

# $CP$ violation

(charm sector and  $\gamma$  measurements)

Denis Derkach

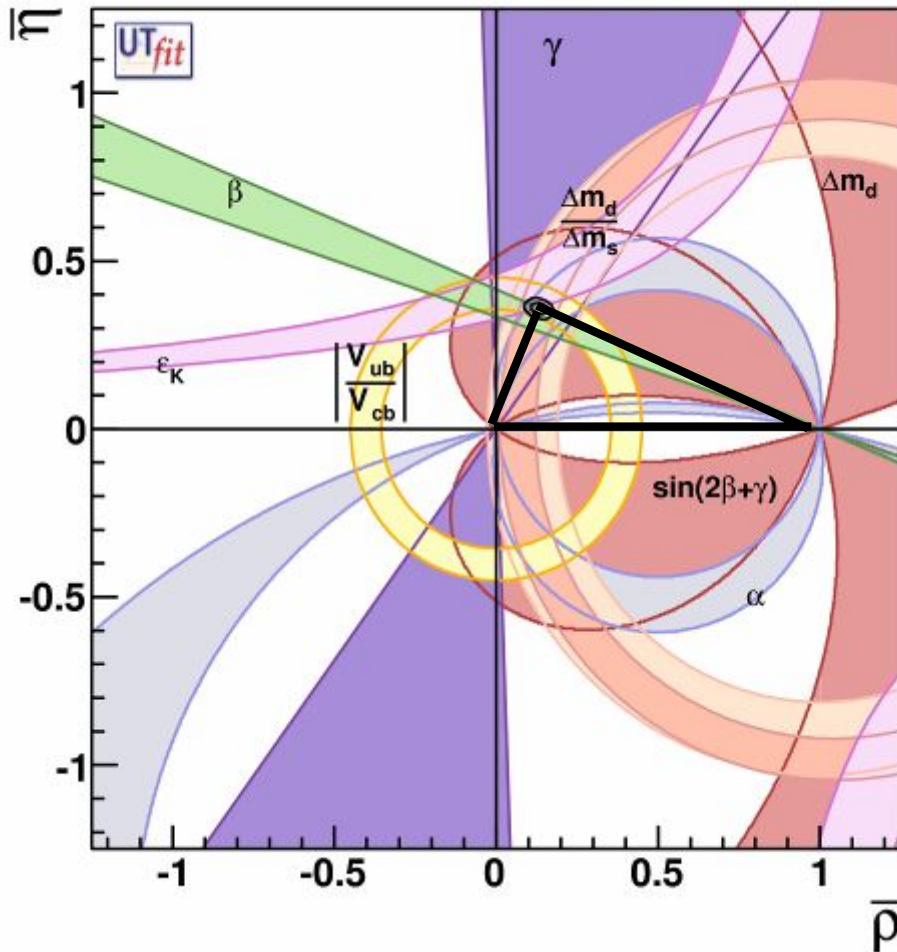
Laboratoire de l'Accélérateur Linéaire – ORSAY  
CNRS/IN2P3



Heavy Quarks and Leptons  
Frascati, 13<sup>th</sup> October, 2010



# Motivation and outline



CP violation studies showed good agreement with the SM by now

In this talk:

$D^0$  mesons mixing

CP violation in charm

$\gamma$  measurements

See next talk by Yosuke Yusa for more CP violation results

Experiments providing most of analyses today



3.1 GeV  $e^+$   
9 GeV  $e^-$   
468M BB pairs

3.5 GeV  $e^+$   
8 GeV  $e^-$   
772M BB pairs

See talk by Luca Silvestrini for more phenomenological details

# D<sup>0</sup> mixing

Flavor eigenstate	Mass eigenstate
$ D^0(\bar{c}u)\rangle$	$ D^0(M_1, \Gamma_1)\rangle$
$ \bar{D}^0(c\bar{u})\rangle$	$ D^0(M_2, \Gamma_2)\rangle$

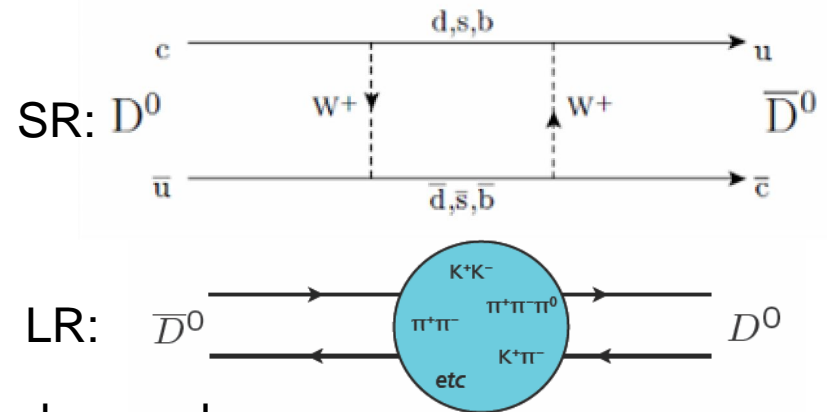
$$|D_1\rangle = p|D^0\rangle + q|\bar{D}^0\rangle$$

$$|D_2\rangle = p|D^0\rangle - q|\bar{D}^0\rangle \quad \text{If } p \neq q, \text{ CP violation is observed.}$$

For the studies several mixing observables are used:

$$x = \frac{M_1 - M_2}{\Gamma} \quad y = \frac{\Gamma_1 - \Gamma_2}{2\Gamma}$$

In the Standard model  
 Mixing parameters  $\sim 10^{-2}$   
 CP violation  $\sim 10^{-3}$



First observed by BaBar and Belle

PRL 98 211802 (2007)

PRL 98 211803 (2007)

Confirmed by CDF

PRL 100 121802 (2008)



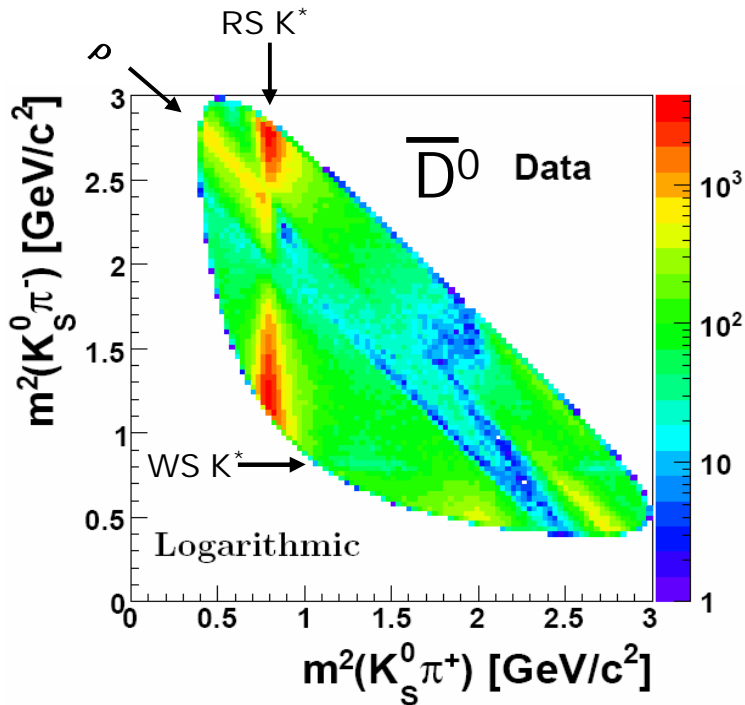
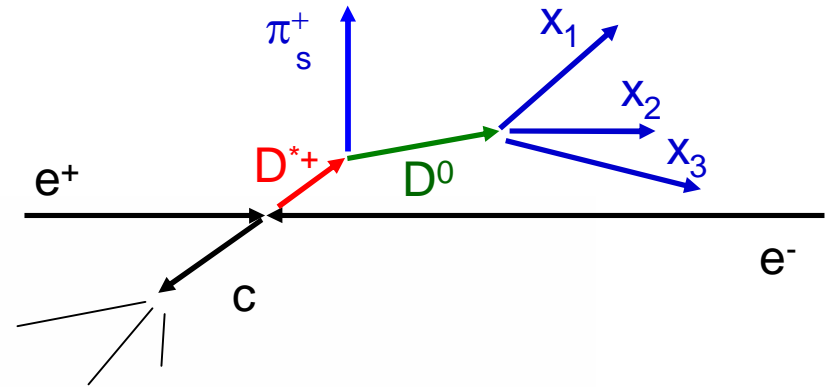
CP self-conjugate final state

$$D^0 \rightarrow K_S \pi^+ \pi^-$$

$$D^0 \rightarrow K_S K^+ K^-$$

609M  $c\bar{c}$  pairs. (468.5 fb<sup>-1</sup>)

Time-dependent Dalitz analysis

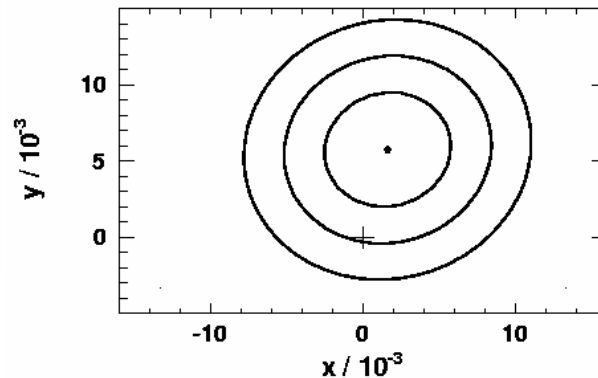


No CPV is observed.

If CP conservation assumed:

$$x = (1.6 \pm 2.3_{\text{stat}} \pm 1.2_{\text{syst}} \pm 0.8_{\text{mod}}) \cdot 10^{-3},$$

$$y = (5.7 \pm 2.0_{\text{stat}} \pm 1.3_{\text{syst}} \pm 0.7_{\text{mod}}) \cdot 10^{-3}$$



The most accurate measurement by now

# Direct CP violation in D decays



$$A_{CP} = \frac{\Gamma_D - \Gamma_{\bar{D}}}{\Gamma_D + \Gamma_{\bar{D}}} \quad \Gamma = \text{yields}$$

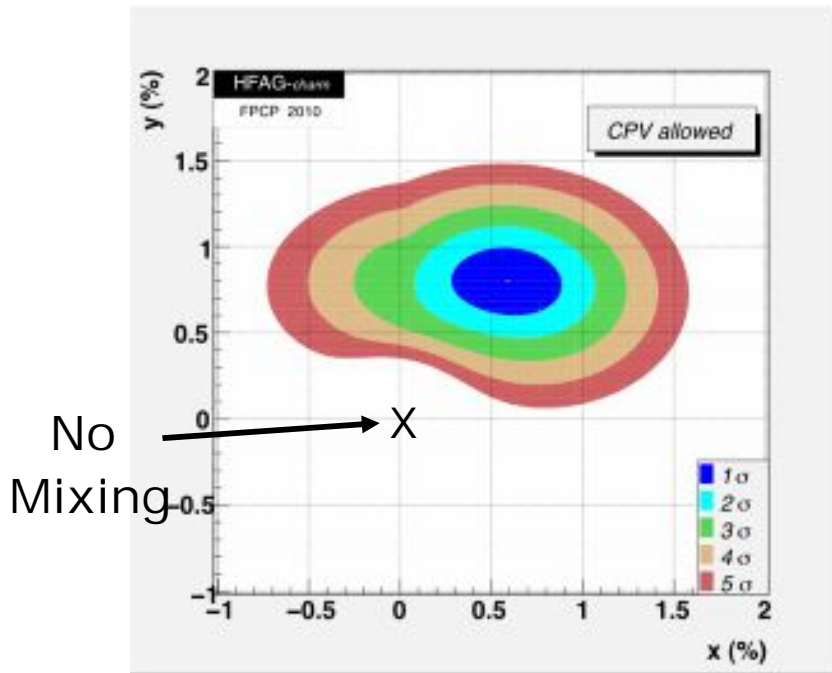
Possible bias from detector asymmetries can be estimated if use several decays at a time (see PRL 104,181602 (2010) for details):

		Decay Mode	$A_{CP}$ (%) (Belle)	$A_{CP}$ (%) (other)	$A_{CP}$ (%) (SM from $K_S^0$ )
673 fb <sup>-1</sup>	PRL 104,181602	$D^+ \rightarrow K_S^0 \pi^+$	$-0.71 \pm 0.19 \pm 0.20$	$-1.3 \pm 0.7 \pm 0.3$	-0.332
		$D^+ \rightarrow K_S^0 K^+$	$-0.16 \pm 0.58 \pm 0.25$	$-0.2 \pm 1.5 \pm 0.9$	-0.332
		$D_s^+ \rightarrow K_S^0 \pi^+$	$+5.45 \pm 2.50 \pm 0.33$	$+16.3 \pm 7.3 \pm 0.3$	+0.332
		$D_s^+ \rightarrow K_S^0 K^+$	$+0.12 \pm 0.36 \pm 0.22$	$+4.7 \pm 1.8 \pm 0.9$	-0.332
791 fb <sup>-1</sup>	Preliminary	$D^0 \rightarrow K_S^0 \pi^0$	$-0.28 \pm 0.19 \pm 0.10$	$+0.1 \pm 1.3$	-0.332
		$D^0 \rightarrow K_S^0 \eta$	$+0.54 \pm 0.51 \pm 0.13$	N.A.	-0.332
		$D^0 \rightarrow K_S^0 \eta'$	$+0.90 \pm 0.67 \pm 0.15$	N.A.	-0.332

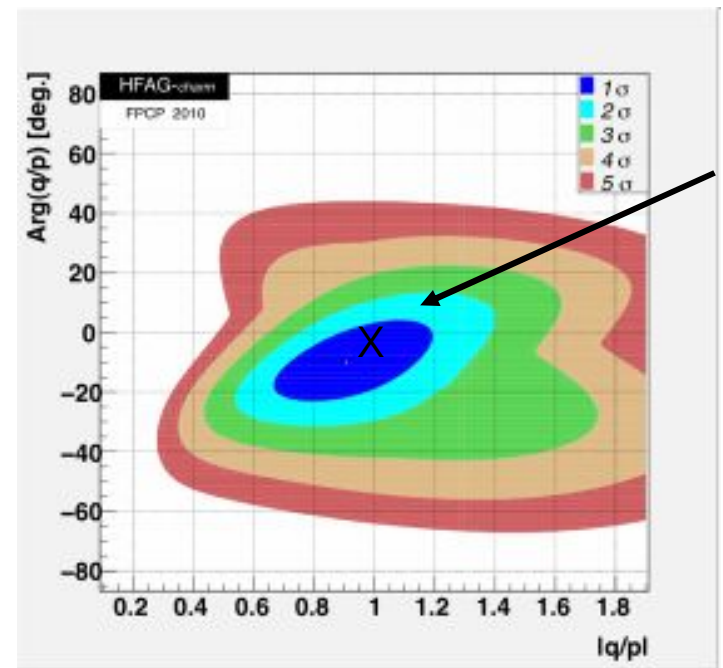
Another solution: normalize CP asymmetry to CF channels

PRL 95,231801 (2005)

# HFAG mixing and CPV summary



$x = (0.59 \pm 0.20)\%$   
 $x \in [0.19, 0.97] @ 95\% \text{ C.L.}$   
 $y = (0.80 \pm 0.13)\%$   
 $y \in [0.54, 1.05] @ 95\% \text{ C.L.}$

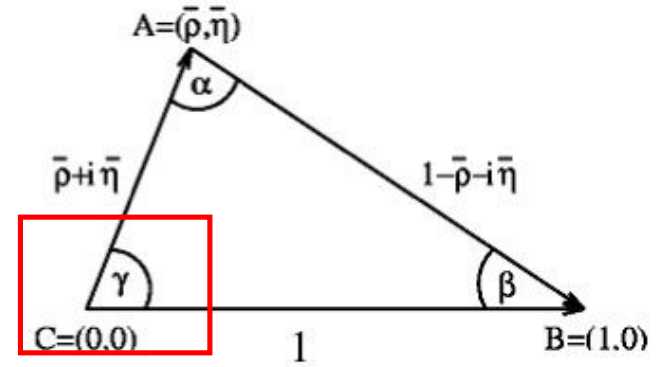
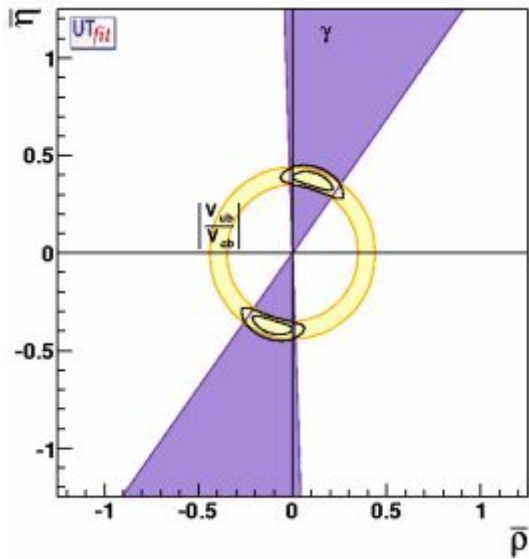


$|q/p| = (0.91^{+0.19}_{-0.16})$   
 $|q/p| \in [0.60, 1.29] @ 95\% \text{ C.L.}$   
 $\arg(q/p) = (-10.0^{+9.3}_{-8.7})^\circ$   
 $\arg(q/p) \in [-26.9, 8.4] @ 95\% \text{ C.L.}$

Evidence for mixing is  $>10\sigma$   
 No evidence for *CPV*

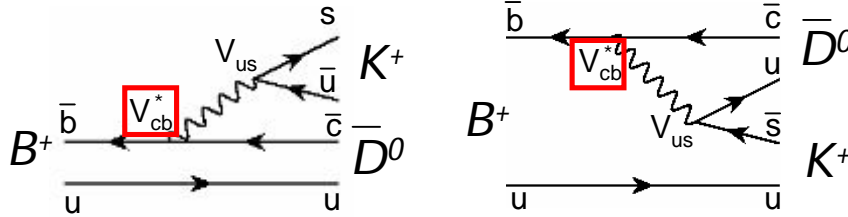
No  
CPV

# $\gamma$ measurements

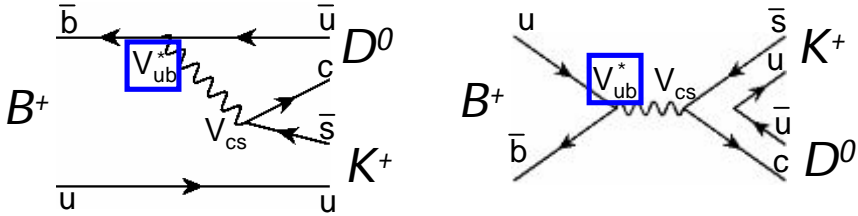


# $\gamma/\phi_3$ measurements from $B \rightarrow D^{(*)}K^{(*)}$

$b \rightarrow c$



$b \rightarrow u$



relative phase  $\gamma$

- Advantages:
- Only tree decays.
  - Largely unaffected by the New Physics scenarios
  - Clear theoretical interpretation

- Disadvantages:
- Rare decays and low  $r_B$

Related variables (depend on the  $B$  meson decay channel):

$$r_B = \frac{|A_{b \rightarrow u}|}{|A_{b \rightarrow c}|} \begin{cases} r_B \sim 0.1 & \text{For charged } B \text{ mesons} \\ r_B \sim 0.3 & \text{For neutral } B \text{ mesons} \end{cases}$$

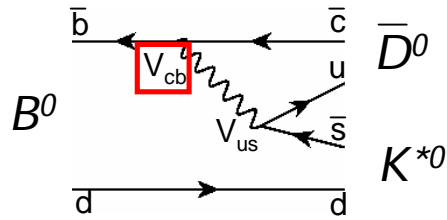
$\delta_B$  strong phase ( $CP$  conserving)

- Experimentally not easy to measure.  
Three ways to extract the information:
- GLW
  - ADS
  - Dalitz



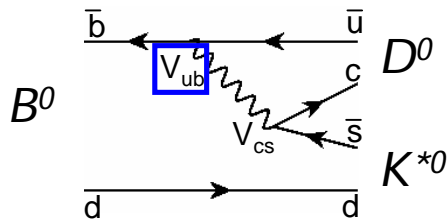
# $\gamma/\phi_3$ measurements from $B \rightarrow D^{(*)}K^{(*)}$

$b \rightarrow c$  ( $V_{cb}$ , real)



relative phase  $\gamma$

$b \rightarrow u$  ( $V_{ub} = |V_{ub}| e^{-i\gamma}$ )



- Advantages:
- Only tree decays.
  - Largely unaffected by the New Physics scenarios
  - Clear theoretical interpretation

- Disadvantages:
- Rare decays and low  $r_B$

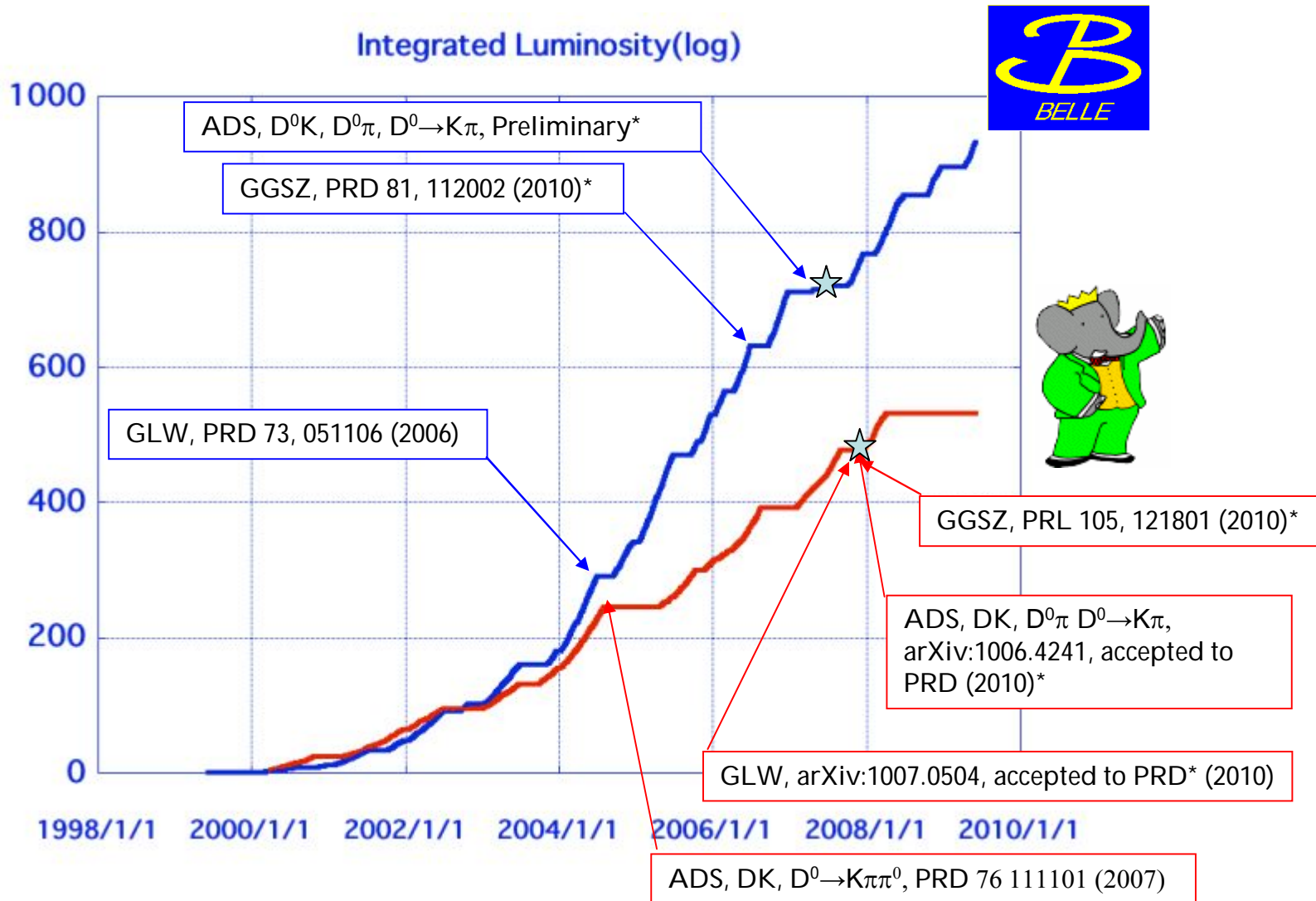
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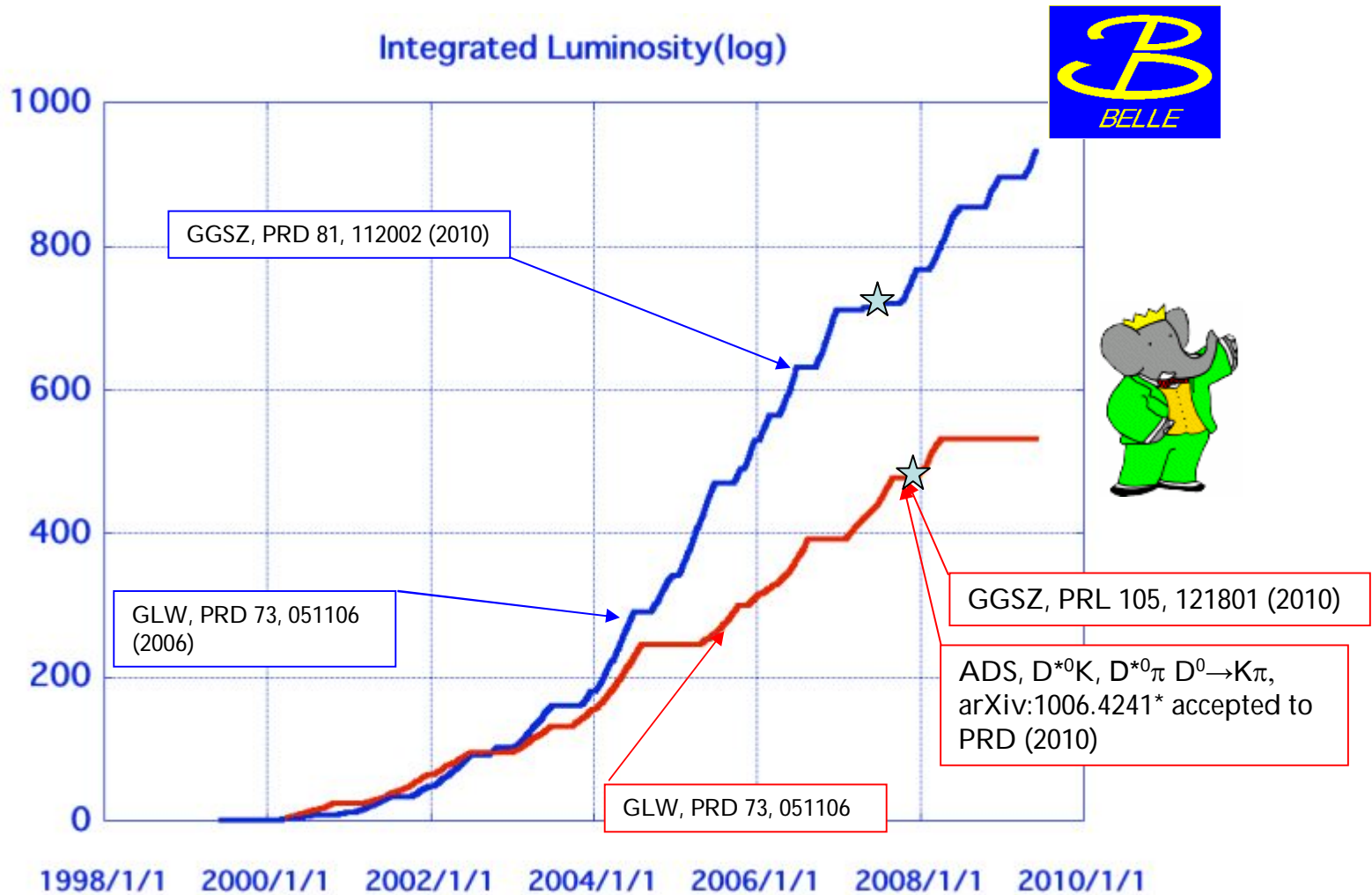
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# Results from $B \rightarrow D^0 K^+$

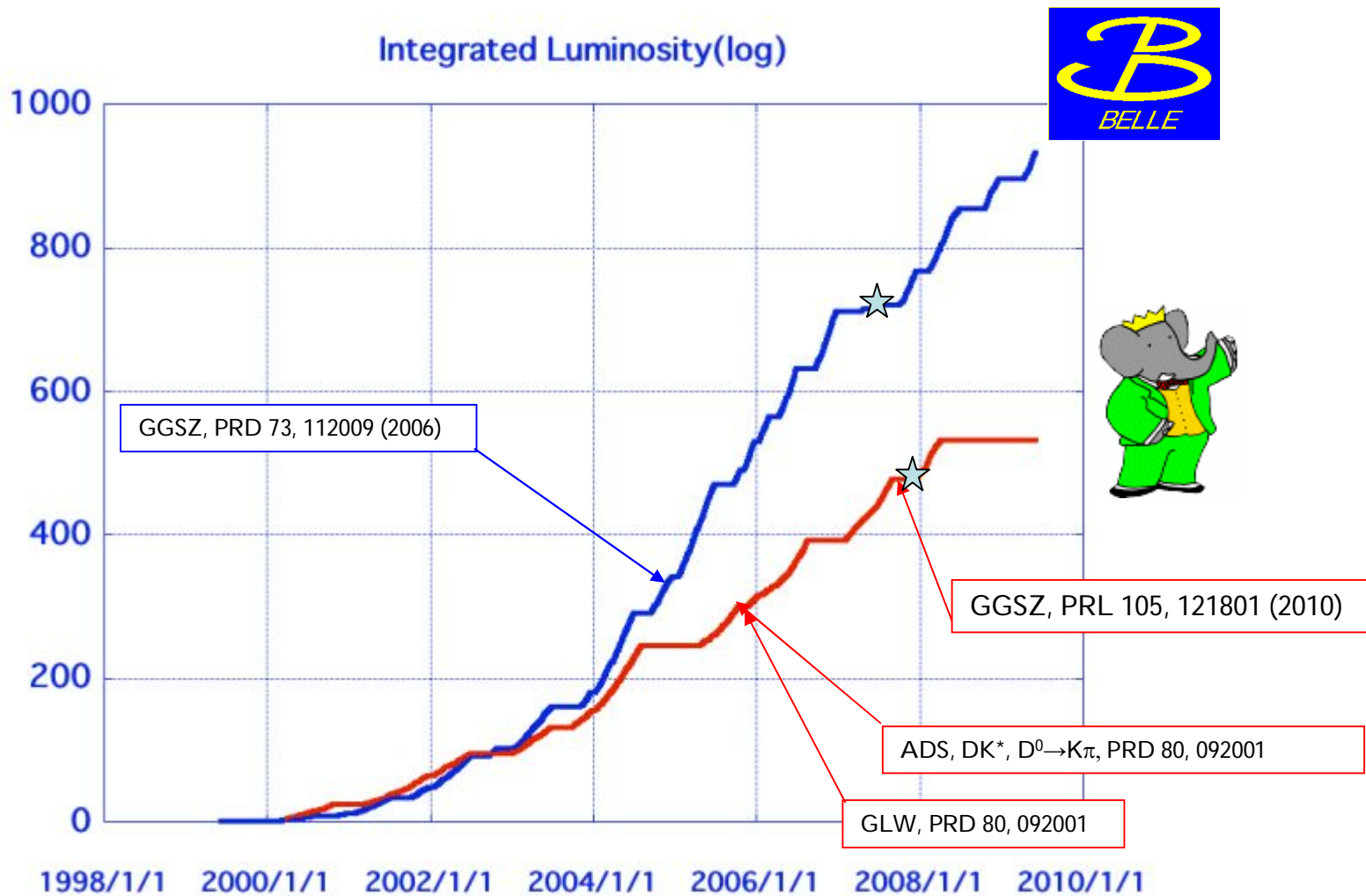


\* = in this talk

# Results from $B \rightarrow D^{*0}K^+$



# Results from $B \rightarrow D^0 K^{*+}$



# $\gamma/\phi_3$ measurements with GGSZ

## Dalitz Method

A. Giri, Yu. Grossman, A. Soffer, J. Zupan, PRD 68, 054018 (2003)

Modes:

$$K_S \pi^+ \pi^- \quad x_{\pm} = \text{Re}(r_B e^{i(\delta \pm \gamma)}) = r_B \cos(\delta \pm \gamma)$$

$$\begin{matrix} K_S K^+ K^- \\ \pi^+ \pi^- \pi^0 \end{matrix} \quad y_{\pm} = \text{Im}(r_B e^{i(\delta \pm \gamma)}) = r_B \sin(\delta \pm \gamma)$$

## ADS Method

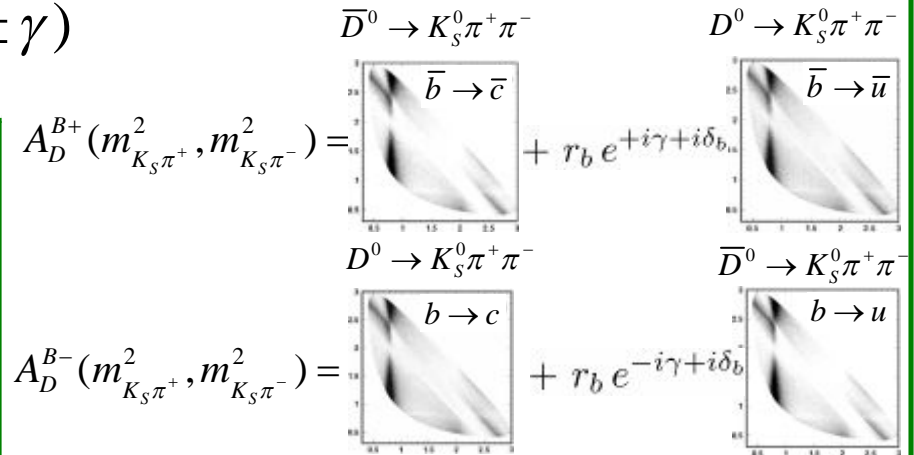
$$\begin{matrix} \text{Modes:} \\ K^+ \pi^-, \\ K^+ \pi^- \pi^0, \\ K^+ \pi^- \pi^+ \pi^- \end{matrix} \quad R_{ADS} = \frac{\Gamma([K^+ \pi^- \pi^0] K^-) + \Gamma([K^- \pi^+ \pi^0] K^+)}{\Gamma([K^- \pi^- \pi^0] K^-) + \Gamma([K^+ \pi^+ \pi^0] K^+)}$$

$$A_{ADS} = \frac{\Gamma([K^+ \pi^- \pi^0] K^-) - \Gamma([K^- \pi^+ \pi^0] K^+)}{\Gamma([K^+ \pi^- \pi^0] K^-) + \Gamma([K^- \pi^+ \pi^0] K^+)}$$

## GLW Method

$$D^0 \text{ Modes: } R_{CP\pm} = \frac{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}{2\Gamma(B^+ \rightarrow D^0 K^+)}$$

$$\begin{matrix} CP+ \\ CP- \end{matrix} \quad A_{CP\pm} = \frac{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) - \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}$$



Advantages:

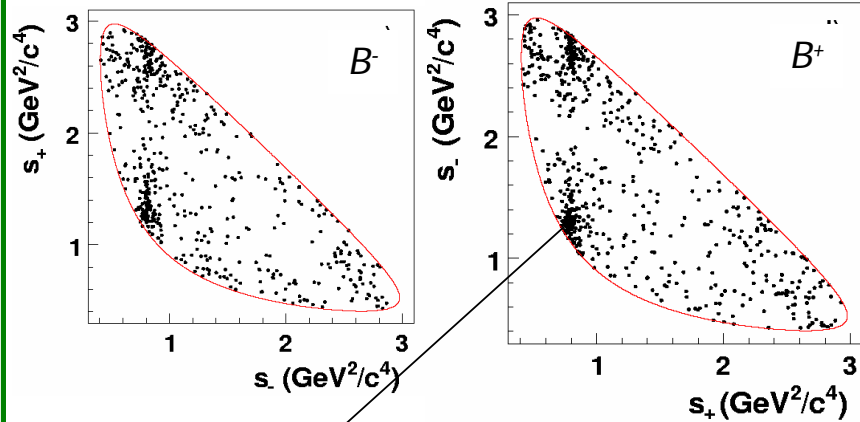
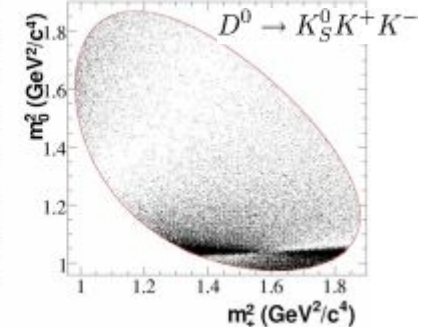
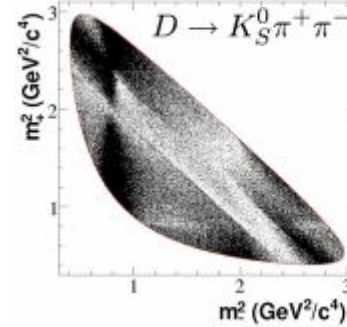
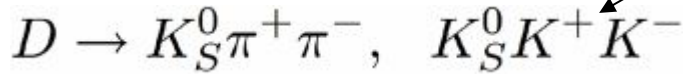
- large interferences in some Dalitz regions
- strong phases varying over the Dalitz plane

Dalitz Method



BaBar 425 fb<sup>-1</sup>  
(468 MBB)

BaBar only!

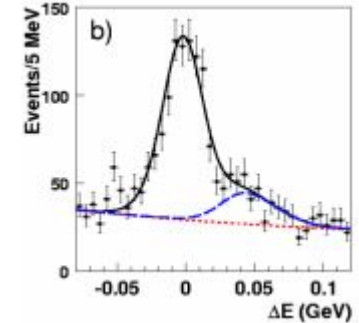
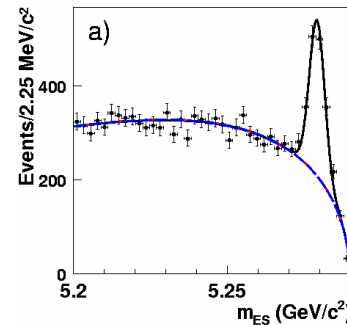


Resonance structure provides an important information on the phases

Signal is separated from background using  $m_{ES}$ , Fisher (on event shape variables),  $\Delta E$ , ( $s_+$ ,  $s_-$ ) (invariant masses of  $K_S \pi^+$  and  $K_S \pi^-$ )

$$m_{ES} = \sqrt{E_{\text{beam}}^2 - p_B^2}$$

$$\Delta E = E_B - E_{\text{beam}}$$



The reconstruction efficiency is 22%  
Fit for yields and CP violating parameters

Dalitz Method

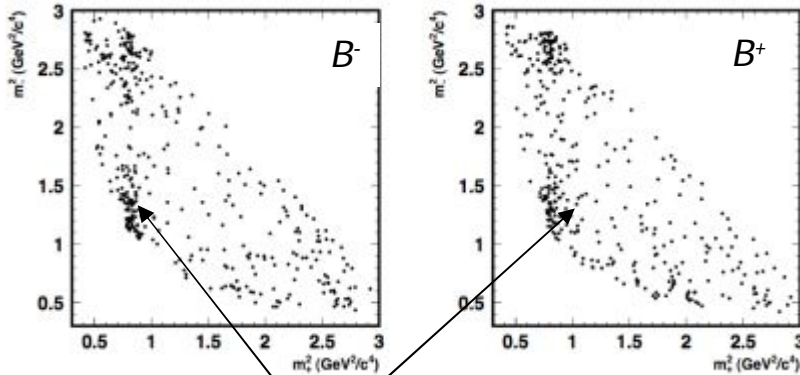


Belle 605 fb<sup>-1</sup>  
(657 MBB)

$$D \rightarrow K_S^0 \pi^+ \pi^-$$

Signal events yield

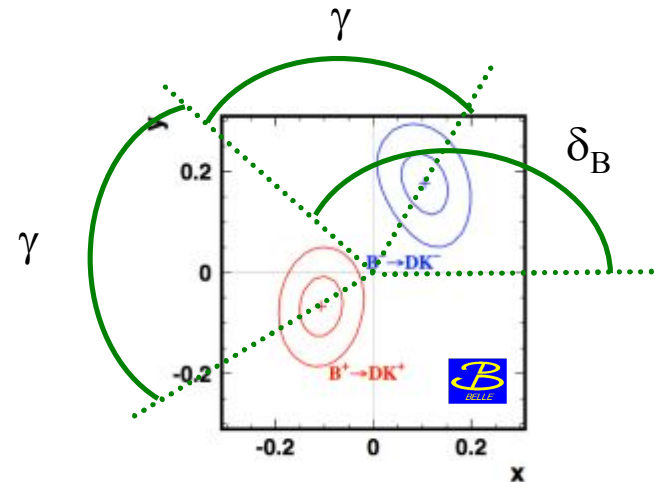
	(K <sub>S</sub> ππ)	(K <sub>S</sub> ππ)	(K <sub>S</sub> KK)
	657 MBB	468 MBB	468 MBB
B <sup>±</sup> → DK <sup>±</sup>	757 ± 30	920 ± 35	142 ± 14



Resonance structure provides an important information on the phases

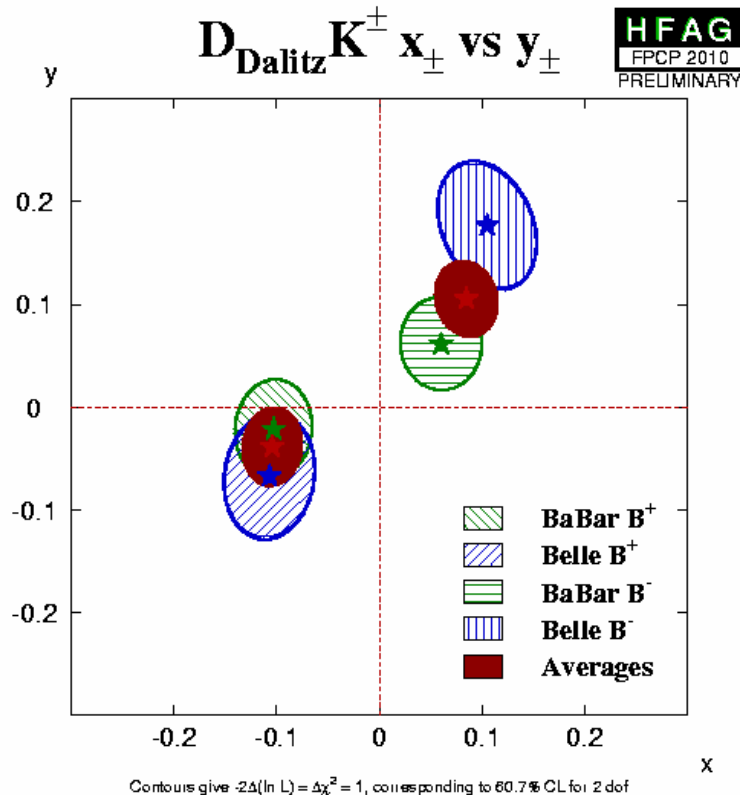
$$x_{\pm} = \text{Re}(r_B e^{i(\delta \pm \gamma)}) = r_B \cos(\delta \pm \gamma)$$

$$y_{\pm} = \text{Im}(r_B e^{i(\delta \pm \gamma)}) = r_B \sin(\delta \pm \gamma)$$



# $\gamma/\phi_3$ extraction from the GGSZ results

## Dalitz Method



Not an easy task to average the results, the model errors are not easy to be combined

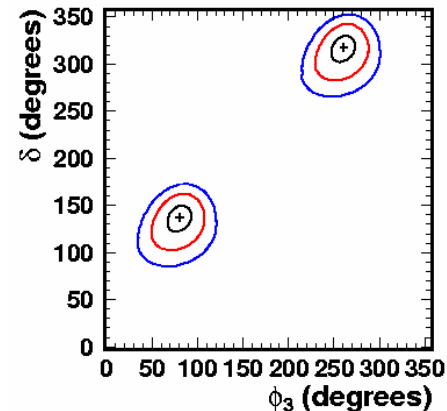
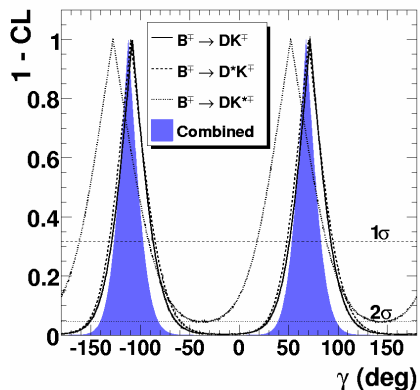
Main differences in  $D^0 \rightarrow K_s \pi^+ \pi^-$ :

- BaBar: K-matrix formalism for  $\pi\pi$  S-wave, LASS model for  $K\pi$  S-wave.
- Belle: Includes  $\sigma_1$  and  $\sigma_2$   $\pi\pi$  scalar resonances.  $K^{*0}(1430)$  for  $K\pi$  Swave.

BaBar result also includes  $D^0 \rightarrow K_s K^+ K^-$



# $\gamma/\phi_3$ from Belle/BaBar



Parameter	68.3% CL	95.4% CL
$\gamma$ ( $^\circ$ )	$68^{+15}_{-14}$ {4, 3}	[39, 98]
$r_B$ (%)	$9.6 \pm 2.9$ {0.5, 0.4}	[3.7, 15.5]
$r_B^*$ (%)	$13.3^{+4.2}_{-3.9}$ {1.3, 0.3}	[4.9, 21.5]
$\kappa r_s$ (%)	$14.9^{+6.6}_{-6.2}$ {2.6, 0.6}	< 28.0
$\delta_B$ ( $^\circ$ )	$119^{+19}_{-20}$ {3, 3}	[75, 157]
$\delta_B^*$ ( $^\circ$ )	$-82 \pm 21$ {5, 3}	[-124, -38]
$\delta_s$ ( $^\circ$ )	$111 \pm 32$ {11, 3}	[42, 178]

Parameter	$B^+ \rightarrow DK^+$ mode	$B^+ \rightarrow D^*K^+$ mode
$\phi_3$	$(80.8^{+13.1}_{-14.8} \pm 5.0 \pm 8.9)^\circ$	$(73.9^{+18.9}_{-20.2} \pm 4.2 \pm 8.9)^\circ$
$r$	$0.161^{+0.040}_{-0.038} \pm 0.011^{+0.050}_{-0.010}$	$0.196^{+0.073}_{-0.072} \pm 0.013^{+0.062}_{-0.012}$
$\delta$	$(137.4^{+13.0}_{-15.7} \pm 4.0 \pm 22.9)^\circ$	$(341.7^{+18.6}_{-20.9} \pm 3.2 \pm 22.9)^\circ$

BaBar obtains  
 $\gamma = (68^{+15}_{-14} \pm 4 \pm 3)^\circ$   
 (from  $DK^-$ ,  $D^*K^-$ ,  $DK^{*-}$ )

Belle obtains  
 $\phi_3 = (78^{+11}_{-12} \pm 4 \pm 9)^\circ$   
 (from  $DK^-$  and  $D^*K^-$ )

PRL 105, 121801 (2010)

PRD 81, 112002 (2010)

# $\gamma/\phi_3$ measurements with ADS

## Dalitz Method

Modes:

$K_S \pi^+ \pi^-$

$K_S K^+ K^-$

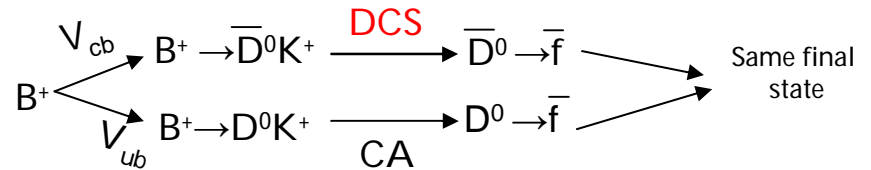
$\pi^+ \pi^- \pi^0$

$$x_{\pm} = r_B \cos(\delta \pm \gamma)$$

$$y_{\pm} = r_B \sin(\delta \pm \gamma)$$

D. Atwood, I. Dunietz and A. Soni, PRL 78, 3357 (1997).

Interplay between **Doubly-Cabibbo-Suppressed** and Cabibbo allowed  $D$  meson decay



Branching fraction of processes is quite low ( $\sim 10^{-7}$ )

## ADS Method

$D^0$  Modes:

$K^+ \pi^-$ ,

$K^+ \pi^- \pi^0$ ,

$K^+ \pi^- \pi^+ \pi^-$

$$R_{ADS} = \frac{\Gamma([\bar{f}]K^-) + \Gamma([\bar{f}]K^+)}{\Gamma([f]K^-) + \Gamma([f]K^+)} = r_B^2 + r_D^2 + 2k_D r_B r_D \cos(\delta_B + \delta_D) \cos \gamma$$

$$A_{ADS} = \frac{\Gamma([\bar{f}]K^-) - \Gamma([\bar{f}]K^+)}{\Gamma([f]K^-) + \Gamma([f]K^+)} = 2k_D r_B r_D \cos(\delta_B + \delta_D) \cos \gamma / R_{ADS}$$

$$r_D = \frac{|A_{c \rightarrow u}|}{|A_{c \rightarrow s}|}$$

Parameters:

$\{\gamma; r_B; \delta_B\}$

$$k_D e^{i\delta_D} = \frac{\int A_D \bar{A}_D e^{i(\bar{\delta}(m) - \delta(m))} dm}{\sqrt{\int |A_D|^2 dm \int |\bar{A}_D|^2 dm}}$$

External Inputs:

$\{r_D; \delta_D; k_D\}$



CDF also gave the results with this type of analysis

# $\gamma/\phi_3$ measurements with ADS from BELLE



Belle 711 fb<sup>-1</sup>  
(772 MBB)

PRELIMINARY

Two decay chains:

$$B^- \rightarrow D^0 h^-, D^0 \rightarrow K^- \pi^+$$

Same sign

$h = K, \pi$

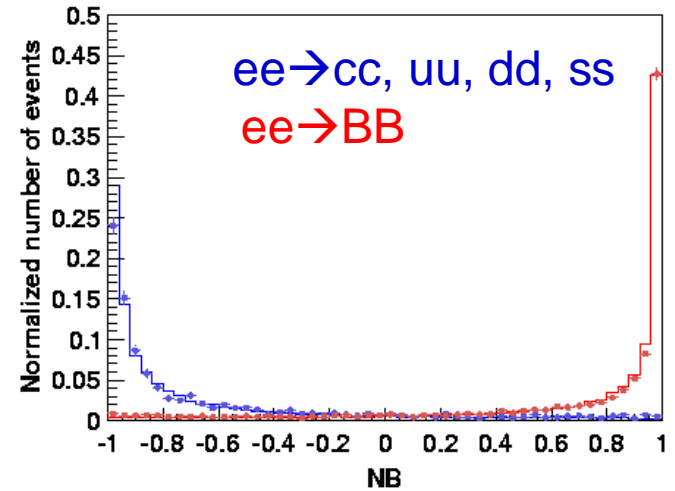
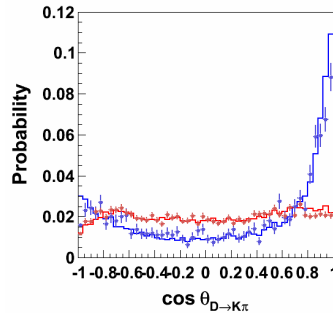
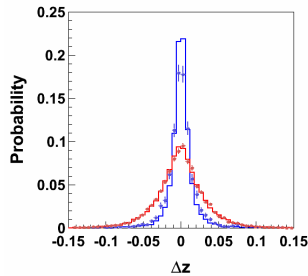
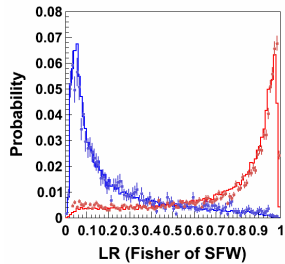
$$B^- \rightarrow D^0 h^-, D^0 \rightarrow K^+ \pi^-$$

Opposite sign

Simultaneous fit to  $\Delta E$  and NeuroBayes neural network to  $Dh$  sample

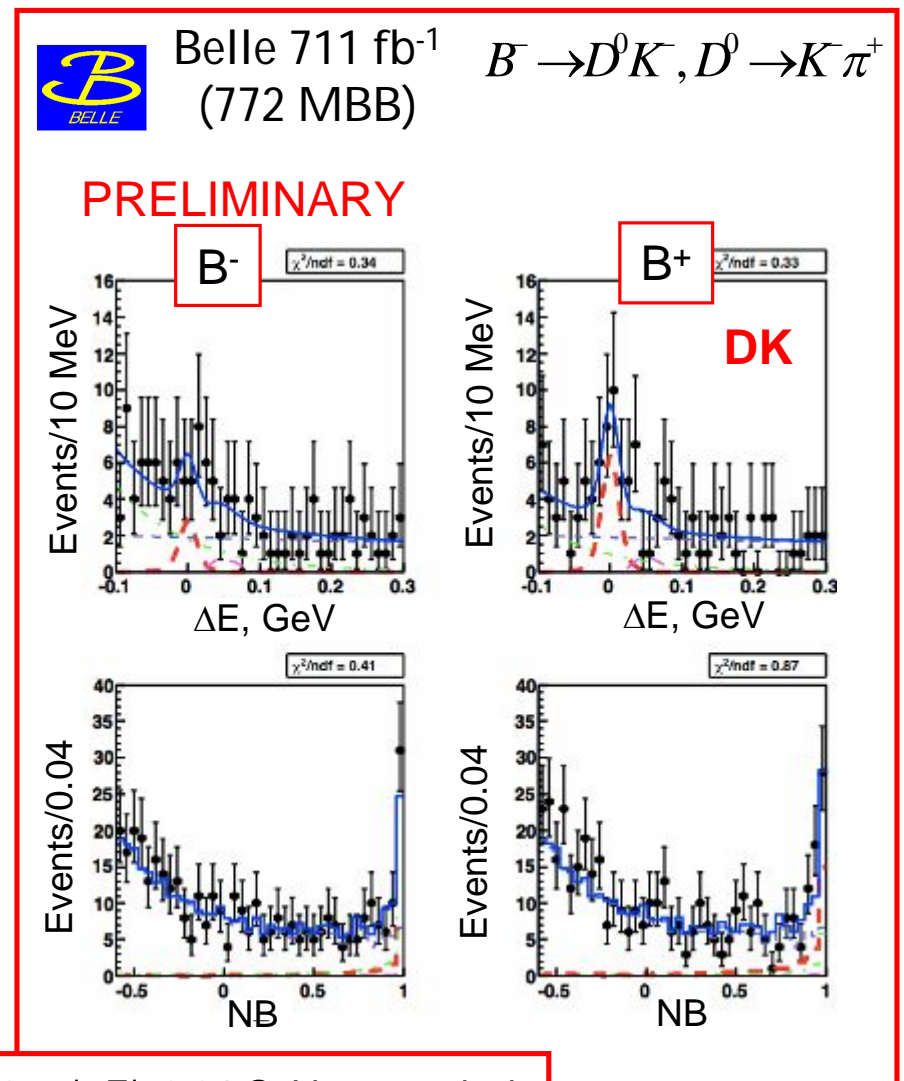
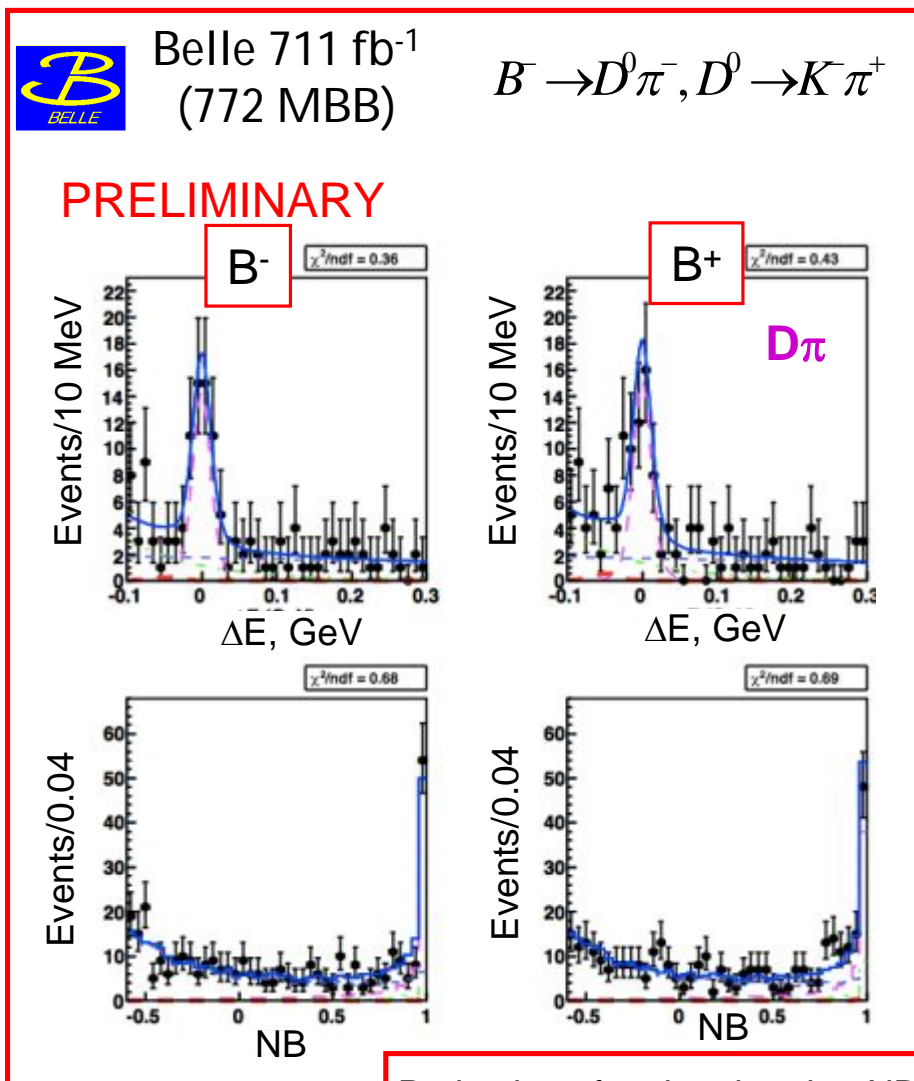
## NeuroBayes neural network (NB), 10 inputs:

- LR for Fisher of SFW moments
  - Vertex separation between reconstructed B and the other B ( $\Delta z$ )
  - Decay angle for  $D \rightarrow K\pi$
- Etc...



Fit region:  $NB > -0.6, -0.1 < \Delta E < 0.3$  GeV




# $\gamma/\phi_3$ measurements with ADS from BELLE



Projections for signal region NB>0.5,  $|\Delta E| < 0.04$  GeV, respectively

# $\gamma/\phi_3$ measurements with ADS from BaBar/BELLE ( $B \rightarrow DK$ )

## ADS $B \rightarrow Dh$ summary

	 772 MBB	 657 MBB	 468 MBB
$\mathcal{R}_{DK} [\times 10^{-2}]$	$1.62 \pm 0.42 \begin{smallmatrix} +0.16 \\ -0.19 \end{smallmatrix} *$	$0.78 \begin{smallmatrix} +0.62 & +0.20 \\ -0.57 & -0.28 \end{smallmatrix}$	$1.1 \pm 0.6 \pm 0.2$
$\mathcal{R}_{D\pi} [\times 10^{-3}]$	$3.28 \pm 0.37 \begin{smallmatrix} +0.22 \\ -0.23 \end{smallmatrix} *$	$3.40 \begin{smallmatrix} +0.55 & +0.15 \\ -0.53 & -0.22 \end{smallmatrix}$	$3.3 \pm 0.6 \pm 0.4$
$A_{DK}$	$-0.39 \pm 0.26 \begin{smallmatrix} +0.06 \\ -0.04 \end{smallmatrix}$	$-0.1 \begin{smallmatrix} +0.8 \\ -1.0 \end{smallmatrix} \pm 0.4$	$-0.86 \pm 0.47 \begin{smallmatrix} +0.12 \\ -0.16 \end{smallmatrix}$
$A_{D\pi}$	$-0.04 \pm 0.11 \begin{smallmatrix} +0.01 \\ -0.02 \end{smallmatrix}$	$-0.02 \begin{smallmatrix} +0.15 \\ -0.16 \end{smallmatrix} \pm 0.04$	$0.03 \pm 0.17 \pm 0.04$

All the values are very consistent with yet leading statistical error

- \* Most precise measurements to date with a significance  $8.4\sigma$  (including syst).
- \* First evidence is obtained with a significance  $3.8\sigma$  (including syst).



@CKM workshop

$$R_{\text{ADS}}(DK) = (2.25 \pm 0.84(\text{stat}) \pm 0.79(\text{syst})) \cdot 10^{-2}$$

$$R_{\text{ADS}}(D\pi) = (4.1 \pm 0.8(\text{stat}) \pm 0.4(\text{syst})) \cdot 10^{-3}$$

$$A_{\text{ADS}}(DK) = -0.63 \pm 0.40(\text{stat}) \pm 0.23(\text{syst})$$

$$A_{\text{ADS}}(D\pi) = 0.22 \pm 0.18(\text{stat}) \pm 0.06(\text{syst})$$

PRELIMINARY

# $\gamma/\phi_3$ measurements with GLW

## Dalitz Method

Modes:

$$\begin{aligned} K_S \pi^+ \pi^- & \quad x_{\pm} = r_B \cos(\delta \pm \gamma) \\ K_S K^+ K^- & \quad y_{\pm} = r_B \sin(\delta \pm \gamma) \\ \pi^+ \pi^- \pi^0 & \end{aligned}$$

## ADS Method

$$\begin{aligned} \text{Modes: } & R_{ADS} = \frac{\Gamma([K^+ \pi^- \pi^0] K^-) + \Gamma([K^- \pi^+ \pi^0] K^+)}{\Gamma([K^- \pi^- \pi^0] K^-) + \Gamma([K^+ \pi^+ \pi^0] K^+)} \\ & K^+ \pi^-, \\ & K^+ \pi^- \pi^0, \\ & K^+ \pi^- \pi^+ \pi^- \quad A_{ADS} = \frac{\Gamma([K^+ \pi^- \pi^0] K^-) - \Gamma([K^- \pi^+ \pi^0] K^+)}{\Gamma([K^+ \pi^- \pi^0] K^-) + \Gamma([K^- \pi^+ \pi^0] K^+)} \end{aligned}$$

## GLW Method

$D^0$  Modes:

$CP_+$

$CP_-$

$$\begin{aligned} R_{CP_{\pm}} &= \frac{\Gamma(B^- \rightarrow D_{CP_{\pm}}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP_{\pm}}^0 K^+)}{2\Gamma(B^+ \rightarrow D^0 K^+)} = 1 + r_B^2 \pm 2r_B \cos \gamma \cos \delta_B \\ A_{CP_{\pm}} &= \frac{\Gamma(B^- \rightarrow D_{CP_{\pm}}^0 K^-) - \Gamma(B^+ \rightarrow D_{CP_{\pm}}^0 K^+)}{\Gamma(B^- \rightarrow D_{CP_{\pm}}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP_{\pm}}^0 K^+)} = \pm 2r_B \cos \gamma \cos \delta_B / R_{CP_{\pm}} \end{aligned}$$

M. Gronau, D. London, D. Wyler, PLB253,483 (1991);  
PLB 265, 172 (1991)

Theoretically very clean to determine  $\gamma$  (with four observable)

Many  $D^0$  Modes reconstructed:

$$CP_+ : D^0 \rightarrow K^+ K^-, \pi^+ \pi^-$$

$$CP_- : D^0 \rightarrow K_S^0 \pi^0, K_S^0 \omega, K_S^0 \phi, (K_S^0 \eta)$$



CDF also gave the results with this type of analysis

4 observables  
(3 independent) and  
3 unknowns



BaBar 425 fb<sup>-1</sup>  
(468 MBB)

ML fit to { $m_{ES}$ ,  $\Delta E$ , Fisher(same vars as GGSZ + ratio of 2nd and 0th order Fox-Wolfram moments)}

Simultaneous fit to the subsamples corresponding to different D decays

$$A_{CP+} = 0.25 \pm 0.06 \pm 0.02$$

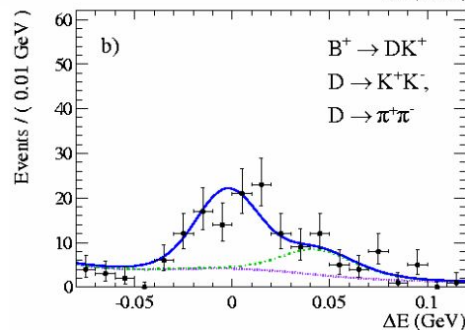
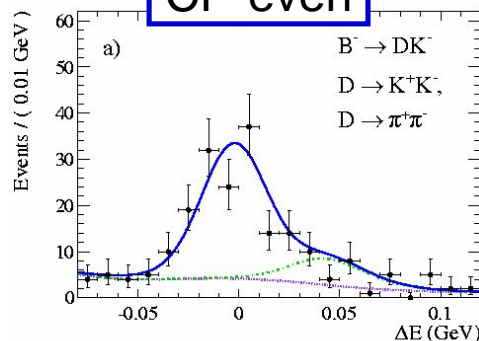
$$A_{CP-} = -0.09 \pm 0.07 \pm 0.02$$

$$R_{CP+} = 1.18 \pm 0.09 \pm 0.05$$

$$R_{CP-} = 1.07 \pm 0.08 \pm 0.04$$

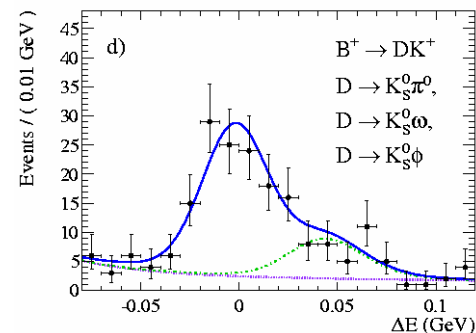
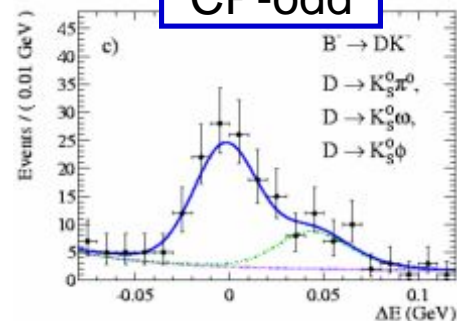
Direct CPV at 3.6 $\sigma$   
in  $B \rightarrow D_{CP+} K$  decays !

CP-even



$$N_{CP+} = 477 \pm 28$$

CP-odd



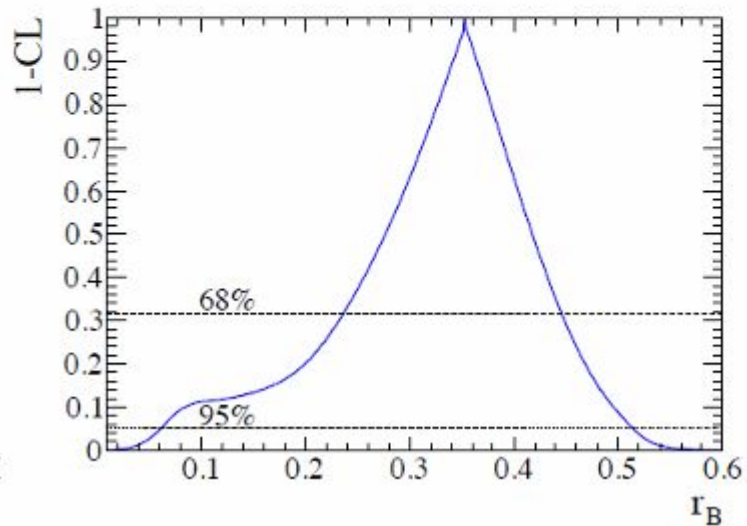
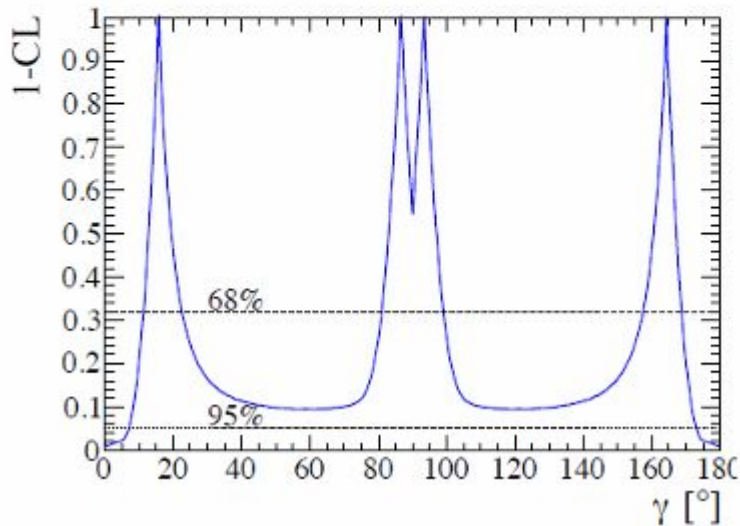
$$N_{CP-} = 506 \pm 26$$



# $\gamma/\phi_3$ measurements with the GLW method from BaBar

Frequentist interpretation gives:

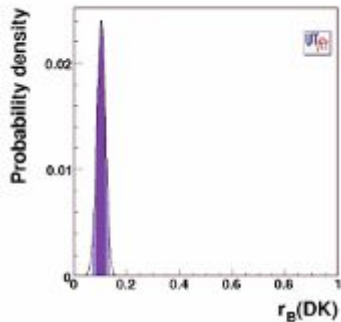
	$\gamma \text{ mod } 180 [^\circ]$	$r_B$
68% CL	[11.3, 22.7] [80.9, 99.1] [157.3, 168.7]	[0.24, 0.45]
95% CL	[7.0, 173.0]	[0.06, 0.51]



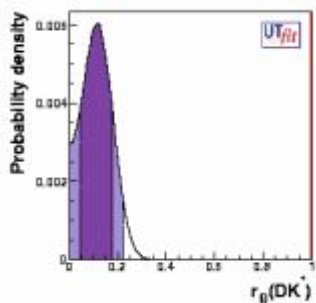
Large value of  $r_B$  is favored (but large uncertainty: less than  $2\sigma$  from 0)



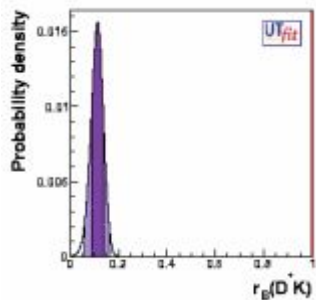
# $\gamma/\phi_3$ measurements combination



$$r_B(D^0 K^+) = (0.106 \pm 0.016)$$



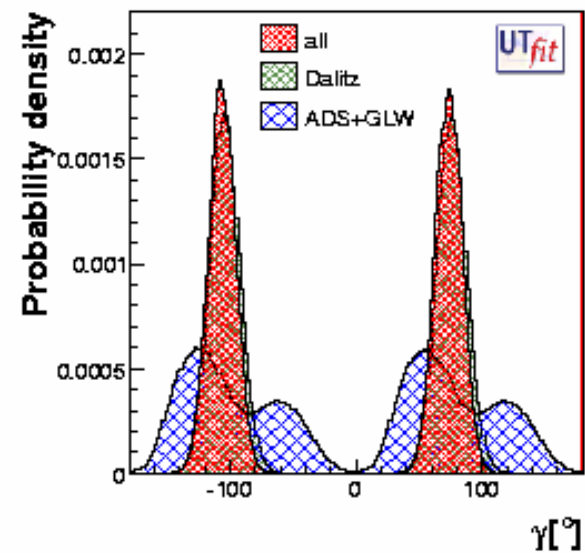
$$r_B(D^0 K^{*+}) = (0.11 \pm 0.07)$$



$$r_B(D^{*0} K^+) = (0.113 \pm 0.025)$$

The combination of all the methods can be performed giving

$$\gamma = (74 \pm 11)^\circ$$



# Conclusions

No significant  $CP$  violation in charm sector is observed

The  $D^0$  mixing is confirmed with more than  $10\sigma$  evidence

$\gamma/\phi_3$  measurements

Several analyses with  $>3\sigma$  CPV evidence in a single measurement

The combination can be performed separately. Big contributors are DK decay modes using Dalitz method.

The combination of all the method gives

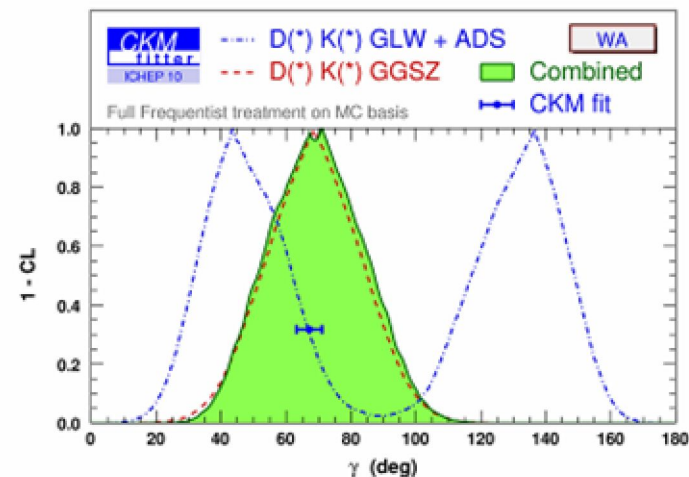
$$\gamma = (74 \pm 11)^\circ \text{ (Bayesian approach)}$$

$$\gamma = (73^{+21}_{-25})^\circ \text{ (Frequentist approach)}$$

Well compatible with the prediction from SM

$$\gamma = (69.6 \pm 3.0)^\circ \text{ (Bayesian approach)}$$

$$\gamma = (67.2^{+3.7}_{-3.7})^\circ \text{ (Frequentist approach)}$$



Need to reduce the error in order to see possible deviations:

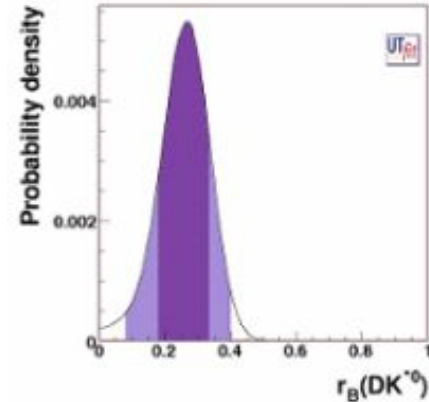
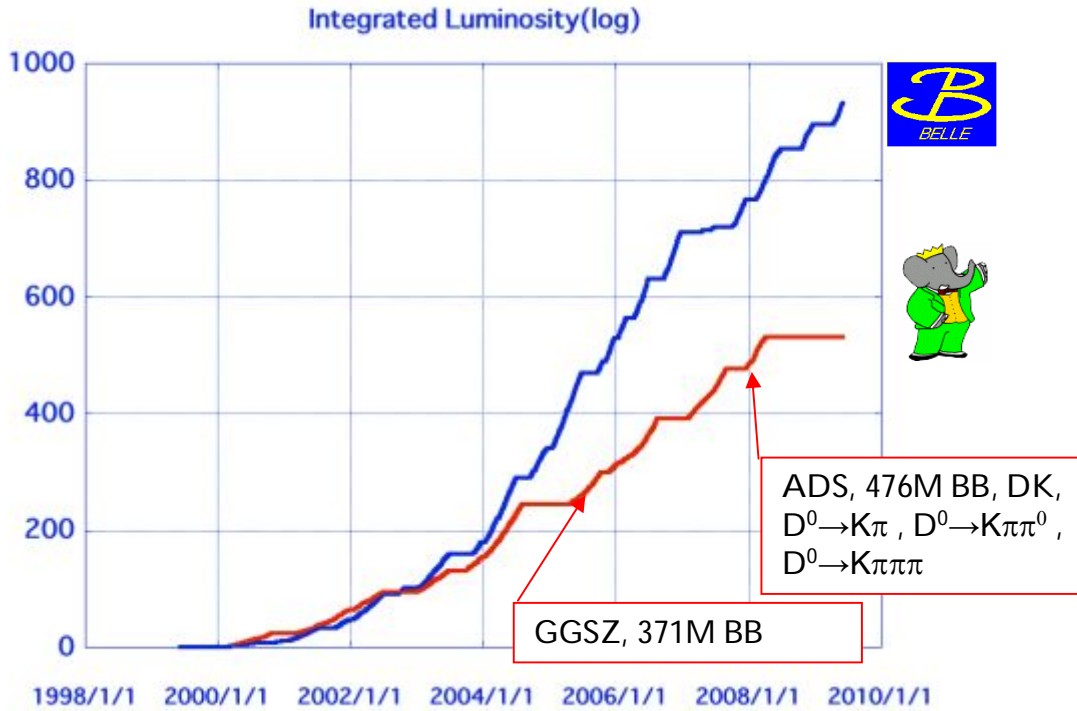


## Backup

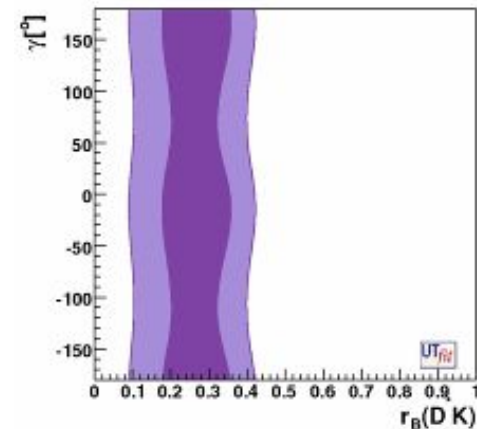
# Breakdown of the systematic uncertainties for BELLE ADS

Source	$\mathcal{R}_{DK}$	$\mathcal{R}_{D\pi}$	$\mathcal{A}_{DK}$	$\mathcal{A}_{D\pi}$
Fit	+9.7% -6.3%	+6.5% -5.3%	+0.05 -0.04	+0.009 -0.018
( $\Delta E$ -PDF	+4.4% -3.6%	+2.4% -2.3%	$\pm 0.02$	$\pm 0.003$ )
( $\mathcal{NB}$ -PDF	+4.2% -1.6%	+4.0% -2.8%	+0.02 -0.01	+0.001 -0.010 )
( Yield and asymmetry	$\pm 1.1\%$	$\pm 0.1\%$	$\pm 0.01$	$\pm 0.005$ )
Peaking backgrounds	+0.7% -9.9%	+0.0% -4.1%	+0.03 -0.00	+0.002 -0.000
Efficiency	$\pm 1.7\%$	$\pm 1.5\%$	...	...
Detector asymmetry	...	...	$\pm 0.02$	$\pm 0.005$

# $\gamma/\phi_3$ measurements from $B^0 \rightarrow DK^{*0}$



$$r_B(D^0 K^{*0}) = (0.26 \pm 0.076)$$

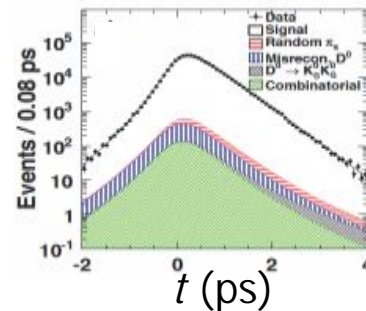
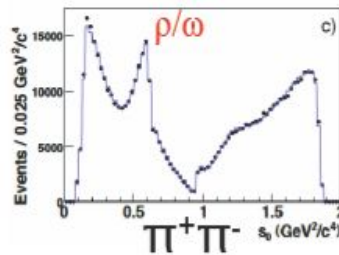
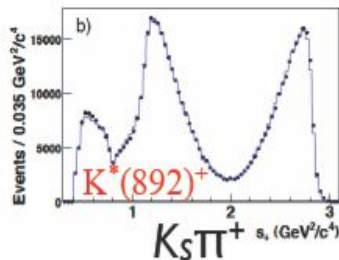
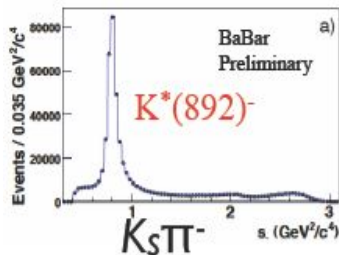


Promising channel at future experiments for measuring  $\gamma$  due to large value of  $r_B$ .  
More statistics needed  
 $D$  sector measurements play an important role.



$K_S \pi^+ \pi^-$

Signal : 541K  
purity 98.5%



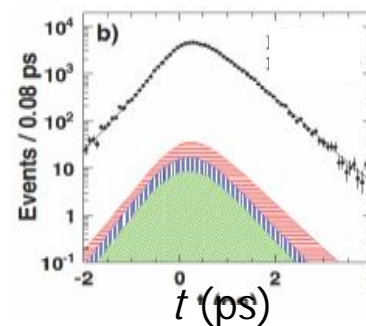
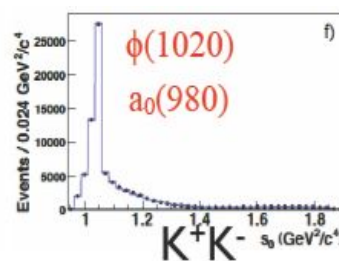
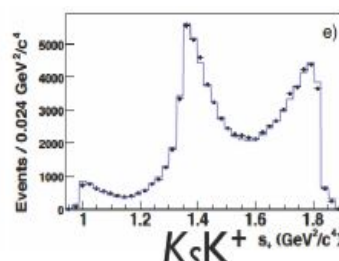
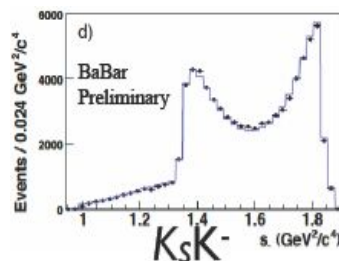
$A_f$  : **S-wave  $\pi^+ \pi^-$**   
K-matrix model

**S-wave  $K^0 \pi^-$**   
LASS model

**P- and D-waves**  
Breit-Wigner model

$K_S K^+ K^-$

Signal : 80K  
purity 99.2%



$A_f$  : **S-wave  $K^+ K^-$**   
**All other waves**

**Coupled-channel Breit-Wigner  $a_0(980)$**   
**Breit-Wigners**