

# Core-crust transition in neutron stars

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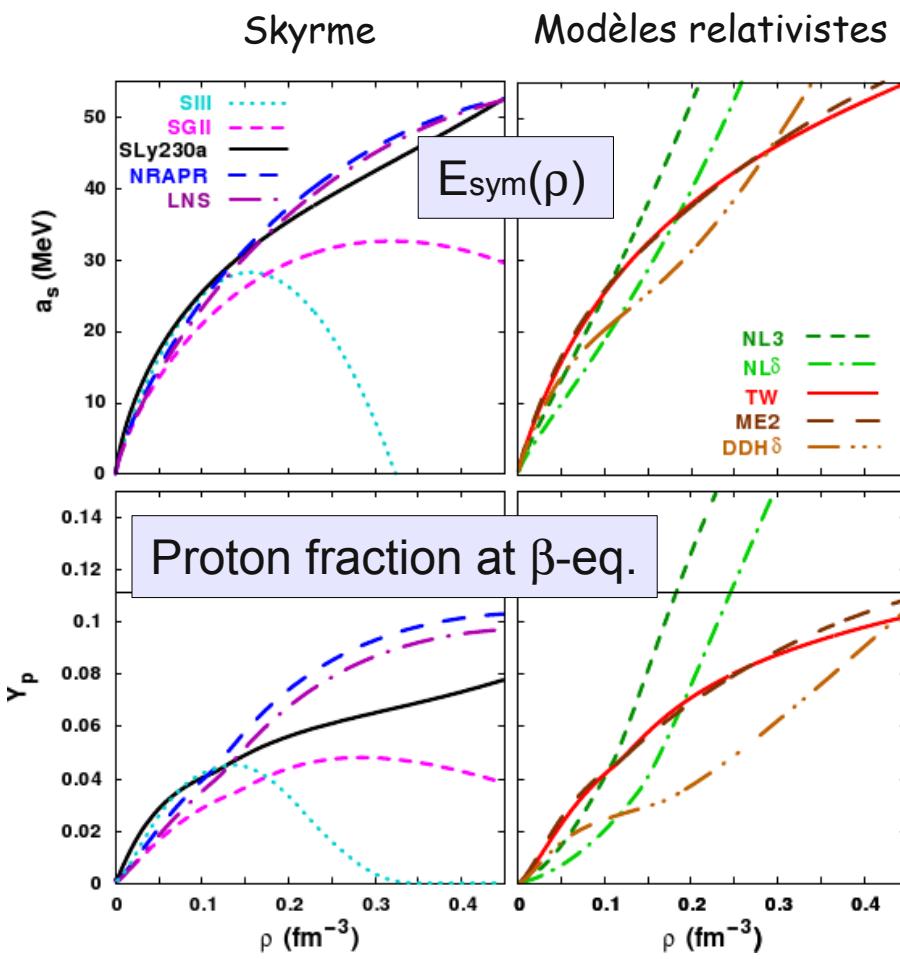
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## Collaborators:

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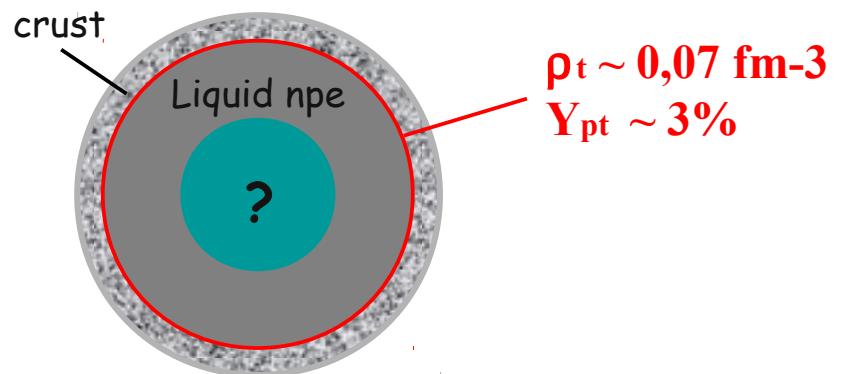
# Introduction

asy-EOS : a crucial issue  
for compact-star physics



C. D. et al., PRC 78 (2008)

Focus : core-crust transition



asy-EOS affects:

- × Transition density  $\rho_t$
  - × Transition pressure  $P_t$
- } Mass + Width of the crust

**Observations:** glitches, X-ray transients, ...

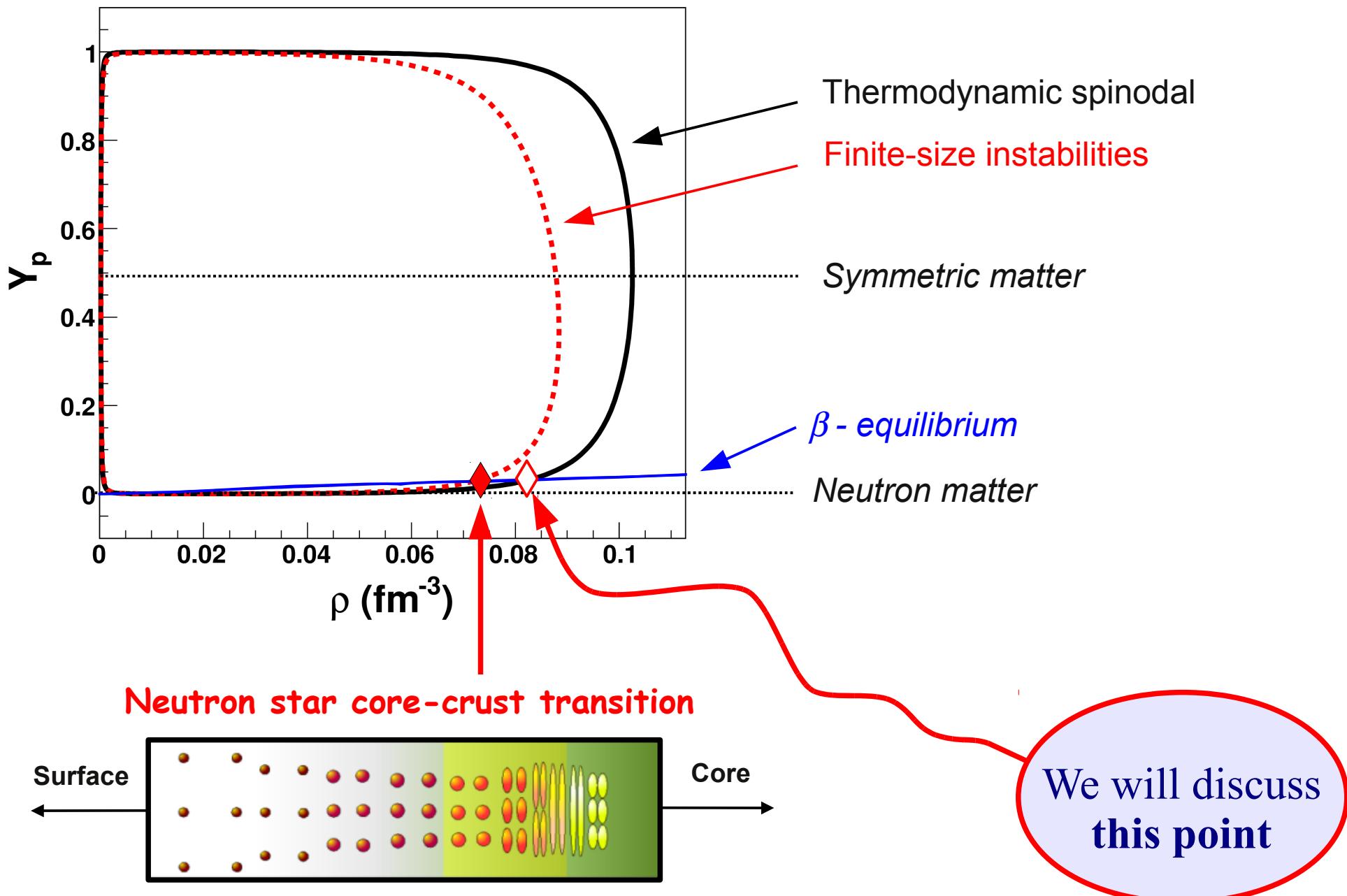
This work :

how the **symmetry-energy slope** at saturation  
affects transition **position** and **pressure**  
using Skyrme + Relativistic effective models

# Symmetry-energy slope L and position of the core-crust transition

$$L = 3 \rho_0 \frac{\partial E_{sym}}{\partial \rho}(\rho_0)$$

# Core-crust transition : $\beta$ -spino crossing



# Effect of L on the proton fraction Y<sub>p</sub>

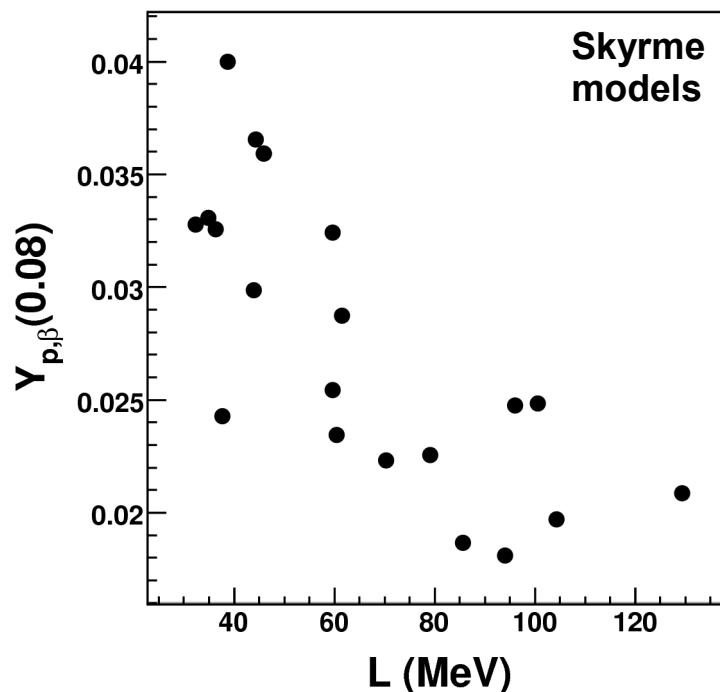
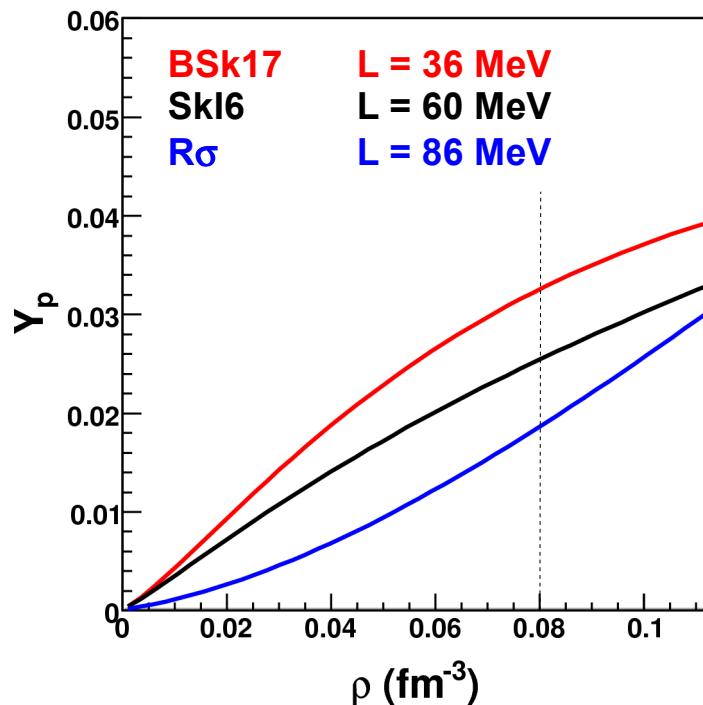
**$\beta$ -equilibrium :**  $p + e^- \rightarrow n (+\nu_e)$        $(\mu_n - \mu_p) + (\mu_e - \mu_\nu) = 0$

$\underbrace{\hspace{10em}}$

$\sim 4 E_{sym}(\rho) * (1 - 2Y_p)$

$L = 3 \rho_0 \frac{\partial E_{sym}}{\partial \rho}(\rho_0)$

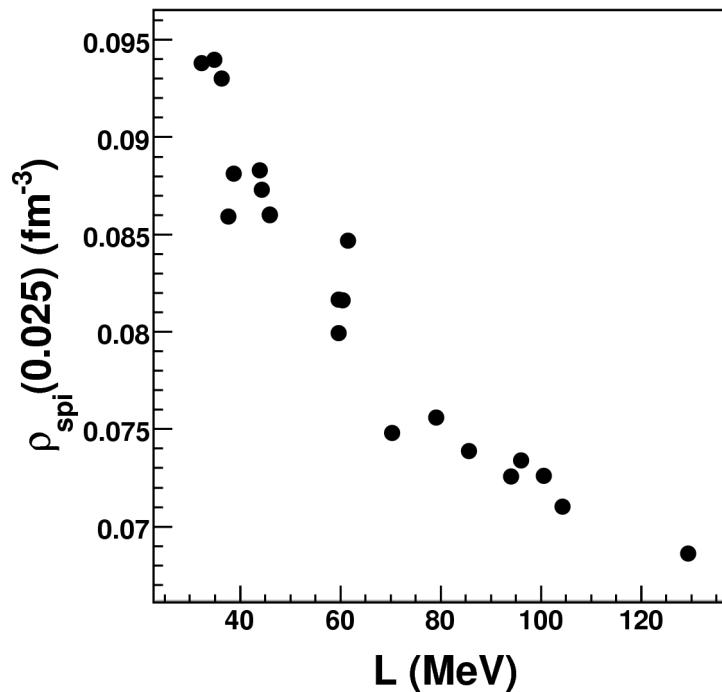
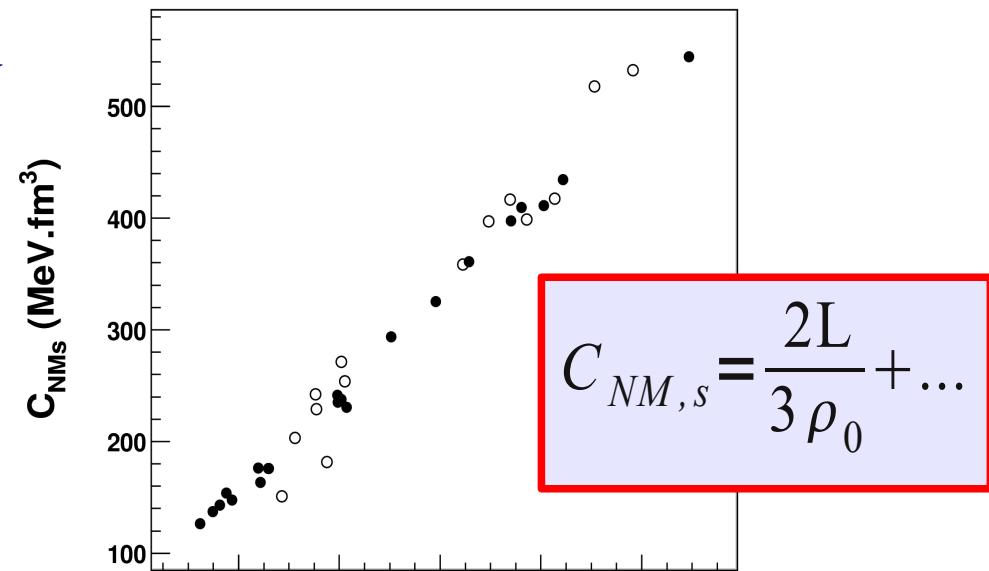
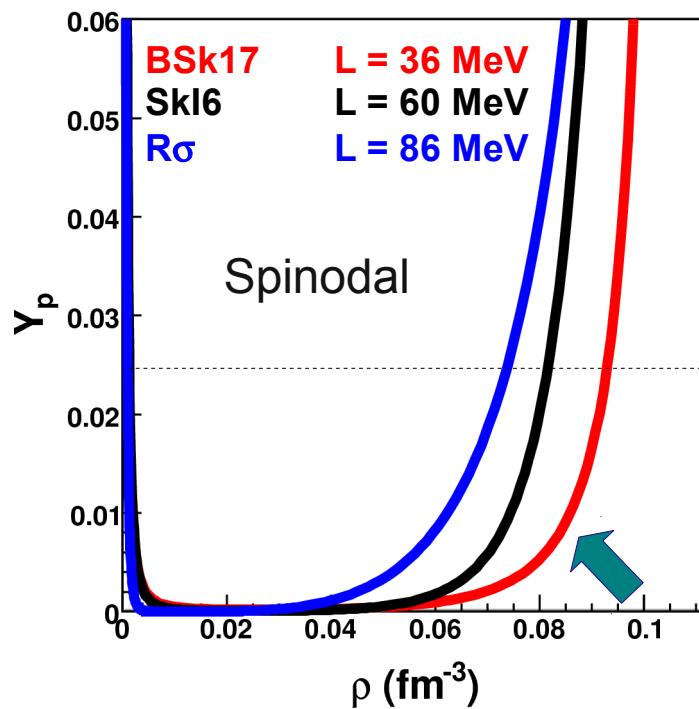
Higher  $L \rightarrow$  Lower  $E_{sym}(\rho < \rho_0) \rightarrow$  Higher  $Y_p(\rho < \rho_0)$



# Effect of L on the spinodal border

$C_{NM,s}$  = Energy-density curvature  
of neutron matter at spinodal density  
( $\sim 0.1 \text{ fm}^{-3}$ )

- Higher  $L$
- Higher  $C_{NM,s}$
- Lower  $p_t$

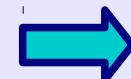


# Effect of L on the transition point

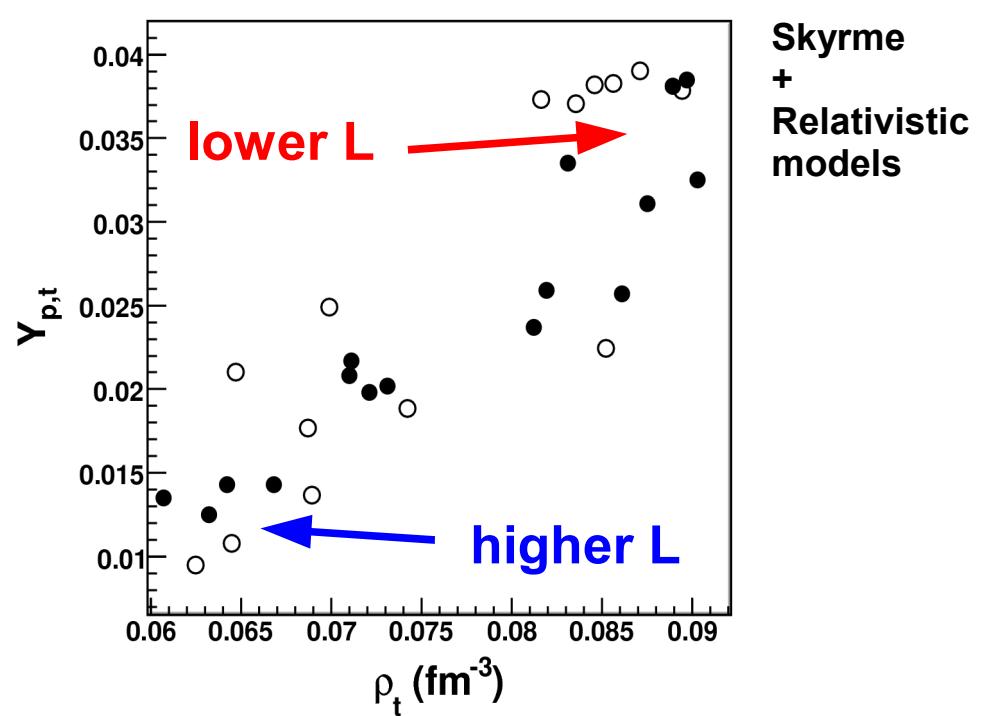
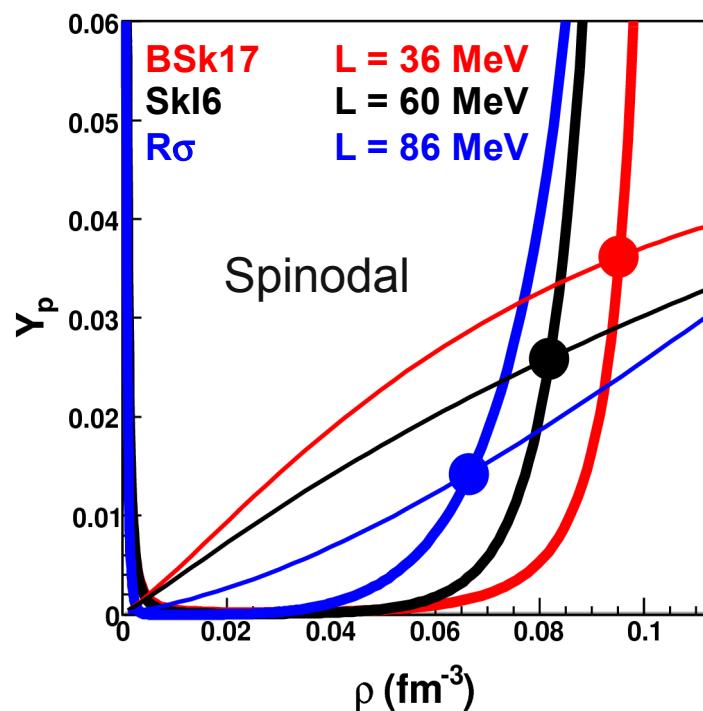
Crossing between  $\beta$ -equilibrium and spinodal border:

L affects  $Y_{p,\beta}(\rho)$   
L affects  $\rho_{\text{spino}}(Y_p)$

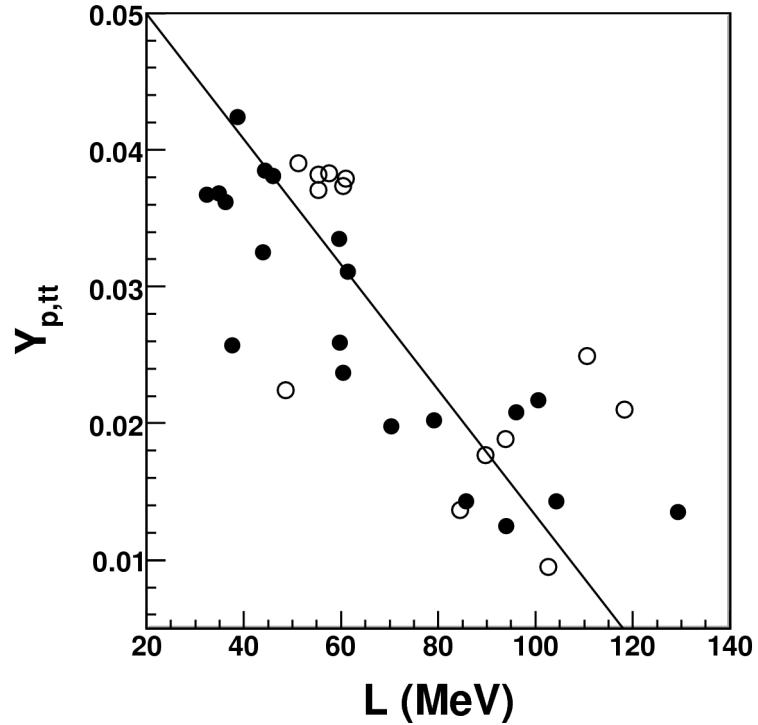
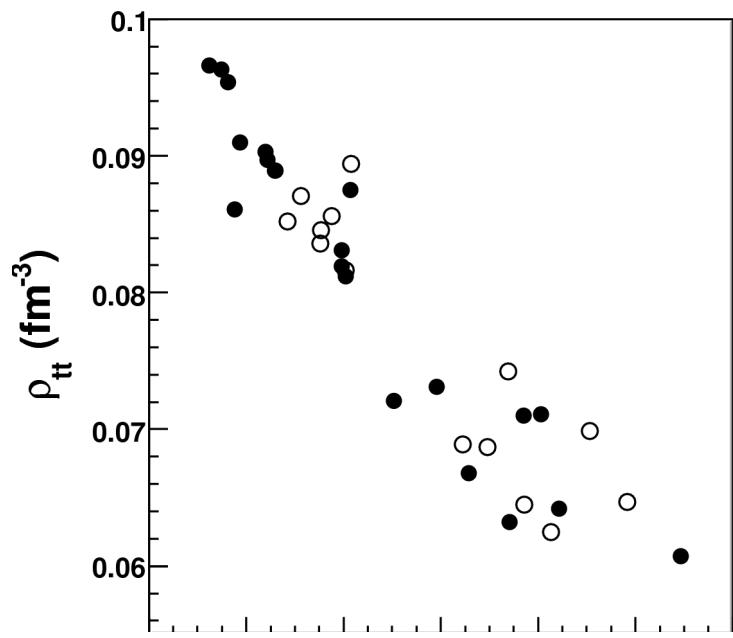
Conjonction  
of the 2 effects



Higher L  
Lower  $Y_{p,t}$   
Lower  $\rho_t$



# Effect of L on the transition point

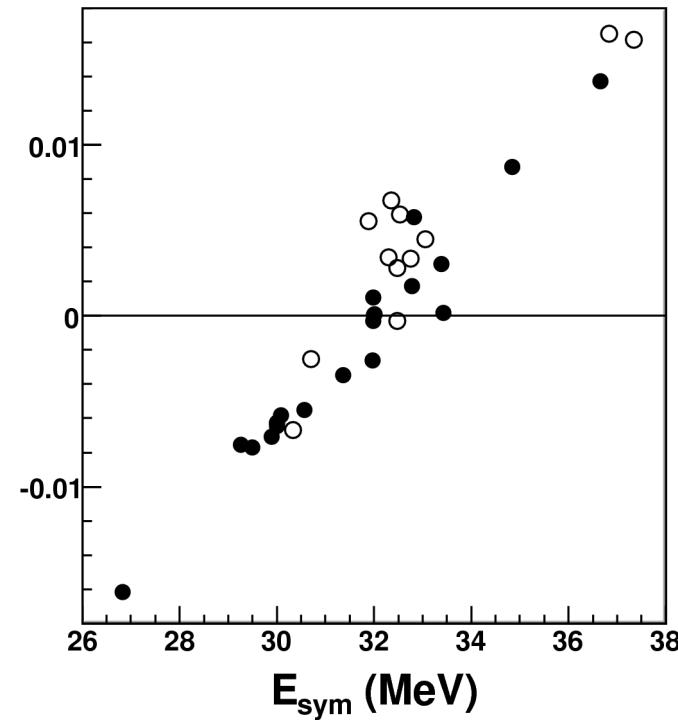


✓ Clear decreasing correlations

Higher  $L$   $\left\{ \begin{array}{l} \text{Lower } \rho_t \\ \text{Lower } Y_{p,t} \end{array} \right.$

✓ Important dispersion for  $Y_{p,t}$

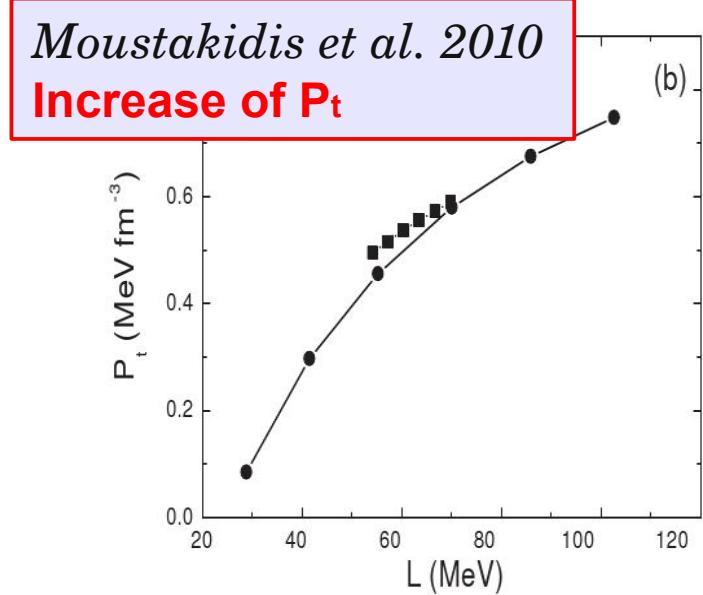
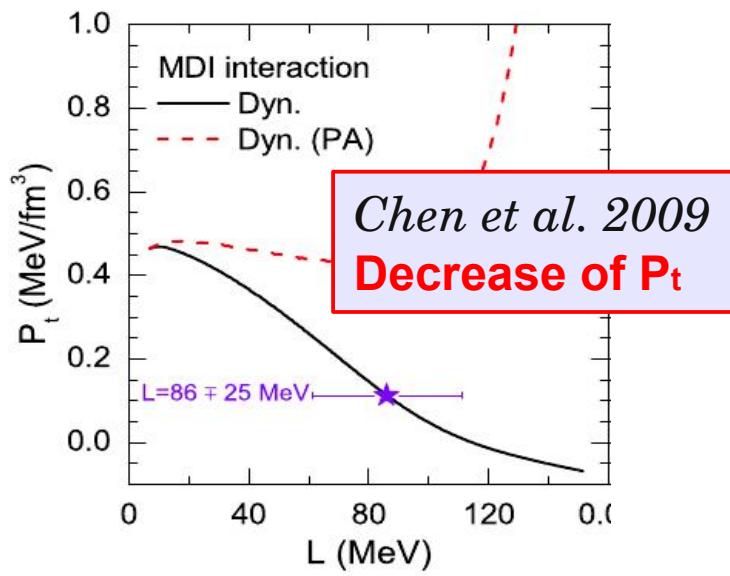
Linked to dispersion for  $E_{\text{sym}}(\rho_0)$



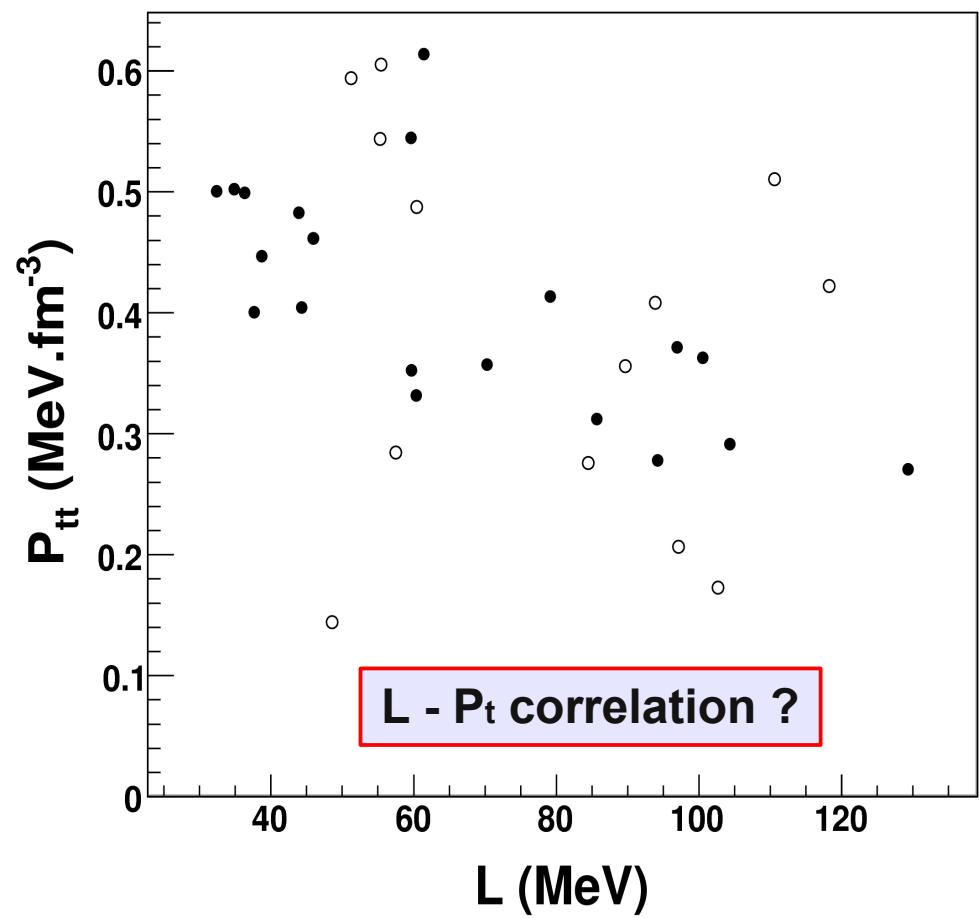
# Symmetry-energy slope L and core-crust transition pressure

$$L = 3 \rho_0 \frac{\partial E_{sym}}{\partial \rho}(\rho_0)$$

# Effet of L on the transition pressure



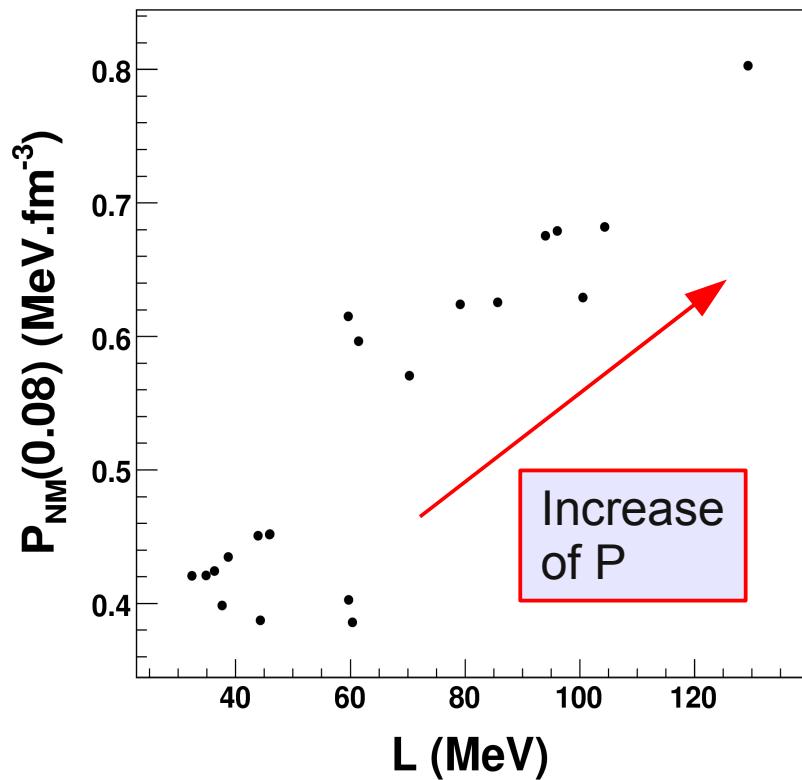
**Skyrme + Relativistic effective models**



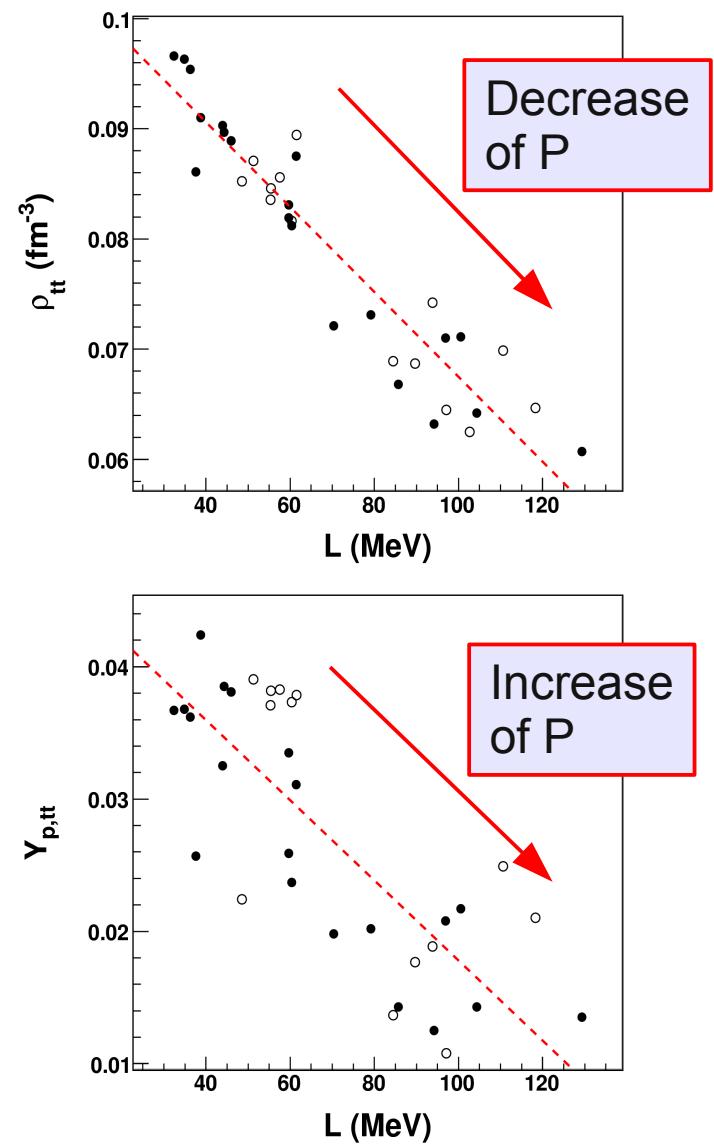
# $P_t(L)$ : what should we expect ?

In n-rich matter, for a fixed density:  
**P increases with L**

$$P(\rho, y) = \frac{\rho^2}{3\rho_0} \left[ Ly^2 + (K_0 + K_s y^2) \frac{\rho - \rho_0}{3\rho_0} + \dots \right]$$



**But the transition point moves...**



# Transition pressure: different contributions

$$P(\rho, y) = \frac{\rho^2}{3\rho_0} \left[ Ly^2 + (K_0 + K_s y^2) \frac{\rho - \rho_0}{3\rho_0} + \dots \right]$$

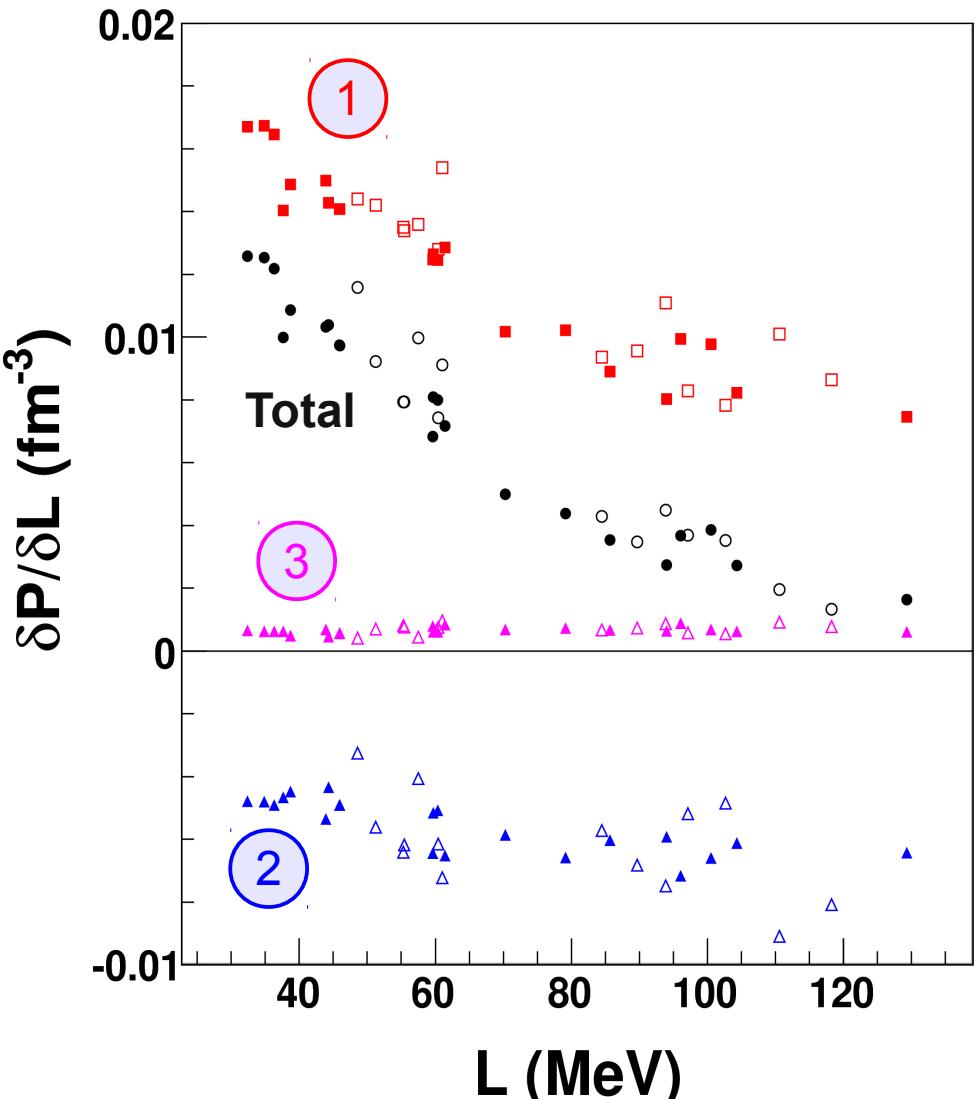
Variations due to  $\delta L$ :

$$1 \quad \left( \frac{\partial P}{\partial L} \right)_{\rho, y} (\rho_t, y_t)$$

$$2 \quad \left( \frac{\partial P}{\partial \rho} \right)_{y, L} (\rho_t, y_t) * \frac{\delta \rho_t}{\delta L}$$

$$3 \quad \left( \frac{\partial P}{\partial y} \right)_{\rho, L} (\rho_t, y_t) * \frac{\delta y_t}{\delta L}$$

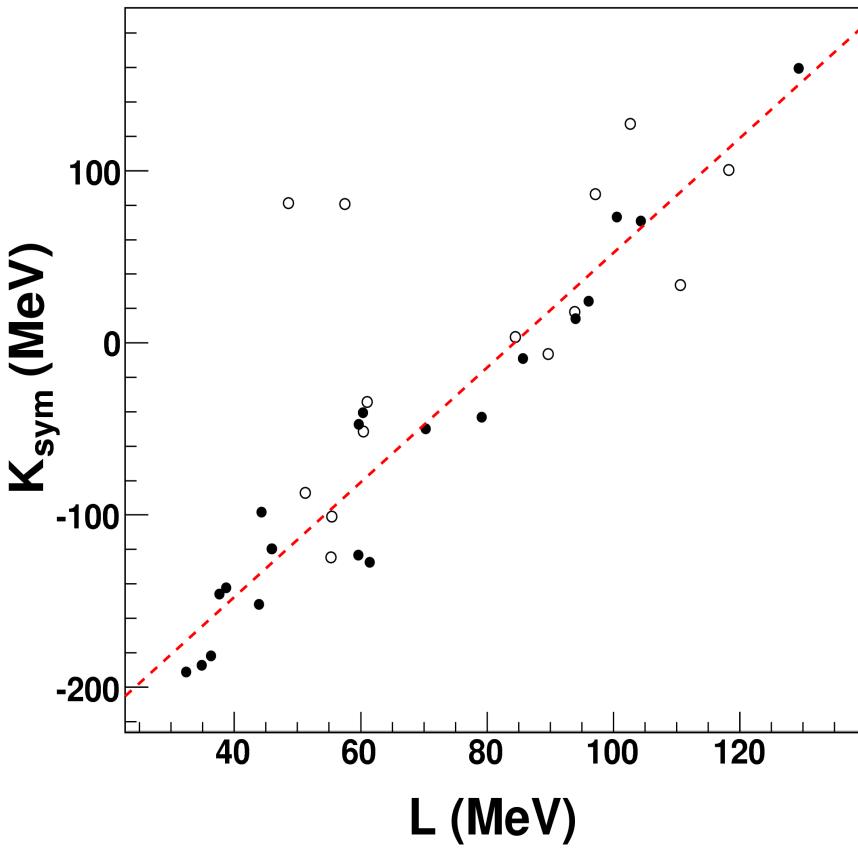
Opposite contributions  
Total  $\rightarrow P_t(L)$  increases



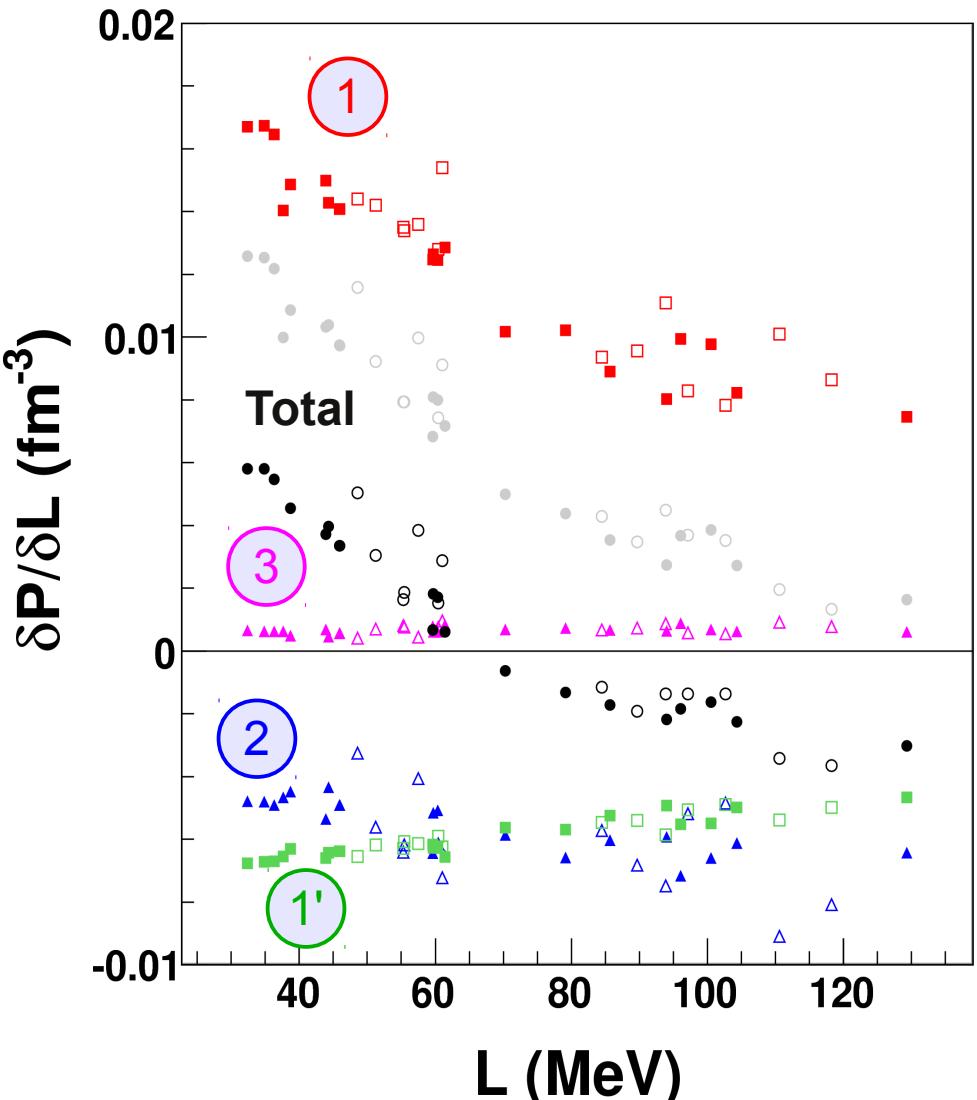
# Role of the correlation $K_{\text{sym}}(L)$

$$P(\rho, y) = \frac{\rho^2}{3\rho_0} \left[ Ly^2 + (K_0 + K_s y^2) \frac{\rho - \rho_0}{3\rho_0} + \dots \right]$$

1'  $\left( \frac{\partial P}{\partial K_s} \right)_{\rho, y, L} (\rho_t, y_t) * \frac{\delta K_s}{\delta L}$



Opposite contributions  
Total  $\rightarrow P_t(L)$  in/decreases



# Previsions of a schematic model

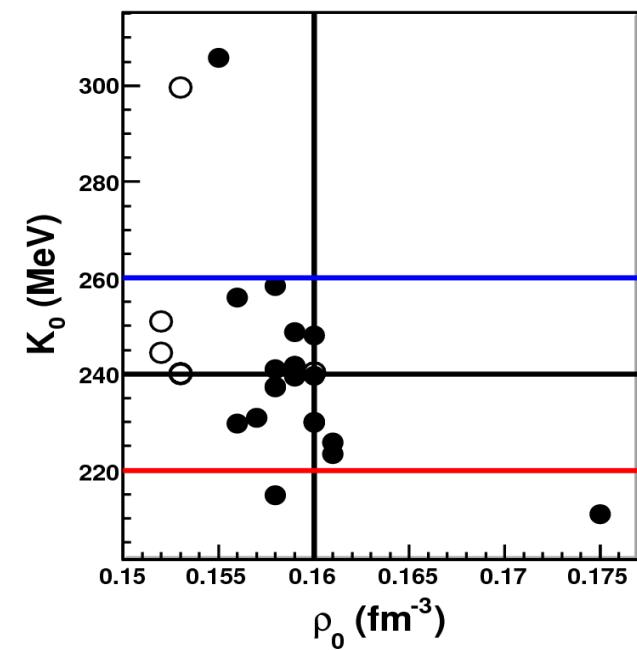
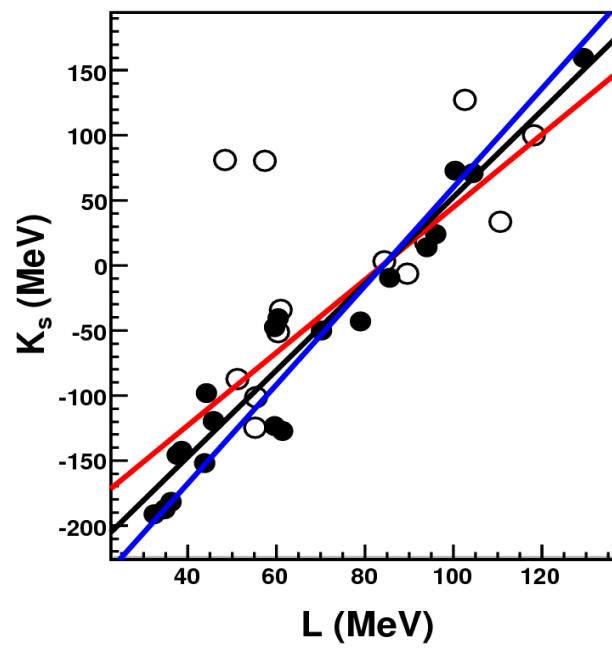
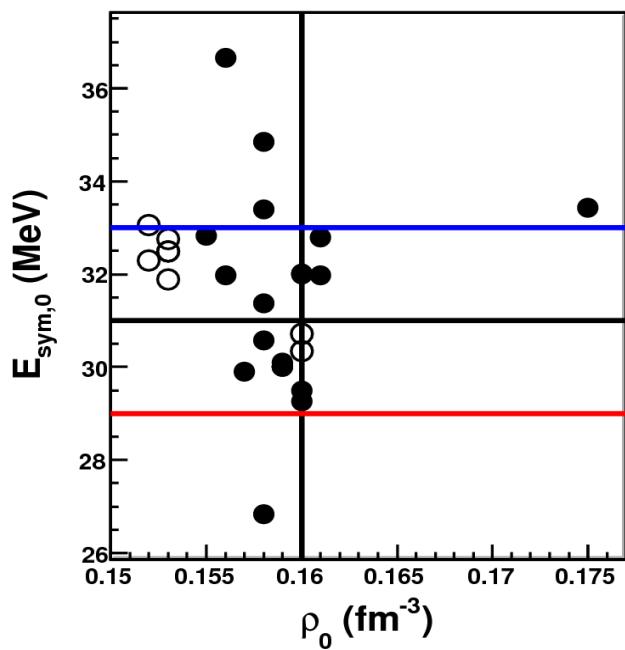
$$E = E_0 + E_s y^2 + L y^2 \frac{\rho - \rho_0}{3 \rho_0} + (K_0 + K_s y^2) \left( \frac{\rho - \rho_0}{3 \rho_0} \right)^2 + (Q_0 + Q_s y^2) \left( \frac{\rho - \rho_0}{3 \rho_0} \right)^3 + \dots$$

**Typical values (isoscalar):**

$$\begin{aligned} \rho_0 &= 0.16 \text{ fm}^{-3}; \\ E_0 &= -16 \text{ MeV}; \\ K_0 &= 240 \text{ MeV}; \\ Q_0 &= -350 \text{ MeV} \end{aligned}$$

**Typical values (isovector):**

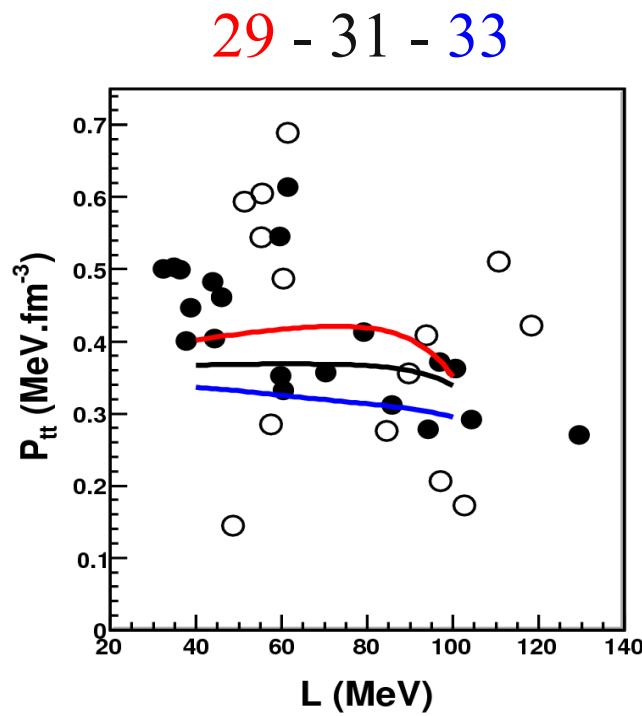
$$\begin{aligned} E_s &= 31 \text{ MeV} \\ L &= [40-100] \text{ MeV} \\ K_s &= 3.33 * L - 281 \text{ MeV} \\ Q_s &= -6,63 * L + 765 \text{ MeV} \end{aligned}$$



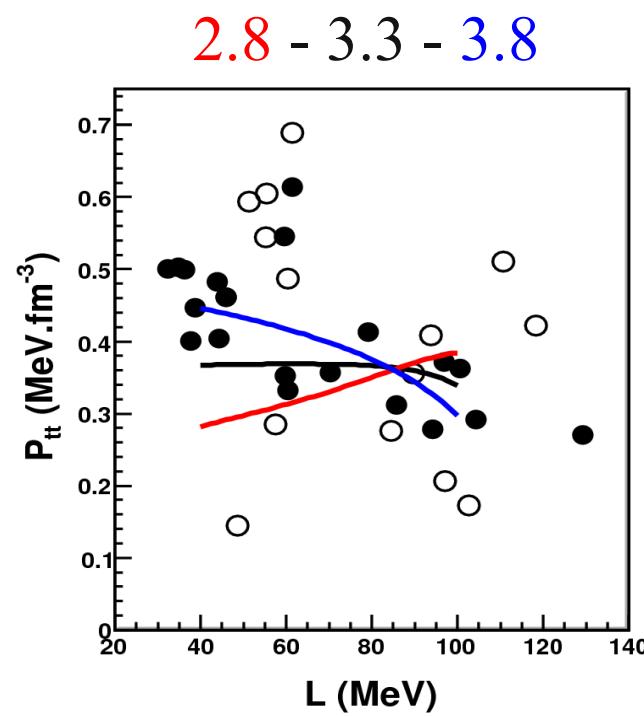
# Previsions of a schematic model

$$E = E_0 + E_s y^2 + L y^2 \frac{\rho - \rho_0}{3 \rho_0} + (K_0 + K_s y^2) \left( \frac{\rho - \rho_0}{3 \rho_0} \right)^2 + (Q_0 + Q_s y^2) \left( \frac{\rho - \rho_0}{3 \rho_0} \right)^3 + \dots$$

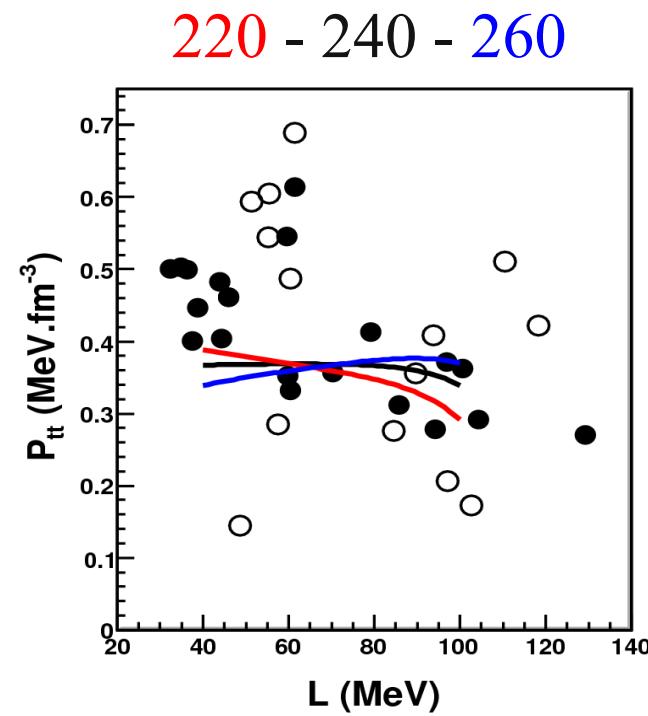
**Different  $E_s$  (MeV):**



**Different  $dK_s/dL$ :**



**Different  $K_0$  (MeV):**



# **Conclusion**

# Summary

→ Robust correlation between symmetry-energy slope L and core-crust transition position ( $r_t$ ,  $Y_p, t$ ) :

- ✗ Good correlation  $L - \rho_t$
- ✗ Correlation  $L - Y_{p,t}$  : dispersion due to different  $E_{\text{sym}}(\rho_0)$

→ Delicate link between L and the transition pressure  $P_t$  :

- ✗ Opposite contributions : no qualitative prediction is possible
- ✗ Important role of L-K<sub>sym</sub> correlation

# Outlook

*How can we obtain lab-experimental constraints on  $P_t$  ?*

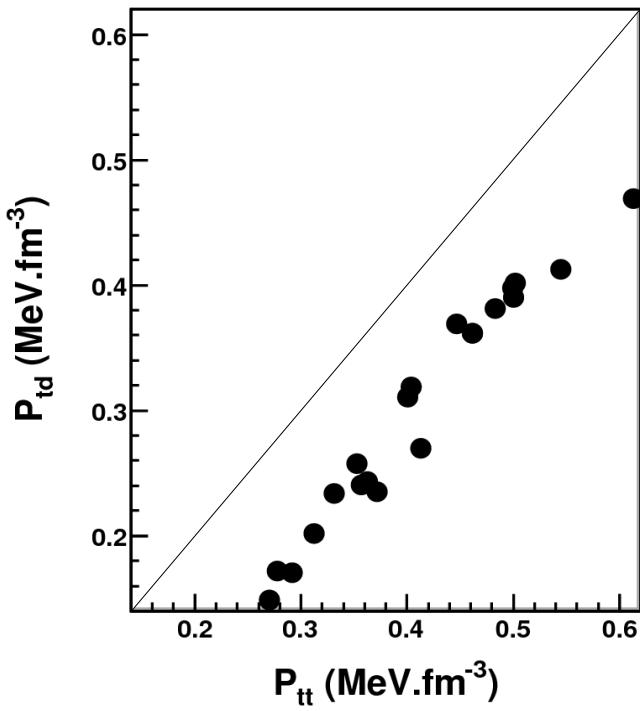
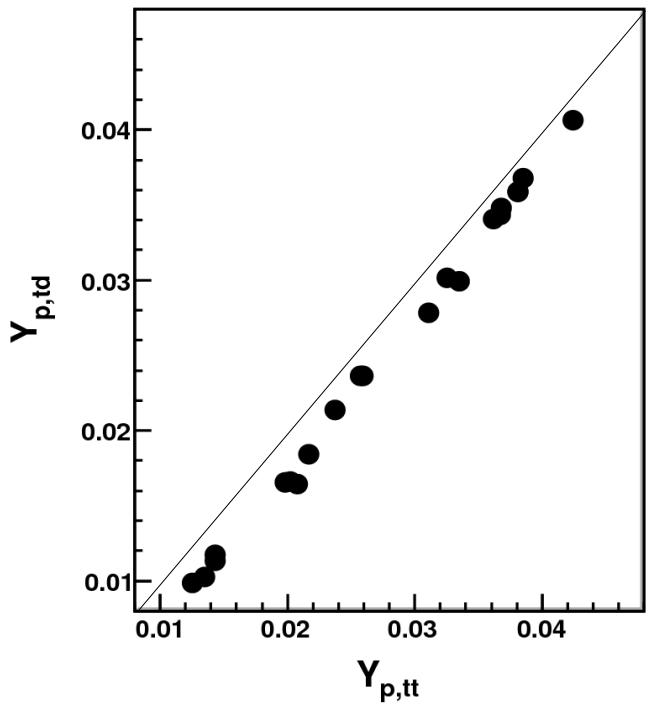
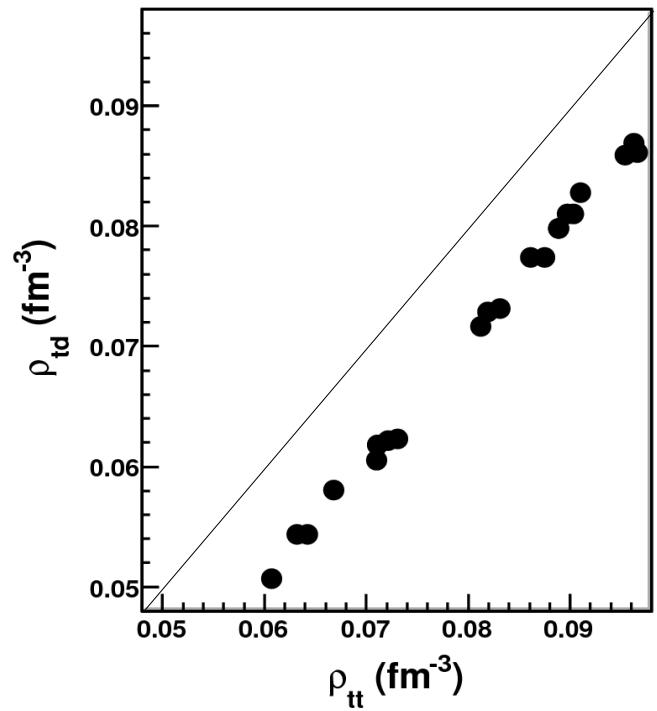
*What model-independence can be reached?*

- Understanding the correlations between coeffs of the asy-EOS expansion (such as L-K<sub>sym</sub>-Q<sub>sym</sub>)
- Constraining the n-rich functional at lower density points ( $\sim 0.1 \text{ fm}^3$ ) instead of  $\rho_0$  through relevant observables (neutron skin, multifragmentation, isospin diffusion...)

Grazie

# Dynamic versus Thermodynamic

Skyrme models



# Generalized Liquid Drop Model (GLDM)

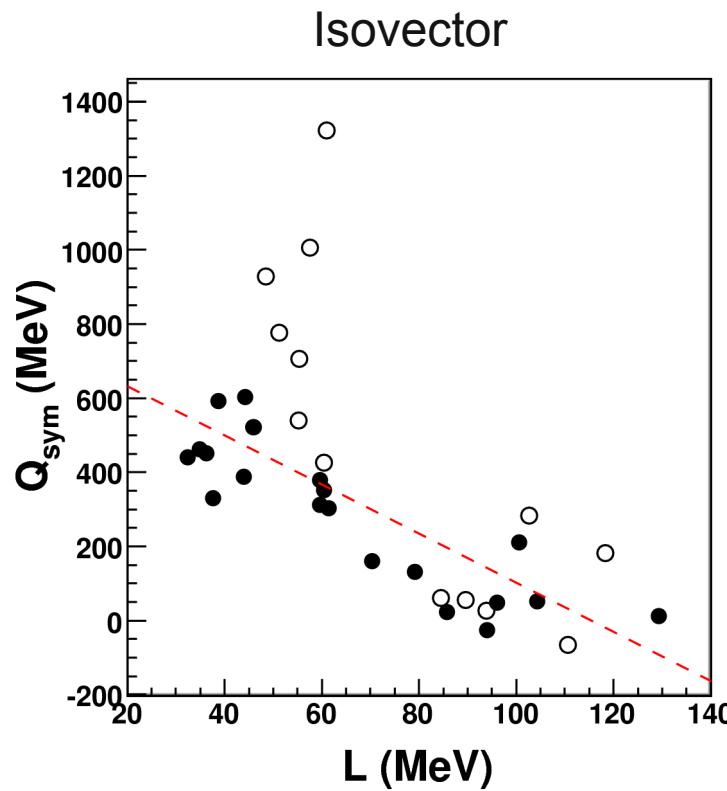
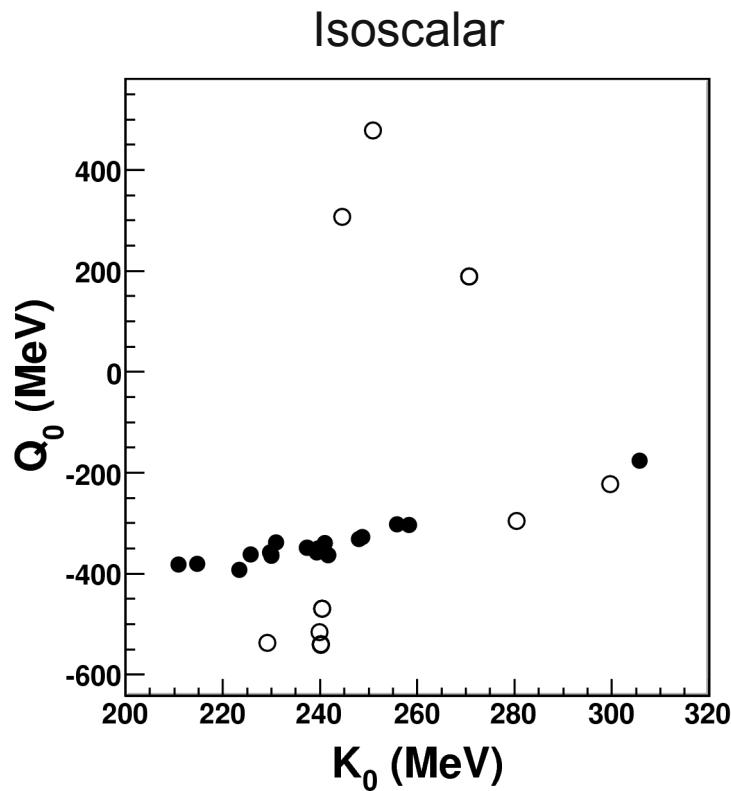
$$x = \frac{\rho - \rho_0}{3 \rho_0}$$

$$E(\rho, y) = \sum_{n \geq 0} \left( c_{IS,n} + c_{IV,n} y^2 \right) \frac{x^n}{n!} + (E_{kin} - E_{kin}^{para})$$

$$P(\rho, y) = \frac{\rho^2}{3 \rho_0} \left[ L y^2 + \sum_{n \geq 2} \left( c_{IS,n} + c_{IV,n} y^2 \right) \frac{x^{n-1}}{(n-1)!} \right] + \rho^2 \frac{\partial (E_{kin} - E_{kin}^{para})}{\partial \rho}$$

$$C_{NM,s} = \frac{2L}{3 \rho_0} + \frac{1}{3 \rho_0} \sum_{n \geq 2} c_{IV,n} \frac{x^{n-2}}{(n-2)!} \underbrace{\left[ \frac{n+1}{n-1} x + \frac{1}{3} \right]}_{0 \text{ for } n=2, \rho/\rho_0=2/3} + \frac{\partial^2 [\rho (E_{kin} - E_{kin}^{para})]}{\partial \rho^2}$$

# Third order of the GLDM



Skyrme data fit:  
 $Q_{\text{sym}} = -6,63 * L + 765$

Modele	$\rho_0$	$E_0$	$K_0$	$Q_0$	$E_{\text{sym}}$	$L$	$K_{\text{sym}}$	$Q_{\text{sym}}$
BSk14	0.159	-15.9	239.4	-358.8	30.0	43.9	-152.0	388.3
BSk16	0.159	-16.1	241.7	-363.7	30.0	34.9	-187.4	461.9
BSk17	0.159	-16.1	241.7	-363.7	30.0	36.3	-181.9	450.5
$G_\sigma$	0.158	-15.6	237.3	-348.8	31.4	94.0	14.0	-26.8
$R_\sigma$	0.158	-15.6	237.4	-348.5	30.6	85.7	-9.1	22.2
LNS	0.175	-15.3	210.8	-382.7	33.4	61.5	-127.4	302.5
NRAPR	0.161	-15.9	225.7	-362.6	32.8	59.6	-123.3	311.6
RATP	0.160	-16.1	239.6	-349.9	29.3	32.4	-191.3	440.7
SV	0.155	-16.1	305.8	-175.9	32.8	96.1	24.2	48.0
SGII	0.158	-15.6	214.7	-381.0	26.8	37.6	-145.9	330.4
SkI2	0.158	-15.8	241.0	-339.8	33.4	104.3	70.7	51.6
SkI3	0.158	-16.0	258.2	-304.0	34.8	100.5	73.1	211.5
SkI4	0.160	-15.9	248.0	-331.3	29.5	60.4	-40.5	351.1
SkI5	0.156	-15.9	255.9	-302.1	36.6	129.3	159.6	11.7
SkI6	0.159	-15.9	248.6	-327.4	30.1	59.7	-47.3	379.0
SkMP	0.157	-15.6	230.9	-338.2	29.9	70.3	-49.8	159.4
SkO	0.160	-15.8	223.4	-393.0	32.0	79.1	-43.2	131.1
SLy230a	0.160	-16.0	229.9	-364.3	32.0	44.3	-98.2	602.9
SLy230b	0.160	-16.0	230.0	-363.2	32.0	46.0	-119.7	521.5
SLy4	0.160	-16.0	230.0	-363.2	32.0	45.9	-119.7	521.6
SLy10	0.156	-15.9	229.7	-358.4	32.0	38.7	-142.2	591.3
NL3	0.148	-16.2	270.7	188.8	37.3	118.3	100.5	182.6
TM1	0.145	-16.3	280.4	-295.4	36.8	110.6	33.6	-65.2
GM1	0.153	-16.3	299.7	-222.1	32.5	93.9	17.9	25.8
GM3	0.153	-16.3	239.9	-515.5	32.5	89.7	-6.5	55.9
FSU	0.148	-16.3	229.2	-537.4	32.5	60.4	-51.4	426.6
NL $\omega\rho(025)$	0.148	-16.2	270.7	188.8	32.4	61.1	-34.4	1322.0
NL $\rho\delta(0)$	0.160	-16.1	240.4	-470.2	30.3	84.5	3.3	61.4
TW	0.153	-16.3	240.2	-541.0	32.8	55.3	-124.7	539.0
DDME1	0.152	-16.2	244.5	307.6	33.1	55.4	-101.0	706.3
DDME2	0.152	-16.1	250.9	478.3	32.3	51.2	-87.2	777.1
DDHDI-25	0.153	-16.3	240.2	-540.3	25.6	48.6	81.1	928.3
DDHDII-30	0.153	-16.3	240.2	-540.3	31.9	57.5	80.7	1005.0
NL $\rho\delta(2.5)$	0.160	-16.1	240.4	-470.2	30.7	102.7	127.2	282.9