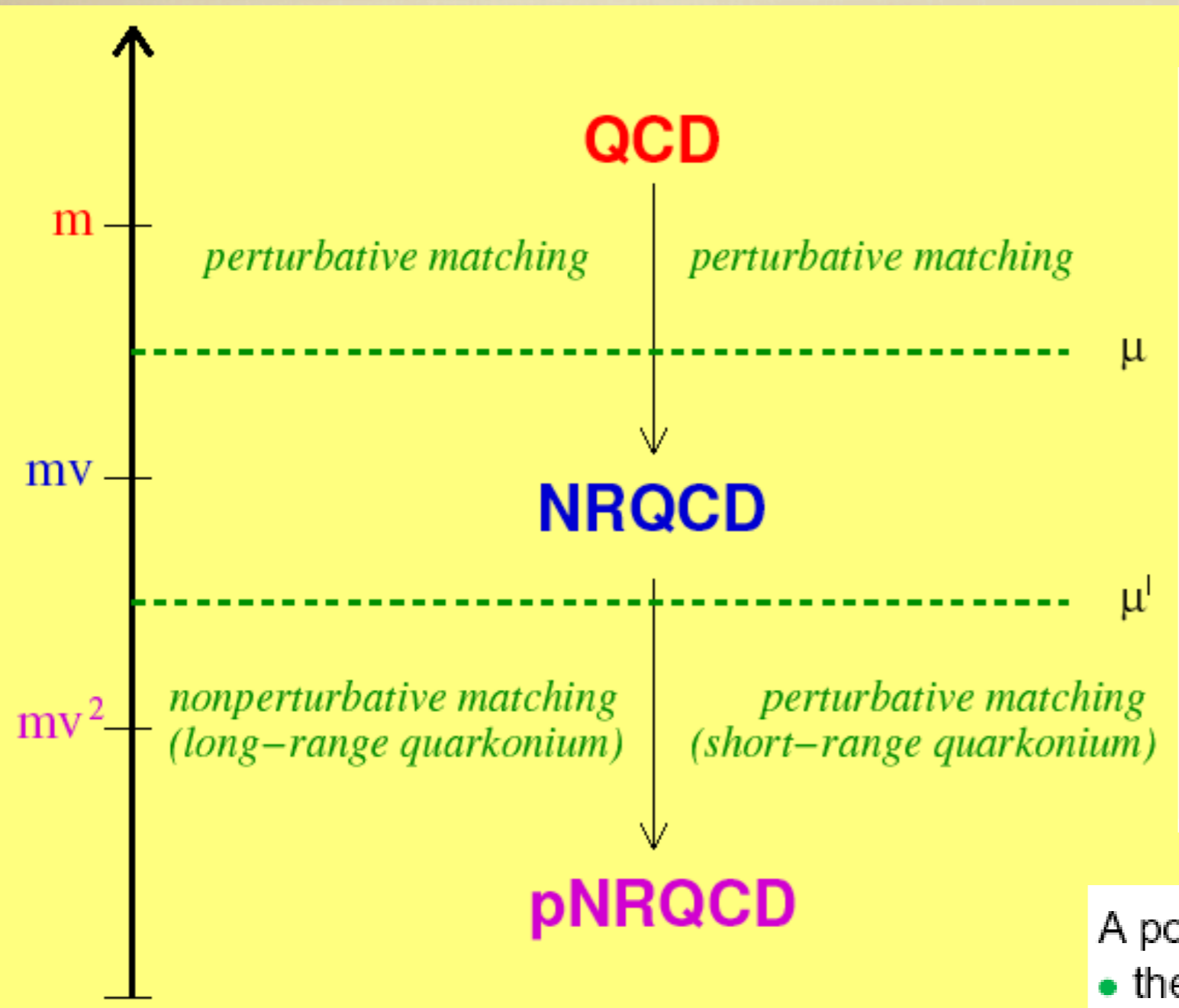
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weakly coupled  
pNRQCD

strongly coupled  
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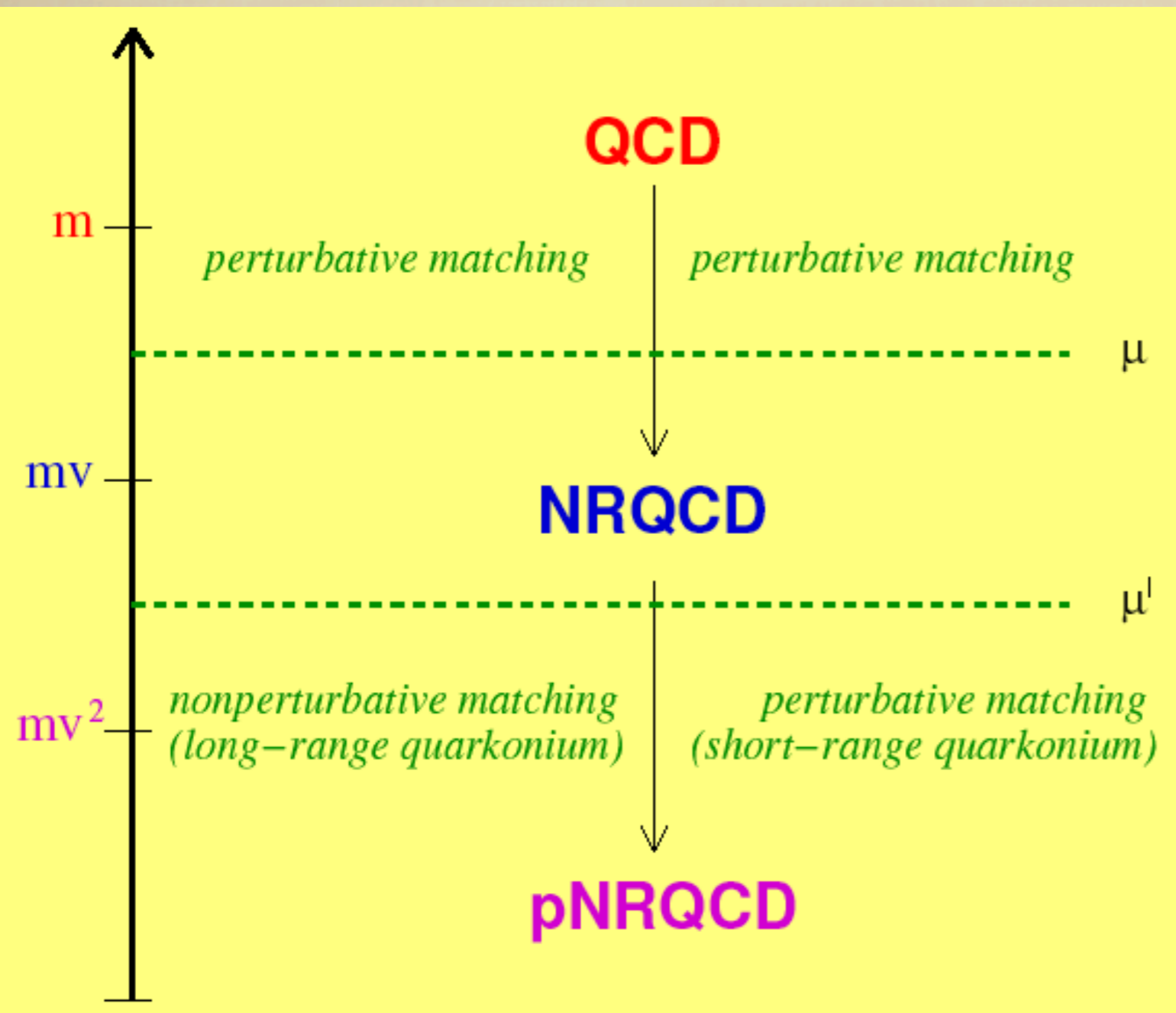
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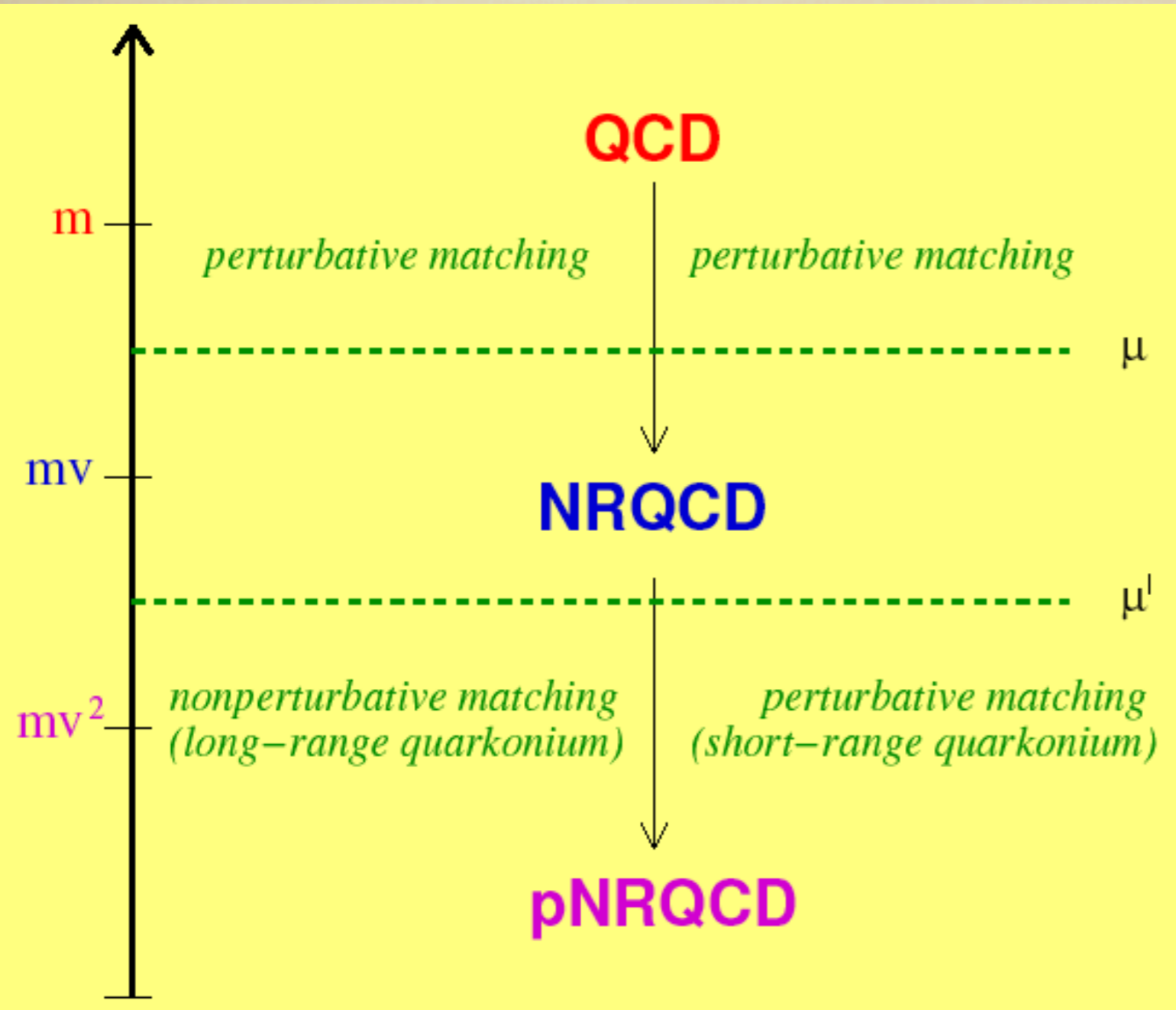
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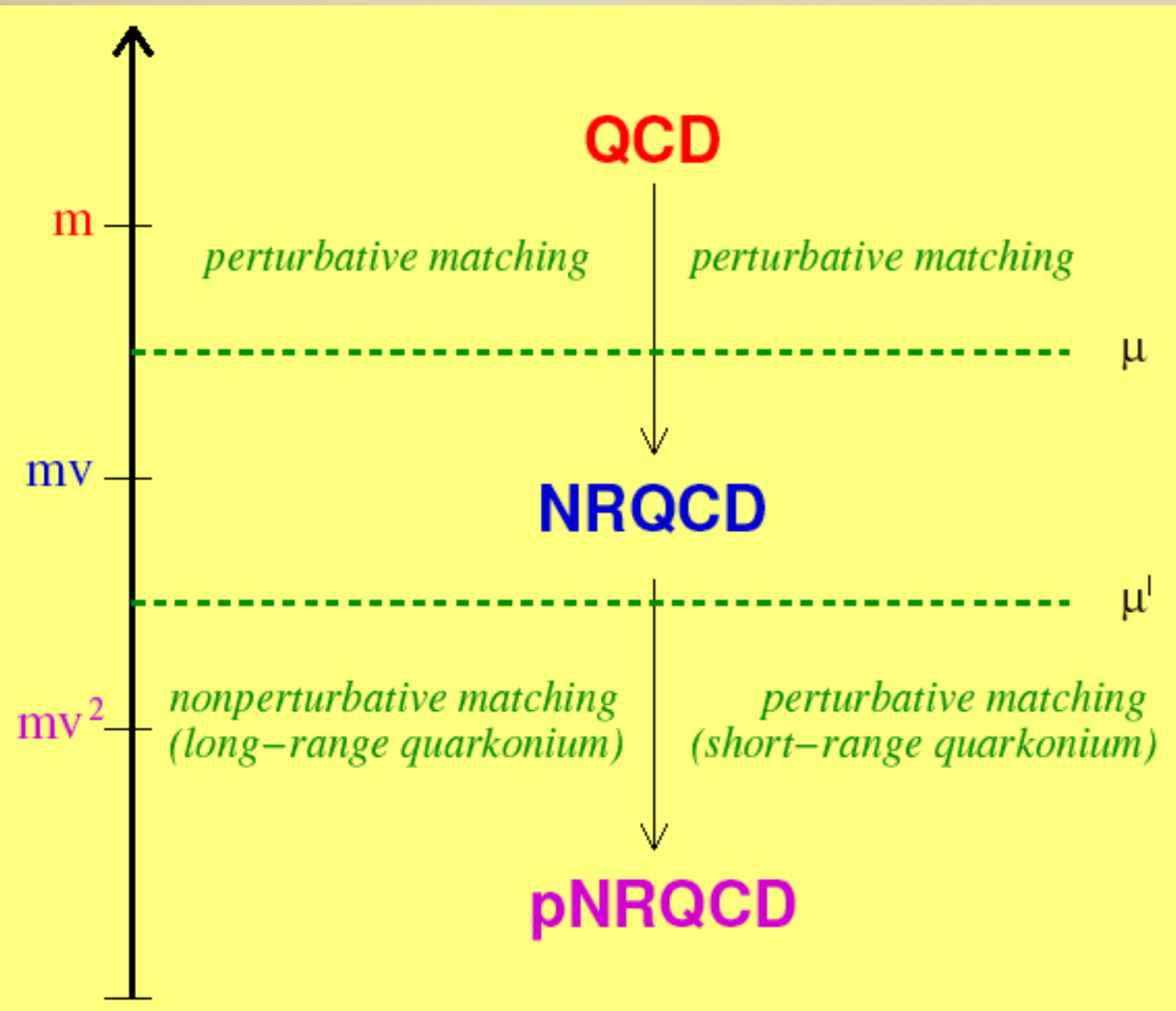
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Caswell, Lepage 86,  
Lepage, Thacker 88  
Bodwin, Braaten, Lepage 95.....



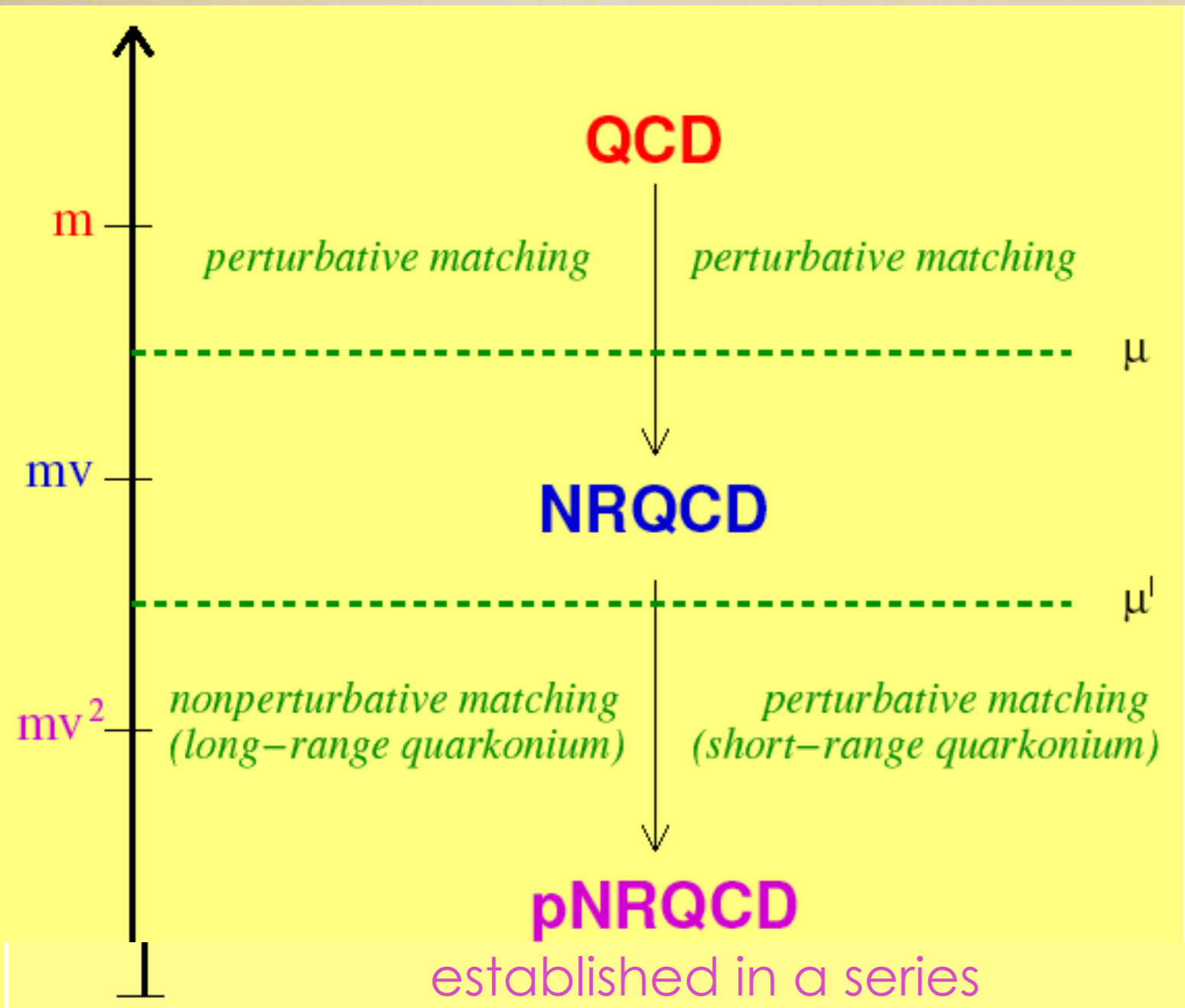
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Pineda, Soto 97, N.B. et al, 99,00,  
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of papers: Pineda, Soto 97, N. Brambilla, Pineda, Soto,  
Vairo, 99, N. Brambilla et al. 00-09  
N.B, Pineda, Soto, Vairo Review of Modern Physics 04



# Physics at the scale $m$ : NRQCD

## Quarkonium production and decays

terrific progress in production in the last few years



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- Proof of NRQCD factorization at NNLO QIU, NAYAK, STERMAN 05-08
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- Development of fragmentation function approach QIU, NAYAK, STERMAN 05--
- New calculation of the NLO color singlet channel in ep at HERA Artoisenet, et al.09, Butenshon Kniehl 09
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a coherent picture in NRQCD for quarkonium production at Tevatron, Rhic, Hera is emerging -> to be scrutinized at LHC!



# Inclusive decays

- Annihilation: the NRQCD factorization formula reads

$$\Gamma(H \rightarrow l.h.) = \sum_n \frac{2 \operatorname{Im} f^{(n)}}{M^{d_{O_n}-4}} \langle H | O_n^{4\text{-fermion}} | H \rangle$$



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Progress has been made in

- the evaluation of the factorization formula at order  $v^7$ ;
  - Brambilla Mereghetti Vairo JHEP 0608(06)039  
PRD 79(09)074002
- the (lattice) evaluation of the matrix elements.
  - Bodwin Lee Sinclair PRD 72(05)014009

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- ... and in the experimental data. E.g.

Ratio	PDGO10	PDG00	LO	NLO
$\frac{\Gamma(\chi_{c0} \rightarrow \gamma\gamma)}{\Gamma(\chi_{c2} \rightarrow \gamma\gamma)}$	$4.9 \pm 0.8$	$13 \pm 10$	3.75	$\approx 5.43$
$\frac{\Gamma(\chi_{c2} \rightarrow l.h.) - \Gamma(\chi_{c1} \rightarrow l.h.)}{\Gamma(\chi_{c0} \rightarrow \gamma\gamma)}$	$440 \pm 100$	$270 \pm 200$	$\approx 347$	$\approx 383$
$\frac{\Gamma(\chi_{c0} \rightarrow l.h.) - \Gamma(\chi_{c1} \rightarrow l.h.)}{\Gamma(\chi_{c0} \rightarrow \gamma\gamma)}$	$4000 \pm 600$	$3500 \pm 2500$	$\approx 1300$	$\approx 2781$
$\frac{\Gamma(\chi_{c0} \rightarrow l.h.) - \Gamma(\chi_{c2} \rightarrow l.h.)}{\Gamma(\chi_{c2} \rightarrow l.h.) - \Gamma(\chi_{c1} \rightarrow l.h.)}$	$8.0 \pm 0.9$	$12.1 \pm 3.2$	2.75	$\approx 6.63$
$\frac{\Gamma(\chi_{c0} \rightarrow l.h.) - \Gamma(\chi_{c1} \rightarrow l.h.)}{\Gamma(\chi_{c2} \rightarrow l.h.) - \Gamma(\chi_{c1} \rightarrow l.h.)}$	$9.0 \pm 1.1$	$13.1 \pm 3.3$	3.75	$\approx 7.63$

$m_c = 1.5 \text{ GeV}$      $\alpha_s(2m_c) = 0.245$   
in NLO,  $v^7$  terms are not included

The table clearly shows that the data are sensitive to NLO corrections in the Wilson coefficients  $f^{(n)}$  (and perhaps also to relativistic corrections).



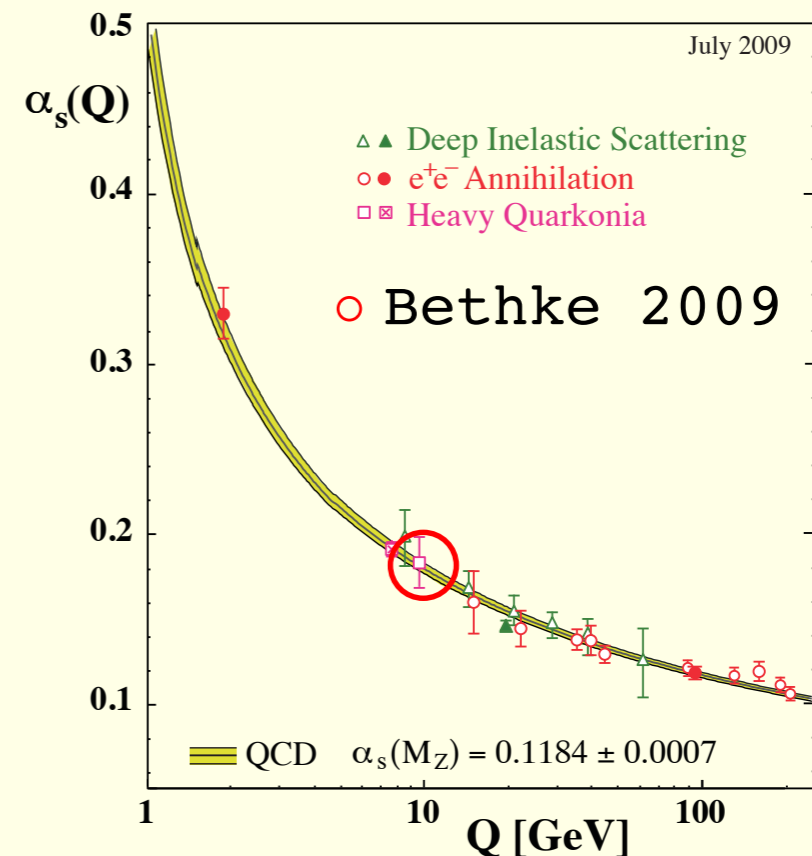
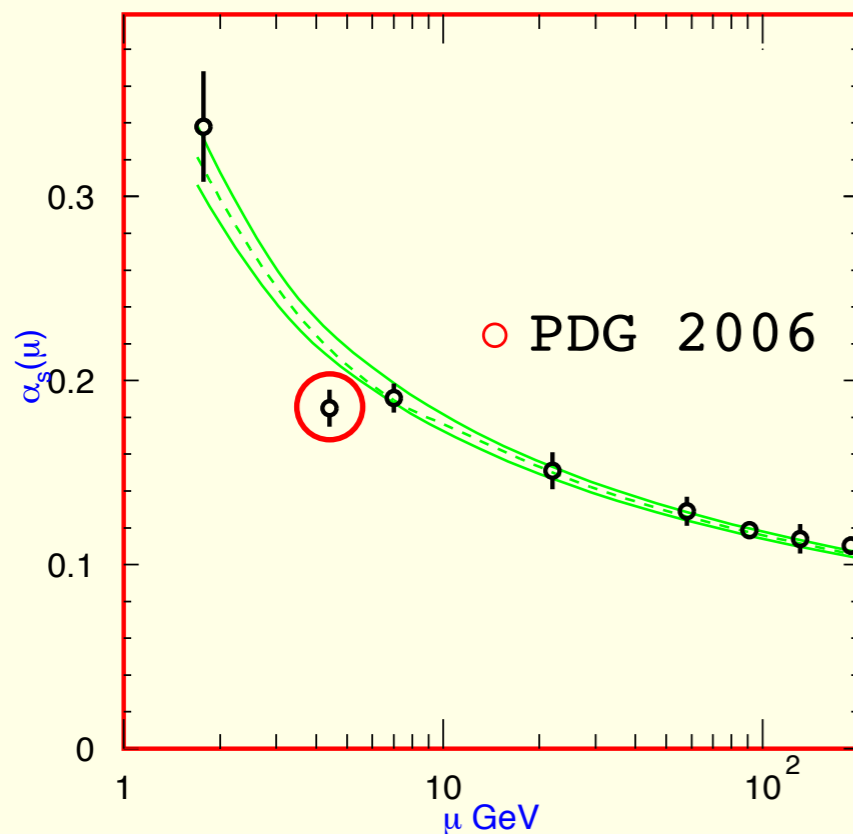
## $\alpha_s$ from $\Upsilon(1S)$ decay

- New CLEO data on  $\Upsilon(1S) \rightarrow \gamma X$ ,
- new lattice determinations of NRQCD matrix elements,

have led to an improved NLO analysis of  $\Gamma(\Upsilon(1S) \rightarrow \gamma X)/\Gamma(\Upsilon(1S) \rightarrow X)$  and to an improved determination of  $\alpha_s$  at the  $\Upsilon$ -mass scale:

$$\alpha_s(M_{\Upsilon(1S)}) = 0.184^{+0.015}_{-0.014}, \quad \alpha_s(M_Z) = 0.119^{+0.006}_{-0.005}$$

○ Brambilla Garcia Soto Vairo PRD 75(07)074014



Physics at the scale  $mv$  and  $mv^2$  : pNRQCD



# Physics at the scale $mv$ and $mv^2$ : pNRQCD

pNRQCD is today the theory used to address quarkonium bound states properties

- Spectra
  - high order perturbative calculations
  - Resonances
- Decays
  - Inclusive & seminclusive decays
  - M1 and E1 transitions
  - Electromagnetic widths, Lines Shapes
- Doubly charmed baryons and QQQ
- Standard model parameters extraction
  - c and b masses,  $\alpha_s$
- Gluelumps and Hybrids
- Threshold  $t\bar{t}$  cross section (for the ILC)
- Nonperturbative potentials for the lattice
- General features of the NR EFTs



# PNRQCD and quarkonium

Several cases for the physics at hand

The EFT has been constructed

- \*Work at calculating higher order perturbative corrections in  $v$  and  $\alpha_s$
- \*Resumming the log
- \*Calculating/extracting nonperturbatively the low energy quantities
- \*Extending the theory (electromagnetic effect, 3 bodies)



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- \*Mass and width of quarkonium at  $m \alpha^5(Y(1S) \text{ bbar at LHC})$  N. B. et al. 2010
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The EFT has not yet been constructed (Exotics close to threshold)

- \*Degrees of freedom still to be identified



Weakly coupled pNRQCD  $r \ll \Lambda_{\text{QCD}}^{-1}$



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$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu}^a F^{\mu\nu a} + \text{Tr} \left\{ S^\dagger \left( i\partial_0 - \frac{\mathbf{p}^2}{m} - V_s \right) S \right. \\ \left. + O^\dagger \left( iD_0 - \frac{\mathbf{p}^2}{m} - V_o \right) O \right\}$$

LO in  $r$

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LO in  $r$

$$+ V_A \text{Tr} \left\{ O^\dagger \mathbf{r} \cdot g\mathbf{E} S + S^\dagger \mathbf{r} \cdot g\mathbf{E} O \right\} \\ + \frac{V_B}{2} \text{Tr} \left\{ O^\dagger \mathbf{r} \cdot g\mathbf{E} O + O^\dagger O \mathbf{r} \cdot g\mathbf{E} \right\} \\ + \dots$$

NLO in  $r$



Weakly coupled pNRQCD  $r \ll \Lambda_{\text{QCD}}^{-1}$

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Singlet static potential

LO in  $r$

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NLO in  $r$

# Quarkonium singlet static potential at N<sup>4</sup>LO

$$\begin{aligned} V_s(r, \mu) = & -C_F \frac{\alpha_s(1/r)}{r} \left[ 1 + a_1 \frac{\alpha_s(1/r)}{4\pi} + a_2 \left( \frac{\alpha_s(1/r)}{4\pi} \right)^2 \right. \\ & + \left( \frac{16\pi^2}{3} C_A^3 \ln r\mu + a_3 \right) \left( \frac{\alpha_s(1/r)}{4\pi} \right)^3 \\ & \left. + \left( a_4^{L2} \ln^2 r\mu + \left( a_4^L + \frac{16}{9} \pi^2 C_A^3 \beta_0 (-5 + 6 \ln 2) \right) \ln r\mu + a_4 \right) \left( \frac{\alpha_s(1/r)}{4\pi} \right)^4 \right] \end{aligned}$$



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$a_1$  Billoire 80

$a_2$  Schroeder 99, Peter 97

coeff  $\ln r\mu$  N.B. Pineda, Soto, Vairo 99

$a_4^{L2}, a_4^L$  N.B., Garcia, Soto, Vairo 06

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$a_4^{L2}, a_4^L$  N.B., Garcia, Soto, [Vainsen 00](#) **4LOOPS REDUCES TO 2LOOPS IN THE EFT**

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Two problems:

- 1) Bad convergence of the series due to large beta<sub>0</sub> terms
- 2) Large logs



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The eft cures both:

- 1) Renormalon subtracted scheme

BENEKE 98, HOANG, LEE 99, PINEDA 01,  
N. BRAMBILLA ET AL 09

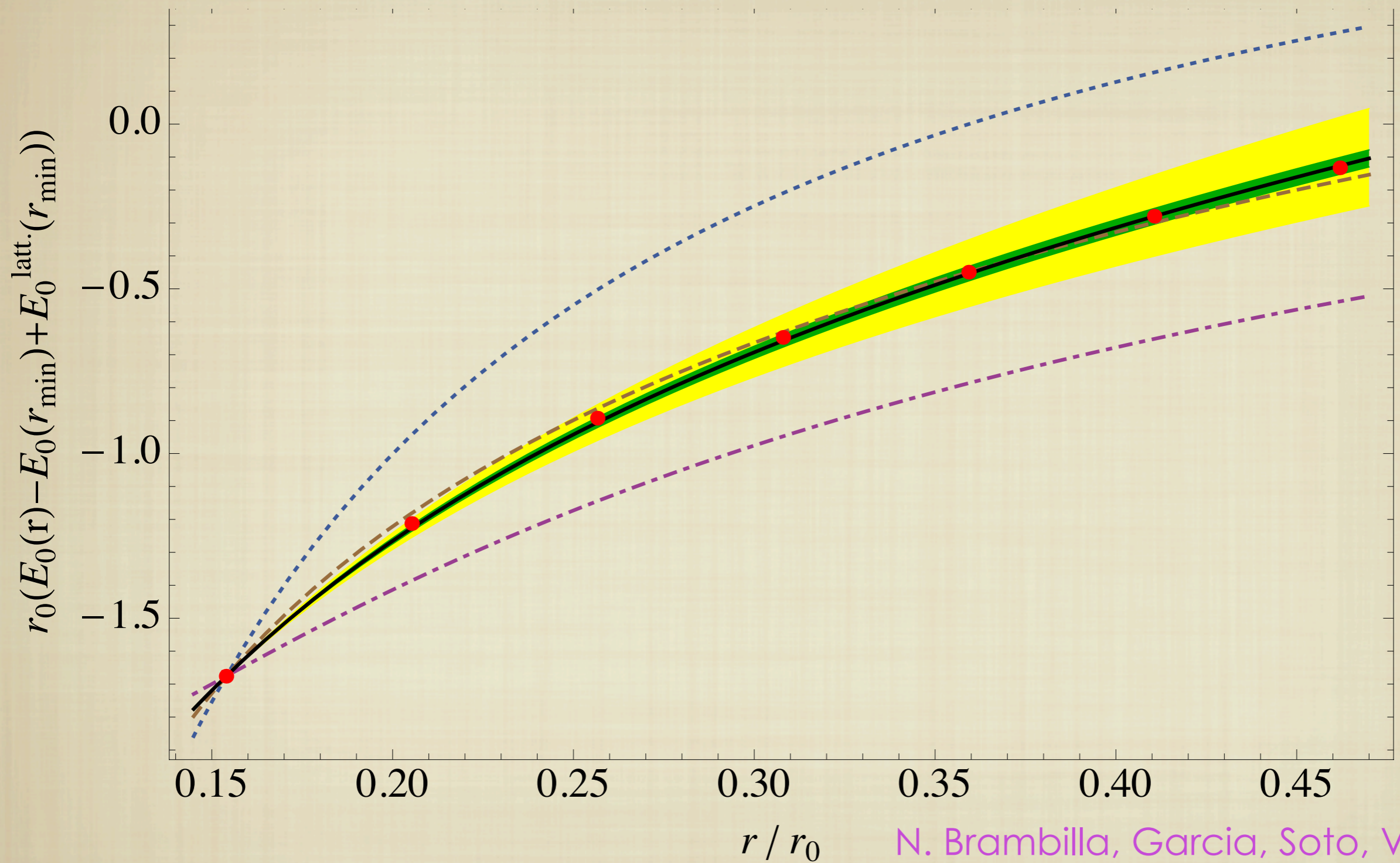
- 2) Renormalization group summation of the logs

up to N<sup>3</sup>LL  $(\alpha_s^{4+n} \ln^n \alpha_s)$  N. BRAMBILLA. ET AL 2007, 2009

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# Quarkonium singlet static energy at $N^3LL$ in comparison with lattice data (red points) NECCO SOMMER 2002



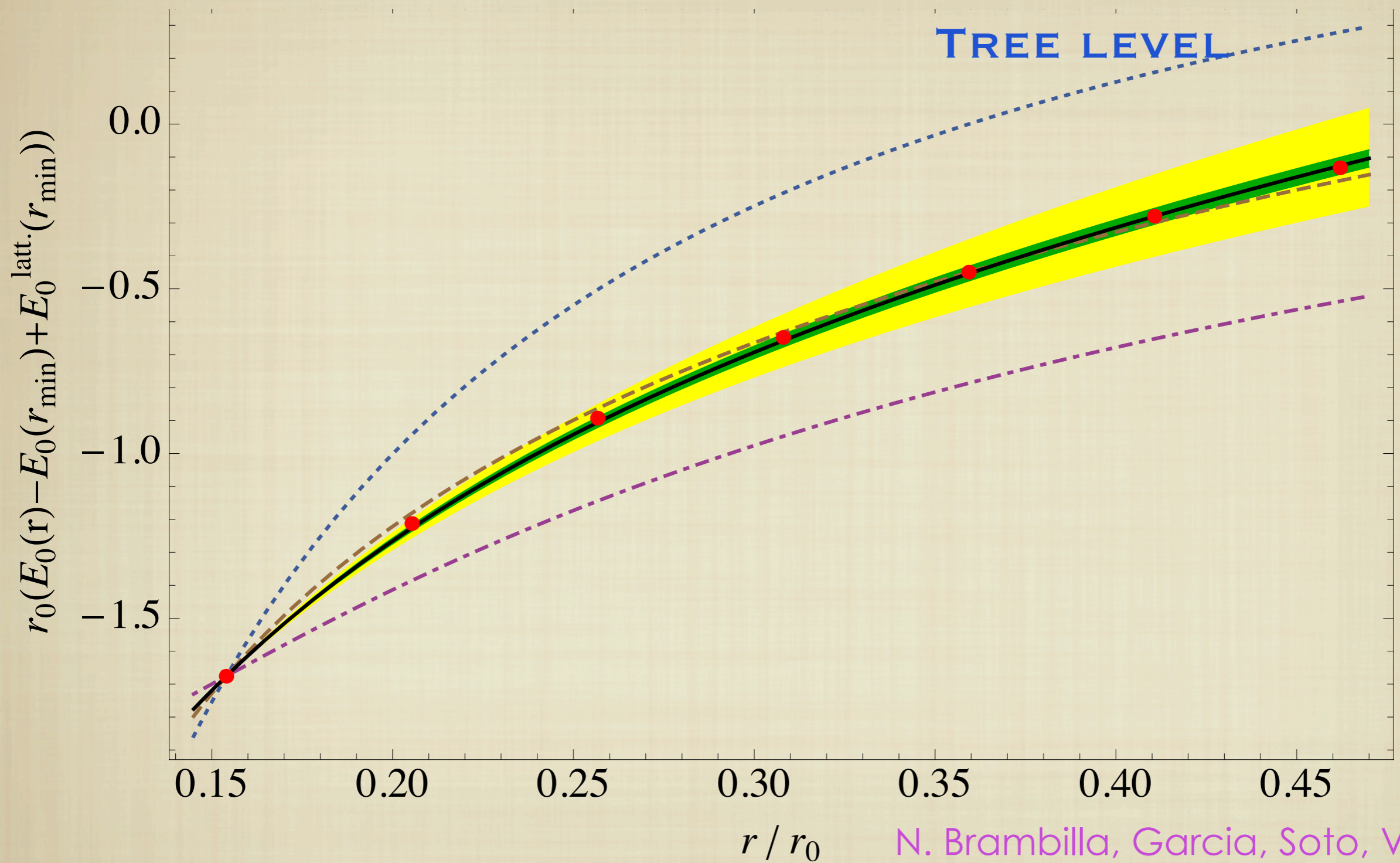
N. Brambilla, Garcia, Soto, Vairo 010

Yellow band : uncertainty in  $\alpha_s$  ( $r_0 \cdot \Lambda_{\text{QCD}}(\overline{\text{MS}})$ )

Green band: uncertainty in higher order terms



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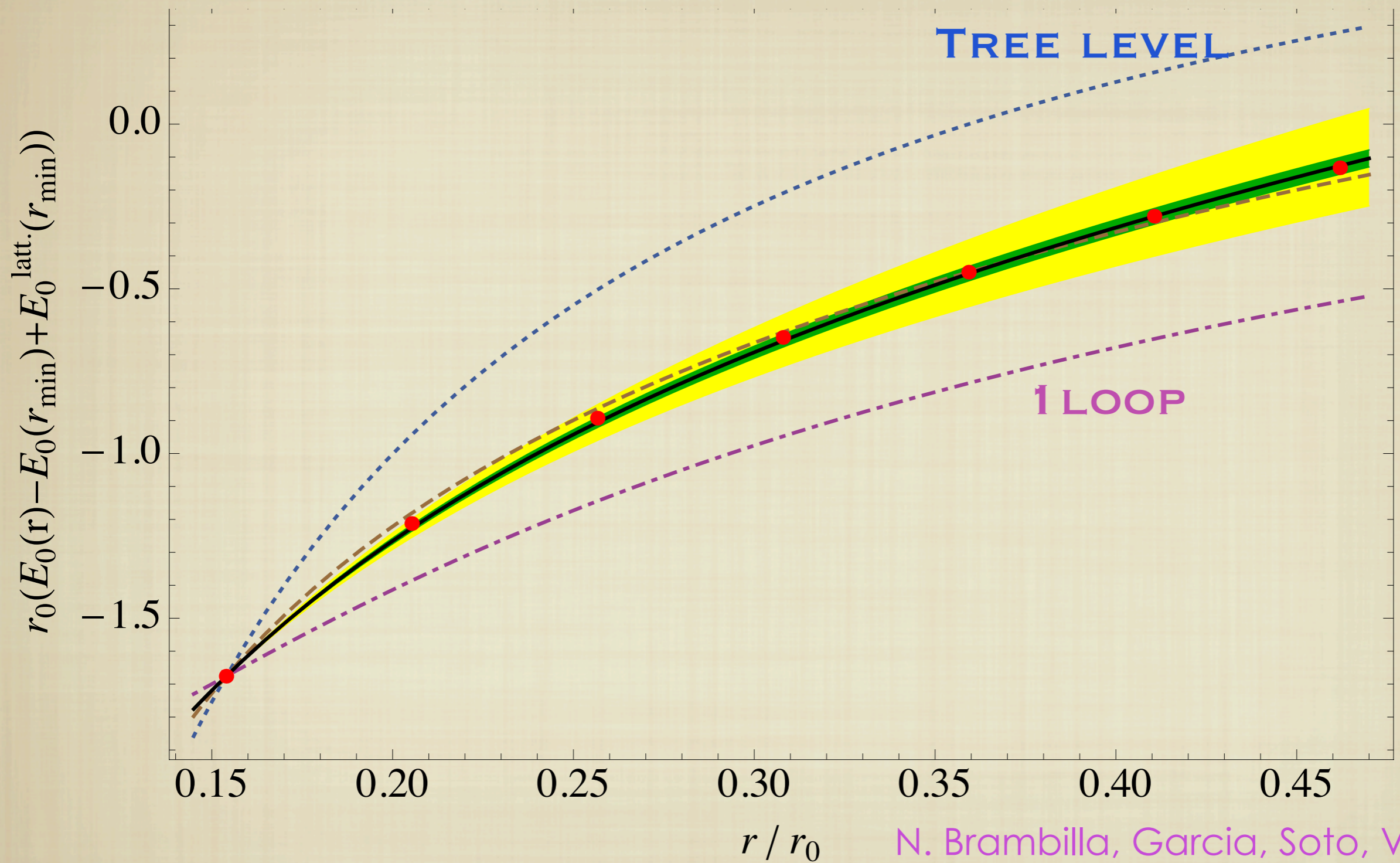
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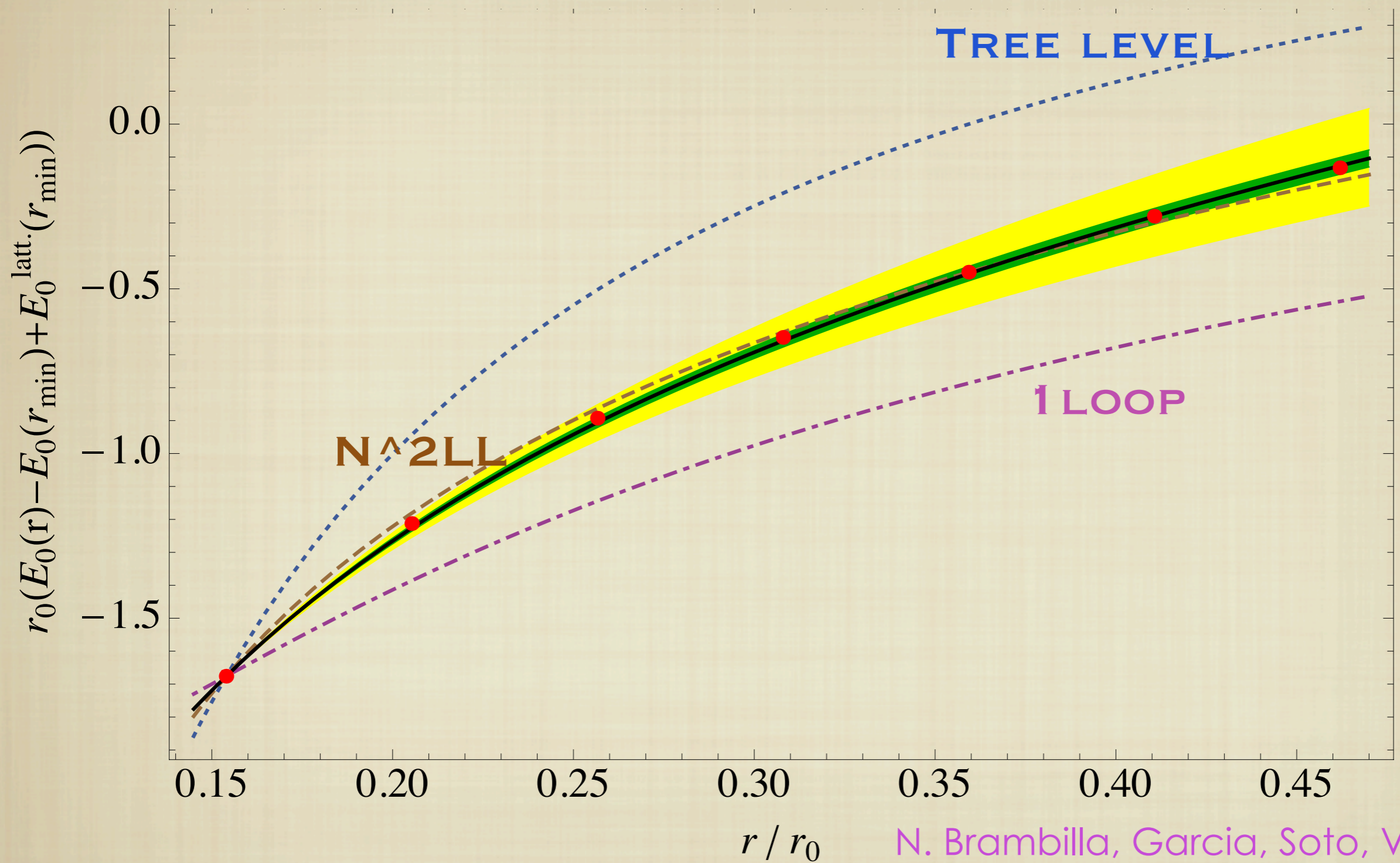
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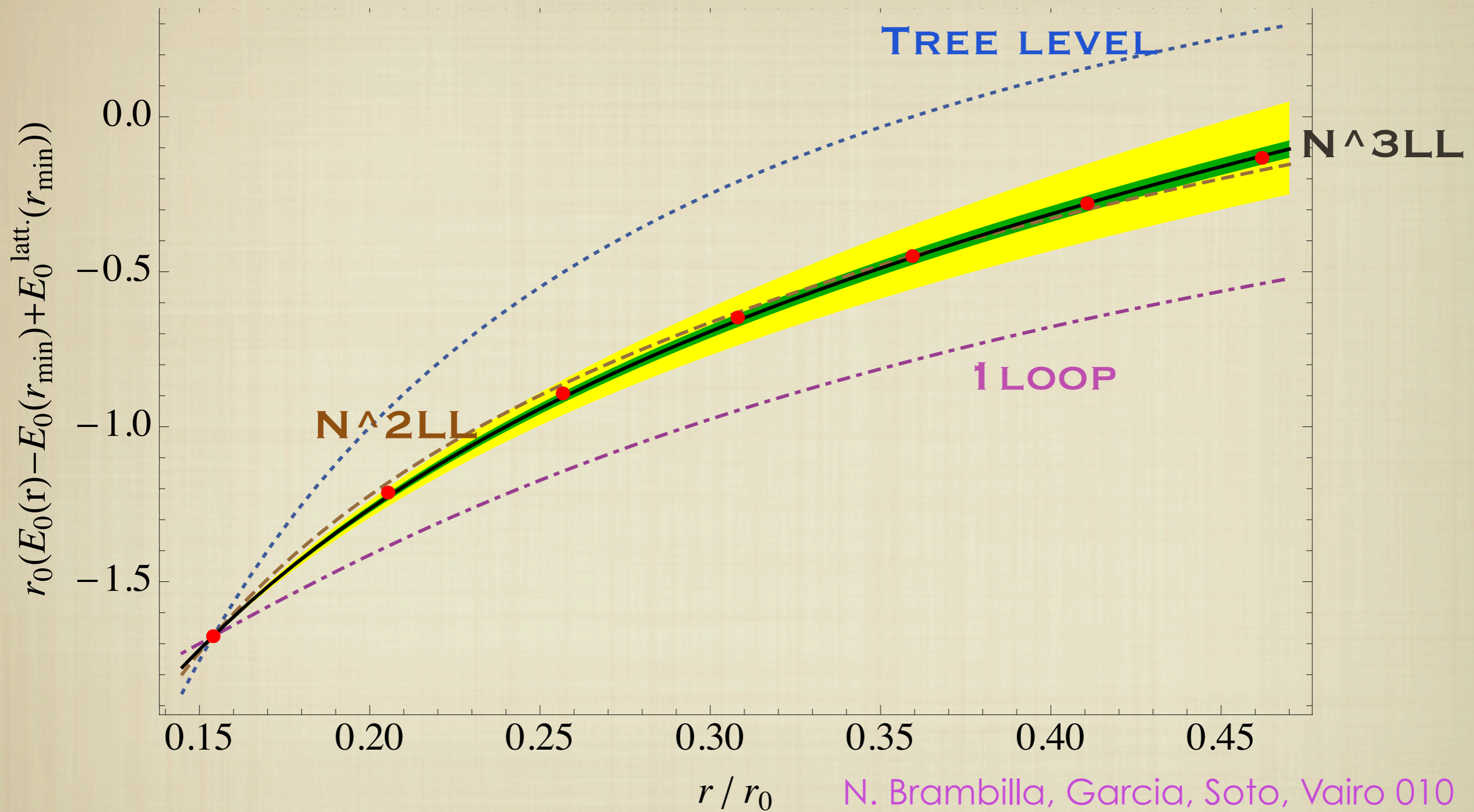
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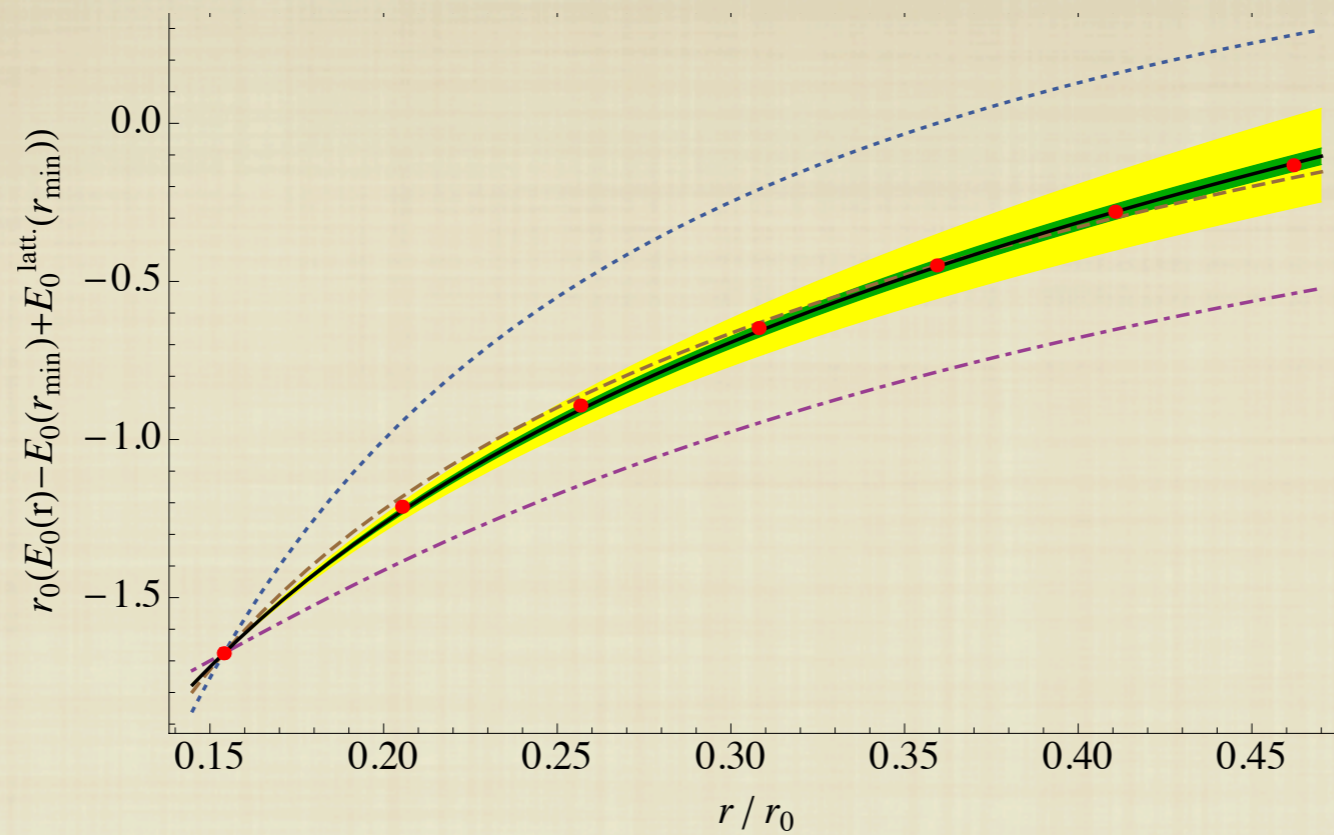
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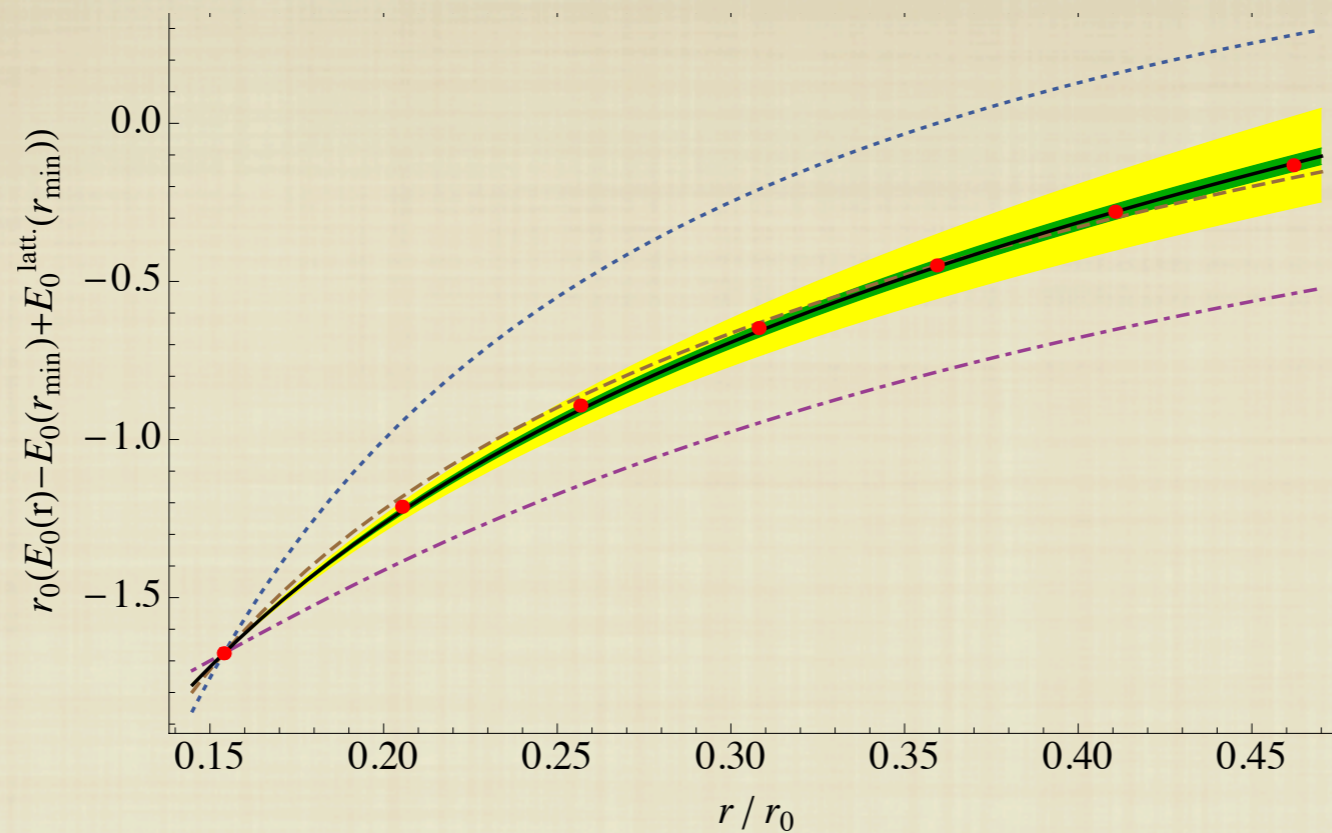


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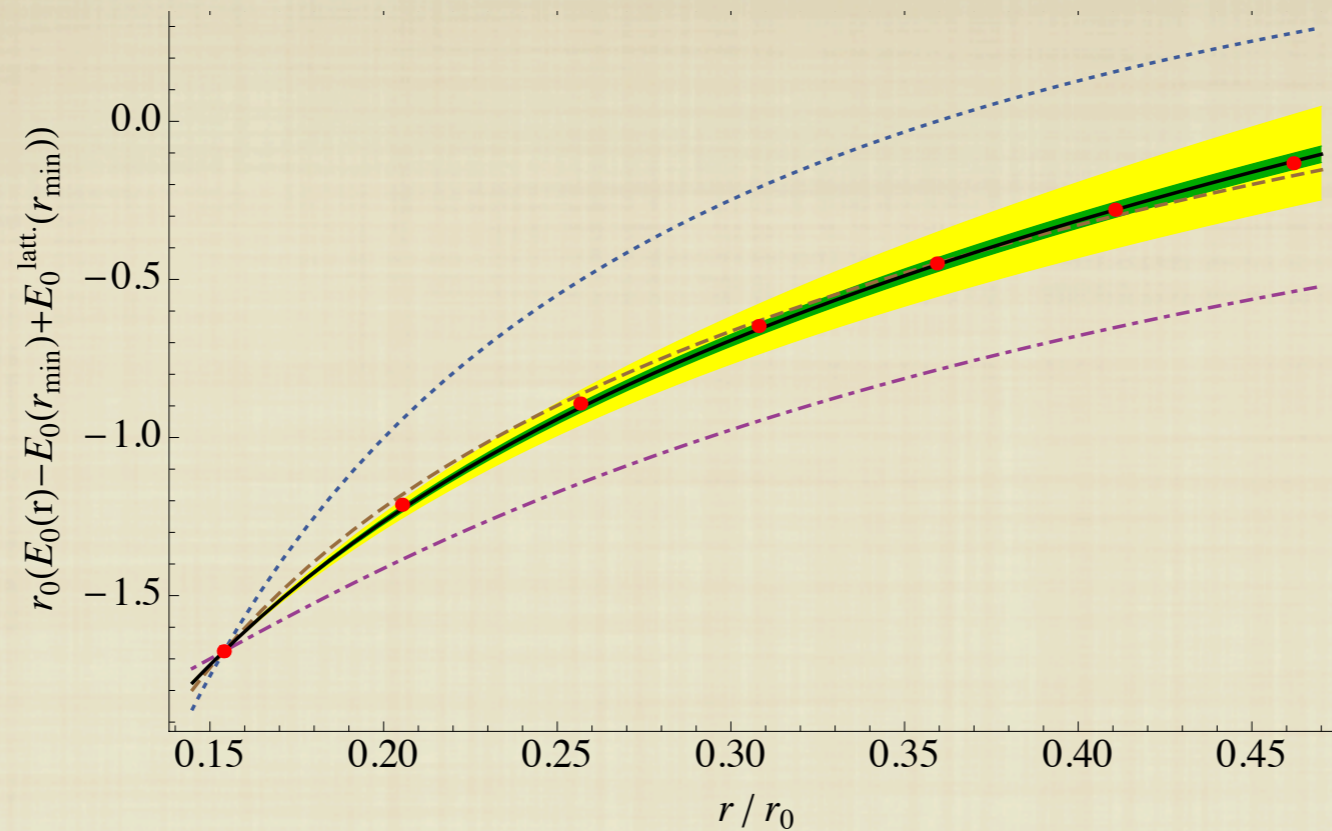
# Quarkonium singlet static energy at $N^3LL$ in comparison with lattice data (red points) NECCO SOMMER 2002



- Very good convergence of the QCD bound state perturbative series



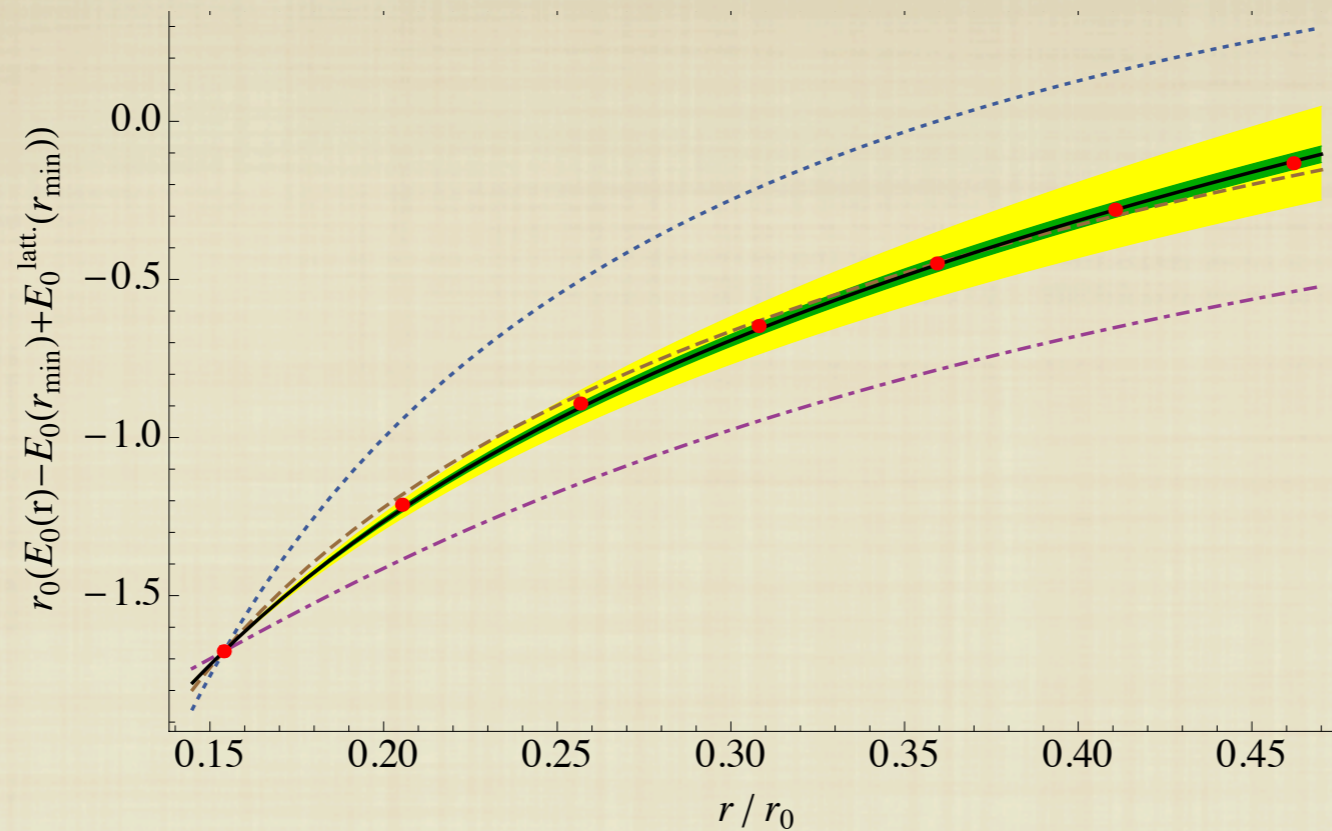
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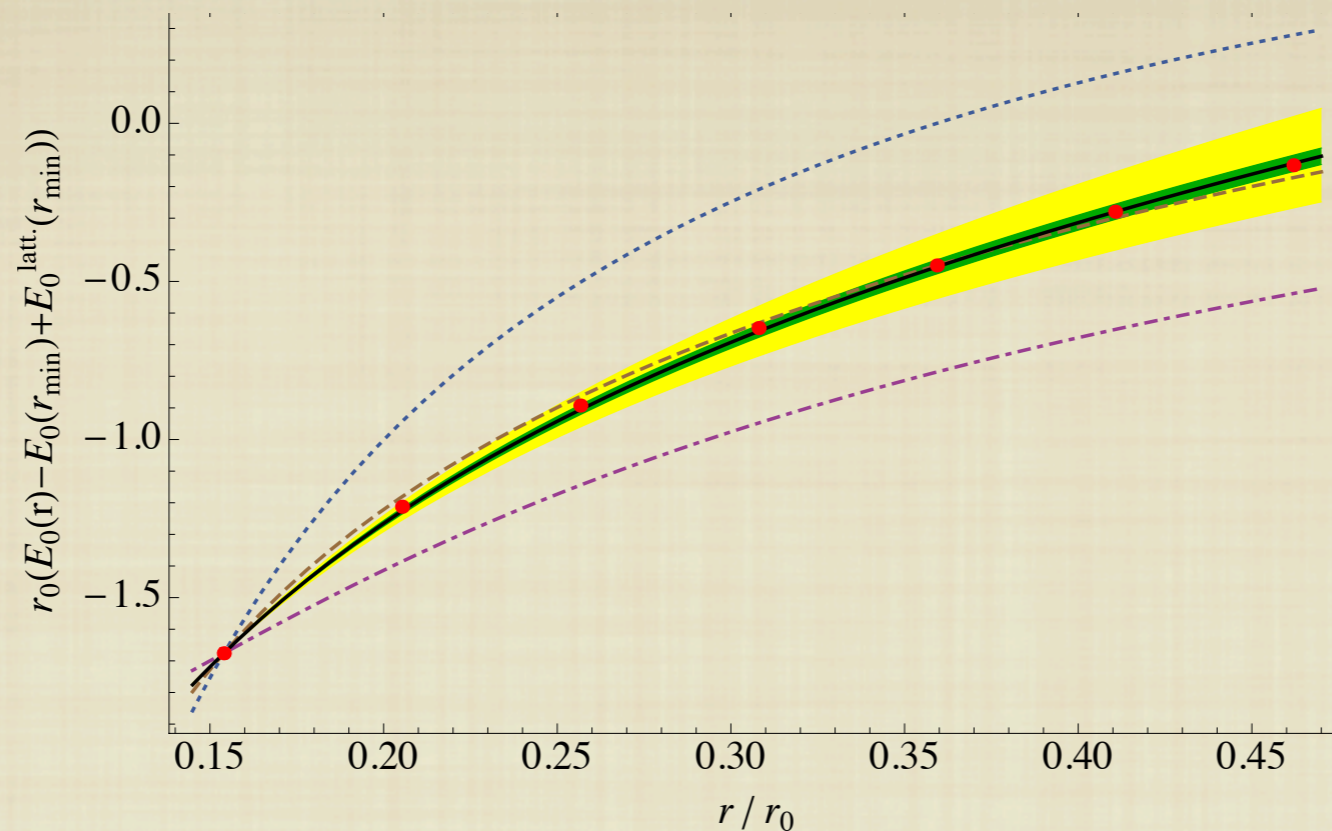
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- The lattice data are perfectly described from perturbation theory up to more than 0.2 fm
- Allows to rule out models: no string contribution at small  $r$  !
- Allows precise extraction of fundamental parameters of QCD

$$r_0 \Lambda_{\bar{M}S} = 0.622^{+0.019}_{-0.015}$$

(N. Brambilla, Garcia, Soto, Vairo 010)



several high order calculations of matching coefficients, spectra, decay  
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e.g. QQQ static singlet potential at N<sup>2</sup>LO

BRAMBILLA GHIGLIERI VAIR  
2010

$$\begin{aligned}
 V_s(\mathbf{r}) = & -\frac{2}{3} \sum_{q=1}^3 \frac{\alpha_s(1/|\mathbf{r}_q|)}{|\mathbf{r}_q|} \left\{ 1 + \frac{\alpha_s(1/|\mathbf{r}_q|)}{4\pi} \left[ \frac{31}{3} + 22\gamma_E - \left( \frac{10}{9} + \frac{4}{3}\gamma_E \right) n_f \right] \right. \\
 & + \left( \frac{\alpha_s(1/|\mathbf{r}_q|)}{4\pi} \right)^2 \left[ +66\zeta(3) + 484\gamma_E^2 + \frac{1976}{3}\gamma_E + \frac{3}{4}\pi^4 + \frac{121}{3}\pi^2 + \frac{4343}{18} \right. \\
 & - \left( \frac{52}{3}\zeta(3) + \frac{176}{3}\gamma_E^2 + \frac{916}{9}\gamma_E + \frac{44}{9}\pi^2 + \frac{1229}{27} \right) n_f \\
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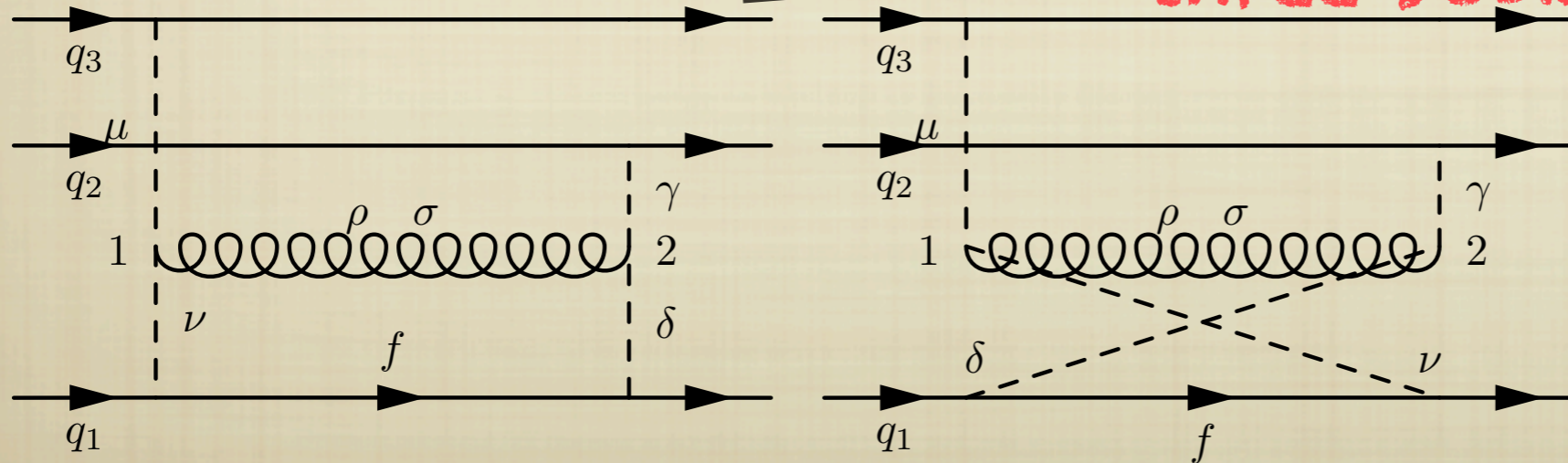
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 \end{aligned}$$

three bodies contributions





# Applications to Quarkonium physics

for references see the QWG doc



# Applications to Quarkonium physics

- $c$  and  $b$  masses at NNLO,  $N^3\text{LO}^*$ , NNLL\*;
- $B_c$  mass at NNLO;
- $B_c^*$ ,  $\eta_c$ ,  $\eta_b$  masses at NLL;
- Quarkonium  $1P$  fine splittings at NLO;
- $\Upsilon(1S)$ ,  $\eta_b$  electromagnetic decays at NNLL;
- $\Upsilon(1S)$  and  $J/\psi$  radiative decays at NLO;
- $\Upsilon(1S) \rightarrow \gamma\eta_b$ ,  $J/\psi \rightarrow \gamma\eta_c$  at NNLO;
- $t\bar{t}$  cross section at NNLL\*;

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N. B. Yu Jia A. Vairo 2005



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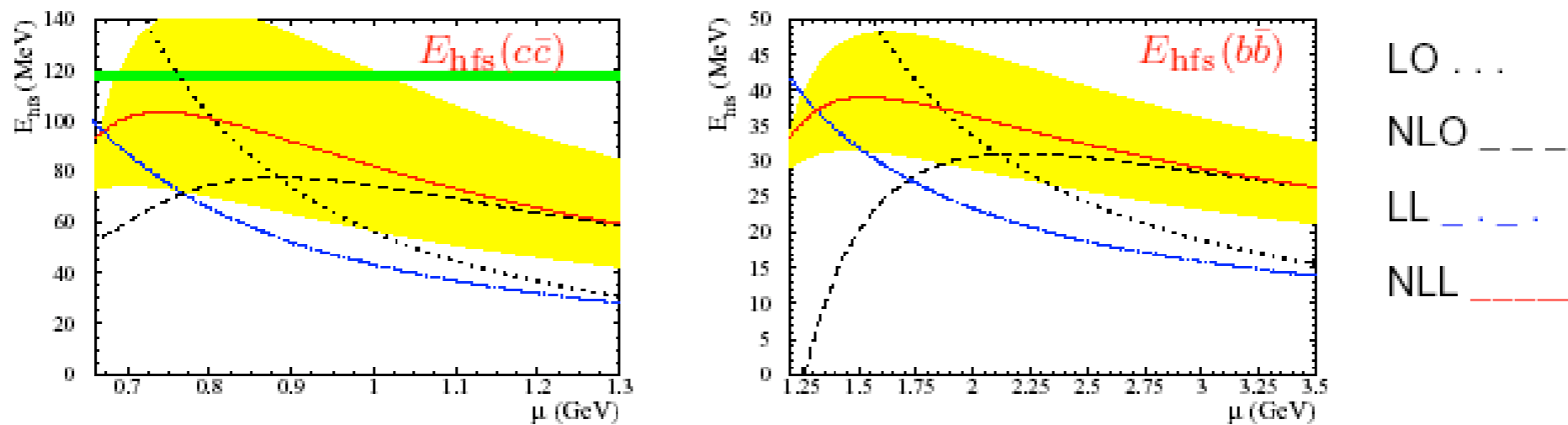
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$$\Gamma(\eta_b(1S) \rightarrow \gamma\gamma) = 0.54 \pm 0.15 \text{ keV}.$$

Y. Kiyo, A. Pineda, A. Signer 2010

$$\Gamma(\eta_b(1S) \rightarrow \text{LH}) = 7\text{-}16 \text{ MeV}$$

# Predictions for $\eta_b$



$$M_{\eta_b} = 9419 \pm 11 (th)_8^{+9} (\delta\alpha_s) \text{ MeV}$$

Kniefel et al 03

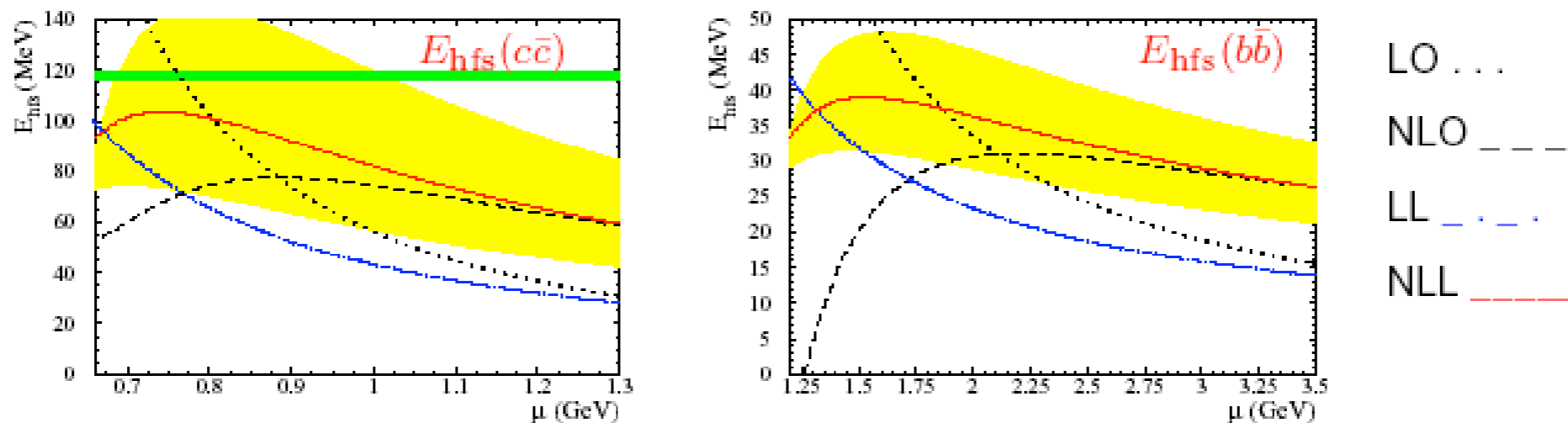
BABAR 08, 09

$$M_{\eta_b} = 9390, 9 \pm 3.1 \text{ MeV}$$

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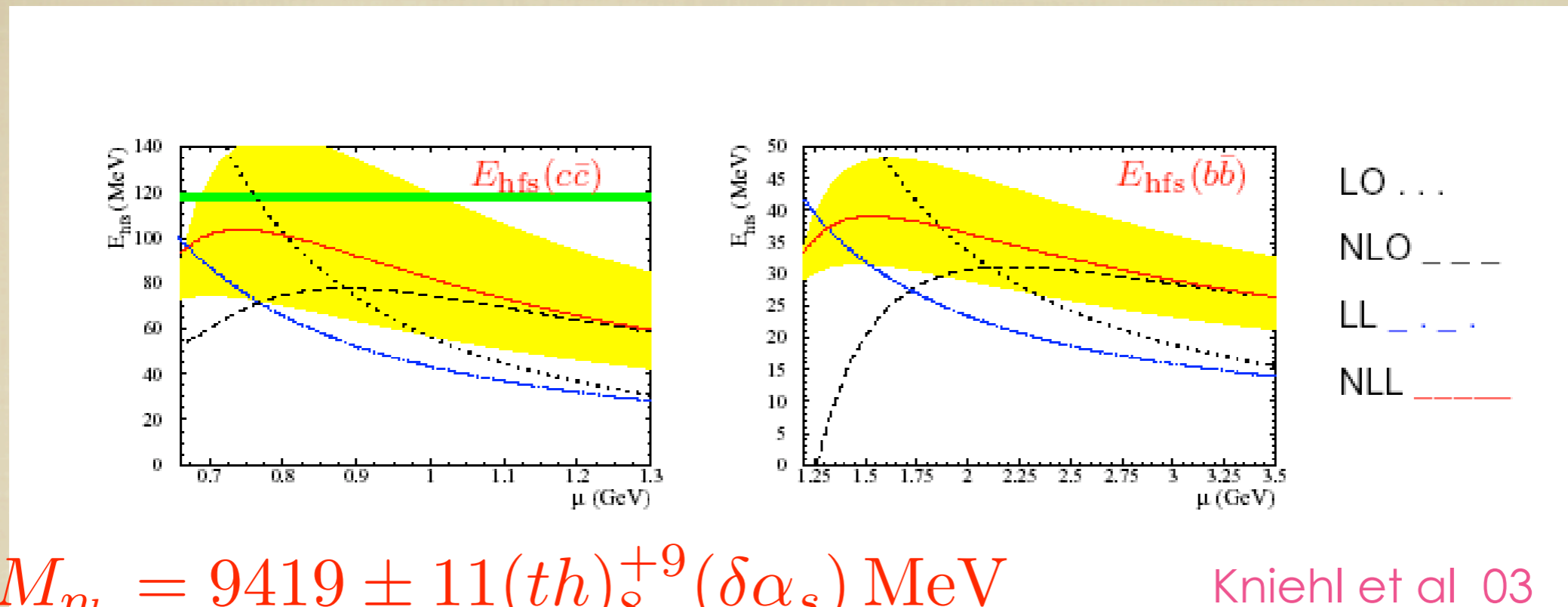
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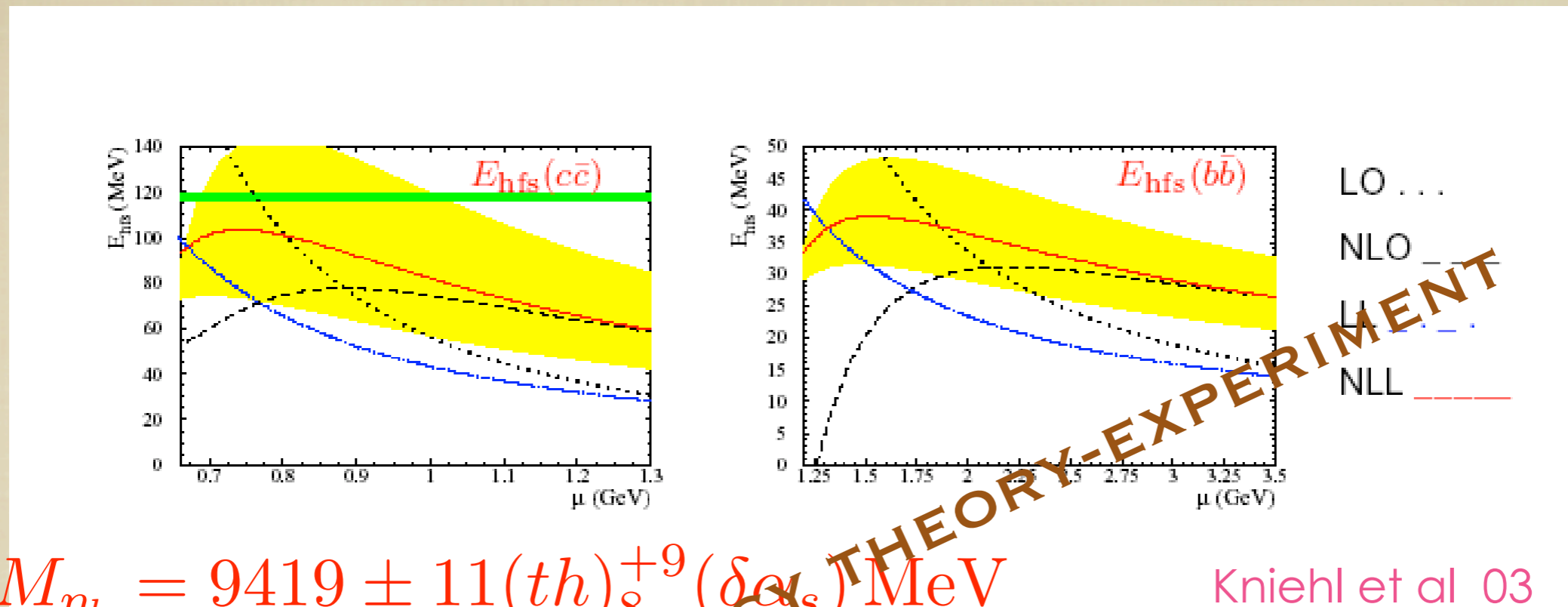
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Calculate once for ever the potential and get the full charmonium spectroscopy





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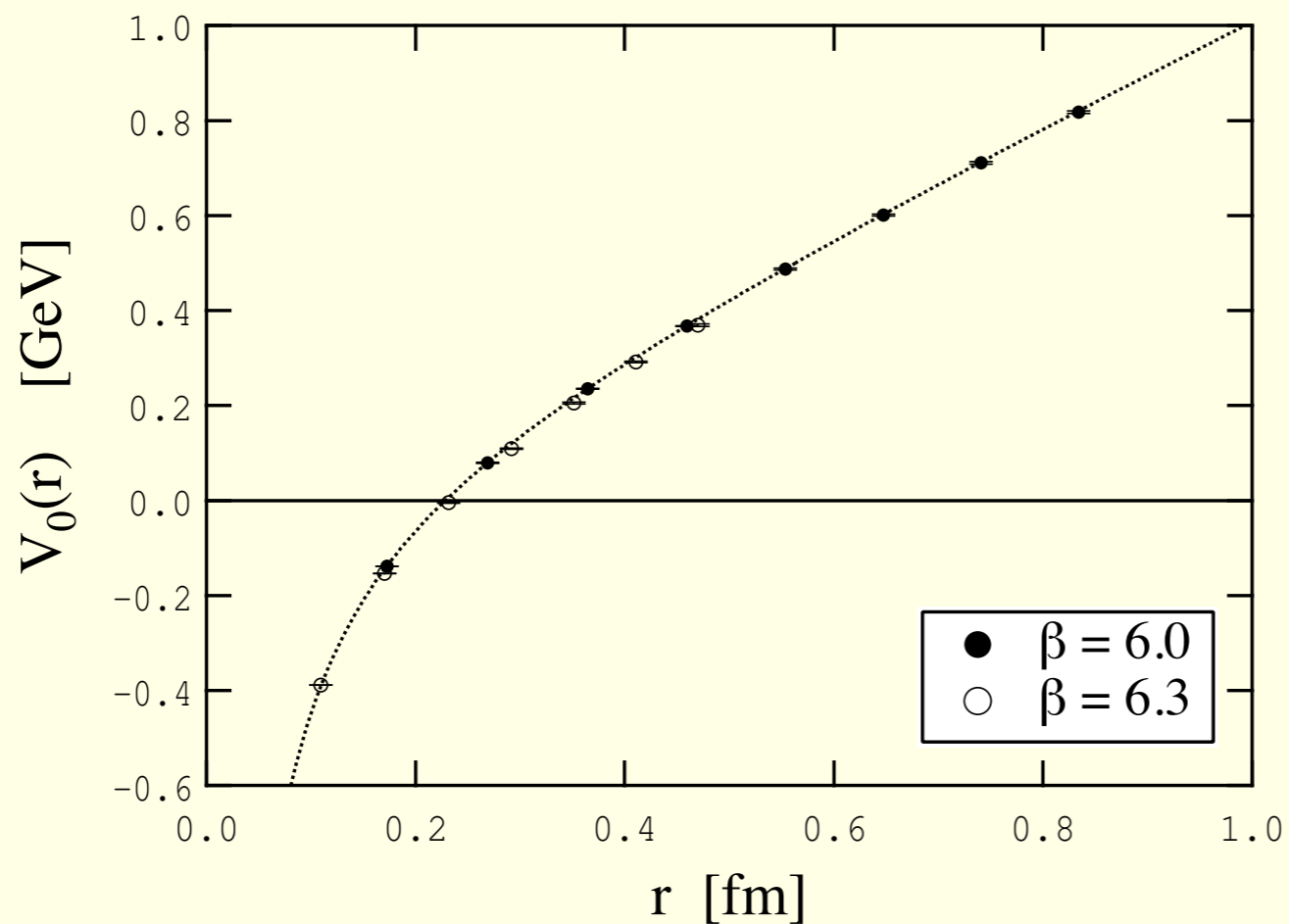
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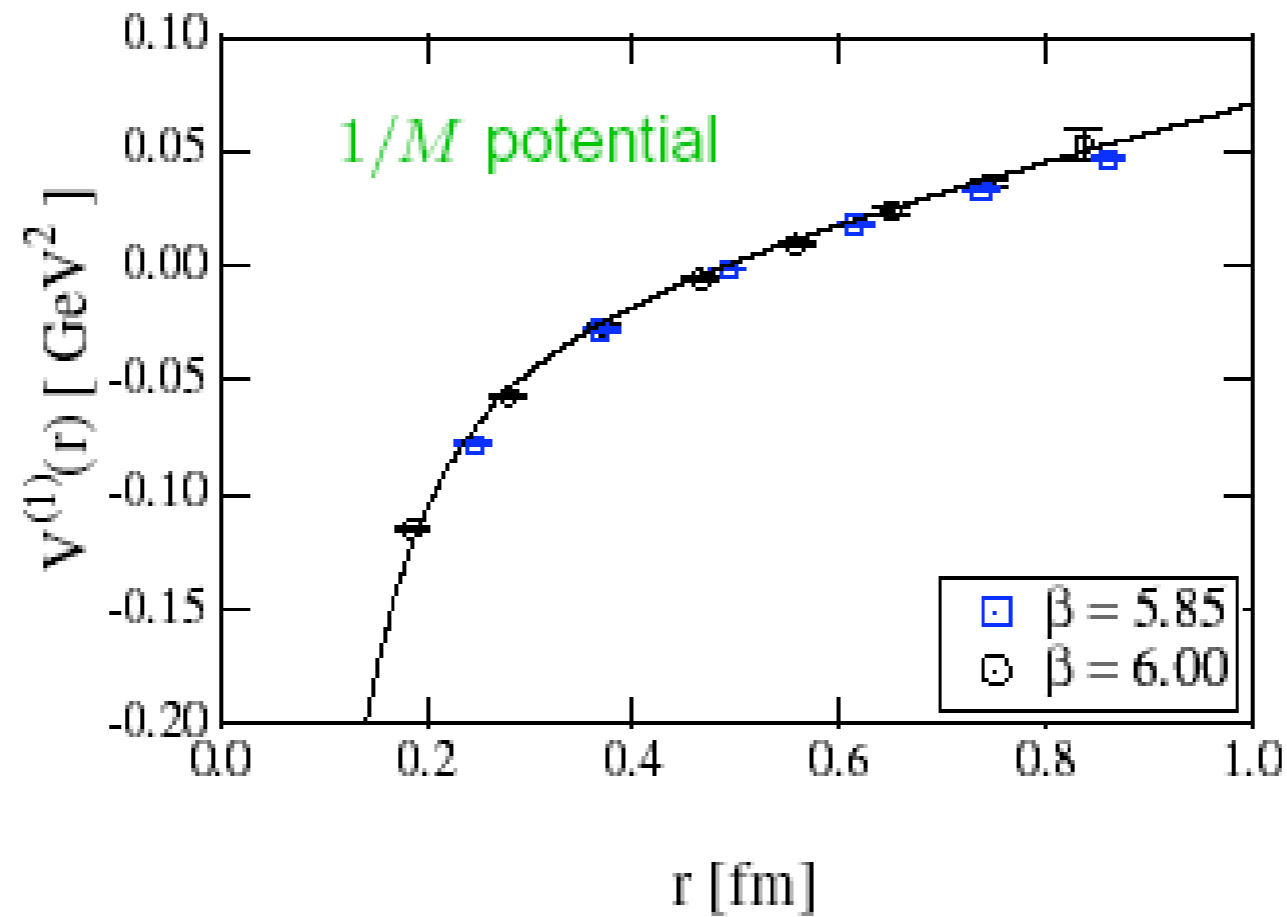


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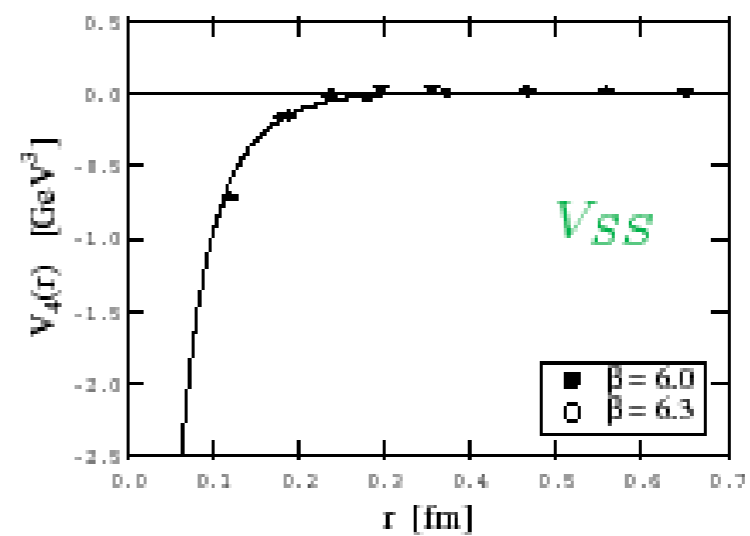
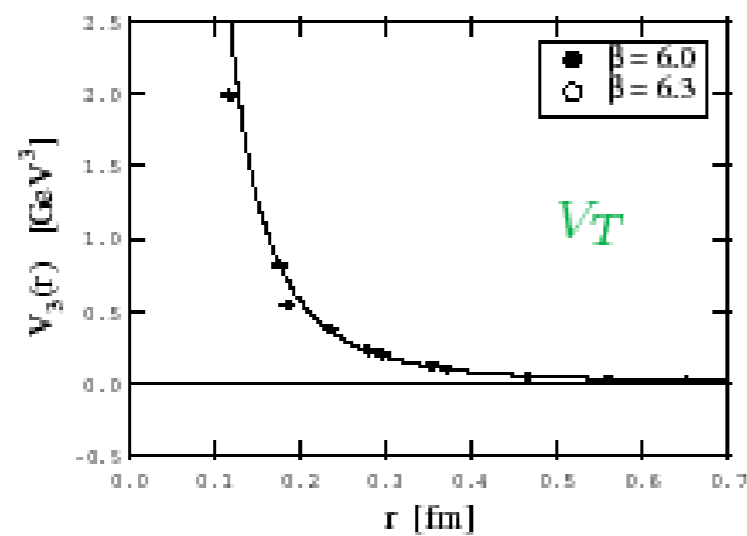
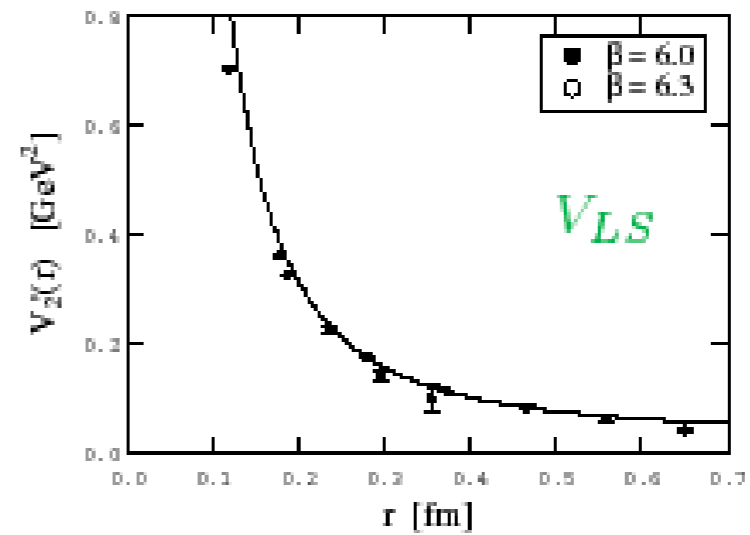
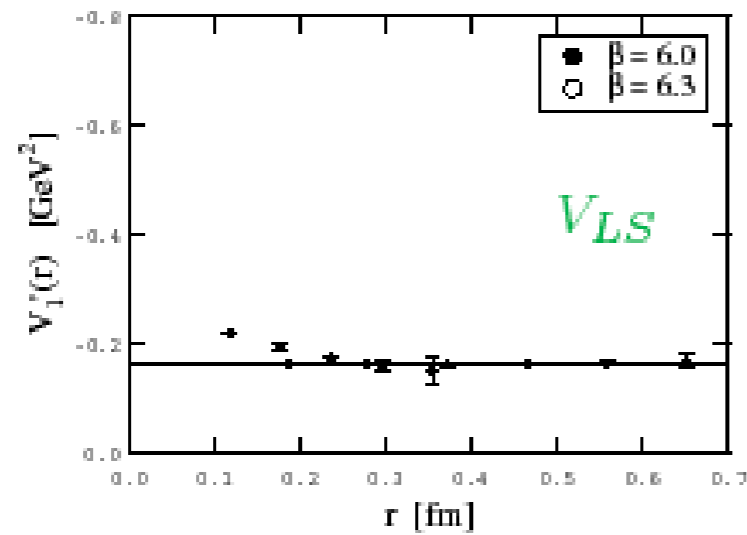
○ Koma Koma Wittig PoS LAT2007(07)111

$$\frac{V_s^{(1)}}{m} = -\frac{1}{2m} \int_0^\infty dt t \left( \begin{array}{c} \text{E} \\ \bullet \quad \bullet \\ \square \end{array} \right)$$

Brambilla et al 00



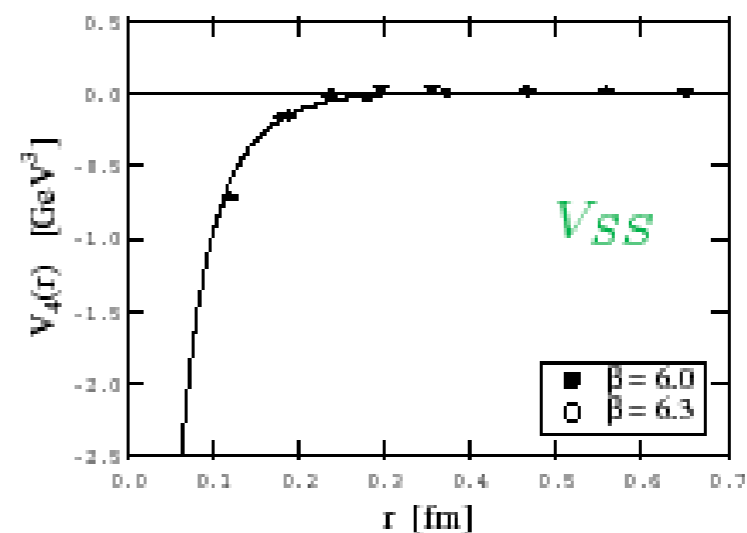
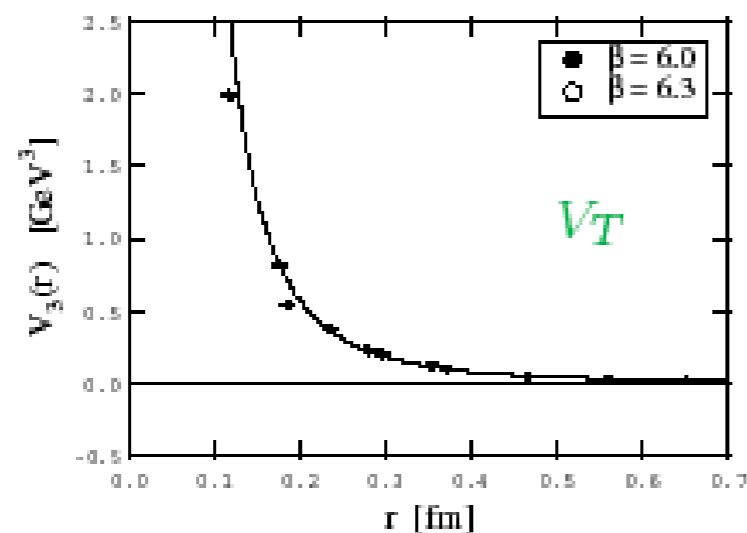
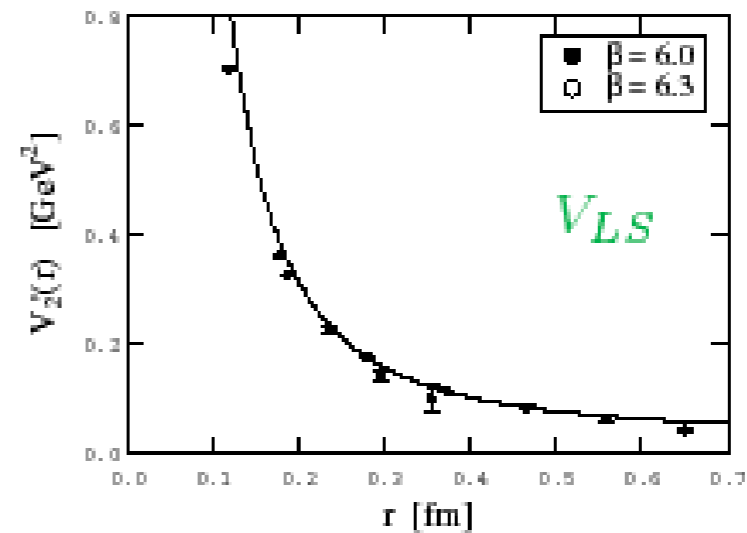
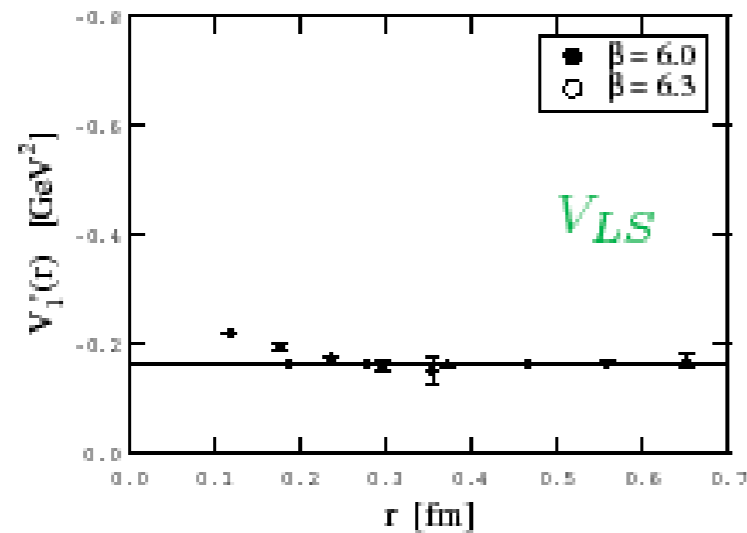
# Spin dependent potentials



Koma Koma Wittig 05, Koma Koma 06

Terrific advance in the data precision with Lüscher multivel algorithm!

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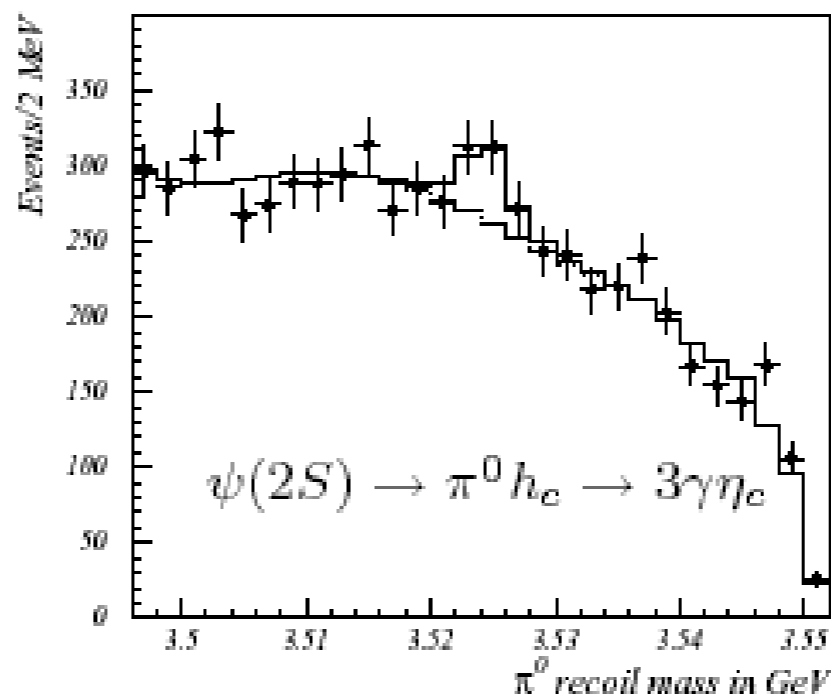
Terrific advance in the data precision with Lüscher multivel algorithm!

Such data can distinguish different models for the dynamics of low energy QCD



# Confirmed in the spectrum, e.g. no long range spin-spin interaction

$h_c$



$$M = 3524.4 \pm 0.6 \pm 0.4 \text{ MeV}$$

CLEO 05

Also

$$M = 3525.8 \pm 0.2 \pm 0.2 \text{ MeV}, \quad \Gamma < 1 \text{ MeV}$$

E835 05

- To be compared with  $M_{c.o.g.}(1P) = 3525.36 \pm 0.2 \pm 0.2 \text{ MeV}$ .

no  $\Lambda_{QCD}$  gap: close and above threshold



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## Gluonic excitations

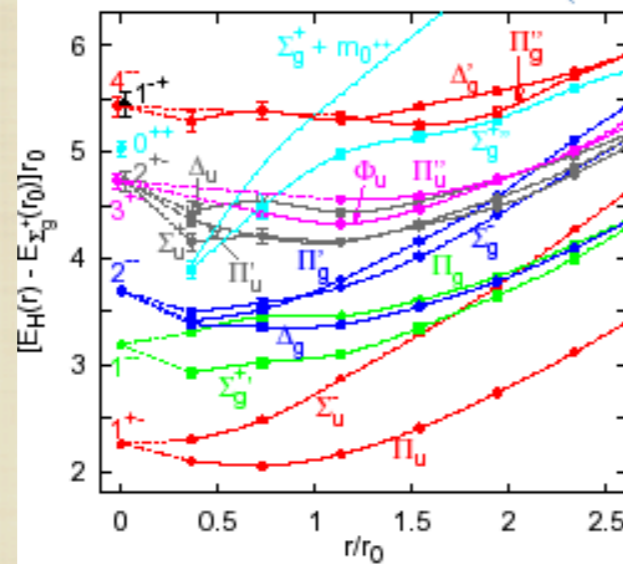
A plethora of states built on each of the hybrid potentials is expected. These states typically develop a width also without including light quarks, since they may decay into lower states, e.g. like **hybrid**  $\rightarrow$  **glueball** + **quark-antiquark**.

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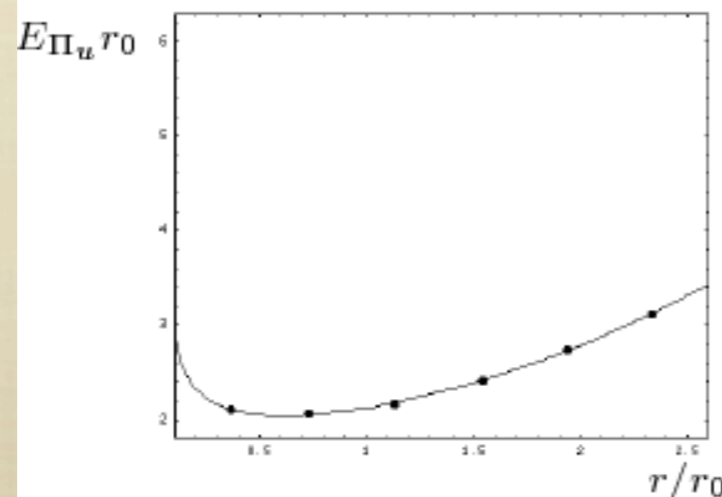
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### $Y(4260)$ : a $c\bar{c}$ hybrid candidate



$J^{PC}$	$H$	$\Lambda_H^{RS} r_0$	$\Lambda_H^{RS}/\text{GeV}$
$1^{+-}$	$B_i$	2.25(39)	0.87(15)
$1^{--}$	$E_i$	3.18(41)	1.25(16)
$2^{--}$	$D_{\{i}B_{j\}}$	3.69(42)	1.45(17)
$2^{+-}$	$D_{\{i}E_{j\}}$	4.72(48)	1.86(19)
$3^{+-}$	$D_{\{i}D_{j}B_{k\}}$	4.72(45)	1.86(18)
$0^{++}$	$B^2$	5.02(46)	1.98(18)
$4^{--}$	$D_{\{i}D_{j}D_{k}B_{l\}}$	5.41(46)	2.13(18)
$1^{-+}$	$(B \wedge E)_i$	5.45(51)	2.15(20)

- Foster Michael PRD 59(99)094509
- Bali Pineda PRD 69(04)094001



Fitting the  $\Pi_u$  curve,  $E_{\Pi_u} = (0.87 + 0.11/r + 0.24 r^2)$  GeV and solving the Schrödinger equation, one gets

$$M(Y) = 2 \times 1.48 + 0.87 + 0.53 = 4.36 \text{ GeV}$$

- Vairo IJMP A22(07)5481



## The QCD spectrum with light quarks

- We still have states just made of heavy quarks and gluons. They may develop a width because of the decay through pion emission. If new states made with heavy and light quarks develop a mass gap of order  $\Lambda_{\text{QCD}}$  with respect to the former ones, then these new states may be absorbed into the definition of the potentials or of the (local or non-local) condensates.
  - Brambilla et al. PRD 67(03)034018
- In addition new states built using the light quark quantum numbers may form.
  - Soto NP PS 185(08)107

## States made of two heavy and light quarks

- Pairs of heavy-light mesons:  $D\bar{D}, B\bar{B}, \dots$

- Molecular states, i.e. states built on the pair of heavy-light mesons.
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- Tetraquark states.

**MAIANI, PICCININI, POLOSA ET AL. 2005--**

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Having the spectrum of tetraquark potentials, like we have for the gluonic excitations, would allow us to build a plethora of states on each of the tetraquark potentials, many of them developing a width due to decays through pion (or other light hadrons) emission. Diquarks have been recently investigated on the lattice.

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## Coupled channels

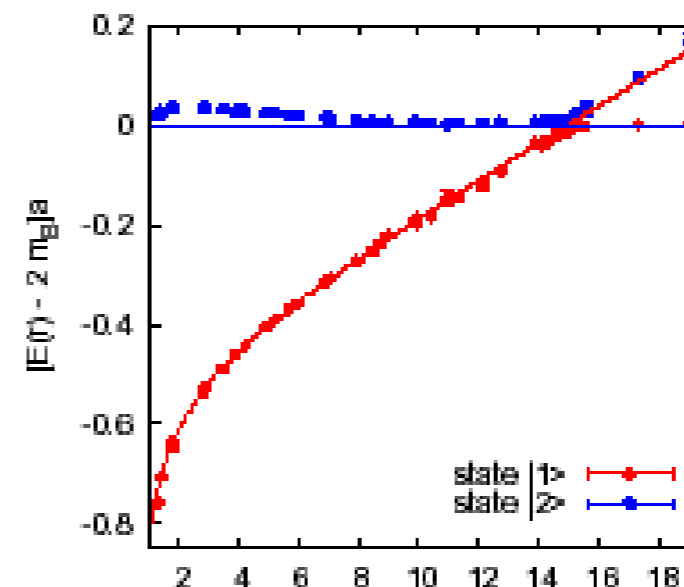
An important (and unsolved) issue is how all the different kind of states (with and without light quarks) interact with each other.

A systematic treatment does not exist so far. For the coupling with two-meson states, most of the existing analyses rely on two models, which are now more than 30 years old:

- the Cornell coupled-channel model;
  - Eichten et al. PRD 17(78)3090, 21(80)313
  - Eichten et al. PRD 69(04)094019, 73(06)014014, 73(06)079903
- and the  $^3P_0$  model.
  - Le Yaouanc et al. PRD 8(73)2223
  - Kalashnikova PRD 72(05)034010

Steps towards a lattice based approach have been undertaken

- SESAM PRD 71(05)114513



States near or above threshold: "exotics" !  
hybrids, molecular states, tetraquarks

Many new states from  
experiments: Xs, Ys, Zs



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In some cases it is possible to develop an EFT  
owing to special dynamical condition

- An example is the  $X(3872)$  interpreted as a  $D^0 \bar{D}^{*0}$  or  $\bar{D}^0 D^{*0}$  molecule. In this case, one may take advantage of the hierarchy of scales:

$$\Lambda_{\text{QCD}} \gg m_\pi \gg m_\pi^2/M_{D^0} \approx 10 \text{ MeV} \gg E_{\text{binding}} \\ \approx M_X - (M_{D^{*0}} + M_{D^0}) = (0.1 \pm 1.0) \text{ MeV}$$

*Systems with a short-range interaction and a large scattering length have universal properties that may be exploited: in particular, production and decay amplitudes factorize in a short-range and a long-range part, where the latter depends only on one single parameter, the scattering length*

Braaten Hammer 06

Pakvasa Suzuki 03, Voloshin 03, Braaten Kusunoki 03



## Conclusions

Effective field theories gives us invaluable tools to investigate strong interactions

Nonrelativistic Effective Field Theories provide a systematic tool to investigate a wide range of heavy quarkonium observables in the realm of QCD

Allow us to make calculations with unprecedented precision, where high order perturbative calculations are possible and to systematically factorize short from long range contributions where observables are sensitive to the nonperturbative dynamics of QCD

They allow us to give the appropriate definition and define a calculational scheme for quantities of huge phenomenological interest like the  $q\bar{q}$  interaction, spectra, decays ... and the  $q\bar{q}$  potential at finite  $T$

in the EFT framework heavy quark bound states become a unique laboratory for the study of strong interaction from the high energy to the low energy scales



Outlook1: future research



## Outlook1: future research

Finite T : masses, width of quarkonia states, impact of anisotropy of the medium, transport coefficients of heavy quarks, viscosity



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ALICE, RHIC

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**CMS, ATLAS**