

# IceCube constraints on Violation of Equivalence Principle

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XIX International Workshop on Neutrino Telescopes

based on D. Fiorillo, G. Mangano, S. Morisi, O. Pisanti, arXiv:2012.07867



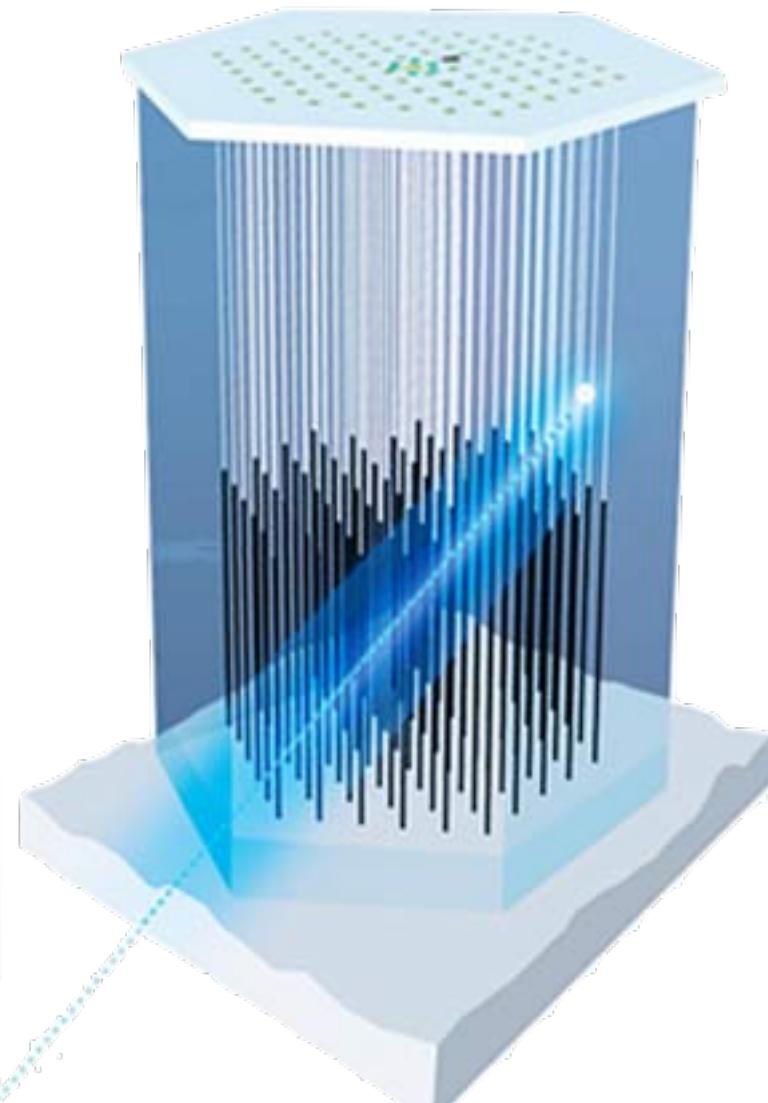
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# Violation of Equivalence Principle (VEP)

General Relativity

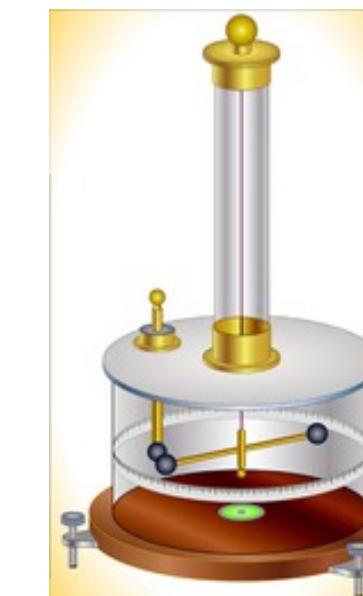


**Equivalence Principle**  
All particles couple  
equally to the  
gravitational field



**IceCube** can  
constrain at the  
level of  $10^{-22}$

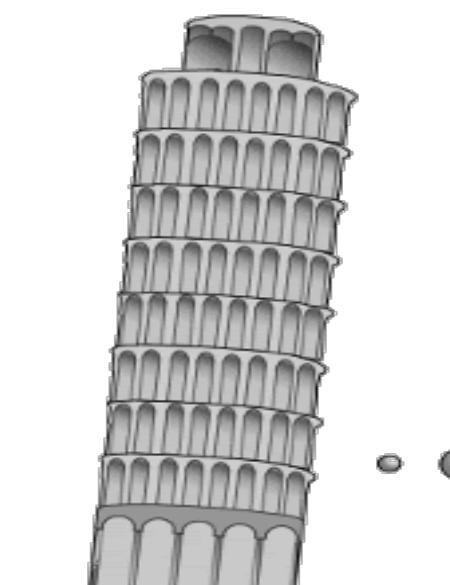
Testing the Equivalence Principle  
can guide toward complete theory



Lab experiments

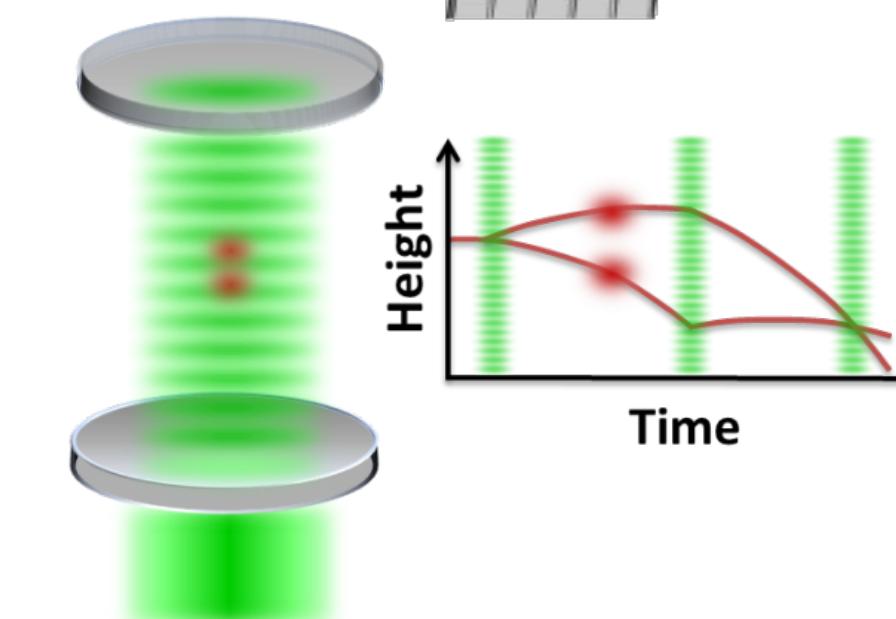
$\delta G/G$

$10^{-13} - 10^{-14}$



Free fall

$10^{-10} - 10^{-15}$



Atom  
interferometry

$10^{-9} - 10^{-15}$

# VEP and high energy neutrinos

Why does VEP influence neutrinos?

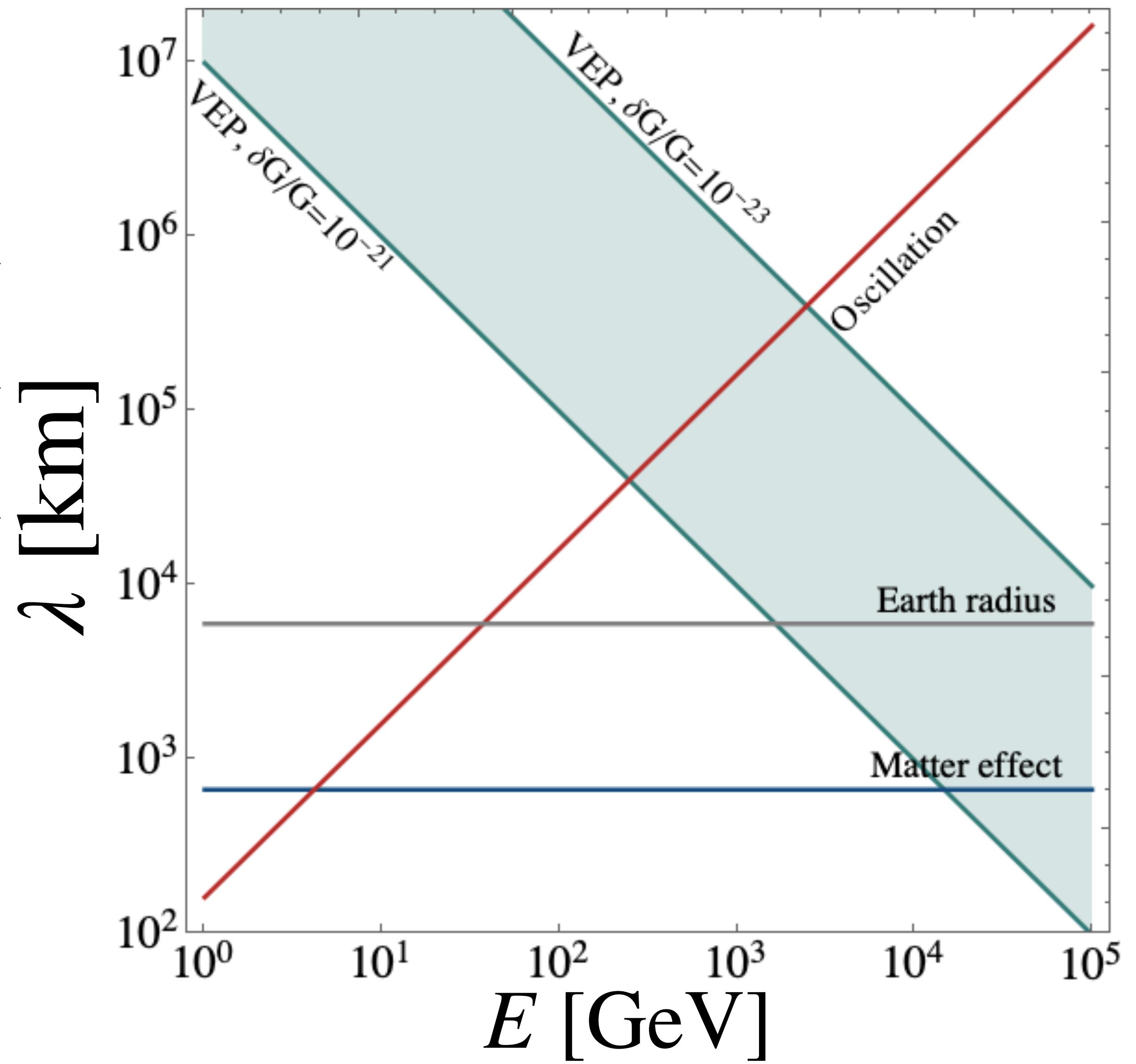
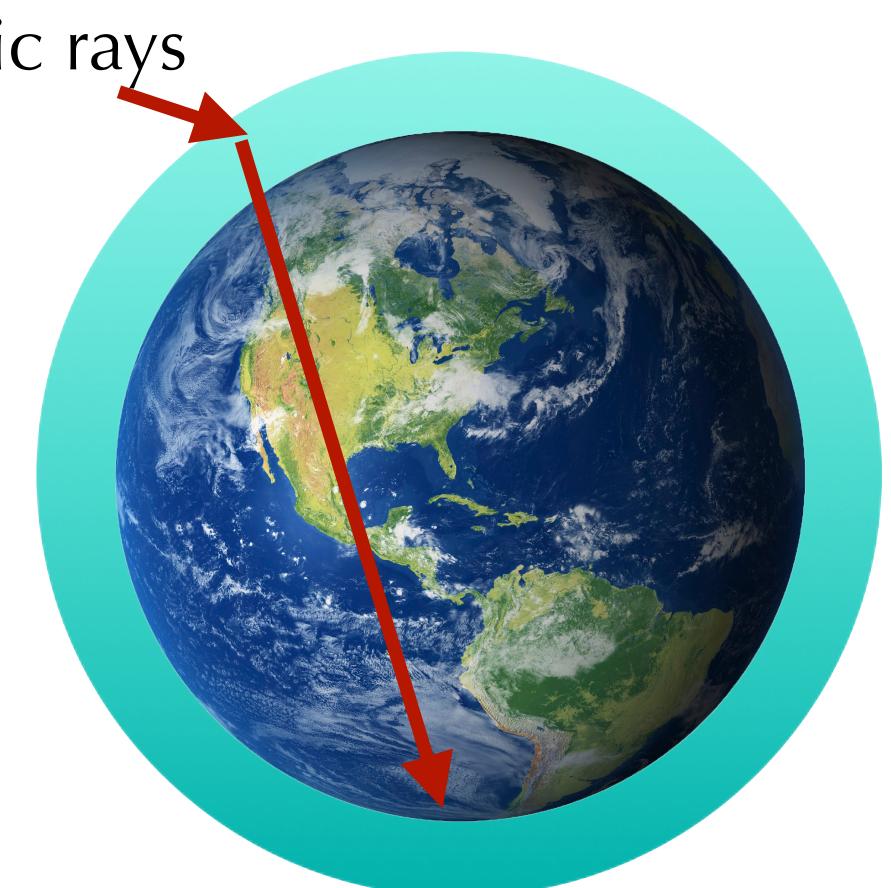
$$\nu \rightarrow \left\{ \begin{array}{l} \frac{\nu_1}{\nu_2} \rightarrow G'_1 = \gamma_1 G \\ \frac{\nu_2}{\nu_3} \rightarrow G'_2 = \gamma_2 G \\ \frac{}{} \quad \quad \quad G'_3 = \gamma_3 G \end{array} \right.$$

Dephasing leads to oscillations

$E \gtrsim 1 \text{ TeV}$

Atmospheric neutrinos

Gonzalez-Garcia et al., 2004;  
Battistoni et al., 2005; Abbasi et  
al., 2009; Esmaili et al., 2014



# VEP-induced oscillations

$$i \frac{d\nu}{dl} = \left( \frac{UM^2U^\dagger}{2p} + V + 2\phi p \tilde{U} \Gamma \tilde{U}^\dagger \right) \nu$$

Flavor basis  
Mass term  
Matter term  
VEP term

$U$  PMNS matrix

$p$  neutrino momentum

$\phi$  gravitational potential (in natural units)

# VEP-induced oscillations

$$i \frac{d\nu}{dl} = \left( \frac{UM^2U^\dagger}{2p} + V + 2\phi p \tilde{U} \Gamma \tilde{U}^\dagger \right) \nu$$

Flavor basis  
Mass term  
Matter term  
VEP term

$$\Gamma = \begin{pmatrix} \gamma_1 & 0 & 0 \\ 0 & \gamma_2 & 0 \\ 0 & 0 & \gamma_3 \end{pmatrix}$$

Only differences can cause physical effects

$$\Gamma = \begin{pmatrix} 0 & 0 & 0 \\ 0 & \gamma_{21} & 0 \\ 0 & 0 & \gamma_{31} \end{pmatrix}$$

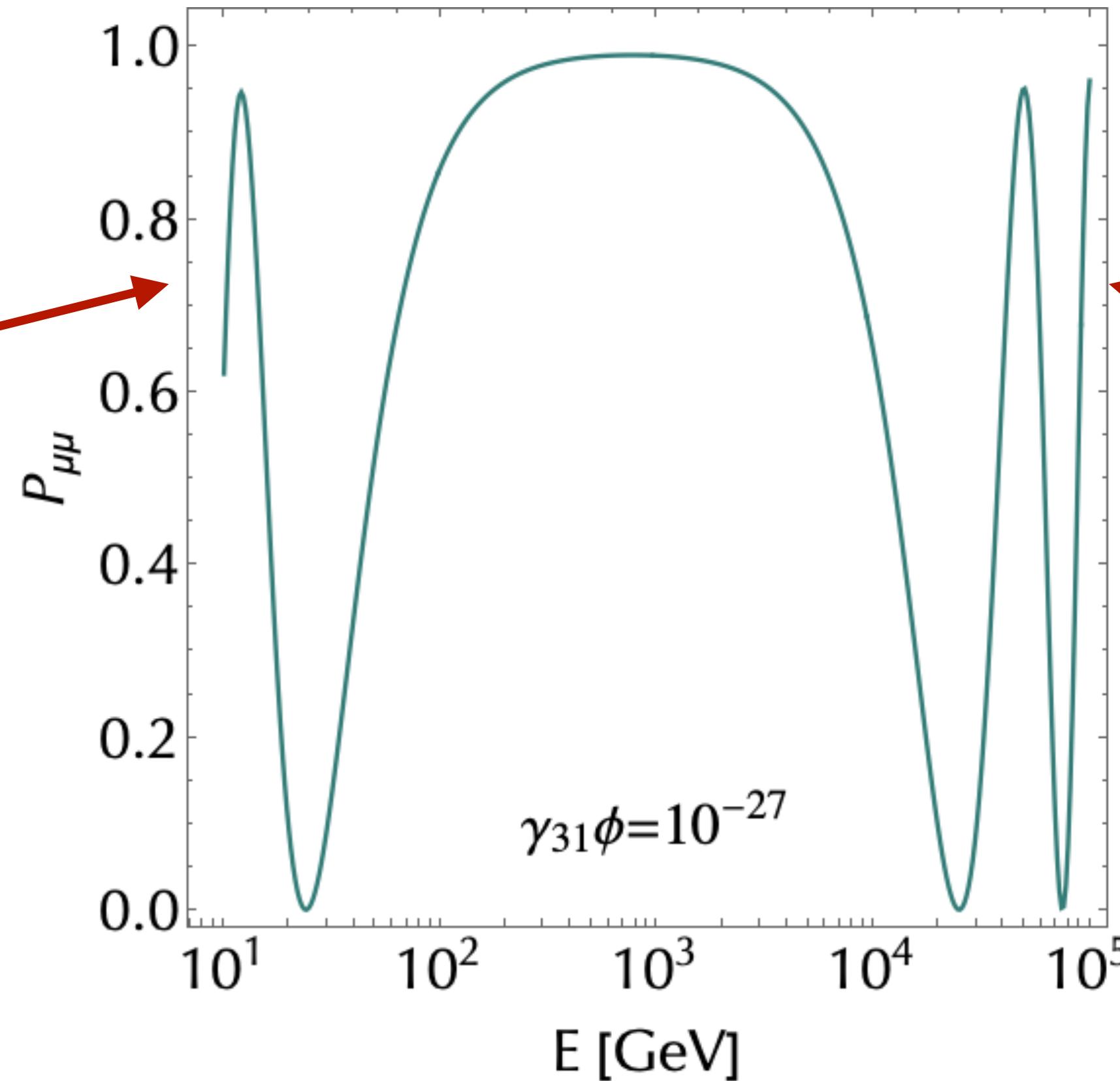
Simple **benchmark** choice: gravity couples (diagonally) to mass eigenstates

$$U = \tilde{U}$$

# VEP-induced oscillations

$$i \frac{d\nu}{dl} = \left( \frac{UM^2U^\dagger}{2p} + V + 2\phi p \tilde{U} \Gamma \tilde{U}^\dagger \right) \nu$$

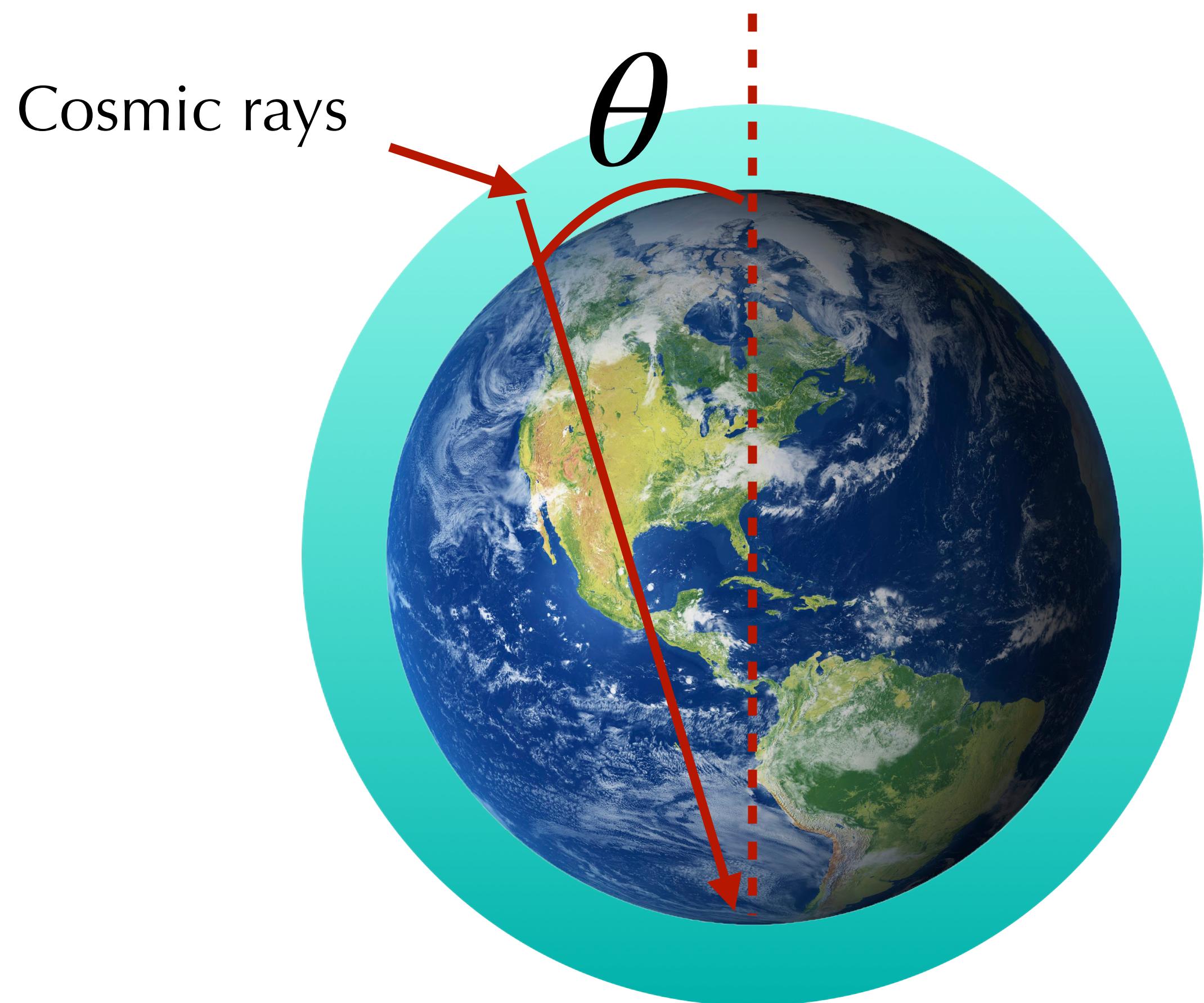
Conventional  
oscillations



VEP-dominated  
oscillations

# VEP and atmospheric neutrinos

Model of atmospheric fluxes from Honda et al., 2006



Gravitational potential dominated  
by Great Attractor

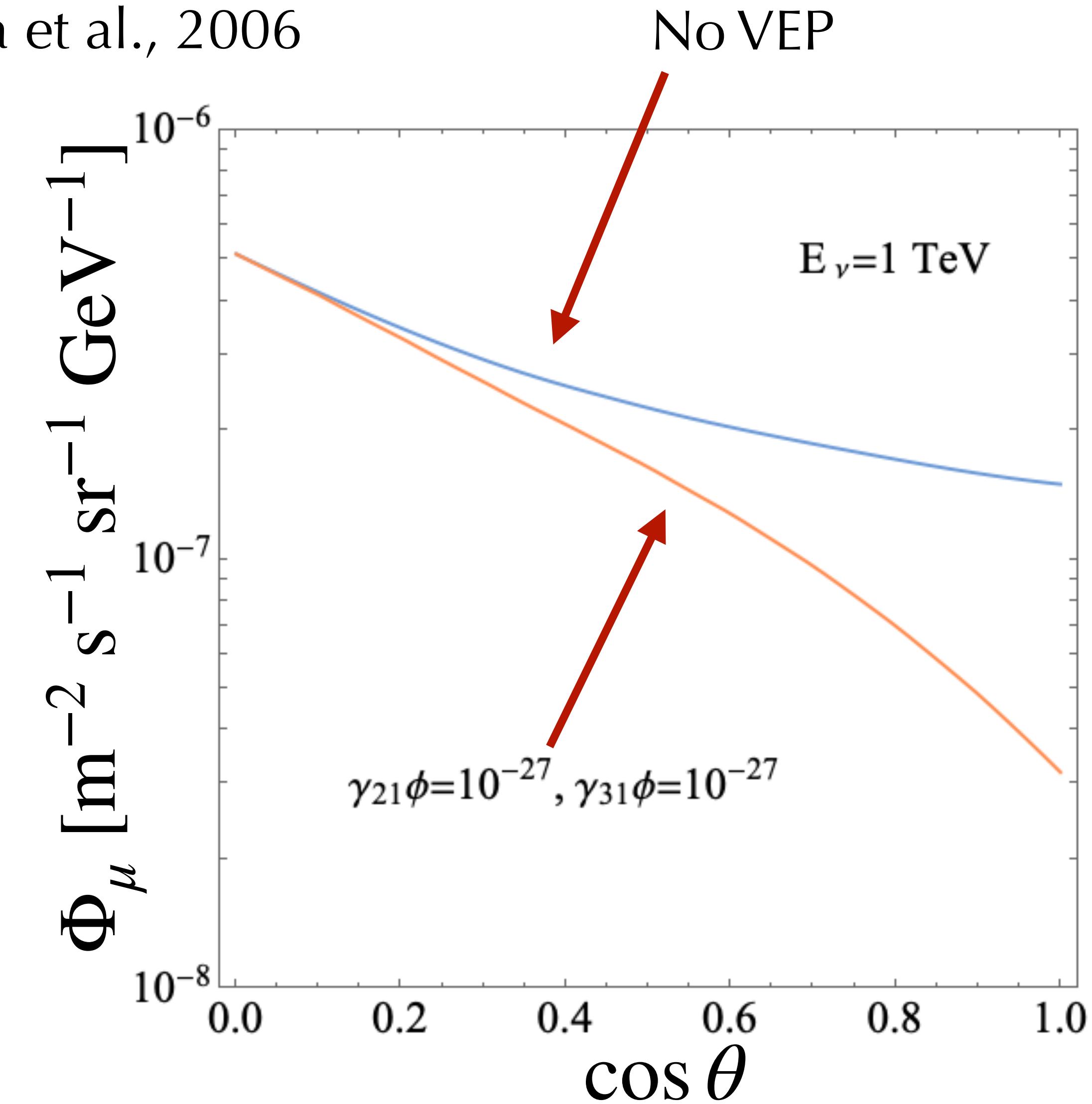
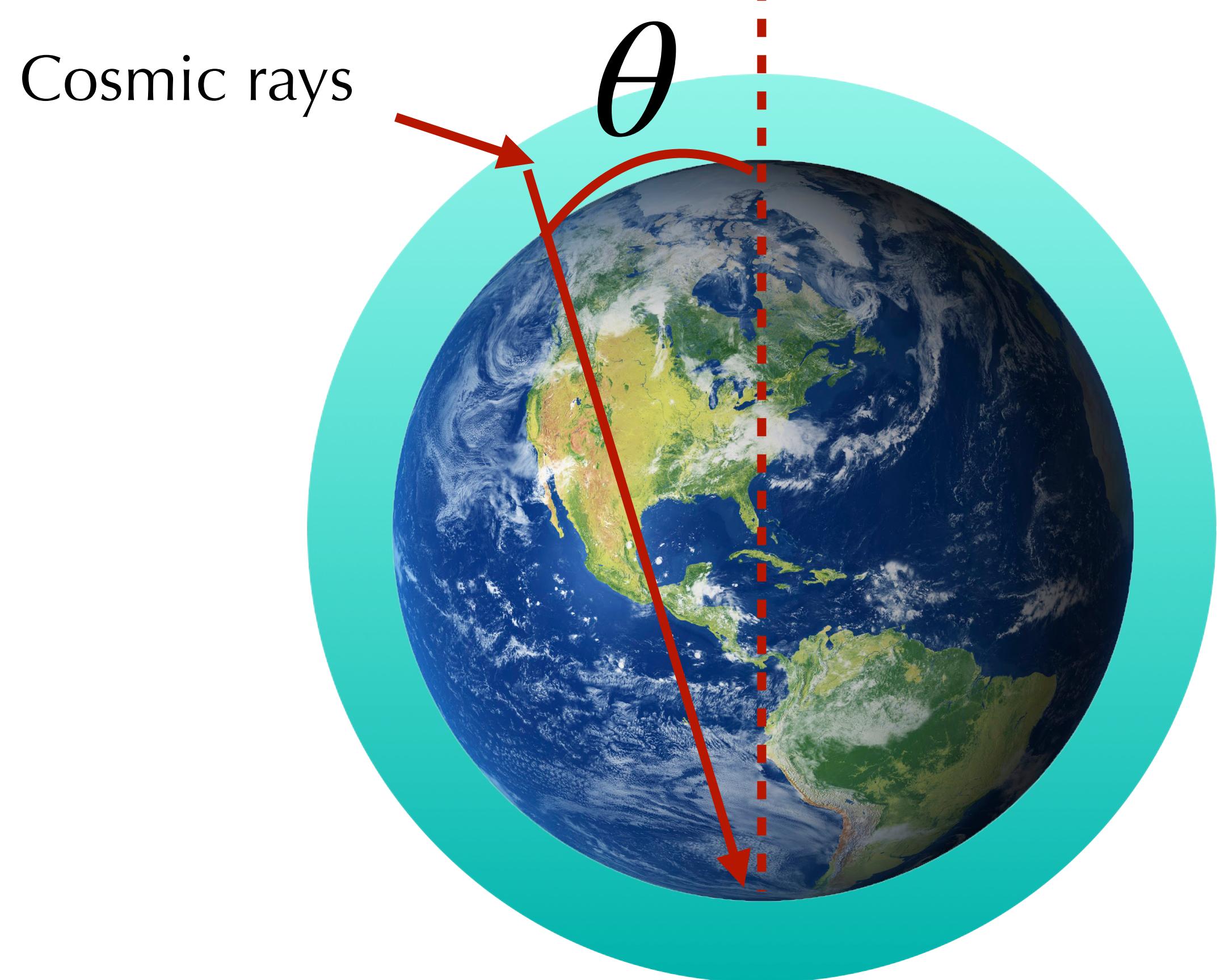
$$\phi \sim 10^{-5}$$

Earth gravitational potential negligible  
( $\phi \sim 10^{-9}$ )

$$\frac{\delta G}{G} \sim 10^{-22} \longrightarrow \gamma\phi \sim 10^{-27}$$

# VEP and atmospheric neutrinos

Model of atmospheric fluxes from Honda et al., 2006



# VEP and atmospheric neutrinos

Model of atmospheric fluxes from Honda et al., 2006

Analysis on IC40 and IC79

Esmaili et al., 2014

Analysis on through-going muons

Aartsen et al., 2017

IC79

IC86-11

IC86-12/18

Aartsen et al., 2017

Aartsen et al., 2020

$$\chi^2(\gamma_{21}\phi, \gamma_{31}\phi, \alpha, \beta) =$$

$$\sum_i \frac{[N_i^{\text{data}} - \alpha(1 + \beta(0.5 + \cos \theta))N_i^{\text{th}}]^2}{\sigma_{i,\text{stat}}^2 + \sigma_{i,\text{sys}}^2} +$$

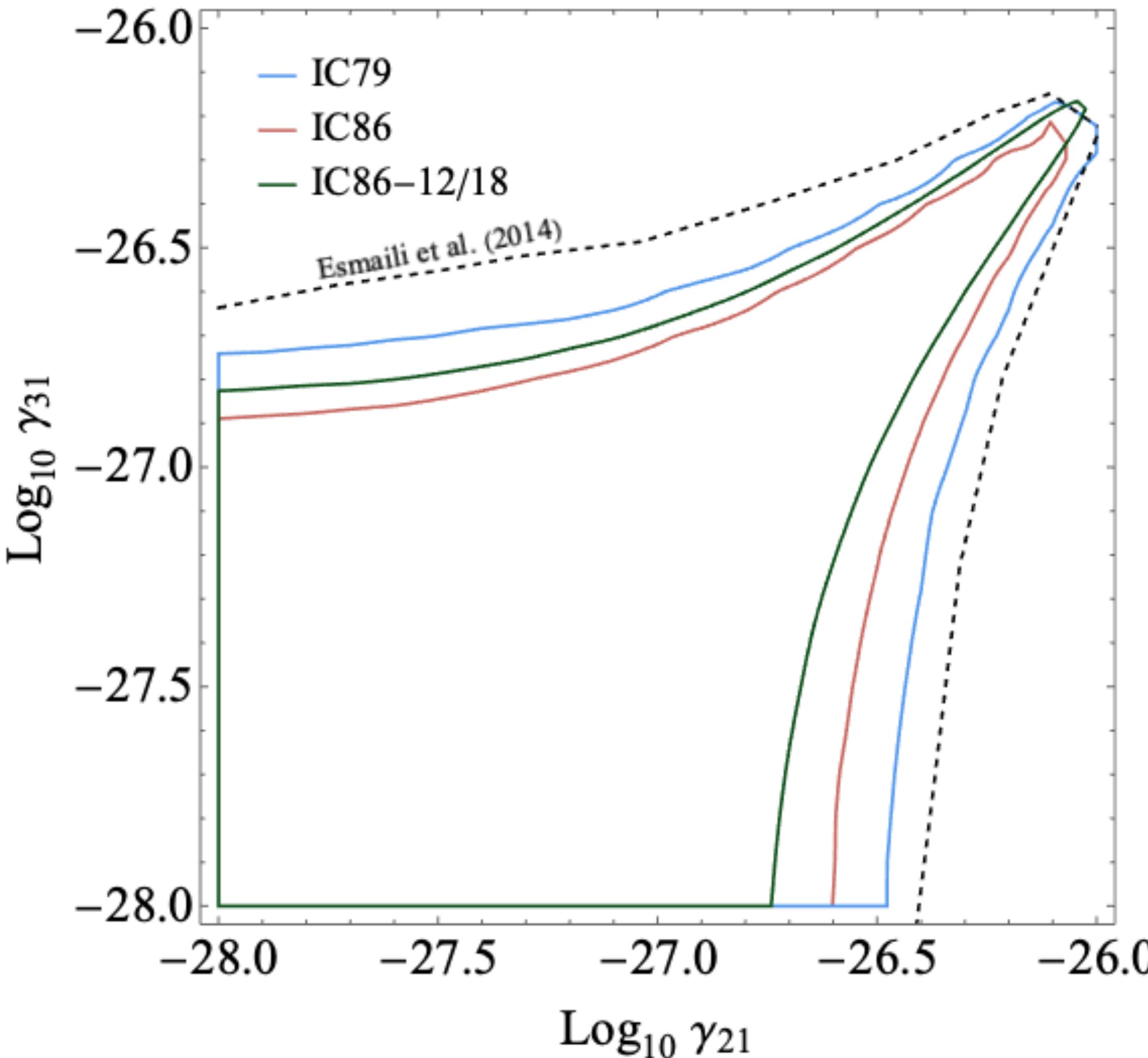
$$\frac{(1 - \alpha)^2}{\sigma_\alpha^2} + \frac{\beta^2}{\sigma_\beta^2}$$

Normalization

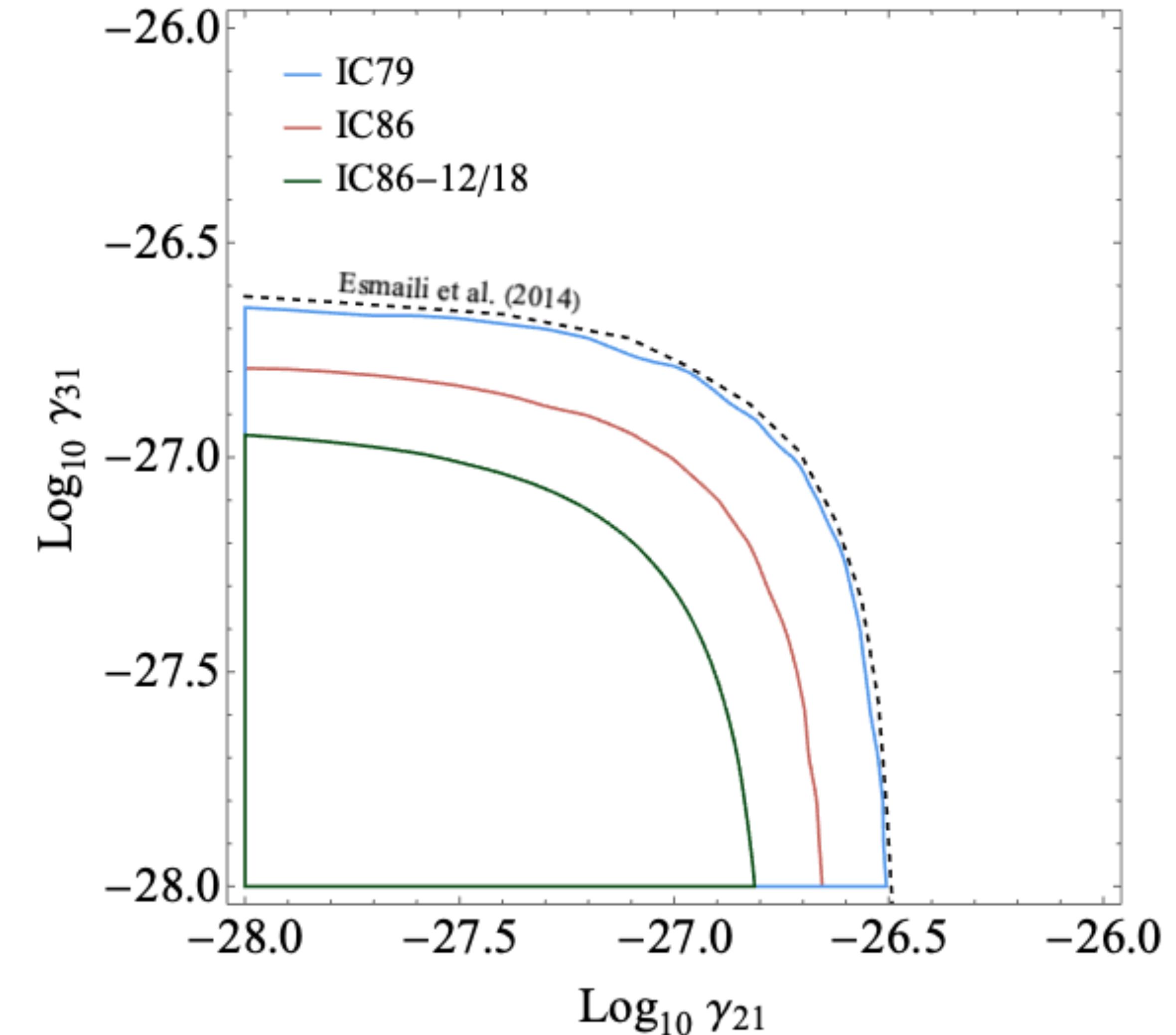
Angular distribution

# Constraints from atmospheric neutrinos

$\gamma_{21}, \gamma_{31}$  have same signs



$\gamma_{21}, \gamma_{31}$  have opposite signs



# Gravitational basis

Simple **benchmark** choice: gravity couples (diagonally) to mass eigenstates

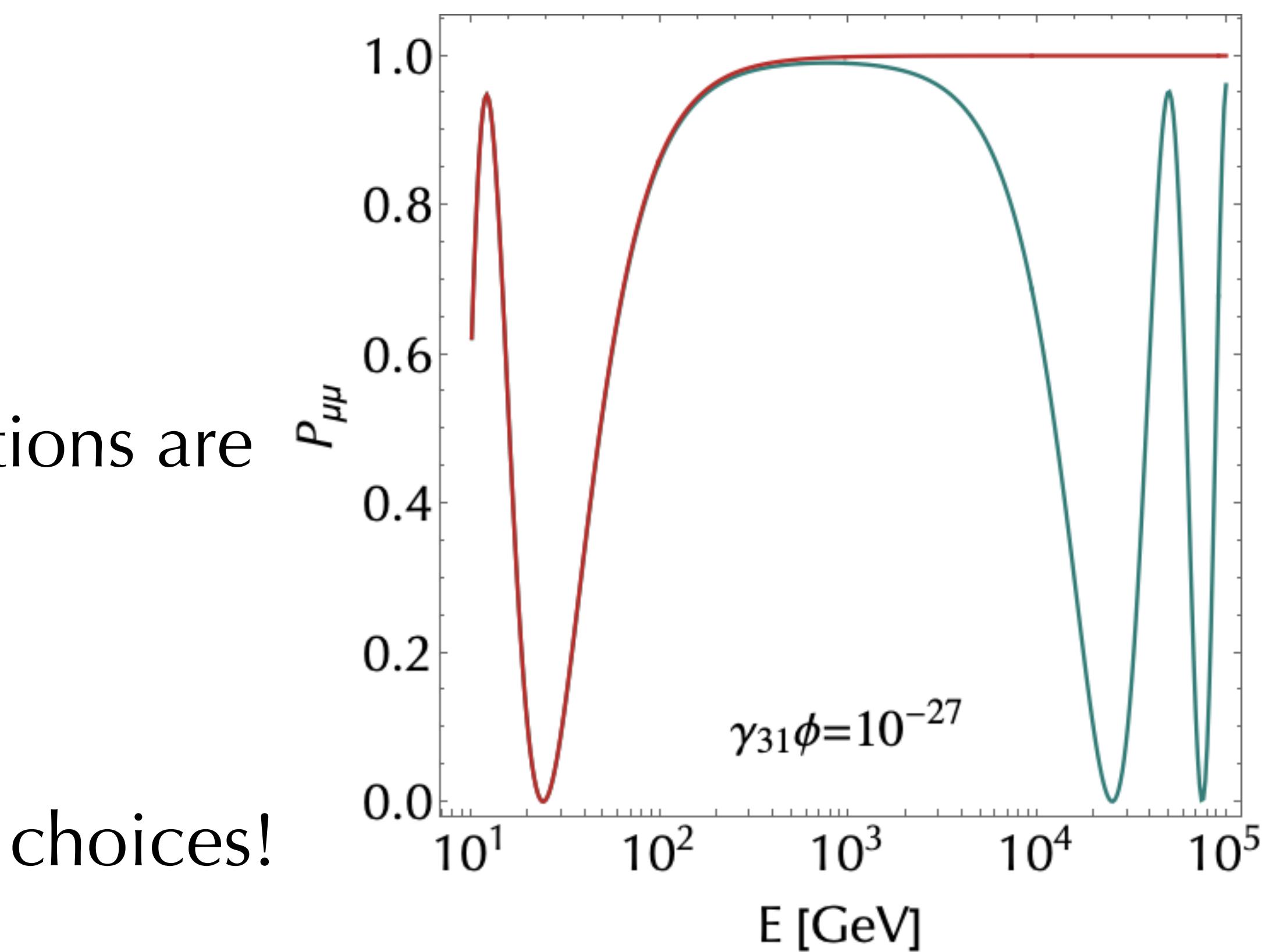
Parameterized by 3 mixing angles, 1 phase

$\tilde{U}$  connects gravitational and flavor eigenstates

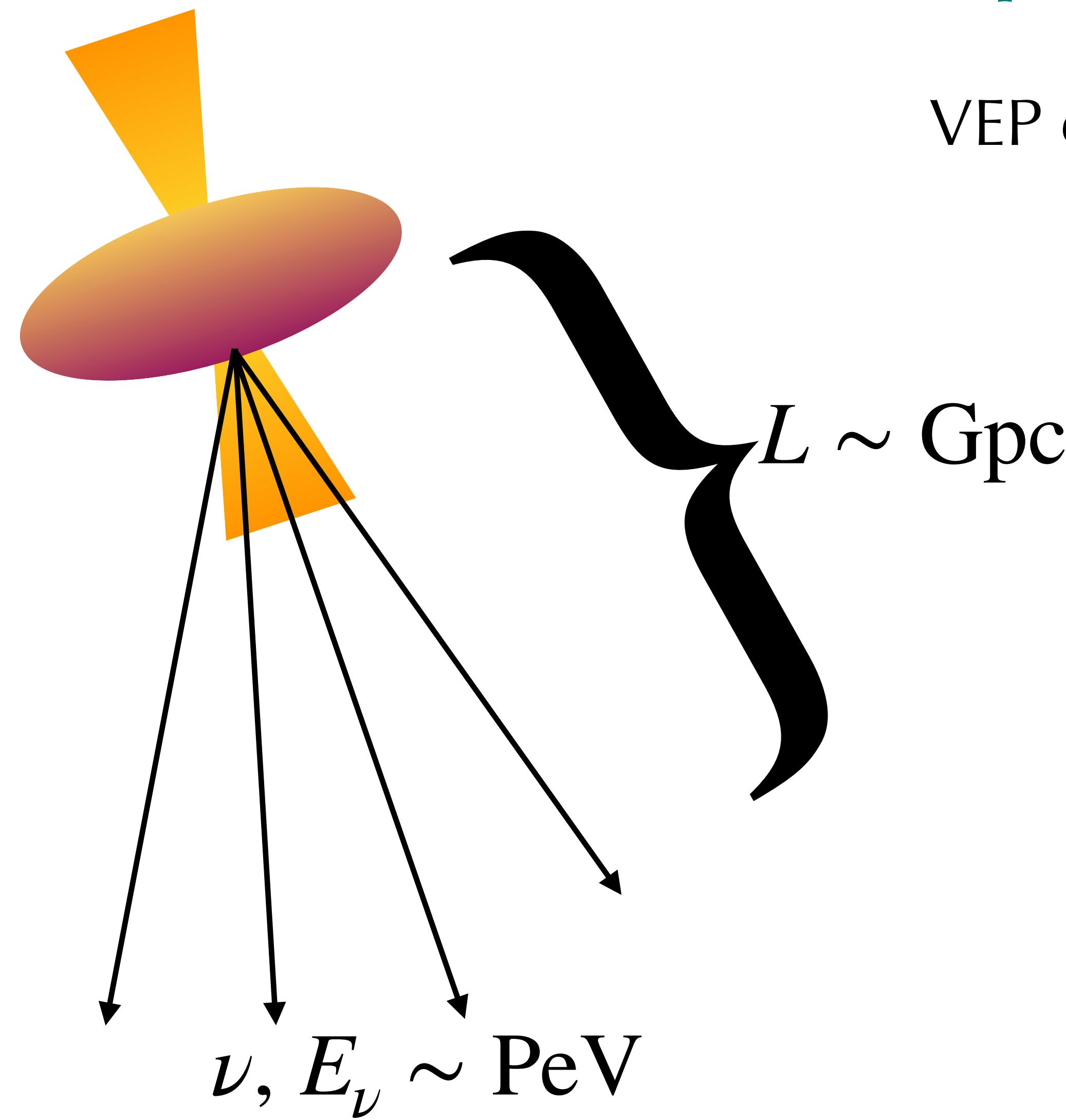
Extreme **benchmark** choice: gravity couples (diagonally) to **flavor** eigenstates

$\rightarrow$  VEP oscillations are inhibited

Atmospheric neutrinos cannot constrain all choices!



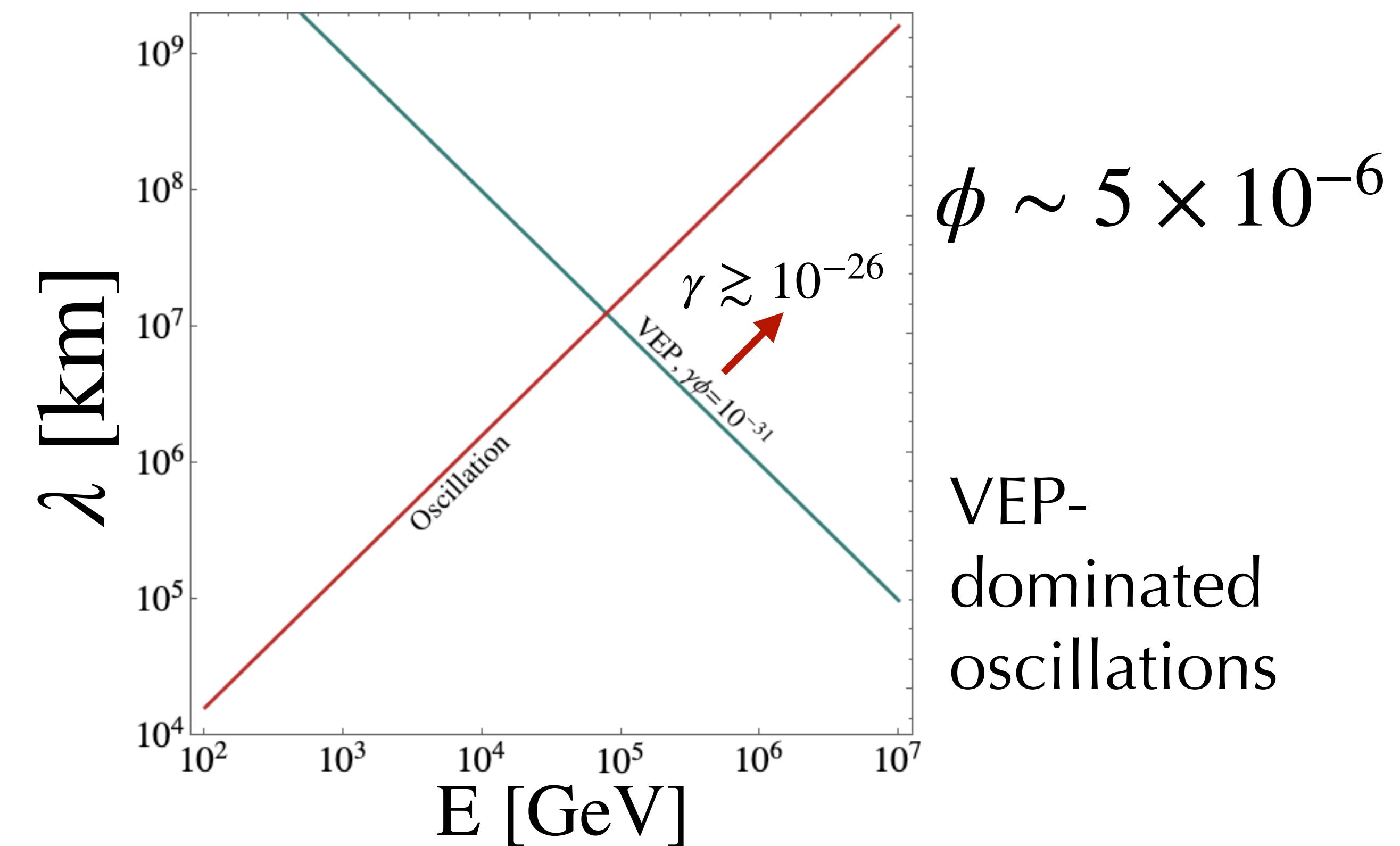
# VEP and astrophysical neutrinos



VEP effects depend on gravitational field structure

Minakata et al. 1996

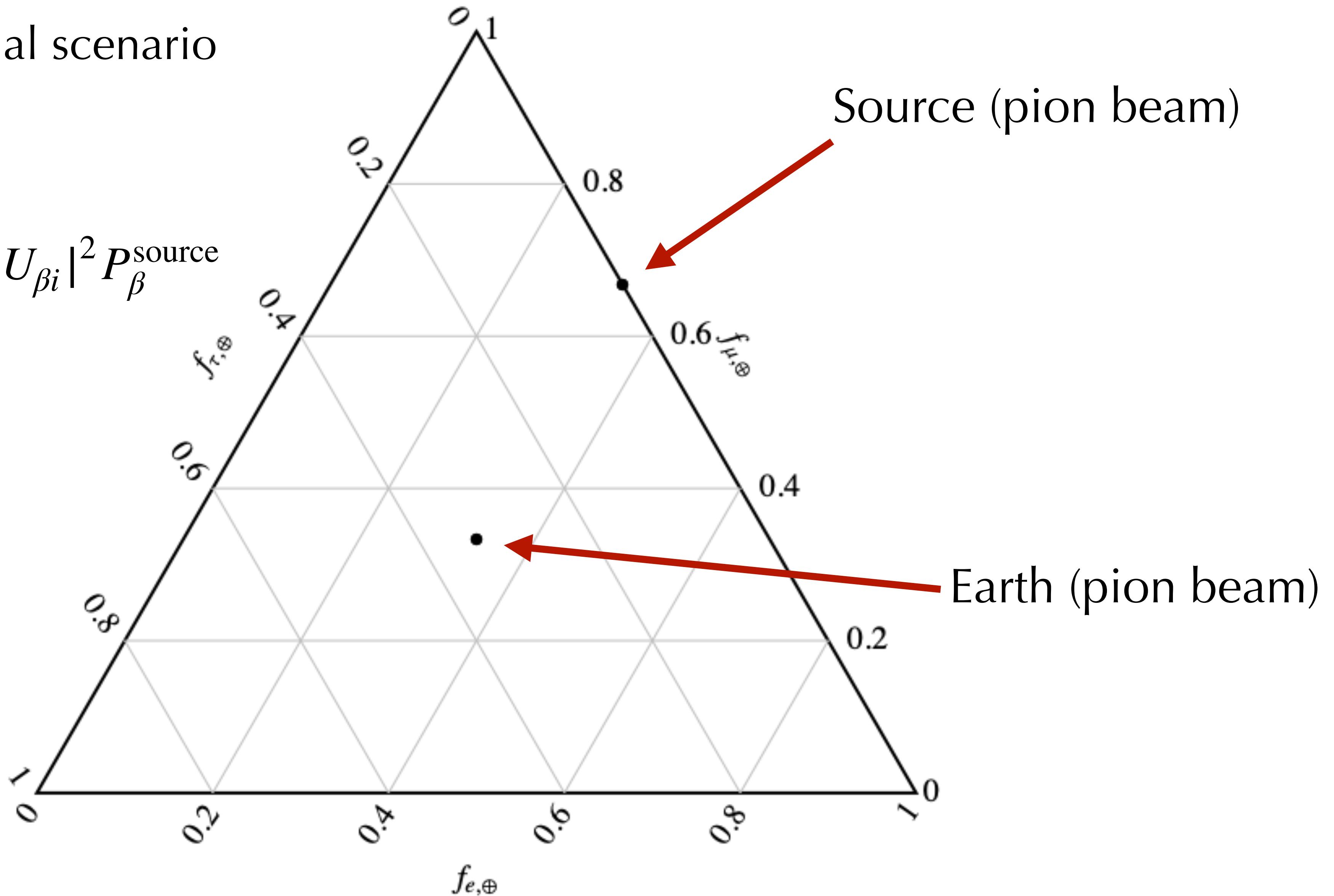
Simple scenario model independent



# VEP and astrophysical neutrinos

Conventional scenario

$$P_{\alpha}^{\text{Earth}} = \sum_i |U_{\alpha i}|^2 |U_{\beta i}|^2 P_{\beta}^{\text{source}}$$



# VEP and astrophysical neutrinos

VEP-dominated scenario

$$P_{\alpha}^{\text{Earth}} = \sum_i |\tilde{U}_{\alpha i}|^2 |\tilde{U}_{\beta i}|^2 P_{\beta}^{\text{source}}$$

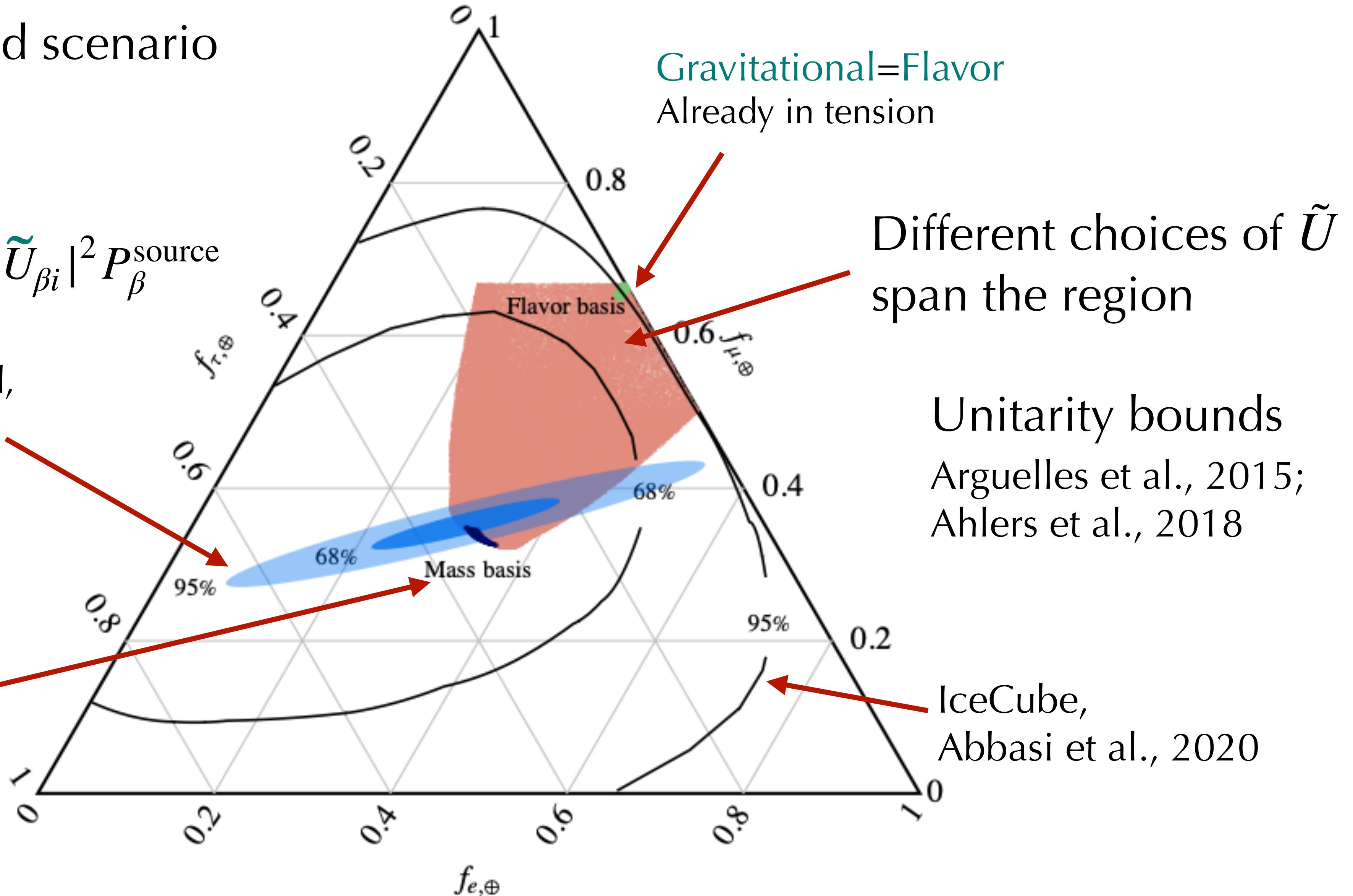
IceCube-Gen 2 estimated,  
Bustamante et al., 2019

See also Shoemaker et al.,  
2016; Song et al., 2020

$$\tilde{U} = U$$

Gravitational=Mass

Cannot be distinguished!



# Conclusions

- ◆ VEP in the neutrino sector can be tested by IceCube observations
- ◆ Complementarity between two approaches
  - ◆ Atmospheric neutrinos constrain at the level of  $\gamma\phi \sim 10^{-27}$  for some choices of the gravitational basis
  - ◆ Astrophysical neutrinos constrain at the level of  $\gamma\phi \sim 10^{-31}$  for other choices of the gravitational basis

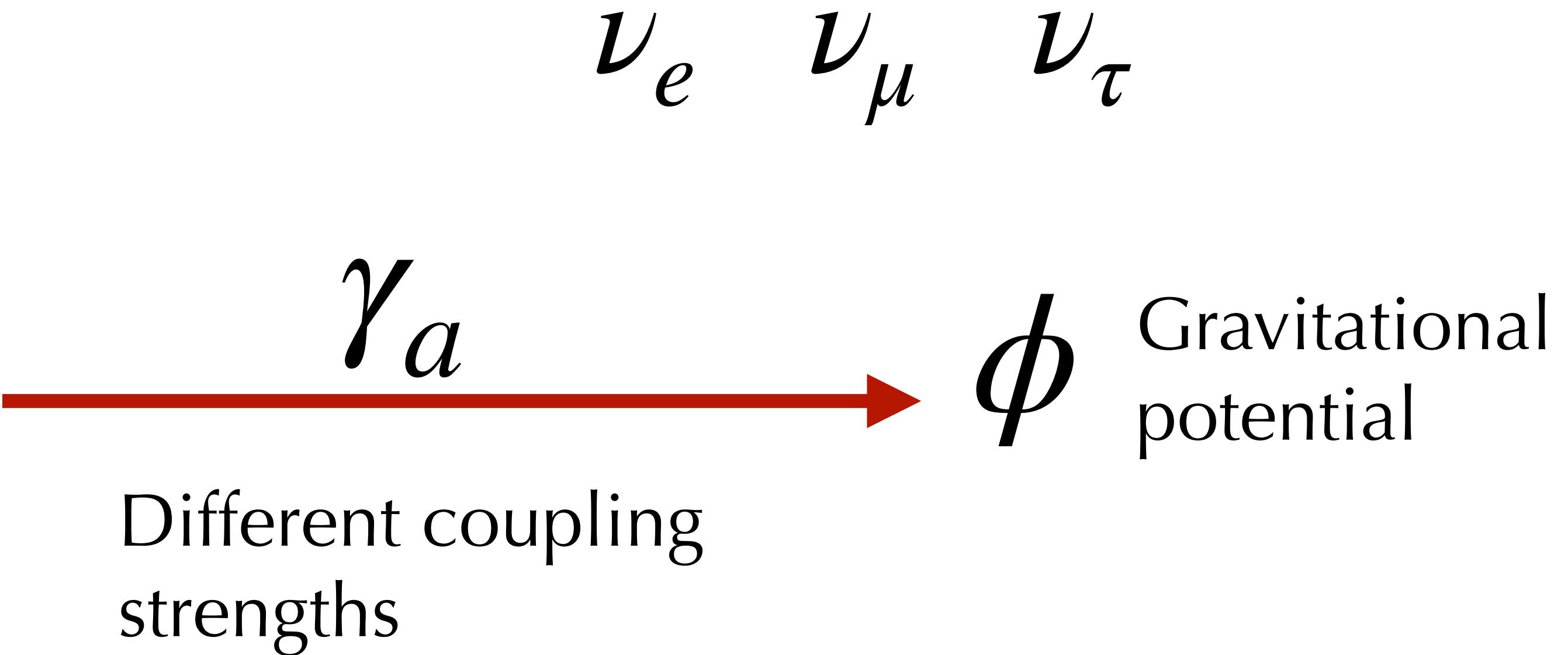
# Backup slides

# VEP and high energy neutrinos

Why does VEP influence neutrinos?

Three  
neutrino states

$$\nu_a = \sum_{\beta} \tilde{U}_{\beta a}^* \nu_{\beta}$$



Simple **benchmark** case: mass eigenstates couple differently to gravity

$$E^2(1 + 2\gamma_a \phi) - p^2(1 - 2\gamma_a \phi) = m_a^2$$

Modified dispersion relation