

**3 sectors :** \* direct pair production  
of new heavy states...

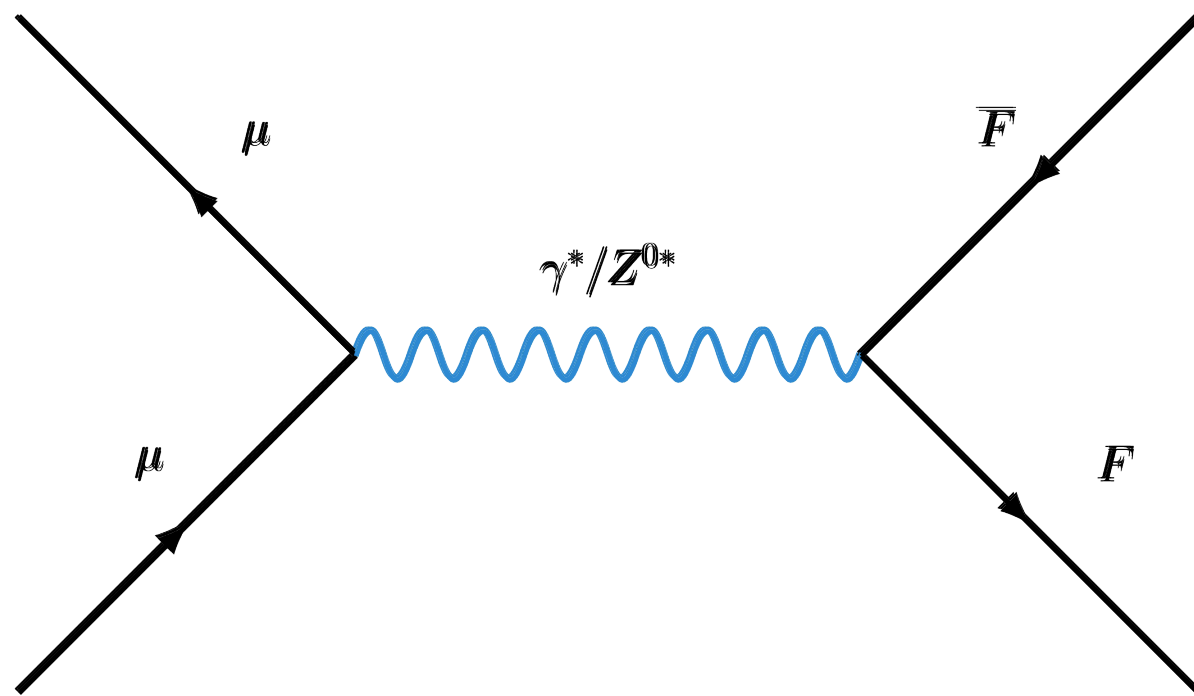
\*  $W^+W^- \rightarrow X \nu\nu$  (vs  $\mu^+\mu^- \rightarrow X$ )

\* indirect / off-shell / radiative  
effects of even heavier states

(e.g.  $\mu^+\mu^- \rightarrow Z'$  ( $M_{Z'} > \sqrt{S}$ ))

\* what can one do with muon collisions  
 @  $\sqrt{S_{\mu\mu}}$  up to tens of TeV ???

FIRST AND FOREMOST



$$\mu^+ \mu^- \rightarrow F \bar{F}$$

\* plain pair production  
 of new heavy states...

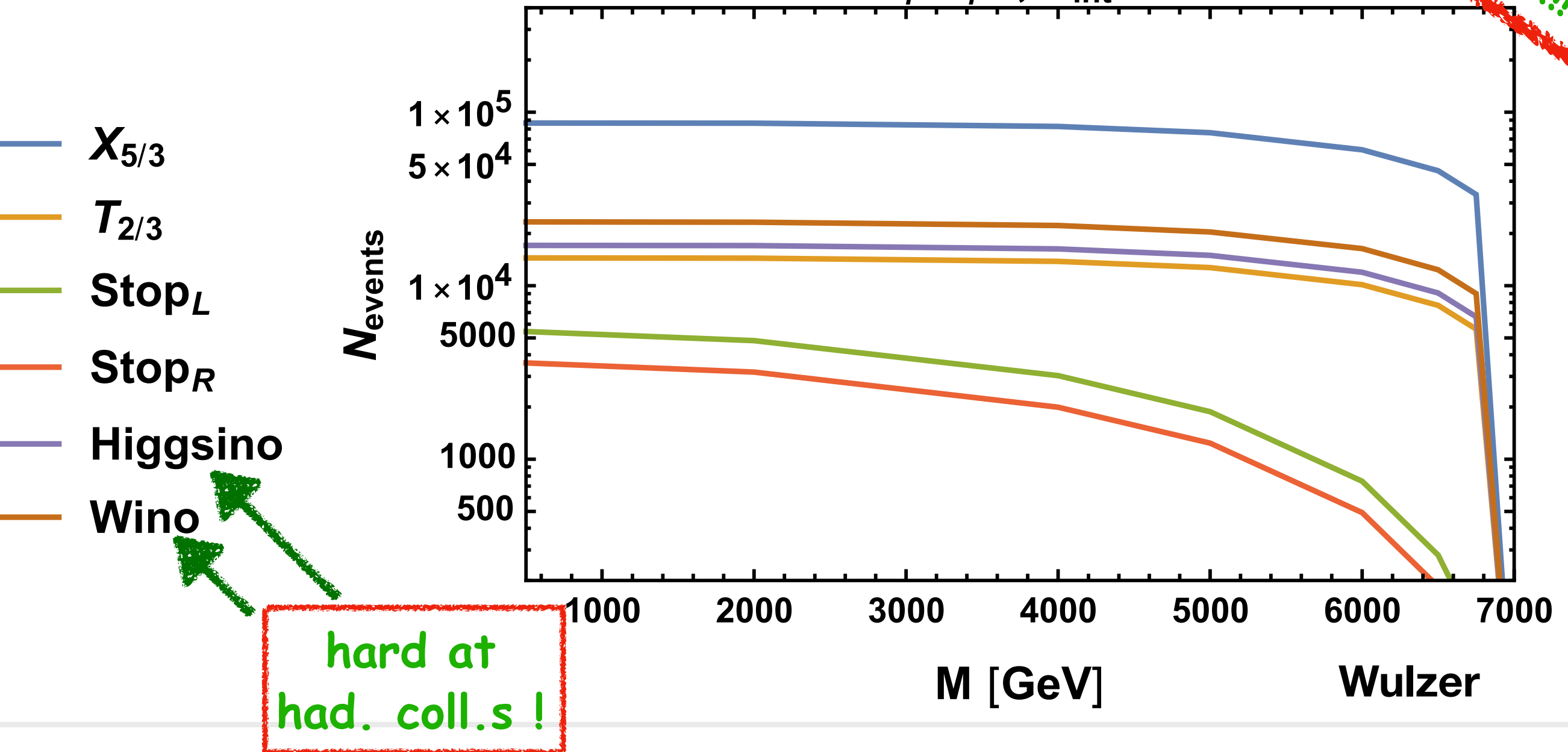
$$m_F \lesssim \sqrt{S_{\mu\mu}}/2$$

$$\sim 3, 5, 7, 15 \text{ TeV !!!}$$

# Direct production $\mu\mu \rightarrow XX$

in a clean environment !!!

14 TeV  $\mu^+ \mu^-$ ,  $L_{\text{int}}=20 \text{ ab}^{-1}$



$\sigma_{\mu\mu \rightarrow XX} \sim \text{uniform up to threshold } m_F \sim \sqrt{S_{\mu\mu}}/2 !$

# → Luminosity ruled by heavy pair x-section

rate for new p.le pair production :

$$\sigma_{EW} \sim \sigma(\mu^+ \mu^- \rightarrow \gamma^* \rightarrow e^+ e^-) \sim \frac{4\pi\alpha^2}{3S}$$

point x-section

$$\rightarrow 1 \text{ fb} \left( \frac{10 \text{ TeV}}{\sqrt{S}} \right)^2$$

no  $m_e$  dependence  
up to  $m_e \sim \sqrt{S}/2$  !

$$L \sim 10^{35} \text{ cm}^{-2} \text{ s}^{-1} \sim 1 \text{ ab}^{-1} / \text{y}$$

$$\rightarrow 1000 \text{ evs/y} \left( \frac{10 \text{ TeV}}{\sqrt{S}} \right)^2$$

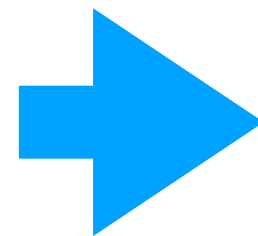
$\sqrt{S}_{\mu\mu}$

$\int L_{10y}$

10 TeV

10  $\text{ab}^{-1}$

$10^4 \text{ evs} / (10 \text{ years})$



14 TeV

20  $\text{ab}^{-1}$

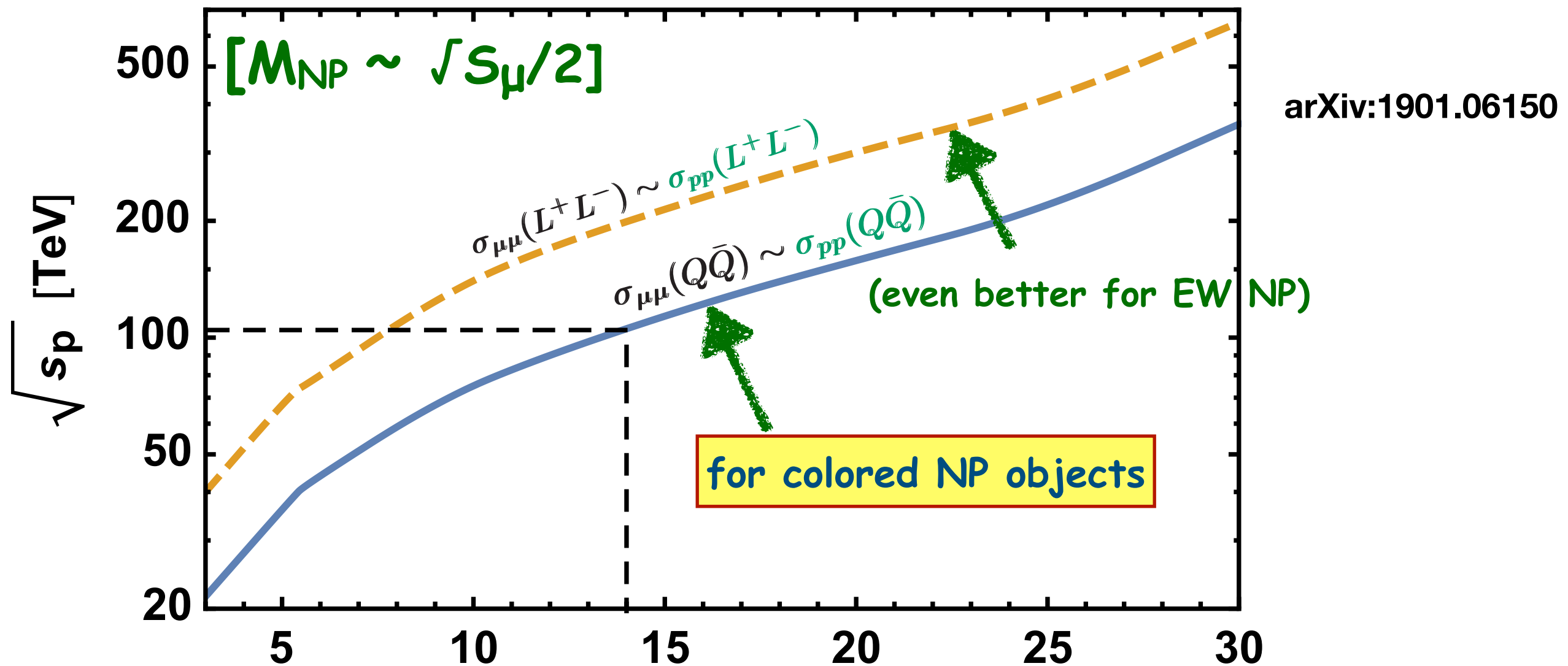
$\delta_{\text{stat}} \sim 1\%$

30 TeV

100  $\text{ab}^{-1}$

$$L \sim 10^{36} \text{ cm}^{-2} \text{ s}^{-1}$$

# "equivalent" reach in pp after rescaling for pdf's

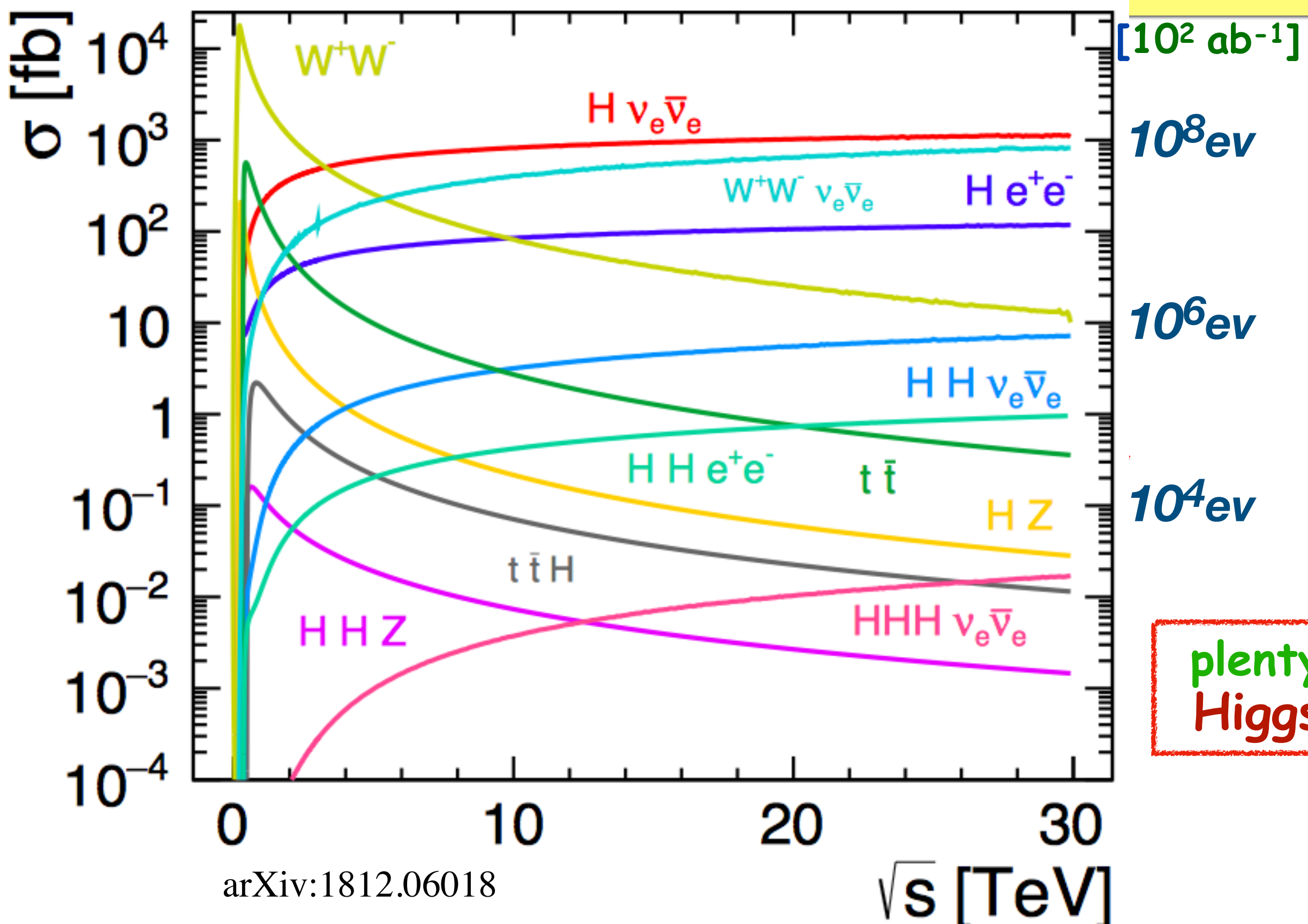


- $\sqrt{s_\mu}$  [TeV]
- \*  $\mu\mu$  @ 14 TeV  $\rightarrow$  pp @ 100 (200)<sub>EW</sub> TeV !
  - \*  $\mu\mu$  @ 30 TeV  $\rightarrow$  pp @ 350 (600)<sub>EW</sub> TeV !!
- yet unexplored pheno !!!*

# WARNING !!

- \* actually physical BACKGROUND  
to  $\mu^+\mu^-$  ( $e^+e^-$ ) collisions hugely better  
than in hadron collisions
- \* this moves equivalent  $\sqrt{S}_{\mu\mu}$  (at fixed  $\sqrt{S}_{pp}$ )  
at even lower values in general...

at  $\sqrt{S_{\mu\mu}} > \text{a few TeV's}$   
point  $\sigma_{\mu\mu \rightarrow X}$  superseded by  $\sigma_{WW \rightarrow X}$  !



plenty of  
Higgs's !

# # VBF events (green) + $\sigma_{WW \rightarrow X} / \sigma_{\mu\mu \rightarrow X}$ (red)

# events	3 TeV/5/ab	(VBF)/(s-ch)3TeV	14 TeV/20/ab	(VBF)/(s-ch)14TeV	30 TeV/100/ab	(VBF)/(s-ch)30TeV
<b>H</b>	2,5E+06		1,9E+07		1,2E+08	
<b>HZ</b>	4,9E+04	7	9,0E+05	700	7,4E+06	5300
<b>HZZ</b>	6,0E+02	1,5	3,2E+04	180	3,7E+05	1500
<b>HWW</b>	1,5E+03	0,3	6,8E+04	30	7,6E+05	190
<b>HH</b>	4,1E+03		8,8E+04		7,4E+05	
<b>HHZ</b>	4,7E+01	0,3	2,8E+03	40	3,3E+04	300
<b>HHZZ</b>	4,6E-01	0,1	7,8E+01	16	1,2E+03	130
<b>HHWW</b>	1,2E+00	0,02	1,8E+02	1	2,9E+03	1
<b>HHH</b>	1,5E+00		1,4E+02		1,9E+03	
<b>HHHZ</b>	2,4E-02	0,3	3,8E+00	12	5,1E+01	100

*[Maltoni et al]*

<b>tt</b>	2,6E+04	0,3	4,2E+05	24	3,1E+06	160
<b>ttH</b>	6,5E+01	0,03	3,0E+03	5	3,1E+04	40
<b>ttZ</b>	5,5E+02	0,07	2,6E+04	7	2,8E+05	50
<b>ttHH</b>	1,7E-01	0,006	1,3E+01	1	1,6E+02	10
<b>ttHZ</b>	1,8E+00	0,01	2,0E+02	2	2,7E+03	14
<b>ttZZ</b>	7,0E+00	0,03	1,2E+03	4	1,7E+04	30
<b>ttWW</b>	1,4E+01	0,008	2,2E+03	0,8	3,0E+04	5
<b>tttt</b>	3,4E-01	0,01	2,2E+01	0,4	2,1E+02	2



# brand new study on VBF vs s-channel

## Vector boson fusion at multi-TeV muon colliders

Costantini, De Lillo, Maltoni, Mantani, Mattelaer, Ruiz, Zhao  
arXiv:2005.10289v1 [hep-ph] 20 May 2020

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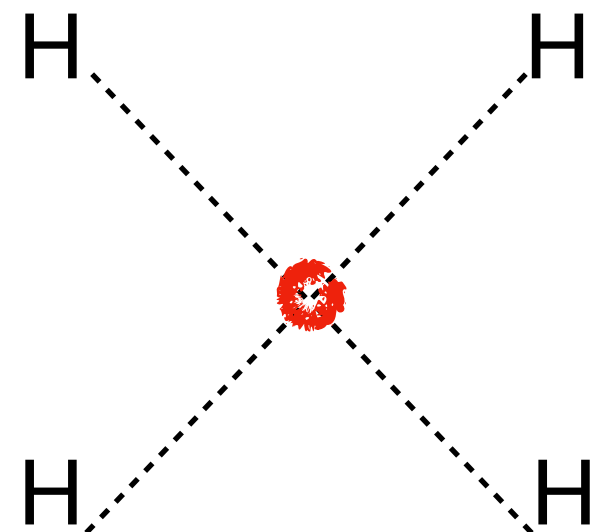
# Higgs self-interaction couplings

- \* the "tough topic" even at "most-future" colliders
- \* most interesting to measure from theory side....

$$\mathcal{L} = -\frac{1}{2}m_h^2 h^2 - \boxed{\lambda_3} \frac{m_h^2}{2v} h^3 - \boxed{\lambda_4} \frac{m_h^2}{8v^2} h^4$$

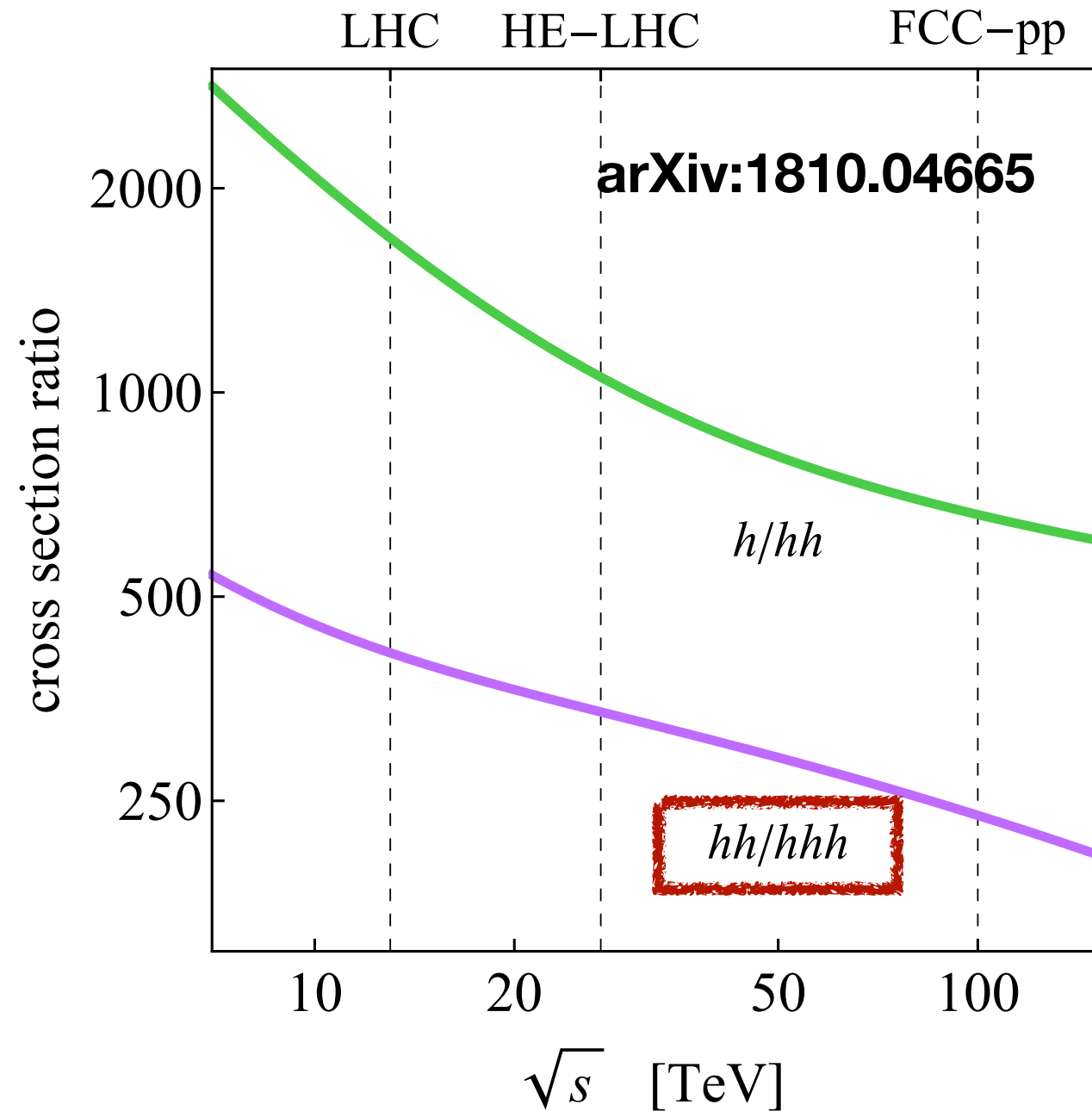
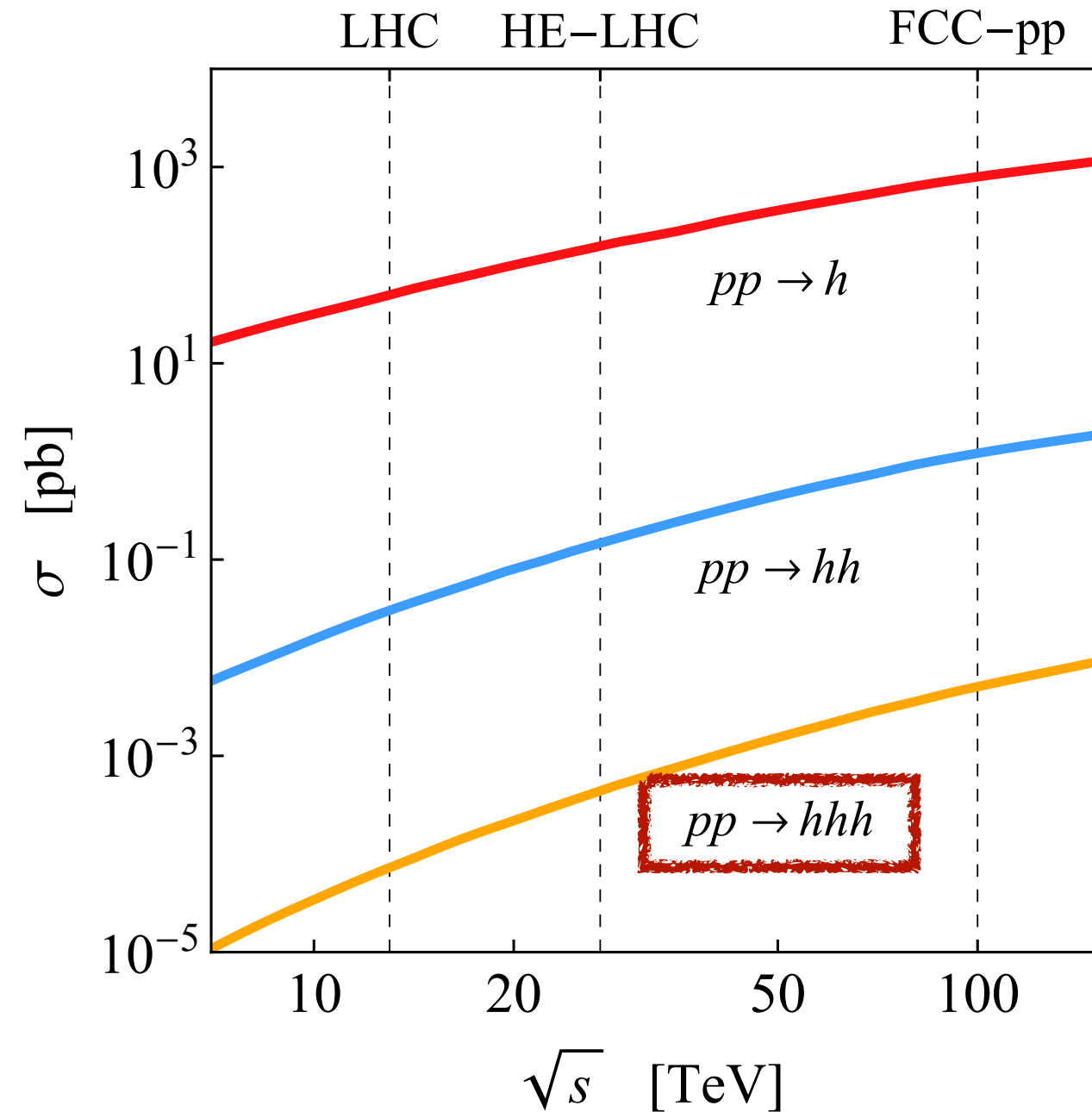
$$\lambda_3^{SM} = \lambda_4^{SM} = 1$$

what about **quartic**  
H self-coupling ?



**FCC-pp :  $\lambda_4$**

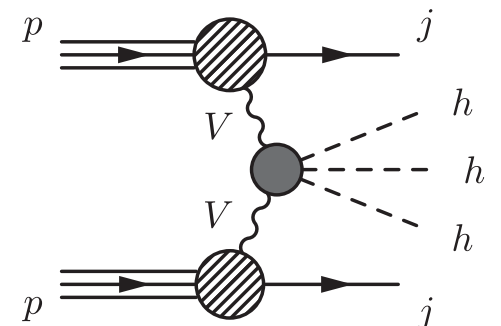
$$\mathcal{L} = -\frac{1}{2}m_h^2 h^2 - \lambda_3 \frac{m_h^2}{2v} h^3 - \boxed{\lambda_4 \frac{m_h^2}{8v^2} h^4}$$



**$hhh \rightarrow (b\bar{b})(b\bar{b})(\gamma\gamma)$  [optimistic scenario !!!] :**

**$\lambda_4 \in [\sim -4, \sim +16]$**   
(95% C.L.)

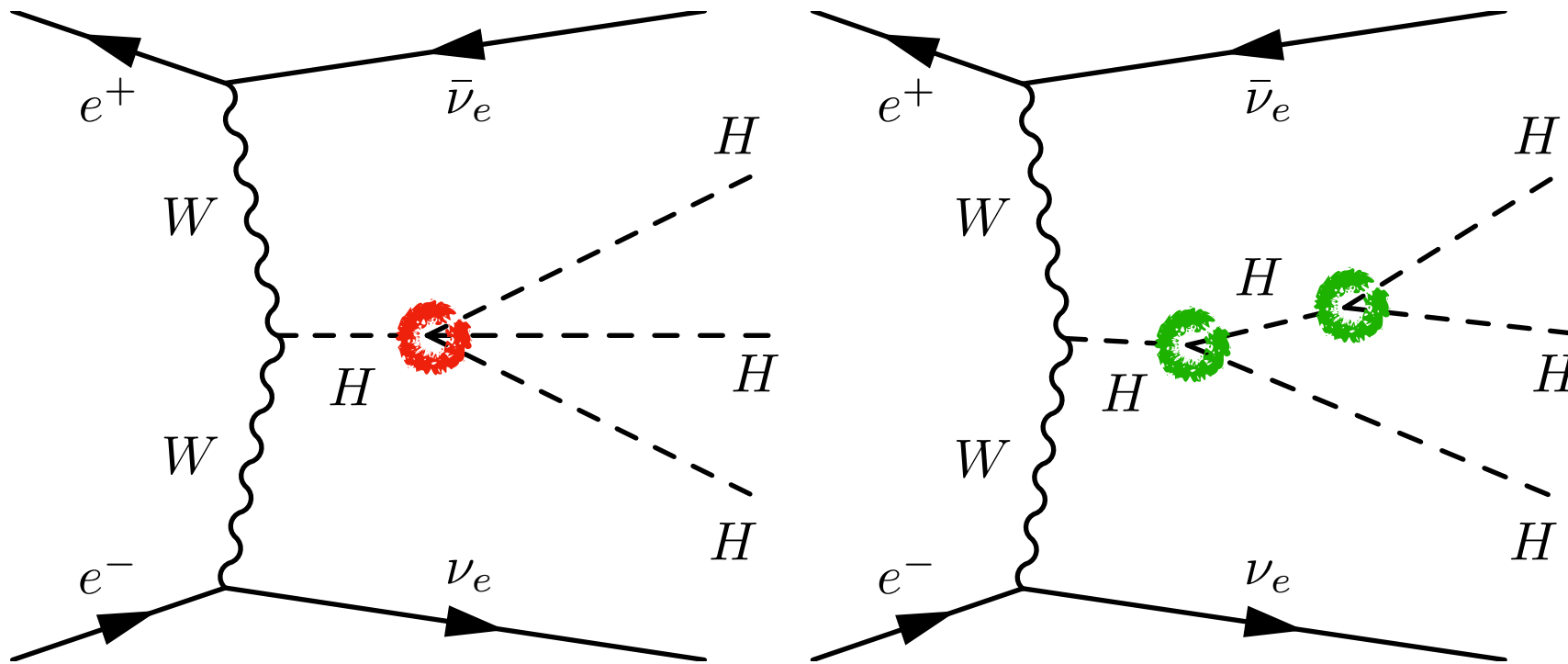
**at 100 TeV, 30 ab $^{-1}$**



**arXiv:1606.09408**

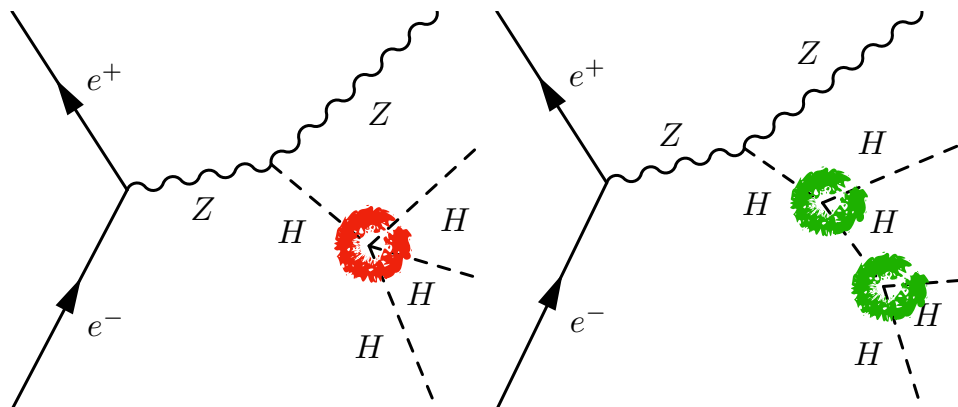
$$\mu^+ \mu^- \rightarrow HHH\nu\bar{\nu}, \quad (\nu = \nu_e, \nu_\mu, \nu_\tau)$$

$$V_h = \frac{m_h^2}{2} h^2 + (1 + \boxed{\kappa_3}) \lambda_{hhh}^{\text{SM}} v h^3 + \frac{1}{4} (1 + \boxed{\kappa_4}) \lambda_{hhhh}^{\text{SM}} h^4$$



$(\kappa_i \rightarrow \delta_i)$

$$\Delta = \frac{N - N_{SM}}{\sqrt{N_{SM}}} = \left( c_1 \kappa_3 + c_2 \kappa_4 + c_3 \kappa_3 \kappa_4 + c_4 \kappa_3^2 + c_5 \kappa_4^2 + c_6 \kappa_3^3 + c_7 \kappa_3^2 \kappa_4 + c_8 \kappa_3^4 \right)$$



**HHHZ negligible !**

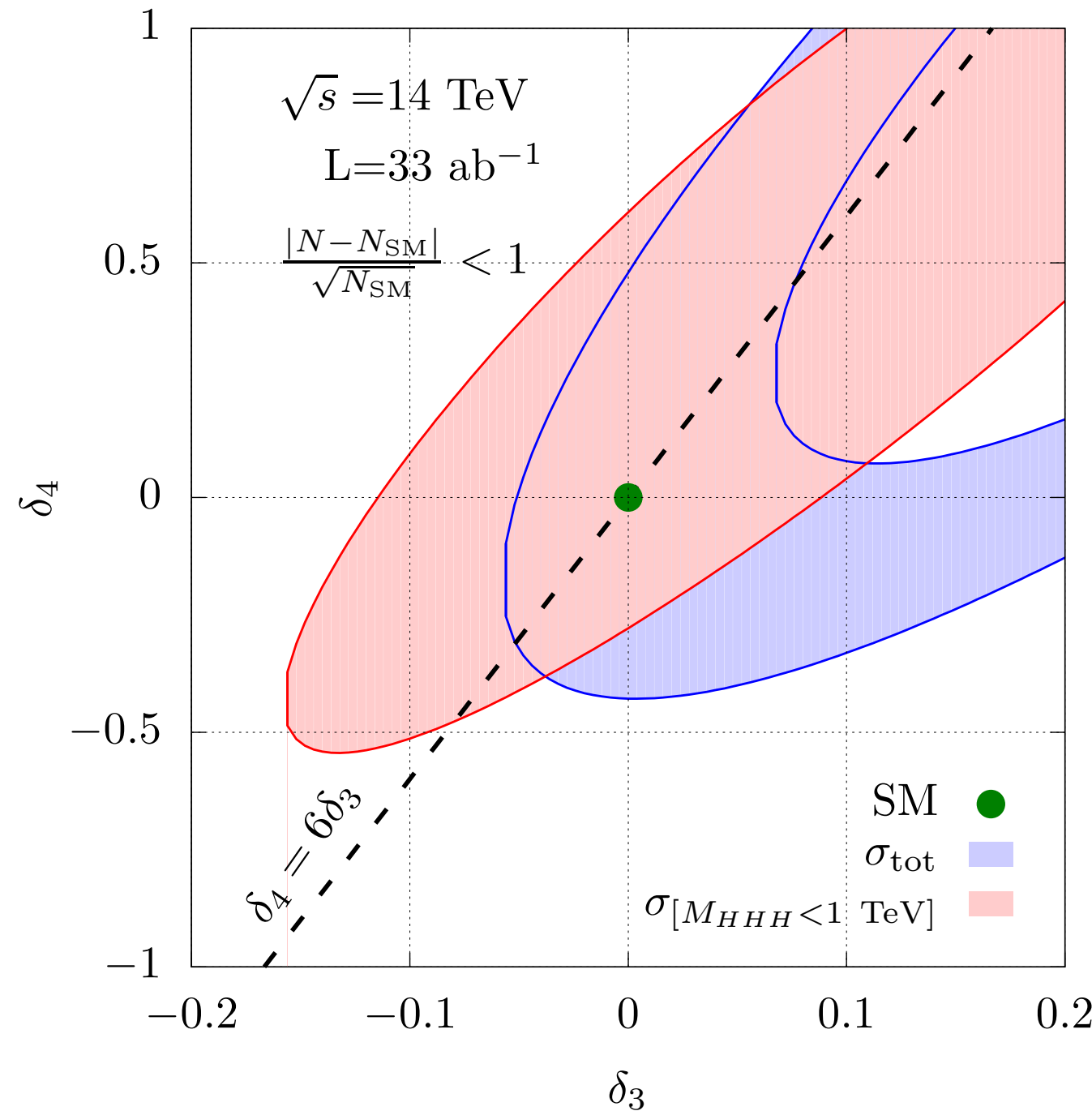
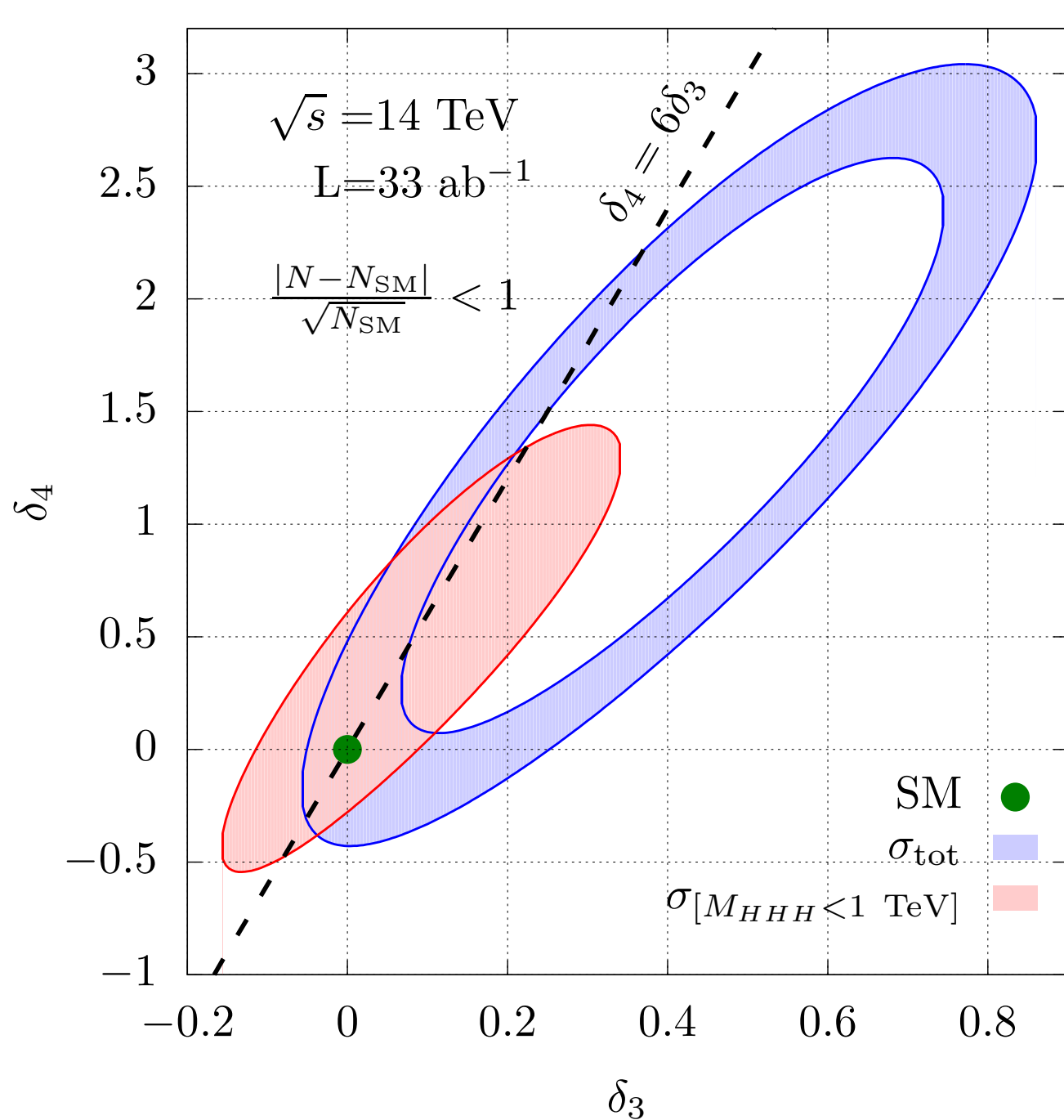
**$\sigma_{HHHZ} \sim 1/2 \sigma_{HHH} @ 3\text{TeV}$**

**$\sim 1/50 \sigma_{HHH} @ 30\text{TeV}$**

# $(N-N_{SM})/\sqrt{N_{SM}}$ versus $(\delta_3, \delta_4)$

**VBF  $\rightarrow$  HHH**

Chiesa, Maltoni, Mantani, BM, Piccinini, Zhao, 2003.13628



**[  $\delta_3 = 0$  ]  $-0.4 < \delta_4 < 0.4$  (68%CL) !!!**

# $(N - N_{SM})/\sqrt{N_{SM}}$ versus $\delta_4$

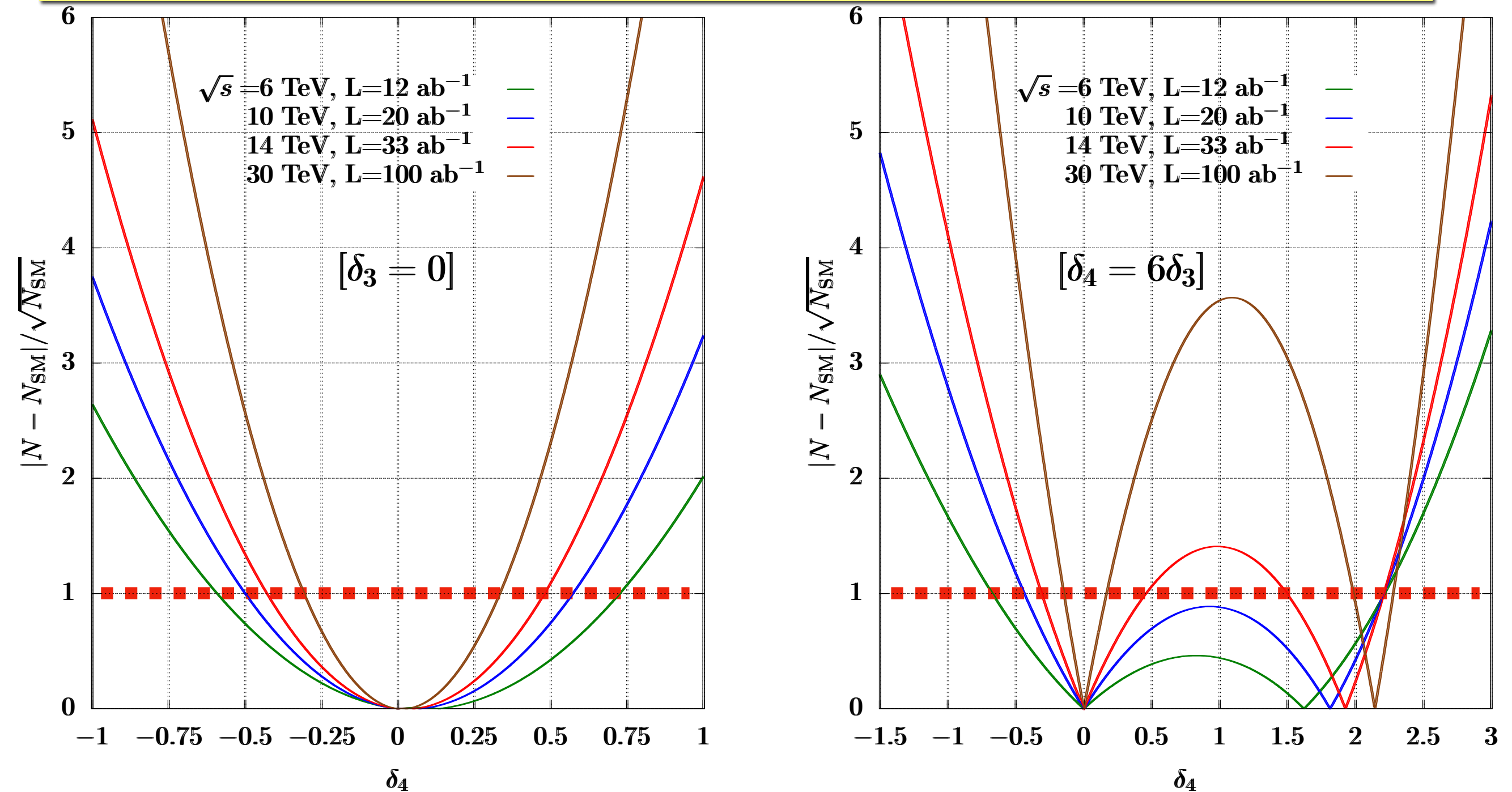
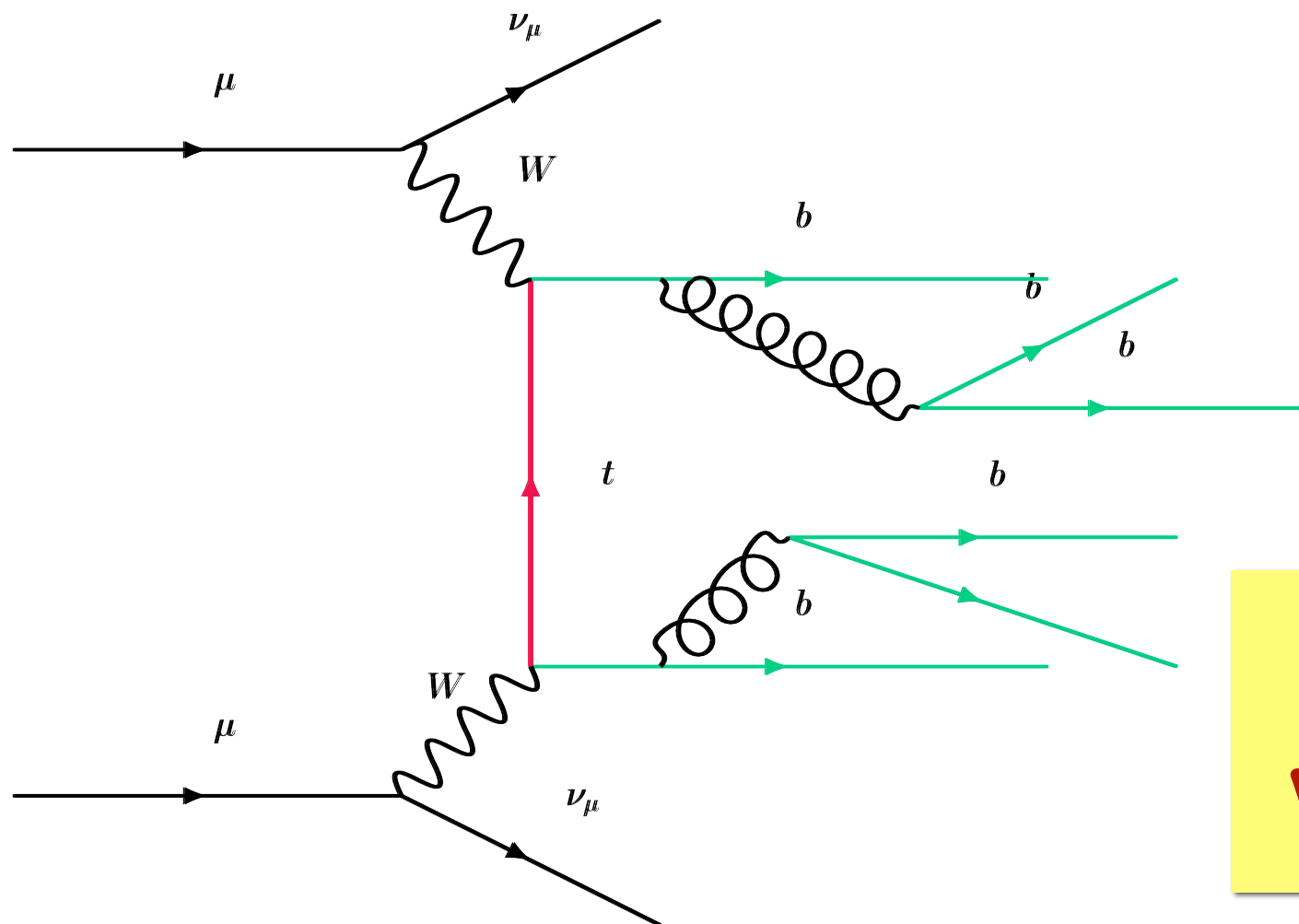


Figure 13: Sensitivity to the quartic Higgs self-coupling in terms of standard deviations  $|N - N_{SM}|/\sqrt{N_{SM}}$  with respect to the SM configuration, where the event numbers  $N$  refer to  $\sigma(\mu^+\mu^- \rightarrow HHH\nu\bar{\nu})$ , for  $M_{\nu\nu} \gtrsim 150\text{GeV}$ , for  $\delta_3 = 0$  (left), and  $\delta_4 = 6\delta_3$  (right). Results are obtained considering deviations from the inclusive cross sections only.

# backgrounds to $VBF \rightarrow HHH$

- \* 8-body final states (at least !)  
→ very hard to evaluate via MC's
- \* all H decay modes are relevant ! [BR(HHH  $\rightarrow$  6 b)  $\sim$  20 %]
- \* 6b-jet bckgr moderate at FCC-pp [arXiv:1801.10157]
- \* might be  $S/B \gg 1$  at multi-TeV muon colliders...



**MC** development for  
**WW** approx. needed !

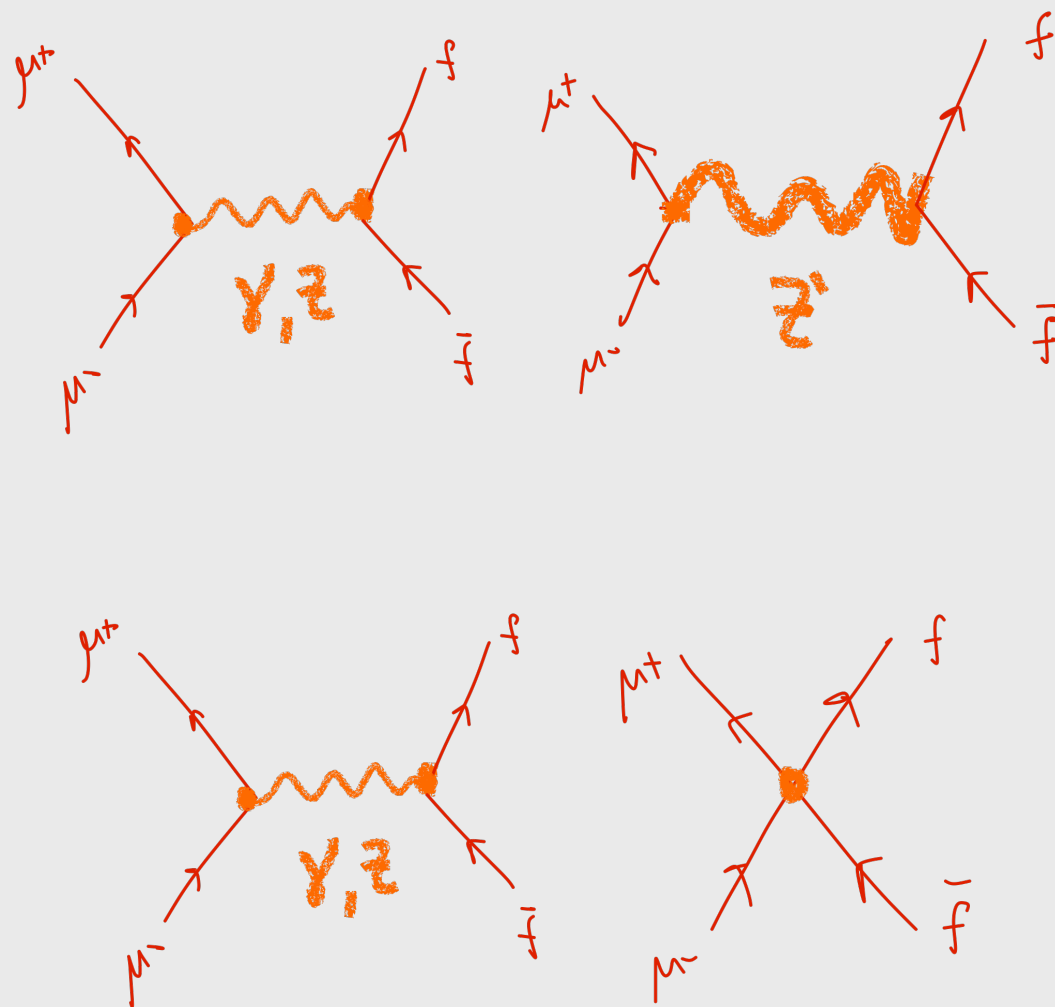


# off-shell effects

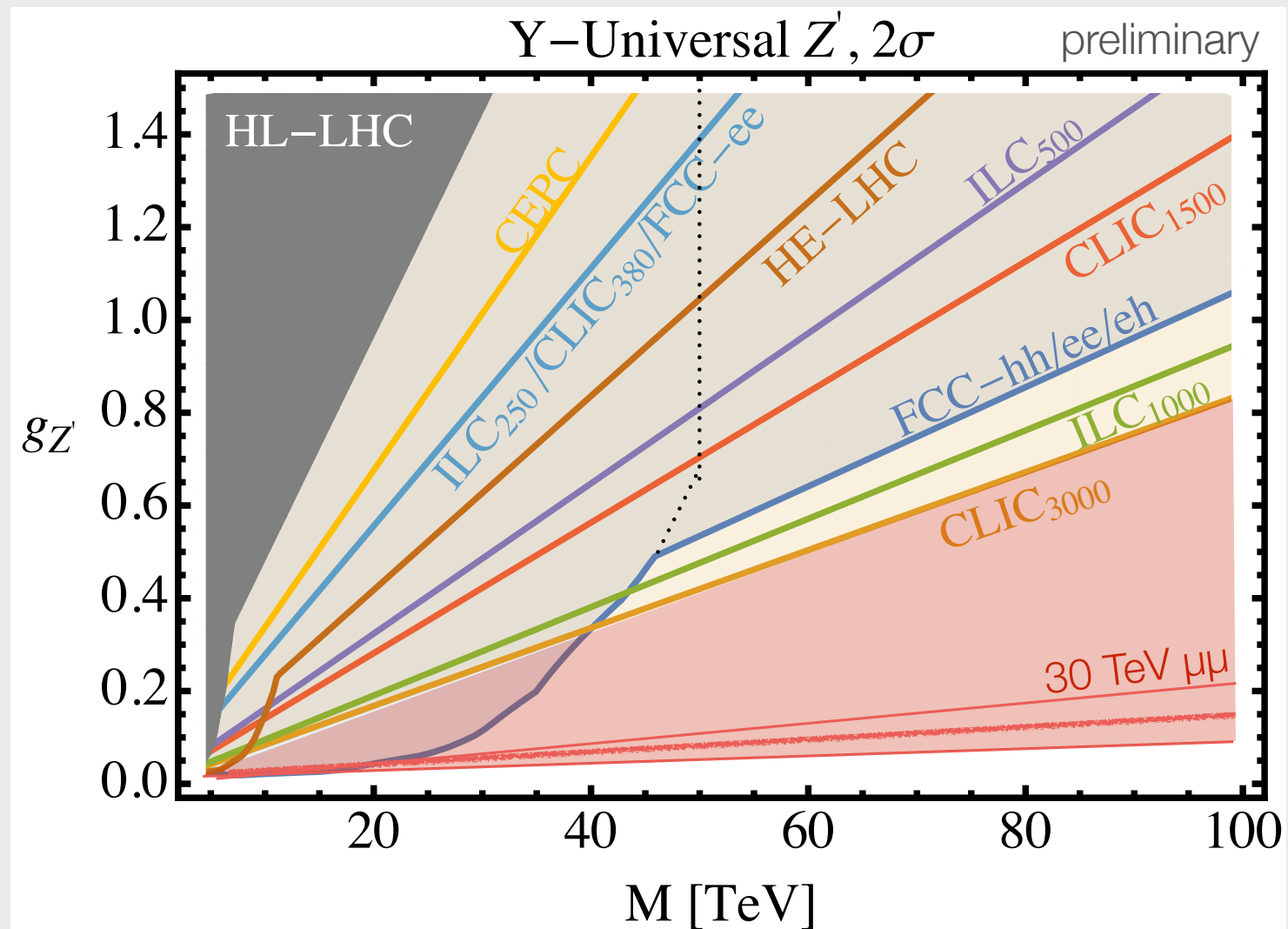
## A heavy $Z'$

DRELL-YAN

RATES AND ANGULAR DISTRIBUTIONS



Franceschini





# the “size” of the Higgs boson

Buttazzo, Franceschini, Wulzer

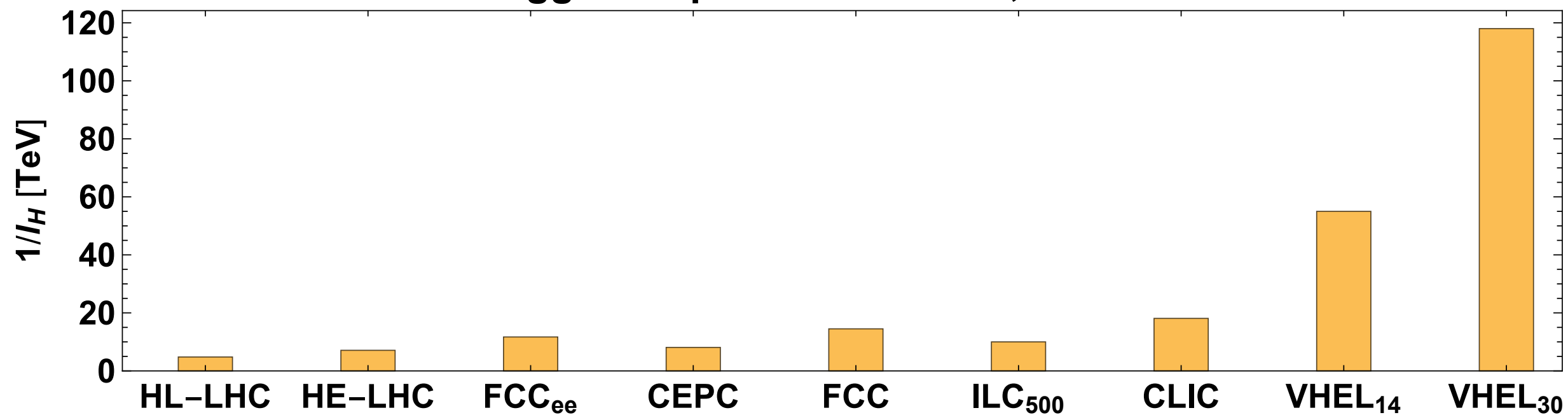
$$\ell_{Higgs} \sim m_{\star}^{-1}$$



(EFT approach)

Compositeness Reach:

Higgs compositeness scale,  $2\sigma$  reach



# a few final comments

- \* such a high energy at pointlike level opens up hugely new perspectives !
- \* capability of direct production of new heavy states paramount!
- \*  $\mu$  colliders @10's TeV can be considered WW colliders !
- \* qualitatively new Higgs physics (test quartic self-coupl.)
- \* physics bckgds expected mild also for hadronic final states  
BUT simulations are quite hard (many particles in phase-space)  
→ implement Equivalent Vector-Boson Approx. in MC's !
- \* many many possible new directions for exploring BSM  
in off-shell/indirect effects via precision measurements  
[also VBF-production role to be extensively considered...]