# Phenomenology of the minimal inverse-seesaw with Abelian flavour symmetries

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#### Inverse-seesaw (ISS) mechanism

#### **INVERSE SEESAW**

$$\operatorname{ISS}(n_R, n_s)$$

Mohapatra; Mohapatra & Valle'86; Gonzalez-Garcia & Valle'89

$$(3 + n_R + n_s) \times (3 + n_R + n_s)$$
$$\mathcal{M} = \begin{pmatrix} 0 & \mathbf{M}_D^* & 0 \\ \mathbf{M}_D^\dagger & 0 & \mathbf{M}_R \\ 0 & \mathbf{M}_R^T & \mathbf{M}_s \end{pmatrix}$$

Sterile neutrino fields:  $\nu_{Ri}$   $(i = 1, ..., n_R), s_i$   $(i = 1, ..., n_s)$ 

$$-\mathcal{L}_{\text{mass}}^{\text{ISS}} = \overline{e_L} \,\mathbf{M}_\ell \,e_R + \overline{\nu_L} \,\mathbf{M}_D \nu_R + \overline{\nu_R} \,\mathbf{M}_R s + \frac{1}{2} \overline{s^c} \,\mathbf{M}_s s + \text{H.c.}$$

Effective neutrino mass matrix  $(m_D, \mu_s \ll M)$ :

$$\mathbf{M}_{\text{eff}} = -\mathbf{M}_D^* (\mathbf{M}_R^T)^{-1} \mathbf{M}_s \mathbf{M}_R \mathbf{M}_D^{\dagger} \longrightarrow m_{\nu} \sim \mu_s \frac{m_D^2}{M^2}$$

Active-sterile mixing:

$$\mathbf{U}_{\mathrm{Hl}} \simeq \mathbf{V}_{L}^{\dagger} \left( 0, \ \mathbf{M}_{D} (\mathbf{M}_{R}^{\dagger})^{-1} \right) \mathbf{U}_{s} \longrightarrow U_{\mathrm{Hl}} \sim \frac{m_{D}}{M} \sim \sqrt{\frac{m_{\nu}}{\mu_{s}}}$$

Type-I seesaw: 
$$m_{
u} \sim \frac{m_D^2}{M} \;,\; U_{\rm Hl} \sim \frac{m_D}{M} \sim \sqrt{\frac{m_{
u}}{M}}$$

The ISS provides a natural template for (active) neutrino mass suppression with sizeable active-sterile mixing

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Minimal Inverse Seesaw:

$$\operatorname{ISS}(n_R, n_s) \longrightarrow \operatorname{ISS}(2, 2)$$

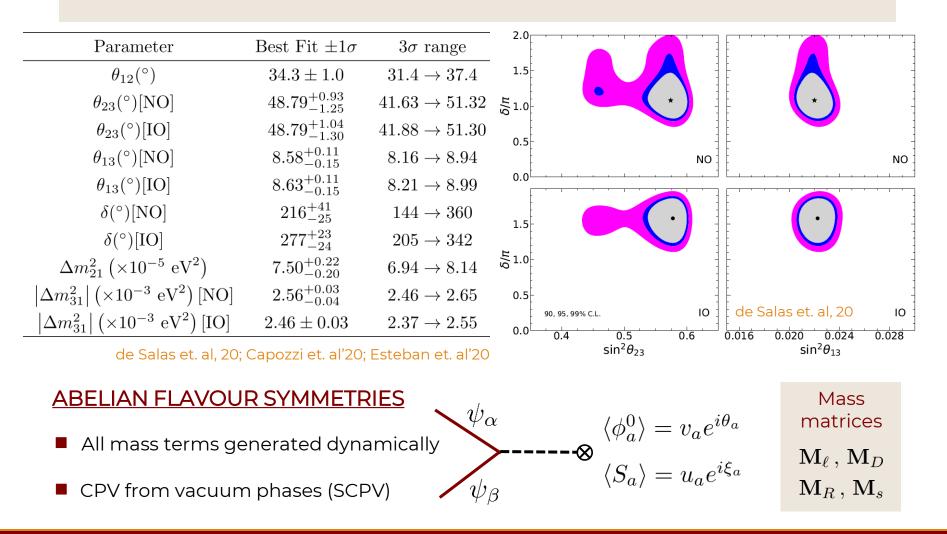
Abada & Lucente'14

- One massless neutrino
- Neutrino data can be accommodated
- Still 17 parameters (in the M<sub>s</sub> diagonal basis)

## Neutrino oscillation data

Minimal Inverse Seesaw ISS(2,2): 17 parameters vs 7 observables

 $\theta_{12} , \theta_{23} , \theta_{13} , \Delta m^2_{21,31} , \delta , \alpha$ 



#### Scalar content and Yukawa Lagrangian

- Need to add a second Higgs doublet to be able to realise the charged-lepton mass matrix textures.
- Add two neutral complex scalar singlets to dynamically generate  $\mathbf{M}_s$  and  $\mathbf{M}_R$ .

$$\Phi_{1,2} = \begin{pmatrix} \phi_{1,2}^+ \\ \phi_{1,2}^0 \\ \phi_{1,2}^0 \end{pmatrix} = \frac{1}{\sqrt{2}} \begin{pmatrix} \sqrt{2}\phi_{1,2}^+ \\ v_{1,2}e^{i\theta_{1,2}} + \rho_{1,2} + i\eta_{1,2} \end{pmatrix} , \qquad S_{1,2} = \frac{1}{\sqrt{2}} \left( u_{1,2}e^{i\xi_{1,2}} + \rho_{3,4} + i\eta_{3,4} \right)$$

$$-\mathcal{L}_{\text{Yuk.}} = \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_D^1 \tilde{\Phi}_1 + \mathbf{Y}_D^2 \tilde{\Phi}_2 \right) \nu_R$$
$$+ \frac{1}{2} \overline{s^c} \left( \mathbf{Y}_s^1 S_1 + \mathbf{Y}_s^2 S_1^* \right) s + \overline{\nu_R} \left( \mathbf{Y}_R^1 S_2 + \mathbf{Y}_R^2 S_2^* \right) s + \text{H.c.}$$

 $\frac{\text{SCALAR POTENTIAL}}{V(\Phi_a, S_a) = V_{\text{sym.}} + V_{\text{soft}}(\Phi_a, S_a)} = V_{\text{soft}}(\Phi_a, S_a) = \mu_{12}^2 \Phi_1^{\dagger} \Phi_2 + \mu_3^2 S_1^2 + \mu_4 |S_1|^2 S_1 + \mu_5 |S_2|^2 S_2 + \text{H.c.}$ 

SCPV IS ACHIEVED WITH:  $\theta, \xi_2 = 0, \xi_1 = \arctan\left(\frac{\sqrt{32\mu_3^4 - \mu_4^2 u_1^2}}{\mu_4 u_1}\right)$ 

### Abelian flavour symmetries

 Maximally-restrictive sets compatible with neutrino oscillation data that are realizable by Abelian symmetries:

		$(5_{1,I}^{\ell}, T_{45})$	$(4_3^\ell, T_{124})$	$(4_3^\ell, T_{456})$	$(4_3^\ell, T_{136,I})$	$(4_3^\ell, T_{146,I})$
Fields	U(1)	$\mathbb{Z}_2 \times \mathrm{U}(1)_\mathrm{F}$	$\mathbb{Z}_2 \times \mathrm{U}(1)_\mathrm{F}$	$\mathbb{Z}_2 \times \mathrm{U}(1)_\mathrm{F}$	$\mathbb{Z}_4 \times \mathrm{U}(1)_\mathrm{F}$	$\mathbb{Z}_4 \times \mathrm{U}(1)_\mathrm{F}$
$\Phi_1$	0	(1,1)	(0, -5)	(1,1)	(1,2)	(0,1)
$\Phi_2$	0	(0, -1)	(1, -3)	(0, -1)	(0,1)	(3,0)
$S_1$	0	(0,2)	(0, -2)	(0, -2)	(0, -2)	(0, -2)
$S_2$	1	(0, 0)	(0, 0)	(1, 0)	(0,0)	(0, 0)
$\ell_{e_L}$	1	(1,0)	(0,0)	(0,0)	(2, 0)	(2, 0)
$\ell_{\mu_L}$	1	(0,2)	(1, 2)	(1, -2)	(1,-1)	(1, -1)
$\ell_{ au_L}$	1	(0, -2)	(0,4)	(0, -4)	(0, -2)	(0, -2)
$e_R$	1	(1, -3)	(0,9)	(1, -5)	(3, -4)	(0, -3)
$\mu_R$	1	(0,3)	(1,7)	(0,-3)	(0, -3)	(1, -2)
$ au_R$	1	(0, -1)	(0,5)	(1,-1)	(1, -2)	(2, -1)
$ u_{R_1}$	1	(0,1)	(0, -1)	(0,-1)	(0,-1)	(0, -1)
$ u_{R_2}$	1	(1, -1)	(1,1)	(1,1)	(2,1)	(2,1)
$s_1$	0	(1, -1)	(1,1)	(0,1)	(2,1)	(2,1)
$s_2$	0	(0,1)	(0, -1)	(1, -1)	(0, -1)	(0, -1)

 $\mathbf{G}_{\mathrm{F}} = \mathrm{U}(1) \times \mathbb{Z}_n \times \mathrm{U}(1)_{\mathrm{F}}, \ n = 2, 4$ 

#### Abelian flavour symmetries

INTERESTING CASE				
		$(5_{1,I}^{\ell}, T_{45})$		
Fields	U(1)	$\mathbb{Z}_2 \times \mathrm{U}(1)_\mathrm{F}$		
$\Phi_1$	0	(1,1)		
$\Phi_2$	0	(0, -1)		
$S_1$	0	(0,2)		
$S_2$	1	(0,0)		
$\ell_{e_L}$	1	(1,0)		
$\ell_{\mu_L}$	1	(0,2)		
$\ell_{ au_L}$	1	(0, -2)		
$e_R$	1	(1, -3)		
$\mu_R$	1	(0,3)		
$ au_R$	1	(0, -1)		
$ u_{R_1}$	1	(0,1)		
$ u_{R_2}$	1	(1, -1)		
$s_1$	0	(1, -1)		
$s_2$	0	(0,1)		

ONLY

$-\mathcal{L}_{\text{Yuk.}} = \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2 \Phi_2 \right) e_R + \overline{\ell_L} \left( \mathbf{Y}_{\ell}^1 \Phi_1 + \mathbf{Y}_{\ell}^2$	$\left( \mathbf{Y}_D^1  ilde{\Phi}_1 + \mathbf{Y}_D^2  ilde{\Phi}_2  ight)  u_R$
$+\frac{1}{2}\overline{s^c}\left(\mathbf{Y}_s^1S_1 + \mathbf{Y}_s^2S_1^*\right)s + \overline{\nu_R}\left(\mathbf{Y}_s^1S_1 + \mathbf{Y}$	$\mathbf{Y}_{R}^{1}S_{2} + \mathbf{Y}_{R}^{2}S_{2}^{*}$ ) s + H.c.

#### Mass matrices Yukawa decompositions

$\mathbf{M}_\ell$	$\mathbf{Y}^1_\ell$	$\mathbf{Y}_\ell^2$	$\mathbf{M}_R$ $\mathbf{Y}_R$
$5^\ell_{1,\mathrm{I}}$	$\begin{pmatrix} 0 & 0 & \times \\ 0 & 0 & 0 \\ \times & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 0 & 0 \\ 0 & \times & 0 \\ 0 & 0 & \times \end{pmatrix}$	$\mathbf{T}_{14}  \begin{pmatrix} 0 & \times \\ \times & 0 \end{pmatrix}$
$\mathbf{M}_D$	$\mathbf{Y}_D^1$	$\mathbf{Y}_D^2$	$\mathbf{M}_s$ $\mathbf{Y}_s^1$ $\mathbf{Y}_s^2$
$T_{45}$	$\begin{pmatrix} \times & 0 \\ 0 & 0 \\ 0 & \times \end{pmatrix}$	$\begin{pmatrix} 0 & \times \\ \times & 0 \\ 0 & 0 \end{pmatrix}$	$\mathbf{T}_{23}  \begin{pmatrix} \times & 0 \\ 0 & 0 \end{pmatrix}  \begin{pmatrix} 0 & 0 \\ 0 & \times \end{pmatrix}$

## A common origin for Leptonic CPV

Parameterisation of the charged lepton-mass matrix:

$$5_1^{\ell}: \quad \mathbf{M}_{\ell} = \begin{pmatrix} 0 & 0 & a_1 \\ 0 & m_{\ell_1}^2 & 0 \\ a_2 & 0 & a_4 \end{pmatrix} , \quad \mathbf{H}_{\ell} = \begin{pmatrix} a_1^2 & 0 & a_1 a_4 \\ 0 & a_3^2 & 0 \\ a_1 a_4 & 0 & a_2^2 + a_4^2 \end{pmatrix} , \quad \mathbf{V}_L' = \begin{pmatrix} c_L & 0 & s_L \\ 0 & 1 & 0 \\ -s_L & 0 & c_L \end{pmatrix} \quad \theta_L$$

 $5_1^e: \mathbf{V}_{L,R} = \mathbf{V}'_{L,R} \mathbf{P}_{12}, \quad 5_1^\mu: \mathbf{V}_{L,R} = \mathbf{V}'_{L,R}, \quad 5_1^\tau: \mathbf{V}_{L,R} = \mathbf{V}'_{L,R} \mathbf{P}_{23},$ 

 $NO_{e,\mu,\tau}$  ,  $IO_{e,\mu,\tau}$   $\longrightarrow$  6 distinct cases to be analysed

REAL YUKAWAS (CP is conserved @ the Lagrangian level)  

$$\mathbf{Y}_D^1 = \begin{pmatrix} b_1 & 0\\ 0 & 0\\ 0 & b_2 \end{pmatrix}, \ \mathbf{Y}_D^2 = \begin{pmatrix} 0 & b_3\\ b_4 & 0\\ 0 & 0 \end{pmatrix}, \ \mathbf{Y}_R = \begin{pmatrix} 0 & d_2\\ d_1 & 0 \end{pmatrix}, \ \mathbf{Y}_s^1 = \begin{pmatrix} f_2 & 0\\ 0 & 0 \end{pmatrix}, \ \mathbf{Y}_s^2 = \begin{pmatrix} 0 & 0\\ 0 & f_1 \end{pmatrix}$$

VEV configuration:

## Correlation between low-energy observables

#### EFFECTIVE NEUTRINO MASS MATRIX: $\mathbf{V}_L^\dagger \mathbf{M}_{ ext{eff}} \mathbf{V}_L$

$$\mathbf{M}_{\text{eff}} = e^{-i\xi} \begin{pmatrix} \frac{y^2}{x} + \frac{z^2}{w} e^{2i\xi} & y & ze^{2i\xi} \\ y & x & 0 \\ ze^{2i\xi} & 0 & we^{2i\xi} \end{pmatrix}, \mathbf{V}_L = \begin{pmatrix} \cos\theta_L & 0 & \sin\theta_L \\ 0 & 1 & 0 \\ -\sin\theta_L & 0 & \cos\theta_L \end{pmatrix} \qquad \begin{bmatrix} 5_1^e : \mathbf{V}_{L,R} = \mathbf{V}'_{L,R} \mathbf{P}_{12} \\ 5_1^\mu : \mathbf{V}_{L,R} = \mathbf{V}'_{L,R} \\ 5_1^\mu : \mathbf{V}_{L,R} = \mathbf{V}'_{L,R} \mathbf{P}_{23} \end{bmatrix}$$

$$z = \mu_s \frac{m_{D_2} m_{D_3}}{M^2} \frac{p}{q^2} , \ w = \mu_s \frac{m_{D_2}^2}{M^2} \frac{p}{q^2} , \quad x = \mu_s \frac{m_{D_4}^2}{M^2} , \ y = \mu_s \frac{m_{D_1} m_{D_4}}{M^2}$$

The effective light neutrino mass matrix is written solely in terms of 6 effective parameters:

$$(x, y, z, w, \theta_L, \xi) \longrightarrow \mathcal{O}_i \equiv (\Delta m_{21}^2, \Delta m_{31}^2, \theta_{ij}, \delta, \alpha)$$

$$\text{NO}: M_{ij} = \left[ \mathbf{U}'^* \text{diag} \left( 0, \sqrt{\Delta m_{21}^2}, \sqrt{\Delta m_{31}^2} \right) \mathbf{U}'^\dagger \right]_{ij}$$

$$\text{IO}: M_{ij} = \left[ \mathbf{U}'^* \text{diag} \left( \sqrt{\Delta m_{31}^2}, \sqrt{\Delta m_{21}^2 + \Delta m_{31}^2}, 0 \right) \mathbf{U}'^\dagger \right]_{ij}$$

$$\text{D}_{ij} = M_{ii} M_{jj} - M_{ij}^2$$

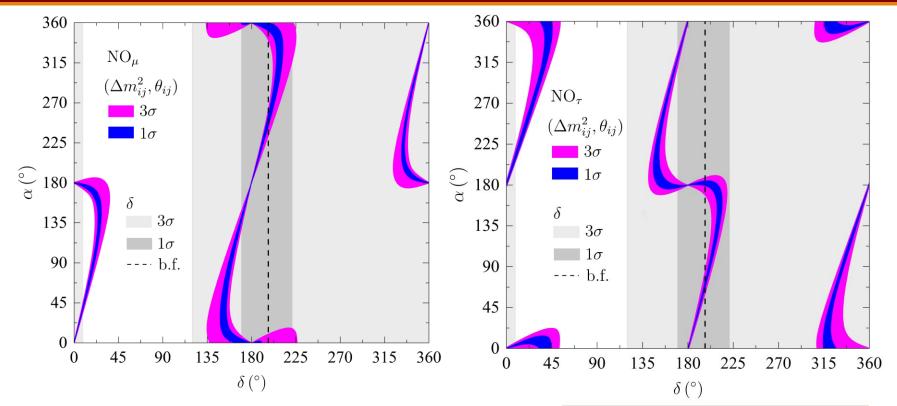
$$\text{Low-energy relations: - 5^e_1 : arg \left[ M_{11}^{*2} M_{13}^2 \frac{D_{12}}{D_{23}} \right] = 0$$

$$5^{\mu}_1 : arg \left[ M_{12}^{*2} M_{23}^2 \frac{D_{12}}{D_{23}} \right] = 0$$

$$5^{\pi}_1 : arg \left[ M_{12}^{*2} M_{23}^2 \frac{D_{12}}{D_{23}} \right] = 0$$

$$5^{\pi}_1 : arg \left[ M_{13}^{*2} M_{33}^2 \frac{D_{12}}{D_{23}} \right] = 0$$

#### Leptonic CP violation



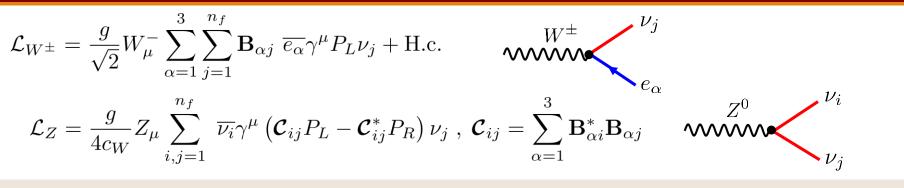
• Strong correlation between  $\alpha$  and  $\delta$ 

- Approximate symmetry  $\delta \rightarrow \delta + \pi$
- No Dirac CPV implies no Majorana CPV

 $\langle S_1 
angle = u_1 e^{i\xi}$  $\mathcal{J}_{\mathrm{Dirac}}^{\mathrm{CP}}, \ \mathcal{J}_{\mathrm{Maj}}^{\mathrm{CP}} \propto \sin(2\xi)$ as in Branco, Felipe, FRJ, Serôdio (2012)

• A measurement of  $\delta$  in the intervals [45°, 135°] and [225°, 315°] would exclude the NO<sub>u</sub> and NO<sub> $\tau$ </sub> cases

## Heavy-light mixing relations



$$\frac{\mathbf{B}_{e4}}{\mathbf{B}_{\mu4}} \simeq \frac{\mathbf{B}_{e5}}{\mathbf{B}_{\mu5}} \simeq \frac{x}{yc_L} , \ \frac{\mathbf{B}_{\tau4}}{\mathbf{B}_{\mu4}} \simeq \frac{\mathbf{B}_{\tau5}}{\mathbf{B}_{\mu5}} \simeq \tan\theta_L , \ \frac{\mathbf{B}_{\mu6}}{\mathbf{B}_{\tau6}} \simeq \frac{\mathbf{B}_{\mu7}}{\mathbf{B}_{\tau7}} \simeq \frac{z - w \tan\theta_L}{w + z \tan\theta_L} , \ \mathbf{B}_{e6} \simeq \mathbf{B}_{e7} \simeq 0$$

#### NUMERICAL ESTIMATES

	$\mathrm{NO}_{e}$	$\mathrm{NO}_{\mu}$	$NO_{\tau}$	$IO_e$	$\mathrm{IO}_{\mu}$	$IO_{\tau}$
$\mathbf{B}_{e4}/\mathbf{B}_{\mu4}\simeq\mathbf{B}_{e5}/\mathbf{B}_{\mu5}$	0.21	0.17	0.17	2.73	0.21	0.41
$\mathbf{B}_{ au 4}/\mathbf{B}_{\mu 4} \simeq \mathbf{B}_{ au 5}/\mathbf{B}_{\mu 5}$	0.27	0.88	0.87	0.51	1.09	1.24
$\mathbf{B}_{ au 4}/\mathbf{B}_{e4}\simeq \mathbf{B}_{ au 5}/\mathbf{B}_{e5}$	1.27	5.07	5.24	0.19	5.33	5.02
$\mathbf{B}_{e6}/\mathbf{B}_{\mu 6}\simeq \mathbf{B}_{e7}/\mathbf{B}_{\mu 7}$	0	_	0.36	0	_	4.96
$\mathbf{B}_{ au 6}/\mathbf{B}_{\mu 6}\simeq \mathbf{B}_{ au 7}/\mathbf{B}_{\mu 7}$	0.61	_	0	1.14	_	0
$\mathbf{B}_{ au 6} / \mathbf{B}_{e6} \simeq \mathbf{B}_{ au 7} / \mathbf{B}_{e7}$	_	1.64	0	_	0.23	0

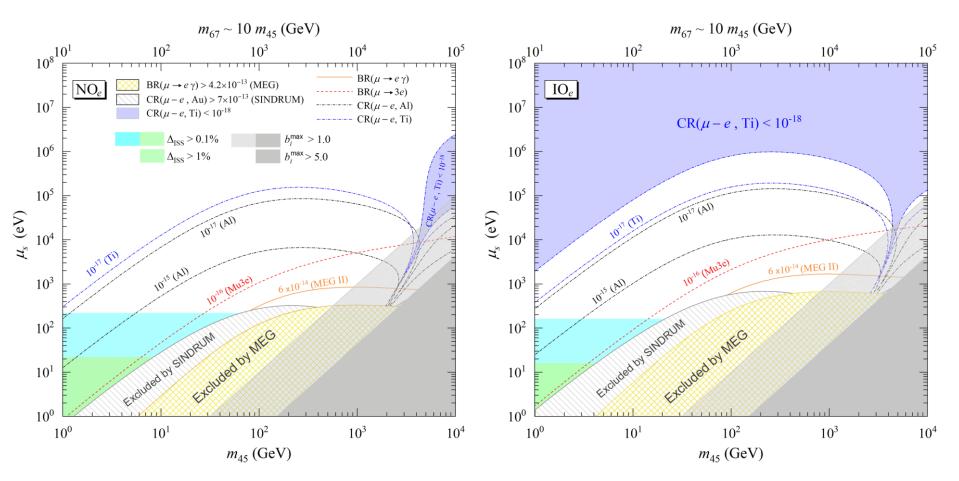
- The  $B_{\alpha i}$  ( $\alpha = e, \mu, \tau$ ) (i = 4, ..., 7) are related to each other,
- The relations are expressed solely in terms of the low-energy neutrino observables,
- Due to the flavour symmetries the heavy-light mixing parameters are not independent,

This establishes relations among cLFV processes (no time to discuss here)

## Charged lepton flavour violation (cLFV)

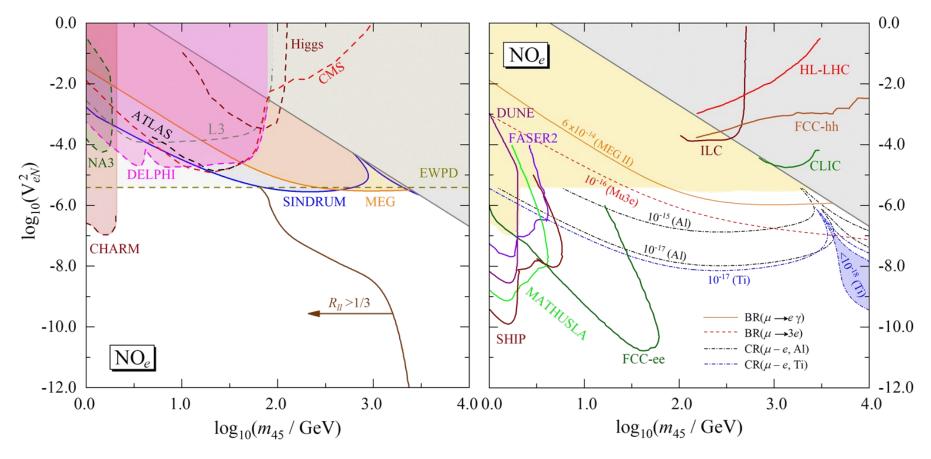
cLFV process	Present limit $(90\% \text{ CL})$	Future sensitivity
$BR(\mu \to e\gamma)$	$4.2 \times 10^{-13} \text{ (MEG)}$	$6 \times 10^{-14}$ (MEG II)
$BR(\tau \to e\gamma)$	$3.3 \times 10^{-8} $ (BaBar)	$3 \times 10^{-9}$ (Belle II)
${ m BR}( au  o \mu \gamma)$	$4.4 \times 10^{-8}$ (BaBar)	$10^{-9}$ (Belle II)
$BR(\mu^- \to e^- e^+ e^-)$	$1.0 \times 10^{-12}$ (SINDRUM)	$10^{-16}$ (Mu3e)
$BR(\tau^- \to e^- e^+ e^-)$	$2.7 \times 10^{-8}$ (Belle)	$5 \times 10^{-10}$ (Belle II)
${\rm BR}(\tau^- \to e^- \mu^+ \mu^-)$	$2.7 \times 10^{-8}$ (Belle)	$5 \times 10^{-10}$ (Belle II)
${\rm BR}(\tau^- \to e^+ \mu^- \mu^-)$	$1.7 \times 10^{-8}$ (Belle)	$3 \times 10^{-10}$ (Belle II)
$\mathrm{BR}(\tau^- \to \mu^- e^+ e^-)$	$1.8 \times 10^{-8}$ (Belle)	$3 \times 10^{-10}$ (Belle II)
$\mathrm{BR}(\tau^- \to \mu^+ e^- e^-)$	$1.5 \times 10^{-8}$ (Belle)	$3 \times 10^{-10}$ (Belle II)
$BR(\tau^- \to \mu^- \mu^+ \mu^-)$	$2.1 \times 10^{-8}$ (Belle)	$4 \times 10^{-10}$ (Belle II)
$CR(\mu - e, Al)$	_	$3 \times 10^{-17} $ (Mu2e)
		$10^{-15} - 10^{-17}$ (COMET I-II)
$CR(\mu - e, Ti)$	$4.3 \times 10^{-12}$ (SINDRUM II)	$10^{-18}$ (PRISM/PRIME)
$CR(\mu - e, Au)$	$7 \times 10^{-13}$ (SINDRUM II)	_
$CR(\mu - e, Pb)$	$4.6 \times 10^{-11}$ (SINDRUM II)	_

## cLFV in the ISS(2,2) with Abelian symmetries



- (Almost) the whole parameter space will be scrutinized by future μ–e conversion experiments (Mu2e, COMET, PRISM/PRIME) for normal neutrino mass ordering;
- For inverted ordering the prospects are less optimistic.

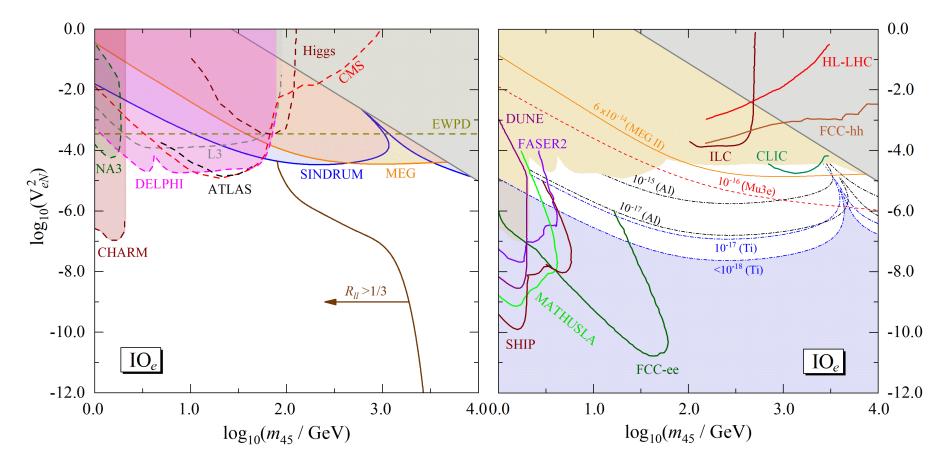
#### Constraints on heavy sterile neutrinos



Current data implies an upper bound  $V_{eN}^2 \sim 10^{-6} - 10^{-5}$ ;

Future probes will be sensitive to much smaller mixings. LFV complementary to other searches.

#### Constraints on heavy sterile neutrinos



- EWPD is less constraining in the IO case;
- Future CLV probes will be sensitive to  $V_{eN}^2 \sim 10^{-7}$

- Minimal inverse seesaw mechanism constrained by Abelian flavour symmetries with all mass terms generated via SSB;
- Majorana and Dirac-type CP violation are related;
- Relations among LFV parameters in our framework provide a very constrained setup for phenomenological studies;
- Constraining power of cLFV processes in the model's parameter space;
- Alternative probes such as beam-dump, hadron-collider, linearcollider, displaced-vertex experiments as well as EWPD.

Impact of radiative correction on neutrino masses, neutrinoless double beta decay, relations among tau and mu decays,...

#### Grazie!

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