

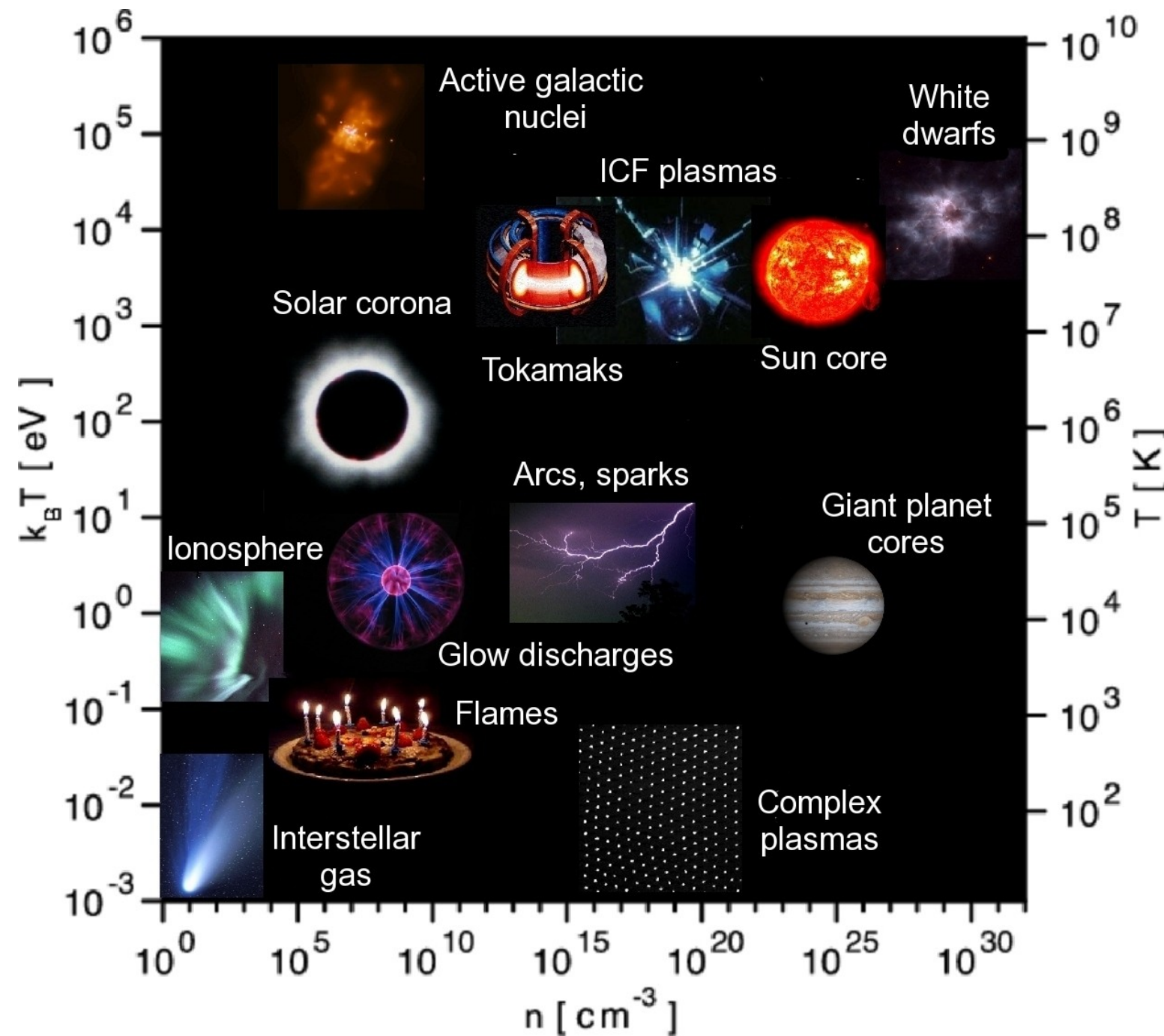
Resonant control of Kelvin-Helmholtz modes of arbitrary wavenumber by rotating electric fields in magnetized nonneutral plasmas

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WHAT IS PLASMA?



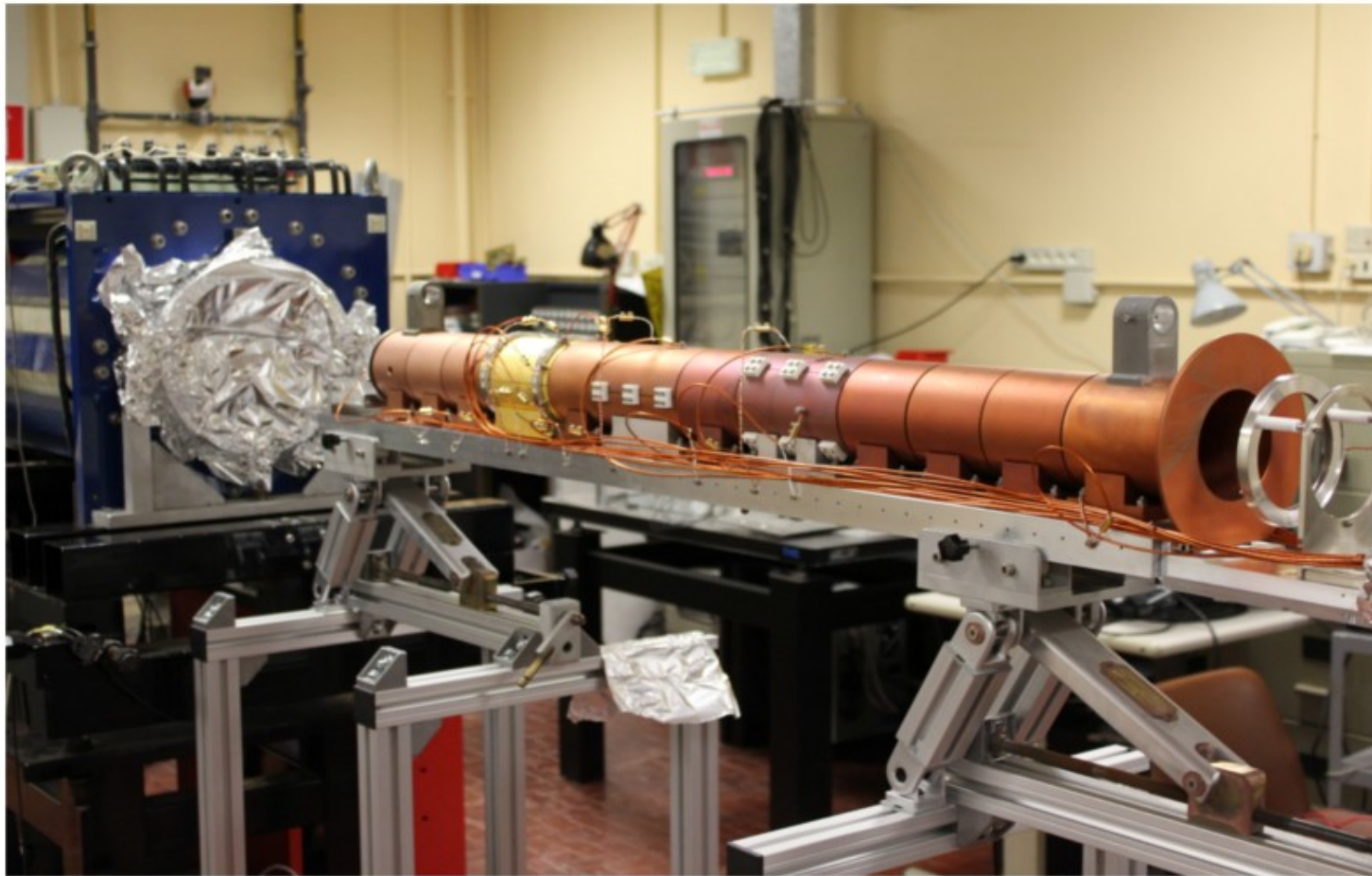
Neutral plasma:

$$\sum Q_i = 0$$

Nonneutral plasma:

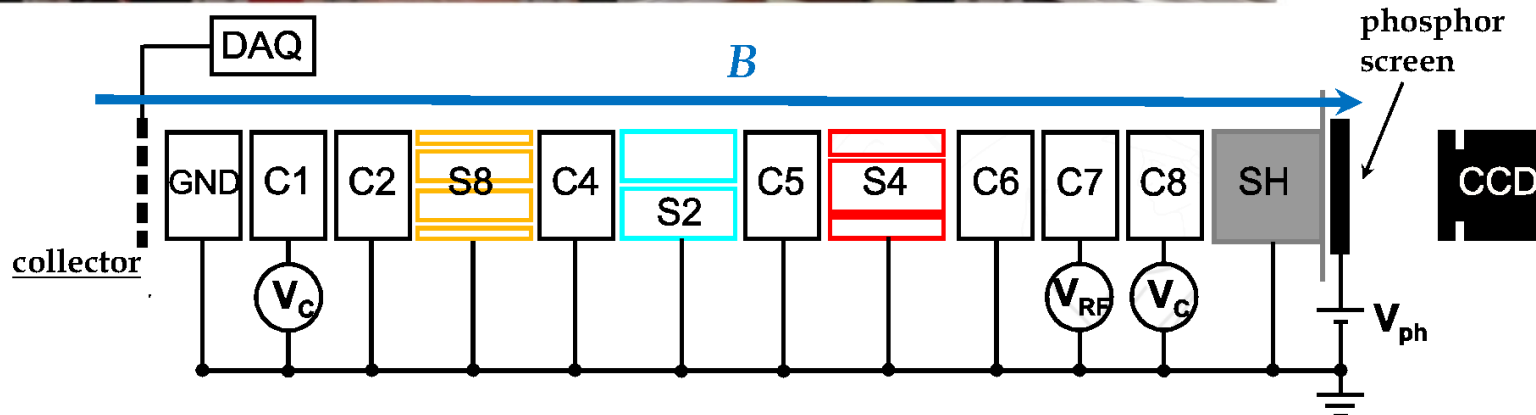
$$\sum Q_i \neq 0$$

ELTRAP



- $L < 1$ m
- $\varnothing = 90$ mm
- $B < 0.2$ T
- $V_{\text{con}} = \pm 100$ V
- $p \sim 10^{-8}$ mbar

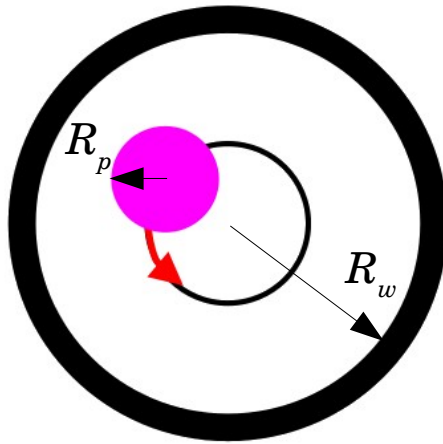
- $n_e \sim 10^7 \text{ cm}^{-3}$
- $\nu_{\text{lon}} \sim \text{MHz}$
- $\nu_{E \times B} \sim \text{kHz}$
- $T_e \sim 10$ eV



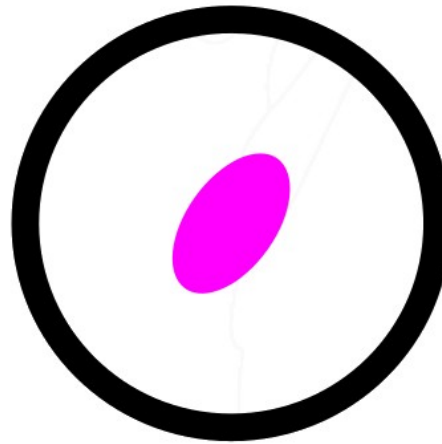
FLUID ANALOGY

2D Ideal Fluid	2D Electron Plasma
$\frac{\partial \zeta}{\partial t} + \mathbf{v} \cdot \nabla \zeta = 0$	$\frac{\partial n}{\partial t} + \mathbf{v} \cdot \nabla n = 0$
$\nabla^2 \psi = \zeta$	$\nabla^2 \phi = 4\pi e n$
$\mathbf{v} = \mathbf{e}_z \times \nabla \psi$	$\mathbf{v} = \frac{\mathbf{e}_z \times \nabla \phi}{B} c$
$\zeta = (\nabla \times \mathbf{v}) \cdot \mathbf{e}_z$	$\zeta = \frac{c}{B} \nabla^2 \phi = \frac{4\pi e c}{B} n$
$\psi(\text{wall}) = \text{constant}$	$\phi(\text{wall}) = \text{constant}$

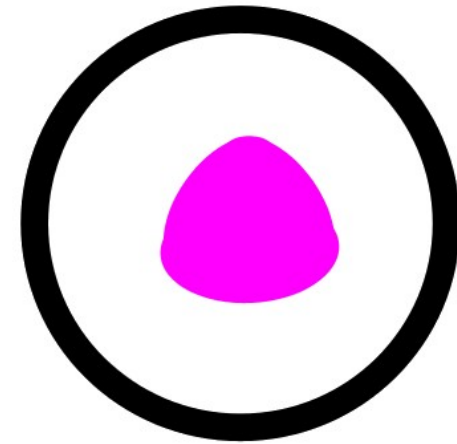
DIOCOTRON MODE



$l = 1$



$l = 2$



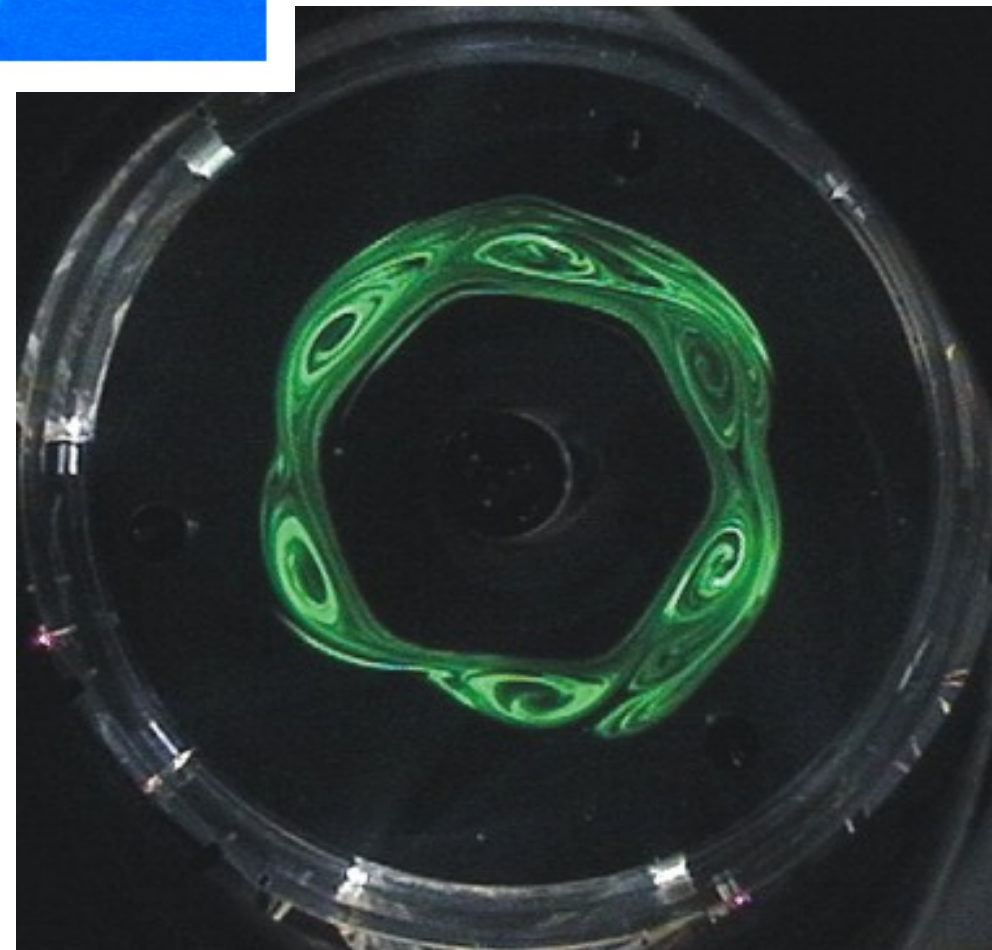
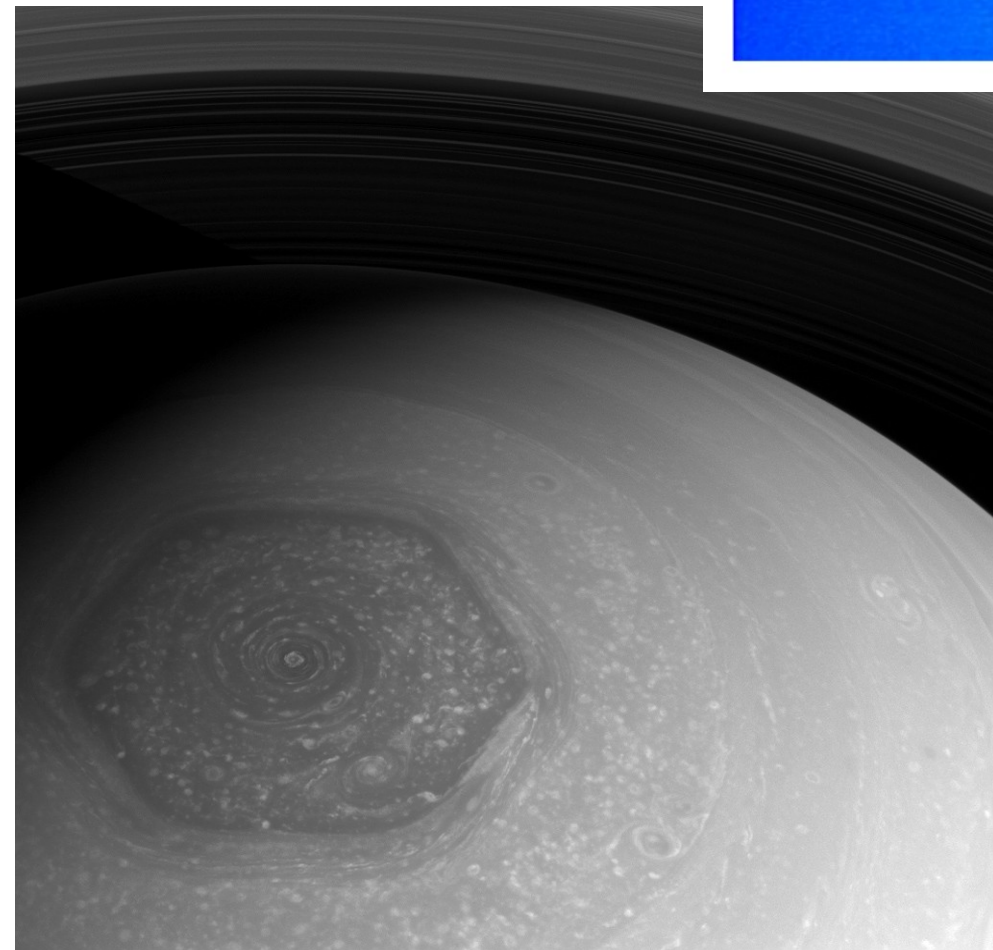
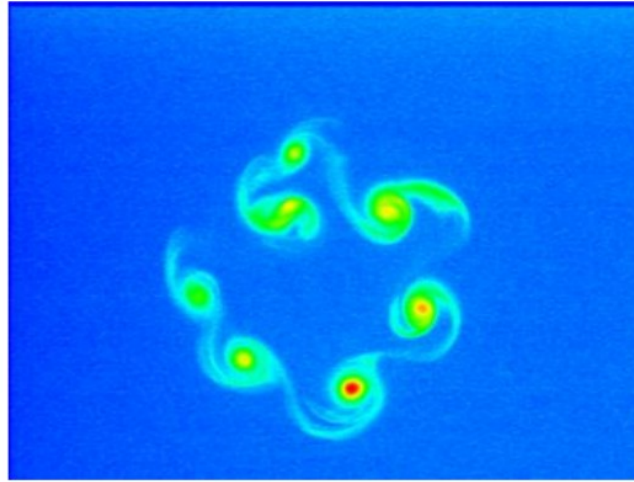
$l = 3$

$$n_e(r, \theta, t) = n_e^0(r) + \sum_{l=-\infty}^{\infty} \delta n_e^l(r) \exp(il\theta - i\omega t)$$

$$\phi(r, \theta, t) = \phi^0(r) + \sum_{l=-\infty}^{\infty} \delta \phi^l(r) \exp(il\theta - i\omega t)$$

$$\Omega_l = \frac{n_e e}{2\epsilon_0 B} \left(l - 1 + \left(\frac{R_p}{R_w} \right)^{2l} \right)$$

FLUID STRUCTURES IN NATURE AND IN LABORATORY



ROTATING ELECTRIC FIELD TECHNIQUE

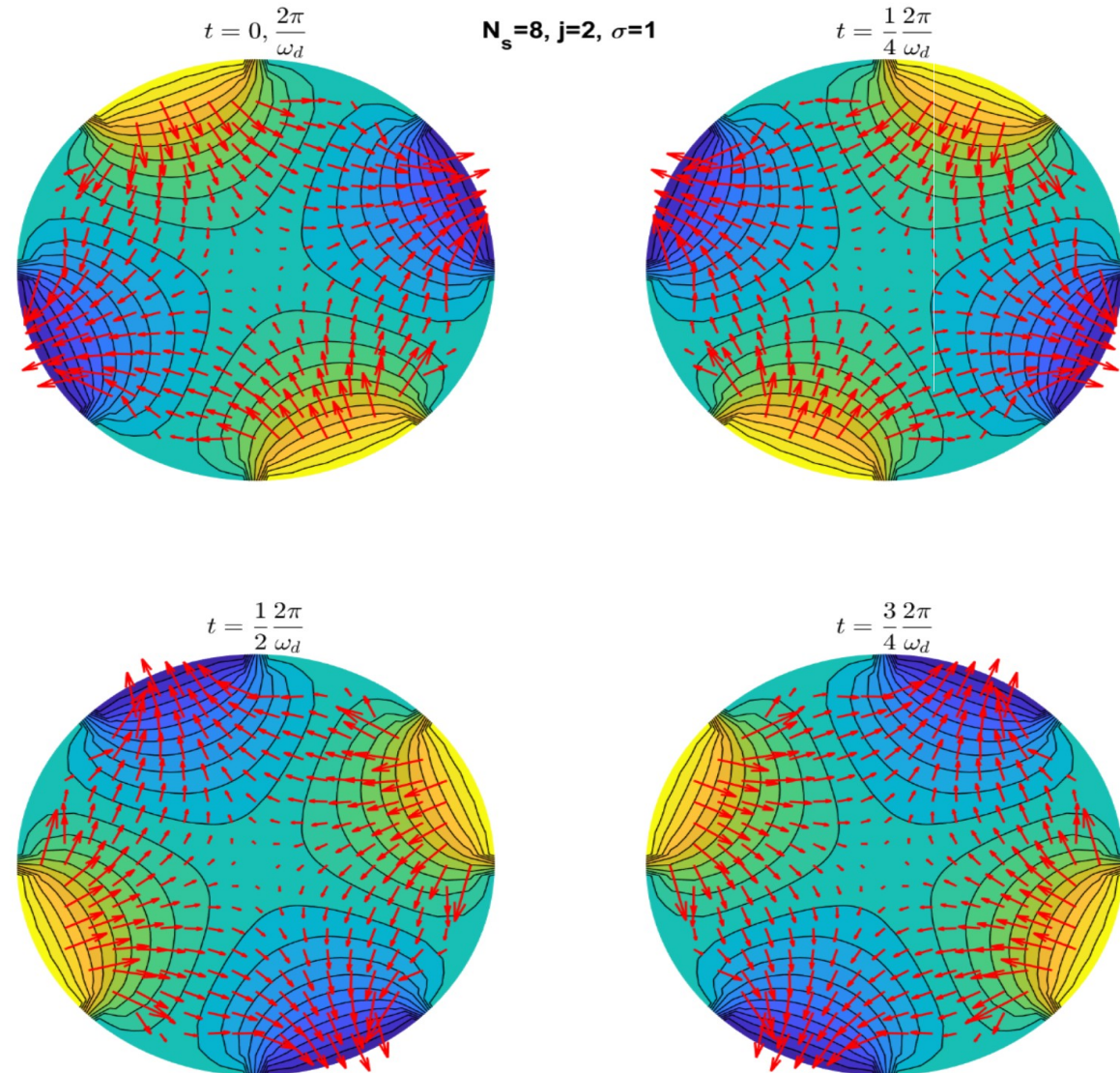
$$\delta\phi(r = R_w, \theta, t) = \sum_{m=0}^{N_s-1} V_m(t) [H(\theta - 2m\pi / N_s) - H(\theta - 2(m+1)\pi / N_s)]$$

$$V_m = V_d \cos(\omega_d t + 2\pi\sigma mj / N_s)$$

$$m = 0, \dots, N_s - 1$$

$$j = 1, \dots, N_s / 2$$

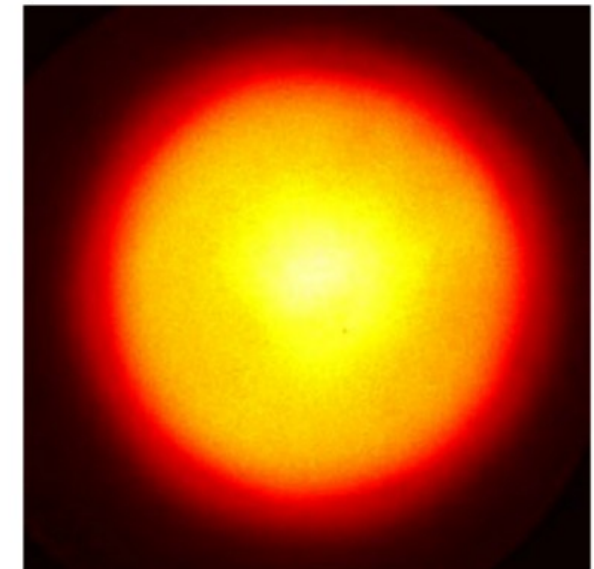
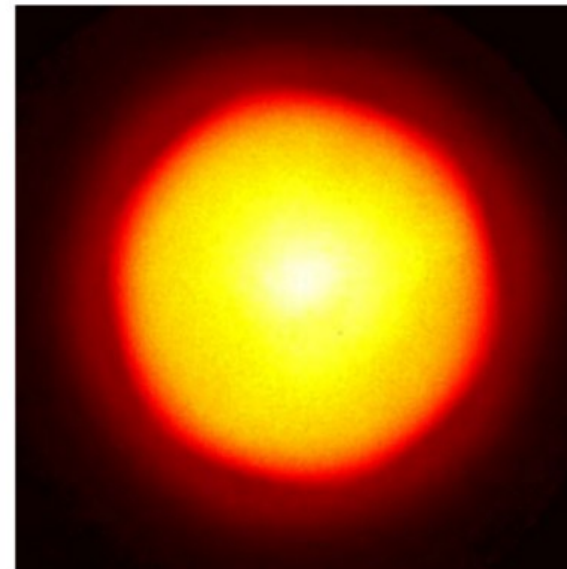
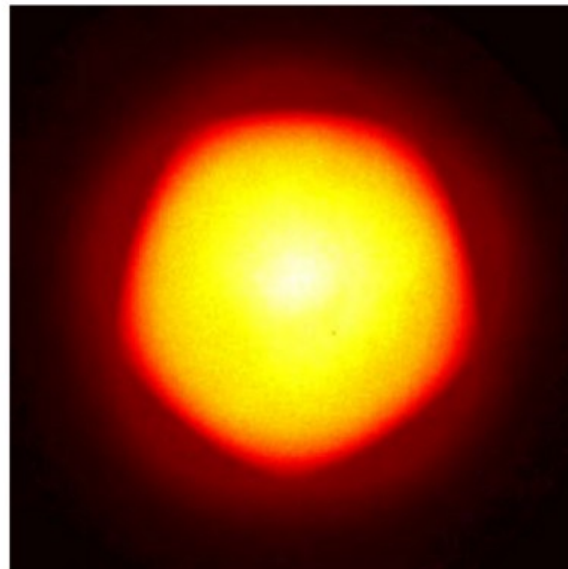
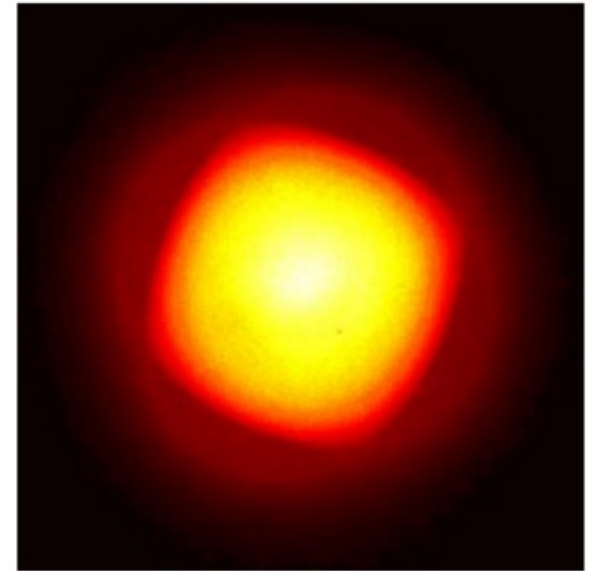
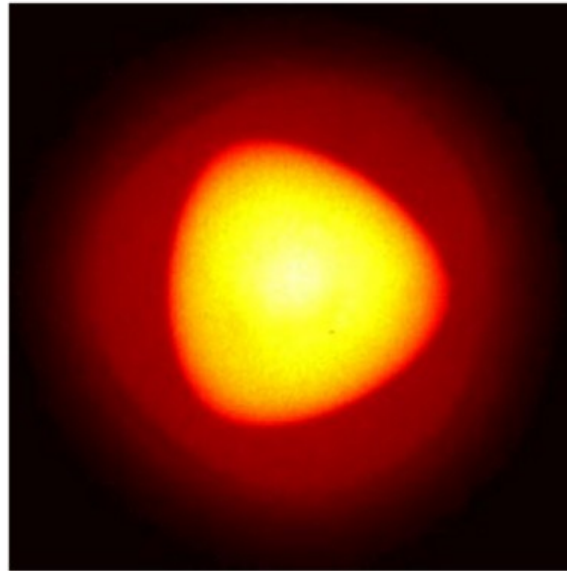
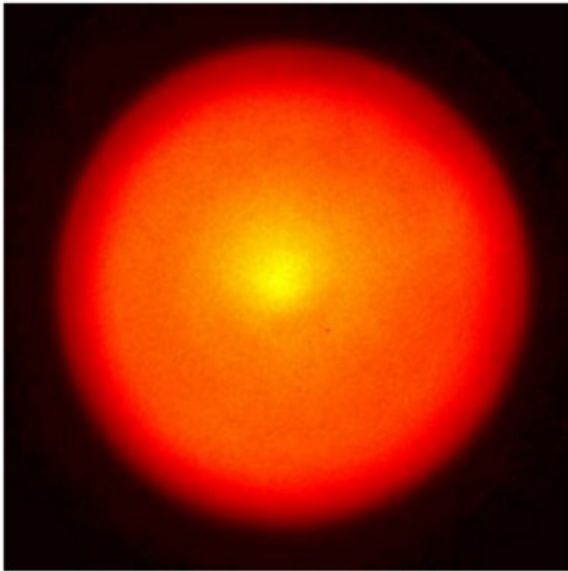
$$N_s = 8$$



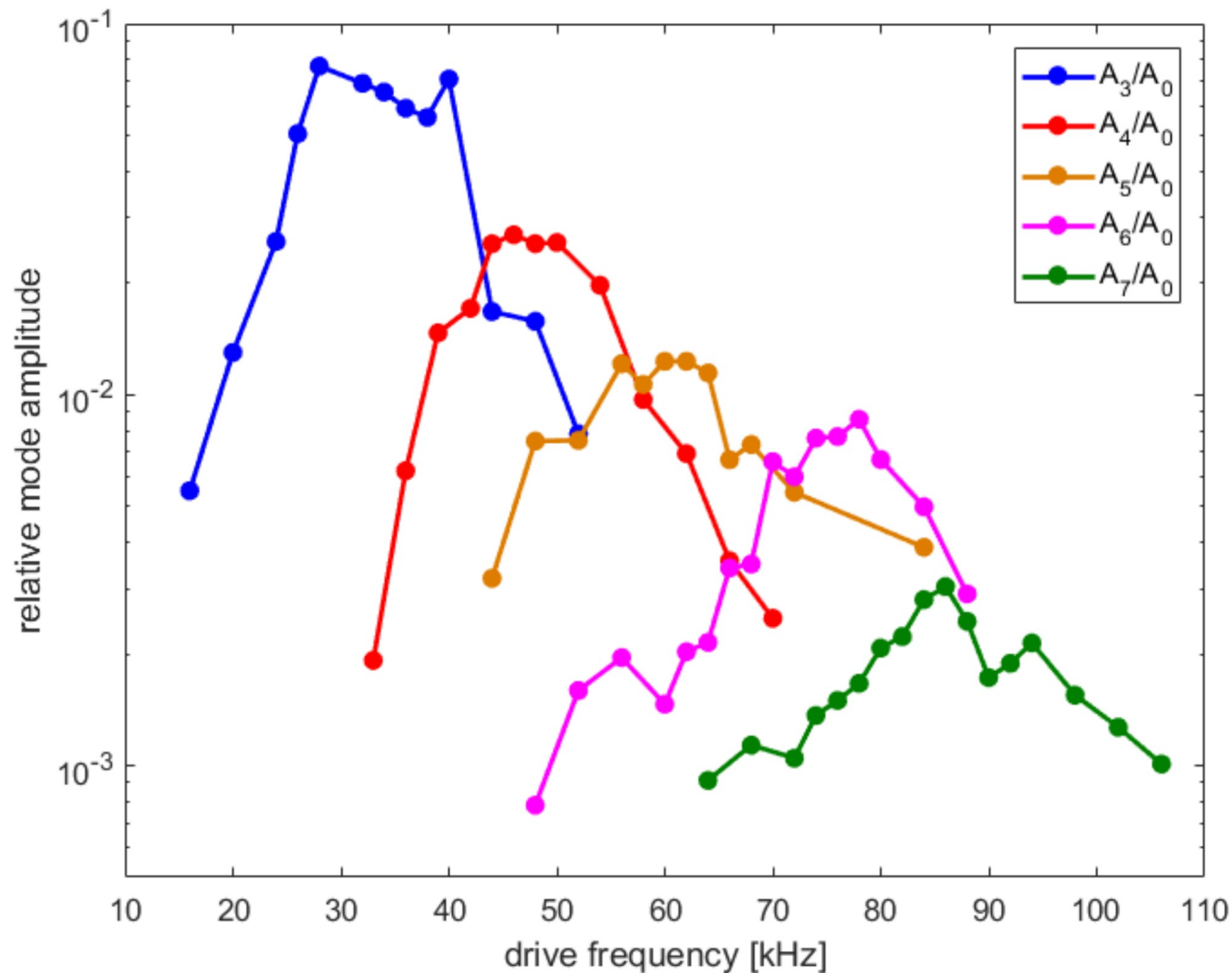
	excited modes		applied drive
j	$\sigma=-1$	$\sigma=+1$	
1	$l=8k+1$	$l=8k+7$	rotating dipole
2	$l=8k+2$	$l=8k+6$	rotating quadrupole
3	$l=8k+3$	$l=8k+5$	rotating sextupole
4	$l=8k+4$	$l=8k+4$	non-rotating octupole

$$k=0,1,2,\dots$$

RESONANT DIOCOTRON MODE EXCITATION



RESONANT DIOCOTRON MODE EXCITATION



- $t_{\text{exc}} \sim 100 \text{ ms}$
- $\Phi_{\text{exc}} \sim 3 \text{ V}$
- $\Phi_{\text{plasma}} \sim 20 \text{ V}$

In this work, we show an experimental technique to control Kelvin-Helmholtz modes of arbitrary wavenumber by rotating electric fields in magnetized nonneutral plasmas. The results are in good agreement with theoretical predictions, proving this technique to be a useful tool in the study and control of fluid instabilities. In the future we are going to

- 1) Study the nonlinear relationship between wave frequency and amplitude.
- 2) Provide a more thorough characterization of the cascade decay of the modes and their damping.
- 3) Observe nonlinear dynamics of the wave growth and accurately control the amplitude via autoresonant excitation.