FRUSTRATION OF BEING ODD

Vanja Marić

Collaborators: Fabio Franchini, Salvatore Marco Giampaolo, Domagoj Kuić



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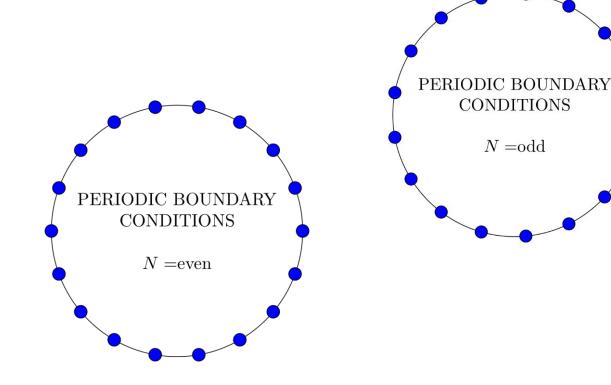


MANY-BODY SYSTEMS WITH LOCAL INTERACTIONS

• Typical expectation:

The effects of boundary conditions are negligible.

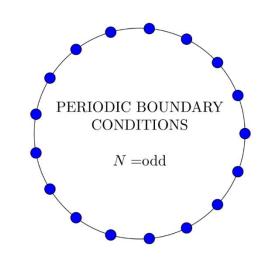
 We show that this expectation can be wrong.



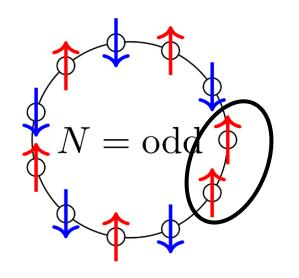
OPEN BOUNDARY CONDITIONS

• Studied system: Quantum XY Chain

$$H = \sum_{j=1}^{N} \sigma_{j}^{x} \sigma_{j+1}^{x} + \lambda \sum_{j=1}^{N} \sigma_{j}^{y} \sigma_{j+1}^{y} , \ \lambda \in (-1, 1)$$



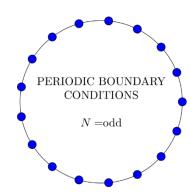
- Exactly solvable
- What is special about this setting?



Geometrical frustration

 Not all spins can be aligned oppositely from their nearest neighbors.

$$H = \sum_{j=1}^{N} \sigma_{j}^{x} \sigma_{j+1}^{x} + \lambda \sum_{j=1}^{N} \sigma_{j}^{y} \sigma_{j+1}^{y} , \ \lambda \in (-1, 1)$$



Idea:

- To solve the model and to compute the magnetization $\left<\sigma_j^x\right>_{\mathrm{GS}}$

References:

- [VM, SM Giampaolo, D Kuić, F Franchini. *The Frustration of being Odd: How Boundary Conditions can destroy Local Order* New Journal of Physics, 2020.]
- [VM, SM Giampaolo, F Franchini. *The Frustration of being Odd: Can Boundary Conditions induce a Quantum Phase Transition?* arXiv:2002.07197, 2020.]

Some mathematics had to be developed:

• [VM, F Franchini. Asymptotic behavior of Toeplitz determinants with delta function singularities—arXiv:2006.01922, 2020.]

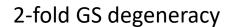
Results
$$H = \sum_{j=1}^{N} \sigma_j^x \sigma_{j+1}^x + \lambda \sum_{j=1}^{N} \sigma_j^y \sigma_{j+1}^y$$

Gapless System, Gap $\sim \frac{1}{N^2}$

$$\lambda = -1$$

$$\lambda = 0$$

$$\lambda = 1$$



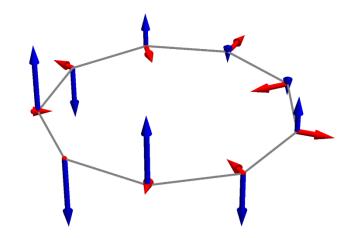
4-fold GS degeneracy

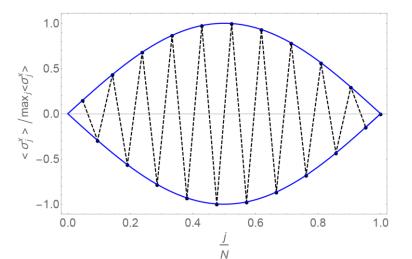
Mesoscopic Ferromagnetic Order

$$\langle \sigma_j^x \rangle_{\text{GS}} \simeq \frac{1}{N} (1 - \lambda^2)^{1/4}$$

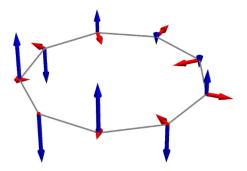
Incommensurate Antiferromagnetic Order

$$\left\langle \sigma_j^x \right\rangle_{\text{GS}} \simeq (-1)^j \frac{2}{\pi} (1 - \lambda^2)^{1/4} \cos \left(\pi \frac{j}{N} + \theta \right)$$





Conclusions



- Different boundary conditions can result in a different behavior of the order parameter of a quantum system.
- Quantum Phase Transition induced by a special choice of Boundary Conditions.

Other questions:

- How robust is the observed phenomenology to defects? [G Torre, VM, F Franchini, SM Giampaolo. *The Frustration of being Odd: effects of defects* arXiv:2008.08102, 2020.]
- Are there effects in other phases of matter? Topological, nematic...
 [VM, F Franchini, D Kuić, SM Giampaolo. The Frustration of being Odd: Resilience of the Topological Phases arXiv:2006.09397, 2020.]