

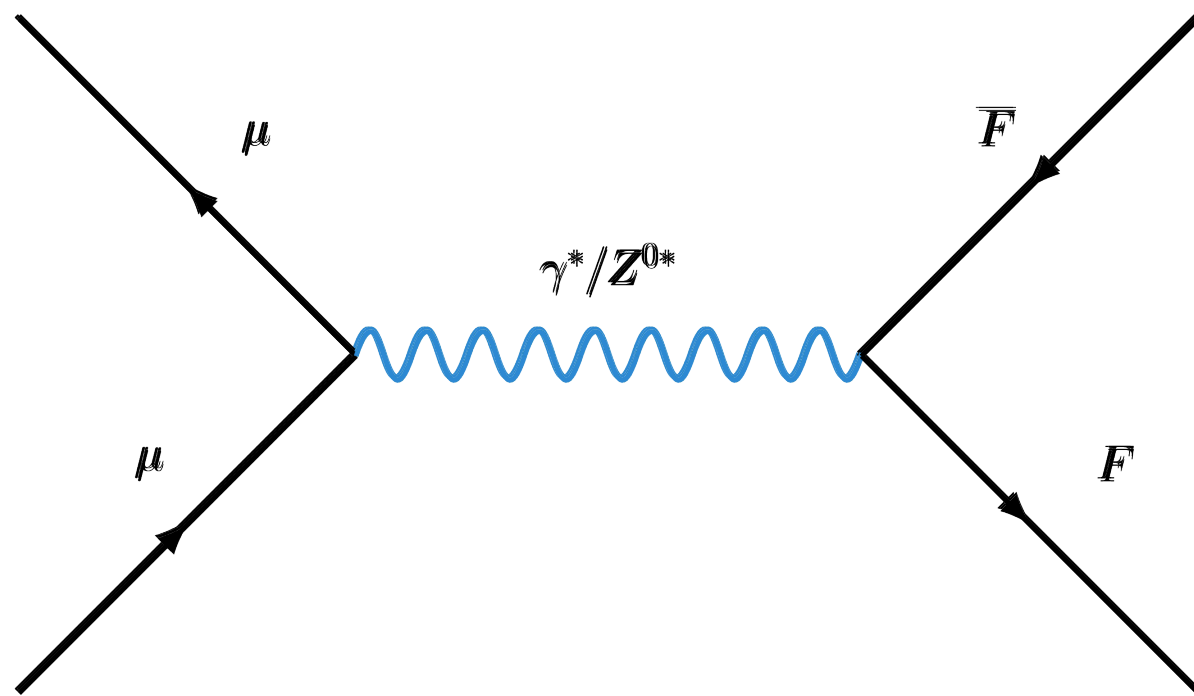
3 sectors : * direct pair production
of new heavy states...

* $W^+W^- \rightarrow X \nu\nu$ (vs $\mu^+\mu^- \rightarrow X$)

* indirect / off-shell / radiative
effects of even heavier states
(e.g. $\mu^+\mu^- \rightarrow Z'$)

* what can one do with muon collisions
 @ $\sqrt{S_{\mu\mu}}$ up to tens of TeV ???

FIRST AND FOREMOST



$$\mu^+ \mu^- \rightarrow F \bar{F}$$

* plain pair production
 of new heavy states...

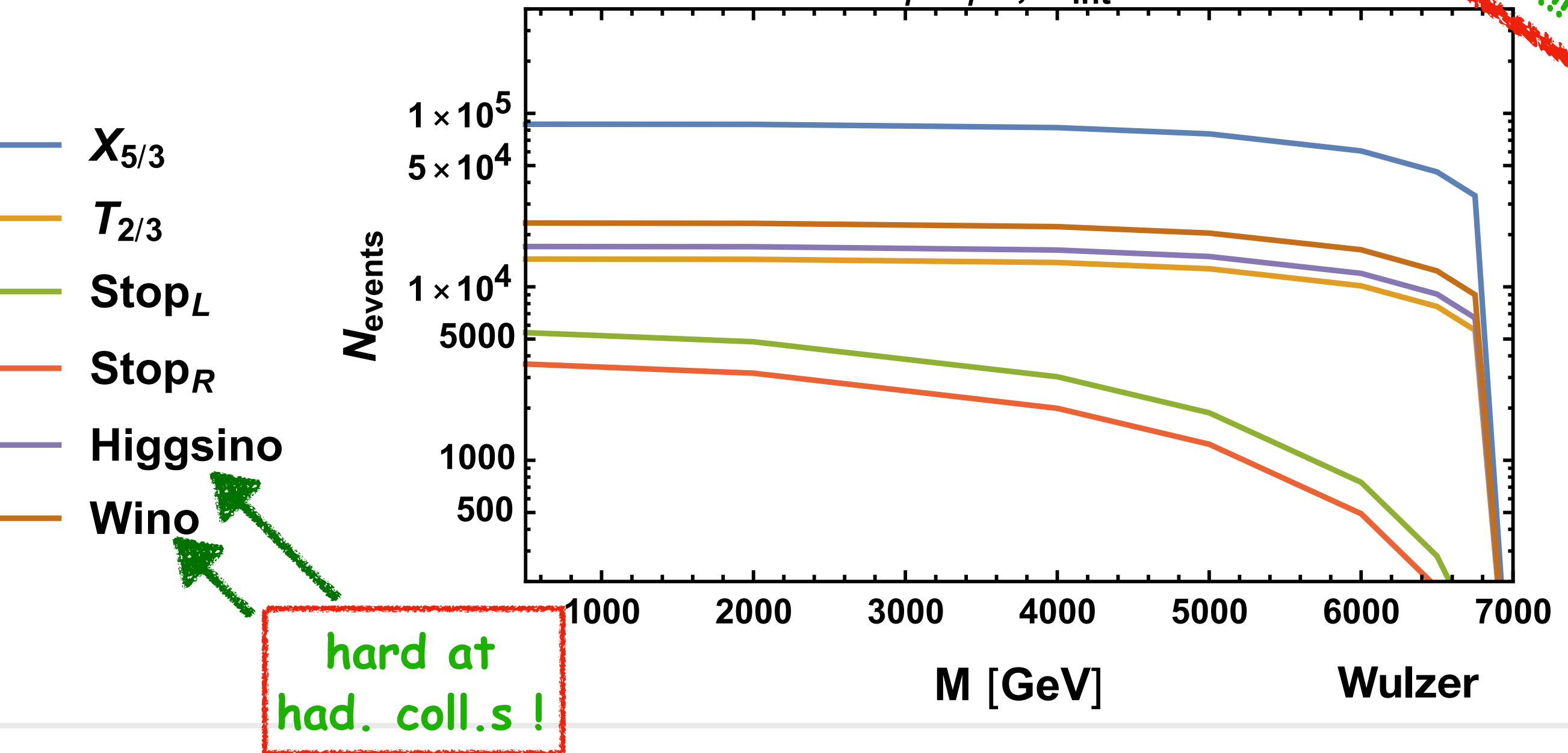
$$m_F \lesssim \sqrt{S_{\mu\mu}}/2$$

$$\sim 3, 5, 7, 15 \text{ TeV !!!}$$

Direct production $\mu\mu \rightarrow XX$

in a clean environment !!!

14 TeV $\mu^+ \mu^-$, $L_{\text{int}}=20 \text{ ab}^{-1}$



$\sigma_{\mu\mu \rightarrow XX} \sim \text{uniform up to threshold } m_F \sim \sqrt{S_{\mu\mu}}/2 !$

→ Luminosity ruled by heavy pair x-section

rate for new p.le pair production :

$$\sigma_{EW} \sim \sigma(\mu^+ \mu^- \rightarrow \gamma^* \rightarrow e^+ e^-) \sim \frac{4\pi\alpha^2}{3S}$$

point x-section

$$\rightarrow 1 \text{ fb} \left(\frac{10 \text{ TeV}}{\sqrt{S}} \right)^2$$

no m_e dependence
up to $m_e \sim \sqrt{S}/2$!

$$L \sim 10^{35} \text{ cm}^{-2} \text{ s}^{-1} \sim 1 \text{ ab}^{-1} / \text{y}$$

$$\rightarrow 1000 \text{ evs/y} \left(\frac{10 \text{ TeV}}{\sqrt{S}} \right)^2$$

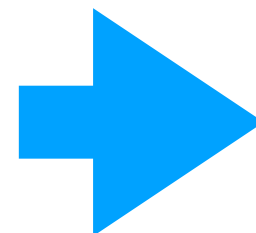
$\sqrt{S}_{\mu\mu}$

$\int L_{10y}$

10 TeV

10 ab^{-1}

$10^4 \text{ evs} / (10 \text{ years})$



14 TeV

20 ab^{-1}

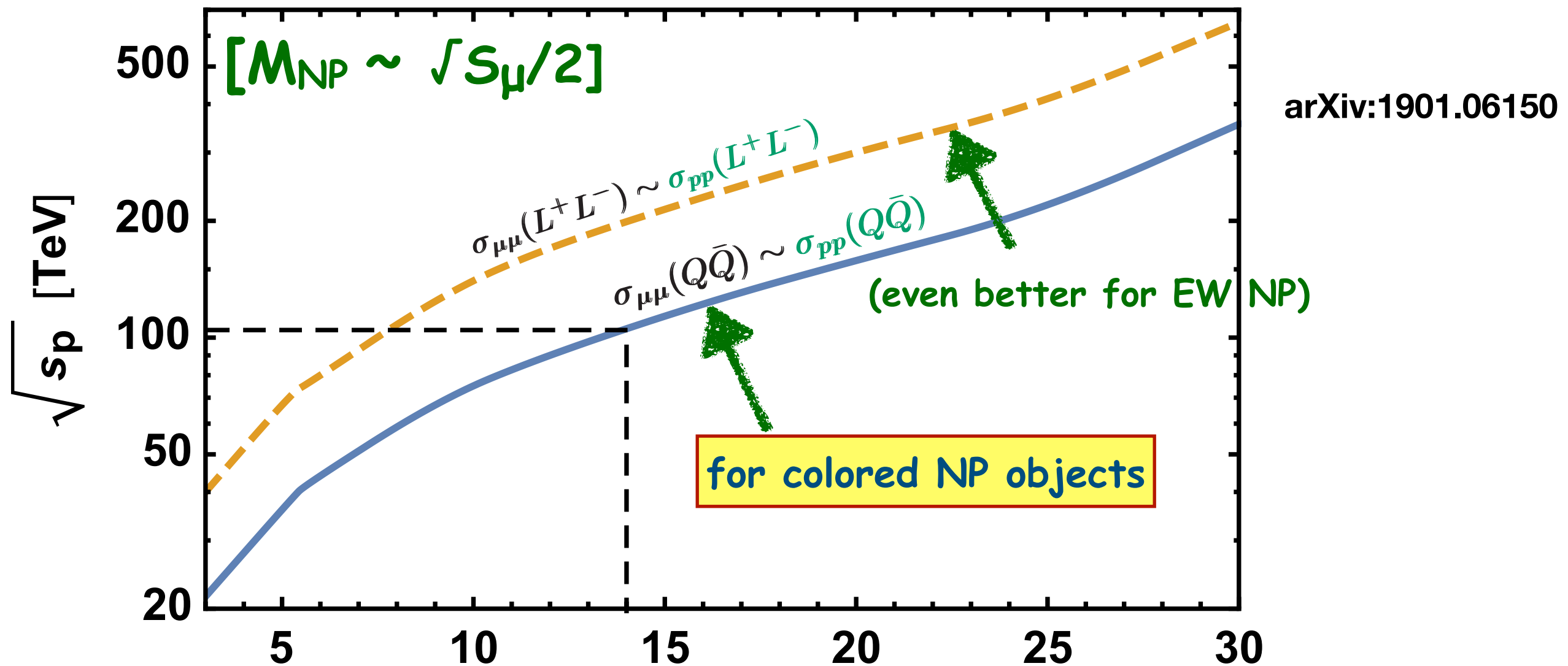
$\delta_{\text{stat}} \sim 1\%$

30 TeV

100 ab^{-1}

$$L \sim 10^{36} \text{ cm}^{-2} \text{ s}^{-1}$$

"equivalent" reach in pp after rescaling for pdf's

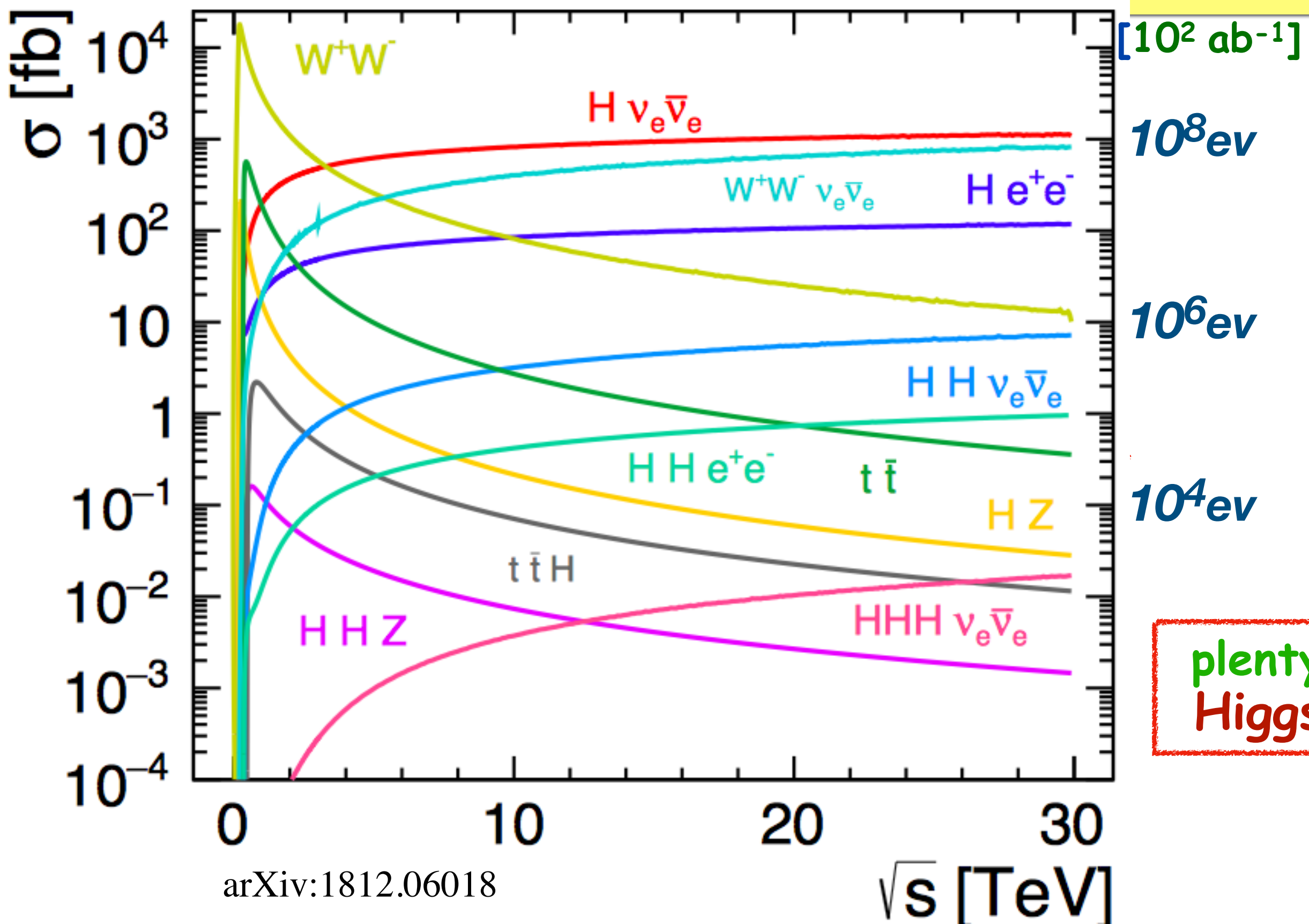


- $\sqrt{s_\mu}$ [TeV]
- * $\mu\mu$ @ 14 TeV \rightarrow pp @ 100 (200)_{EW} TeV !
 - * $\mu\mu$ @ 30 TeV \rightarrow pp @ 350 (600)_{EW} TeV !!
- yet unexplored pheno !!!*

WARNING !!

- * actually physical BACKGROUND
to $\mu^+\mu^-$ (e^+e^-) collisions hugely better
than in hadron collisions
- * this moves equivalent $\sqrt{S}_{\mu\mu}$ (at fixed \sqrt{S}_{pp})
at even lower values in general...

at $\sqrt{s}_{\mu\mu} > \text{a few TeV's}$
 point $\sigma_{\mu\mu \rightarrow X}$ superseded by $\sigma_{WW \rightarrow X}$!



VBF events (green) + $\sigma_{WW \rightarrow X} / \sigma_{\mu\mu \rightarrow X}$ (red)

# events	3 TeV/5/ab	(VBF)/(s-ch)3TeV	14 TeV/20/ab	(VBF)/(s-ch)14TeV	30 TeV/100/ab	(VBF)/(s-ch)30TeV
<i>H</i>	2,5E+06		1,9E+07		1,2E+08	
<i>HZ</i>	4,9E+04	7	9,0E+05	700	7,4E+06	5300
<i>HZZ</i>	6,0E+02	1,5	3,2E+04	180	3,7E+05	1500
<i>HWW</i>	1,5E+03	0,3	6,8E+04	30	7,6E+05	190
<i>HH</i>	4,1E+03		8,8E+04		7,4E+05	
<i>HHZ</i>	4,7E+01	0,3	2,8E+03	40	3,3E+04	300
<i>HHZZ</i>	4,6E-01	0,1	7,8E+01	16	1,2E+03	130
<i>HHWW</i>	1,2E+00	0,02	1,8E+02	1	2,9E+03	1
<i>HHH</i>	1,5E+00		1,4E+02		1,9E+03	
<i>HHHZ</i>	2,4E-02	0,3	3,8E+00	12	5,1E+01	100

[Maltoni et al]

<i>tt</i>	2,6E+04	0,3	4,2E+05	24	3,1E+06	160
<i>ttH</i>	6,5E+01	0,03	3,0E+03	5	3,1E+04	40
<i>ttZ</i>	5,5E+02	0,07	2,6E+04	7	2,8E+05	50
<i>ttHH</i>	1,7E-01	0,006	1,3E+01	1	1,6E+02	10
<i>ttHZ</i>	1,8E+00	0,01	2,0E+02	2	2,7E+03	14
<i>ttZZ</i>	7,0E+00	0,03	1,2E+03	4	1,7E+04	30
<i>ttWW</i>	1,4E+01	0,008	2,2E+03	0,8	3,0E+04	5
<i>tttt</i>	3,4E-01	0,01	2,2E+01	0,4	2,1E+02	2

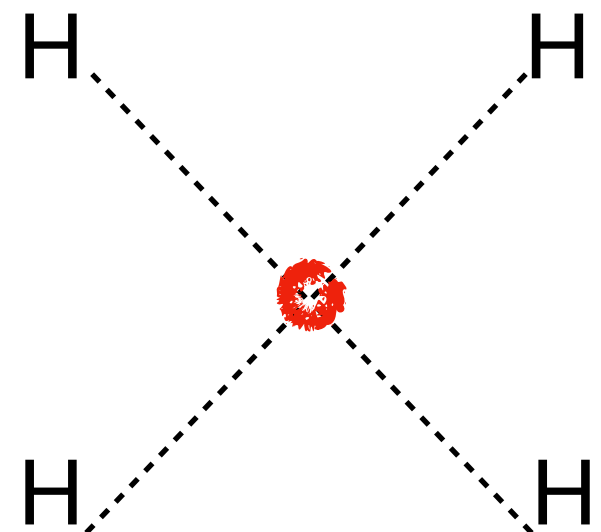
Higgs self-interaction couplings

- * the "tough topic" even at "most-future" colliders
- * most interesting to measure from theory side....

$$\mathcal{L} = -\frac{1}{2}m_h^2 h^2 - \boxed{\lambda_3} \frac{m_h^2}{2v} h^3 - \boxed{\lambda_4} \frac{m_h^2}{8v^2} h^4$$

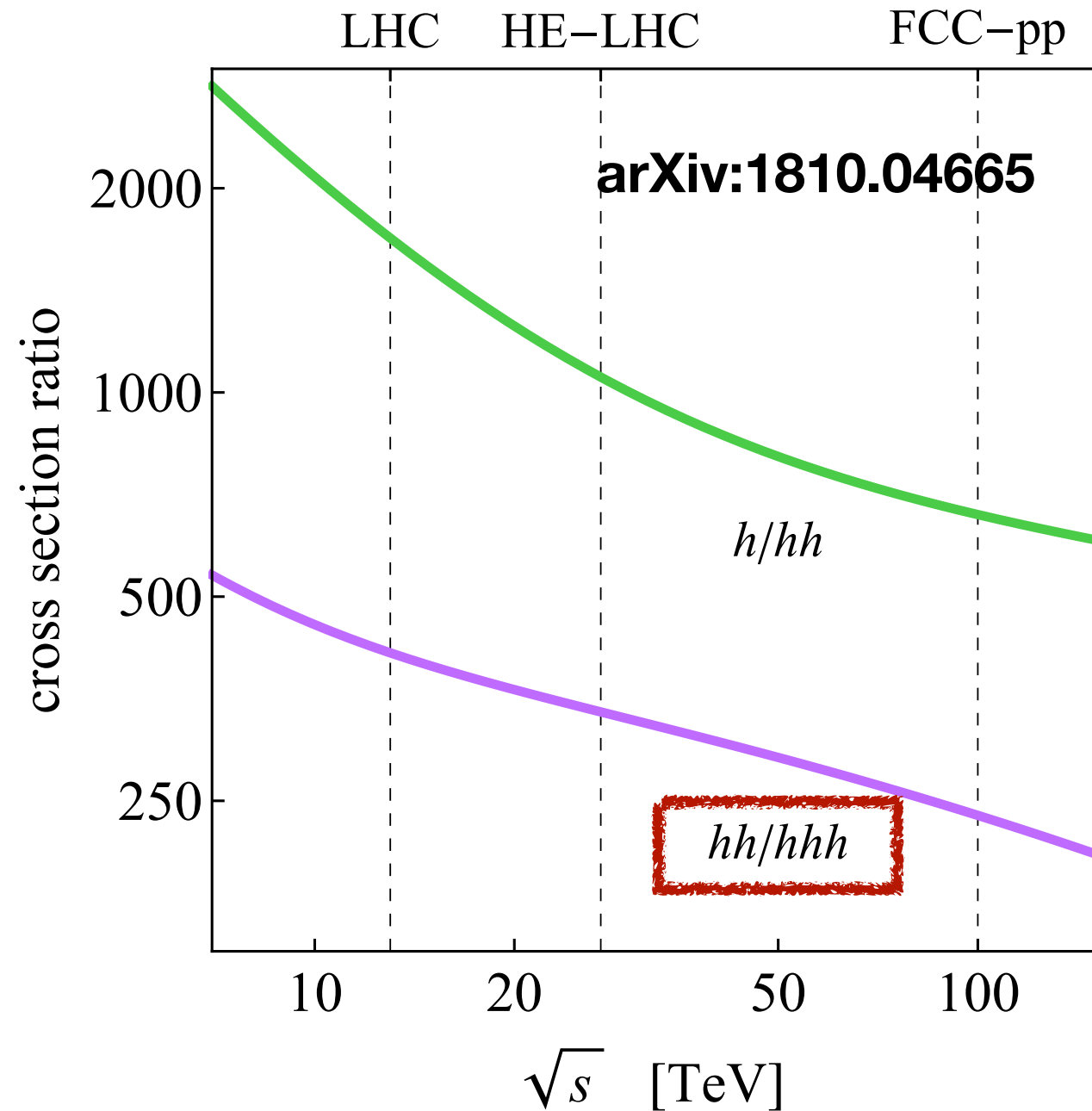
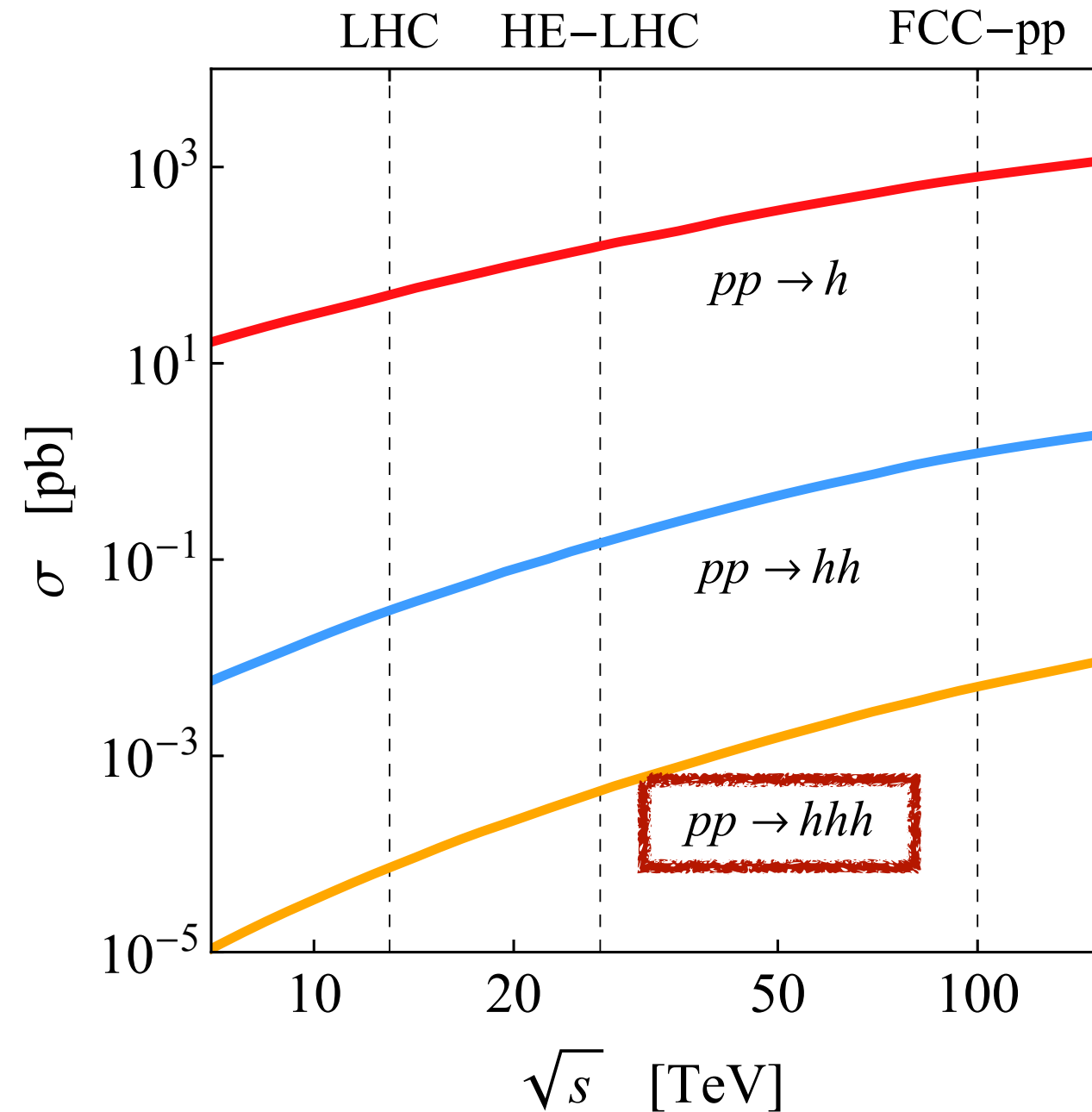
$$\lambda_3^{SM} = \lambda_4^{SM} = 1$$

what about **quartic**
H self-coupling ?



FCC-pp : λ_4

$$\mathcal{L} = -\frac{1}{2}m_h^2 h^2 - \lambda_3 \frac{m_h^2}{2v} h^3 - \boxed{\lambda_4 \frac{m_h^2}{8v^2} h^4}$$

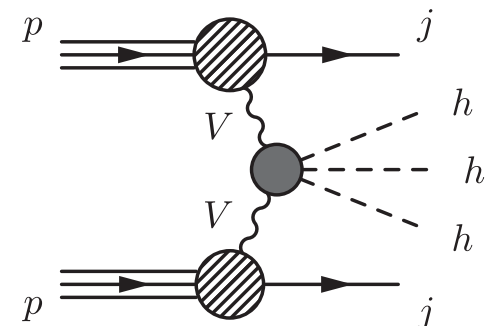


$hhh \rightarrow (b\bar{b})(b\bar{b})(\gamma\gamma)$ [optimistic scenario !!!] :

$$\lambda_4 \in [\sim -4, \sim +16]$$

at 100 TeV, 30 ab $^{-1}$

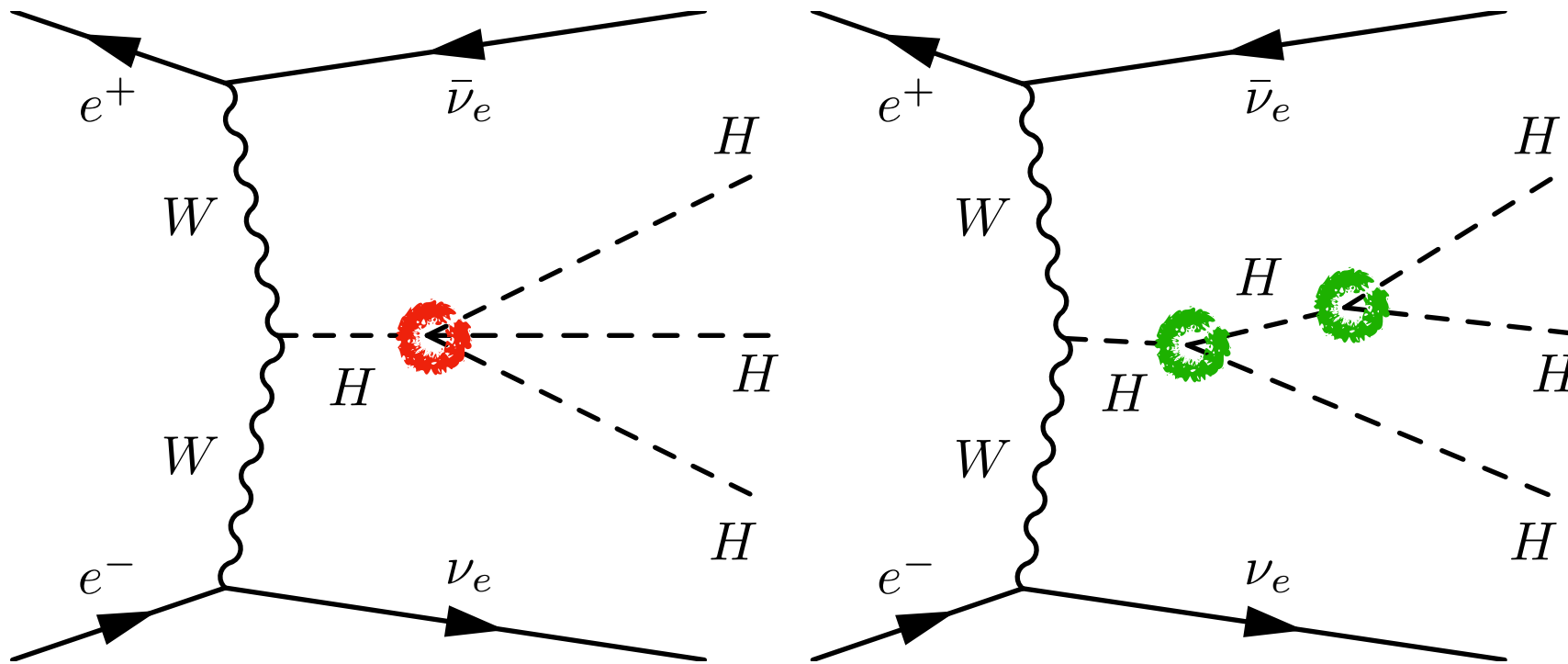
(95% C.L.)



arXiv:1606.09408

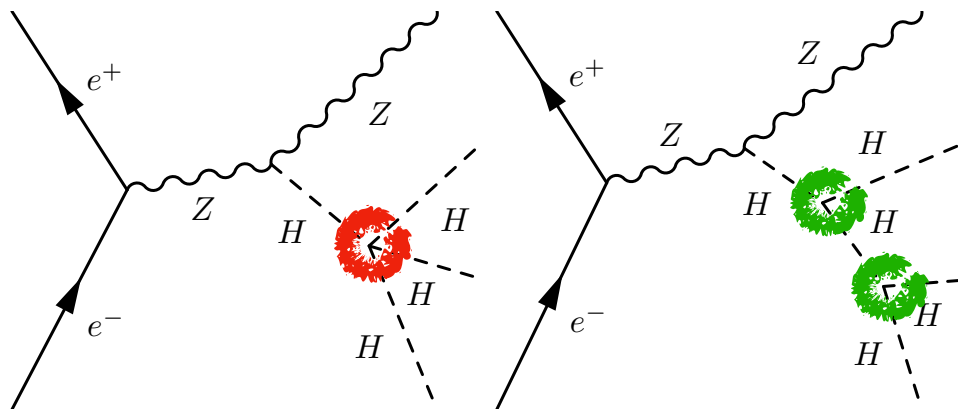
$$\mu^+ \mu^- \rightarrow HHH\nu\bar{\nu}, \quad (\nu = \nu_e, \nu_\mu, \nu_\tau)$$

$$V_h = \frac{m_h^2}{2} h^2 + (1 + \boxed{\kappa_3}) \lambda_{hhh}^{\text{SM}} v h^3 + \frac{1}{4} (1 + \boxed{\kappa_4}) \lambda_{hhhh}^{\text{SM}} h^4$$



$$(\kappa_i \rightarrow \delta_i)$$

$$\Delta = \frac{N - N_{SM}}{\sqrt{N_{SM}}} = \left(c_1 \kappa_3 + c_2 \kappa_4 + c_3 \kappa_3 \kappa_4 + c_4 \kappa_3^2 + c_5 \kappa_4^2 + c_6 \kappa_3^3 + c_7 \kappa_3^2 \kappa_4 + c_8 \kappa_3^4 \right)$$



HHHZ negligible !

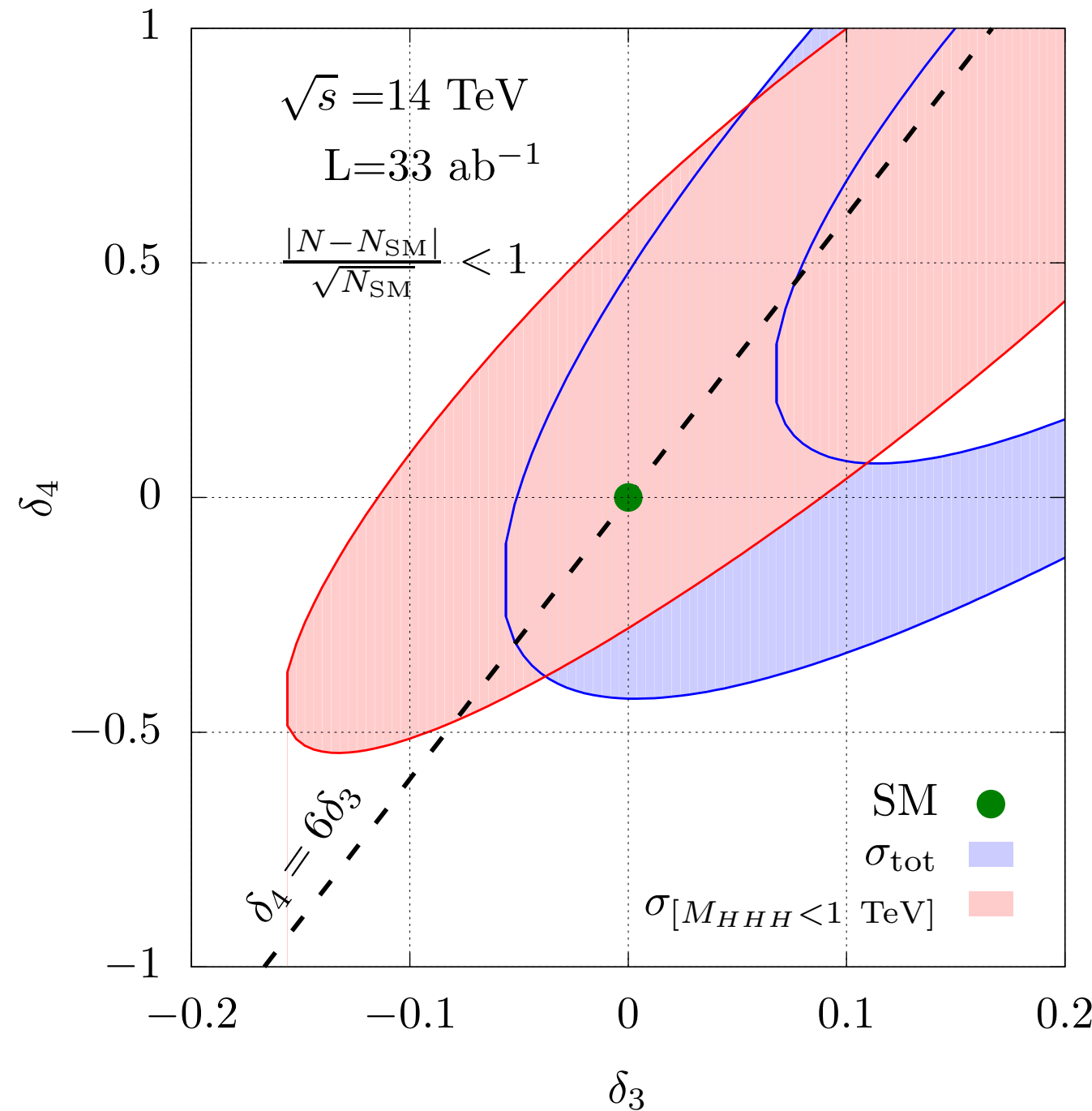
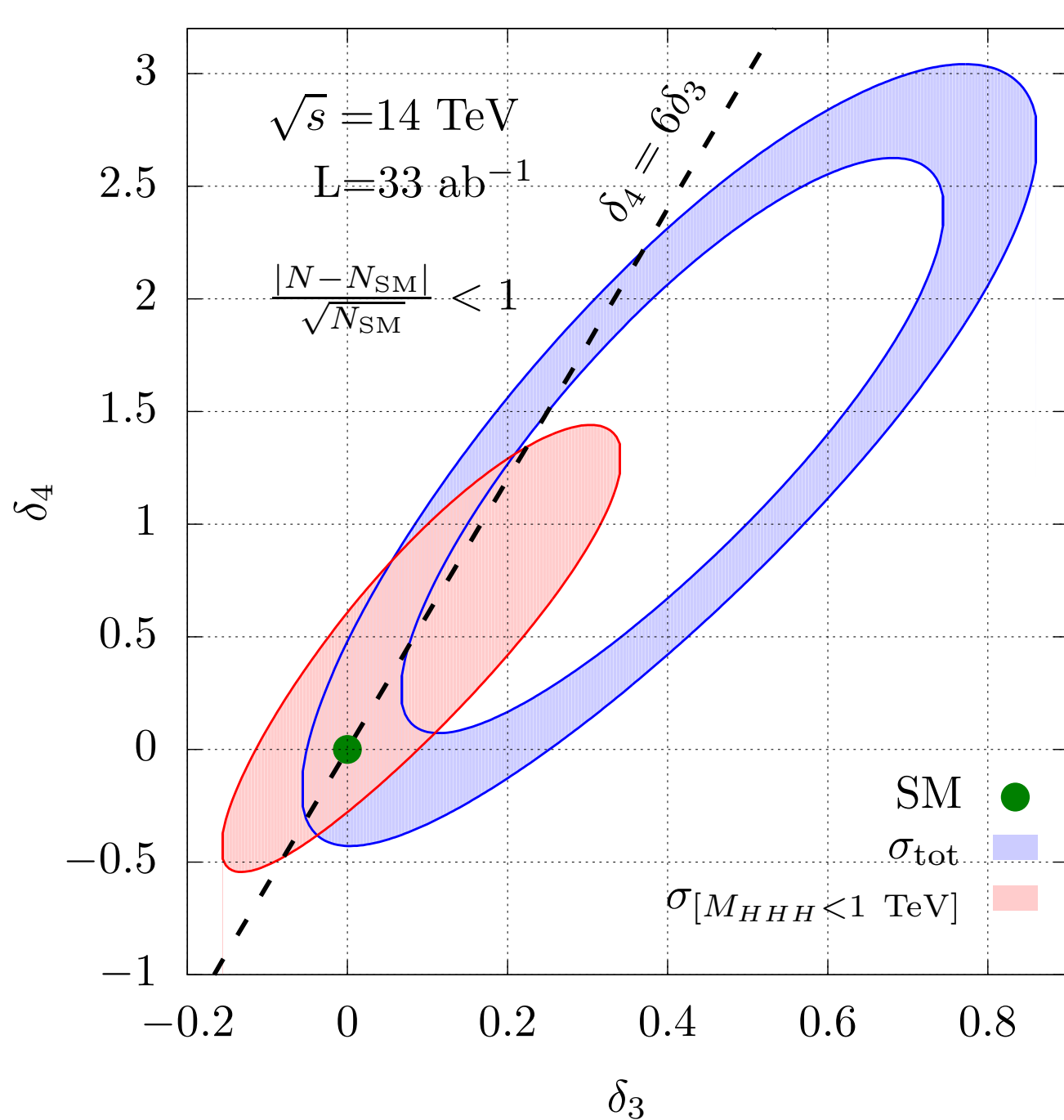
$$\sigma_{HHHZ} \sim 1/2 \sigma_{HHH} \text{ @ } 3\text{TeV}$$

$$\sim 1/50 \sigma_{HHH} \text{ @ } 30\text{TeV}$$

$(N-N_{SM})/\sqrt{N_{SM}}$ versus (δ_3, δ_4)

VBF \rightarrow HHH

Chiesa, Maltoni, Mantani, BM, Piccinini, Zhao, 2003.13628



[$\delta_3=0$] $-0.4 < \delta_4 < 0.4$ (68%CL) !!!

$(N - N_{\text{SM}})/\sqrt{N_{\text{SM}}}$ versus δ_4

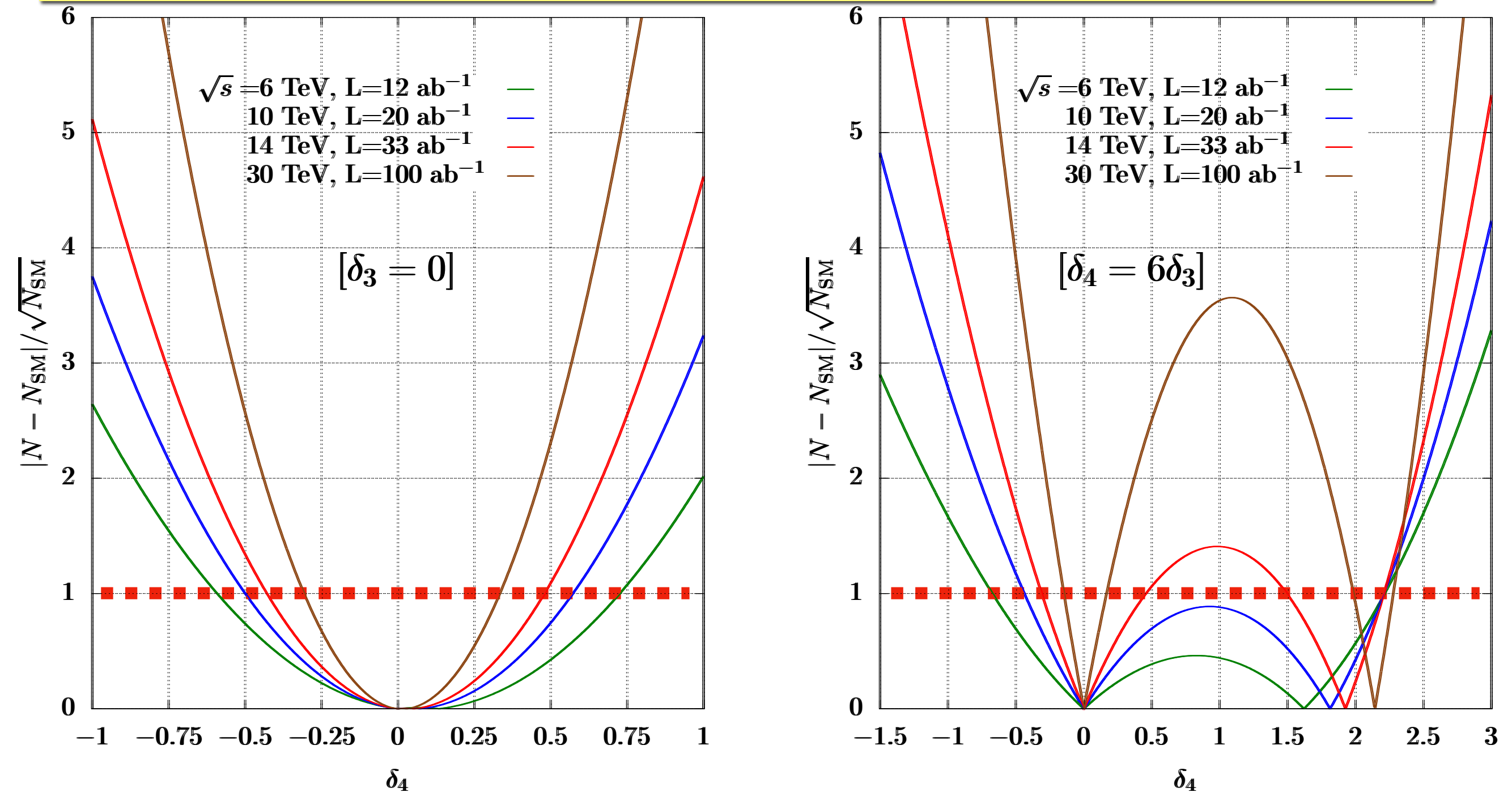
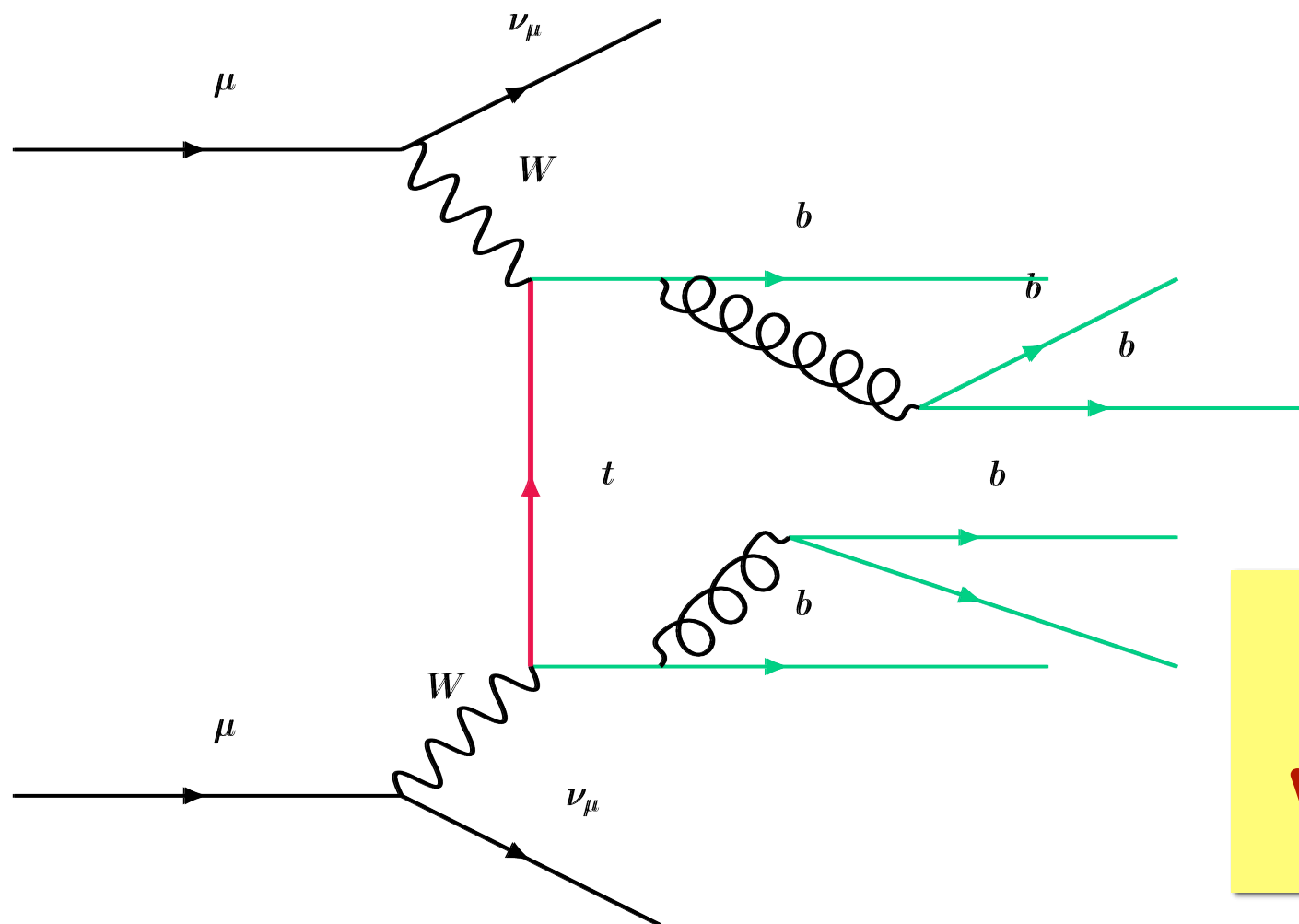


Figure 13: Sensitivity to the quartic Higgs self-coupling in terms of standard deviations $|N - N_{\text{SM}}|/\sqrt{N_{\text{SM}}}$ with respect to the SM configuration, where the event numbers N refer to $\sigma(\mu^+ \mu^- \rightarrow H H H \nu \bar{\nu})$, for $M_{\nu\nu} \gtrsim 150 \text{ GeV}$, for $\delta_3 = 0$ (left), and $\delta_4 = 6\delta_3$ (right). Results are obtained considering deviations from the inclusive cross sections only.

backgrounds to $VBF \rightarrow HHH$

- * 8-body final states (at least !)
→ very hard to evaluate via MC's
- * all H decay modes are relevant ! [BR(HHH \rightarrow 6 b) \sim 20 %]
- * 6b-jet bckgr moderate at FCC-pp [arXiv:1801.10157]
- * might be $S/B \gg 1$ at multi-TeV muon colliders...



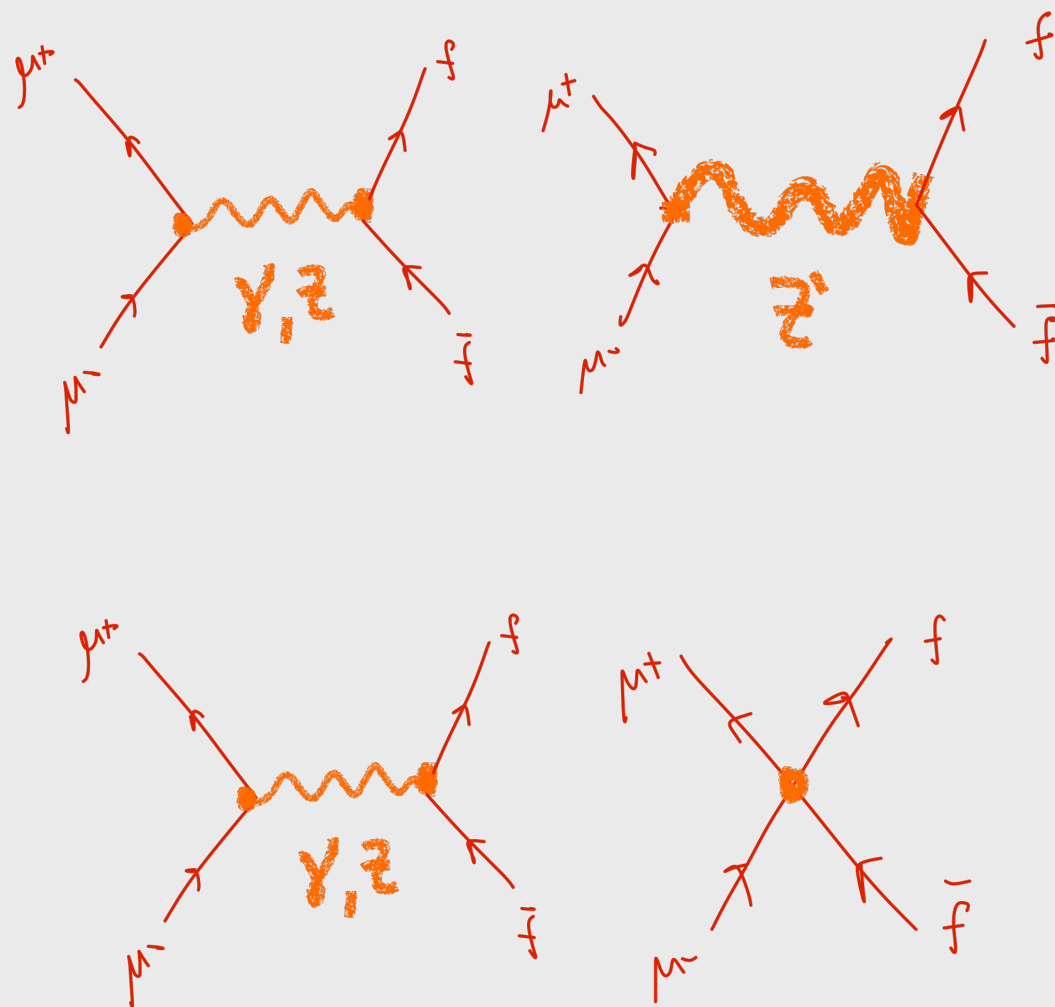
MC development for
WW approx. needed !

off-shell effects

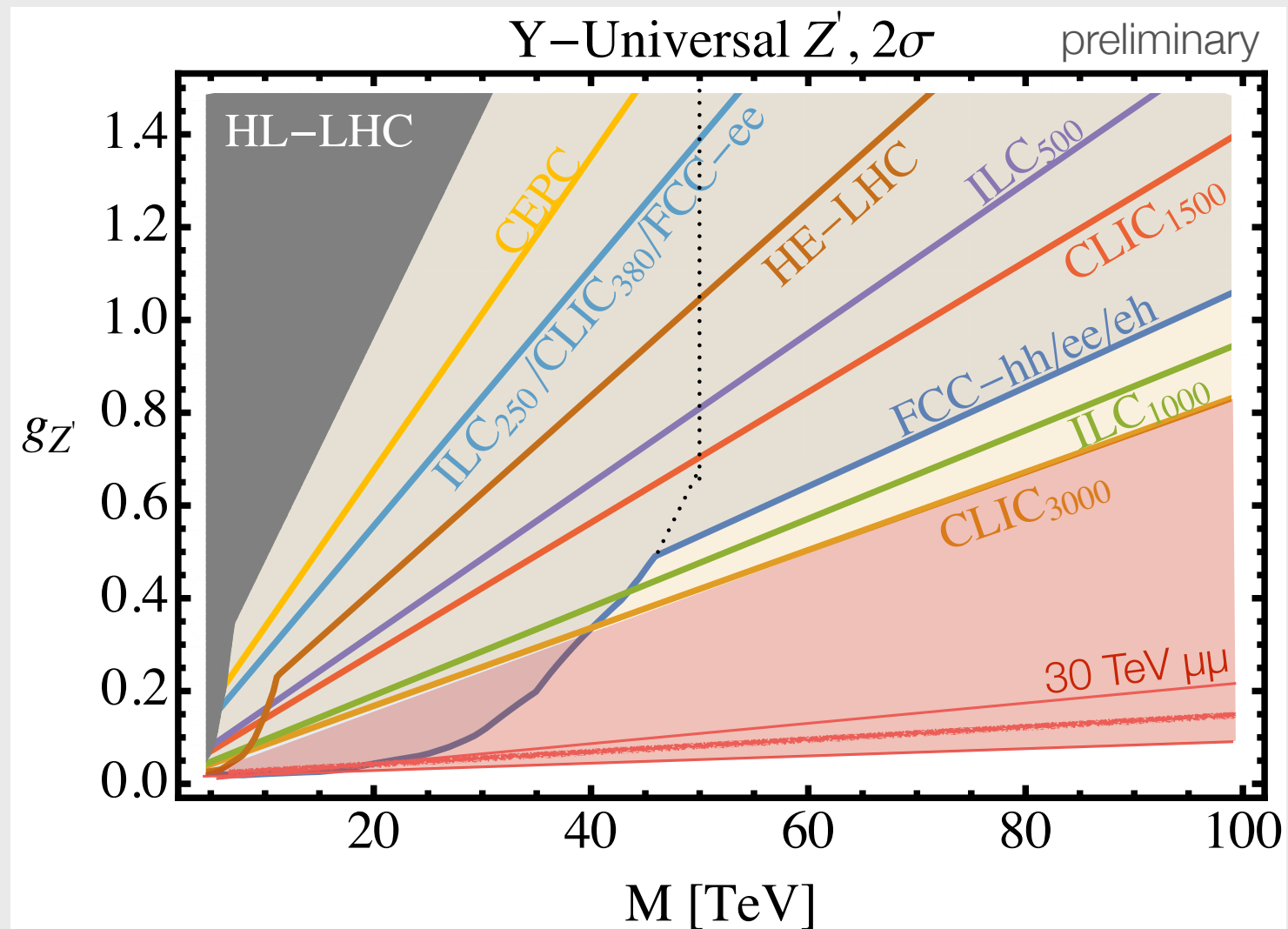
A heavy Z'

DRELL-YAN

RATES AND ANGULAR DISTRIBUTIONS



Franceschini



the “size” of the Higgs boson

Buttazzo, Franceschini, Wulzer

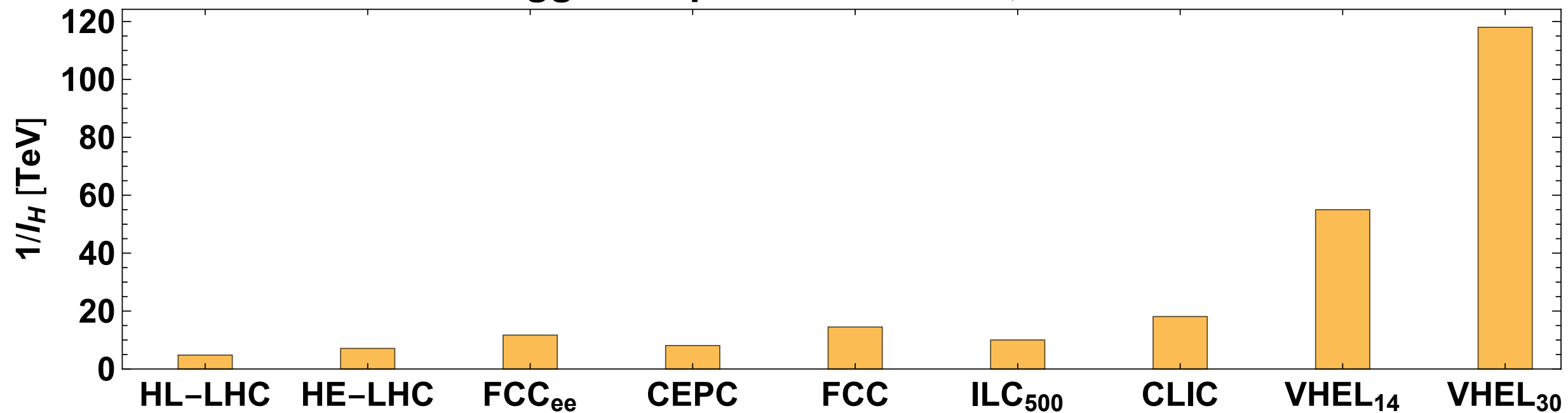
$$\ell_{Higgs} \sim m_{\star}^{-1}$$




(EFT approach)

Compositeness Reach:

Higgs compositeness scale, 2σ reach



a few final comments

- * such a high energy at pointlike level opens up hugely new perspectives !
- * μ colliders @10's TeV can be considered WW colliders !
- * qualitatively new Higgs physics (test quartic self-coupl.)
- * physics bckgds expected mild also for hadronic final states BUT simulations are quite hard (many particles in phase-space)  implement Equivalent Vector-Boson Approx. in MC's !
- * many many possible new directions for exploring BSM in off-shell/indirect effects via precision measurements [also VBF-production role to be extensively considered...]