

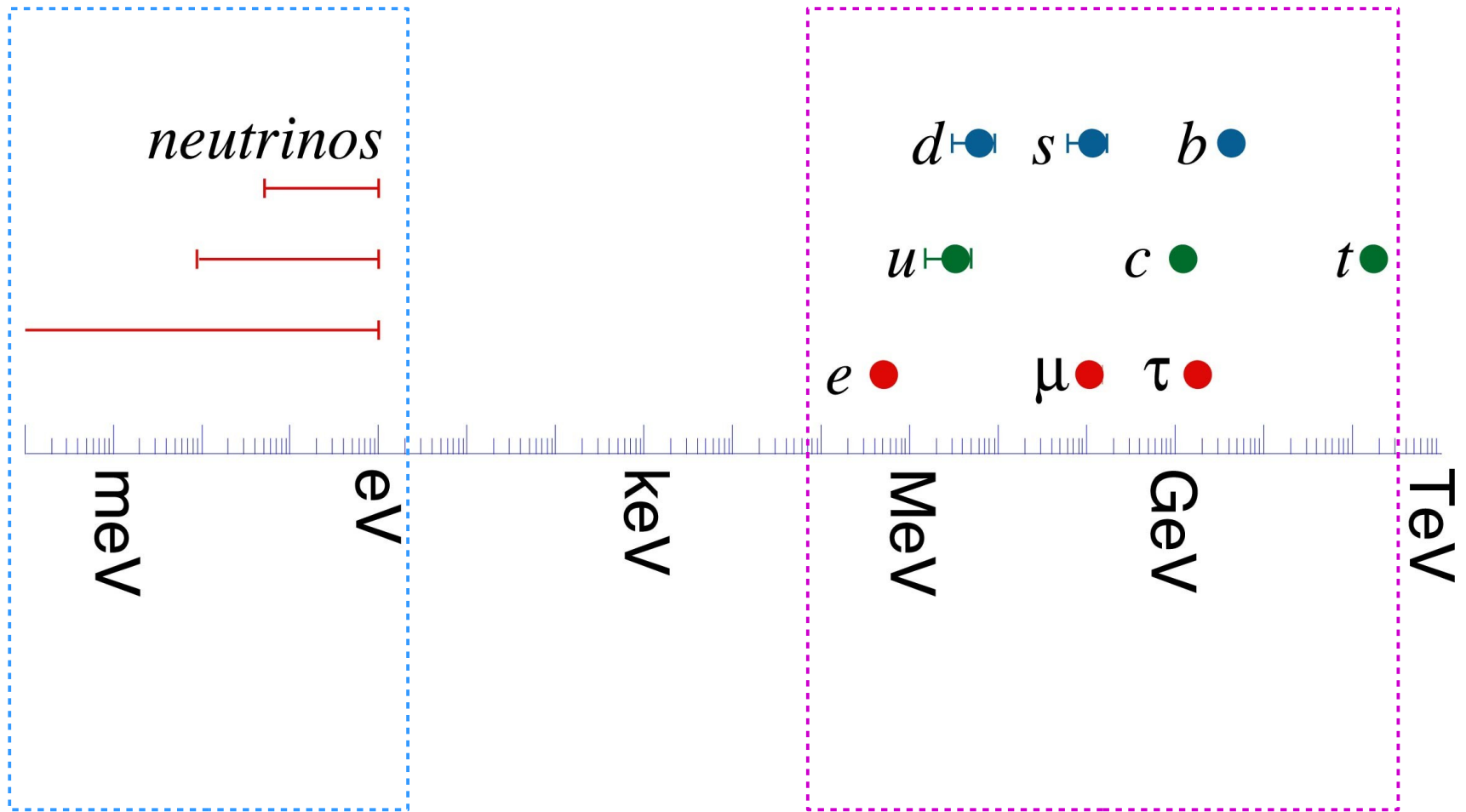
Sterile neutrino phenomenology

Pilar Coloma



NeuTel Conference
Feb 26th, 2021

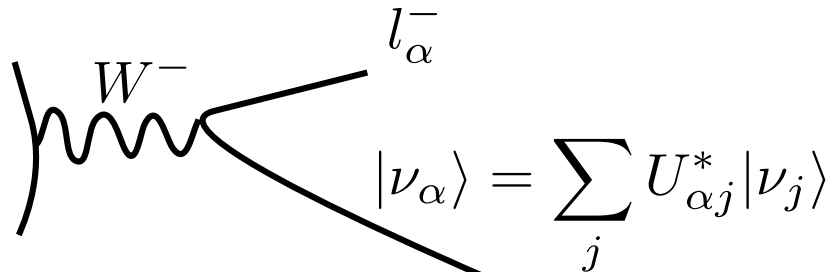
Neutrinos have mass!



Oscillations at long-baseline exps

Neutrino oscillations

Source



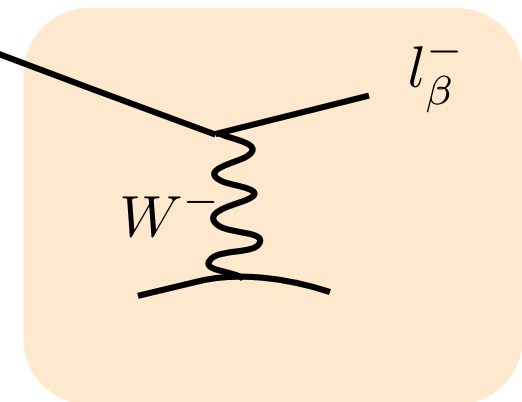
$$|\nu_\alpha\rangle = \sum_j U_{\alpha j}^* |\nu_j\rangle$$

$$|\nu_j(L, t)\rangle = e^{-i(E_j t - p_j L)} |\nu_j\rangle$$

$$P_{\alpha\beta} = \sin^2 2\theta \sin^2 \left(\frac{\Delta m^2 L}{4E} \right) \quad (\text{appearance})$$

$$P_{\alpha\alpha} = 1 - \sin^2 2\theta \sin^2 \left(\frac{\Delta m^2 L}{4E} \right) \quad (\text{disappearance})$$

Detector



$$\langle \nu_\beta | \nu_\alpha(L) \rangle \simeq \sum_j U_{\beta j} e^{-\frac{i m_j^2 L}{2E}} U_{\alpha j}^*$$

Non-Unitarity

$$Y_\nu \bar{L}_L \tilde{\phi} \nu_R + \frac{1}{2} M_R \bar{\nu}_R^c \nu_R \quad \rightarrow \quad m_D \bar{\nu}_L \nu_R + \frac{1}{2} M_R \bar{\nu}_R^c \nu_R$$

$$\mathcal{M}_\nu = U^t \begin{pmatrix} 0 & m_D^t \\ m_D & M_R \end{pmatrix} U = \begin{pmatrix} m & 0 \\ 0 & M \end{pmatrix}$$

Non-Unitarity

$$Y_\nu \bar{L}_L \tilde{\phi} \nu_R + \frac{1}{2} M_R \bar{\nu}_R^c \nu_R \rightarrow m_D \bar{\nu}_L \nu_R + \frac{1}{2} M_R \bar{\nu}_R^c \nu_R$$

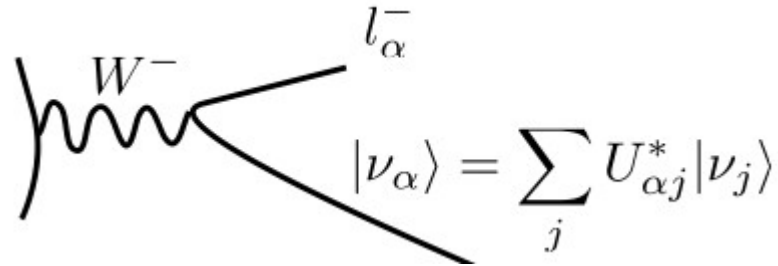
$$\mathcal{M}_\nu = U^t \begin{pmatrix} 0 & m_D^t \\ m_D & M_R \end{pmatrix} U = \begin{pmatrix} m & 0 \\ 0 & M \end{pmatrix}$$

↑

The full matrix is unitary,
but the 3x3 block **is not**:

$$U = \begin{pmatrix} N & \Theta \\ R & S \end{pmatrix} \longleftarrow \mathcal{O} \left(\frac{m_D}{M_R} \right)$$

Non-unitarity in oscillations



A Feynman diagram showing a W^- boson (represented by a wavy line) decaying into a lepton l_α^- and a neutrino $|\nu_\alpha\rangle$. The neutrino is represented by a solid line. The equation $|\nu_\alpha\rangle = \sum_j U_{\alpha j}^* |\nu_j\rangle$ is written next to the neutrino line.

Heavy steriles
(not kinematically accessible)

$$P_{\alpha\beta} = \sum_{i,j} N_{\beta i} N_{\alpha i}^* N_{\alpha j} N_{\beta j}^* e^{-i \frac{\Delta m_{ij}^2 L}{2E}}$$

Non-unitarity in oscillations

$$| \nu_\alpha \rangle = \sum_j U_{\alpha j}^* | \nu_j \rangle$$

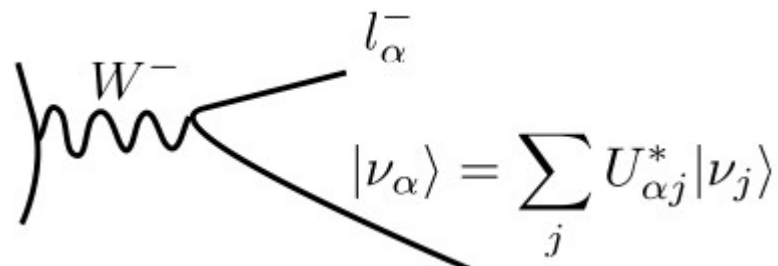
Heavy steriles
(not kinematically accessible)

$$P_{\alpha\beta} = \sum_{i,j} N_{\beta i} N_{\alpha i}^* N_{\alpha j} N_{\beta j}^* e^{-i \frac{\Delta m_{ij}^2 L}{2E}}$$

Light steriles
(kinematically accessible)

$$P_{\alpha\beta} = \sum_{i,j} N_{\beta i} N_{\alpha i}^* N_{\alpha j} N_{\beta j}^* e^{-i \frac{\Delta m_{ij}^2 L}{2E}} \\ + \sum_{I,J} \Theta_{\beta I} \Theta_{\alpha I}^* \Theta_{\alpha J} \Theta_{\beta J}^* e^{-i \frac{\Delta m_{IJ}^2 L}{2E}} \\ + \sum_{i,J} N_{\beta i} N_{\alpha i}^* \Theta_{\alpha J} \Theta_{\beta J}^* e^{-i \frac{\Delta m_{iJ}^2 L}{2E}}$$

Non-unitarity in oscillations



$$| \nu_{\alpha} \rangle = \sum_j U_{\alpha j}^* | \nu_j \rangle$$

Heavy steriles
(not kinematically accessible)

$$P_{\alpha\beta} = \sum_{i,j} N_{\beta i} N_{\alpha i}^* N_{\alpha j} N_{\beta j}^* e^{-i \frac{\Delta m_{ij}^2 L}{2E}}$$

Light steriles
(kinematically accessible)

$$P_{\alpha\beta} \simeq \sum_{i,j} N_{\beta i} N_{\alpha i}^* N_{\alpha j} N_{\beta j}^* e^{-i \frac{\Delta m_{ij}^2 L}{2E}} + \mathcal{O}(\Theta^4)$$

→ Equal at leading order

Blennow, PC, Fernandez-Martinez, Hernandez-Garcia, Lopez-Pavon, 1609.08637
(see also Fong, Minakata, Nunokawa, 1609.08623)

Non-unitarity in oscillations

A triangular parametrization is most convenient:

$$N = (I - \alpha) U \quad \alpha = \begin{pmatrix} \alpha_{ee} & 0 & 0 \\ \alpha_{e\mu} & \alpha_{\mu\mu} & 0 \\ \alpha_{e\tau} & \alpha_{\mu\tau} & \alpha_{\tau\tau} \end{pmatrix}$$

In a 3+1 scenario (light sterile), one can further identify:

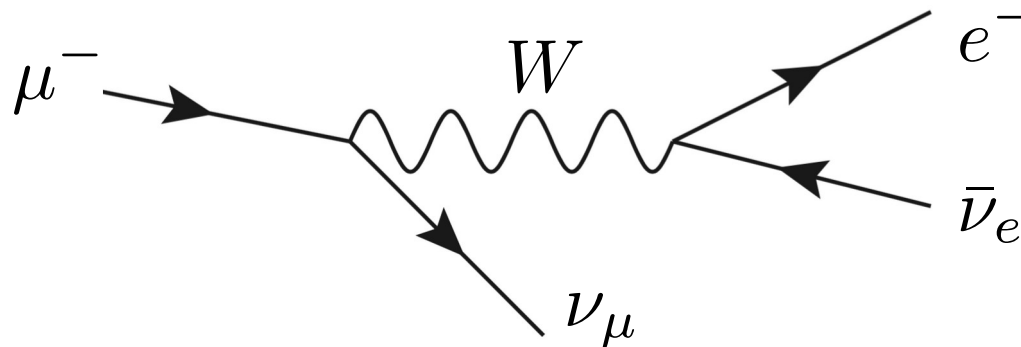
$$N = \left(\hat{O}_{34} \hat{O}_{24} O_{14} O_{23} \hat{O}_{13} O_{12} \right)_{3 \times 3} \quad \alpha \simeq \begin{pmatrix} \frac{1}{2} s_{14}^2 & 0 & 0 \\ s_{14} \hat{s}_{24}^* & \frac{1}{2} s_{24}^2 & 0 \\ s_{14} \hat{s}_{34}^* & \hat{s}_{24} \hat{s}_{34}^* & \frac{1}{2} s_{34}^2 \end{pmatrix}$$

$$\hat{s}_{ij} \equiv s_{ij} e^{i\phi_{ij}}$$

Xing, 0709.2220 and 0902.2469
Escrihuela, Forero, Miranda, Tortola, Valle, 1503.08879

Current bounds

If the new states are above EW scale, weak processes get affected right away:



$$G_\mu = G_{SM} (NN^\dagger)_{ee} (NN^\dagger)_{\mu\mu}$$

With

$$G_{SM} = \frac{\alpha\pi M_Z^2}{\sqrt{2}M_W^2(M_Z^2 - M_W^2)}$$

They agree at the 0.1% level!

See e.g., Fernandez-Martinez, Hernandez-Garcia and Lopez-Pavon, 1605.08774, Antusch and Fischer, 1407.6607

Current bounds

If the heavy neutrinos are **above the EW scale**, the bounds are really strong:

$$|\alpha_{\beta\gamma}| \leq \begin{pmatrix} 1.3 \cdot 10^{-3} & 0 & 0 \\ 6.8 \cdot 10^{-4} * & 2.2 \cdot 10^{-4} & 0 \\ 2.7 \cdot 10^{-3} & 1.2 \cdot 10^{-3} & 2.8 \cdot 10^{-3} \end{pmatrix} \quad (\text{at } 2\sigma)$$

Bounds adapted from Fernandez-Martinez, Hernandez-Garcia and Lopez-Pavon, 1605.08774
(see also Antusch and Fischer, 1407.6607)

The bounds are relaxed if they are **below EW scale**

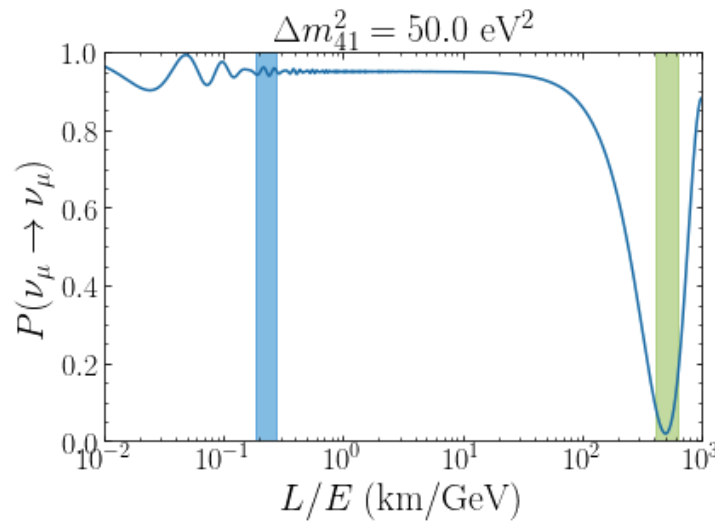
$$|\alpha_{\beta\gamma}| \leq \begin{pmatrix} 2.4 \cdot 10^{-3} & 0 & 0 \\ 2.5 \cdot 10^{-2} & 2.2 \cdot 10^{-2} & 0 \\ 6.9 \cdot 10^{-2} & 1.2 \cdot 10^{-2} & 1 \cdot 10^{-1} \end{pmatrix} \quad (\text{at } 95\%, \text{ for } \Delta m^2 > 100 \text{ eV}^2)$$

Blennow, Coloma, Fernandez-Martinez, Hernandez-Garcia, Lopez-Pavon, 1609.08637

* this bound becomes stronger if we consider $\mu \rightarrow e\gamma$ ($< 2.4 \cdot 10^{-5}$)

Role of near detectors

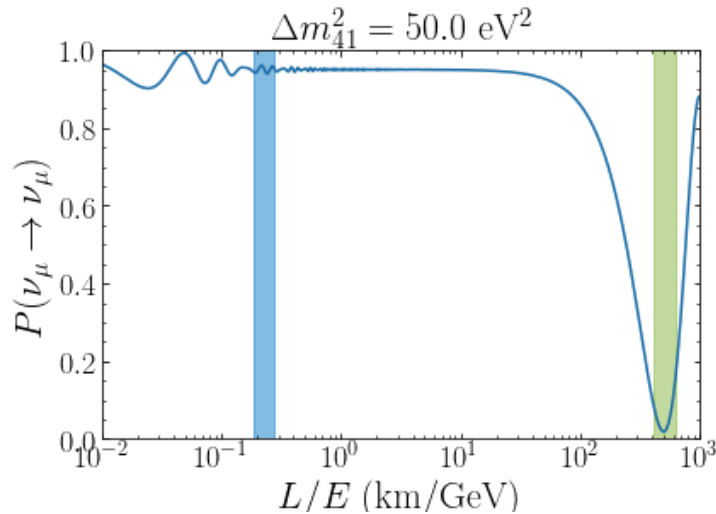
Long-baseline experiments measure a “ratio” of event rates:



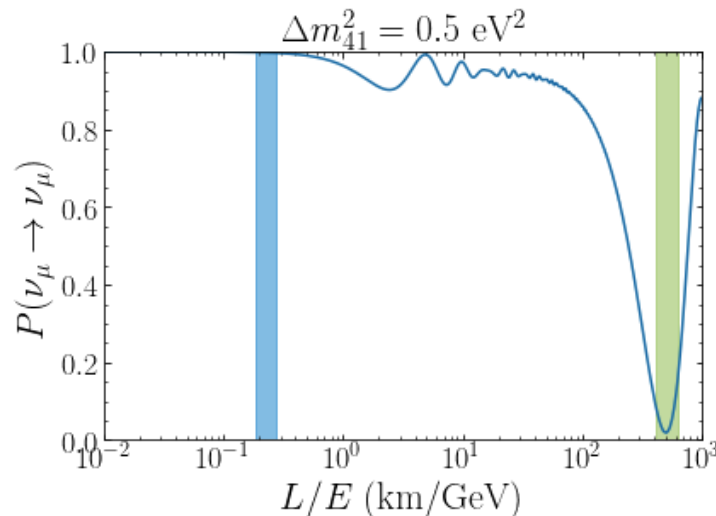
$$\Rightarrow \mathcal{P}_{\alpha\beta}^{FD} = \frac{|(NS^0 N^\dagger)_{\beta\alpha}|^2}{((NN^\dagger)_{\alpha\alpha})^2}$$

Role of near detectors

Long-baseline experiments measure a “ratio” of event rates:



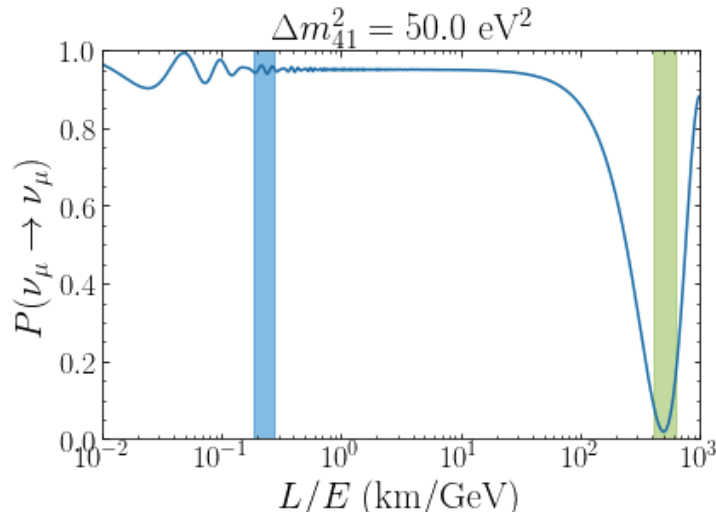
$$\Rightarrow \mathcal{P}_{\alpha\beta}^{FD} = \frac{|(NS^0 N^\dagger)_{\beta\alpha}|^2}{((NN^\dagger)_{\alpha\alpha})^2}$$



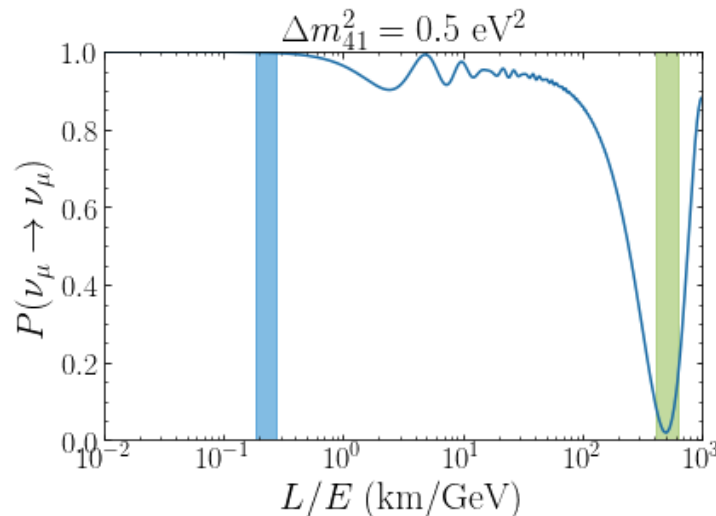
$$\Rightarrow \mathcal{P}_{\alpha\beta}^{FD} \simeq |(NS^0 N^\dagger)_{\beta\alpha}|^2$$

Role of near detectors

Long-baseline experiments measure a “ratio” of event rates:



$$\mathcal{P}_{\mu\mu}^{FD} = 1 - \sin^2 2\theta_{23} \sin^2 \Delta_{31} + \mathcal{O}(\alpha^2)$$

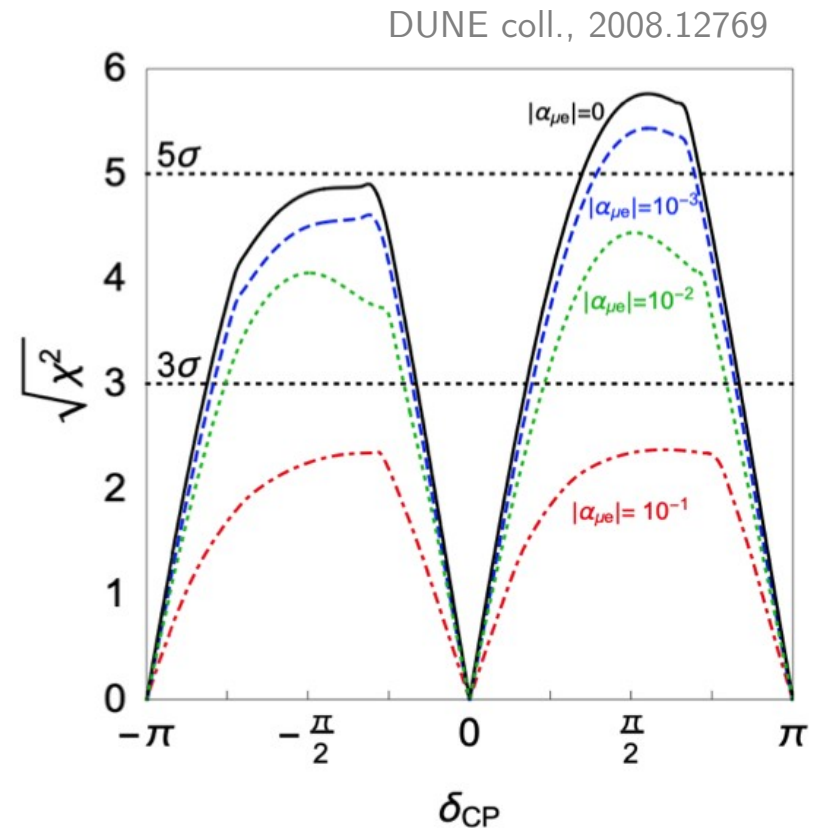


$$\mathcal{P}_{\mu\mu}^{FD} = (1 - 4\alpha_{\mu\mu})(1 - \sin^2 2\theta_{23} \sin^2 \Delta_{31}) + \mathcal{O}(\alpha^2)$$

Impact at long-baseline experiments

$$\mathcal{P}_{\mu e} = (1 - 2\alpha_{ee} + 2\alpha_{\mu\mu})P_{\mu e}^{3\times 3} + \alpha_{\mu e}P_{\mu e}^I + \mathcal{O}(\alpha^2)$$

Escrivuela, Forero, Miranda, Tortola, Valle, 1503.08879
(see also 1612.07377)



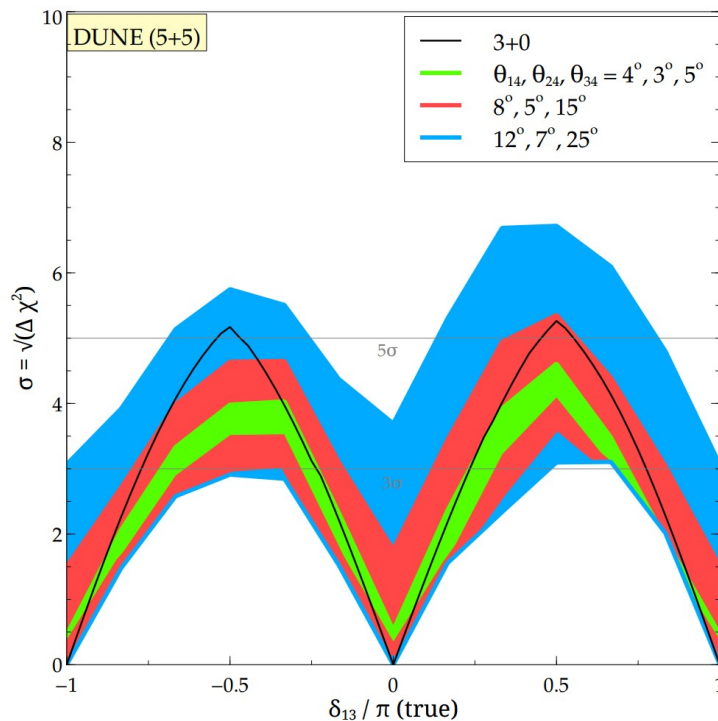
Impact at long-baseline experiments

$$\mathcal{P}_{\mu e} = (1 - 2\alpha_{ee} + 2\alpha_{\mu\mu})P_{\mu e}^{3\times 3} + \alpha_{\mu e}P_{\mu e}^I + \mathcal{O}(\alpha^2)$$

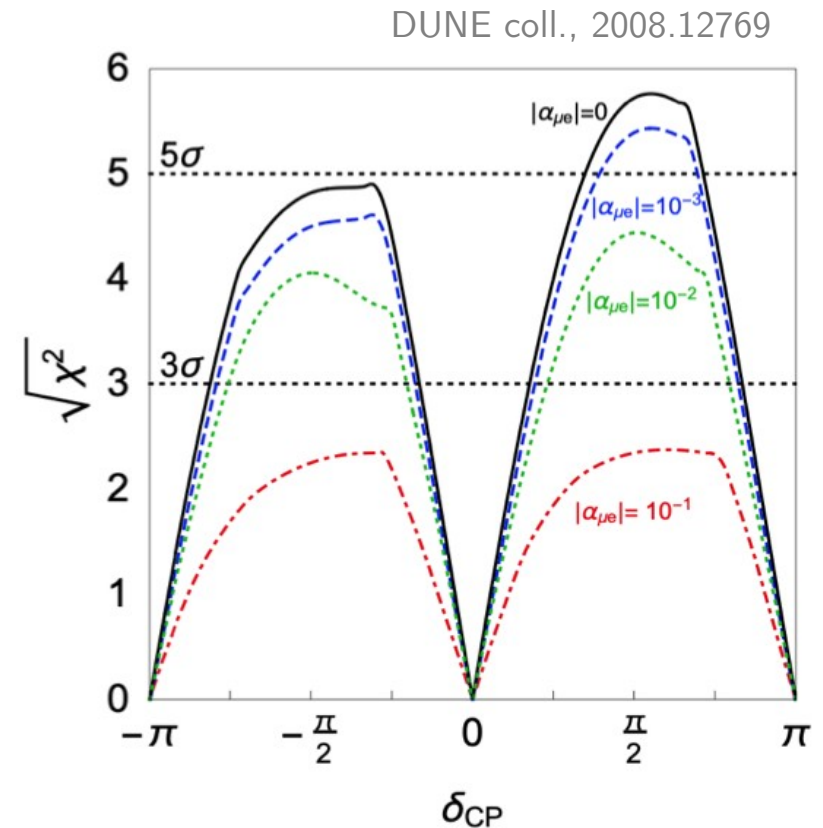
Escrivuela, Forero, Miranda, Tortola, Valle, 1503.08879
(see also 1612.07377)

In a 3+1 scenario, we can identify

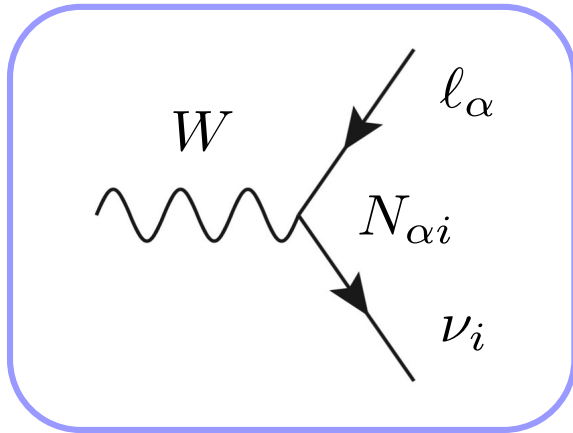
$$|\alpha_{\mu e}| = s_{14}s_{24}$$



Dutta, Gandhi, Kayser, Masud, Prakash, 1607.02152
See also Agarwalla, Chatterjee, Palazzo, 1605.04299



NSI from non-unitarity



$$P_{\alpha\beta} = | (NSN^\dagger)_{\beta\alpha} |^2$$

$$= | [(1 - \alpha)USU^\dagger(1 - \alpha)^\dagger]_{\beta\alpha} |^2$$

Effects in production, propagation and detection are correlated and simultaneously generated:

$$\epsilon_{\alpha\beta}^{s*} = \epsilon_{\alpha\beta}^d = -\alpha_{\alpha\beta}$$

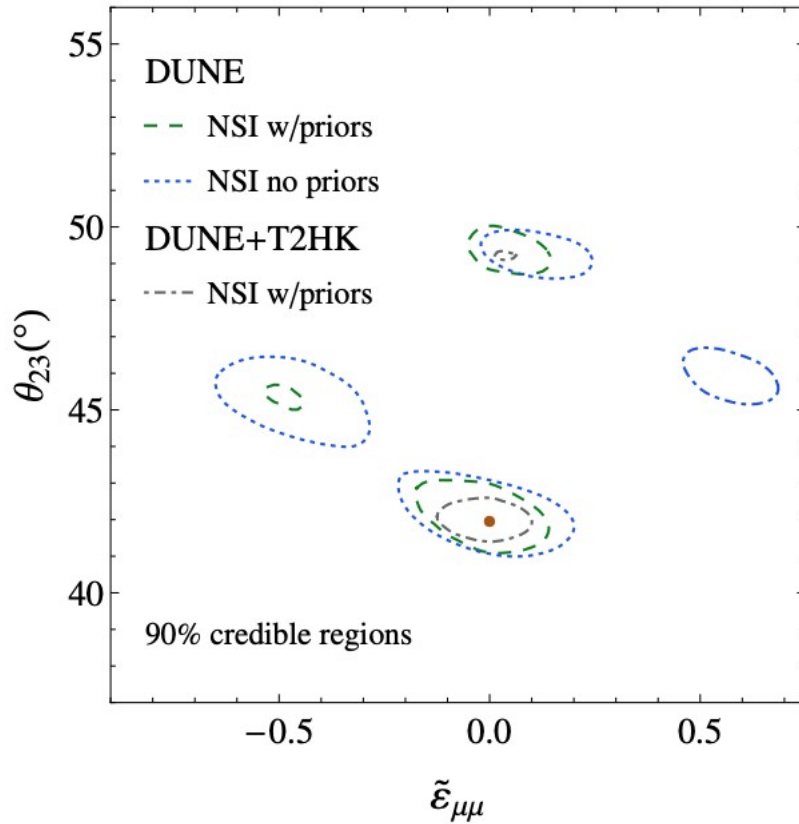
$$\epsilon_{ee}^m = -\alpha_{ee}$$

$$\epsilon_{\mu\mu}^m = \alpha_{\mu\mu}$$

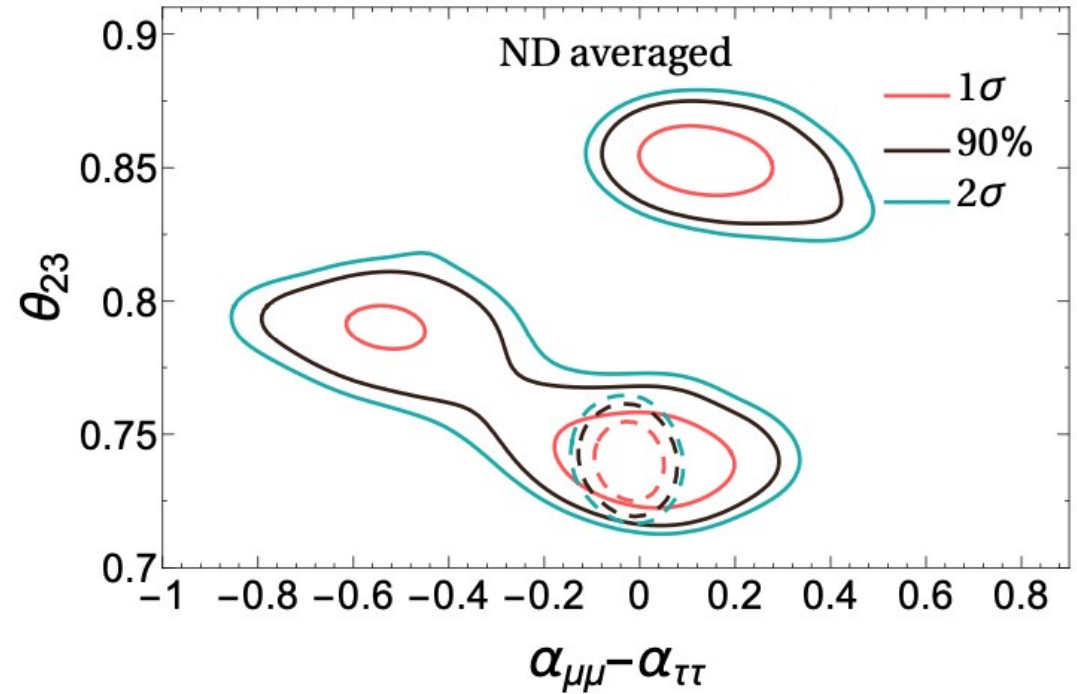
$$\epsilon_{\tau\tau}^m = \alpha_{\tau\tau}$$

$$\epsilon_{\alpha\beta}^m = \frac{1}{2}\alpha_{\beta\alpha}^*$$

NSI from non-unitarity



Coloma,1511.06357

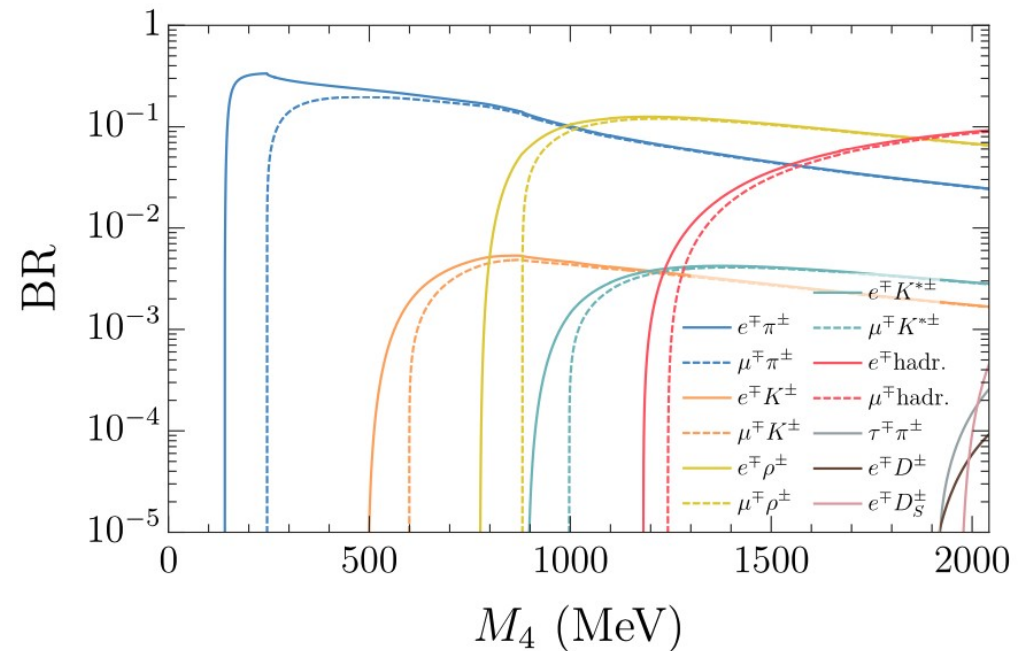
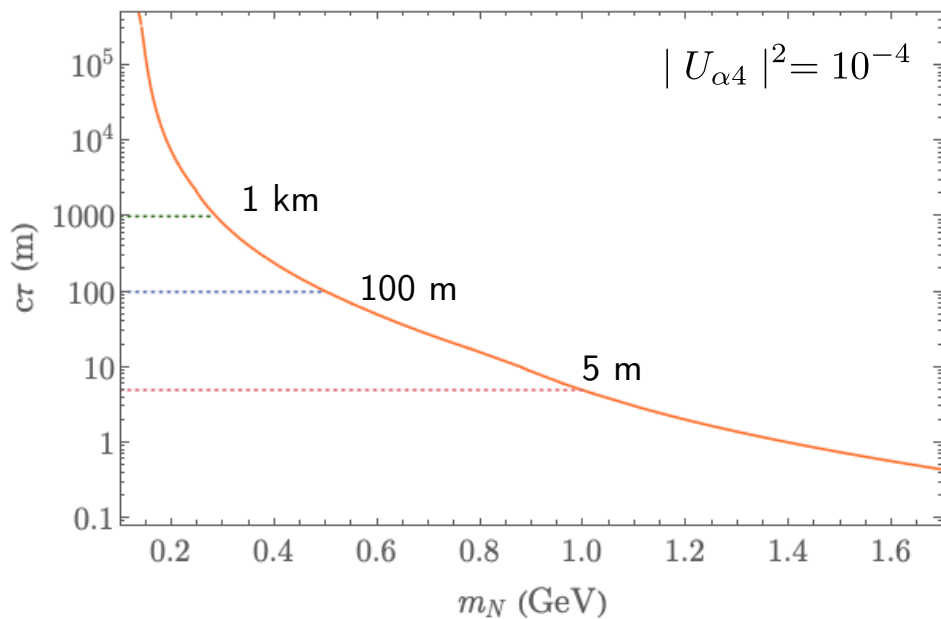
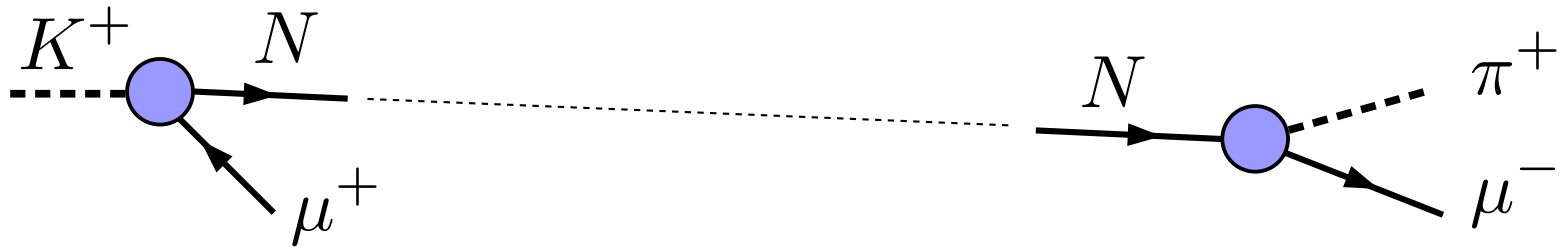


Blennow, Coloma, Fernandez-Martinez,
Hernandez-Garcia, Lopez-Pavon, 1609.08637

→ see also Agarwalla, Chatterjee and Palazzo, 1605.04299 for a similar effect with averaged-out sterile

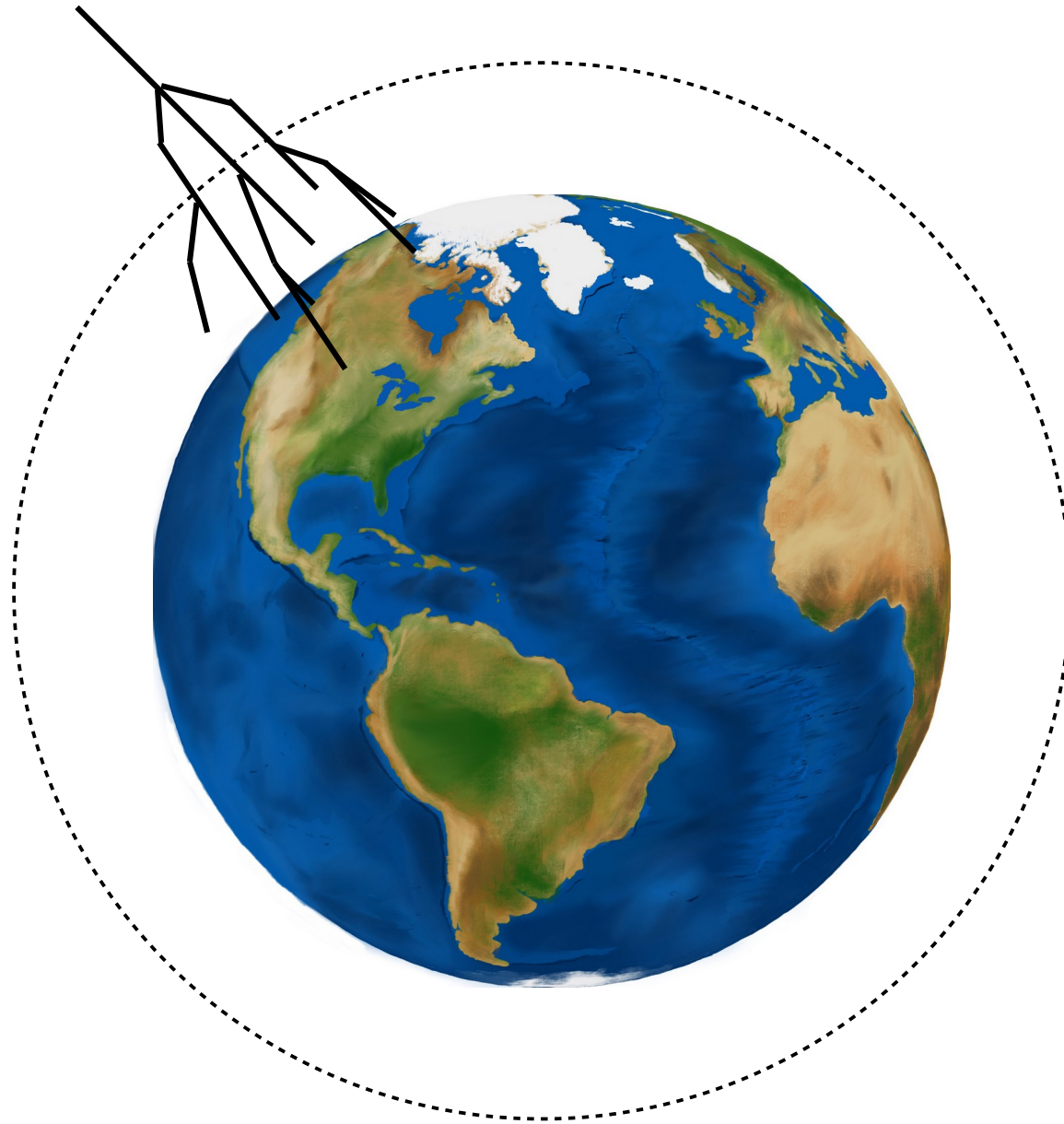
Displaced HNL decays

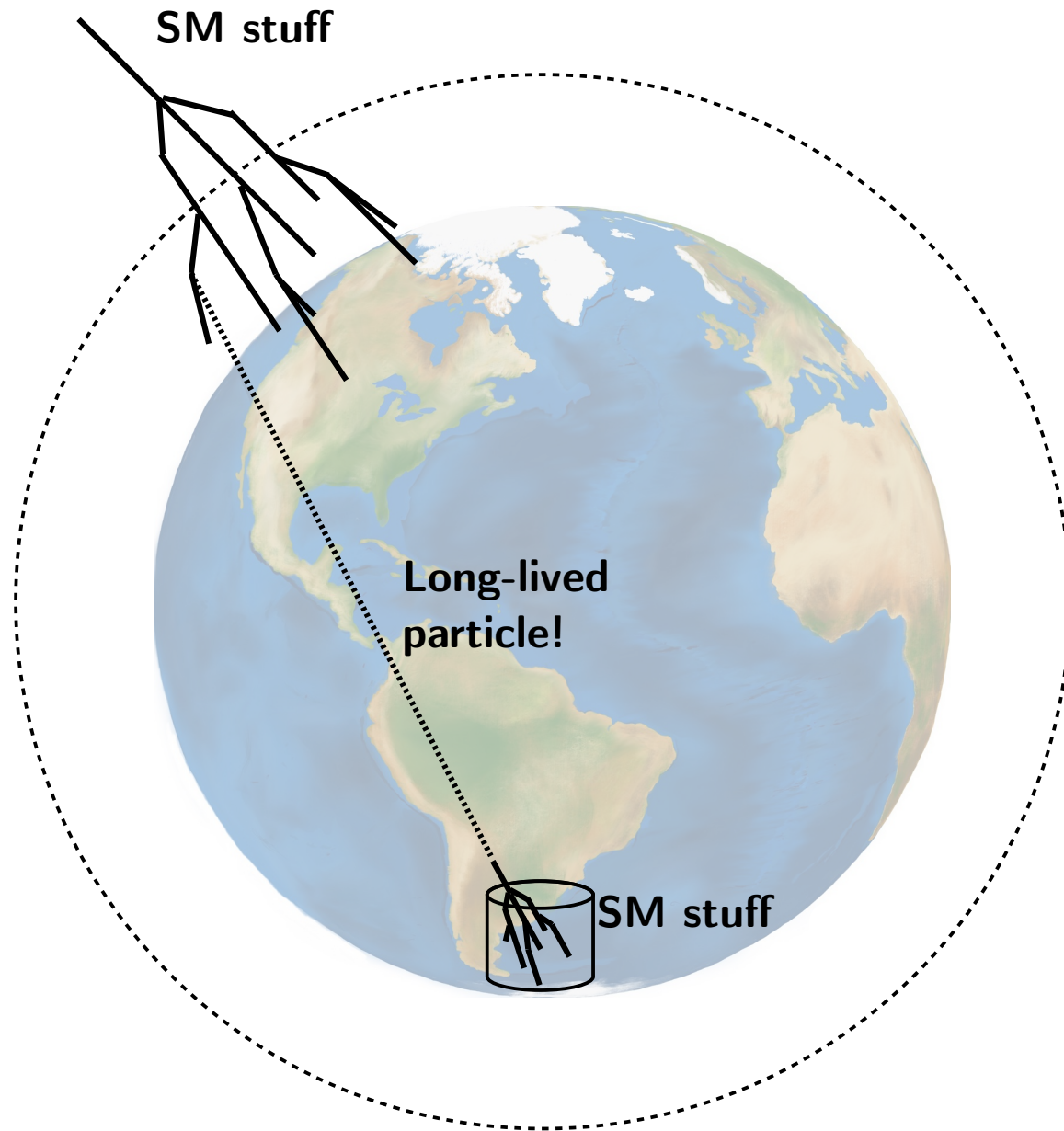
Displaced decays



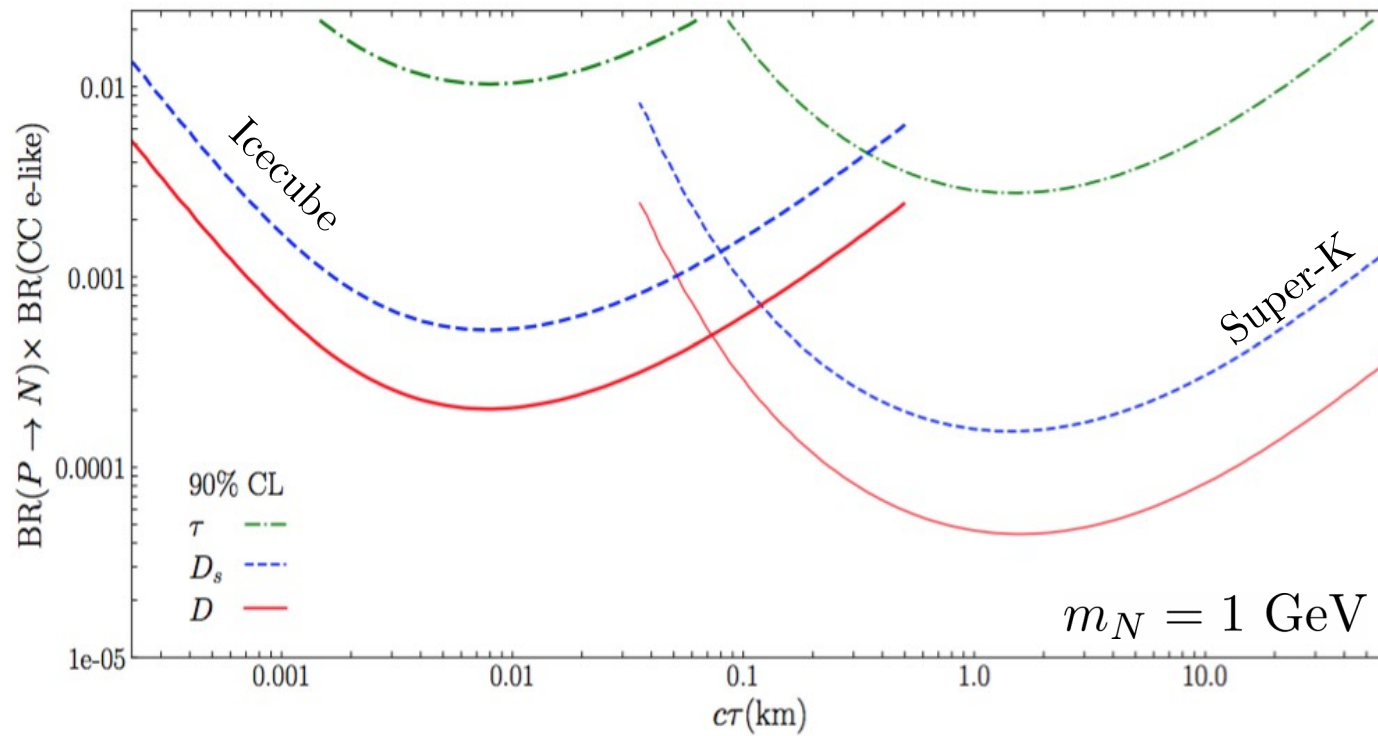
Coloma, Fernandez-Martinez, Gonzalez-Lopez, Hernandez-Garcia, Pavlovic, 2007.03701

See also works by Ballett, Boschi & Pascoli, Berryman et al, Bondarenko et al, Breitbach et al, Shrock, Drewes & Garbrecht, Krasnov, ...





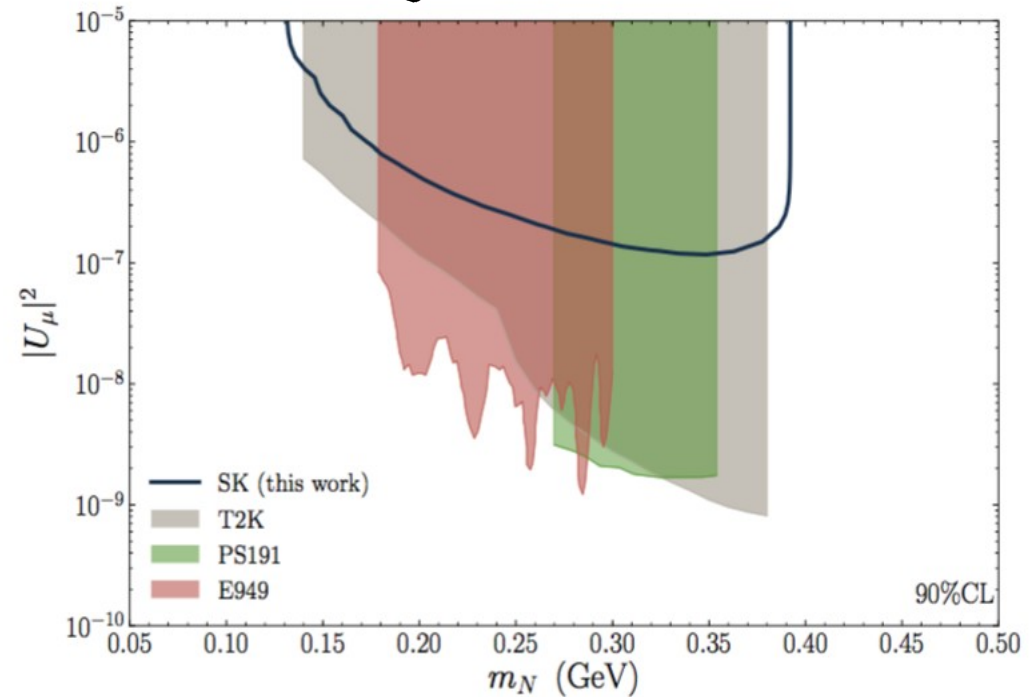
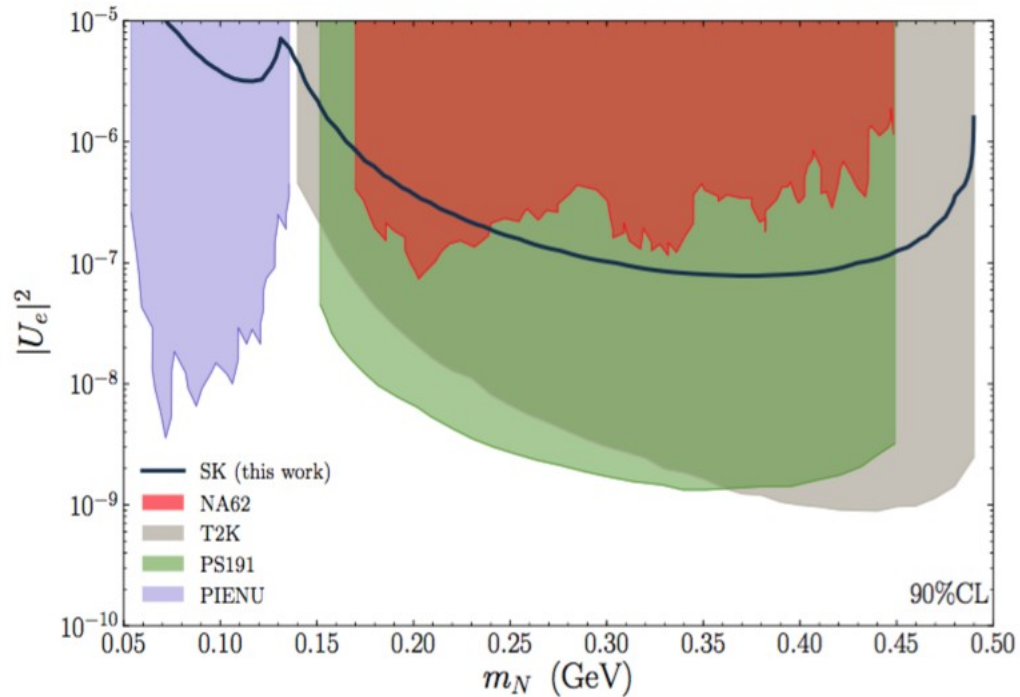
HNL **above** the kaon mass



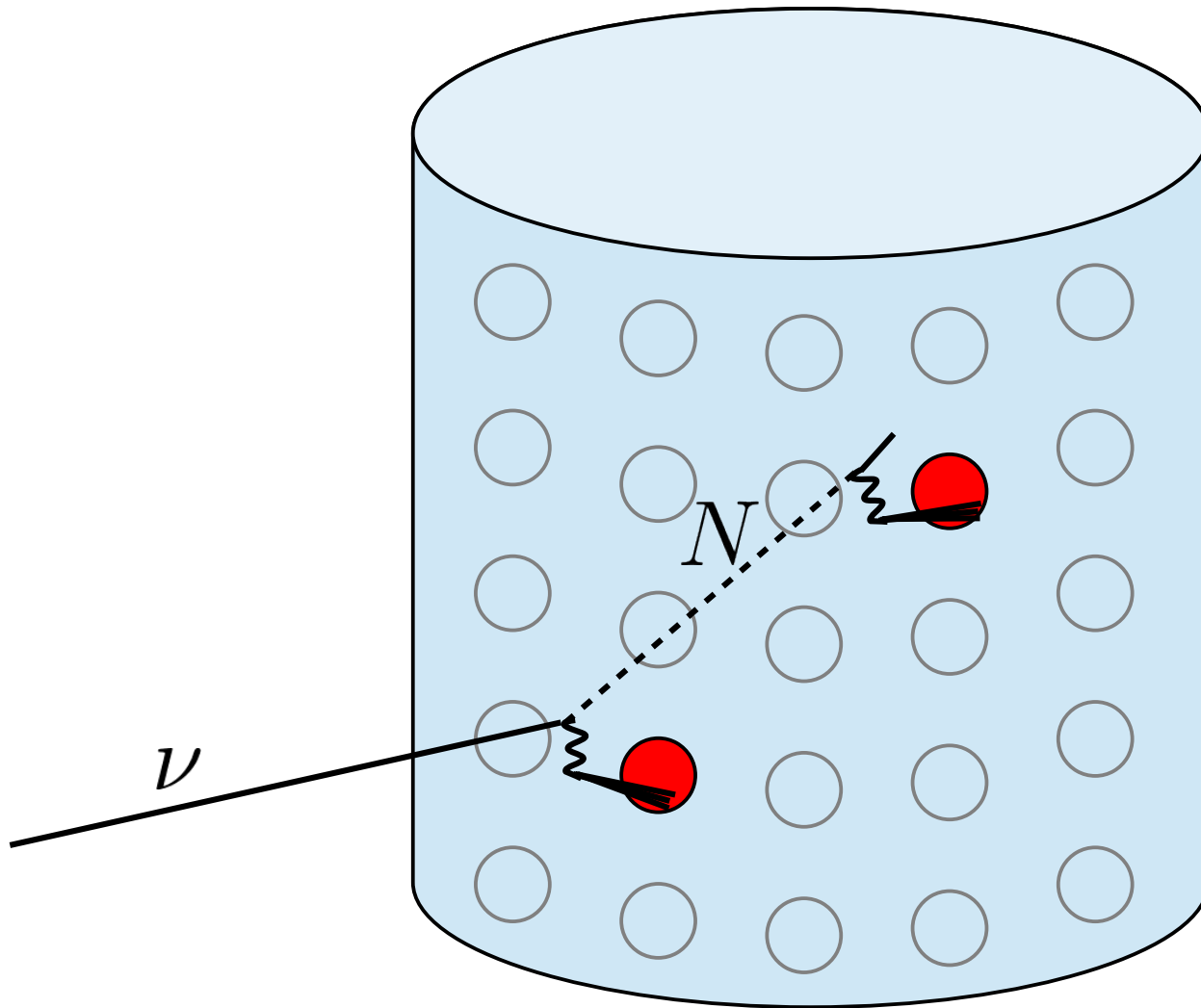
Argüelles, Coloma, Hernandez, Muñoz, 1910.12839

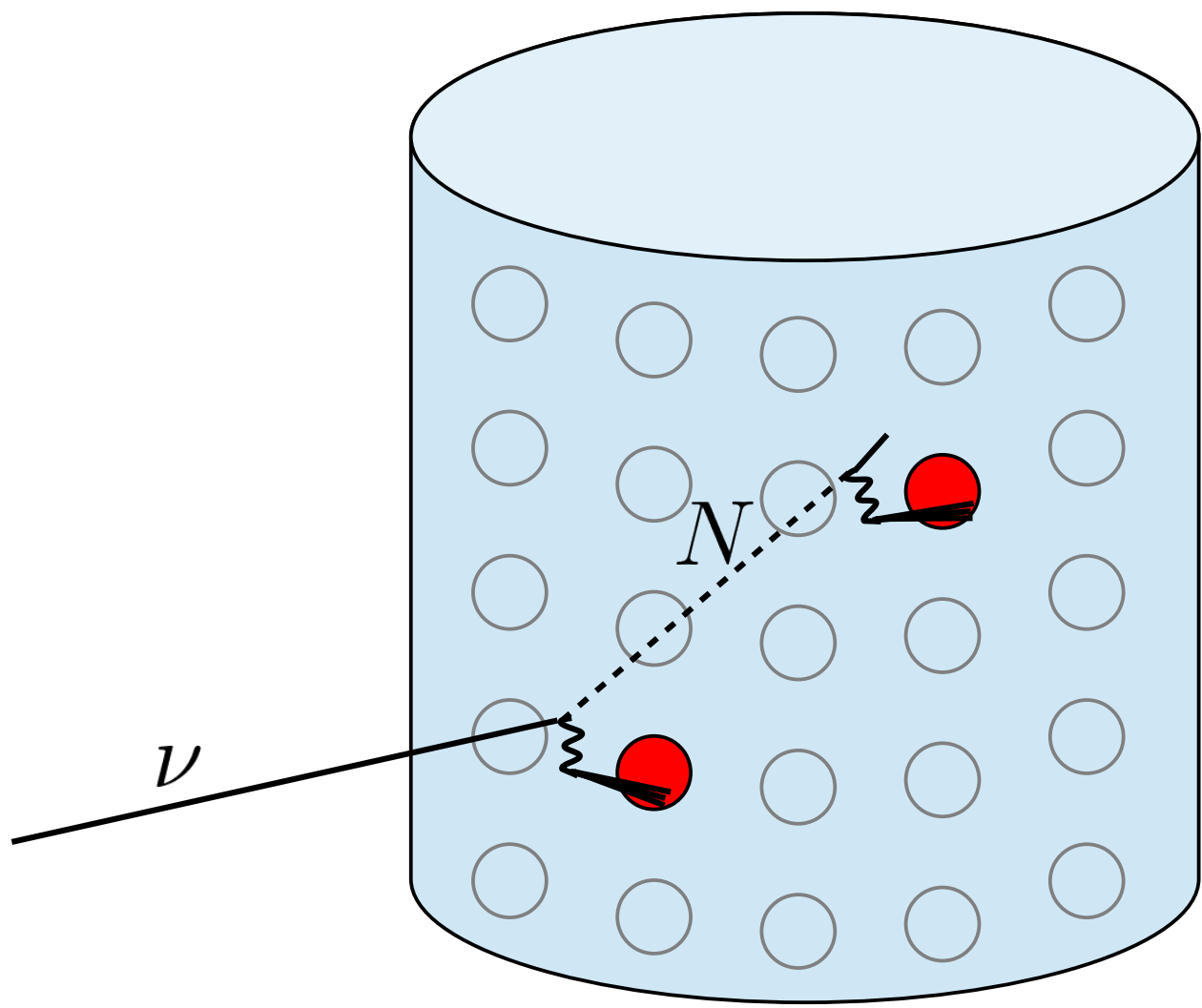
HNL below the kaon mass

→ See talk by Víctor Muñoz on Feb 25th!

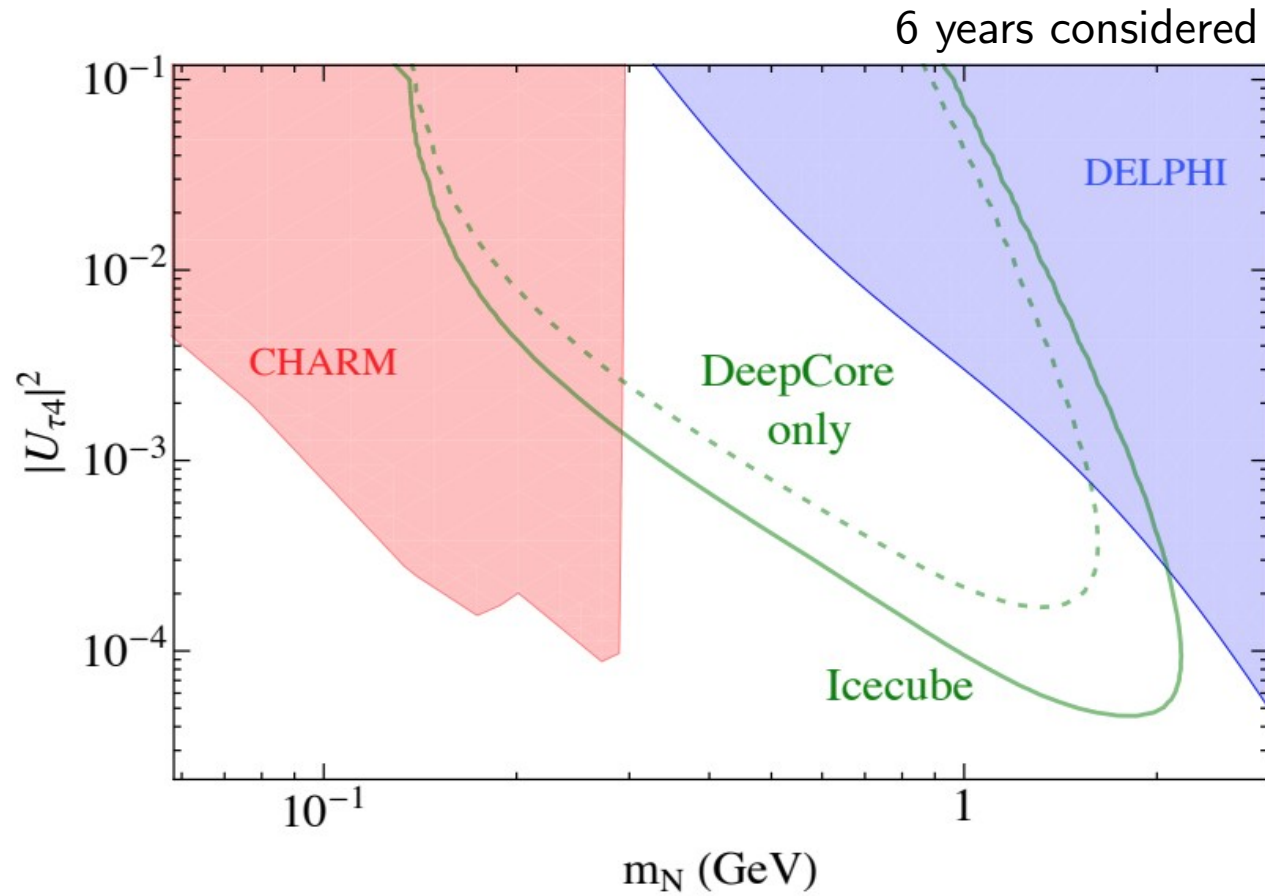


Coloma, Hernandez, Muñoz, Shoemaker, 1911.09129
(see also Asaka and Watanabe, 1202.0725, Kusenko, Pascoli and Semikoz, hep-ph/0405198)





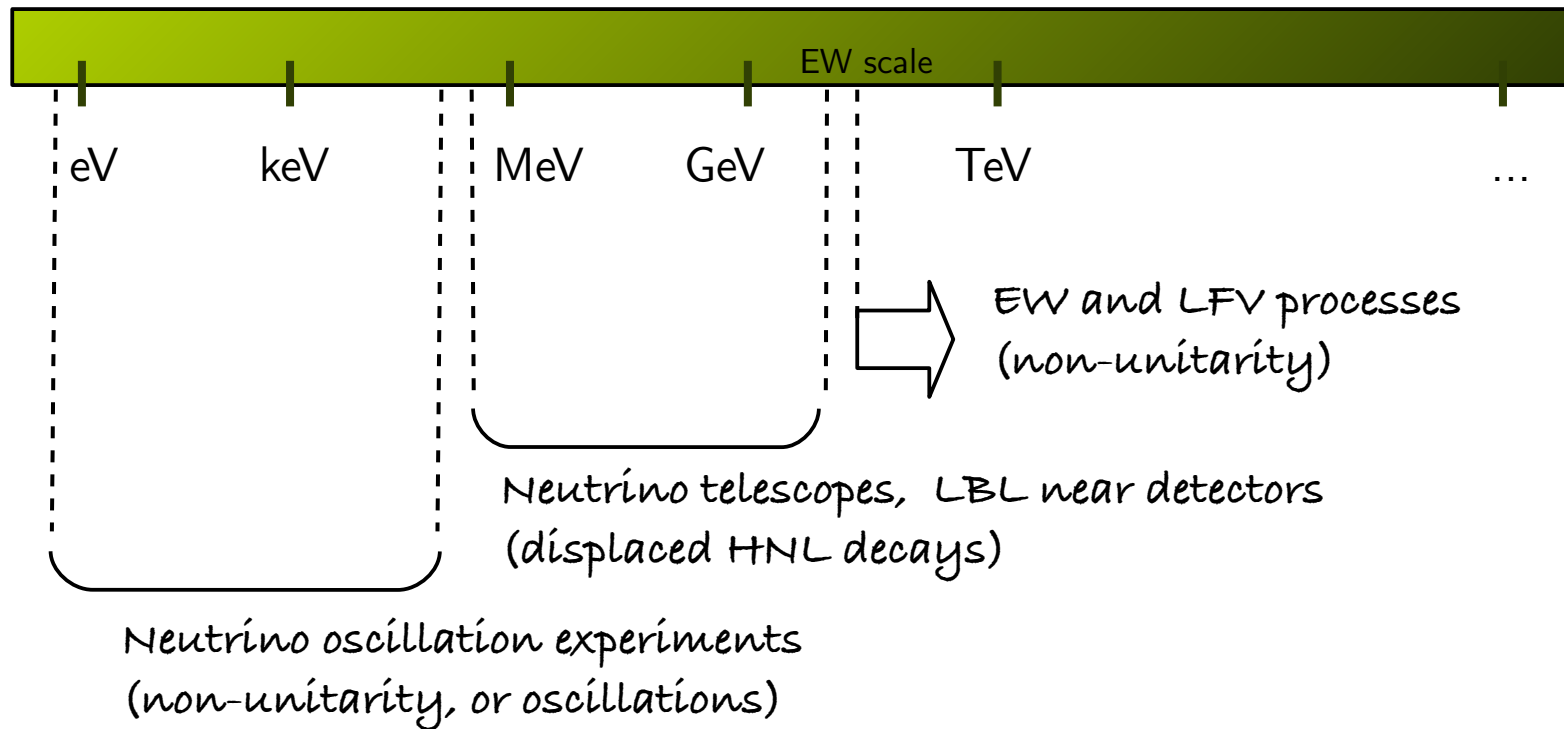
Double-bangs at low energies



Coloma, Machado, Martinez-Soler and Shoemaker, 1707.08573

Summary and conclusions

Many ways to probe the existence of sterile neutrinos in neutrino experiments at very different scales:



Thank you!!