

CP VIOLATION

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- Introduction
- CP Violation in $\Delta F=2$ processes
 - Standard model predictions
 - Constraints on New Physics
- Conclusions and Outlook

INTRODUCTION

The Standard Model works beautifully up to a few hundred GeV's, but it must be an effective theory valid up to a scale $\Lambda \leq M_{\text{planck}}$:

$$\mathcal{L}(M_W) = \Lambda^2 H^\dagger H + \lambda (H^\dagger H)^2 + \mathcal{L}_{\text{SM}}^{\text{gauge}} + \mathcal{L}_{\text{SM}}^{\text{Yukawa}} + \frac{1}{\Lambda} \mathcal{L}^5 + \frac{1}{\Lambda^2} \mathcal{L}^6 + \dots$$

The diagram illustrates the Lagrangian $\mathcal{L}(M_W)$ and its components. The equation is $\mathcal{L}(M_W) = \Lambda^2 H^\dagger H + \lambda (H^\dagger H)^2 + \mathcal{L}_{\text{SM}}^{\text{gauge}} + \mathcal{L}_{\text{SM}}^{\text{Yukawa}} + \frac{1}{\Lambda} \mathcal{L}^5 + \frac{1}{\Lambda^2} \mathcal{L}^6 + \dots$. A green oval encircles the terms $\mathcal{L}_{\text{SM}}^{\text{gauge}} + \mathcal{L}_{\text{SM}}^{\text{Yukawa}}$, with an arrow pointing from a box labeled "Has accidental symmetries". A red oval encircles the higher-order terms $\frac{1}{\Lambda} \mathcal{L}^5 + \frac{1}{\Lambda^2} \mathcal{L}^6 + \dots$, with an arrow pointing from a box labeled "Violates accidental symmetries". Another arrow points from a box labeled "EW scale" to the $\Lambda^2 H^\dagger H$ term.

Two accidental symmetries of the SM are crucial for our discussion:

1) Absence of tree-level flavour changing neutral currents, GIM suppression of FCNC @ the loop level

2) No CP violation @ tree level

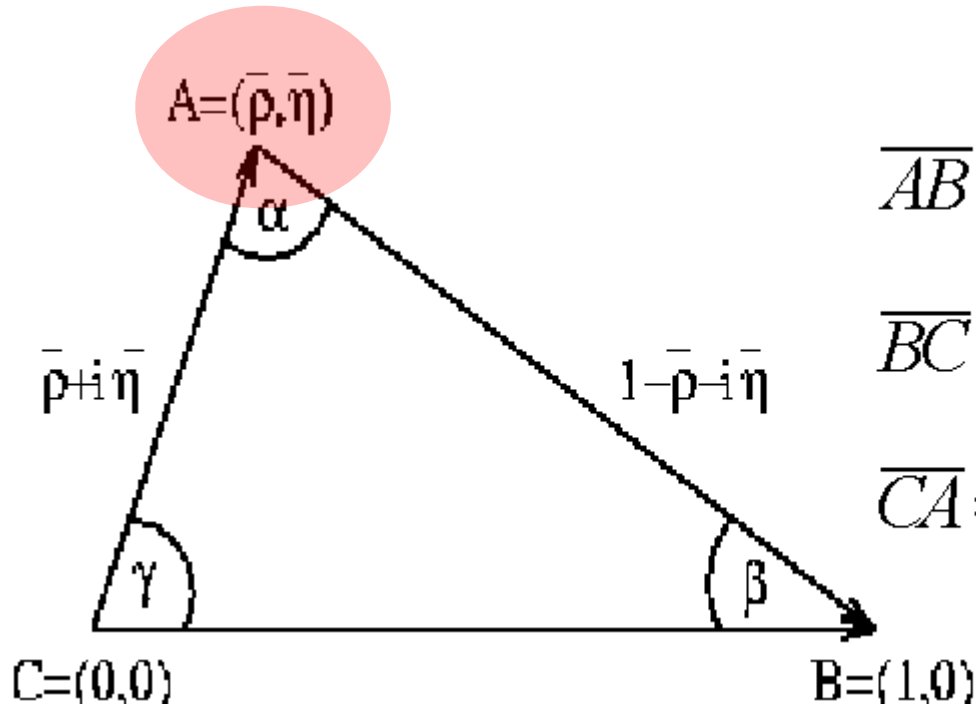
⇒ Flavour physics extremely sensitive to NP!!

The CP violation mechanism of the SM is very peculiar

- ▶ CP symmetry is explicitly broken by the Yukawa couplings
- ▶ CP is not an approximate symmetry of the model. CP violation is suppressed by mixing angles, but **the phase is of $O(1)$**
- ▶ **A single source of CP violation** in the weak interactions of quarks
- ▶ Three-generations unitarity: **CP violation from the measurement of CP conserving observables**

All these features, if experimentally confirmed, provide strong constraints on New Physics

CP physics \Leftrightarrow \overline{CP} physics



$$\overline{AB} = \frac{V_{td} V_{tb}^*}{V_{cd} V_{cb}^*}$$

$$\overline{BC} = 1$$

$$\overline{CA} = \frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*}$$

Triangle

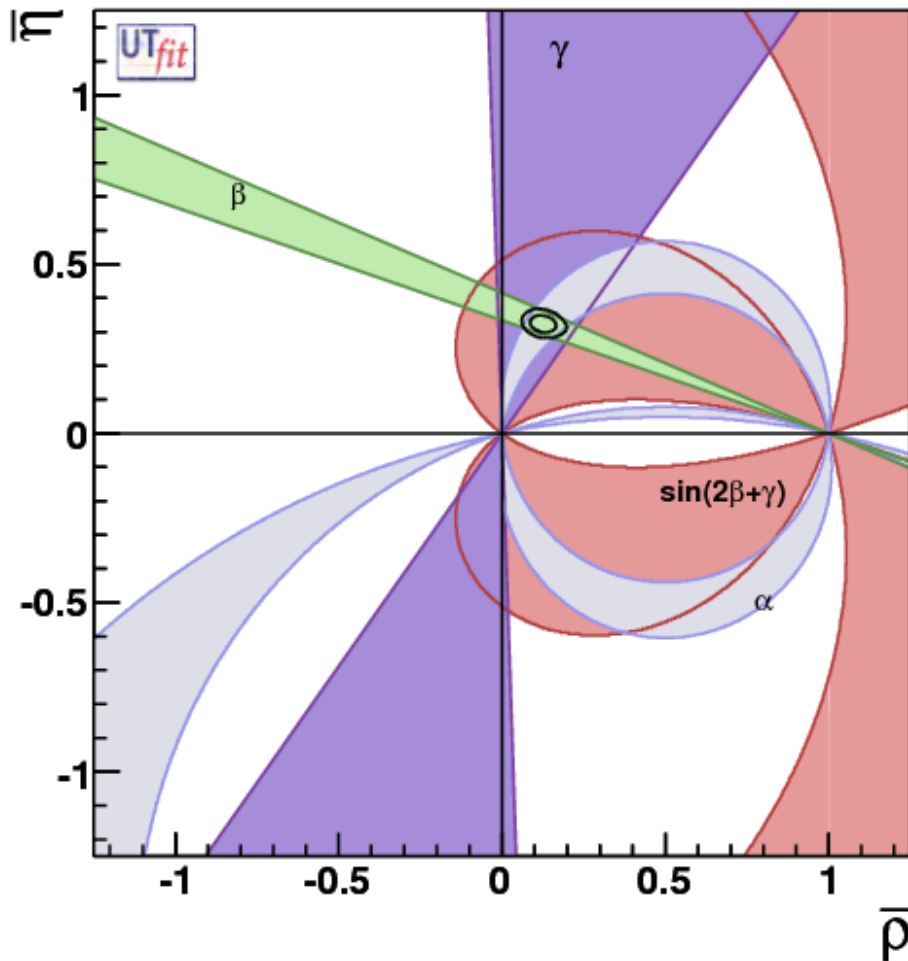
sides \leftrightarrow angles

$$|VV^*| \leftrightarrow \alpha, \beta, \gamma$$

$$\alpha \equiv \arg \left(-\frac{V_{td} V_{tb}^*}{V_{ud} V_{ub}^*} \right), \quad \beta \equiv \arg \left(-\frac{V_{cd} V_{cb}^*}{V_{td} V_{tb}^*} \right), \quad \gamma \equiv \arg \left(-\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*} \right)$$

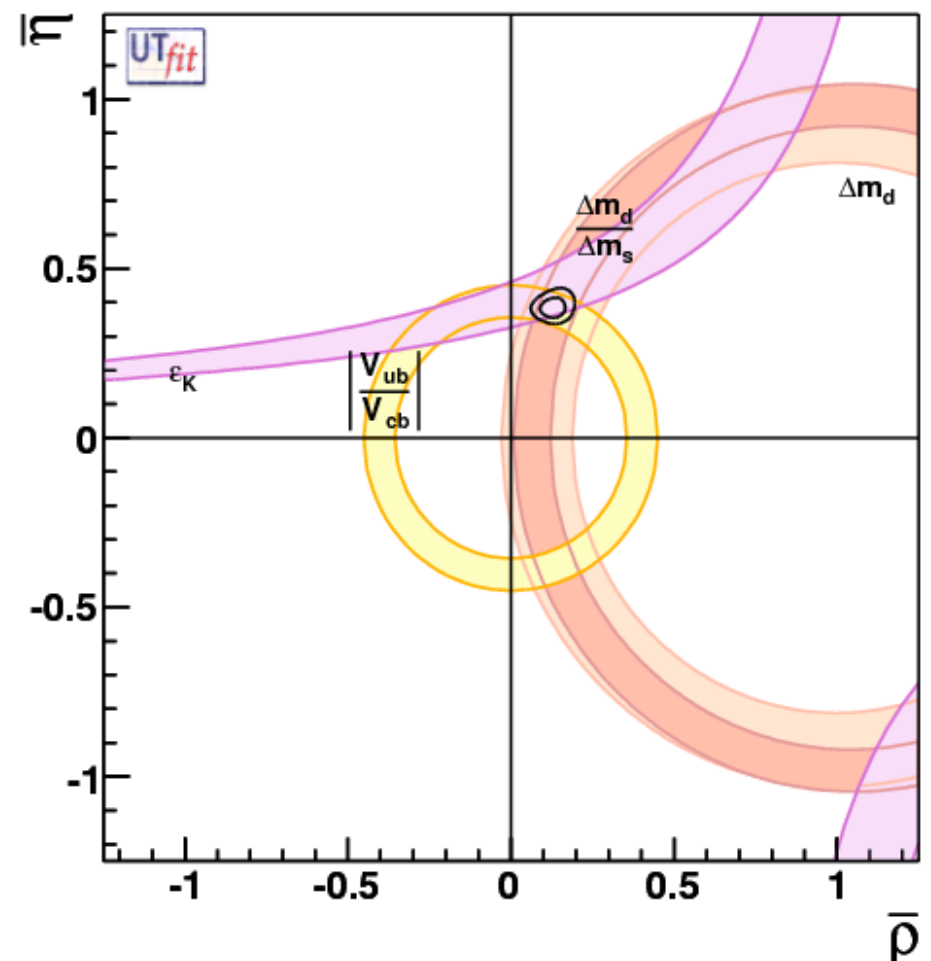
► CP violation \propto the Jarlskog invariant $J = \text{Im } V_{ij} V_{kl} V_{il}^* V_{kj}^*$

ANGLES vs NON-ANGLES



$$\bar{\rho} = 0.126 \pm 0.028$$

$$\bar{\eta} = 0.324 \pm 0.017$$



$$\bar{\rho} = 0.131 \pm 0.028$$

$$\bar{\eta} = 0.387 \pm 0.021$$

CPV IN KAON MIXING: ϵ_K

$$\epsilon_K = e^{i\phi_\epsilon} \sin \phi_\epsilon \left(\frac{\text{Im}(M_{12}^K)}{\Delta M_K} + \xi \right)$$

- Aim at reaching the % level for SM error

$$- M_{12}^K: C_6 \langle Q_6 \rangle + \sum_i C_8^i \langle Q_8^i \rangle + \dots$$

- C_6 : NNLO in progress, 3.3% enhancement from η_{ct}

Brod, Gorbahn '10

- $\langle Q_6 \rangle$: $B_K = 0.731 \pm 0.036$ UTfit average

- long-distance: estimate using Ch.p.t. Buras, Guadagnoli, Isidori '10

$$- \xi = \text{Im}A_0 / \text{Re}A_0:$$

- estimate using ϵ'/ϵ few percent decrease Buras, Guadagnoli '08

ϵ_K : SM vs experiment

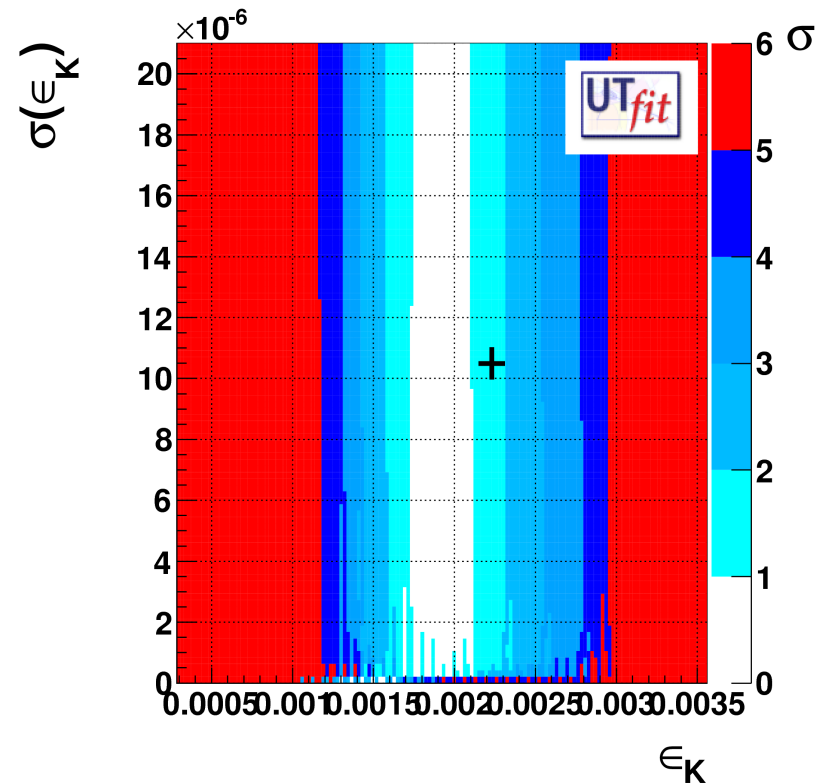
- SM prediction
(UTfit, does not
include NNLO η_{ct}):

$$(1.9 \pm 0.2) 10^{-3}$$

to be compared with

$$(2.23 \pm 0.01) 10^{-3}$$

agreement at 1.5σ



CPV in B_q mixing in the SM & beyond

B_q mixing is governed by:

- M_{12} , dominated by the exchange of virtual heavy states (top + NP) in loops
- Γ_{12} , dominated by real intermediate states \Rightarrow tree-level dominated

Assume that NP is a negligible correction to tree level processes

$$M_{12}^{\text{full}} = \langle B | H^{\text{eff}} | \bar{B} \rangle = M_{12}^{\text{SM}} + M_{12}^{\text{NP}} = C_{Bq} e^{2i\phi_{Bq}} M_{12}^{\text{SM}}$$

$$\Gamma_{12}^{\text{full}} \sim \Gamma_{12}^{\text{SM}} (+ \text{small effects due to penguins})$$

Notice that $\Gamma_{12}^{\text{SM}} / M_{12}^{\text{SM}} \sim \text{real}$ due to GIM

suppression, since

$$\Gamma_{12}^{\text{SM}} \propto (V_{tb} V_{tq}^*)^2 D^{\text{cc}} + \text{GIM-suppressed}$$

$$M_{12}^{\text{SM}} \propto (V_{tb} V_{tq}^*)^2$$

On the other hand,

$$\text{Arg}(M_{12}^{\text{SM}})_d = 2\beta \sim O(1)$$

$$\text{Arg}(M_{12}^{\text{SM}})_s = -2\beta_s \sim O(10^{-2})$$

What can we actually measure?

$$-\Delta m_{Bq} = 2 |M_{12}^{\text{full}}| = C_{Bq} \Delta m_{Bq}^{\text{SM}}$$

$$-\Delta \Gamma_q / \Delta m_{Bq} = \text{Re}(\Gamma_{12}^{\text{full}} / M_{12}^{\text{full}}) \sim$$

$$(\Delta \Gamma_q / \Delta m_{Bq})^{\text{SM}} \cos 2\phi_{Bq} / C_{Bq}$$

$$-A_{SL}^q = \text{Im}(\Gamma_{12}^{\text{full}} / M_{12}^{\text{full}}) \sim -(\Delta \Gamma_q / \Delta m_{Bq})^{\text{SM}} \times$$

$$\sin 2\phi_{Bq} / C_{Bq} = -\Delta \Gamma_q / \Delta m_{Bq} \tan 2\phi_{Bq}$$

$$-S_{J/\Psi K} \sim \sin 2(\beta + \phi_{Bd}), S_{J/\Psi \phi} \sim \sin 2(-\beta_s + \phi_{Bs})$$

- Use tree-level processes to determine the CKM matrix and thus disentangle NP from SM contributions to meson mixing:

$|V_{ub}|$ and $|V_{cb}|$ from inclusive and exclusive semileptonic B decays

γ from $B \rightarrow DK$ and α from $B \rightarrow \pi\pi, \rho\pi, \rho\rho$ decays

A FEW REMARKS

- The values of C_ε , ϕ_{B_d} and ϕ_{B_s} extracted from the analysis potentially contain a mixture of $\Delta F=1$ & $\Delta F=2$ NP contributions. Disentangling them is a difficult task.

- For the B_s analysis, we use an improved theoretical prediction for $\Delta\Gamma$:

$$\Delta\Gamma_s/\Gamma_s = 0.14 \pm 0.02$$

Ciuchini et al., in preparation;
see also Lenz & Nierste

and allow for NP penguin effects in Γ_{12}

Results for NP parameters:

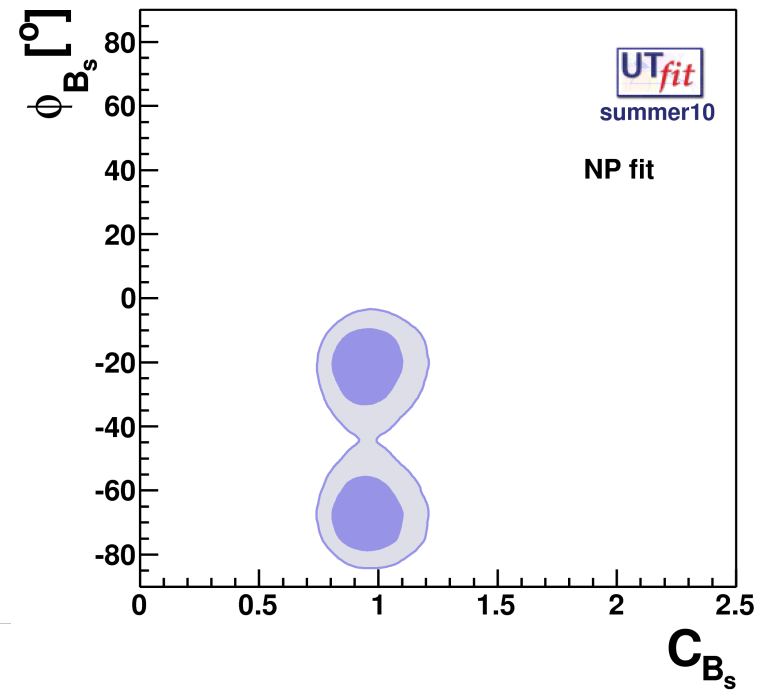
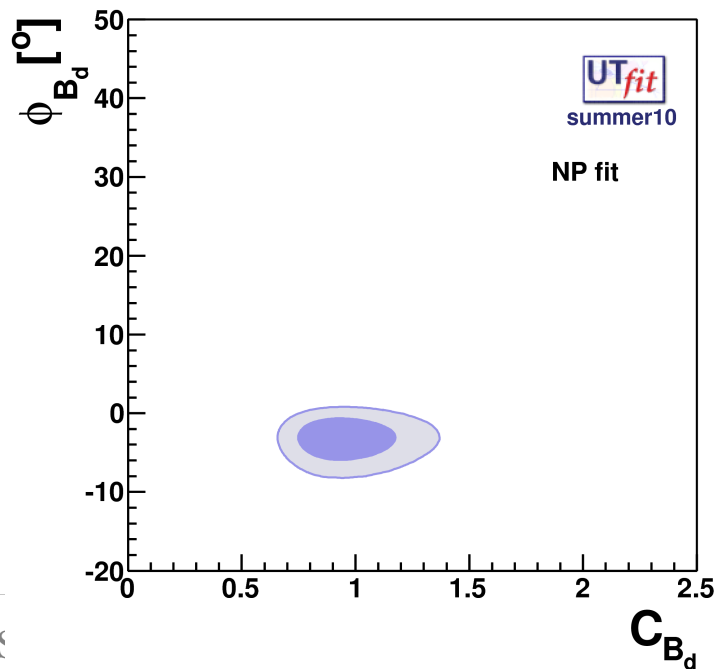
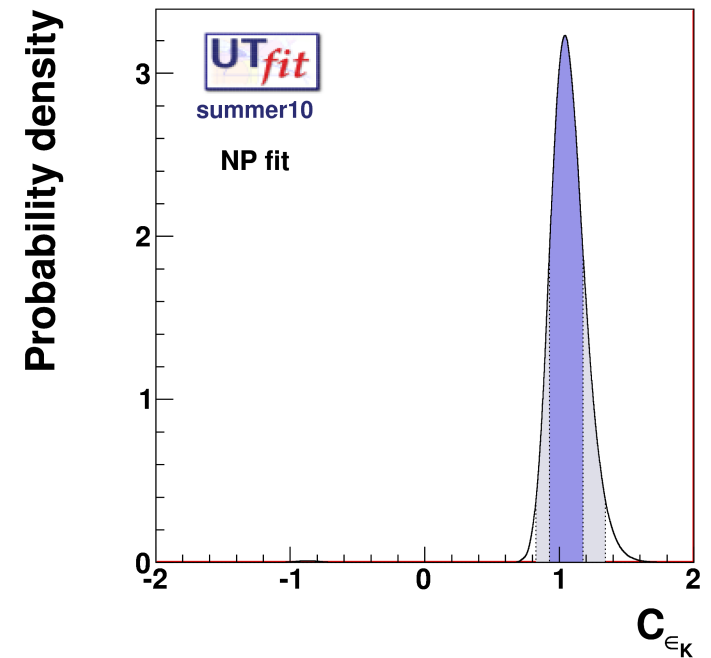
$$C_{\epsilon K} = 1.05 \pm 0.12 [0.82, 1.34]$$

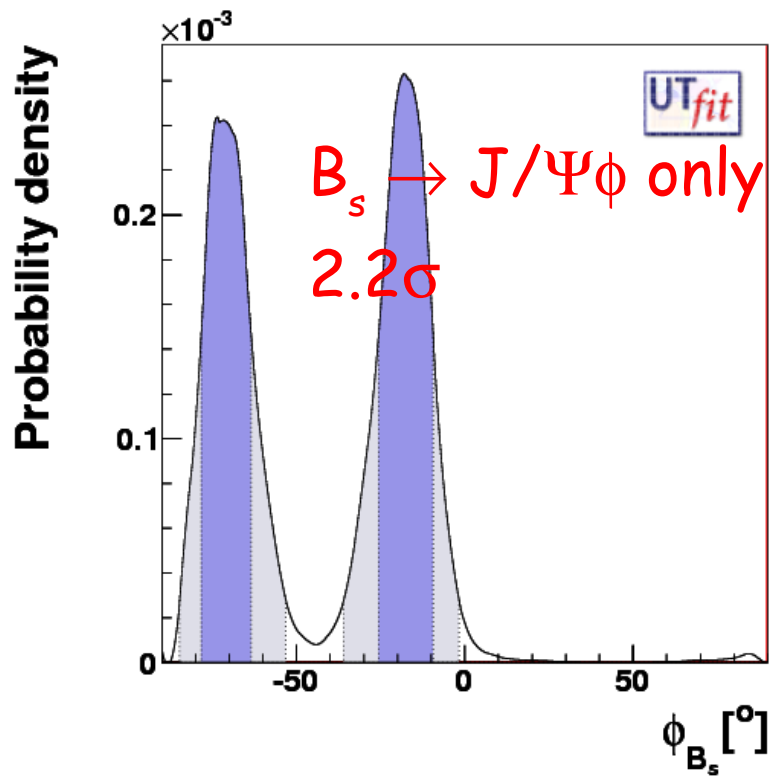
$$C_{B_d} = 0.95 \pm 0.14 [0.70, 1.27]$$

$$\phi_{B_d} = (-3.1 \pm 1.7)^\circ [-7.0, 0.1]^\circ$$

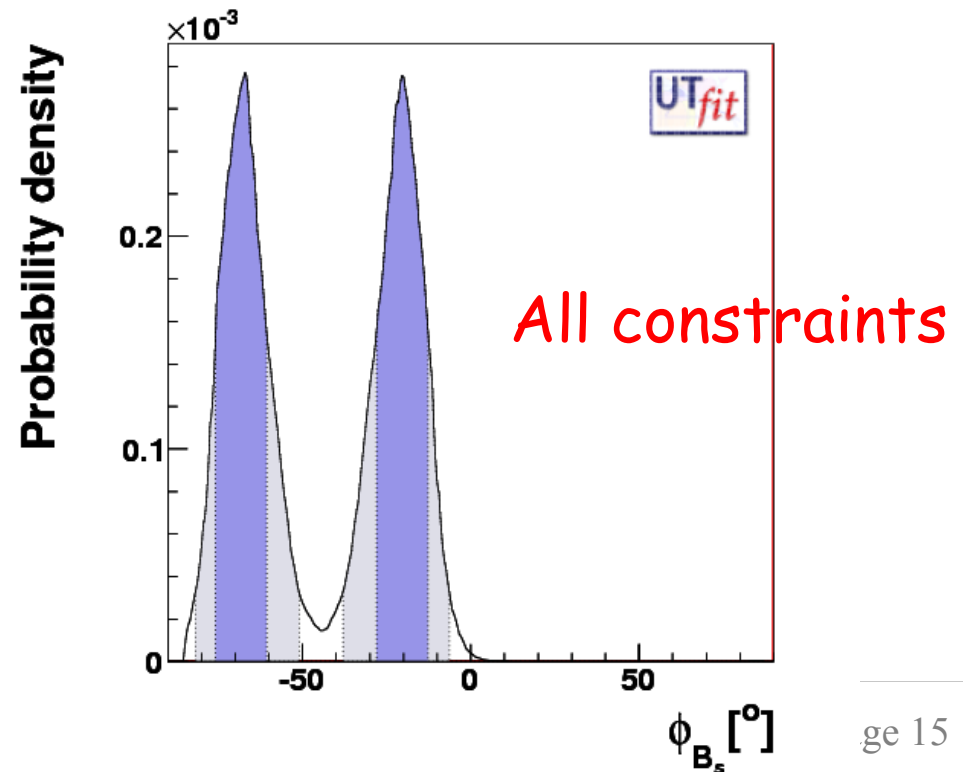
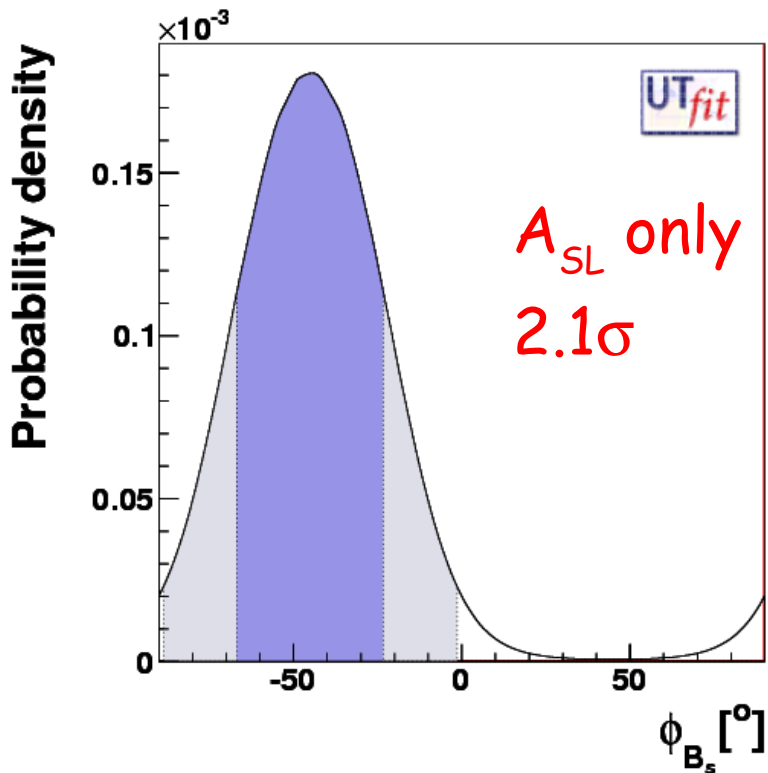
$$C_{B_s} = 0.95 \pm 0.10 [0.77, 1.16]$$

$$\phi_{B_s} = (-20 \pm 8)^\circ \cup (-68 \pm 8)^\circ [-38, -6]^\circ \cup [-81, -51]^\circ$$





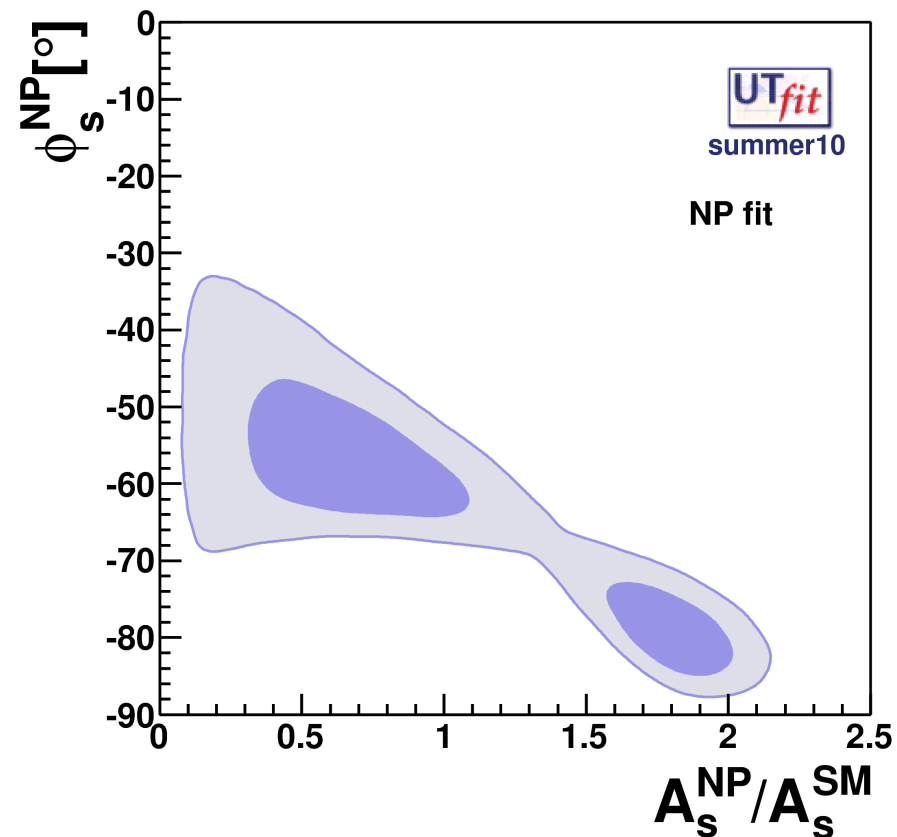
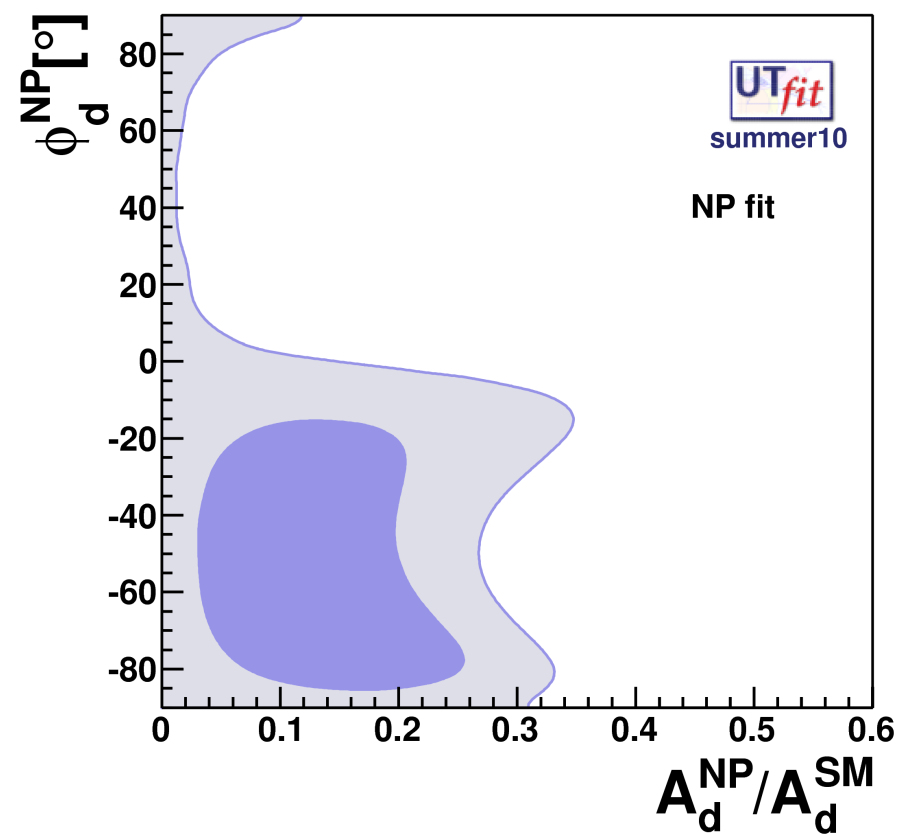
We use the combined Tevatron likelihood which does not include the new CDF result, and the recent $A_{\mu\mu}$. Using all data we are at 3.2 σ .



SEMILEPTONIC ASYMMETRIES

Asymmetry	Input	Prediction	Fit
$A_{SL}^d 10^3$	(-0.5 ± 5.6)	(-0.9 ± 2.7)	(-2.8 ± 2.4)
$A_{SL}^s 10^3$	(-1.7 ± 9.1)	(-3.7 ± 1.5)	(-4.4 ± 1.4)
$A_{\mu\mu} 10^3$	(-9.6 ± 2.9)	(-2.3 ± 1.7)	(-3.7 ± 1.4)

The D0 result on $A_{\mu\mu}$ cannot be reproduced given our theoretical prediction for Γ_{12} in the SM and the assumption of no tree-level NP



Ratio of NP/SM contributions is $< 35\%$ @ 95% prob.
in B_d mixing, and $\sim 70\%$ in B_s mixing (but 2σ range is very large)

See also Lenz & Nierste, Lunghi & Soni, Buras & Guadagnoli, Faller et al, Lenz et al, ...

- Large NP contributions to $b \leftrightarrow s$ transitions are natural in nonabelian flavour models, given the large breaking of flavour $SU(3)$ due to the top quark mass

Pomarol, Tommasini; Barbieri, Dvali, Hall; Barbieri, Hall; Barbieri, Hall, Romanino; Berezhiani, Rossi; Masiero et al; ...

- GUTs can naturally connect the large mixing in ν oscillations with a large $b \leftrightarrow s$ mixing

Baek et al.; Moroi; Akama et al.; Chang, Masiero, Murayama; Hisano, Shimizu; Goto et al.; ...

- Might show up also in $\Delta F=1$ transitions ($b \rightarrow s\gamma$, $b \rightarrow sl^+l^-$, $B \rightarrow K\pi$, $B_s \rightarrow K^{*0}K^{*0}$, ...) and/or LFV ($\tau \rightarrow \mu\gamma$, $\mu \rightarrow e\gamma$)

EFT analysis of $\Delta F=2$ transitions

The mixing amplitudes $A_q e^{2i\phi_q} = \left\langle \bar{M}_q \left| H_{eff}^{\Delta F=2} \right| M_q \right\rangle$

$$H_{eff}^{\Delta B=2} = \sum_{i=1}^5 C_i(\mu) Q_i(\mu) + \sum_{i=1}^3 \tilde{C}_i(\mu) \tilde{Q}_i(\mu)$$

$$Q_1 = \bar{q}_L^\alpha \gamma_\mu b_L^\alpha \bar{q}_L^\beta \gamma^\mu b_L^\beta \quad (\text{SM/MFV})$$

$$Q_2 = \bar{q}_R^\alpha b_L^\alpha \bar{q}_R^\beta b_L^\beta$$

$$Q_3 = \bar{q}_R^\alpha b_L^\beta \bar{q}_R^\beta b_L^\beta$$

$$Q_4 = \bar{q}_R^\alpha b_L^\alpha \bar{q}_L^\beta b_R^\beta$$

$$Q_5 = \bar{q}_R^\alpha b_L^\beta \bar{q}_L^\beta b_R^\beta$$

$$\tilde{Q}_1 = \bar{q}_R^\alpha \gamma_\mu b_R^\alpha \bar{q}_R^\beta \gamma^\mu b_R^\beta$$

$$\tilde{Q}_2 = \bar{q}_L^\alpha b_R^\alpha \bar{q}_L^\beta b_R^\beta$$

$$\tilde{Q}_3 = \bar{q}_L^\alpha b_R^\beta \bar{q}_L^\beta b_R^\beta$$

7 new operators beyond MFV involving quarks with different chiralities

H_{eff} can be recast in terms of the $C_i(\Lambda)$ computed at the NP scale

- $C_i(\Lambda)$ can be extracted from the data (one by one)
- the associated NP scale Λ can be defined from

$$C_i(\Lambda) = \frac{LF_i}{\Lambda^2}$$

tree/strong interact. NP: $L \sim 1$
perturbative NP: $L \sim a_s^2, a_w^2$

Flavour structures:

MFV

- $F_1 = F_{SM} \sim (V_{tq} V_{tb}^*)^2$
- $F_{i \neq 1} = 0$

next-to-MFV

- $|F_i| \sim F_{SM}$
- arbitrary
phases

generic

- $|F_i| \sim 1$
- arbitrary
phases

present lower bound on the NP scale (TeV):

Process	C_4 (GeV ⁻²)	Λ_{GEN} (TeV)	Λ_{NMFV} (TeV)
ε_K	$4.6 \cdot 10^{-18}$	$47 \cdot 10^4$	107
B_d	$9.3 \cdot 10^{-14}$	$3.3 \cdot 10^3$	7
B_s	$1.5 \cdot 10^{-11}$	$2.6 \cdot 10^2$	8

* $\Delta F=2$ chirality-flipping operators are RG enhanced and thus probe larger NP scales

* suppression of the $1 \leftrightarrow 2$ transitions strongly weakens the lower bounds

Bounds on Λ_{MFV} from $\Delta F=2$ processes: for low $\tan\beta$

$$F_{\text{tt}} \in [-0.326, 0.487] \rightarrow \Lambda_{\text{MFV}} > 8.4 \text{ (6.9) TeV}$$

CPV in nonleptonic decays

- ε'/ε : $\Delta I=1/2$ rule indicates large (huge) nonperturbative effects in (penguin) matrix elements
- The computation of $K \rightarrow (\pi\pi)_{I=2}$ amplitudes is progressing well, with the preliminary result for $\text{Re } A_2$ in good agreement with the physical value.
 - Normalized $\text{Im } A_2$ available soon.
 - This will become a benchmark computation which will be improved in the coming years (finer lattices?).
- The exploratory results for $K \rightarrow (\pi\pi)_{I=0}$ decays encourage us to proceed to physical kinematics.

\Rightarrow an understanding of the $\Delta I = 1/2$ rule and the value of ε'/ε .

C. Sachrajda 2010

CP ASYMMETRIES IN $B \rightarrow K\pi$

$$\mathcal{A}_{K^\pm \pi^\mp} \equiv \frac{N(\bar{B}^0 \rightarrow K^- \pi^+) - N(B^0 \rightarrow K^+ \pi^-)}{N(\bar{B}^0 \rightarrow K^- \pi^+) + N(B^0 \rightarrow K^+ \pi^-)} = -0.094 \pm 0.018 \pm 0.008$$

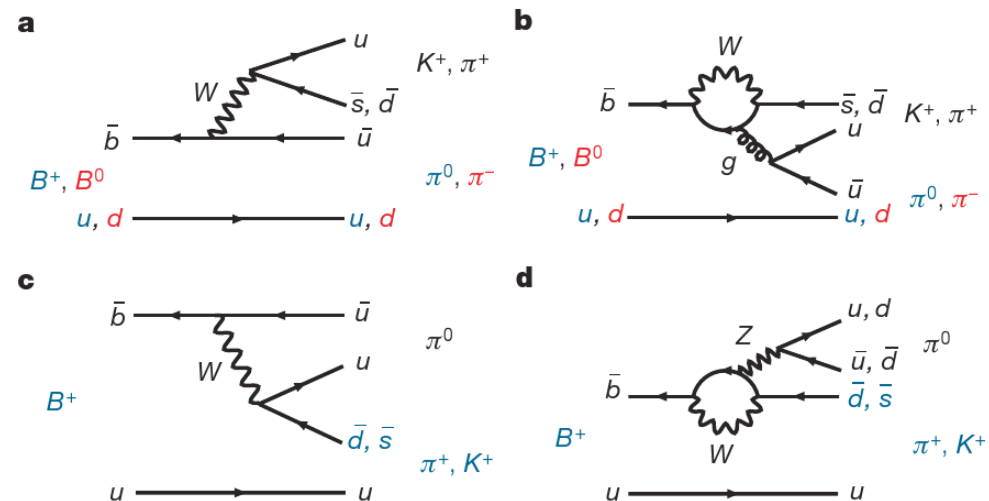
Belle collaboration
Nature 452,2008

$$\mathcal{A}_{K^\pm \pi^0} = +0.07 \pm 0.03 \pm 0.01$$

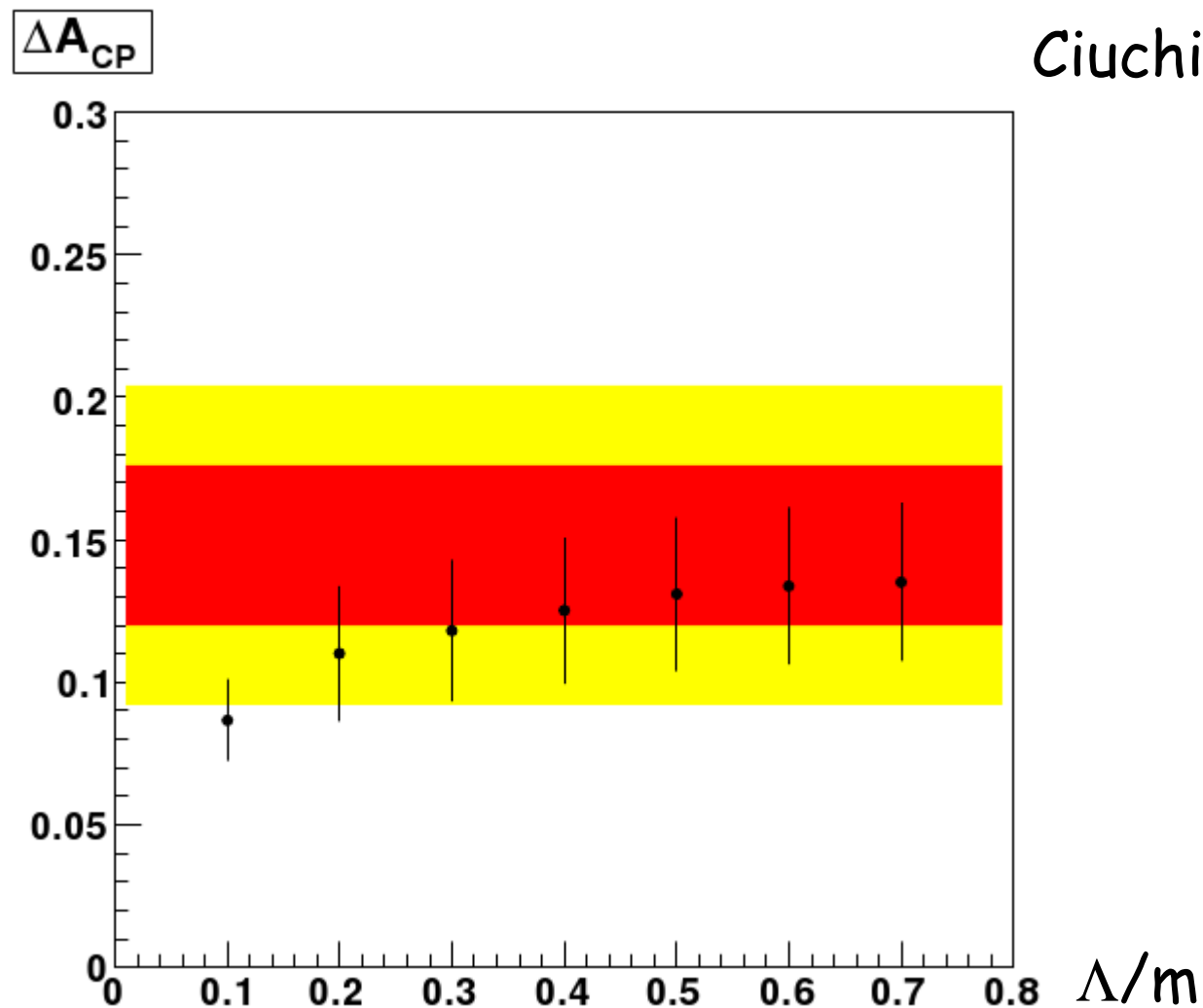
$$\Delta\mathcal{A} \equiv \mathcal{A}_{K^\pm \pi^0} - \mathcal{A}_{K^\pm \pi^\mp} = +0.164 \pm 0.037$$

Is this new physics?

It could be but SM predictions depend on hadronic models



- Factorization in its various incarnations (QCDF, PQCD, SCET) gives results valid in the $m_b \rightarrow \infty$ limit
- Corrections to this limit are $O(\Lambda/m_b)$, but not calculable
- How much do the th predictions depend on power corrections?



A good fit can be obtained either for $\Delta/m \sim 0.3$ or for NP in $b \rightarrow sZ$ vertex. Inconclusive at present.

See also Buraisamy & Kagan 08, Li & Mishima 09

CONCLUSIONS

- CP Violation is an extremely powerful test of the SM and probe of New Physics
- We are reaching the 5% th uncertainty on meson-antimeson mixing
- ε_K and B_d mixing give strong constraints on NP contributions, naively pushing the NP scale of several models far beyond the LHC reach

CONCLUSIONS

- CPV in B_s mixing off from SM at $\sim 3\sigma$
- Requires new sources of flavour & CPV, natural in many extensions of the SM
- Wait for confirmation from Tevatron/LHCb, look for other NP signals in $b \rightarrow s$ transitions
- Progress in CPV in nonleptonic decays slow and painful, but we won't give up...

BACKUP SLIDES

FIT PREDICTIONS vs INPUTS

	Prediction	Measurement	Pull (σ)
$\sin 2\beta$	0.771 ± 0.036	0.654 ± 0.026	2.6
α	$(85 \pm 4)^\circ$	$(91 \pm 6)^\circ$	<1
γ	$(70 \pm 3)^\circ$	$(74 \pm 11)^\circ$	<1
Δm_s	$(18.3 \pm 1.3) \text{ps}^{-1}$	$(17.77 \pm 0.12) \text{ps}^{-1}$	<1
$ V_{ub} $	$(35.5 \pm 1.4) 10^{-4}$	$(37.6 \pm 2.0) 10^{-4}$	<1
ϵ_K	$(1.9 \pm 0.2) 10^{-3}$	$(2.23 \pm 0.01) 10^{-3}$	1.5
$\text{BR}(B \rightarrow \tau \nu)$	$(81 \pm 7) 10^{-6}$	$(172 \pm 28) 10^{-6}$	3.2

RESULTS OF GENERALIZED UTA

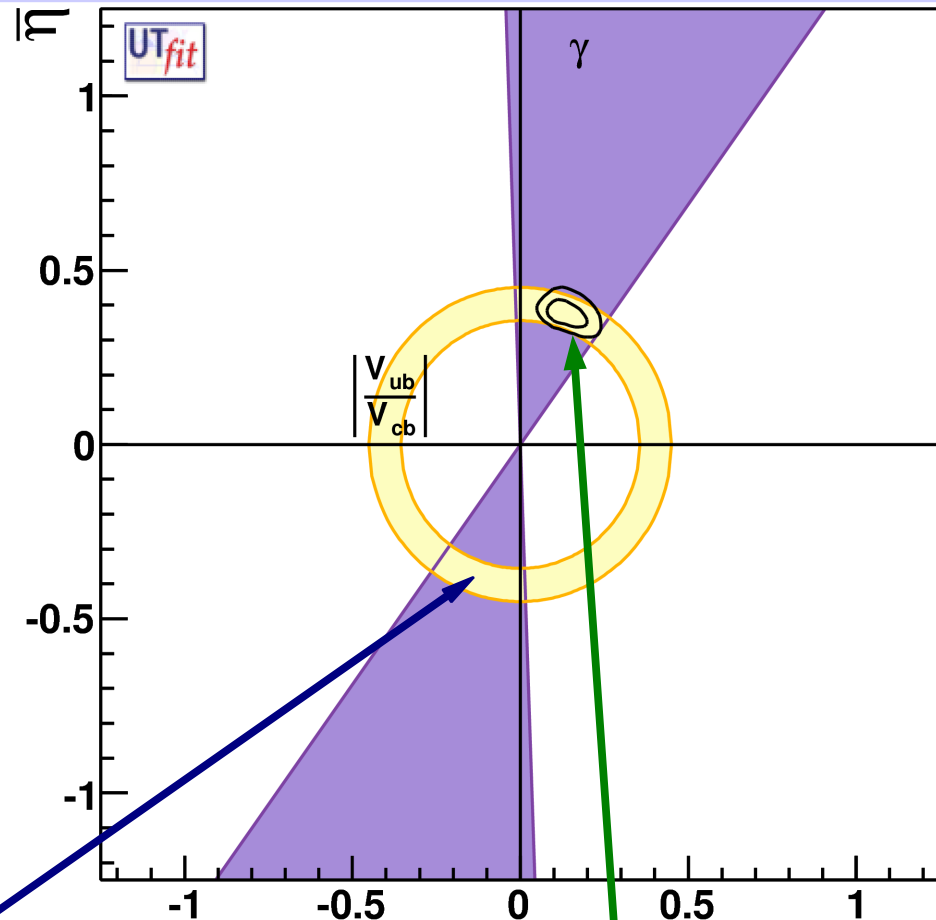
$$\bar{\rho} = 0.135 \pm 0.040$$

$$\bar{\eta} = 0.374 \pm 0.026$$

in the SM was:

$$\rho = 0.132 \pm 0.020$$

$$\eta = 0.358 \pm 0.012$$



degeneracy of γ broken by A_{SL} (assuming no huge NP effects in Γ_{12})

Accuracy improved by α (assuming no huge NP contribution to EWP)