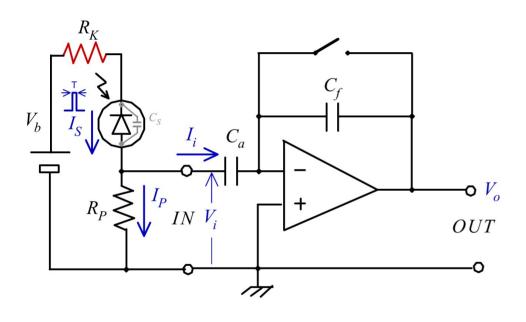


# HIDRA input circuit study: model and simulation

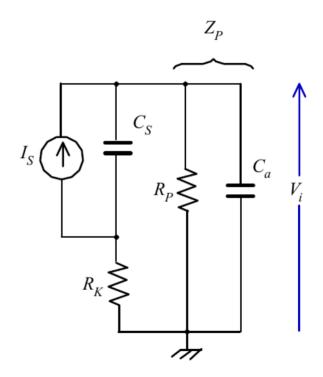
Lorenzo Pacini on behalf of Sebastiano Detti

## **Approximation of the circuit**

#### Simplified scheme



#### Equivalent circuit



The exact calculation is described in: "Risposta globale all'impulso Sebastiano Detti"

#### Results of the calculation: equation

$$\begin{split} V_{idG} &= \left[ V_{iT} \cdot \left( \frac{1}{2} + \frac{\omega_o}{2 \cdot \sqrt{\omega_o^2 - 4 \cdot \omega_n^2}} \right) + \frac{\sqrt{\omega_o^2 - 4 \cdot \omega_n^2} \cdot (R_P + R_K)}{\sqrt{\omega_o^2 - 4 \cdot \omega_n^2} \cdot C_a \cdot R_P \cdot R_K} \right] \cdot e^{-\frac{1}{2} \cdot \left( \omega_o - \sqrt{\omega_o^2 - 4 \cdot \omega_n^2} \right) \cdot t} \\ &+ \left[ V_{iT} \cdot \left( \frac{1}{2} - \frac{\omega_o}{2 \cdot \sqrt{\omega_o^2 - 4 \cdot \omega_n^2}} \right) + \frac{\sqrt{\omega_o^2 - 4 \cdot \omega_n^2} \cdot C_a \cdot R_P \cdot R_K}}{\sqrt{\omega_o^2 - 4 \cdot \omega_n^2} \cdot C_a \cdot R_P \cdot R_K} \right] \cdot e^{-\frac{1}{2} \cdot \left( \omega_o + \sqrt{\omega_o^2 - 4 \cdot \omega_n^2} \right) \cdot t} \end{split}$$

Check Sebastiano's report

Sintesi rete d'ingresso

$$V_{ST} = I_{S} \cdot \left\{ \frac{\left[ 2 - C_{S} \cdot (R_{P} + R_{K}) \cdot (\omega_{o} + \sqrt{\omega_{o}^{2} - 4 \cdot \omega_{a}^{2}}) \right] \cdot e^{-\frac{1}{2} (\omega_{o} - \sqrt{\omega_{o}^{2} - 4 \cdot \omega_{a}^{2}}) \cdot T} + \left[ C_{S} \cdot (R_{P} + R_{K}) \cdot (\omega_{o} - \sqrt{\omega_{o}^{2} - 4 \cdot \omega_{a}^{2}}) - 2 \right] \cdot e^{-\frac{1}{2} (\omega_{o} + \sqrt{\omega_{o}^{2} - 4 \cdot \omega_{a}^{2}}) \cdot T} + R_{P} + R_{K} \right\}$$

$$2 \cdot C_{S} \cdot \sqrt{\omega_{o}^{2} - 4 \cdot \omega_{a}^{2}} + \left[ C_{S} \cdot (R_{P} + R_{K}) \cdot (\omega_{o} - \sqrt{\omega_{o}^{2} - 4 \cdot \omega_{a}^{2}}) - 2 \right] \cdot e^{-\frac{1}{2} (\omega_{o} + \sqrt{\omega_{o}^{2} - 4 \cdot \omega_{a}^{2}}) \cdot T} + R_{P} + R_{K} \right\}$$

$$V_{iG} = I_{S} \cdot R_{P} \cdot \left[ \frac{2 \cdot \omega_{a}^{2}}{\sqrt{\omega_{o}^{2} - 4 \cdot \omega_{a}^{2}}} \cdot \left( \frac{e^{-\frac{\omega_{o}^{2} \cdot \sqrt{\omega_{o}^{2} - 4 \cdot \omega_{a}^{2}}}{2}} \cdot e^{-\frac{\omega_{o}^{2} \cdot \sqrt{\omega_{o}^{2} - 4 \cdot \omega_{a}^{2}}}{2}} \right) + 1 \right]$$

$$W_{iG} = I_{S} \cdot R_{P} \cdot \left[ \frac{2 \cdot \omega_{a}^{2}}{\sqrt{\omega_{o}^{2} - 4 \cdot \omega_{a}^{2}}} \cdot \left( \frac{e^{-\frac{\omega_{o}^{2} \cdot \sqrt{\omega_{o}^{2} - 4 \cdot \omega_{a}^{2}}}{2}} \cdot e^{-\frac{\omega_{o}^{2} \cdot \sqrt{\omega_{o}^{2} - 4 \cdot \omega_{a}^{2}}}{2}} \right) + 1 \right]$$

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$$W_{iG} = I_{S} \cdot \left[ \frac{2 \cdot \omega_{a}^{2}}{\sqrt{\omega_{o}^{2} - 4 \cdot \omega_{a}^{2}}} \cdot$$

## Results of the calculation: some plots

Vi vs Time

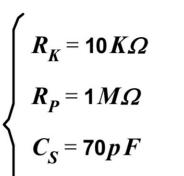
Current pulse

parameters:

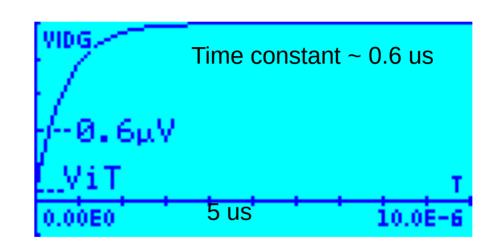
Width: 50 ns

Amplitude: 300 nA

Charge: 15 fC



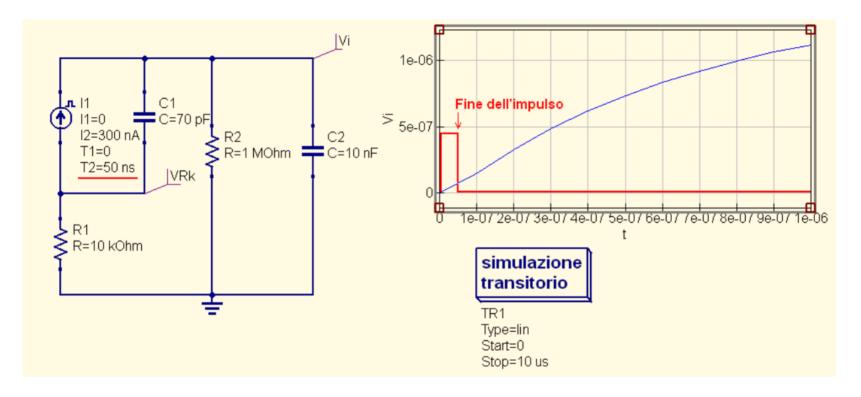
$$C_a = 10 n F$$



The input voltage of the HIDRA chip increases for a long time (~1 us) after the end of the input current.

This feature is not present when the Rk is  $\sim 0$ .

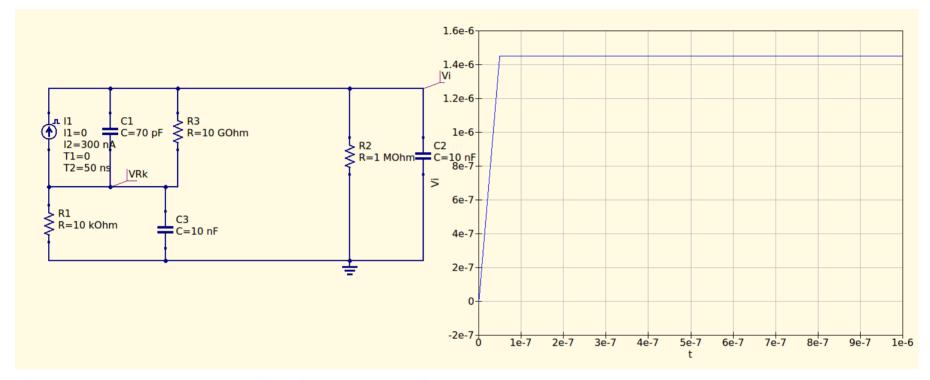
#### **QUCS** simulation confirmation



QUCS simple simulation confirm the model.

How to solve: remove Rk (of course), add a big capacitance after Rk

#### QUCS: test of the 10 nF capacitance



Both solutions seems to completely remove the issue.

Real case: a residual dependence steel remains, is it due to a parasitic R? Unknown effect?

## **Summary**

Rk separates the diode capacitor and Ci. This allows a different voltage of Ci and Cs during the injection of the current. A long time is needed to recover from this difference, since Cs discharges through Rk ( $\mathbf{Cs*Rk} \sim \mathbf{0.7}$  us as observed by simulation and calculation)

Removing Rk or adding a big capacitor solves the issue.

Residual dependence remains: to be understood.

#### Next step:

- confirm the residual dependence with MIP (using SiPMs in parallel to the PD to select true MIP signals).
- check the LED light tentative slow talis.

