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## Problem at high momenta

Initially the simulation of dE/dx for the single hit was implemented in PacTrk/  
PacTrkHitViewDch.cc, and the spread was generated according to a Gaussian **without requiring dedx>0.**

Here is the relevant line in PacTrkHitViewDch::getHitInfo(...) in revision 1543:

```
dedx = RandGauss::shoot(rng,dedx_ave,ededx);
```

Note that the absence of a requirement "dedx>0" was a feature,not a bug. At some point the line above was changed to:

```
dedx = std::max(RandGauss::shoot(rng,dedx_ave,ededx),0.0);
```

See PacTrkdEdxMeas::get\_dedx(...), revision 1714. I think that this cut has been introduced when the dE/dx of SVT has been implemented.

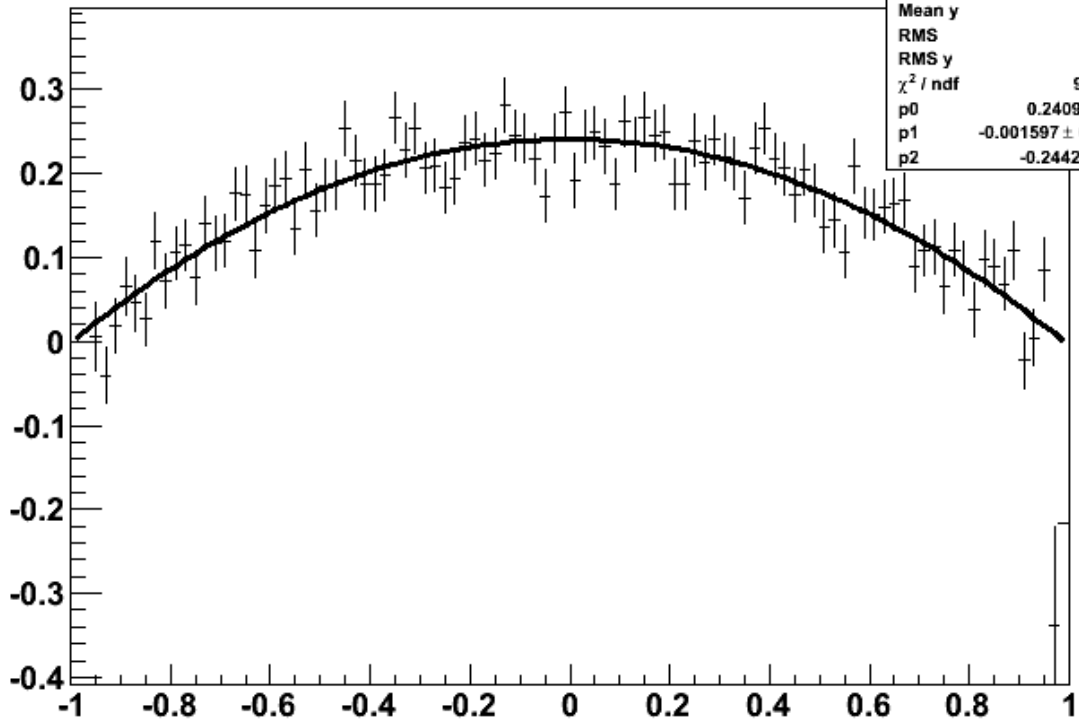
Why for DCH it's important that the requirement dedx>0 is NOT applied? Because the dE/dx error of the single hit is such that there is a non-negligible probability that the Gaussian-generated measurement takes a value<0, but at the same time the probability that the *average* over the hits of the track is negative is extremely small, practically zero.

In other words, it is fine if the |dE/dx| measurement of a single hit can be negative, provided that the |dE/dx| measurement of the *track* is *positive* defined.

**With dedx = std::max(RandGauss::shoot(rng,dedx\_ave,ededx),0.0):**

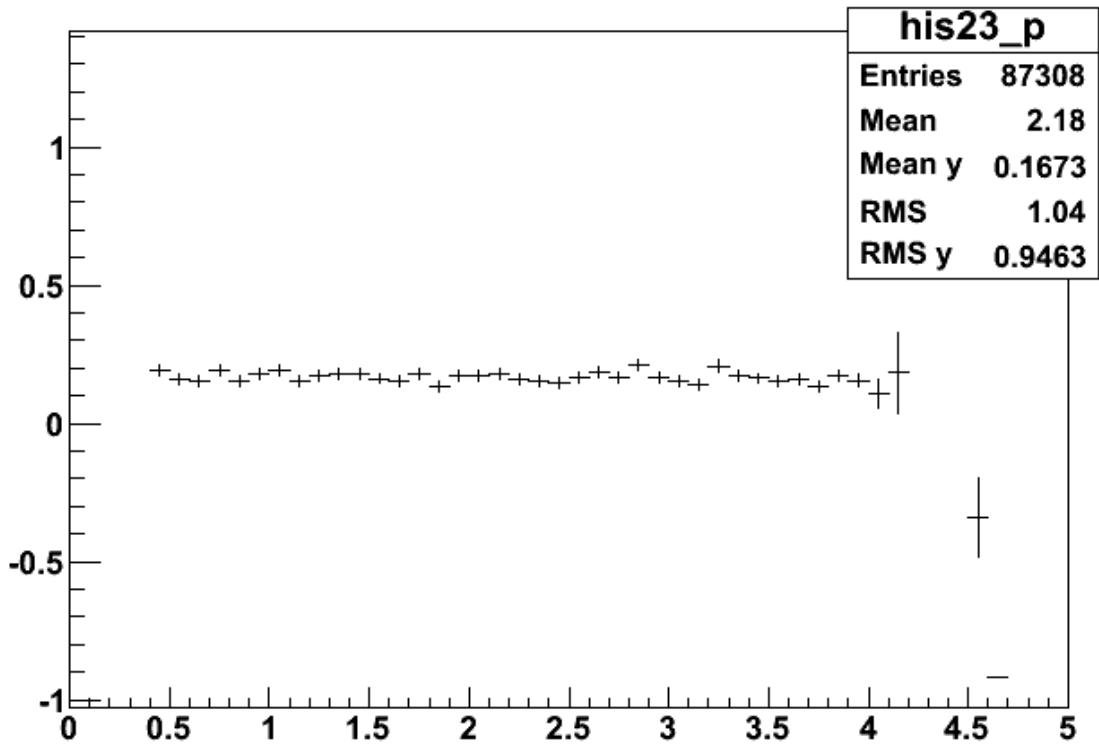
Below: dE/dx pull vs. cos(theta) **before** the fix (p>0.4 GeV)

### dE/dx pull vs cos(theta) profile



Below: dE/dx pull vs.  $p$  **before** the fix ( $p > 0.4$  GeV)

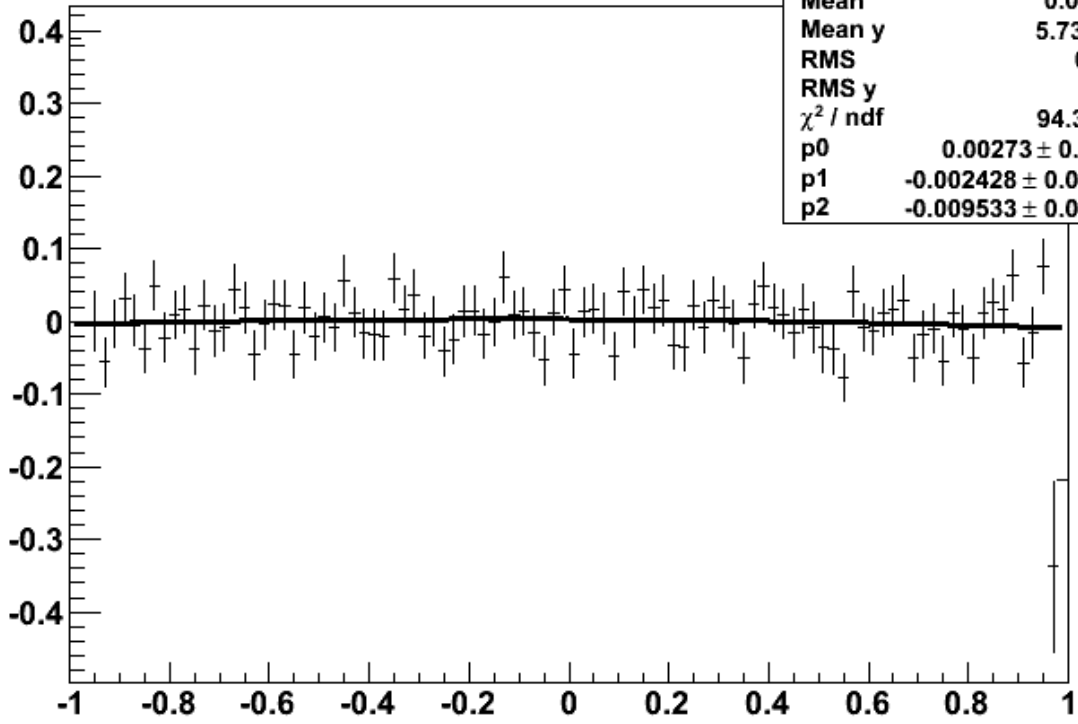
**dE/dx pull vs p profile**



**With  $dedx = RandGauss::shoot(rng, dedx\_ave, ededx);$**

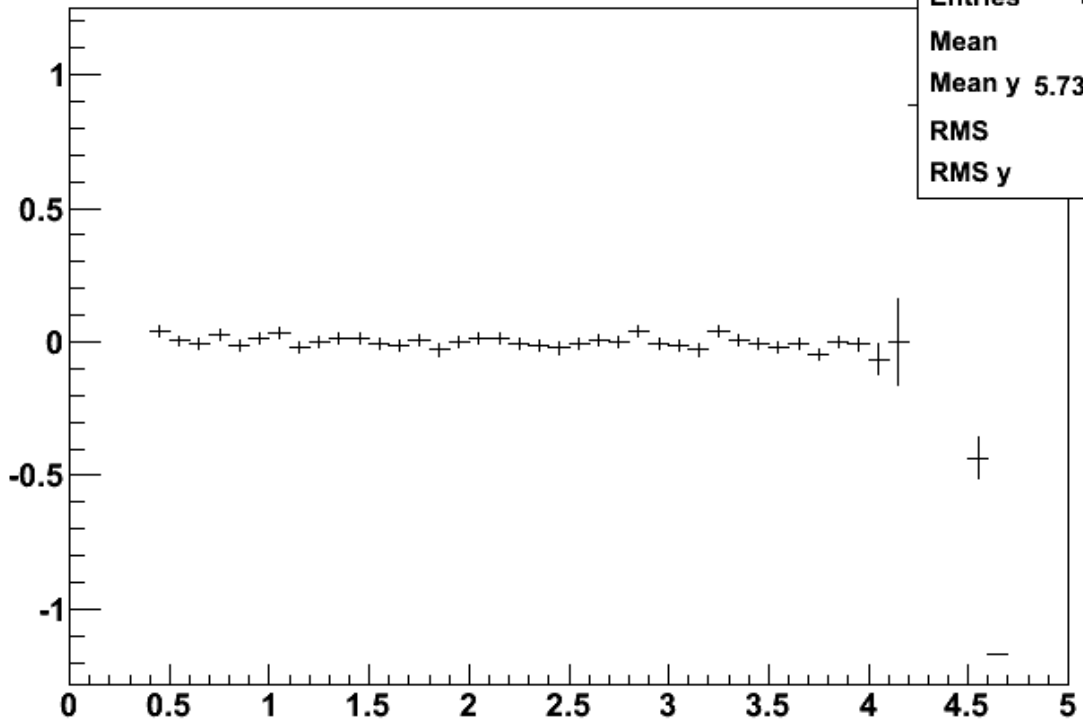
*Below:  $dE/dx$  pull vs  $\cos(\theta)$  after the fix ( $p > 0.4$  GeV)*

**dE/dx pull vs cos(theta) profile**



*Below: dE/dx pull vs. p after the fix ( $p > 0.4$  GeV)*

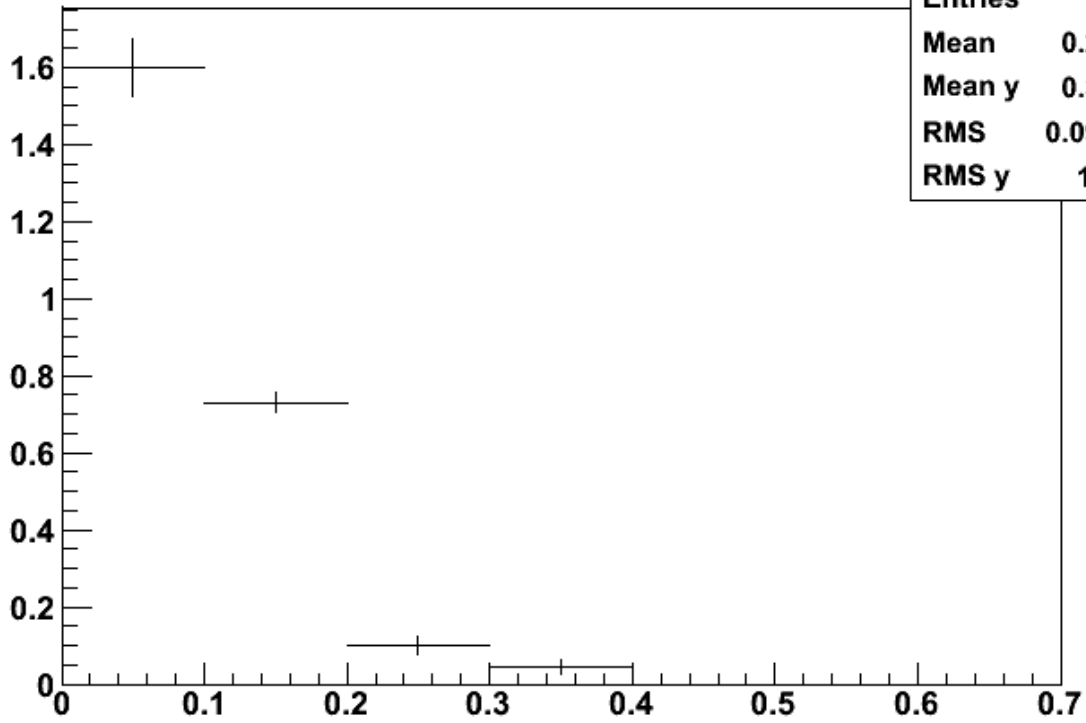
dE/dx pull vs p profile



**At low momenta there is a bias in the dE/dx pull. Under investigation:**

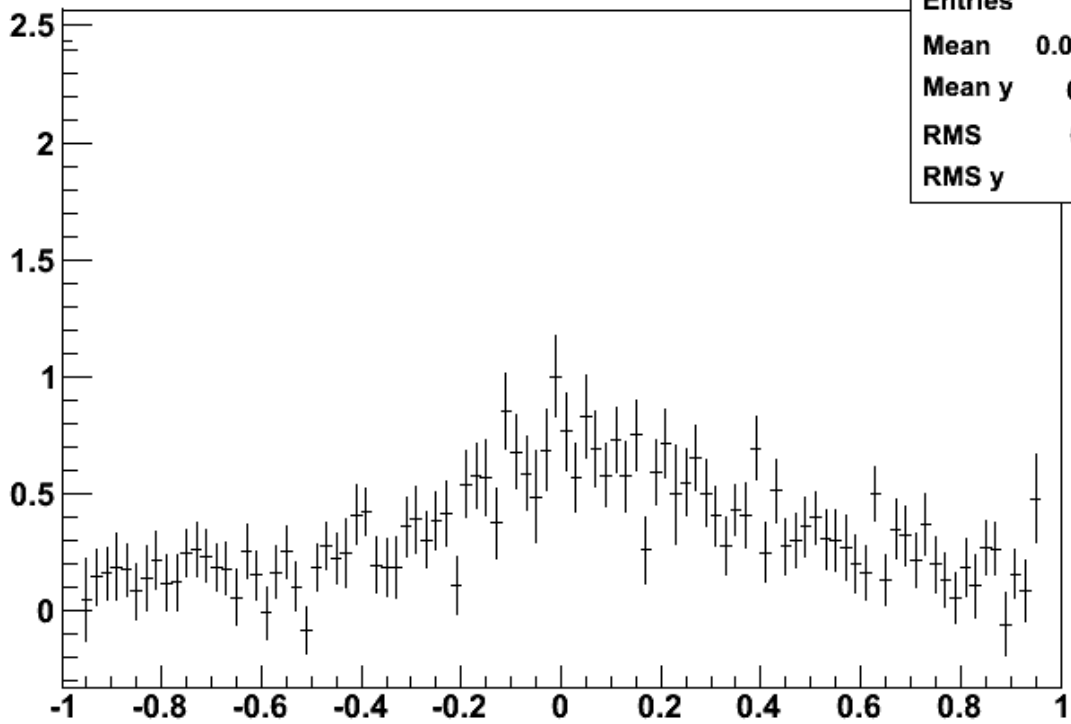
*Below: dE/dx pull vs. p **after** the fix ( $p < 0.4$  GeV). Particles are pions.*

**dE/dx pull vs p profile**



| <b>his23_p</b> |         |
|----------------|---------|
| Entries        | 7545    |
| Mean           | 0.2443  |
| Mean y         | 0.3408  |
| RMS            | 0.09054 |
| RMS y          | 1.184   |

**dE/dx pull vs cos(theta) profile**



| <b>his22_p</b> |          |
|----------------|----------|
| Entries        | 7545     |
| Mean           | 0.007633 |
| Mean y         | 0.3408   |
| RMS            | 0.5341   |
| RMS y          | 1.184    |

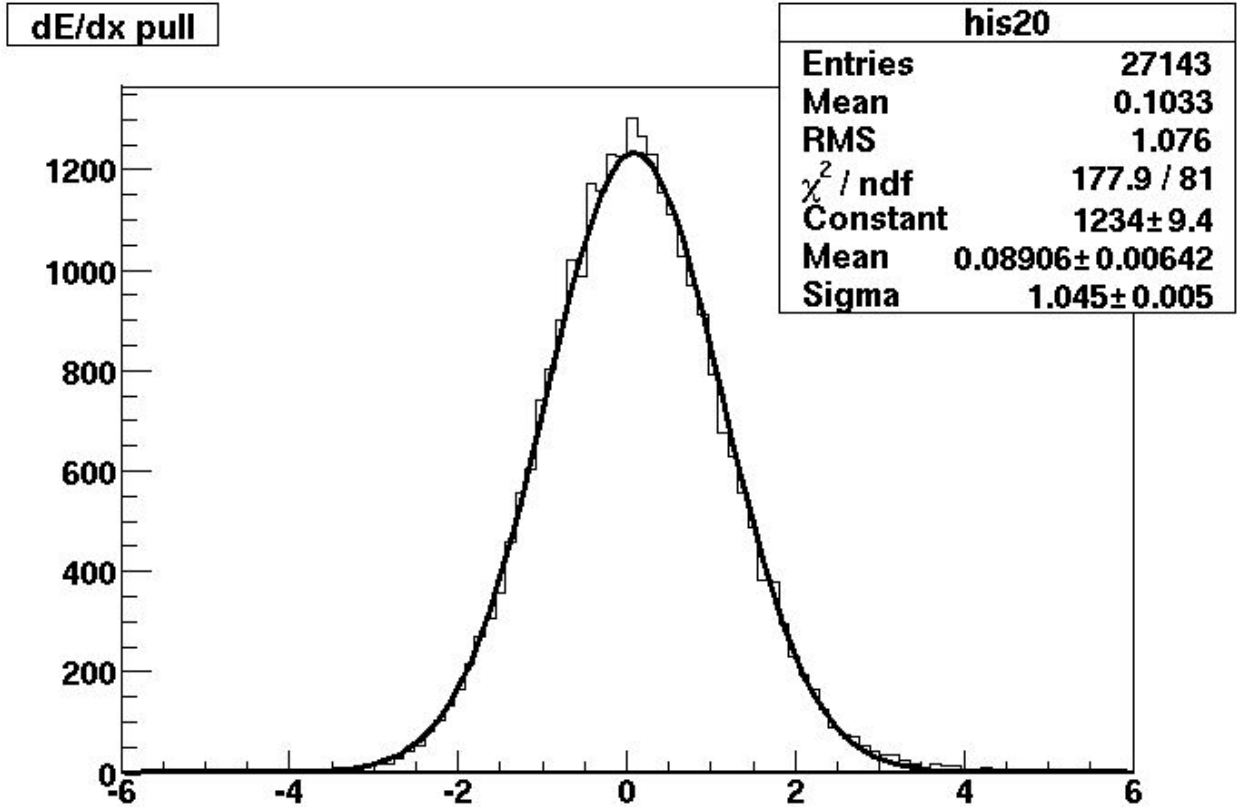
## Problem at low momenta

### Current code (using p (reco) at the origin)

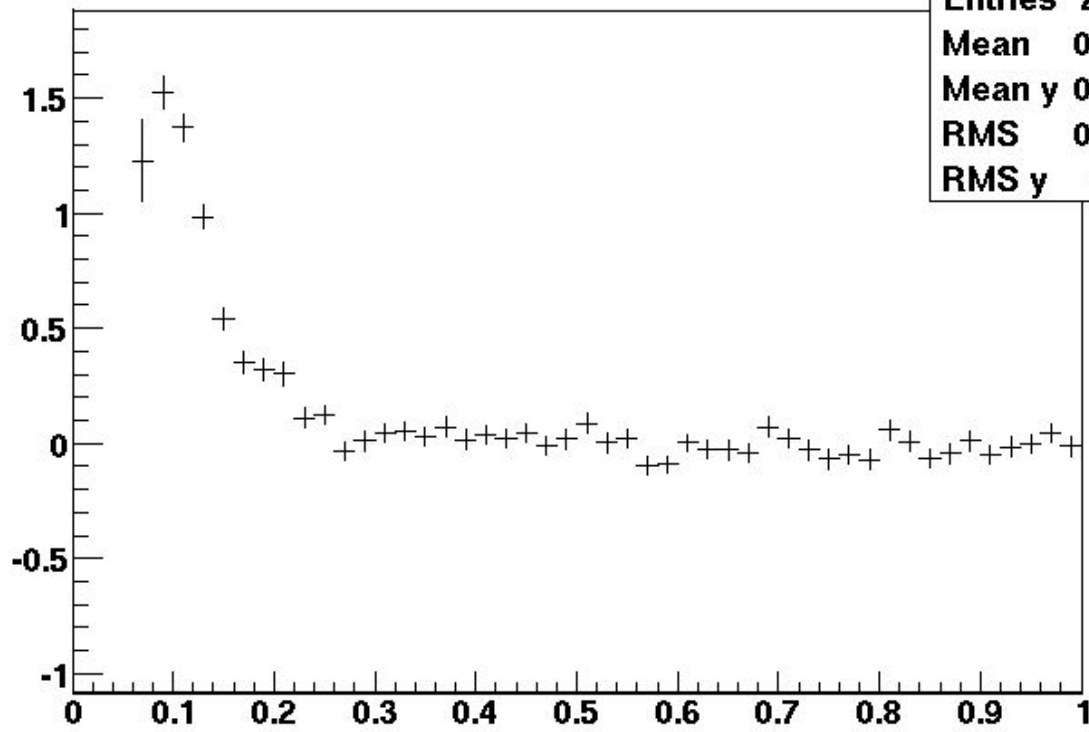
dEdxExpPi computed with reco computed at the origin (current code in SVN)

dE/dx reco computed from (truncated) weighted mean in PacTrunc

Comments: the pull is bad at low p values.

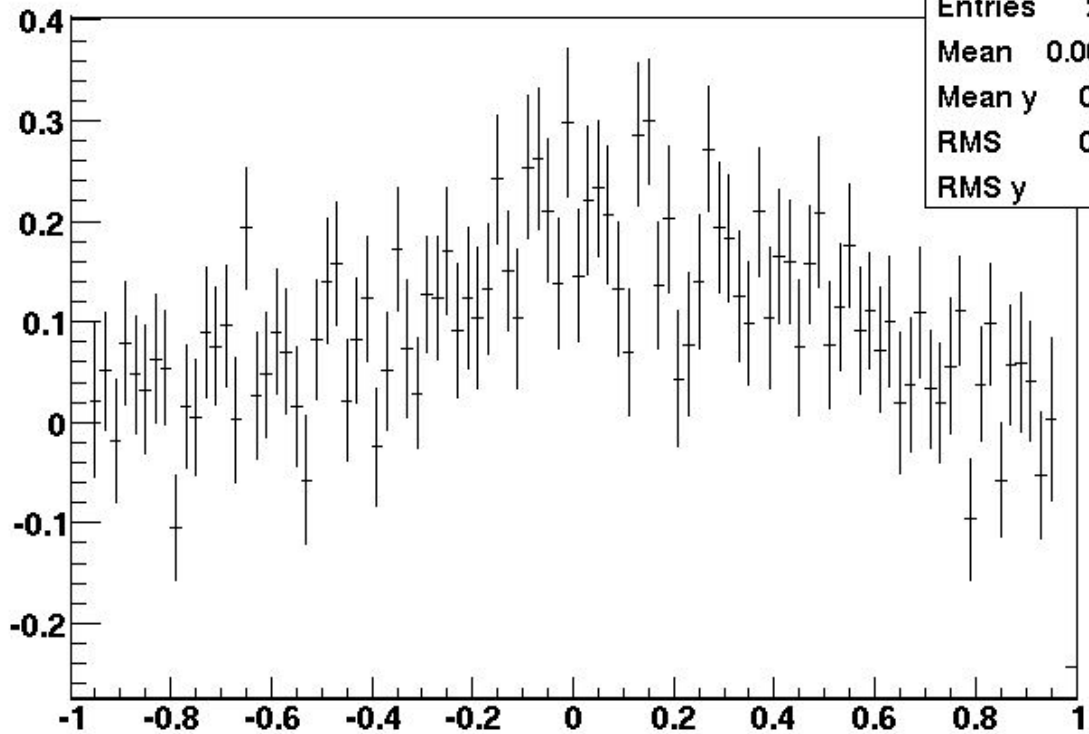


**dE/dx pull vs p profile**



| <b>his23 p</b> |        |
|----------------|--------|
| Entries        | 27124  |
| Mean           | 0.5456 |
| Mean y         | 0.1039 |
| RMS            | 0.2606 |
| RMS y          | 1.076  |

**dE/dx pull vs cos(theta) profile**



| <b>his22 p</b> |          |
|----------------|----------|
| Entries        | 27124    |
| Mean           | 0.006814 |
| Mean y         | 0.1033   |
| RMS            | 0.5425   |
| RMS y          | 1.076    |

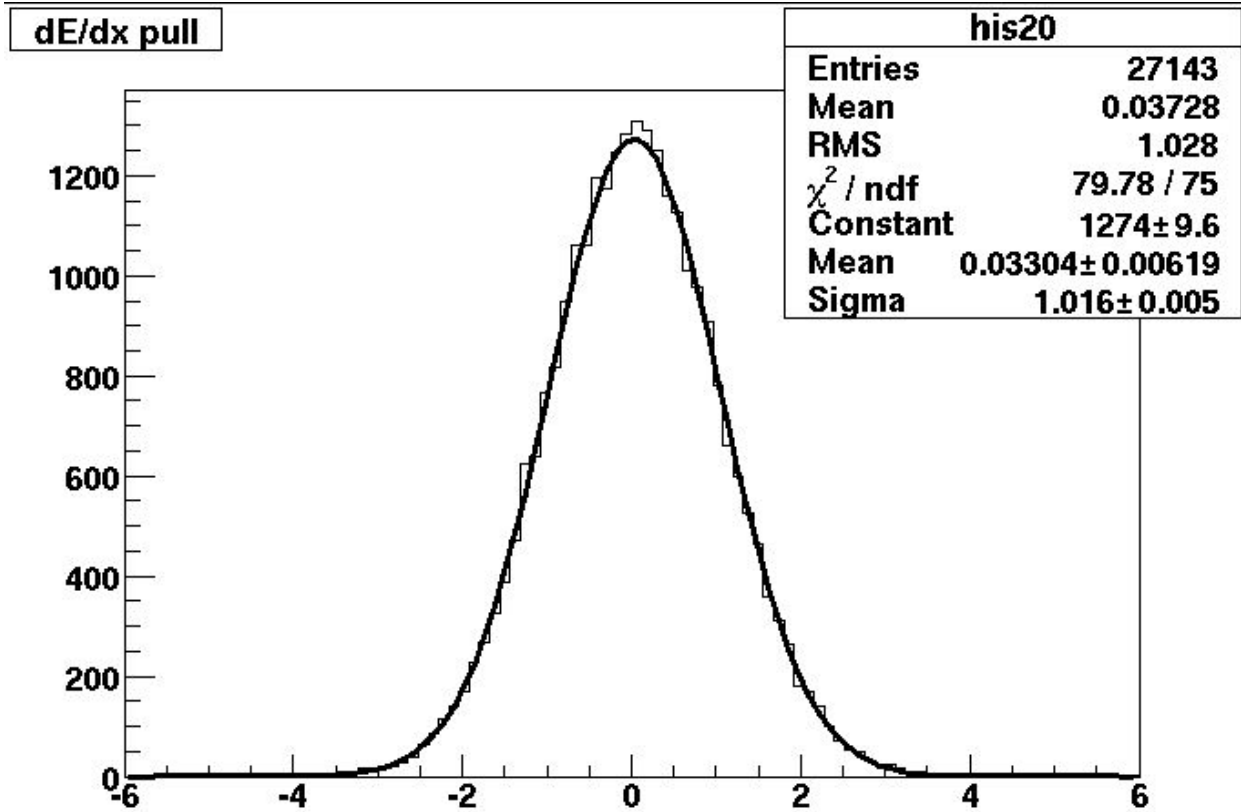


## Using p(reco) at DCH

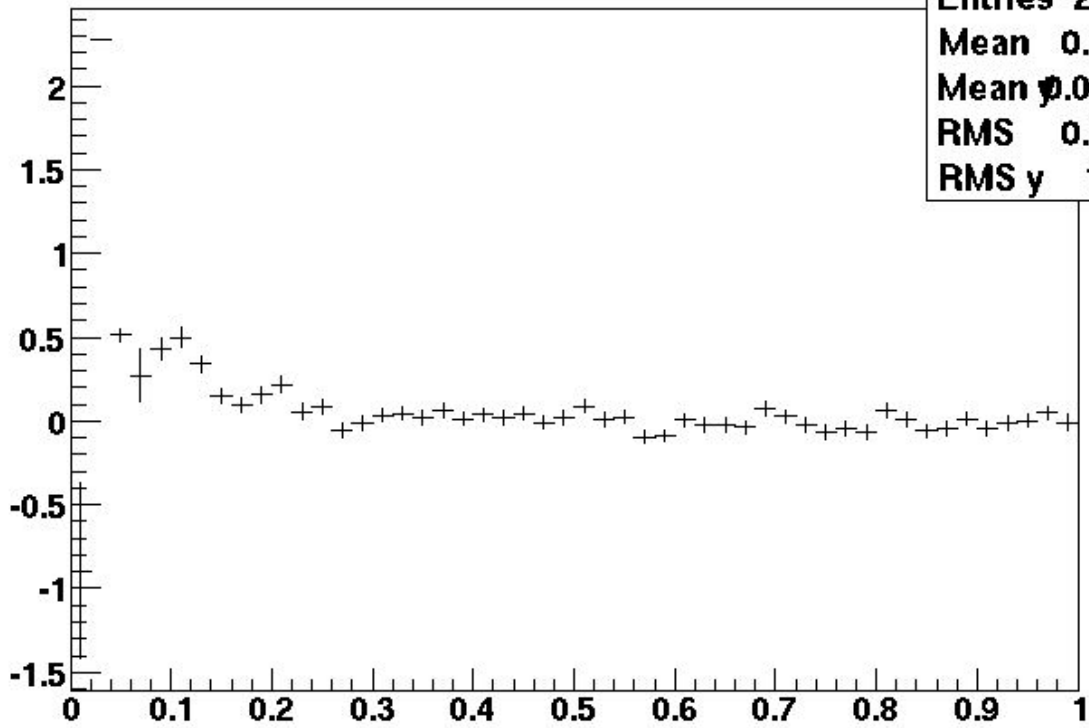
dEdxExpPi computed with p reco computed at the DCH (first DCH hit)

dE/dx reco computed from (truncated) weighted mean in PacTrunc

Comments: the pull is not good at low p values, though it has improved with respect to the when p is computed at the origin

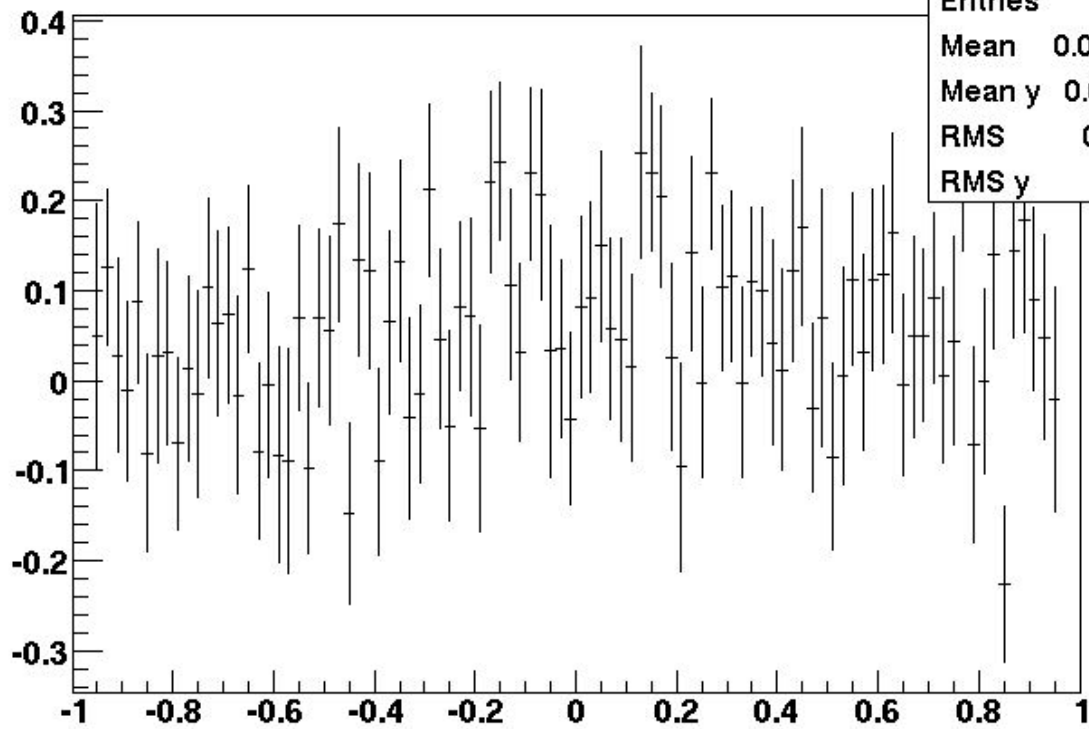


**dE/dx pull vs p profile**



| his23_p       |         |
|---------------|---------|
| Entries       | 27129   |
| Mean          | 0.5455  |
| Mean $\sigma$ | 0.03777 |
| RMS           | 0.2606  |
| RMS y         | 1.028   |

**dE/dx pull vs cos(theta) profile**



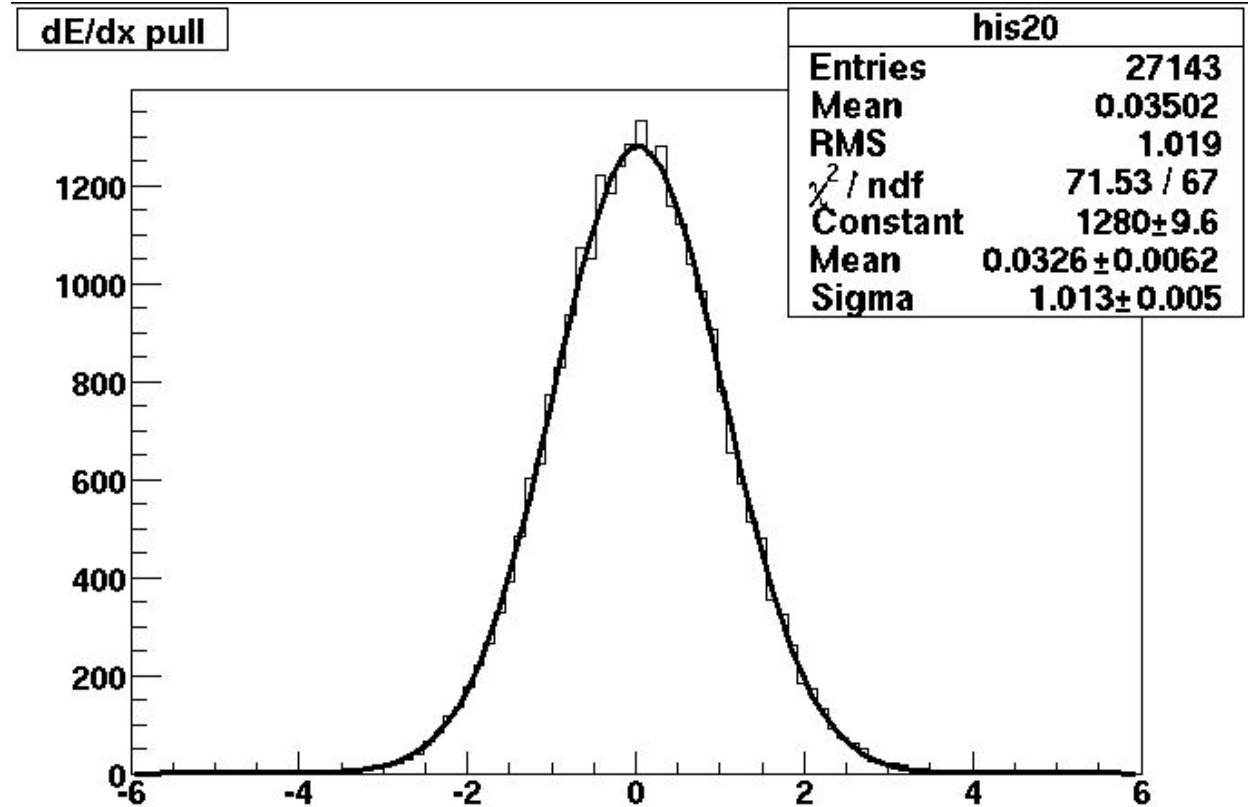
| his22_p |          |
|---------|----------|
| Entries | 9077     |
| Mean    | 0.009121 |
| Mean y  | 0.06054  |
| RMS     | 0.5398   |
| RMS y   | 1.018    |

## Using p(true) at DCH

dEdxExpPi computed with p true (1st PacSimHit of DCH)

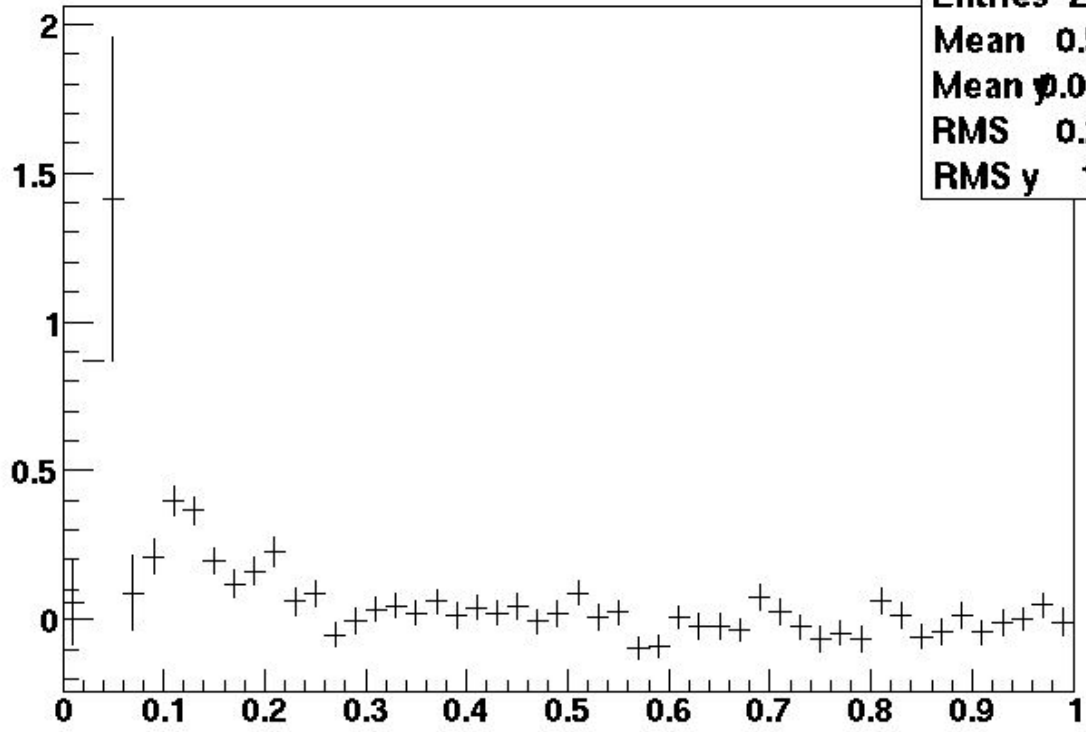
dE/dx reco computed from (truncated) weighted mean in PacTrunc

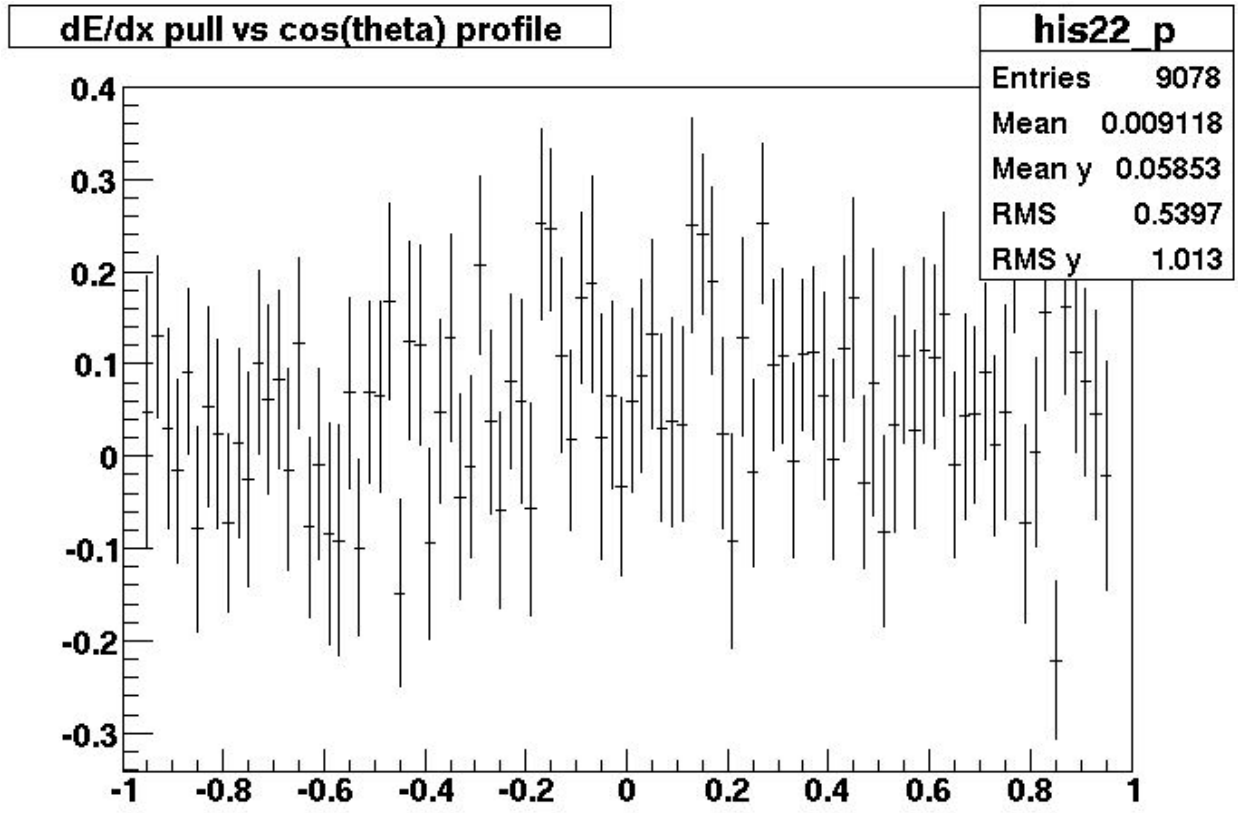
Comments: the pull is still not perfect because the true p changes slightly along the track due to the energy loss. A small bias at positive values is visible at very low momenta.



**dE/dx pull vs p profile**

| <b>his23_p</b> |         |
|----------------|---------|
| Entries        | 27139   |
| Mean           | 0.5453  |
| Mean $\sigma$  | 0.03516 |
| RMS            | 0.2607  |
| RMS y          | 1.019   |

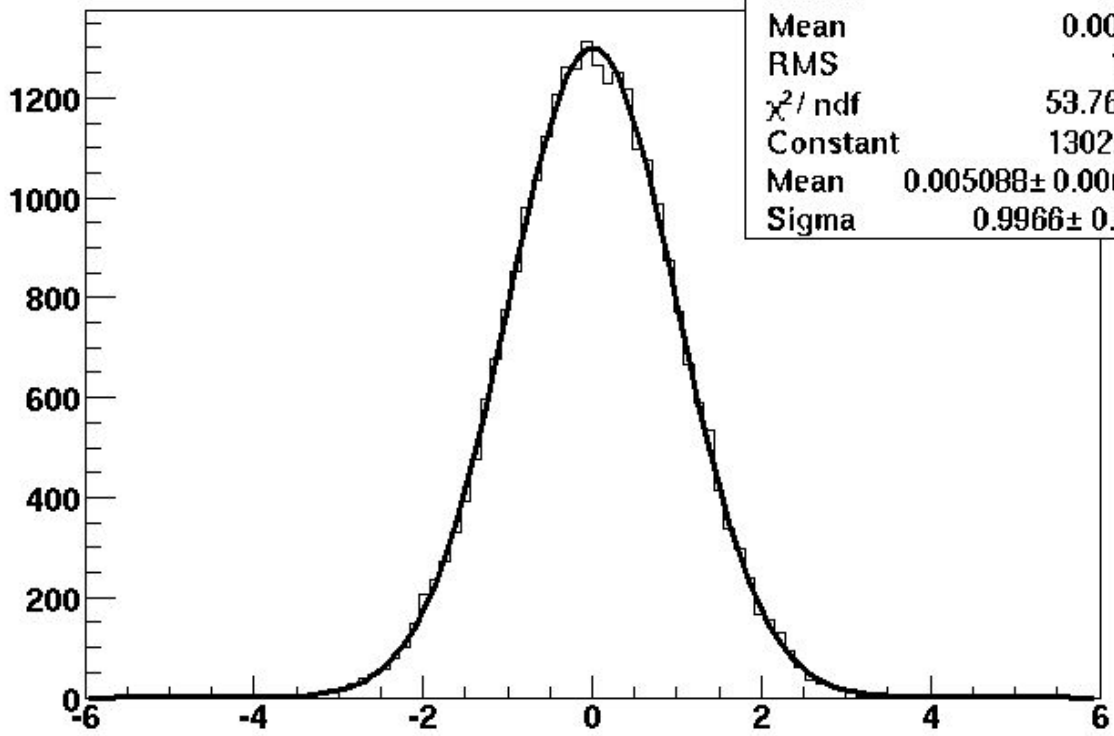




**Using p(true) at DCH and only the info of first (sim)hit**

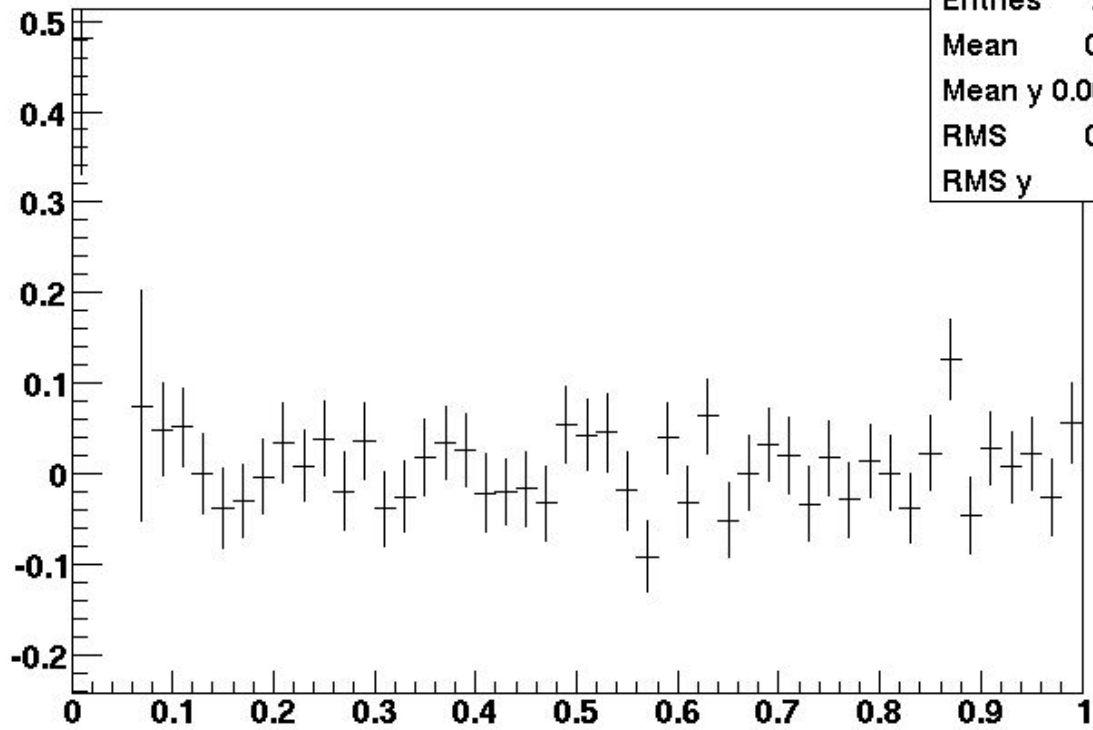
dEdxExpPi computed with p true (1st PacSimHit of DCH)  
dE/dx reco computed from Gauss(dEdxExpPi,sigma) where sigma=error\_1st\_DchHit/  
sqrt(nhit)  
Comments: the pull is perfect at all p values, including the lowest ones.

dE/dx pull



| his20                 |                     |
|-----------------------|---------------------|
| Entries               | 27147               |
| Mean                  | 0.005921            |
| RMS                   | 1.001               |
| $\chi^2 / \text{ndf}$ | 53.76 / 63          |
| Constant              | 1302 ± 9.7          |
| Mean                  | 0.005088 ± 0.006063 |
| Sigma                 | 0.9966 ± 0.0043     |

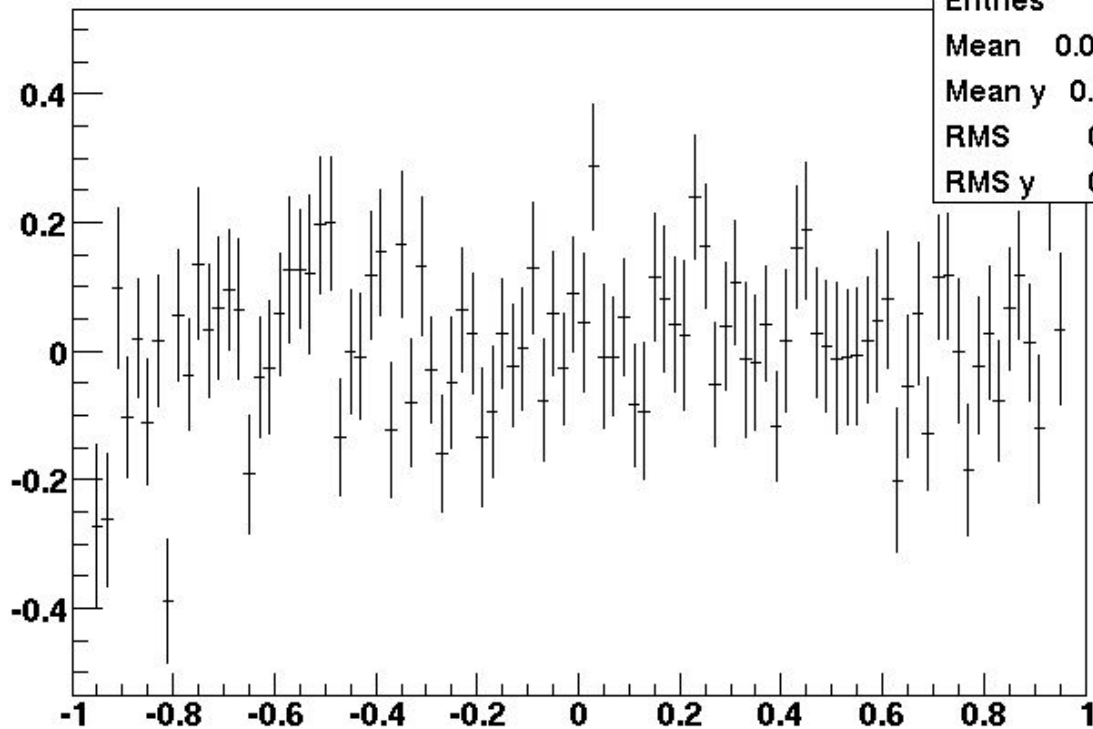
**dE/dx pull vs p profile**



**his23\_p**

|         |          |
|---------|----------|
| Entries | 27145    |
| Mean    | 0.5452   |
| Mean y  | 0.005842 |
| RMS     | 0.2607   |
| RMS y   | 1        |

**dE/dx pull vs cos(theta) profile**



**his22\_p**

|         |          |
|---------|----------|
| Entries | 9078     |
| Mean    | 0.008894 |
| Mean y  | 0.01564  |
| RMS     | 0.5397   |
| RMS y   | 0.9918   |

## Comments

The main reason of the bad shape of the  $dE/dx$  pull in FastSim at very low momenta is the fact that the expected  $dE/dx$  is calculated using the reconstructed momentum at the origin, instead of  $p$  at the DCH. Using  $p$  at the DCH reduces the bias by at least a factor 3 [see [here](#)].

Even using  $p$  at the DCH a small bias of the pull remains. Is it due to the fact that  $p$  at the DCH is not evaluated well enough? No, because the bias remains even when the true  $p$  at the DCH (the  $p$  of the first SimHit) is used [see [here](#)].

The remaining bias is due to the fact that the particle momentum changes in a non negligible way within the DCH portion of the track. Therefore if the pull is built from  $dE/dx_{\text{measured}} - dE/dx_{\text{expected}}$  where  $dE/dx_{\text{expected}}$  is the value expected at the first hit of the DCH, and  $dE/dx_{\text{measured}}$  is a weighted average over the DCH hits of the track, then there is a small (positive) bias for tracks with small betagamma.

### Possible solution:

Note: the small bias at low betagamma is not due to a problem in the  $dE/dx$  measurement, but rather in the calculation of the expected  $dE/dx$ .

Possible solutions:

| option | measured $dE/dx$   | expected $dE/dx$                         | comments  |
|--------|--|--|---|
| 1      | Measured $dE/dx$ of first DCH hit. The error is calculated as "error of 1st hit/sqrt(# of $dE/dx$ hits)" | $dE/dx$ of the first hit                 | Pro: Pulls good at low betagamma.<br>Cons: $dE/dx$ measurement perhaps unnecessarily simplified   |
| 2      | Weighted average of $dE/dx$ of the hits of the track   | $dE/dx$ of the first hit                 | As it has been so far.<br>Cons: small bias of pulls at low betagamma  |
| 3      | Weighted average of $dE/dx$ of the hits of the track   | weighted average of $dE/dx$ of the track | Pro: Pulls good at all betagamma.<br>Pro: It may be implemented so that even in case of hit-merging the pull is good.<br>Cons(?): It needs to know the PacSimHit corresponding to a reco hit. |